Formale Semantik o7. Einfach getypte höherstufige L-Sprachen

Roland Schäfer

Institut für Germanistische Sprachwissenschaft Friedrich-Schiller-Universität Jena

Achtung: Folien in Überarbeitung. Englische Teile sind noch von 2007! Stets aktuelle Fassungen: https://github.com/rsling/VL-Semantik

Inhalt

- **Preliminaries**
 - Different but related semantics
 - Sets and charactersitic functions
 - Functional application
- Simply typed languages

 New names for old categories

- The syntax of types
- Higher orders
- Summed up semantics for a higher-order language
- Lambda languages
 - From set constructor to the functional λ abstractor
 - General syntax/semantics for λ languages
 - A glimpse at quantification in Montague's system

Preliminaries

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- Montague: direct translation of NL into logic
- Monatgue's LF is just a notational system for NL semantics

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- Understand how λ languages allow dramatically elegant formalizations.
- ... while keeping in mind that these devices are extensions to our PC representation for NL semantics.

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- a CF 'checks' individuals into a set
- denotations can be stated as sets or their CF

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 - ideally: generalize to all nodes

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Possible denotations of types

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- $\bullet \ D_{\langle \boldsymbol{e},\langle \boldsymbol{e},t\rangle\rangle} = (D_{\langle \boldsymbol{t}\rangle}^{D_{\langle \boldsymbol{e}\rangle}})^{^{D_{\langle \boldsymbol{e}\rangle}}}$
- ullet just a systematic way of naming types, model-theoretic interpretations still by V, g

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- complex types: functions from \(\epsilon \) to \(\lambda t \)
 or generally from any (complex) type to any (comlex) type.

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- for any pred₂ P and its arguments $a_1, a_2, P(a_2)(a_1)$ is a wff
- connectives are of types $\langle t, t \rangle$ (\neg), $\langle t, \langle t, t \rangle$) (\wedge , etc.)

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General semantics of typed languages

- generalized CF/FA approach
- $\langle e \rangle$ -types (terms): $\llbracket a_n \rrbracket^{\mathcal{M},g} = V(a_n)$ $\llbracket x_n \rrbracket^{\mathcal{M},g} = g(x_n)$
- the rest: functional application

$$\llbracket \delta(\alpha) \rrbracket^{\mathcal{M}, g} = \llbracket \delta \rrbracket^{\mathcal{M}, g} (\llbracket \alpha \rrbracket^{\mathcal{M}, g})$$

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- vs. set of meaningful expressions of that type: ΜΕ_(α)

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- so: $\mathbf{v}_{1_{\langle e,t\rangle}}[\mathbf{v}_1(m)]$
- if V(m) = Mary, v_1 is the set of all of Mary's properties

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- alternatively abbreviated by old symbols x_1 , a, P, etc.

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- variable α : $[\alpha]^{\mathcal{M},g} = V(\alpha)$
- $\bullet \ \alpha \in \langle \mathbf{a}, \mathbf{b} \rangle, \ \overline{\beta \in \mathbf{a}, \text{then } [\![\alpha(\beta)]\!]^{\mathcal{M}, \mathbf{g}} = [\![\alpha]\!]^{\mathcal{M}, \mathbf{g}}([\![\beta]\!]^{\mathcal{M}, \mathbf{g}})}$

Logical constants and quantifiers

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- if $\mathbf{v}_{1_{\langle \alpha \rangle}}$ is a variable and $\phi \in \mathit{ME}_t$ then $[\![(\forall \mathbf{v}_1)\phi]\!]^{\mathcal{M},g} = 1\mathit{iff}$ for all $a \in \mathcal{D}_{\alpha}$ $[\![\phi]\!]^{\mathcal{M},g[a/\mathbf{v}_1]} = 1$

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- else in $\forall v_{0_{\langle e,t\rangle}}$, \forall wouldn't hold

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- result denotes complement of the original adjective in $D_{\langle e \rangle}$
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- ullet result denotes complement of the original adjective in $D_{\langle e
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- adjective: (e,t), non: ((e,t), (e,t))
- a function h s.t. for every $k \in D_{\langle e,t \rangle}$ and every $d \in D_{\langle e \rangle}$ (h(k))(d) = 1 iff k(d) = 0 and (h(k))(d) = 0 iff k(d) = 1

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- passives as similar subject deletion



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- does not create a set but a function which can be taken as the CF of a set

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- x can be of any type

Two informal examples

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- $\lambda x_{\langle e,t \rangle}[x(l)]$ is the characteristic function of the set of those properties $k \in D_{\langle e,t \rangle}$ that the individual l has

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- hence, it holds: $\lambda x [L(x)](a) \Leftrightarrow L(a)$
- for every wff ϕ , any $x \in Var$, and any $a \in Con$
- λ conversion: $\lambda x [\phi](a) \rightarrow \phi^{[x/a]}$

λ in and out

• $\lambda \mathbf{x} \left[\phi \right] \left(\mathbf{a} \right) \leftrightarrow \phi^{\left[\mathbf{x} / \mathbf{a} \right]}$

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- notice: $\lambda \mathbf{x}_{\langle \alpha \rangle} [\phi]$ is in $ME_{\langle \alpha, t \rangle}$
- while ϕ (as a wff) is in $\mathit{ME}_{\langle t \rangle}$

The full rules

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- If $\alpha \in ME_{\alpha}$ and $u \in Var_b$, then $\lambda u [\alpha] \in ME_{\langle b,a \rangle}$.
- If $\alpha \in ME_a$ and $u \in Var_b$ then $[\![\lambda u \ [\alpha]\!]]^{\mathcal{M},g}$ is that function h from D_b into D_a s.t. for all objects k in D_b , h(k) is equal to $[\![\alpha]\!]^{\mathcal{M},g[k/u]}$.

$$\bullet \ \forall x \forall v_{0^{\langle e,t \rangle}} \left[(\mathbf{non}(v_{0_{\langle e,t \rangle}}))(x) \leftrightarrow \neg (v_{0_{\langle e,t \rangle}}(x)) \right]$$

- $\bullet \ \forall \mathbf{X} \forall \mathbf{V}_{0^{\langle \mathbf{e}, \mathbf{t} \rangle}} \left[(\mathbf{non}(\mathbf{V}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}}))(\mathbf{X}) \leftrightarrow \neg (\mathbf{V}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}}(\mathbf{X})) \right]$
- $\forall \mathbf{v}_{0_{\langle e,t\rangle}} \left[\lambda \mathbf{x} \left[(\mathbf{non}(\mathbf{v}_{0_{\langle e,t\rangle}}))(\mathbf{x}) \right] = \lambda \mathbf{x} \left[\neg (\mathbf{v}_{0_{\langle e,t\rangle}}(\mathbf{x})) \right] \right]$

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- $\bullet \ \forall \mathbf{V_0}_{\langle e,t\rangle} \left[\lambda \mathbf{X} \left[(\mathbf{non}(\mathbf{V_0}_{\langle e,t\rangle}))(\mathbf{X}) \right] = \lambda \mathbf{X} \left[\neg (\mathbf{V_0}_{\langle e,t\rangle}(\mathbf{X})) \right] \right]$
- $\forall \mathsf{V}_{0_{\langle e,t\rangle}}\left[\mathbf{non}(\mathsf{V}_{0_{\langle e,t\rangle}}) = \lambda \mathsf{X}\left[\neg(\mathsf{V}_{0_{\langle e,t\rangle}}(\mathsf{X}))\right]\right]$ (since $\lambda \mathsf{X}\left[\mathbf{non}(\mathsf{V})(\mathsf{X})\right]$ is unnecessarily abstract/ η reduction)

- $\bullet \ \forall \mathbf{X} \forall \mathbf{V}_{0^{\langle \mathbf{e}, \mathbf{t} \rangle}} \left[(\mathbf{non}(\mathbf{V}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}}))(\mathbf{X}) \leftrightarrow \neg(\mathbf{V}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}}(\mathbf{X})) \right]$
- $\bullet \ \forall \mathbf{V_0}_{\langle e,t\rangle} \left[\lambda \mathbf{X} \left[(\mathbf{non}(\mathbf{V_0}_{\langle e,t\rangle}))(\mathbf{X}) \right] = \lambda \mathbf{X} \left[\neg (\mathbf{V_0}_{\langle e,t\rangle}(\mathbf{X})) \right] \right]$
- $\forall \mathbf{V}_{0_{\langle e,t\rangle}}\left[\mathbf{non}(\mathbf{V}_{0_{\langle e,t\rangle}}) = \lambda \mathbf{X}\left[\neg(\mathbf{V}_{0_{\langle e,t\rangle}}(\mathbf{X}))\right]\right]$ (since $\lambda \mathbf{X}\left[\mathbf{non}(\mathbf{V})(\mathbf{X})\right]$ is unnecessarily abstract/ η reduction)
- $\bullet \ \lambda \mathbf{v}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}} \left[\mathbf{non}(\mathbf{v}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}}) = \lambda \mathbf{v}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}} \left[\lambda \mathbf{x} \left[\neg (\mathbf{v}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}}(\mathbf{x})) \right] \right] \right]$

- $\bullet \ \forall \mathbf{X} \forall \mathbf{V}_{0^{\langle \mathbf{e}, \mathbf{t} \rangle}} \left[(\mathbf{non}(\mathbf{V}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}}))(\mathbf{X}) \leftrightarrow \neg(\mathbf{V}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}}(\mathbf{X})) \right]$
- $\bullet \ \forall \mathbf{v}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}} \left[\lambda \mathbf{x} \left[(\mathbf{non}(\mathbf{v}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}}))(\mathbf{x}) \right] = \lambda \mathbf{x} \left[\neg (\mathbf{v}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}}(\mathbf{x})) \right] \right]$
- $\forall \mathbf{V}_{0_{\langle e,t\rangle}}\left[\mathbf{non}(\mathbf{V}_{0_{\langle e,t\rangle}}) = \lambda \mathbf{X}\left[\neg(\mathbf{V}_{0_{\langle e,t\rangle}}(\mathbf{X}))\right]\right]$ (since $\lambda \mathbf{X}\left[\mathbf{non}(\mathbf{V})(\mathbf{X})\right]$ is unnecessarily abstract/ η reduction)
- $\bullet \ \lambda \mathbf{v}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}} \left[\mathbf{non}(\mathbf{v}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}}) = \lambda \mathbf{v}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}} \left[\lambda \mathbf{x} \left[\neg (\mathbf{v}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}}(\mathbf{x})) \right] \right] \right]$
- and since that is about all assignments for $\lambda \mathbf{v}_{0_{\langle e,t \rangle}}$: $\mathbf{non} = \lambda \mathbf{v}_{0_{\langle e,t \rangle}} \left[\lambda \mathbf{X} \left[\neg \mathbf{v}_{0_{\langle e,t \rangle}}(\mathbf{X}) \right] \right]$

Mary is non-adjacent.

(translate 'adjacent' as $c_{0_{\langle e,t \rangle}}$, 'Mary' as $c_{0_{\langle e \rangle}}$, ignore the copula)

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- semantically like PC quantifiers

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- $\bullet \ \ \text{Some student walks.:} \ \forall \mathbf{v}_{0_{\langle \mathbf{e} \rangle}} \left[\mathbf{c}_{0_{\langle \mathbf{e}, t \rangle}}(\mathbf{v}_{0_{\langle \mathbf{e} \rangle}}) \wedge \mathbf{c}_{1_{\langle \mathbf{e}, t \rangle}}(\mathbf{v}_{0_{\langle \mathbf{e} \rangle}}) \right]$

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- $\bullet \ \ \text{Every student walks.:} \ \forall \mathsf{v}_{0_{\langle e \rangle}} \left[\mathsf{c}_{0_{\langle e,t \rangle}}(\mathsf{v}_{0_{\langle e \rangle}}) \to \mathsf{c}_{1_{\langle e,t \rangle}}(\mathsf{v}_{0_{\langle e \rangle}}) \right]$
- Some student walks.: $\forall \mathsf{v}_{0_{\langle e \rangle}} \left[\mathsf{c}_{0_{\langle e, t \rangle}}(\mathsf{v}_{0_{\langle e \rangle}}) \wedge \mathsf{c}_{1_{\langle e, t \rangle}}(\mathsf{v}_{0_{\langle e \rangle}}) \right]$
- making referential NPs and QNPs the same type?

 $\bullet \ \lambda \mathbf{v}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}} \forall \mathbf{v}_{0_{\langle \mathbf{e} \rangle}} \left[\mathbf{c}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}}(\mathbf{v}_{0_{\langle \mathbf{e} \rangle}}) \rightarrow \mathbf{v}_{0_{\langle \mathbf{e}, \mathbf{t} \rangle}}(\mathbf{v}_{0_{\langle \mathbf{e} \rangle}}) \right]$

- $\bullet \ \lambda \mathbf{v_0}_{\langle e,t\rangle} \forall \mathbf{v_0}_{\langle e\rangle} \left[\mathbf{c_0}_{\langle e,t\rangle} (\mathbf{v_0}_{\langle e\rangle}) \rightarrow \mathbf{v_0}_{\langle e,t\rangle} (\mathbf{v_0}_{\langle e\rangle}) \right]$
- a second order function

$$\bullet \ \lambda \mathbf{v}_{0_{\langle e,t\rangle}} \forall \mathbf{v}_{0_{\langle e\rangle}} \left[\mathbf{c}_{0_{\langle e,t\rangle}}(\mathbf{v}_{0_{\langle e\rangle}}) \rightarrow \mathbf{v}_{0_{\langle e,t\rangle}}(\mathbf{v}_{0_{\langle e\rangle}}) \right]$$

- a second order function
- characterizes the set of all predicates true of every student

- $\bullet \ \lambda \mathbf{v_{0}}_{\langle e,t\rangle} \forall \mathbf{v_{0}}_{\langle e\rangle} \left[\mathbf{c_{0}}_{\langle e,t\rangle} (\mathbf{v_{0}}_{\langle e\rangle}) \rightarrow \mathbf{v_{0}}_{\langle e,t\rangle} (\mathbf{v_{0}}_{\langle e\rangle}) \right]$
- a second order function
- characterizes the set of all predicates true of every student
- equally: $\lambda v_{0_{\langle e,t\rangle}} \exists v_{0_{\langle e\rangle}} \left[c_{0_{\langle e,t\rangle}}(v_{0_{\langle e\rangle}}) \wedge v_{0_{\langle e,t\rangle}}(v_{0_{\langle e\rangle}}) \right]$

Combining with some predicate

Literatur I

Autor

Kontakt

Prof. Dr. Roland Schäfer Institut für Germanistische Sprachwissenschaft Friedrich-Schiller-Universität Jena Fürstengraben 30 07743 Jena

https://rolandschaefer.netroland.schaefer@uni-jena.de

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