

# Formale Semantik

## o6. Quantifikation und Modelltheorie

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**Achtung: Folien in Überarbeitung. Englische Teile sind noch von 2007!**  
Stets aktuelle Fassungen: <https://github.com/rsling/VL-Semantik>

- 1 From PC to F1
    - Taking stock
    - Pronouns and context
    - Phrase structure version of PC
    - Trees
    - C-command
  - 2 Model theory
    - Models and valuations
    - Assignment functions
  - 3 Problems with natural language
    - Restricted quantification
    - Variable binding and scope
    - Pre-spellout movement
    - LF movement
  - 4 Quantification in English: F2
    - Movement rules
    - Fragment F2
- Modified assignment functions

From PC to F1

- before we turn to quantification in F1/F2 English:
- names refer to individuals
- itr. verbs refer to sets of individuals
- tr. verbs refer to sets of ordered pairs of individuals
- sentences refer to truth values

- ***This*** drives a Golf.
- *this* = a pronominal NP
- denotes an individual
- but not rigidly
- fixed only within a specific context (SOA)

- quantified expression:  $(\forall x)Px$
- *for all assignments of 'this', 'this' has property P*
- Q evaluation in PC is algorithmic
- variables interpreted like definite pronominal NPs (within a fixed context)

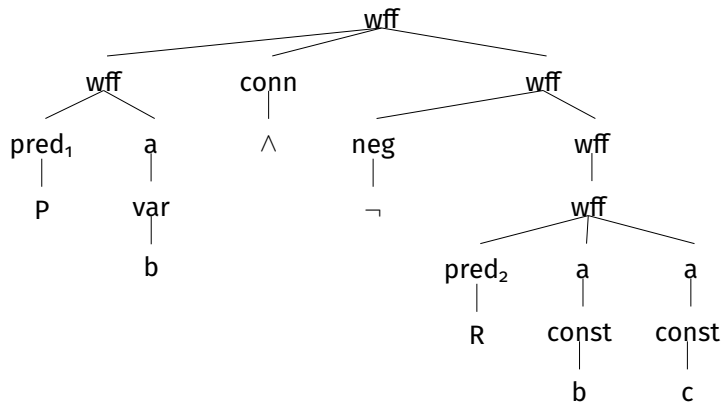
- $a \rightarrow \text{const, var}$
- $\text{conn} \rightarrow \wedge, \vee, \rightarrow, \leftrightarrow$
- $\text{neg} \rightarrow \neg$
- $Q \rightarrow \exists, \forall$

- $\text{pred}_1 \rightarrow P, Q$
- $\text{pred}_2 \rightarrow R$
- $\text{pred}_3 \rightarrow S$
- $\text{const} \rightarrow b, c$
- $\text{var} \rightarrow x_1, x_2, \dots, x_n$

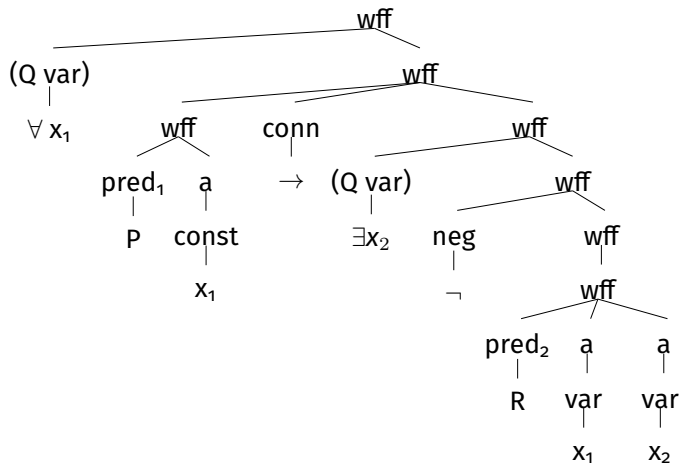


- $wff \rightarrow pred_n a_1 a_2 \dots a_n$
- $wff \rightarrow neg\ wff$
- $wff \rightarrow wff\ con\ wff$
- $wff \rightarrow (Q\ var)\ wff$

# A wff without Q



# A wff with Q's

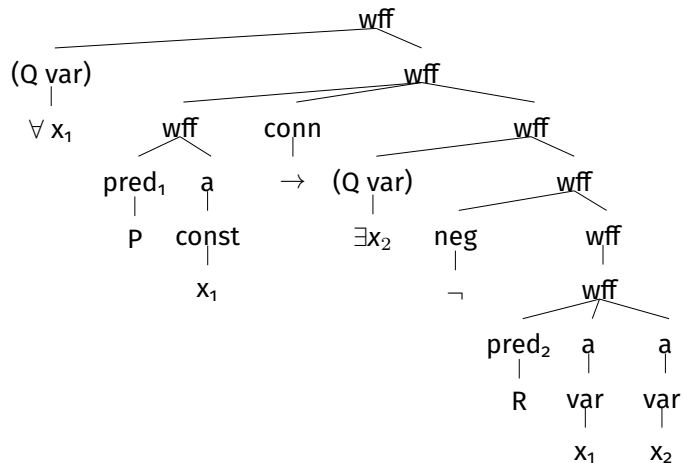


# Definition of c-command

- Node A **c-commands** (constituent-commands) node B iff
  - ▶ A does not dominate B and
  - ▶ and the first branching node dominating A also dominates B.
- The definition in CM allows a node to dominate itself.

- in configurational tree-structures:
- A variables is bound by the closest c-commanding coindexed quantifier.
- scope = binding domain

# A wff with Q's



## Model theory

- remember T-sentences: **S of L is true in v iff p.**
- $\mathcal{M}$  is a model of the accessible universe of discourse
  - ▶  $\mathcal{M} = \langle U_n, V_n \rangle$
  - ▶  $U_n$  = the set of accessible individuals (domain)
  - ▶  $V_n$  = a valuation function which assigns
    - ★ individuals to names
    - ★ sets of n-tuples of individuals to  $\text{pred}_n$
- $g$  is function from variables to individuals in  $\mathcal{M}$
- we evaluate:  $\llbracket \alpha \rrbracket^{\mathcal{M}_n, g_n}$
- *the extension of  $\alpha$  relative to  $\mathcal{M}_n$  and  $g_n$*



- $V_n$  evaluates *statically*
- Q's require flexible valuation of pronominal matrices
- $g_n$  is like  $V_n$  for constants, only flexible
- it can *iterate through*  $U_n$
- initial assignment can be anything:

$$g_1 = \left[ \begin{array}{l} x_1 \rightarrow \textit{Herr Webelhuth} \\ x_2 \rightarrow \textit{Frau Eckardt} \\ x_3 \rightarrow \textit{Turm – Mensa} \end{array} \right]$$

- for each Q loop, one modification
- read  $g_n[d/x_m]$  as  
‘...relative to  $g_n$  where  $x_m$  is reassigned to  $d$ ’
- $\llbracket x_1 \rrbracket^{\mathcal{M}_1, g_1[Eckardt/x_1]} = \textit{Frau Eckardt}$
- $\llbracket x_2 \rrbracket^{\mathcal{M}_1, g_1[[Eckardt/x_1]Mensa/x_2]} = \textit{Mensa}$

- $\llbracket (\forall x_1) Px_1 \rrbracket^{\mathcal{M}_1, g_1}$
- start with initial assignment:  $\llbracket x_1 \rrbracket^{\mathcal{M}_1, g_1} = \textit{Webelhuth}$   
check:  $\llbracket Px_1 \rrbracket^{\mathcal{M}_1, g_1}$
- modify:  $\llbracket x_1 \rrbracket^{\mathcal{M}_1, g_1[\textit{Eckardt}/x_1]} = \textit{Eckardt}$   
check:  $\llbracket Px_1 \rrbracket^{\mathcal{M}_1, g_1}$
- modify:  $\llbracket x_1 \rrbracket^{\mathcal{M}_1, g_1[\textit{Mensa}/x_1]} = \textit{Mensa}$   
check:  $\llbracket Px_1 \rrbracket^{\mathcal{M}_1, g_1}$
- iff the answer was never 0, then  $\llbracket (\forall x_1) Px_1 \rrbracket^{\mathcal{M}_1, g_1} = 1$

# Multiple Q's: subloops

- $\llbracket (\forall x_1)(\exists x_2)Px_1x_2 \rrbracket^{\mathcal{M}_1, g_1}$
- $\llbracket x_1 \rrbracket^{\mathcal{M}_1, g_1} = \text{Webelhuth}$ 
  - ▶  $\llbracket x_2 \rrbracket^{\mathcal{M}_1, g_1} = \text{Eckardt}$
  - ▶  $\llbracket x_2 \rrbracket^{\mathcal{M}_1, g_1 [\text{Webelhuth}/x_2]} = \text{Webelhuth}$
  - ▶  $\llbracket x_2 \rrbracket^{\mathcal{M}_1, g_1 [\text{Mensa}/x_2]} = \text{Mensa}$
- $\llbracket x_1 \rrbracket^{\mathcal{M}_1, g_1 [\text{Eckardt}/x_1]} = \text{Eckardt}$ 
  - ▶  $\llbracket x_2 \rrbracket^{\mathcal{M}_1, g_1 [\text{Eckardt}/x_1]} = \text{Eckardt}$
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  - ▶  $\llbracket x_2 \rrbracket^{\mathcal{M}_1, g_1 [[\text{Mensa}/x_1]\text{Mensa}/x_2]} = \text{Mensa}$

## Problems with natural language

- quantifying expressions in NL beyond  $\forall$  and  $\exists$
- some seem to work differently:
- *All patients* adore Dr. Rick Dagless M.D.  
 $(\forall x_1)Px_1 \rightarrow Ax_1d$  (ok)
- but: *Most patients* adore Dr. Rick Dagless M.D.  
 $(MOST x_1)Px_1 \rightarrow Ax_1d$  (wrong interpretation)
- domain should be the set of patients, not individuals
- For NL: Assume that the checking domain for Q is the set denoted by CN.

- c-command condition on binding/scope fails in NL
- no PNF's in NL
- Q and common noun (CN) usually *in-situ* (e.g., argument position)
- *ambiguities independent of Q position*
  - ▶ *Everybody loves somebody. (ELS)*
  - ▶  $(\forall x_1)(\exists x_2)Lx_1x_2$
  - ▶  $(\exists x_2)(\forall x_1)Lx_1x_2$
- *Q ambiguity cannot be structural* (e.g.,  $\exists$  will never c-command  $\forall$ )

# Cases of overt movement and traces

- **wh** movement:
  - *What<sub>i</sub> will Agent Cooper solve t<sub>i</sub>?*
  -
- **passive** movement:
  - *(Laura Palmer)<sub>i</sub> was killed t<sub>i</sub>.*
  -
- **raising** verbs:
  - *(Laura Palmer)<sub>i</sub> seems t<sub>i</sub> to be dead.*
  -



# Levels of representation

- construction of an independent representational level LF
- could use movement mechanism as used at surface level
- All quantifiers adjoin to the left periphery of S at LF.
- LF is constructed by syntactic rules!

- $[_{S''} \text{everybody}_i [_{S'} \text{somebody}_j [_S t_i \text{ loves } t_j ]]]$
- 
- $[_{S''} \text{somebody}_j [_{S'} \text{everybody}_i [_S t_i \text{ loves } t_j ]]]$
-

## Quantification in English: F2

# The Q raising rule

$$[_S X NP Y] \Rightarrow [_{S'} NP_i [_S X t_i Y]]$$

- specify a PS as input and output
- QR rule also introduces coindexing of traces

- copies all definitions from F1
- adds appropriate definitions of quantifying determiners etc.
  - ▶  $Det \rightarrow \textit{every, some}$
  - ▶  $NP \rightarrow DetN_{\textit{common-count}}$
- adds the QR rule
- assume introduction of reasonable syntactic types/rules without specifying
- assume **admissible (reasonable, possible) models**  $\mathcal{M}$

$$\begin{aligned} \llbracket [\textit{every } \beta]_i S \rrbracket^{\mathcal{M},g} = 1 \text{ iff for all } u \in U : \\ \text{if } u \in \llbracket \beta \rrbracket^{\mathcal{M},g} \text{ then } \llbracket S \rrbracket^{\mathcal{M},g[u/t_i]} \end{aligned}$$

A sentence containing the trace  $t_i$  with an adjoined  $NP_i$  (which consists of *every* plus the common noun  $\beta$ ) extend to 1 iff for each individual  $u$  in the universe  $U$  which is in the set referred to by the common noun  $\beta$ ,  $S$  denotes 1 with  $u$  assigned to the pronominal trace  $t_i$ .  $g$  is modified iteratively to check that.

$$\begin{aligned} \llbracket [a \beta]_i S \rrbracket^{\mathcal{M},g} = 1 \text{ iff for some } u \in U : \\ u \in \llbracket \beta \rrbracket^{\mathcal{M},g} \text{ and } \llbracket S \rrbracket^{\mathcal{M},g[u/t_i]} \end{aligned}$$

(similar)





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