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A search for sparticles in zero lepton final states

2

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6

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7

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8

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ABSTRACT

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A search for sparticles in zero lepton final states

14

Russell W. Smith

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16 center, but the abstract itself should be written as a regular paragraph on the page,

17 and it should not have indentation. Just replace this text.

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Acknowledgements

Introduction

Particle physics is a remarkably successful field of scientific inquiry. The ability to precisely predict the properties of a exceedingly wide range of physical phenomena, such as the description of the cosmic microwave background [1, 2], the understanding of the anomalous magnetic dipole moment of the electron [3, 4], and the measurement of the number of weakly-interacting neutrino flavors [5] is truly amazing.

The theory that has allowed this range of predictions is the *Standard Model* of particle physics (SM). The Standard Model combines the electroweak theory of Glashow, Weinberg, and Salam [6–8] with the theory of the strong interactions, as first envisioned by Gell-Mann and Zweig [9, 10]. This quantum field theory (QFT) contains a tiny number of particles, whose interactions describe phenomena up to at least the TeV scale. These particles are manifestations of the fields of the Standard Model, after application of the Higgs Mechanism. The particle content of the SM consists only of the six quarks, the six leptons, the four gauge bosons, and the scalar Higgs boson.

Despite its impressive range of described phenomena, the Standard Model has some theoretical and experimental deficiencies. The SM contains 26 free parameters¹. It would be more theoretically pleasing to understand these free parameters in terms of a more fundamental theory. The major theoretical concern of the Standard Model, as it pertains to this thesis, is the *hierachy problem*[11–15]. The light mass

¹This is the Standard Model corrected to include neutrino masses. These parameters are the fermion masses (6 leptons, 6 quarks), CKM and PMNS mixing angles (8 angles, 2 CP-violating phases), W/Z/Higgs masses (3), the Higgs field expectation value, and the couplings of the strong, weak, and electromagnetic forces (3 α_{force}) .

84 of the Higgs boson (125 GeV) should be quadratically dependent on the scale of UV
 85 physics, due to the quantum corrections from high-energy physics processes. The
 86 most perplexing experimental issue is the existence of *dark matter*, as demonstrated
 87 by galactic rotation curves [16–22]. This data has shown that there exists additional
 88 matter which has not yet been seen interacting with the particles of the Standard
 89 Model. There is no particle in the SM which can act as a candidate for dark matter.

90 Both of these major issues, as well as numerous others, can be solved by the
 91 introduction of *supersymmetry* (SUSY) [15, 23–33]. In supersymmetric theories, each
 92 SM particles has a so-called *superpartner*, or sparticle partner, differing from given SM
 93 particle by 1/2 in spin. These theories solve the hierachy problem, since the quantum
 94 corrections induced from the superpartners exactly cancel those induced by the SM
 95 particles. In addition, these theories are usually constructed assuming R -parity,
 96 which can be thought of as the “charge” of supersymmetry, with SM particles having
 97 $R = 1$ and sparticles having $R = -1$. In collider experiments, since the incoming
 98 SM particles have total $R = 1$, the resulting sparticles are produced in pairs. This
 99 produces a rich phenomenology, which is characterized by significant hadronic activity
 100 and large missing transverse energy (E_T^{miss}), which provide significant discrimination
 101 against SM backgrounds [34].

102 Despite the power of searches for supersymmetry where E_T^{miss} is a primary
 103 discriminating variable, there has been significant interest in the use of other variables
 104 to discriminate against SM backgrounds. These include searches employing variables
 105 such as αT , $M_{T,2}$, and the razor variables (M_R, R^2) [35–45]. In this thesis, we
 106 will present the first search for supersymmetry using the novel Recursive Jigsaw
 107 Reconstruction (RJR) technique. RJR can be considered the conceptual successor
 108 of the razor variables. We impose a particular final state “decay tree” on an events,
 109 which roughly corresponds to a simplified Feynmann diagram in decays containing
 110 weakly-interacting particles. We account for the missing degrees of freedom associated

111 to the weakly-interacting particles by a series of simplifying assumptions, which allow
112 us to calculate our variables of interest at each step in the decay tree. This allows an
113 unprecedented understanding of the internal structure of the decay and the ability to
114 construct additional variables to reject Standard Model backgrounds.

115 This thesis details a search for the superpartners of the gluon and quarks, the
116 gluino and squarks, in final states with zero leptons, with 13.3 fb^{-1} of data using the
117 ATLAS detector. We organize the thesis as follows. The theoretical foundations of
118 the Standard Model and supersymmetry are described in Chapters 2 and 3. The
119 Large Hadron Collider and the ATLAS detector are presented in Chapters 4 and 5.
120 Chapter 5 provides a detailed description of Recursive Jigsaw Reconstruction and a
121 description of the variables used for the particular search presented in this thesis.
122 Chapter 6 presents the details of the analysis, including details of the dataset, object
123 reconstruction, and selections used. In Chapter 7, the final results are presented;
124 since there is no evidence of a supersymmetric signal in the analysis, we present the
125 final exclusion curves in simplified supersymmetric models.

The Standard Model

2.1 Overview

The Standard Model is another name for the theory of the internal symmetry group $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$. This quantum field theory is the culmination of years of work in both theoretical and particle physics. In this thesis, we take the view one constructs a model with the field content and symmetries as inputs, and then writes down the most general Lagrangian consistent with those symmetries. This will be applicable for this chapter and the following one. Additional theoretical background is in 9.6.

cite Yuval's
lectures
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2.2 Field Content

The Standard Model field content is

$$\begin{aligned} \text{Fermions } Q_L(3, 2)_{+1/3}, U_R(3, 1)_{+4/3}, D_R(3, 1)_{-2/3}, L_L(1, 2)_{-1}, E_R(1, 1)_{-2} \\ \text{Scalar (Higgs) } \phi(1, 2)_{+1} \end{aligned} \quad (2.1)$$

$$\text{Vector Fields } G^\mu(8, 1)_0 W^\mu(1, 3)_0 B^\mu(1, 1)_0$$

where the $(A, B)_Y$ notation represents the irreducible representation under $SU(3)$ and $SU(2)$, with Y being the electroweak hypercharge. Each of these fields has an additional index, representing the three generation of fermions.

141 We observed that Q_L, U_R , and D_R are triplets under $SU(3)_C$; these are the *quark*
 142 fields. The *color* group, $SU(3)_C$ is mediated by the *gluon* field $G^\mu(8, 1)_0$, which has
 143 8 degrees of freedom. The fermion fields $L_L(1, 2)_{-1}$ and $E_R(1, 1)_{-2}$ are singlets under
 144 $SU(3)_C$; we call them the *lepton* fields.

145 Next, we note the “left-handed” (“right-handed”) fermion fields, denoted by L (R)
 146 subscript, The left-handed fields form doublets under $SU(2)_L$. These are mediated
 147 by the three degrees of freedom of the “W” fields $W^\mu(1, 3)_0$. These fields only act
 148 on the left-handed particles of the Standard Model. This is the reflection of the
 149 “chirality” of the Standard Model; the left-handed and right-handed particles are
 150 treated differently by the electroweak forces. The right-handed fields, U_R, D_R , and
 151 E_R , are singlets under $SU(2)_L$.

152 The $U(1)_Y$ symmetry is associated to the $B^\mu(1, 1)_0$ boson with one degree of
 153 freedom. The charge Y is known as the electroweak hypercharge.

154 To better understand the phenomenology of the Standard Model, let us investigate
 155 each of the *sectors* of the Standard Model separately.

156 Electroweak sector

The electroweak sector refers to the $SU(2)_L \otimes U(1)_Y$ portion of the Standard Model gauge group. Following our philosophy of writing all gauge-invariant and renormalizable (maximum degree 4 in the mass) terms, the electroweak Lagrangian can be written as

$$\mathcal{L} = W_a^{\mu\nu} W_{\mu\nu}^a + B^{\mu\nu} B_{\mu\nu} + (D^\mu \phi)^\dagger D_\mu \phi - \mu^2 \phi^\dagger \phi - \lambda (\phi^\dagger \phi)^2. \quad (2.2)$$

where $W_a^{\mu\nu}$ are the three ($a = 1, 2, 3$) gauge bosons associated to the $SU(2)_L$ gauge group, $B^{\mu\nu}$ is the one gauge boson of the $U(1)_Y$ gauge group, and ϕ is the complex Higgs multiplet with weak hypercharge $Y = 1$. The covariant derivative D^μ is given

by

$$D^\mu = \partial^\mu + i\frac{g}{2}W_a^\mu\sigma_a + \frac{i}{2}g'B^\mu \quad (2.3)$$

where σ_a are the Pauli matrices, which are the generators for $SU(2)_L$, and g and g' are the $SU(2)_L$ and $U(1)_Y$ coupling constants, respectively. The field strength tensors $W_a^{\mu\nu}$ and $B^{\mu\nu}$ are given by the commutator of the covariant derivative associated to each field

$$\begin{aligned} B^{\mu\nu} &= \partial^\mu B^\nu - \partial^\nu B^\mu \\ W_a^{\mu\nu} &= \partial^\mu W_a^\nu - \partial^\nu W_a^\mu - g\epsilon_{abc}W_a^\mu W_b^\nu, i = 1, 2, 3 \end{aligned} \quad (2.4)$$

157 The terms proportional in the Lagrangian to μ^2 and λ make up the “Higgs
158 potential” . As normal (i.e. in Appendix 9.6), we restrict $\lambda > 0$ to guarantee
159 our potential is bounded from below, and we also require $\mu^2 < 0$, which gives us the
160 standard “sombbrero” potential shown in ??.

Cite

161

This potential has a minimum at $VALUE$; the ground state is *spontaneously* broken by the choice of ground state, which induces a vacuum expectation value (VEV). Without loss of generality, we can choose the Higgs field ϕ to point in the real direction, and write the Higgs field ϕ in the following form :

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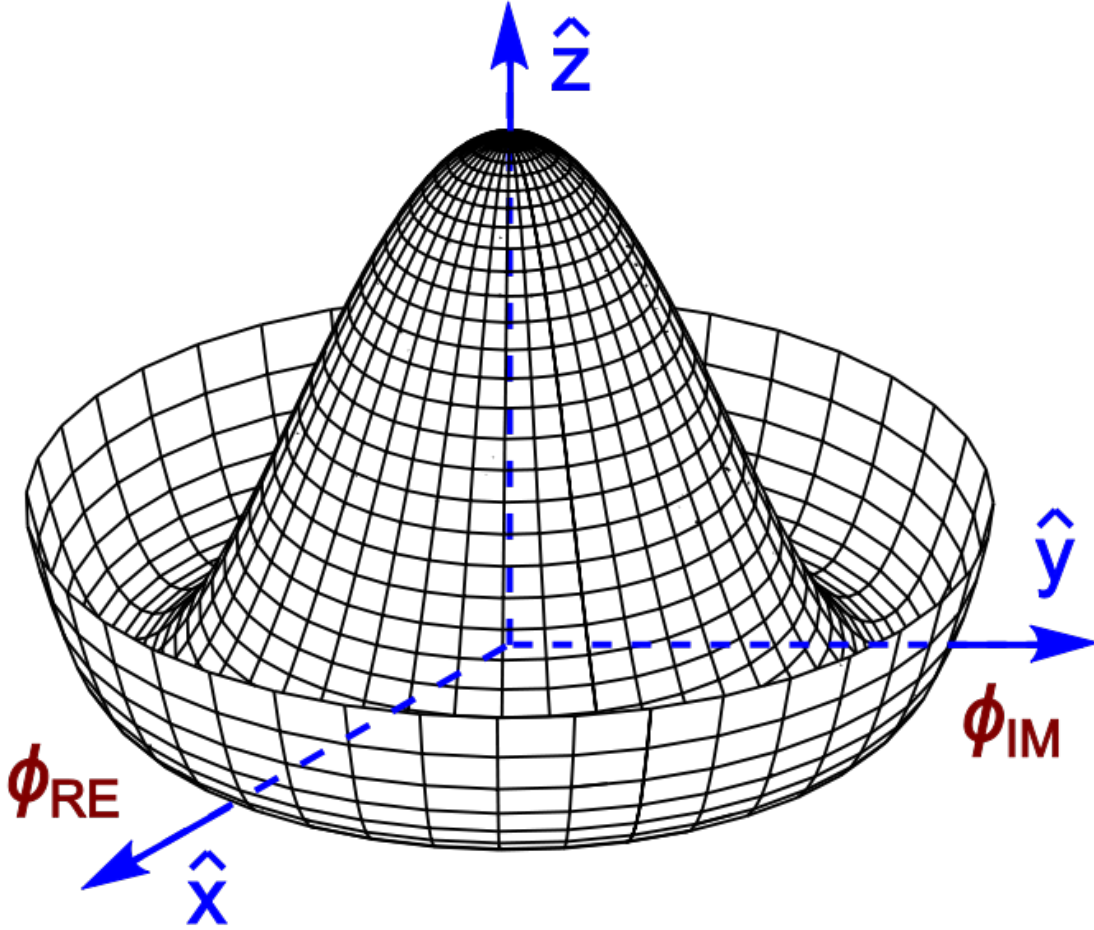
$$\phi = \frac{1}{\sqrt{2}} \exp\left(\frac{i}{v}\sigma_a\theta_a\right) \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}. \quad (2.5)$$

We can choose a gauge to rotate away the dependent on θ_a , such that we can write simply

$$\phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}. \quad (2.6)$$

Now, we can see how the masses of the vector bosons are generated from the application of the Higgs mechanism. We plug Eq.2.6 back into the electroweak Lagrangian, and only showing the relevant mass terms in the vacuum state where

Figure 2.1: Sombrero potential



$h(x) = 0$ see that (dropping the Lorentz indices) :

$$\begin{aligned}\mathcal{L}_M &= \frac{1}{8} \left| \begin{pmatrix} gW_3 + g'B & g(W_1 - iW_2) \\ g(W_1 + iW_2) & -gW_3 + g'B \end{pmatrix} \begin{pmatrix} 0 \\ v \end{pmatrix} \right|^2 \\ &= \frac{g^2 v^2}{8} [W_1^2 + W_2^2 + (\frac{g'}{g}B - W_3)^2]\end{aligned}\tag{2.7}$$

Defining the *Weinberg* angle $\tan(\theta_W) = g'/g$ and the following physical fields :

$$\begin{aligned}W^\pm &= \frac{1}{\sqrt{2}}(W_1 \mp iW_2) \\ Z^0 &= \cos \theta_W W_3 - \sin \theta_W B \\ A^0 &= \sin \theta_W W_3 + \cos \theta_W B\end{aligned}\tag{2.8}$$

CHECK 162

THIS EQUATION, especially the squaring?, I'm a bit confused

we see we can write the piece of the Lagrangian associated to the vector boson masses as

$$\mathcal{L}_{M_V} = \frac{1}{4}g^2v^2W^+W^- + \frac{1}{8}(g^2 + g'^2)v^2Z^0Z^0. \quad (2.9)$$

and we have the following values of the masses for the vector bosons :

$$\begin{aligned} m_W^2 &= \frac{1}{4}v^2g^2 \\ m_Z^2 &= \frac{1}{4}v^2(g^2 + g'^2) \\ m_A^2 &= 0 \end{aligned} \quad (2.10)$$

163 We thus see how the Higgs mechanism gives rise to the masses of the W^\pm and Z
 164 boson in the Standard Model; the mass of the photon is zero, as expected. The
 165 $SU(2)_L \otimes U(1)_Y$ symmetry of the initially massless $W_{1,2,3}$ and B fields is broken to
 166 the $U(1)_{EM}$. Of the four degrees of freedom in the complex Higgs doublet, three are
 167 “eaten” when we give mass to the W^\pm and Z_0 , while the other degree of freedom is
 168 the Higgs particle, as found in 2012 .

cite

169 Quantum Chromodynamics

Quantum chromodynamics (or the theory of the *strong* force) characterizes the behavior of *colored* particles, collectively known as *partons*. The partons of the Standard Model are the (fermionic) quarks, and the (bosonic) gluons. The strong force is governed by $SU(3)_C$ which is an unbroken symmetry in the Standard Model; this implies the gluon remains massless. Defining the covariant derivative for QCD as

$$D^\mu = \partial^\mu + ig_s G_a^\mu L_a \quad (2.11)$$

where L_a are the generators of $SU(3)_C$, often represented by the Gell-Mann matrices, and g_s is the coupling constant of the strong force. . The QCD Lagrangian then is given by

$$\mathcal{L}_{\text{QCD}} = i\bar{\psi}_f D_\mu \gamma^\mu \psi_f - \frac{1}{4} G_{\mu\nu}^a G_a^{\mu\nu} \quad (2.12)$$

check the logic here?
are teh actually them?

where the summation over f is for quarks *families*, and $G_a^{\mu\nu}$ is the gluon field strength tensor, given by

$$G_a^{\mu\nu} = \partial^\mu G_a^\nu - \partial^\nu G_a^\mu - g_s f^{abc} G_b^\mu G_c^\nu, a = 1, \dots, 8 \quad (2.13)$$

where f^{abc} are the structure constants of $SU(3)_C$, which are analogous to ϵ_{abc} for $SU(2)_L$. The kinetic term for the quarks is contained in the standard ∂_μ term, while the field strength term contains the interactions between the quarks and gluons, as well as the gluon self-interactions.

Written down in this simple form, the QCD Lagrangian does not seem much different from the QED Lagrangian, with the proper adjustments for the different

group structures. The gluon is massless, like the photon, so one could naïvely expect an infinite range force, and it pays to understand why this is not the case. The reason for this fundamental difference is the gluon self-interactions arising in the

field strength tensor term of the Lagrangian. This leads to the phenomena of *color confinement*, which describes how one only observes color-neutral particles alone in

nature. In contrast to the electromagnetic force, particles which interact via the strong force experience a *greater* force as the distance between the particles increases. At long distances, the potential is given by $V(r) = -kr$. At some point, it is more energetically favorable to create additional partons out of the vacuum than continue pulling apart the existing partons, and the colored particles undergo *fragmentation*. This leads to *hadronization*. Bare quarks and gluons are actually observed as sprays of hadrons (primarily kaons and pions); these sprays are known as *jets*, which are what are observed by experiments.

It is important to recognize the importance of understanding these QCD interactions in high-energy hadron colliders such as the LHC. Since protons are hadrons, proton-proton collisions such as those produced by the LHC are primarily governed by the processes of QCD. In particular, by far the most frequent process observed in LHC experiments is dijet production from gluon-gluon interactions. These gluons

194 that interact are part of the *sea* particles inside the proton; the simple $p = uud$
 195 model does not apply. The main *valence* uud quarks are constantly interacting via
 196 gluons, which can themselves radiate gluons or split into quarks, and so on. A
 197 more useful understanding is given by the colloquially-known *bag* model, where the
 198 proton is seen as a “bag” of (in principle) infinitely many partons, each with energy
 199 $E < \sqrt{s} = 6.5$ TeV. . . One then collides this (proton) bag with another, and views
 200 the products of this very complicated collision.

get that
cross section
picture

201 Fortunately, we are generally saved by the QCD factorization theorem . This
 202 allows one to understand the hard (i.e. short distance or highest energy) $2 \rightarrow 2$ parton
 203 process using the tools of perturbative QCD, while making series of approximations
 204 known as a *parton shower* model to understand the additional corrections from
 205 nonperturbative QCD. We will discuss the reconstruction of jets by experiments in
 206 Ch.??.

bag model?

cite QCD
factorization

207 .

show ratio of
ee to qq?

208 Fermions

209 We will now look more closely at the fermions in the Standard Model.

210 As noted earlier with regards to the field content, the fermions of the Standard
 211 Model can be first distinguished between those that interact via the strong force
 212 (quarks) and those which do not (leptons).

213 There are six leptons in the Standard Model, which can be placed into three
 214 *generations*. There is the electron (e), muon (μ), and tau (τ), each of which has an
 215 associated neutrino (ν_e, ν_μ, ν_τ). Each of the so-called charged (“electron-like”) leptons
 216 has electromagnetic charge -1 , while the neutrinos all have $q_{EM} = 0$.

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probably

217 Often in an experimental context, lepton is used to denote the electron (stable)
 218 and muon (metastable), due to their striking experimental signatures. Taus are often
 219 treated separately, due to their much shorter lifetime of τ_τ ; these decay through

220 hadrons or the other leptons, so often physics analyses at the LHC treat them as jets
 221 or leptons, as will be done in this thesis.

222 As the neutrinos are electrically neutral, nearly massless, and only interact via the
 223 weak force, it is quite difficult to observe them directly. Since LHC experiments rely
 224 overwhelmingly on electromagnetic interactions to observe particles, the presence of
 225 neutrinos is not observed directly. Neutrinos are instead observed by the conservation
 226 of four-momentum in the plane transverse to the proton-proton collisions, known as
 227 *missing transverse energy*.

There are six quarks in the Standard Model : up, down, charm, strange, top, and bottom. Quarks are similar organized into three generations :

$$\begin{pmatrix} u & d \end{pmatrix}, \begin{pmatrix} c & s \end{pmatrix}, \begin{pmatrix} t & b \end{pmatrix} \quad (2.14)$$

228 where we speak of “up-like” quarks and “down-like” quarks.

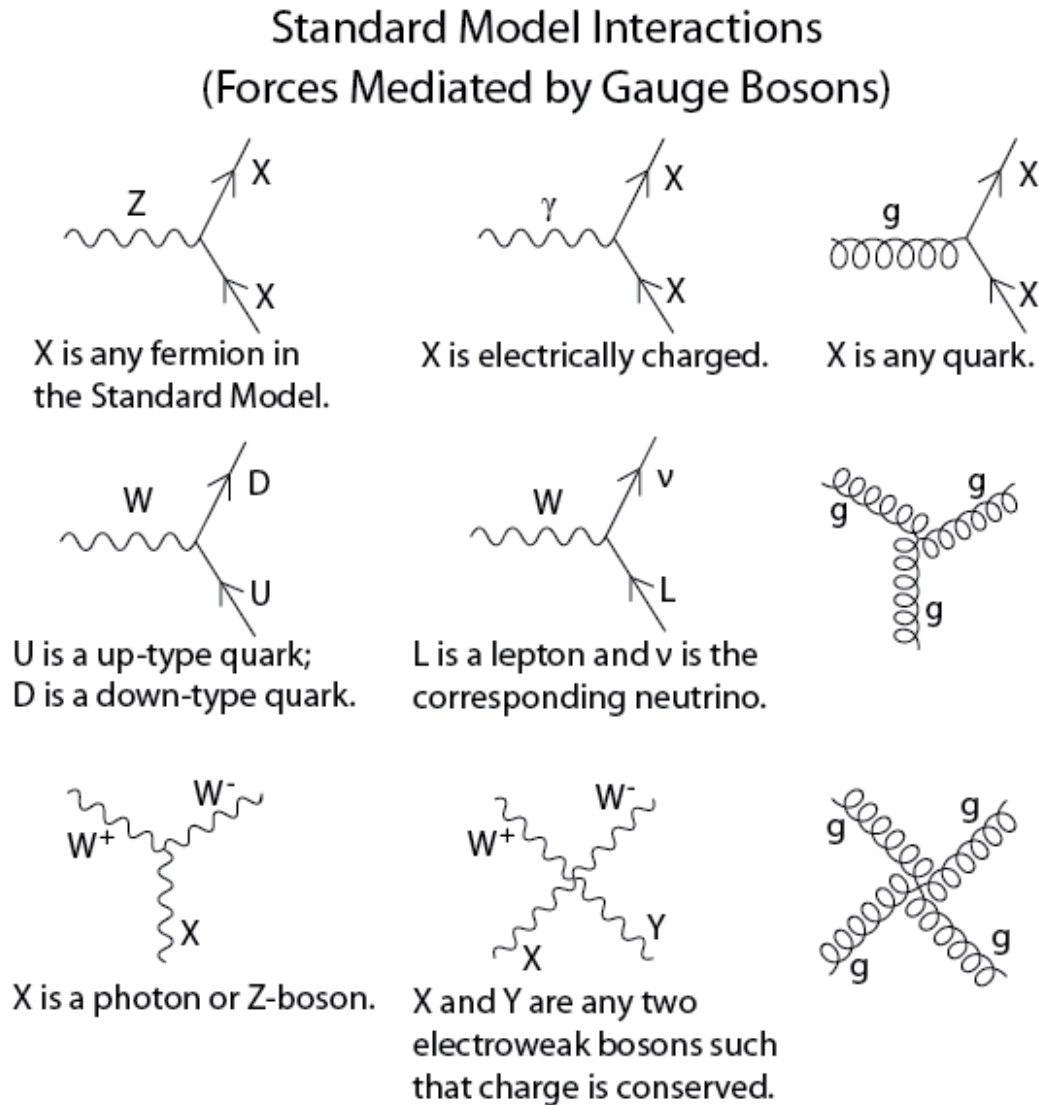
229 Each up-like quark has charge $q_{up} = 2/3$, while the down-like quarks have $q_{down} =$
 230 $-1/3$. At the high energies of the LHC, one often makes the distinction between
 231 the light quarks (u, d, c, s), the bottom quark, and top quark. In general, due to
 232 the hadronization process described above, the light quarks are indistinguishable by

233 LHC experiments, and reconstructed as jets.. The bottom quark hadronizes primarily
 234 through a relatively long-lived particle known as the B (name), which generally travels
 235 a short distance before decay. This feature allows what is known as *b-tagging*; this
 236 will be further discussed in Ch. Due to its large mass, the top quark decays before
 237 it can hadronize; there are no bound states associated to the top quark. The top
 238 is of particular interest at the LHC; it has a striking signature with a large cross-
 239 section, which can be used to distinguish signal processes with decays to top quarks,
 240 or understand top production as a background process.

footnote 233
 about char 234
 tagging 235

refCh 236
 ATLAS. 237

Figure 2.2: The interactions of the Standard Model



241 Interactions in the Standard Model

242

243 We briefly overview the entirety of the fundamental interactions of the Standard
244 Model; these can also be found in [??](#).

245 The electromagnetic force, mediated by the photon, interacts with via a three-
246 point coupling all charged particles in the Standard Model. The photon thus interacts

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247 with all the quarks, the charged leptons, and the charged W^\pm bosons.

248 The weak force is mediated by three particles : the W^\pm and the Z^0 . The Z^0
249 can interact with all fermions via a three-point coupling, governed by the coupling

CHECK 250 constant g' . A real Z_0 can thus decay to two of each fermion in the Standard Model
251 except for the top quark, due to its large mass. The W^\pm has two important three-point
252 interactions with fermions. First, the W^\pm can interact with an up-like quark and a
253 down-like quark. The coupling constants for these interactions are encoded in the

cite 254 CKM matrix Secondly, the W^\pm interacts with a charged lepton and its corresponding
255 neutrino. Finally, there are the self-interactions of the weak gauge bosons. There is
256 a three-point and four-point interaction; all combinations are allowed which conserve
257 electric charge.

258 The strong force is mediated by the gluon, which as discussed above also carries
259 the strong color charge. There is the fundamental three-point interaction, where a
260 gluon interacts with any quark. Additionally, there are the gluon-only interactions,
261 which occur in a three-point and four-point interaction.

262 2.3 Deficiencies of the Standard Model

263 At this point, it is quite easy to simply rest on our laurels. This relatively simple
264 theory is capable of explaining a very wide range of phenomenom, which ultimately
265 break down only to combinations of nine diagrams shown in Eq.???. Unfortunately,
266 there are some unexplained problems with the Standard Model. We cannot go
267 through all of the potential issues in this thesis, but we will motivate the primary
268 issues which naturally lead one to *supersymmetry*, as we will see in Ch.??.

add list of
them from
PDG

The Standard Model has many free paramaters , especially when corrected for
neutrino masses. In general, we prefer models with less free parameters. A great
example of this fact, and additionally some of the strongest experimental proof of

only?

EWSB, is the relationship between the couplings of the weak force and the masses of the gauge bosons of the weak force :

$$\rho m_Z^2 \cos^2 \theta_W \stackrel{?}{=} 1 \quad (2.15)$$

where ? indicates that this is a testable prediction of the Standard Model (in particular, that the gauge bosons gain mass through EWSB). This relation has been shown to be true within experimental and theoretical predictions. We would like to produce additional such relationships, which would exist if the Standard Model is a low-energy approximation of some other theory.

cite pdg

An additional issue, although not strictly fundamental, is the lack of gauge coupling unification. The couplings of any quantum field theory “run” as a function of the distance scales (or inversely, energy scales) of the theory. The idea is closely related to the unification of the electromagnetic and weak forces at the so-called *electroweak scale* of $O(100 \text{ GeV})$. One would hope this behavior was repeated between the electroweak forces and the strong force at some suitable energy scale. The Standard Model does automatically not exhibit this behavior, without some additional theoretical gymnastics.

The most significant problem with the Standard Model is the *hierarchy problem*. In its most straightforward incarnation, the Higgs scalar field is subject to quantum corrections through loop diagrams, as shown in Fig. For demonstration, we use the contributions from the top quark, since the top quark has the largest Higgs Yukawa coupling due to its large mass. In general, we should expect these corrections to quadratically dependent on the scale of the ultraviolet physics, Λ . Briefly assume there is no new physics before the scale of Planck scale of gravity, $\Lambda_{\text{Planck}} = 10^{19} \text{ GeV}$. In this case, we expect the corrections to the Higgs mass like

maybe show the lack of unification for the Standard Model?

loop figure!!

$$\delta m_H^2 \approx \left(\frac{m_t}{8\pi^2 < \phi >_{VEV}} \right)^2 \Lambda_{\text{Planck}}^2. \quad (2.16)$$

282 To achieve the miraculous cancellation required to get the observed Higgs Mass of
283 125 GeV, one needs to then set the bare Higgs mass m_0 , our input to the Standard
284 Model Lagrangian, itself to a *precise* value 10^{19} GeV. This extraordinary level of
285 parameter finetuning is quite undesirable, and within the framework of the Standard
286 Model, there is little that can be done to alleviate this issue.

287 An additional concern, of a different nature, is the lack of a *dark matter* candidate

288 in the Standard Model. Dark matter was discovered by observing galactic rotation
289 curves, which showed that much of the matter that interacted gravitationally was

290 invisible to our (electromagnetic) telescopes. The postulation of the existence of
291 dark matter, which interacts at least through gravity, allows one to understand these

292 galactic rotation curves. Unfortunately, no particle in the Standard Model *could*
293 be this dark matter particle. The only candidate truly worth another look is the
294 neutrino, but it has been shown that the neutrino content of the universe is simply
295 too small to explain the galactic rotation curves (maybe say more). The experimental
296 evidence from the galactic rotations curves thus show there *must* be additional physics
297 beyond the Standard Model, which is yet to be understood.

298 In the next chapter, we will see how these problems can be alleviated by the theory
299 of supersymmetry.

300 2.4 Conclusions

301 The Standard Model is an extraordinary theory. It is a culmination of decades of
302 work in both theoretical and experimental physics. blah some more

303

Chapter 3

304

Supersymmetry

305 Here you can write some introductory remarks about your chapter. I like to give each
306 sentence its own line.

307 When you need a new paragraph, just skip an extra line.

308 **3.1 Motivation**

309 **Only Additional allowed Lorentz invariant symmetry**

310 **Dark Matter**

311 **Cancellation of quadratic divergences in corrections to the**

312 **Higgs Mass**

313 **3.2 Supersymmetry**

314 **3.3 Additional particle content**

315 **3.4 Phenomenology**

316 **R parity Consequences for sq/gl decays**

317

Chapter 4

318

The Large Hadron Collider

319 Here you can write some introductory remarks about your chapter. I like to give each
320 sentence its own line.

321 When you need a new paragraph, just skip an extra line.

322 **4.1 Magnets**

323 By using the asterisk to start a new section, I keep the section from appearing in the
324 table of contents. If you want your sections to be numbered and to appear in the
325 table of contents, remove the asterisk.

326

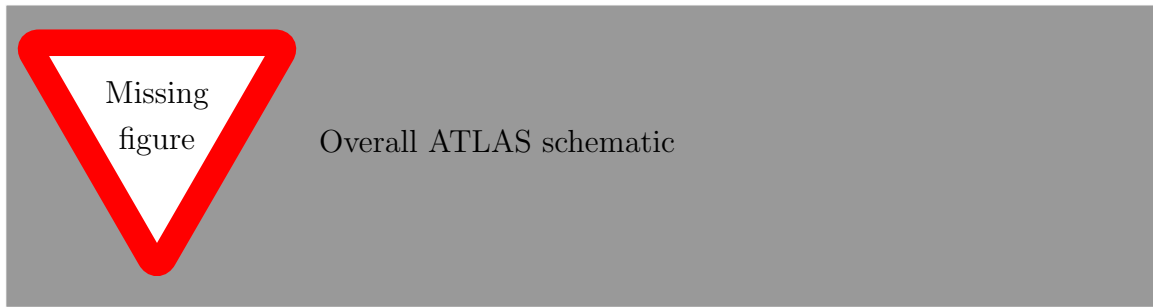
Chapter 5

327

The ATLAS detector

328 Here you can write some introductory remarks about your chapter. I like to give each
329 sentence its own line.

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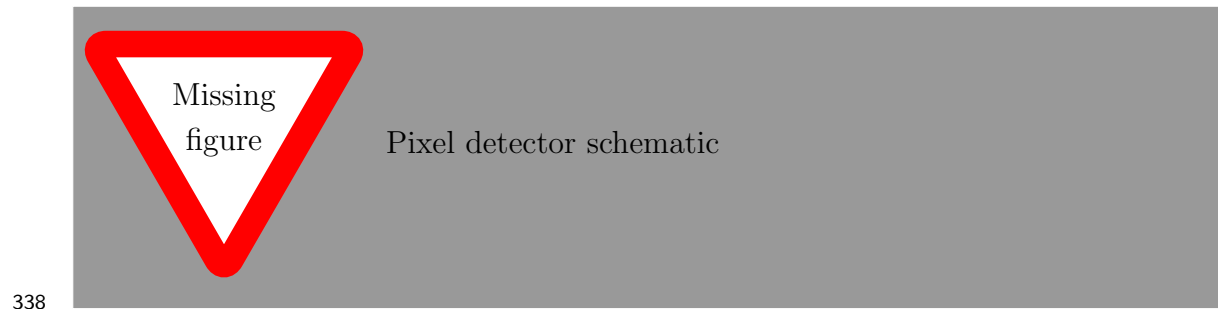
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332

333 **5.1 Inner Detector**

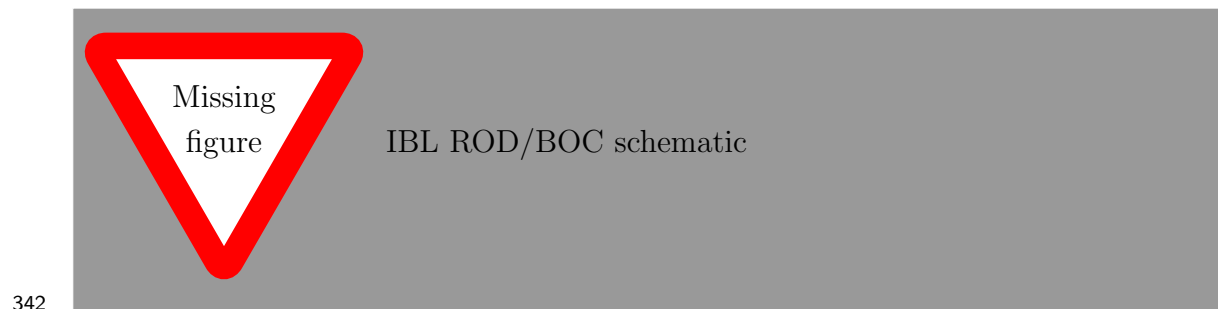
334 By using the asterisk to start a new section, I keep the section from appearing in the
335 table of contents. If you want your sections to be numbered and to appear in the
336 table of contents, remove the asterisk.

337 **Pixel Detector**

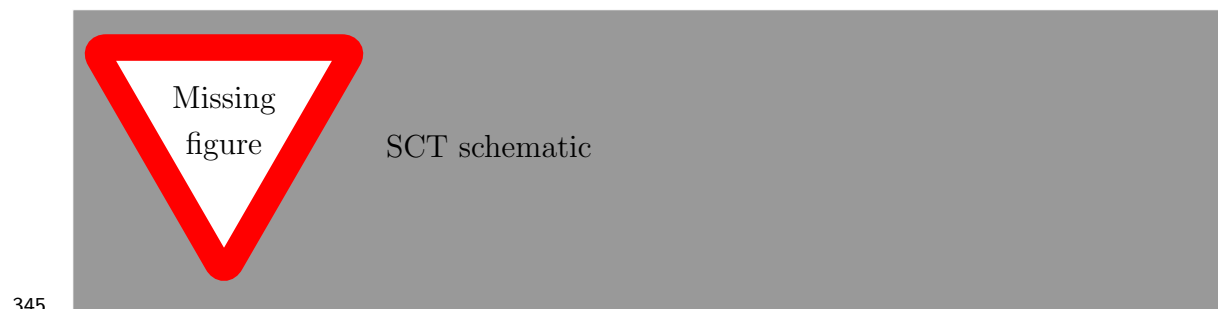


340 **Insertable B-Layer**

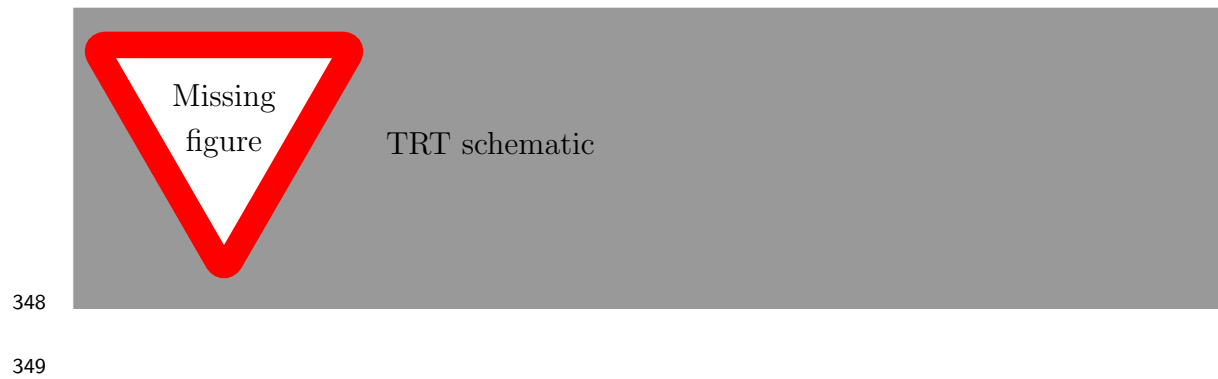
341 Qualification task, so add a bit more.



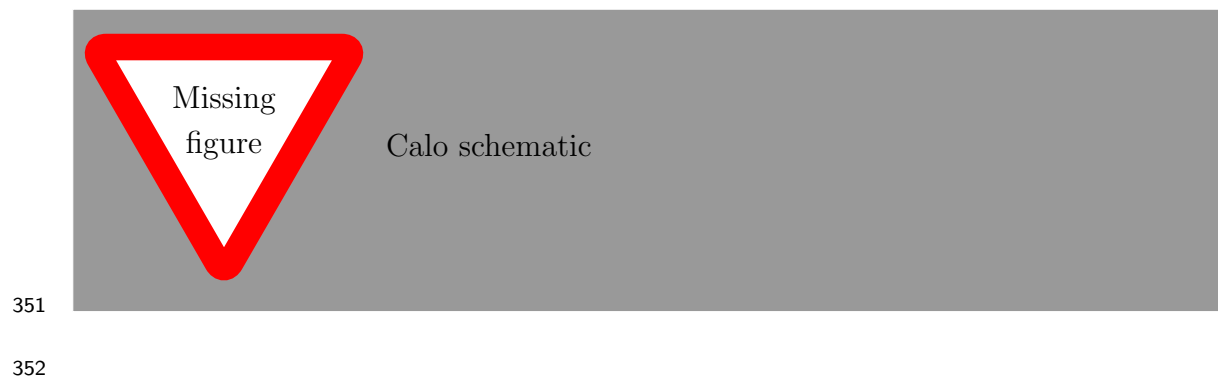
344 **Semiconductor Tracker**



347 **Transition Radiation Tracker**



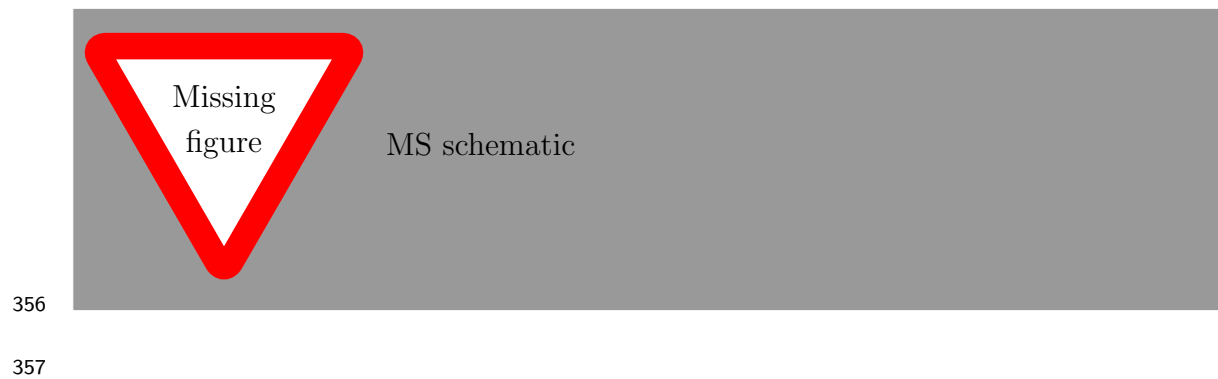
350 **5.2 Calorimeter**



353 **Electromagnetic Calorimeter**

354 **Hadronic Calorimeter**

355 **5.3 Muon Spectrometer**



The Recursive Jigsaw Technique

360 Here you can write some introductory remarks about your chapter. I like to give each
361 sentence its own line.

362 When you need a new paragraph, just skip an extra line.

363 **6.1 Razor variables**

364 By using the asterisk to start a new section, I keep the section from appearing in the
365 table of contents. If you want your sections to be numbered and to appear in the
366 table of contents, remove the asterisk.

367 **6.2 SuperRazor variables**

368 **6.3 The Recursive Jigsaw Technique**

369 **6.4 Variables used in the search for zero lepton**

370 **SUSY**

371

Chapter 7

372

Title of Chapter 1

373

Chapter 8

374

Title of Chapter 1

375 Here you can write some introductory remarks about your chapter. I like to give each
376 sentence its own line.

377 When you need a new paragraph, just skip an extra line.

378 **8.1 Object reconstruction**

379 **Photons, Muons, and Electrons**

380 **Jets**

381 **Missing transverse momentum**

382 Probably longer, show some plots from the PUB note that we worked on

383 8.2 Signal regions

384 Gluino signal regions

385 Squark signal regions

386 Compressed signal regions

387 8.3 Background estimation

388 $Z \nu\nu$

389 $W e\nu$

390 $t\bar{t}$

391

Chapter 9

392

Title of Chapter 1

393 Here you can write some introductory remarks about your chapter. I like to give each
394 sentence its own line.

395 When you need a new paragraph, just skip an extra line.

396 **9.1 Statistical Analysis**

397 maybe to be moved to an appendix

398 **9.2 Signal Region distributions**

399 **9.3 Pull Plots**

400 **9.4 Systematic Uncertainties**

401 **9.5 Exclusion plots**

402

Conclusion

403 Here you can write some introductory remarks about your chapter. I like to give each
404 sentence its own line.

405 When you need a new paragraph, just skip an extra line.

406 **9.6 New Section**

407 By using the asterisk to start a new section, I keep the section from appearing in the
408 table of contents. If you want your sections to be numbered and to appear in the
409 table of contents, remove the asterisk.

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529

The Standard Model

530 In this appendix, we provide a brief overview of the basic ingredients involved in
 531 construction of the Standard Model Lagrangian : quantum field theory, symmetries,
 532 and symmetry breaking.

533 Quantum Field Theory

534

535 In this section, we provide a brief overview of the necessary concepts from
 536 Quantum Field Theory (QFT).

537 In modern physics, the laws of nature are described by the “action” S , with the
 538 imposition of the principle of minimum action. The action is the integral over the
 539 spacetime coordinates of the “Lagrangian density” \mathcal{L} , or Lagrangian for short. The
 540 Lagrangian is a function of “fields”; general fields will be called $\phi(x^\mu)$, where the
 541 indices μ run over the space-time coordinates. We can then write the action S as

$$S = \int d^4x \mathcal{L}[\phi_i(x^\mu), \partial_\mu \phi_i(x^\mu)] \quad (9.1)$$

542 where we have an additional summation over i (of the different fields). Generally,
 543 we impose the following constraints on the Lagrangian :

- 544 1. Translational invariance - The Lagrangian is only a function of the fields ϕ and
 545 their derivatives $\partial_\mu \phi$
- 546 2. Locality - The Lagrangian is only a function of one point x_μ in spacetime.

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- 547 3. Reality condition - The Lagrangian is real to conserve probability.
- 548 4. Lorentz invariance - The Lagrangian is invariant under the Poincaré group of
549 spacetime.
- 550 5. Analyticity - The Lagrangian is an analytical function of the fields; this is to
551 allow the use of perturbation theory.
- 552 6. Invariance and Naturalness - The Lagrangian is invariant under some internal
553 symmetry groups; in fact, the Lagrangian will have *all* terms allowed by the
554 imposed symmetry groups.
555 7. Renormalizability - The Lagrangian will be renormalizable - in practice, this
556 means there will not be terms with more than power 4 in the fields.

557 The key item from the point of view of this thesis is that of “Invariance and
558 Natural”. We impose a set of “symmetries” and then our Lagrangian is the most
559 general which is allowed by those symmetries.

560 Symmetries

561 Symmetries can be seen as the fundamental guiding concept of modern physics.
562 Symmetries are described by “groups”. . To illustrate the importance of symmetries
563 and their mathematical description, groups, we start here with two of the simplest
564 and most useful examples : \mathbb{Z}_2 and $U(1)$.

565 \mathbb{Z}_2 symmetry

566 \mathbb{Z}_2 symmetry is the simplest example of a “discrete” symmetry. Consider the most
567 general Lagrangian of a single real scalar field $\phi(x_\mu)$

$$\mathcal{L}_\phi = \frac{1}{2}\partial_\mu\phi\partial^\mu\phi - \frac{m^2}{2}\phi^2 - \frac{\mu}{2\sqrt{2}}\phi^3 - \lambda\phi^4 \quad (9.2)$$

Now we *impose* the symmetry

$$\mathcal{L}(\phi) = \mathcal{L}(-\phi) \quad (9.3)$$

568 This has the effect of restricting the allowed terms of the Lagrangian. In particular,
 569 we can see the term $\phi^3 \rightarrow -\phi^3$ under the symmetry transformation, and thus must
 570 be disallowed by this symmetry. This means under the imposition of this particular
 571 symmetry, our Lagrangian should be rewritten as

$$\mathcal{L}_\phi = \frac{1}{2}\partial_\mu\phi\partial^\mu\phi - \frac{m^2}{2}\phi^2 - \lambda\phi^4 \quad (9.4)$$

572 The effect of this symmetry is that the total number of ϕ particles can only change
 573 by even numbers, since the only interaction term $\lambda\phi^4$ is an even power of the field.
 574 This symmetry is often imposed in supersymmetric theories, as we will see in Chapter
 575 3.

576 **$U(1)$ symmetry**

577 $U(1)$ is the simplest example of a continuous (or *Lie*) group. Now consider a theory
 578 with a single complex scalar field $\phi = \text{Re } \phi + i \text{Im } \phi$

$$\mathcal{L}_\phi = \delta_{i,j} \frac{1}{2} \partial_\mu \phi_i \partial^\mu \phi_j - \frac{m^2}{2} \phi_i \phi_j - \frac{\mu}{2\sqrt{2}} \phi_i \phi_j \phi_k - \lambda \phi_i \phi_j \phi_k \phi_l \quad (9.5)$$

579 where $i, j, k, l = \text{Re}, \text{Im}$. In this case, we impose the following $U(1)$ symmetry
 580 : $\phi \rightarrow e^{i\theta} \phi, \phi^* \rightarrow e^{-i\theta} \phi^*$. We see immediately that this again disallows the third-order
 581 terms, and we can write a theory of a complex scalar field with $U(1)$ symmetry as

$$\mathcal{L}_\phi = \partial_\mu \phi \partial^\mu \phi^* - \frac{m^2}{2} \phi \phi^* - \lambda (\phi \phi^*)^2 \quad (9.6)$$

582 Local symmetries

583 The two examples considered above are “global” symmetries in the sense that the
584 symmetry transformation does not depends on the spacetime coordinate x_μ . We know
585 look at local symmetries; in this case, for example with a local $U(1)$ symmetry, the
586 transformation has the form $\phi(x_\mu) \rightarrow e^{i\theta(x_\mu)}\phi(x_\mu)$. These symmetries are also known
587 as “gauge” symmetries; all symmetries of the Standard Model are gauge symmetries.

There are wide-ranging consequences to the imposition of local symmetries. To begin, we note that the derivative terms of the Lagrangian 9.2 are *not* invariant under a local symmetry transformation

$$\partial_\mu \phi(x_\mu) \rightarrow \partial_\mu (e^{i\theta(x_\mu)} \phi(x_\mu)) = (1 + i\theta(x_\mu)) e^{i\theta(x_\mu)} \phi(x_\mu) \quad (9.7)$$

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This leads us to note that the kinetic terms of the Lagrangian are also not invariant
590 under a gauge symmetry. This would lead to a model with no dynamics, which is
591 clearly unsatisfactory.

592 Let us take inspiration from the case of global symmetries. We need to define a
593 so-called “covariant” derivative D^μ such that

$$\begin{aligned} D^\mu \phi &\rightarrow e^{iq\theta(x^\mu)} D^\mu \phi \\ D^\mu \phi^* &\rightarrow e^{-iq\theta(x^\mu)} D^\mu \phi \end{aligned} \quad (9.8)$$

594 Since ϕ and ϕ^* transforms with the opposite phase, this will lead the invariance
595 of the Lagrangian under our local gauge transformation. This D^μ is of the following
596 form

$$D^\mu = \partial_\mu - igqA^\mu \quad (9.9)$$

597 where A^μ is a vector field we introduce with the transformation law

$$A^\mu \rightarrow A^\mu - \frac{1}{g} \partial_\mu \theta \quad (9.10)$$

598 and g is the coupling constant associated to vector field. This vector field A^μ is
 599 also known as a “gauge” field.

600 Since we need to add all allowed terms to the Lagrangian, we define

$$F^{\mu\nu} = A^\mu A^\nu - A^\nu A^\mu \quad (9.11)$$

601 and then we must also add the kinetic term :

$$\mathcal{L}_{\text{gauge}} = -\frac{1}{4} F^{\mu\nu} F_{\mu\nu} \quad (9.12)$$

602 The most general renormalizable Lagrangian with fermion and scalar fields can
 603 be written in the following form

$$\mathcal{L} = \mathcal{L}_{kin} + \mathcal{L}_\phi + \mathcal{L}_\psi + \mathcal{L}_{Yukawa} \quad (9.13)$$

604 Symmetry breaking and the Higgs mechanism

605 Here we view some examples of symmetry breaking. We investigate breaking of a
 606 global $U(1)$ symmetry and a local $U(1)$ symmetry. The SM will break the electroweak
 607 symmetry $SU(2) \times U(1)$, and in Chapter 3 we will see how supersymmetry must also
 608 be broken.

609 There are two ideas of symmetry breaking

- 610 • Explicit symmetry breaking by a small parameter - in this case, we have a small
 611 parameter which breaks an “approximate” symmetry of our Lagrangian. An
 612 example would be the theory of the single scalar field [9.2](#), when $\mu \ll m^2$ and
 613 $\mu \ll \lambda$. In this case, we can often ignore the small term when considering
 614 low-energy processes.

615 • Spontaneous symmetry breaking (SSB) - spontaneous symmetry breaking
 616 occurs when the Lagrangian is symmetric with respect to a given symmetry
 617 transformation, but the ground state of the theory is *not* symmetric with respect
 618 to that transformation. This can have some fascinating consequences, as we
 619 will see in the following examples

620 Symmetry breaking a

621 U(1) global symmetry breaking

Consider the theory of a complex scalar field under the $U(1)$ symmetry, or the transformation

$$\phi \rightarrow e^{i\theta} \phi \quad (9.14)$$

The Lagrangian for this theory is

$$\mathcal{L} = \partial^\mu \phi^\dagger \partial_\mu \phi + \frac{\mu^2}{2} \phi^\dagger \phi + \frac{\lambda}{4} (\phi^\dagger \phi)^2 \quad (9.15)$$

Let us write this theory in terms of two scalar fields, h and ξ : $\phi = (h + i\xi)/\sqrt{2}$.

The Lagrangian can then be written as

$$\mathcal{L} = \partial^\mu h \partial_\mu h + \partial^\mu \xi \partial_\mu \xi - \frac{\mu^2}{2} (h^2 + \xi^2) - \frac{\lambda}{4} (h^2 + \xi^2)^2 \quad (9.16)$$

First, note that the theory is only stable when $\lambda > 0$. To understand the effect of SSB, we now enforce that $\mu^2 < 0$, and define $v^2 = -\mu^2/\lambda$. We can then write the scalar potential of this theory as :

$$V(\phi) = \lambda(\phi^\dagger \phi - v^2/2)^2 \quad (9.17)$$

Minimizing this equation with respect to ϕ , we can see that the “vacuum expectation value” of the theory is

$$2 \langle \phi^\dagger \phi \rangle = \langle h^2 + \xi^2 \rangle = v^2 \quad (9.18)$$

622 We now reach the “breaking” point of this procedure. In the (h, ξ) plane, the
623 minima form a circle of radius v . We are free to choose any of these minima to expand
624 our Lagrangian around; the physics is not affected by this choice. For convenience,
625 choose $\langle h \rangle = v, \langle \xi \rangle = 0$.

Now, let us define $h' = h - v, \xi' = \xi$ with VEVs $\langle h' \rangle = 0, \langle \xi' \rangle = 0$. We can then write our spontaneously broken Lagrangian in the form

$$\mathcal{L} = \frac{1}{2} \partial_\mu h' \partial^\mu h' + \frac{1}{2} \partial_\mu \xi' \partial^\mu \xi' - \lambda v^2 h'^2 - \lambda v h' (h'^2 + \xi'^2) - \lambda (h'^2 + \xi'^2)^2 \quad (9.19)$$