1	A search for sparticles in zero lepton final states
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12	ABSTRACT
13	A search for sparticles in zero lepton final states
14	Russell W. Smith
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16	center, but the abstract itself should be written as a regular paragraph on the page
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Introduction

Particle physics is a remarkably successful field of scientific inquiry. The ability to precisely predict the properties of a exceedingly wide range of physical phenomena, 65 such as the description of the cosmic microwave background [1, 2], the understanding 66 of the anomalous magnetic dipole moment of the electron [3, 4], and the measurement 67 of the number of weakly-interacting neutrino flavors [5] is truly amazing. 68 The theory that has allowed this range of predictions is the Standard Model 69 of particle physics (SM). The Standard Model combines the electroweak theory of 70 Glashow, Weinberg, and Salam [6–8] with the theory of the strong interactions, as 71 first envisioned by Gell-Mann and Zweig [9, 10]. This quantum field theory (QFT) 72 contains a tiny number of particles, whose interactions describe phenomena up to at 73 least the TeV scale. These particles are manifestations of the fields of the Standard Model, after application of the Higgs Mechanism. The particle content of the SM 75 consists only of the six quarks, the six leptons, the four gauge bosons, and the scalar 76 Higgs boson. 77 Despite its impressive range of described phenomena, the Standard Model has 78 some theoretical and experimental deficiencies. The SM contains 26 free parameters 79 It would be more theoretically pleasing to understand these free parameters in 80 terms of a more fundamental theory. The major theoretical concern of the Standard Model, as it pertains to this thesis, is the $hierarchy\ problem[11-15]$. The light mass

 $^{^1{\}rm This}$ is the Standard Model corrected to include neutrino masses. These parameters are the fermion masses (6 leptons, 6 quarks), CKM and PMNS mixing angles (8 angles, 2 CP-violating phases), W/Z/Higgs masses (3), the Higgs field expectation value, and the couplings of the strong, weak, and electromagnetic forces (3 α_{force}) .

of the Higgs boson (125 GeV) should be quadratically dependent on the scale of UV physics, due to the quantum corrections from high-energy physics processes. The most perplexing experimental issue is the existence of dark matter, as demonstrated 85 by galactic rotation curves [16-22]. This data has shown that there exists additional 86 matter which has not yet been seen interacting with the particles of the Standard 87 Model. There is no particle in the SM which can act as a candidate for dark matter. 88 Both of these major issues, as well as numerous others, can be solved by the 89 introduction of supersymmetry (SUSY) [15, 23–33]. In supersymmetric theories, each 90 SM particles has a so-called *superpartner*, or sparticle partner, differing from given SM 91 particle by 1/2 in spin. These theories solve the hierarchy problem, since the quantum 92 corrections induced from the superpartners exactly cancel those induced by the SM 93 particles. In addition, these theories are usually constructed assuming R-parity, 94 which can be thought of as the "charge" of supersymmetry, with SM particles having 95

R=1 and sparticles having R=-1. In collider experiments, since the incoming

SM particles have total R=1, the resulting sparticles are produced in pairs. This

produces a rich phenomenology, which is characterized by significant hadronic activity

and large missing transverse energy $(E_{\rm T}^{\rm miss})$, which provide significant discrimination

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against SM backgrounds [34].

Despite the power of searches for supersymmetry where $E_{\mathrm{T}}^{\mathrm{miss}}$ is a primary 101 discriminating variable, there has been significant interest in the use of other variables 102 to discriminate against SM backgrounds. These include searches employing variables 103 such as αT , $M_{T,2}$, and the razor variables (M_R, R^2) [35–45]. In this thesis, we 104 will present the first search for supersymmetry using the novel Recursive Jigsaw 105 Reconstruction (RJR) technique. RJR can be considered the conceptual successor 106 of the razor variables. We impose a particular final state "decay tree" on an events, 107 which roughly corresponds to a simplified Feynmann diagram in decays containing 108 weakly-interacting particles. We account for the missing degrees of freedom associated 109

to the weakly-interacting particles by a series of simplifying assumptions, which allow us to calculate our variables of interest at each step in the decay tree. This allows an unprecedented understanding of the internal structure of the decay and the ability to construct additional variables to reject Standard Model backgrounds.

This thesis details a search for the superpartners of the gluon and quarks, the 114 gluino and squarks, in final states with zero leptons, with $13.3~{\rm fb^{-1}of}$ data using the 115 ATLAS detector. We organzie the thesis as follows. The theoretical foundations of 116 the Standard Model and supersymmetry are described in Chapters 2 and 3. The 117 Large Hadron Collider and the ATLAS detector are presented in Chapters 4 and 5. 118 Chapter 5 provides a detailed description of Recursive Jigsaw Reconstruction and a 119 description of the variables used for the particular search presented in this thesis. 120 Chapter 6 presents the details of the analysis, including details of the dataset, object 121 reconstruction, and selections used. In Chapter 7, the final results are presented; 122 since there is no evidence of a supersymmetric signal in the analysis, we present the 123 final exclusion curves in simplified supersymmetric models. 124

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The Standard Model

$_{7}$ 2.1 Overview

A Standard Model is another name for a theory of the internal symmetry group 128 $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$, with its associated set of parameters. The Standard 129 Model refers specifically to a Standard Model with the proper parameters to describe 130 The SM is the culmination of years of work in both theoretical the universe. 131 and experimental particle physics. In this thesis, we take the view that theorists 132 construct a model with the field content and symmetries as inputs, and write down the 133 most general Lagrangian consistent with those symmetries. Assuming this model is 134 compatible with nature (in particular, the predictions of the model are consistent with 135 previous experiments), experimentalists are responsible measuring the parameters of 136 this model This will be applicable for this chapter and the following one. 137 Additional theoretical background is in 9.6. The philosophy and notations are 138 inspired by [46, 47]. 139

• 2.2 Field Content

The Standard Model field content is

Fermions :
$$Q_L(3,2)_{+1/3}$$
, $U_R(3,1)_{+4/3}$, $D_R(3,1)_{-2/3}$, $L_L(1,2)_{-1}$, $E_R(1,1)_{-2}$
Scalar (Higgs) : $\phi(1,2)_{+1}$ (2.1)
Vector Fields : $G^{\mu}(8,1)_0$, $W^{\mu}(1,3)_0$, $B^{\mu}(1,1)_0$

where the $(A, B)_Y$ notation represents the irreducible representation under SU(3)

and SU(2), with Y being the electroweak hypercharge. Each of these fermion fields

has an additional index, representing the three generation of fermions.

We observed that Q_L, U_R , and D_R are triplets under $SU(3)_C$; these are the quark

fields. The color group, $SU(3)_C$ is mediated by the gluon field $G^{\mu}(8,1)_0$, which has

8 degrees of freedom. The fermion fields $L_L(1,2)_{-1}$ and $E_R(1,1)_{-2}$ are singlets under

147 $SU(3)_C$; we call them the *lepton* fields.

Next, we note the "left-handed" ("right-handed") fermion fields, denoted by L(R)

subscript, The left-handed fields form doublets under $SU(2)_L$. These are mediated

by the three degrees of freedom of the "W" fields $W^{\mu}(1,3)_0$. These fields only act

on the left-handed particles of the Standard Model. This is the reflection of the

treated differently by the electroweak forces. The right-handed fields, U_R, D_R , and

154 E_R , are singlets under $SU(2)_L$.

The $U(1)_Y$ symmetry is associated to the $B^{\mu}(1,1)_0$ boson with one degree of

156 freedom. The charge Y is known as the electroweak hypercharge.

To better understand the phenomenology of the Standard Model, let us investigate

each of the *sectors* of the Standard Model separately.

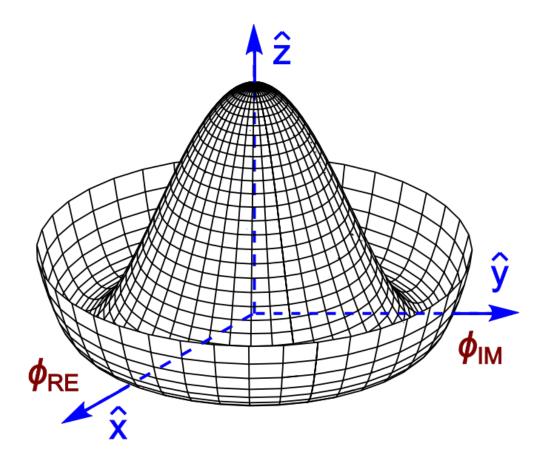
59 Electroweak sector

The electroweak sector refers to the $SU(2)_L \otimes U(1)_Y$ portion of the Standard Model gauge group. Following our philosophy of writing all gauge-invariant and renormalizable terms, the electroweak Lagrangian can be written as

$$\mathcal{L} = W_a^{\mu\nu} W_{\mu\nu}^a + B^{\mu\nu} B_{\mu\nu} + (D^{\mu}\phi)^{\dagger} D_{\mu}\phi - \mu^2 \phi^{\dagger}\phi - \lambda (\phi^{\dagger}\phi)^2. \tag{2.2}$$

where $W_a^{\mu\nu}$ are the three (a=1,2,3) gauge bosons associated to the $SU(2)_L$ gauge group, $B^{\mu\nu}$ is the one gauge boson of the $U(1)_Y$ gauge group, and ϕ is the complex

Figure 2.1: Sombrero potential



Higgs multiplet. The covariant derivative D^{μ} is given by

$$D^{\mu} = \partial^{\mu} + \frac{ig}{2} W_a^{\mu} \sigma_a + \frac{ig'}{2} B^{\mu} \tag{2.3}$$

where $i\sigma_a$ are the Pauli matrices times the imaginary constant, which are the generators for $SU(2)_L$, and g and g' are the $SU(2)_L$ and $U(1)_Y$ coupling constants, respectively. The field strength tensors $W_a^{\mu\nu}$ and $B^{\mu\nu}$ are given by the commutator of the covariant derivative associated to each field

$$B^{\mu\nu} = \partial^{\mu}B^{\nu} - \partial^{\nu}B^{\mu}$$

$$W_{a}^{\mu\nu} = \partial^{\mu}W_{a}^{\nu} - \partial^{\nu}W_{a}^{\mu} - g\epsilon_{abc}W_{a}^{\mu}W_{b}^{\nu}, \qquad i = 1, 2, 3$$

$$(2.4)$$

The terms in the Lagrangian 2.2 proportional to μ^2 and λ make up the "Higgs potential" [48]. As normal (see Appendix 9.6), we restrict $\lambda > 0$ to guarantee our potential is bounded from below, and we also require $\mu^2 < 0$, which gives us the standard "sombrero" potential shown in 2.1.

This potential has infinitely many minima at $\langle \phi \rangle = \sqrt{2m/\lambda}$; the ground state is spontaneously broken by the choice of ground state, which induces a vacuum expection value (VEV). Without loss of generality, we can choose the Higgs field ϕ to point in the real direction, and write the Higgs field ϕ in the following form:

$$\phi = \frac{1}{\sqrt{2}} \exp(\frac{i}{v} \sigma_a \theta_a) \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}. \tag{2.5}$$

We choose a gauge to rotate away the dependence on θ_a , such that we can write simply

$$\phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}. \tag{2.6}$$

Now, we can see how the masses of the vector bosons are generated from the application of the Higgs mechanism. We plug Eq.2.6 back into the electroweak Lagrangian, and only showing the relevant mass terms in the vacuum state where h(x) = 0 see that (dropping the Lorentz indices):

$$\mathcal{L}_{M} = \frac{1}{8} \left| \begin{pmatrix} gW_{3} + g'B & g(W_{1} - iW_{2}) \\ g(W_{1} + iW_{2}) & -gW_{3} + g'B \end{pmatrix} \begin{pmatrix} 0 \\ v \end{pmatrix} \right|^{2}$$

$$= \frac{g^{2}v^{2}}{8} \left[W_{1}^{2} + W_{2}^{2} + (\frac{g'}{g}B - W_{3})^{2} \right]$$
(2.7)

Defining the Weinberg angle $tan(\theta_W) = g'/g$ and the following physical fields:

$$W^{\pm} = \frac{1}{\sqrt{2}} (W_1 \mp iW_2)$$

$$Z^0 = \cos \theta_W W_3 - \sin \theta_W B$$

$$A^0 = \sin \theta_W W_3 + \cos \theta_W B$$
(2.8)

we can write the piece of the Lagrangian associated to the vector boson masses as

$$\mathcal{L}_{M_V} = \frac{1}{4}g^2 v^2 W^+ W^- + \frac{1}{8}(g^2 + g'^2)v^2 Z^0 Z^0.$$
 (2.9)

and we have the following values of the masses for the vector bosons:

$$m_W^2 = \frac{1}{4}v^2g^2$$

$$m_Z^2 = \frac{1}{4}v^2(g^2 + g'^2)$$

$$m_A^2 = 0$$
(2.10)

We thus see how the Higgs mechanism gives rise to the masses of the W^{\pm} and Z boson in the Standard Model; the mass of the photon is zero, as expected. The $SU(2)_L \otimes U(1)_Y$ symmetry of the initially massless $W_{1,2,3}$ and B fields is broken to the $U(1)_{EM}$. Of the four degrees of freedom in the complex Higgs doublet, three are "eaten" when we give mass to the W^{\pm} and Z_0 , while the other degree of freedom is the Higgs particle, as found in 2012 by the ATLAS and CMS collaborations [49, 50].

171 Quantum Chromodynamics

Quantum chromodynamics (or the theory of the *strong* force) characterizes the behavior of *colored* particles, collectively known as *partons*. The partons of the Standard Model are the (fermionic) quarks, and the (bosonic) gluons. The strong force is governed by $SU(3)_C$, an unbroken symmetry in the Standard Model, which implies the gluon remains massless. Defining the covariant derivative for QCD as

$$D^{\mu} = \partial^{\mu} + ig_s G^{\mu}_a L_a, a = 1, ..., 8$$
 (2.11)

where L_a are the generators of $SU(3)_C$, and g_s is the coupling constant of the strong force. The QCD Lagrangian then is given by

$$\mathcal{L}_{\text{QCD}} = i\bar{\psi}_f D_\mu \gamma^\mu \psi_f - \frac{1}{4} G_{a,\mu\nu} G_a^{\mu\nu}$$
 (2.12)

where the summation over f is for quarks families, and $G_a^{\mu\nu}$ is the gluon field strength tensor, given by

$$G_a^{\mu\nu} = \partial^{\mu} G_a^{\nu} - \partial^{\nu} G_a^{\mu} - g_s f^{abc} G_b^{\mu} G_c^{\nu}, a, b, c = 1, ..., 8$$
 (2.13)

where f^{abc} are the structure constants of $SU(3)_C$, which are analogous to ϵ_{abc} for $SU(2)_L$. The kinetic term for the quarks is contained in the standard ∂_{μ} term, while the field strength term contains the interactions between the quarks and gluons, as well as the gluon self-interactions.

Written down in this simple form, the QCD Lagrangian does not seem much 176 different from the QED Lagrangian, with the proper adjustments for the different 177 group structures. The gluon is massless, like the photon, so one could näively expect 178 an infinite range force, and it pays to understand why this is not the case. The 179 reason for this fundamental difference is the gluon self-interactions arising in the 180 field strength tensor term of the Lagrangian. This leads to the phenomena of color 181 confinement, which describes how one only observes color-neutral particles alone in 182 nature. In contrast to the electromagnetic force, particles which interact via the 183 strong force experience a *greater* force as the distance between the particles increases. 184 At long distances, the potential is given by V(r) = -kr. At some point, it is more 185 energetically favorable to create additional partons out of the vacuum than continue 186 pulling apart the existing partons, and the colored particles undergo fragmentation. 187 This leads to hadronization. Bare quarks and gluons are actually observed as sprays 188 of hadrons (primarly kaons and pions); these sprays are known as jets, which are 189 what are observed by experiments. 190

It is important to recognize the importance of understanding these QCD interactions in high-energy hadron colliders such as the LHC. Since protons are hadrons, proton-proton collisions such as those produced by the LHC are primarily governed by the processes of QCD. In particular, by far the most frequent process observed in LHC experiments is dijet production from gluon-gluon interactions (see Fig.2.2). These

Standard Model Production Cross Section Measurements Status: August 2016 σ [pb] **ATLAS** Preliminary Theory $\sqrt{s} = 7, 8, 13 \text{ TeV}$ Run 1,2 10⁶ 10⁵ *p*_T > 25 GeV Data 20.3 fb-1 10^{4} LHC pp $\sqrt{s} = 13 \text{ TeV}$ 10^{3} Data 0.08 - 14.8 fb 10^{2} 10^{1} 1 10- 10^{-2} 10^{-3}

w

fid.

fid.

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fid.

fid.

tot.

Figure 2.2: Cross-sections of various Standard Model processes

gluons that interact are part of the sea particles inside the proton; the simple p = uudmodel does not apply. The main valence uud quarks are constantly interacting via gluons, which can themselves radiate gluons or split into quarks, and so on. A more useful understanding is given by the colloquially-known $baq \mod [51, 52]$, where the proton is seen as a "bag" of (in principle) infinitely many partons, each with energy $E < \sqrt{s} = 6.5$ TeV. One then collides this (proton) bag with another, and views the products of this very complicated collision, where calculations include many loops in nonpertubative QCD calculations.

tot.

fid. fid. ttWttZ tty Zjj ww Zyy Wyy VVjj tot. tot. fid. fid. tot. fid. fid. fid. fid.

tot. tot. fid. fid.

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Fortunately, we are generally saved by the QCD factorization theorems [53]. This 204 allows one to understand the hard (i.e. short distance or high energy) $2 \rightarrow 2$ parton 205 process using the tools of perturbative QCD, while making series of approximations 206 known as a parton shower model to understand the additional corrections from 207 nonpertubative QCD. We will discuss the reconstruction of jets by experiments in 208 Ch.5. 209

210 Fermions

We will now look more closely at the fermions in the Standard Model [54].

As noted earlier in Sec.2.2, the fermions of the Standard Model can be first distinguished between those that interact via the strong force (quarks) and those which do not (leptons).

There are six leptons in the Standard Model, which can be placed into three generations.

 $\begin{pmatrix} e \\ \nu_e \end{pmatrix}, \begin{pmatrix} \mu \\ \nu_{\mu} \end{pmatrix}, \begin{pmatrix} \tau \\ \nu_{\tau} \end{pmatrix}$ (2.14)

There is the electron (e), muon (μ) , and tau (τ) , each of which has an associated neutrino $(\nu_e, \nu_\mu, \nu_\tau)$. Each of the so-called charged ("electron-like") leptons has electromagnetic charge -1, while the neutrinos all have $q_{EM}=0$.

Often in an experimental context, lepton is used to denote the stable electron and metastable muon, due to their striking experimental signatures. Taus are often treated separately, due to their much shorter lifetime of $\tau_{\tau} \sim 10^{-13} s$; these decay through hadrons or the other leptons, so often physics analyses at the LHC treat them as jets or leptons, as will be done in this thesis.

As the neutrinos are electrically neutral, nearly massless, and only interact via the weak force, it is quite difficult to observe them directly. Since LHC experiments rely overwhelmingly on electromagnetic interactions to observe particles, the presence of neutrinos is not observed directly. Neutrinos are instead observed by the conservation of four-momentum in the plane transverse to the proton-proton collisions, known as missing transverse energy.

There are six quarks in the Standard Model: up, down, charm, strange, top, and bottom. Quarks are similar organized into three generations:

$$\begin{pmatrix} u \\ d \end{pmatrix}, \begin{pmatrix} c \\ s \end{pmatrix}, \begin{pmatrix} t \\ b \end{pmatrix} \tag{2.15}$$

where we speak of "up-like" quarks and "down-like" quarks.

Each up-like quark has charge $q_{up} = 2/3$, while the down-like quarks have $q_{down} =$ 230 -1/3. At the high energies of the LHC, one often makes the distinction between 231 the light quarks (u, d, c, s), the bottom quark, and top quark. In general, due to 232 the hadronization process described above, the light quarks, with masses $m_q < \sim$ 233 1.5 GeV are indistinguishable by LHC experiments. Their hadronic decay products 234 generally have long lifetimes and they are reconstructed as jets.¹. The bottom quark 235 hadronizes primarly through the B-mesons, which generally travels a short distance 236 before decaying to other hadrons. This allows one to distinguish decays via b-quarks 237 form other jets; this procedure is known as b-tagging and will be discussed more in 238 Ch.5. Due to its large mass, the top quark decays before it can hadronize; there 239 are no bound states associated to the top quark. The top is of particular interest at 240 the LHC; it has a striking signature through its most common decay mode $t \to Wb$. Decays via tops, especially $t\bar{t}$ are frequently an important signal decay mode, or an 242 important background process. 243

244 Interactions in the Standard Model

We briefly overview the entirety of the fundamental interactions of the Standard Model; these can also be found in 2.3.

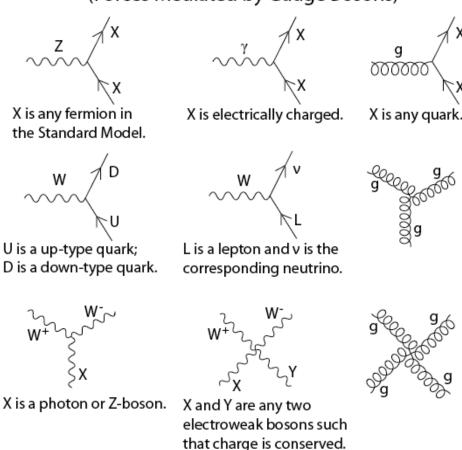
The electromagnetic force, mediated by the photon, interacts with via a threepoint coupling all charged particles in the Standard Model. The photon thus interacts with all the quarks, the charged leptons, and the charged W^{\pm} bosons.

The weak force is mediated by three particles: the W^{\pm} and the Z^0 . The Z^0 can interacts with all fermions via a three-point coupling. A real Z_0 can thus decay to a fermion-antifermion pair of all SM fermions except the top quark, due to its large

¹In some contexts, charm quarks are also treated as a separate category, although it is quite difficult to distinguish charm quarks from the other light quarks.

Figure 2.3: The interactions of the Standard Model

Standard Model Interactions (Forces Mediated by Gauge Bosons)



mass. The W^{\pm} has two important three-point interactions with fermions. First, the 253 W^{\pm} can interact with an up-like quark and a down-like quark; an important example 254 in LHC experiments is $t \to Wb$ The coupling constants for these interactions are 255 encoded in the unitary matrix known as the Cabibbo–Kobayashi–Maskawa (CKM) 256 matrix [55, 56], and are generally known as flavor-changing interactions. Secondly, 257 the W^{\pm} interacts with a charged lepton and its corresponding neutrino. In this case, 258 the unitary matrix that corresponds to CKM matrix for quarks is the identity matrix, 259 which forbids (fundamental) vertices such as $\mu \to We$. For leptons, instead this is 260 a two-step process: $\mu \to \nu_m uW \to \nu_m u\bar{\nu_e}e$. Finally, there are the self-interactions 261

of the weak gauge bosons. There is a three-point and four-point interaction; all combinations are allowed which conserve electric charge.

The strong force is mediated by the gluon, which as discussed above also carries the strong color charge. There is the fundamental three-point interaction, where a quark radiates a gluon. Additionally, there are the three-point and four-point gluon-only interactions.

268 2.3 Deficiencies of the Standard Model

At this point, it is quite easy to simply rest on our laurels. This relatively simple theory is capable of explaining a very wide range of phenomenom, which ultimately break down only to combinations of nine diagrams shown in Fig.2.3. Unfortunately, there are some unexplained problems with the Standard Model. We cannot go through all of the potential issues in this thesis, but we will motivate the primary issues which naturally lead one to *supersymmetry*, as we will see in Ch.3.

The Standard Model has many free parameters; see Table 2.1 In general, we prefer models with less free parameters. A great example of this fact, and the primary experimental evidence for EWSB, is the relationship between the couplings of the weak force and the masses of the gauge bosons of the weak force:

$$\rho \equiv \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} \stackrel{?}{=} 1 \tag{2.16}$$

where ? indicates that this is a testable prediction of the Standard Model (in particular, that the gauge bosons gain mass through EWSB). This relationship has been measured within experimental and theoretical predictions. We would like to produce additional such relationships, which would exist if the Standard Model is a low-energy approximation of some other theory.

An additional issue is the lack of gauge coupling unification. The couplings of any quantum field theory "run" as a function of the distance scales (or inversely,

Table 2.1: Parameters of the Standard Model. For values dependent on the renormalization scheme, we use a combination of the on-shell normalization scheme [57–60] and modified minimal subtraction scheme with $m_{\bar{M}S}$ as indicated in the table [61]

[7]	M11 1 . V
	511 keV
Muon mass	105.7 MeV
Tau mass	1.78 GeV
Up quark mass	$1.9 \text{ MeV } (m_{\bar{MS}} = 2GeV)$
Down quark mass	$4.4 \text{ MeV } (m_{\bar{M}S} = 2GeV)$
Strange quark mass	87 MeV $(m_{\bar{M}S} = 2GeV)$
Charm quark mass	1.32 GeV $(m_{\bar{MS}} = m_c)$
Bottom quark mass	$4.24 \text{ GeV } (m_{\bar{M}S} = m_b)$
Top quark mass	172.7 GeV (on-shell renormalization)
12-mixing angle	13.1°
23-mixing angle	2.4°
13-mixing angle	0.2°
CP-violating Phase	0.995
U(1) gauge coupling	$0.357 \ (m_{\bar{M}S} = m_Z)$
SU(2) gauge coupling	$0.652 \ (m_{\bar{M}S} = m_Z)$
SU(3) gauge coupling	$1.221 \ (m_{\bar{M}S} = m_Z)$
QCD vacuum angle	~0
Higgs vacuum expectation value	$246~{\rm GeV}$
Higgs mass	$125~{ m GeV}$
	Tau mass Up quark mass Down quark mass Strange quark mass Charm quark mass Bottom quark mass Top quark mass 12-mixing angle 23-mixing angle 13-mixing angle CP-violating Phase U(1) gauge coupling SU(2) gauge coupling SU(3) gauge coupling QCD vacuum angle Higgs vacuum expectation value

energy scales) of the theory. The idea is closely related to the unification of the electromagnetic and weak forces at the so-called *electroweak scale* of O(100 GeV). One would hope this behavior was repeated between the electroweak forces and the strong force at some suitable energy scale. The Standard Model does automatically not exhibit this behavior, as we can see in Fig.2.4.

The most significant problem with the Standard Model is the hierarchy problem. In its most straightforward incarnation, the Higgs scalar field is subject to quantum corrections through loop diagrams, as shown in Fig.2.5. For demonstration, we use the contributions from the top quark, since the top quark has the largest Higgs Yukawa coupling due to its large mass. In general, we should expect these corrections to quadratically dependent on the scale of the ultraviolet physics, Λ . Briefly assume there is no new physics before the Planck scale of gravity, $\Lambda_{\rm Planck} = 10^{19}$ GeV. In this

Figure 2.4: The running of Standard Model gauge couplings. The Standard Model couplings do not unify at high energies, which indicates it cannot completely describe nature through the Planck scale.

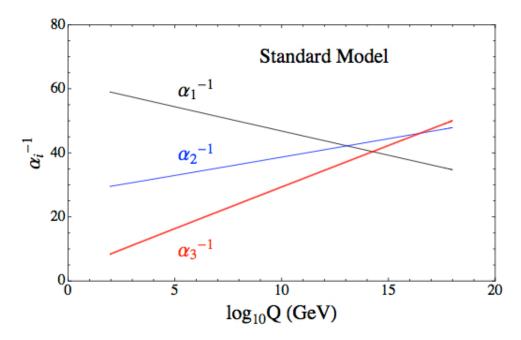
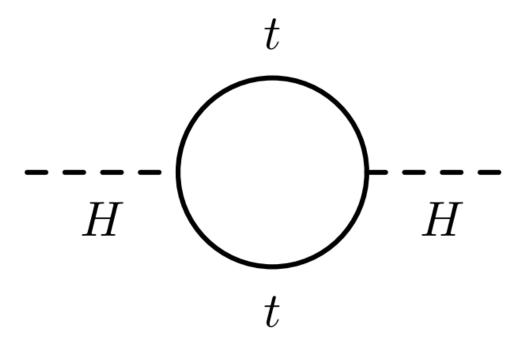


Figure 2.5: The dominant quantum loop correction to the Higgs mass in the Standard Model.



case, we expect the corrections to the Higgs mass like

$$\delta m_H^2 \approx \left(\frac{m_t}{8\pi^2 < \phi >_{VEV}}\right)^2 \Lambda_{Planck}^2.$$
 (2.17)

To achieve the miraculous cancellation required to get the observed Higgs mass of 125 GeV, one needs to then set the bare Higgs mass m_0 , our input to the Standard Model Lagrangian, itself to a *precise* value $\sim 10^{19}$ GeV. This extraordinary level of parameter finetuning is quite undesirable, and within the framework of the Standard Model, there is little that can be done to alleviate this issue.

An additional concern, of a different nature, is the lack of a dark matter candidate 292 in the Standard Model. Dark matter was discovered by observing galactic rotation 293 curves, which showed that much of the matter that interacted gravitionally was 294 invisible to our (electromagnetic) telescopes [16-22]. The postulation of the existence 295 of dark matter, which interacts at least through gravity, allows one to understand 296 these galatic rotation curves. Unfortunately, no particle in the Standard Model could 297 possibly be the dark matter particle. The only candidate truly worth another look is 298 the neutrino, but it has been shown that the neutrino content of the universe is simply 299 too small to explain the galatic rotation curves [22, 62]. The experimental evidence 300 from the galactic rotations curves thus show there must be additional physics beyond 301 the Standard Model, which is yet to be understood. 302

In the next chapter, we will see how these problems can be alleviated by the theory of supersymmetry.

mass → *2.3 MeV/ic² ~173.07 GeV/c² ≈126 GeV/ic² charge → 2/3 1/2 Higgs boson gluon up charm top =4.8 MeV/(c^x *4.18 GeWol QUARKS -103 1/2 1/2 1/2 down strange bottom photon 0.511 MeV/c* 91.2 GeWc* 1/2 1/2 Z boson electron tau muon <2.2 eV/c² <0.17 MeW/c² <15.5 MeV/c² 80.4 GeV/c² LEPTONS 1/2 electron neutrino muon neutrino tau neutrino W boson

Figure 2.6: Particles of the Standard Model

Chapter 3

305

306

Supersymmetry

- 307 Here you can write some introductory remarks about your chapter. I like to give each
- 308 sentence its own line.
- When you need a new paragraph, just skip an extra line.

310 3.1 Motivation

- Only Additional allowed Lorentz invariant symmetry
- 312 Dark Matter
- ³¹³ Cancellation of quadratic divergences in corrections to the
- Higgs Mass
- 315 3.2 Supersymmetry
- 316 3.3 Additional particle content
- 3.4 Phenomenology
- 318 R parity Consequences for sq/gl decays

Chapter 4

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The Large Hadron Collider

- 321 Here you can write some introductory remarks about your chapter. I like to give each
- 322 sentence its own line.
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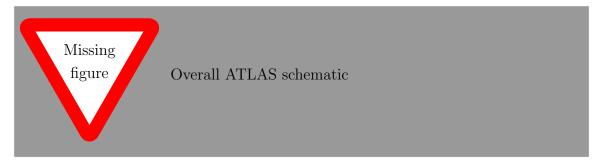
324 4.1 Magnets

- 325 By using the asterisk to start a new section, I keep the section from appearing in the
- 326 table of contents. If you want your sections to be numbered and to appear in the
- table of contents, remove the asterisk.

329

The ATLAS detector

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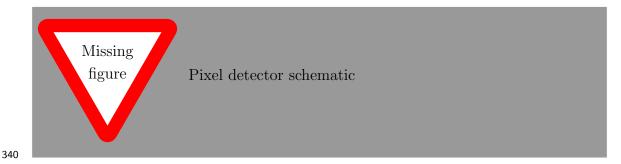
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5.1 Inner Detector

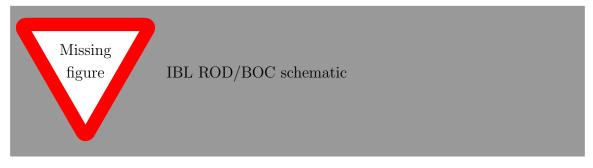
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- 337 table of contents. If you want your sections to be numbered and to appear in the
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Pixel Detector

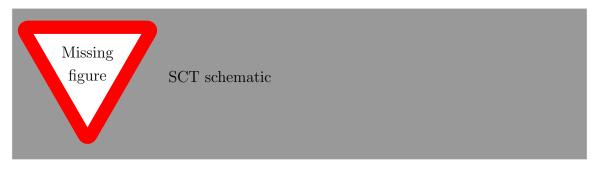


342 Insertable B-Layer

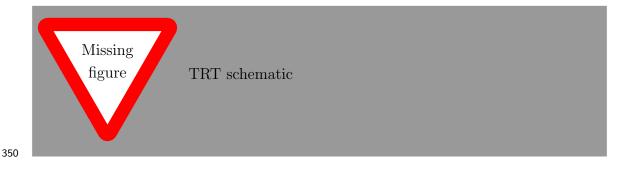
343 Qualification task, so add a bit more.



46 Semiconductor Tracker



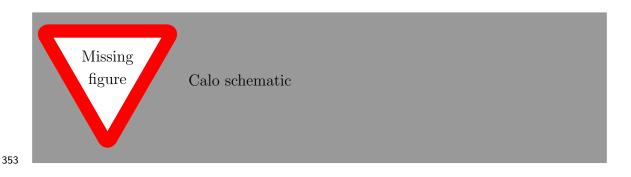
349 Transition Radiation Tracker



352 5.2 Calorimeter

351

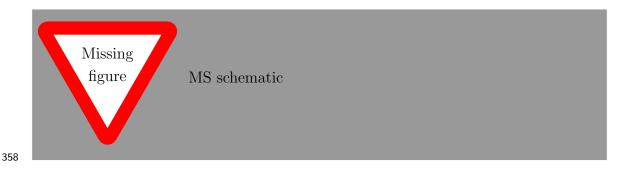
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355 Electromagnetic Calorimeter

356 Hadronic Calorimeter

357 5.3 Muon Spectrometer



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Chapter 6

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The Recursive Jigsaw Technique

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- 363 sentence its own line.
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Razor variables

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- table of contents. If you want your sections to be numbered and to appear in the
- table of contents, remove the asterisk.

369 6.2 SuperRazor variables

- 370 6.3 The Recursive Jigsaw Technique
- ³⁷¹ 6.4 Variables used in the search for zero lepton
- SUSY

373	Chapter 7
374	Title of Chapter 1

376

Title of Chapter 1

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8.1 Object reconstruction

³⁸¹ Photons, Muons, and Electrons

382 Jets

383 Missing transverse momentum

Probably longer, show some plots from the PUB note that we worked on

385 8.2 Signal regions

- 386 Gluino signal regions
- 387 Squark signal regions
- 388 Compressed signal regions

8.3 Background estimation

- 390 **Z** vv
- 391 **W** ev
- 392 ttbar

Chapter 9

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Title of Chapter 1

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396 sentence its own line.

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9.1 Statistical Analysis

399 maybe to be moved to an appendix

400 9.2 Signal Region distributions

- 9.3 Pull Plots
- 9.4 Systematic Uncertainties
- 9.5 Exclusion plots

Conclusion

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9.6 New Section

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410 table of contents. If you want your sections to be numbered and to appear in the

table of contents, remove the asterisk.

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The Standard Model

In this appendix, we provide a brief overview of the basic ingredients involved in construction of the Standard Model Lagrangian: quantum field theory, symmetries, and symmetry breaking.

Quantum Field Theory

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In this section, we provide a brief overview of the necessary concepts from lectures

Quantum Field Theory (QFT).

In modern physics, the laws of nature are described by the "action" S, with the imposition of the principle of minimum action. The action is the integral over the spacetime coordinates of the "Lagrangian density" \mathcal{L} , or Lagrangian for short. The Lagrangian is a function of "fields"; general fields will be called $\phi(x^{\mu})$, where the

indices μ run over the space-time coordinates. We can then write the action S as

$$S = \int d^4x \mathcal{L}[\phi_i(x^\mu), \partial_\mu \phi_i(x^\mu)]$$
 (9.1)

somehow

where we have an additional summation over i (of the different fields). Generally, we impose the following constraints on the Lagrangian:

- 591 1. Translational invariance The Lagrangian is only a function of the fields ϕ and their derivatives $\partial_{\mu}\phi$
- 2. Locality The Lagrangian is only a function of one point x_{μ} in spacetime.

- 3. Reality condition The Lagrangian is real to conserve probability.
- 595 4. Lorentz invariance The Lagrangian is invariant under the Poincarégroup of 596 spacetime.
- 59. Analyticity The Lagrangian is an analytical function of the fields; this is to allow the use of pertubation theory.
- 6. Invariance and Naturalness The Lagrangian is invariant under some internal symmetry groups; in fact, the Lagrangian will have *all* terms allowed by the imposed symmetry groups.

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- 7. Renormalizabilty The Lagrangian will be renormalizable in practice, this means there will not be terms with more than power 4 in the fields.
- The key item from the point of view of this thesis is that of "Invariance and Natural". We impose a set of "symmetries" and then our Lagragian is the most general which is allowed by those symmetries.

607 Symmetries

- 608 Symmetries can be seen as the fundamental guiding concept of modern physics.
- Symmetries are described by "groups". To illustrate the importance of symmetries
- and their mathematical description, groups, we start here with two of the simplest
- and most useful examples: \mathbb{Z}_2 and U(1).

612 \mathbb{Z}_2 symmetry

 \mathbb{Z}_2 symmetry is the simplest example of a "discrete" symmetry. Consider the most general Lagrangian of a single real scalar field $\phi(x_\mu)$

$$\mathcal{L}_{\phi} = \frac{1}{2} \partial_{\mu} \phi \partial^{\mu} \phi - \frac{m^2}{2} \phi^2 - \frac{\mu}{2\sqrt{2}} \phi^3 - \lambda \phi^4$$
 (9.2)

Now we *impose* the symmetry

$$\mathcal{L}(\phi) = \mathcal{L}(-\phi) \tag{9.3}$$

This has the effect of restricting the allowed terms of the Lagrangian. In particular, we can see the term $\phi^3 \to -\phi^3$ under the symmetry transformation, and thus must be disallowed by this symmetry. This means under the imposition of this particular symmetry, our Lagrangian should be rewritten as

$$\mathcal{L}_{\phi} = \frac{1}{2} \partial_{\mu} \phi \partial^{\mu} \phi - \frac{m^2}{2} \phi^2 - \lambda \phi^4 \tag{9.4}$$

The effect of this symmetry is that the total number of ϕ particles can only change by even numbers, since the only interaction term $\lambda \phi^4$ is an even power of the field. This symmetry is often imposed in supersymmetric theories, as we will see in Chapter 3.

U(1) symmetry

624 U(1) is the simplest example of a continuous (or Lie) group. Now consider a theory 625 with a single complex scalar field $\phi = \text{Re } \phi + i \text{Im } \phi$

$$\mathcal{L}_{\phi} = \delta_{i,j} \frac{1}{2} \partial_{\mu} \phi_i \partial^{\mu} \phi_j - \frac{m^2}{2} \phi_i \phi_j - \frac{\mu}{2\sqrt{2}} \phi_i \phi_j \phi_k - \lambda \phi_i \phi_j \phi_k \phi_l$$
 (9.5)

where i, j, k, l = Re, Im. In this case, we impose the following U(1) symmetry $\phi \mapsto e^{i\theta}, \phi^* \to e^{-i\theta}$. We see immediately that this again disallows the third-order terms, and we can write a theory of a complex scalar field with U(1) symmetry as

$$\mathcal{L}_{\phi} = \partial_{\mu}\phi \partial^{\mu}\phi^* - \frac{m^2}{2}\phi\phi^* - \lambda(\phi\phi^*)^2$$
(9.6)

629 Local symmetries

The two examples considered above are "global" symmetries in the sense that the symmetry transformation does not depends on the spacetime coordinate x_{μ} . We know look at local symmetries; in this case, for example with a local U(1) symmetry, the transformation has the form $\phi(x_{\mu}) \to e^{i\theta(x_m u)}\phi(x_{\mu})$. These symmetries are also known as "gauge" symmetries; all symmetries of the Standard Model are gauge symmetries.

There are wide-ranging consequences to the imposition of local symmetries. To begin, we note that the derivative terms of the Lagrangian 9.2 are *not* invariant under a local symmetry transformation

$$\partial_{\mu}\phi(x_{\mu}) \to \partial_{\mu}(e^{(i\theta(x_{\mu})\phi(x_{\mu}))} = (1 + i\theta(x_{\mu}))e^{(i\theta(x_{\mu})\phi(x_{\mu})}$$
(9.7)

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This leads us to note that the kinetic terms of the Lagrangian are also not invariant under a gauge symmetry. This would lead to a model with no dynamics, which is clearly unsatisfactory.

Let us take inspiration from the case of global symmetries. We need to define a so-called "covariant" derivative D^{μ} such that

$$D^{\mu}\phi \to e^{iq\theta(x^{\mu})D^{\mu}\phi} \tag{9.8}$$

$$D^{\mu}\phi^* \to e^{-iq\theta(x^{\mu})D^{\mu}\phi} \tag{9.9}$$

(9.10)

Since ϕ and ϕ^* transforms with the opposite phase, this will lead the invariance of the Lagrangian under our local gauge transformation. This D^{μ} is of the following form

$$D^{\mu} = \partial_{\mu} - igqA^{\mu} \tag{9.11}$$

where A^{μ} is a vector field we introduce with the transformation law

$$A^{\mu} \to A^{\mu} - \frac{1}{q} \partial_{\mu} \theta \tag{9.12}$$

and g is the coupling constant associated to vector field. This vector field A^{μ} is also known as a "gauge" field.

Since we need to add all allowed terms to the Lagrangian, we define

$$F^{\mu\nu} = A^{\mu}A^{\nu} - A^{\nu}A^{\mu} \tag{9.13}$$

and then we must also add the kinetic term:

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$$\mathcal{L}_{\text{gauge}} = -\frac{1}{4} F^{\mu\nu} F_{\mu\nu} \tag{9.14}$$

The most general renormalizable Lagrangian with fermion and scalar fields can be written in the following form

$$\mathcal{L} = \mathcal{L}_{kin} + \mathcal{L}_{\phi} + \mathcal{L}_{\psi} + \mathcal{L}Yukawa \tag{9.15}$$

651 Symmetry breaking and the Higgs mechanism

Here we view some examples of symmetry breaking. We investigate breaking of a global U(1) symmetry and a local U(1) symmetry. The SM will break the electroweak symmetry SU(2)xU(1), and in Chapter 3 we will see how supersymmetry must also be broken.

There are two ideas of symmetry breaking

• Explicit symmetry breaking by a small parameter - in this case, we have a small parameter which breaks an "approximate" symmetry of our Lagrangian. An example would be the theory of the single scalar field 9.2, when $\mu \ll m^2$ and

660 $\mu << \lambda$. In this case, we can often ignore the small term when considering low-energy processes.

• Spontaneous symmetry breaking (SSB) - spontaneous symmetry breaking occurs when the Lagrangian is symmetric with respect to a given symmetry transformation, but the ground state of the theory is *not* symmetric with respect to that transformation. This can have some fascintating consequences, as we will see in the following examples

667 Symmetry breaking a

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$_{668}$ U(1) global symmetry breaking

Consider the theory of a complex scalar field under the U(1) symmetry, or the transformation

$$\phi \to e^{i\theta} \phi$$
 (9.16)

The Lagrangian for this theory is

$$\mathcal{L} = \partial^{\mu} \phi^{\dagger} \partial_{\mu} \phi + \frac{\mu^{2}}{2} \phi^{\dagger} \phi + \frac{\lambda}{4} (\phi^{\dagger} \phi)^{2}$$
 (9.17)

Let us write this theory in terms of two scalar fields, h and ξ : $\phi = (h+i\xi)/\sqrt(2)$. The Lagrangian can then be written as

$$\mathcal{L} = \partial^{\mu} h \partial_{\mu} h + \partial^{\mu} \xi dm u \xi - \frac{\mu^{2}}{2} (h^{2} + \xi^{2}) - \frac{\lambda}{4} (h^{2} + \xi^{2})^{2}$$
 (9.18)

First, note that the theory is only stable when $\lambda > 0$. To understand the effect of SSB, we now enforce that $\mu^2 < 0$, and define $v^2 = -\mu^2/\lambda$. We can then write the scalar potential of this theory as:

$$V(\phi) = \lambda (\phi^{\dagger} \phi - v^2/2)^2 \tag{9.19}$$

Minimizing this equation with respect to ϕ , we can see that the "vacuum expectation value" of the theory is

$$2 < \phi^{\dagger} \phi > = < h^2 + \xi^2 > = v^2 \tag{9.20}$$

We now reach the "breaking" point of this procedure. In the (h, ξ) plane, the minima form a circle of radius v. We are free to choose any of these minima to expand our Lagrangian around; the physics is not affected by this choice. For convenience, choose $\langle h \rangle = v, \langle \xi^2 \rangle = 0$.

Now, let us define $h' = h - v, \xi' = \xi$ with VEVs $< h' >= 0, < \xi' >= 0$. We can then write our spontaneously broken Lagrangian in the form

$$\mathcal{L} = \frac{1}{2} \partial_{\mu} h' \partial^{\mu} h' + \frac{1}{2} \partial_{\mu} \xi' \partial^{\mu} \xi' - \lambda v^2 h'^2 - \lambda v h' (h'^2 + \xi'^2) - \lambda (h'^2 + \xi'^2)^2$$
 (9.21)