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A search for sparticles in zero lepton final states

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Russell W. Smith

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ABSTRACT

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A search for sparticles in zero lepton final states

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Russell W. Smith

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16 center, but the abstract itself should be written as a regular paragraph on the page,

17 and it should not have indentation. Just replace this text.

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Acknowledgements

Introduction

Particle physics is a remarkably successful field of scientific inquiry. The ability to precisely predict the properties of a exceedingly wide range of physical phenomena, such as the description of the cosmic microwave background [1, 2], the understanding of the anomalous magnetic dipole moment of the electron [3, 4], and the measurement of the number of weakly-interacting neutrino flavors [5] is truly amazing.

The theory that has allowed this range of predictions is the *Standard Model* of particle physics (SM). The Standard Model combines the electroweak theory of Glashow, Weinberg, and Salam [6–8] with the theory of the strong interactions, as first envisioned by Gell-Mann and Zweig [9, 10]. This quantum field theory (QFT) contains a tiny number of particles, whose interactions describe phenomena up to at least the TeV scale. These particles are manifestations of the fields of the Standard Model, after application of the Higgs Mechanism. The particle content of the SM consists only of the six quarks, the six leptons, the four gauge bosons, and the scalar Higgs boson.

Despite its impressive range of described phenomena, the Standard Model has some theoretical and experimental deficiencies. The SM contains 26 free parameters¹. It would be more theoretically pleasing to understand these free parameters in terms of a more fundamental theory. The major theoretical concern of the Standard Model, as it pertains to this thesis, is the *hierachy problem*[11–15]. The light mass

¹This is the Standard Model corrected to include neutrino masses. These parameters are the fermion masses (6 leptons, 6 quarks), CKM and PMNS mixing angles (8 angles, 2 CP-violating phases), W/Z/Higgs masses (3), the Higgs field expectation value, and the couplings of the strong, weak, and electromagnetic forces (3 α_{force}) .

84 of the Higgs boson (125 GeV) should be quadratically dependent on the scale of UV
 85 physics, due to the quantum corrections from high-energy physics processes. The
 86 most perplexing experimental issue is the existence of *dark matter*, as demonstrated
 87 by galactic rotation curves [16–22]. This data has shown that there exists additional
 88 matter which has not yet been seen interacting with the particles of the Standard
 89 Model. There is no particle in the SM which can act as a candidate for dark matter.

90 Both of these major issues, as well as numerous others, can be solved by the
 91 introduction of *supersymmetry* (SUSY) [15, 23–33]. In supersymmetric theories, each
 92 SM particles has a so-called *superpartner*, or sparticle partner, differing from given SM
 93 particle by 1/2 in spin. These theories solve the hierachy problem, since the quantum
 94 corrections induced from the superpartners exactly cancel those induced by the SM
 95 particles. In addition, these theories are usually constructed assuming R -parity,
 96 which can be thought of as the “charge” of supersymmetry, with SM particles having
 97 $R = 1$ and sparticles having $R = -1$. In collider experiments, since the incoming
 98 SM particles have total $R = 1$, the resulting sparticles are produced in pairs. This
 99 produces a rich phenomenology, which is characterized by significant hadronic activity
 100 and large missing transverse energy (E_T^{miss}), which provide significant discrimination
 101 against SM backgrounds [34].

102 Despite the power of searches for supersymmetry where E_T^{miss} is a primary
 103 discriminating variable, there has been significant interest in the use of other variables
 104 to discriminate against SM backgrounds. These include searches employing variables
 105 such as αT , $M_{T,2}$, and the razor variables (M_R, R^2) [35–45]. In this thesis, we
 106 will present the first search for supersymmetry using the novel Recursive Jigsaw
 107 Reconstruction (RJR) technique. RJR can be considered the conceptual successor
 108 of the razor variables. We impose a particular final state “decay tree” on an events,
 109 which roughly corresponds to a simplified Feynmann diagram in decays containing
 110 weakly-interacting particles. We account for the missing degrees of freedom associated

111 to the weakly-interacting particles by a series of simplifying assumptions, which allow
112 us to calculate our variables of interest at each step in the decay tree. This allows an
113 unprecedented understanding of the internal structure of the decay and the ability to
114 construct additional variables to reject Standard Model backgrounds.

115 This thesis details a search for the superpartners of the gluon and quarks, the
116 gluino and squarks, in final states with zero leptons, with 13.3 fb^{-1} of data using the
117 ATLAS detector. We organize the thesis as follows. The theoretical foundations of
118 the Standard Model and supersymmetry are described in Chapters 2 and 3. The
119 Large Hadron Collider and the ATLAS detector are presented in Chapters 4 and 5.
120 Chapter 5 provides a detailed description of Recursive Jigsaw Reconstruction and a
121 description of the variables used for the particular search presented in this thesis.
122 Chapter 6 presents the details of the analysis, including details of the dataset, object
123 reconstruction, and selections used. In Chapter 7, the final results are presented;
124 since there is no evidence of a supersymmetric signal in the analysis, we present the
125 final exclusion curves in simplified supersymmetric models.

The Standard Model

2.1 Overview

A Standard Model is another name for a theory of the internal symmetry group $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$, with its associated set of parameters. *The* Standard Model refers specifically to a Standard Model with the proper parameters to describe the universe. The SM is the culmination of years of work in both theoretical and experimental particle physics. In this thesis, we take the view that theorists construct a model with the field content and symmetries as inputs, and write down the most general Lagrangian consistent with those symmetries. Assuming this model is compatible with nature (in particular, the predictions of the model are consistent with previous experiments), experimentalists are responsible measuring the parameters of this model. This will be applicable for this chapter and the following one.

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Additional theoretical background is in [9.6](#).

2.2 Field Content

The Standard Model field content is

$$\begin{aligned}
 \text{Fermions} &: Q_L(3, 2)_{+1/3}, U_R(3, 1)_{+4/3}, D_R(3, 1)_{-2/3}, L_L(1, 2)_{-1}, E_R(1, 1)_{-2} \\
 \text{Scalar (Higgs)} &: \phi(1, 2)_{+1} \\
 \text{Vector Fields} &: G^\mu(8, 1)_0, W^\mu(1, 3)_0, B^\mu(1, 1)_0
 \end{aligned} \tag{2.1}$$

142 where the $(A, B)_Y$ notation represents the irreducible representation under $SU(3)$
 143 and $SU(2)$, with Y being the electroweak hypercharge. Each of these fermion fields
 144 has an additional index, representing the three generation of fermions.

145 We observed that Q_L, U_R , and D_R are triplets under $SU(3)_C$; these are the *quark*
 146 fields. The *color* group, $SU(3)_C$ is mediated by the *gluon* field $G^\mu(8, 1)_0$, which has
 147 8 degrees of freedom. The fermion fields $L_L(1, 2)_{-1}$ and $E_R(1, 1)_{-2}$ are singlets under
 148 $SU(3)_C$; we call them the *lepton* fields.

149 Next, we note the “left-handed” (“right-handed”) fermion fields, denoted by L (R)
 150 subscript, The left-handed fields form doublets under $SU(2)_L$. These are mediated
 151 by the three degrees of freedom of the “W” fields $W^\mu(1, 3)_0$. These fields only act
 152 on the left-handed particles of the Standard Model. This is the reflection of the
 153 “chirality” of the Standard Model; the left-handed and right-handed particles are
 154 treated differently by the electroweak forces. The right-handed fields, U_R, D_R , and
 155 E_R , are singlets under $SU(2)_L$.

156 The $U(1)_Y$ symmetry is associated to the $B^\mu(1, 1)_0$ boson with one degree of
 157 freedom. The charge Y is known as the electroweak hypercharge.

158 To better understand the phenomenology of the Standard Model, let us investigate
 159 each of the *sectors* of the Standard Model separately.

160 Electroweak sector

The electroweak sector refers to the $SU(2)_L \otimes U(1)_Y$ portion of the Standard
 Model gauge group. Following our philosophy of writing all gauge-invariant and
 renormalizable terms, the electroweak Lagrangian can be written as

$$\mathcal{L} = W_a^{\mu\nu} W_{\mu\nu}^a + B^{\mu\nu} B_{\mu\nu} + (D^\mu \phi)^\dagger D_\mu \phi - \mu^2 \phi^\dagger \phi - \lambda(\phi^\dagger \phi)^2. \quad (2.2)$$

where $W_a^{\mu\nu}$ are the three ($a = 1, 2, 3$) gauge bosons associated to the $SU(2)_L$ gauge
 group, $B^{\mu\nu}$ is the one gauge boson of the $U(1)_Y$ gauge group, and ϕ is the complex

Higgs multiplet. The covariant derivative D^μ is given by

$$D^\mu = \partial^\mu + \frac{ig}{2}W_a^\mu\sigma_a + \frac{ig'}{2}B^\mu \quad (2.3)$$

where $i\sigma_a$ are the Pauli matrices times the imaginary constant, which are the generators for $SU(2)_L$, and g and g' are the $SU(2)_L$ and $U(1)_Y$ coupling constants, respectively. The field strength tensors $W_a^{\mu\nu}$ and $B^{\mu\nu}$ are given by the commutator of the covariant derivative associated to each field

$$B^{\mu\nu} = \partial^\mu B^\nu - \partial^\nu B^\mu \quad (2.4)$$

$$W_a^{\mu\nu} = \partial^\mu W_a^\nu - \partial^\nu W_a^\mu - g\epsilon_{abc}W_b^\mu W_c^\nu, \quad i = 1, 2, 3$$

161

162 The terms in the Lagrangian 2.2 proportional to μ^2 and λ make up the “Higgs
163 potential” [46]. As normal (see Appendix 9.6), we restrict $\lambda > 0$ to guarantee our
164 potential is bounded from below, and we also require $\mu^2 < 0$, which gives us the
165 standard “sombbrero” potential shown in 2.1.

This potential has infinitely many minima at $\langle \phi \rangle = \sqrt{2m/\lambda}$; the ground state is *spontaneously* broken by the choice of ground state, which induces a vacuum expectation value (VEV). Without loss of generality, we can choose the Higgs field ϕ to point in the real direction, and write the Higgs field ϕ in the following form :

$$\phi = \frac{1}{\sqrt{2}} \exp\left(\frac{i}{v}\sigma_a\theta_a\right) \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}. \quad (2.5)$$

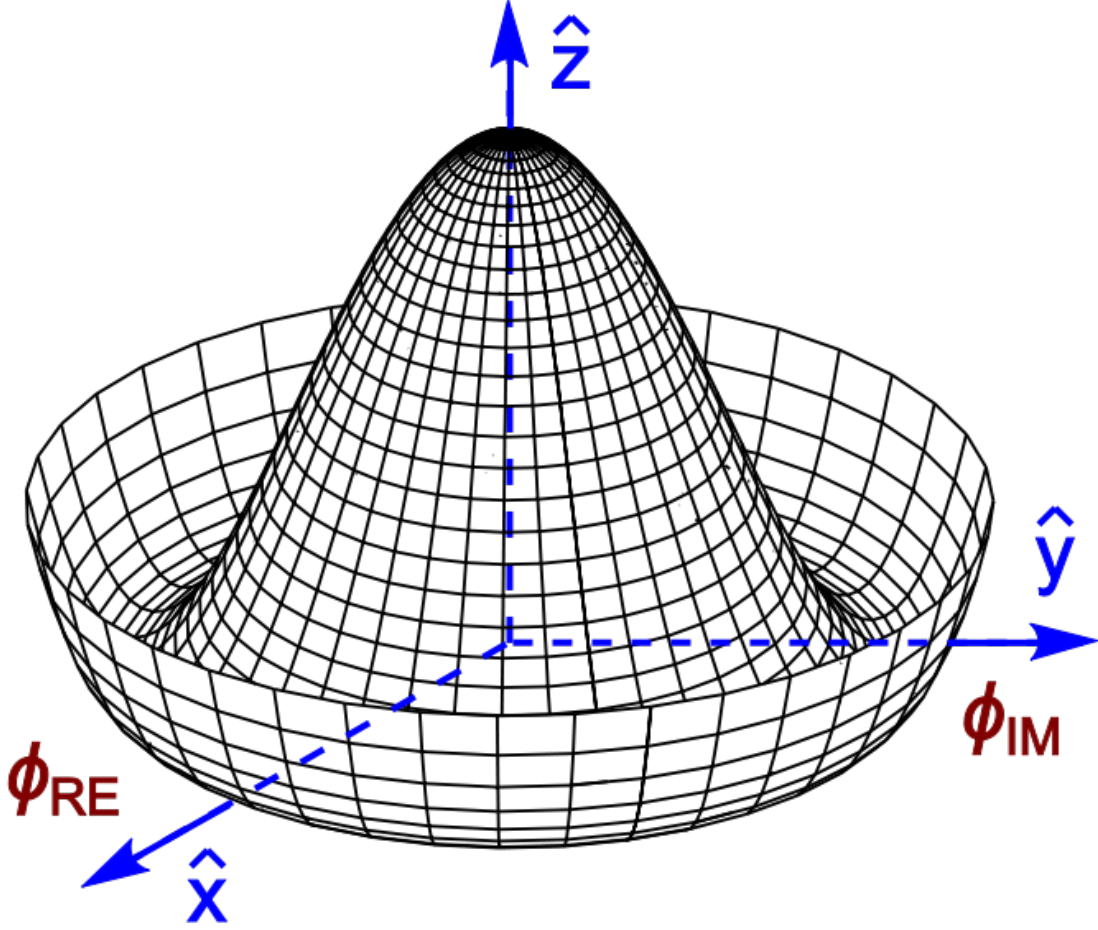
We choose a gauge to rotate away the dependence on θ_a , such that we can write simply

$$\phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}. \quad (2.6)$$

Now, we can see how the masses of the vector bosons are generated from the application of the Higgs mechanism. We plug Eq.2.6 back into the electroweak

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Figure 2.1: Sombrero potential



Lagrangian, and only showing the relevant mass terms in the vacuum state where $h(x) = 0$ see that (dropping the Lorentz indices) :

$$\begin{aligned} \mathcal{L}_M &= \frac{1}{8} \left| \begin{pmatrix} gW_3 + g'B & g(W_1 - iW_2) \\ g(W_1 + iW_2) & -gW_3 + g'B \end{pmatrix} \begin{pmatrix} 0 \\ v \end{pmatrix} \right|^2 \\ &= \frac{g^2 v^2}{8} \left[W_1^2 + W_2^2 + \left(\frac{g'}{g} B - W_3 \right)^2 \right] \end{aligned} \quad (2.7)$$

Defining the *Weinberg* angle $\tan(\theta_W) = g'/g$ and the following *physical* fields :

$$W^\pm = \frac{1}{\sqrt{2}}(W_1 \mp iW_2) \quad (2.8)$$

$$Z^0 = \cos \theta_W W_3 - \sin \theta_W B$$

$$A^0 = \sin \theta_W W_3 + \cos \theta_W B$$

we can write the piece of the Lagrangian associated to the vector boson masses as

$$\mathcal{L}_{M_V} = \frac{1}{4}g^2v^2W^+W^- + \frac{1}{8}(g^2 + g'^2)v^2Z^0Z^0. \quad (2.9)$$

and we have the following values of the masses for the vector bosons :

$$m_W^2 = \frac{1}{4}v^2g^2 \quad (2.10)$$

$$m_Z^2 = \frac{1}{4}v^2(g^2 + g'^2)$$

$$m_A^2 = 0$$

166 We thus see how the Higgs mechanism gives rise to the masses of the W^\pm and Z
 167 boson in the Standard Model; the mass of the photon is zero, as expected. The
 168 $SU(2)_L \otimes U(1)_Y$ symmetry of the initially massless $W_{1,2,3}$ and B fields is broken to
 169 the $U(1)_{EM}$. Of the four degrees of freedom in the complex Higgs doublet, three are
 170 “eaten” when we give mass to the W^\pm and Z_0 , while the other degree of freedom is
 171 the Higgs particle, as found in 2012 by the ATLAS and CMS collaborations [47, 48].

172 Quantum Chromodynamics

Quantum chromodynamics (or the theory of the *strong* force) characterizes the behavior of *colored* particles, collectively known as *partons*. The partons of the Standard Model are the (fermionic) quarks, and the (bosonic) gluons. The strong force is governed by $SU(3)_C$, an unbroken symmetry in the Standard Model, which implies the gluon remains massless. Defining the covariant derivative for QCD as

$$D^\mu = \partial^\mu + ig_s G_a^\mu L_a, a = 1, \dots, 8 \quad (2.11)$$

where L_a are the generators of $SU(3)_C$, and g_s is the coupling constant of the strong force. The QCD Lagrangian then is given by

$$\mathcal{L}_{\text{QCD}} = i\bar{\psi}_f D_\mu \gamma^\mu \psi_f - \frac{1}{4} G_{a,\mu\nu} G_a^{\mu\nu} \quad (2.12)$$

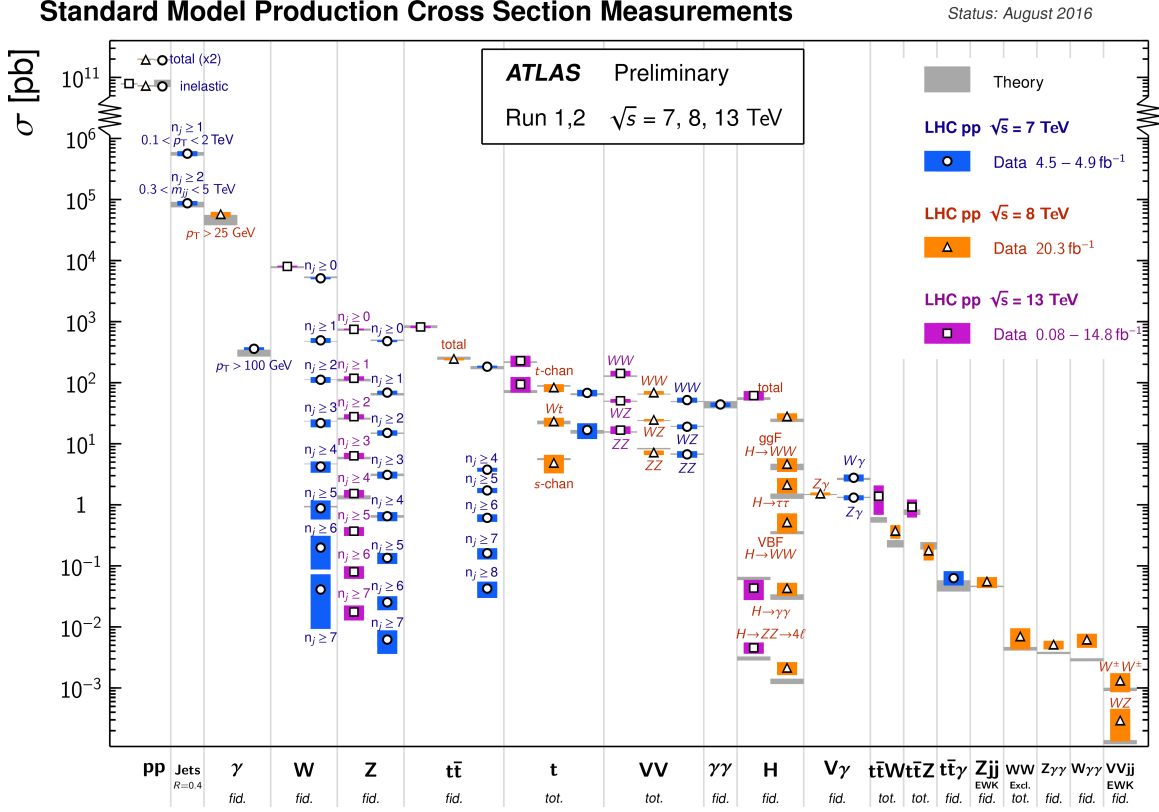
where the summation over f is for quarks *families*, and $G_a^{\mu\nu}$ is the gluon field strength tensor, given by

$$G_a^{\mu\nu} = \partial^\mu G_a^\nu - \partial^\nu G_a^\mu - g_s f^{abc} G_b^\mu G_c^\nu, a, b, c = 1, \dots, 8 \quad (2.13)$$

173 where f^{abc} are the structure constants of $SU(3)_C$, which are analogous to ϵ_{abc} for
 174 $SU(2)_L$. The kinetic term for the quarks is contained in the standard ∂_μ term, while
 175 the field strength term contains the interactions between the quarks and gluons, as
 176 well as the gluon self-interactions.

177 Written down in this simple form, the QCD Lagrangian does not seem much
 178 different from the QED Lagrangian, with the proper adjustments for the different
 179 group structures. The gluon is massless, like the photon, so one could naïvely expect
 180 an infinite range force, and it pays to understand why this is not the case. The
 181 reason for this fundamental difference is the gluon self-interactions arising in the
 182 field strength tensor term of the Lagrangian. This leads to the phenomena of *color*
 183 *confinement*, which describes how one only observes color-neutral particles alone in
 184 nature. In contrast to the electromagnetic force, particles which interact via the
 185 strong force experience a *greater* force as the distance between the particles increases.
 186 At long distances, the potential is given by $V(r) = -kr$. At some point, it is more
 187 energetically favorable to create additional partons out of the vacuum than continue
 188 pulling apart the existing partons, and the colored particles undergo *fragmentation*.
 189 This leads to *hadronization*. Bare quarks and gluons are actually observed as sprays
 190 of hadrons (primarily kaons and pions); these sprays are known as *jets*, which are
 191 what are observed by experiments.

Figure 2.2: Cross-sections of various Standard Model processes



192 It is important to recognize the importance of understanding these QCD inter-
 193 actions in high-energy hadron colliders such as the LHC. Since protons are hadrons,
 194 proton-proton collisions such as those produced by the LHC are primarily governed by
 195 the processes of QCD. In particular, by far the most frequent process observed in LHC
 196 experiments is dijet production from gluon-gluon interactions (see Fig.2.2). These
 197 gluons that interact are part of the *sea* particles inside the proton; the simple $p = uud$
 198 model does not apply. The main *valence* uud quarks are constantly interacting via
 199 gluons, which can themselves radiate gluons or split into quarks, and so on. A more
 200 useful understanding is given by the colloquially-known *bag* model [49, 50], where the
 201 proton is seen as a “bag” of (in principle) infinitely many partons, each with energy
 202 $E < \sqrt{s} = 6.5$ TeV. One then collides this (proton) bag with another, and views the
 203 products of this very complicated collision, where calculations include many loops in
 204 nonperturbative QCD calculations.

205 Fortunately, we are generally saved by the QCD factorization theorems [51]. This
 206 allows one to understand the hard (i.e. short distance or high energy) $2 \rightarrow 2$ parton
 207 process using the tools of perturbative QCD, while making series of approximations
 208 known as a *parton shower* model to understand the additional corrections from
 209 nonperturbative QCD. We will discuss the reconstruction of jets by experiments in
 210 Ch.??.

211 Fermions

212 We will now look more closely at the fermions in the Standard Model.

213 As noted earlier with regards to the field content, the fermions of the Standard
 214 Model can be first distinguished between those that interact via the strong force
 215 (quarks) and those which do not (leptons).

216 There are six leptons in the Standard Model, which can be placed into three
 cite pdg 217 generations. There is the electron (e), muon (μ), and tau (τ), each of which has an
 probably 218 associated neutrino (ν_e, ν_μ, ν_τ). Each of the so-called charged (“electron-like”) leptons
 219 has electromagnetic charge -1 , while the neutrinos all have $q_{EM} = 0$.

220 Often in an experimental context, lepton is used to denote the electron (stable)
 221 and muon (metastable), due to their striking experimental signatures. Taus are often
 222 treated separately, due to their much shorter lifetime of τ_τ ; these decay through
 223 hadrons or the other leptons, so often physics analyses at the LHC treat them as jets
 224 or leptons, as will be done in this thesis.

225 As the neutrinos are electrically neutral, nearly massless, and only interact via the
 footnote? 226 weak force, it is quite difficult to observe them directly. Since LHC experiments rely
 227 overwhelmingly on electromagnetic interactions to observe particles, the presence of
 228 neutrinos is not observed directly. Neutrinos are instead observed by the conservation
 229 of four-momentum in the plane transverse to the proton-proton collisions, known as
 230 *missing transverse energy*.

There are six quarks in the Standard Model : up, down, charm, strange, top, and bottom. Quarks are similar organized into three generations :

$$\begin{pmatrix} u & d \end{pmatrix}, \begin{pmatrix} c & s \end{pmatrix}, \begin{pmatrix} t & b \end{pmatrix} \quad (2.14)$$

where we speak of “up-like” quarks and “down-like” quarks.

Each up-like quark has charge $q_{up} = 2/3$, while the down-like quarks have $q_{down} = -1/3$. At the high energies of the LHC, one often makes the distinction between the light quarks (u, d, c, s), the bottom quark, and top quark. In general, due to the hadronization process described above, the light quarks are indistinguishable by LHC experiments, and reconstructed as jets.. The bottom quark hadronizes primarily through a relatively long-lived particle known as the B (name), which generally travels a short distance before decay. This feature allows what is known as b -tagging; this will be further discussed in Ch. Due to its large mass, the top quark decays before it can hadronize; there are no bound states associated to the top quark. The top is of particular interest at the LHC; it has a striking signature with a large cross-section, which can be used to distinguish signal processes with decays to top quarks, or understand top production as a background process.

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Interactions in the Standard Model

We briefly overview the entirety of the fundamental interactions of the Standard Model; these can also be found in ??.

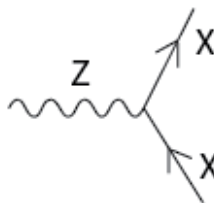
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The electromagnetic force, mediated by the photon, interacts with via a three-point coupling all charged particles in the Standard Model. The photon thus interacts with all the quarks, the charged leptons, and the charged W^\pm bosons.

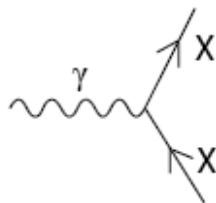
The weak force is mediated by three particles : the W^\pm and the Z^0 . The Z^0 can interacts with all fermions via a three-point coupling, governed by the coupling

Figure 2.3: The interactions of the Standard Model

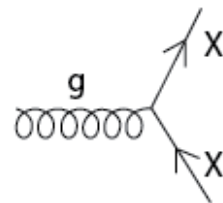
Standard Model Interactions (Forces Mediated by Gauge Bosons)



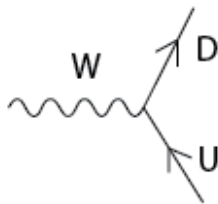
X is any fermion in the Standard Model.



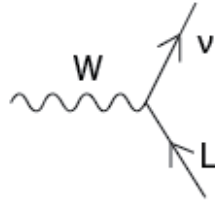
X is electrically charged.



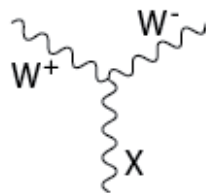
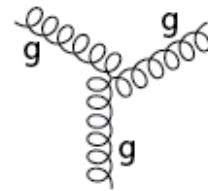
X is any quark.



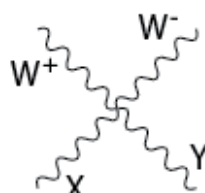
U is a up-type quark;
D is a down-type quark.



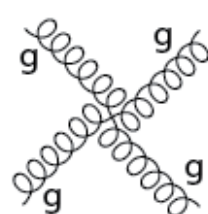
L is a lepton and ν is the corresponding neutrino.



X is a photon or Z-boson.



X and Y are any two electroweak bosons such that charge is conserved.



constant g' . A real Z_0 can thus decay to two of each fermion in the Standard Model except for the top quark, due to its large mass. The W^\pm has two important three-point interactions with fermions. First, the W^\pm can interact with an up-like quark and a down-like quark. The coupling constants for these interactions are encoded in the CKM matrix Secondly, the W^\pm interacts with a charged lepton and its corresponding neutrino. Finally, there are the self-interactions of the weak gauge bosons. There is a three-point and four-point interaction; all combinations are allowed which conserve electric charge.

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The strong force is mediated by the gluon, which as discussed above also carries the strong color charge. There is the fundamental three-point interaction, where a gluon interacts with any quark. Additionally, there are the gluon-only interactions, which occur in a three-point and four-point interaction.

2.3 Deficiencies of the Standard Model

At this point, it is quite easy to simply rest on our laurels. This relatively simple theory is capable of explaining a very wide range of phenomenom, which ultimately break down only to combinations of nine diagrams shown in Eq.???. Unfortunately, there are some unexplained problems with the Standard Model. We cannot go through all of the potential issues in this thesis, but we will motivate the primary issues which naturally lead one to *supersymmetry*, as we will see in Ch.??.

The Standard Model has many free paramaters , especially when corrected for neutrino masses. In general, we prefer models with less free parameters. A great example of this fact, and additionally some of the strongest experimental proof of EWSB, is the relationship between the couplings of the weak force and the masses of the gauge bosons of the weak force :

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$$\rho m_Z^2 \cos^2 \theta_W \stackrel{?}{=} 1 \quad (2.15)$$

where ? indicates that this is a testable prediction of the Standard Model (in particular, that the gauge bosons gain mass through EWSB). This relation has been shown to be true within experimental and theoretical predictions. We would like to produce additional such relationships, which would exist if the Standard Model is a low-energy approximation of some other theory.

An additional issue, although not strictly fundamental, is the lack of gauge coupling unification. The couplings of any quantum field theory “run” as a function of the distance scales (or inversely, energy scales) of the theory. The idea is closely related to the unification of the electromagnetic and weak forces at the so-called *electroweak scale* of $O(100 \text{ GeV})$. One would hope this behavior was repeated between the electroweak forces and the strong force at some suitable energy scale. The Standard Model does automatically not exhibit this behavior, without some

additional theoretical gymnastics.

The most significant problem with the Standard Model is the *hierarchy problem*. In its most straightforward incarnation, the Higgs scalar field is subject to quantum corrections through loop diagrams, as shown in Fig. For demonstration, we use the contributions from the top quark, since the top quark has the largest Higgs Yukawa coupling due to its large mass. In general, we should expect these corrections to quadratically dependent on the scale of the ultraviolet physics, Λ . Briefly assume there is no new physics before the scale of Planck scale of gravity, $\Lambda_{\text{Planck}} = 10^{19} \text{ GeV}$.

In this case, we expect the corrections to the Higgs mass like

$$\delta m_H^2 \approx \left(\frac{m_t}{8\pi^2 < \phi >_{VEV}} \right)^2 \Lambda_{\text{Planck}}^2. \quad (2.16)$$

To achieve the miraculous cancellation required to get the observed Higgs Mass of 125 GeV, one needs to then set the bare Higgs mass m_0 , our input to the Standard Model Lagrangian, itself to a *precise* value 10^{19} GeV . This extraordinary level of parameter finetuning is quite undesirable, and within the framework of the Standard Model, there is little that can be done to alleviate this issue.

290 An additional concern, of a different nature, is the lack of a *dark matter* candidate
291 in the Standard Model. Dark matter was discovered by observing galactic rotation
292 curves, which showed that much of the matter that interacted gravitationally was
293 invisible to our (electromagnetic) telescopes. The postulation of the existence of
294 dark matter, which interacts at least through gravity, allows one to understand these
295 galactic rotation curves. Unfortunately, no particle in the Standard Model *could*
296 be this dark matter particle. The only candidate truly worth another look is the
297 neutrino, but it has been shown that the neutrino content of the universe is simply
298 too small to explain the galactic rotation curves (maybe say more). The experimental
299 evidence from the galactic rotations curves thus show there *must* be additional physics
300 beyond the Standard Model, which is yet to be understood.

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show one

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arxiv?

301 In the next chapter, we will see how these problems can be alleviated by the theory
302 of supersymmetry.

303 2.4 Conclusions

304 The Standard Model is an extraordinary theory. It is a culmination of decades of
305 work in both theoretical and experimental physics. blah some more

306

Chapter 3

307

Supersymmetry

308 Here you can write some introductory remarks about your chapter. I like to give each
309 sentence its own line.

310 When you need a new paragraph, just skip an extra line.

311 **3.1 Motivation**

312 **Only Additional allowed Lorentz invariant symmetry**

313 **Dark Matter**

314 **Cancellation of quadratic divergences in corrections to the**

315 **Higgs Mass**

316 **3.2 Supersymmetry**

317 **3.3 Additional particle content**

318 **3.4 Phenomenology**

319 **R parity Consequences for sq/gl decays**

320

Chapter 4

321

The Large Hadron Collider

322 Here you can write some introductory remarks about your chapter. I like to give each
323 sentence its own line.

324 When you need a new paragraph, just skip an extra line.

325 **4.1 Magnets**

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327 table of contents. If you want your sections to be numbered and to appear in the
328 table of contents, remove the asterisk.

329

Chapter 5

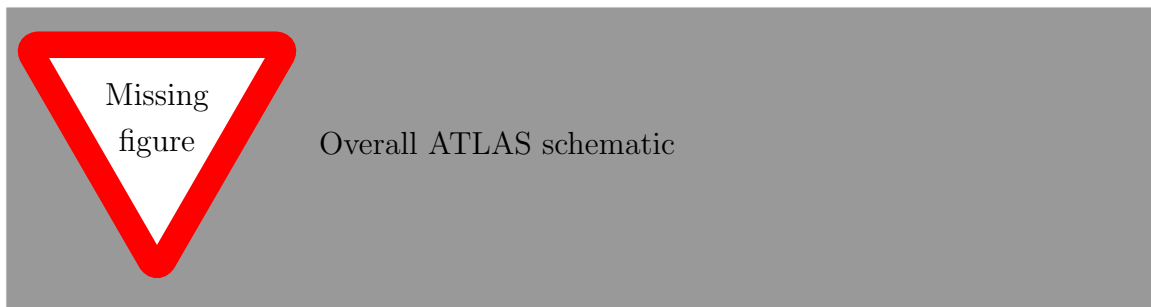
330

The ATLAS detector

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332 sentence its own line.

333 When you need a new paragraph, just skip an extra line.

334

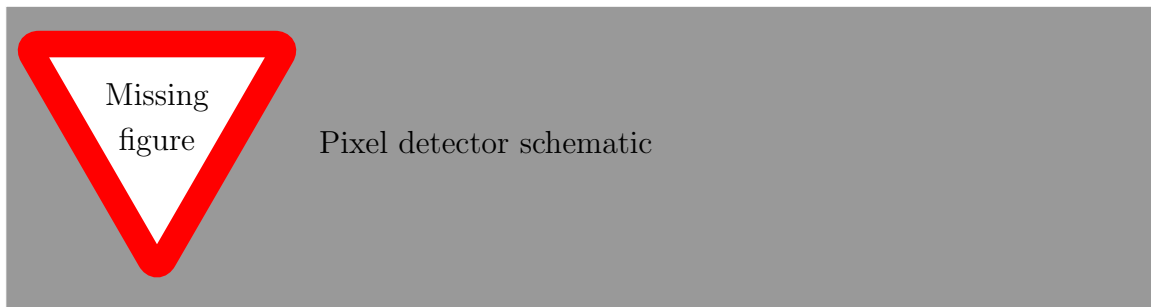


335

336 **5.1 Inner Detector**

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338 table of contents. If you want your sections to be numbered and to appear in the
339 table of contents, remove the asterisk.

340 **Pixel Detector**

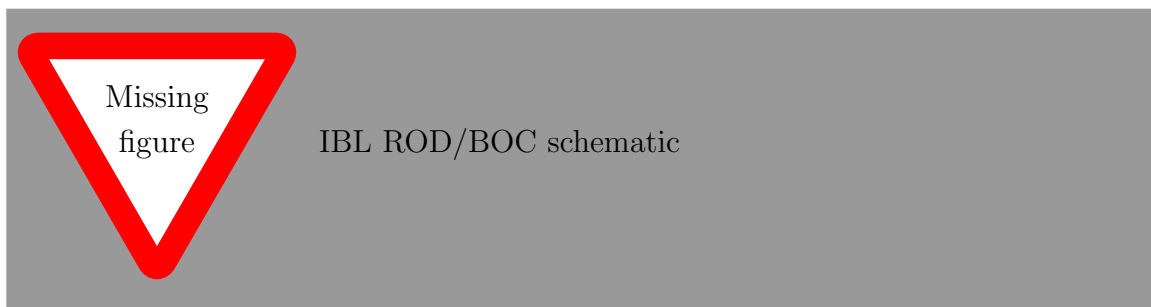


341

342

343 **Insertable B-Layer**

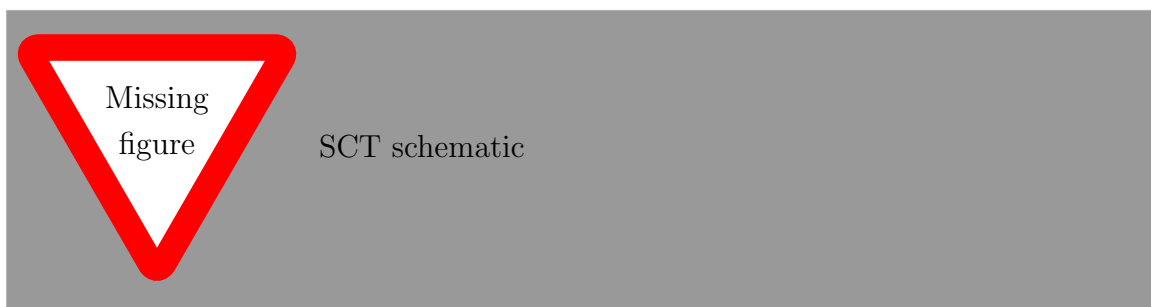
344 Qualification task, so add a bit more.



345

346

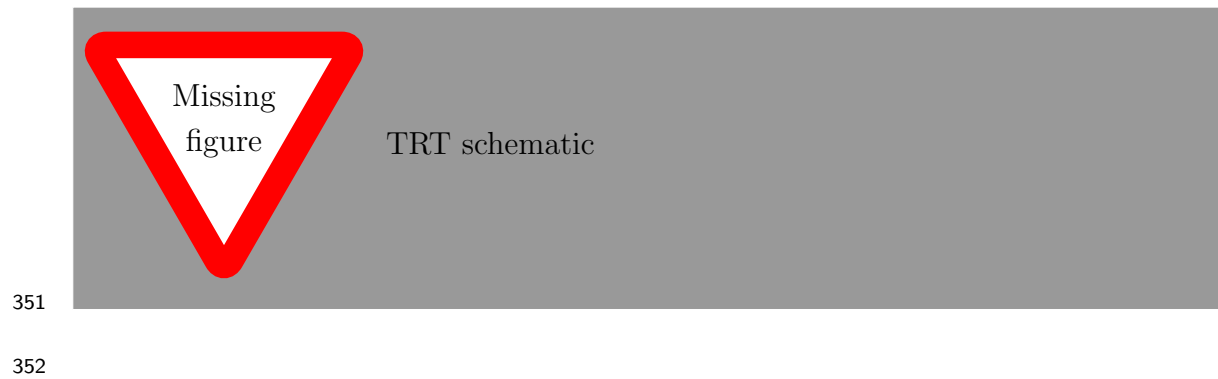
347 **Semiconductor Tracker**



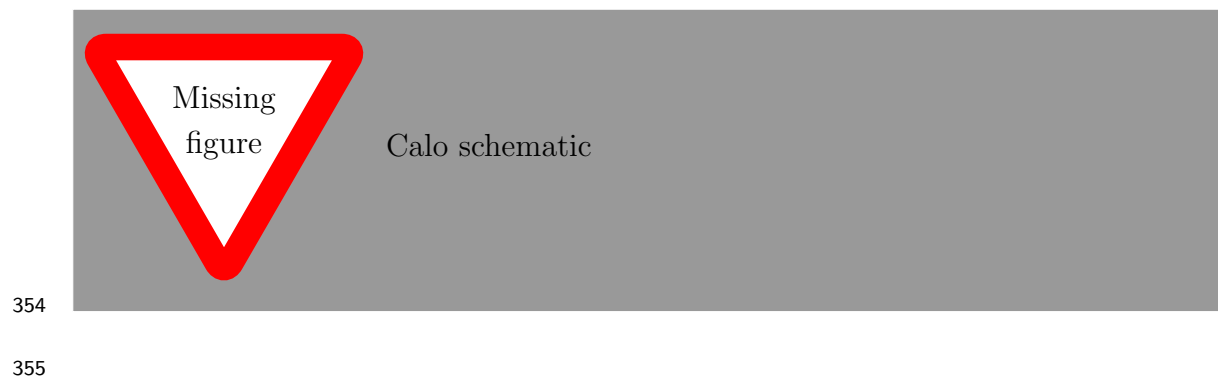
348

349

350 **Transition Radiation Tracker**



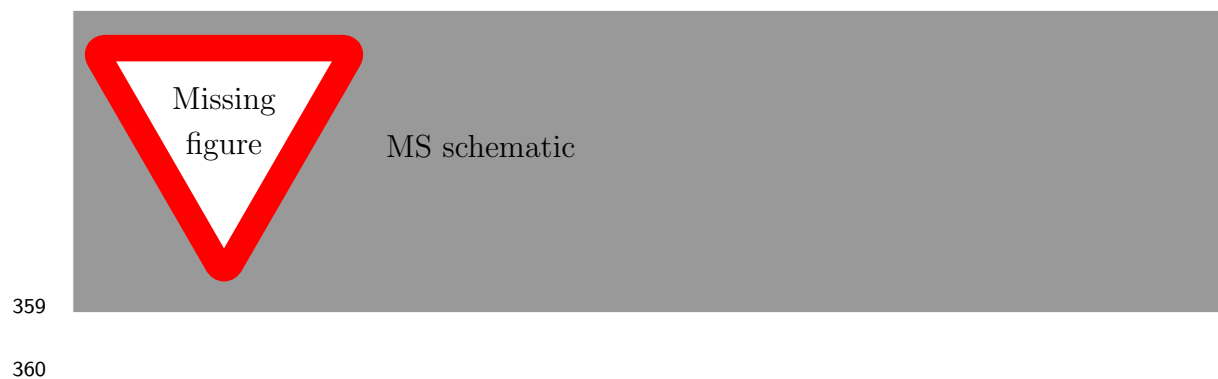
353 **5.2 Calorimeter**



356 **Electromagnetic Calorimeter**

357 **Hadronic Calorimeter**

358 **5.3 Muon Spectrometer**



361

Chapter 6

362

The Recursive Jigsaw Technique

363 Here you can write some introductory remarks about your chapter. I like to give each
364 sentence its own line.

365 When you need a new paragraph, just skip an extra line.

366 **6.1 Razor variables**

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368 table of contents. If you want your sections to be numbered and to appear in the
369 table of contents, remove the asterisk.

370 **6.2 SuperRazor variables**

371 **6.3 The Recursive Jigsaw Technique**

372 **6.4 Variables used in the search for zero lepton**

373 **SUSY**

Title of Chapter 1

376

Chapter 8

377

Title of Chapter 1

378 Here you can write some introductory remarks about your chapter. I like to give each
379 sentence its own line.

380 When you need a new paragraph, just skip an extra line.

381 **8.1 Object reconstruction**

382 **Photons, Muons, and Electrons**

383 **Jets**

384 **Missing transverse momentum**

385 Probably longer, show some plots from the PUB note that we worked on

386 **8.2 Signal regions**

387 **Gluino signal regions**

388 **Squark signal regions**

389 **Compressed signal regions**

390 **8.3 Background estimation**

391 **Z $\nu\nu$**

392 **W $e\nu$**

393 **$t\bar{t}$**

394

Chapter 9

395

Title of Chapter 1

396 Here you can write some introductory remarks about your chapter. I like to give each
397 sentence its own line.

398 When you need a new paragraph, just skip an extra line.

399 **9.1 Statistical Analysis**

400 maybe to be moved to an appendix

401 **9.2 Signal Region distributions**

402 **9.3 Pull Plots**

403 **9.4 Systematic Uncertainties**

404 **9.5 Exclusion plots**

405

Conclusion

406 Here you can write some introductory remarks about your chapter. I like to give each
407 sentence its own line.

408 When you need a new paragraph, just skip an extra line.

409 **9.6 New Section**

410 By using the asterisk to start a new section, I keep the section from appearing in the
411 table of contents. If you want your sections to be numbered and to appear in the
412 table of contents, remove the asterisk.

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The Standard Model

In this appendix, we provide a brief overview of the basic ingredients involved in construction of the Standard Model Lagrangian : quantum field theory, symmetries, and symmetry breaking.

Quantum Field Theory

In this section, we provide a brief overview of the necessary concepts from Quantum Field Theory (QFT).

In modern physics, the laws of nature are described by the “action” S , with the imposition of the principle of minimum action. The action is the integral over the spacetime coordinates of the “Lagrangian density” \mathcal{L} , or Lagrangian for short. The Lagrangian is a function of “fields”; general fields will be called $\phi(x^\mu)$, where the indices μ run over the space-time coordinates. We can then write the action S as

$$S = \int d^4x \mathcal{L}[\phi_i(x^\mu), \partial_\mu \phi_i(x^\mu)] \quad (9.1)$$

where we have an additional summation over i (of the different fields). Generally, we impose the following constraints on the Lagrangian :

1. Translational invariance - The Lagrangian is only a function of the fields ϕ and their derivatives $\partial_\mu \phi$
2. Locality - The Lagrangian is only a function of one point x_μ in spacetime.

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- 566 3. Reality condition - The Lagrangian is real to conserve probability.
- 567 4. Lorentz invariance - The Lagrangian is invariant under the Poincaré group of
568 spacetime.
- 569 5. Analyticity - The Lagrangian is an analytical function of the fields; this is to
570 allow the use of perturbation theory.
- 571 6. Invariance and Naturalness - The Lagrangian is invariant under some internal
572 symmetry groups; in fact, the Lagrangian will have *all* terms allowed by the
573 imposed symmetry groups.
- 574 7. Renormalizability - The Lagrangian will be renormalizable - in practice, this
575 means there will not be terms with more than power 4 in the fields.

576 The key item from the point of view of this thesis is that of “Invariance and
577 Natural”. We impose a set of “symmetries” and then our Lagrangian is the most
578 general which is allowed by those symmetries.

579 Symmetries

580 Symmetries can be seen as the fundamental guiding concept of modern physics.
581 Symmetries are described by “groups”. . To illustrate the importance of symmetries
582 and their mathematical description, groups, we start here with two of the simplest
583 and most useful examples : \mathbb{Z}_2 and $U(1)$.

584 \mathbb{Z}_2 symmetry

585 \mathbb{Z}_2 symmetry is the simplest example of a “discrete” symmetry. Consider the most
586 general Lagrangian of a single real scalar field $\phi(x_\mu)$

$$\mathcal{L}_\phi = \frac{1}{2}\partial_\mu\phi\partial^\mu\phi - \frac{m^2}{2}\phi^2 - \frac{\mu}{2\sqrt{2}}\phi^3 - \lambda\phi^4 \quad (9.2)$$

Now we *impose* the symmetry

$$\mathcal{L}(\phi) = \mathcal{L}(-\phi) \quad (9.3)$$

587 This has the effect of restricting the allowed terms of the Lagrangian. In particular,
 588 we can see the term $\phi^3 \rightarrow -\phi^3$ under the symmetry transformation, and thus must
 589 be disallowed by this symmetry. This means under the imposition of this particular
 590 symmetry, our Lagrangian should be rewritten as

$$\mathcal{L}_\phi = \frac{1}{2}\partial_\mu\phi\partial^\mu\phi - \frac{m^2}{2}\phi^2 - \lambda\phi^4 \quad (9.4)$$

591 The effect of this symmetry is that the total number of ϕ particles can only change
 592 by even numbers, since the only interaction term $\lambda\phi^4$ is an even power of the field.
 593 This symmetry is often imposed in supersymmetric theories, as we will see in Chapter
 594 3.

595 **$U(1)$ symmetry**

596 $U(1)$ is the simplest example of a continuous (or *Lie*) group. Now consider a theory
 597 with a single complex scalar field $\phi = \text{Re } \phi + i \text{Im } \phi$

$$\mathcal{L}_\phi = \delta_{i,j} \frac{1}{2} \partial_\mu \phi_i \partial^\mu \phi_j - \frac{m^2}{2} \phi_i \phi_j - \frac{\mu}{2\sqrt{2}} \phi_i \phi_j \phi_k - \lambda \phi_i \phi_j \phi_k \phi_l \quad (9.5)$$

598 where $i, j, k, l = \text{Re}, \text{Im}$. In this case, we impose the following $U(1)$ symmetry
 599 : $\phi \rightarrow e^{i\theta} \phi, \phi^* \rightarrow e^{-i\theta} \phi^*$. We see immediately that this again disallows the third-order
 600 terms, and we can write a theory of a complex scalar field with $U(1)$ symmetry as

$$\mathcal{L}_\phi = \partial_\mu \phi \partial^\mu \phi^* - \frac{m^2}{2} \phi \phi^* - \lambda (\phi \phi^*)^2 \quad (9.6)$$

601 Local symmetries

602 The two examples considered above are “global” symmetries in the sense that the
603 symmetry transformation does not depend on the spacetime coordinate x_μ . We know
604 look at local symmetries; in this case, for example with a local $U(1)$ symmetry, the
605 transformation has the form $\phi(x_\mu) \rightarrow e^{i\theta(x_\mu)}\phi(x_\mu)$. These symmetries are also known
606 as “gauge” symmetries; all symmetries of the Standard Model are gauge symmetries.

There are wide-ranging consequences to the imposition of local symmetries. To begin, we note that the derivative terms of the Lagrangian 9.2 are *not* invariant under a local symmetry transformation

$$\partial_\mu \phi(x_\mu) \rightarrow \partial_\mu (e^{i\theta(x_\mu)} \phi(x_\mu)) = (1 + i\partial_\mu \theta(x_\mu)) e^{i\theta(x_\mu)} \phi(x_\mu) \quad (9.7)$$

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This leads us to note that the kinetic terms of the Lagrangian are also not invariant
609 under a gauge symmetry. This would lead to a model with no dynamics, which is
610 clearly unsatisfactory.

611 Let us take inspiration from the case of global symmetries. We need to define a
612 so-called “covariant” derivative D^μ such that

$$D^\mu \phi \rightarrow e^{iq\theta(x_\mu)} D^\mu \phi \quad (9.8)$$

$$D^\mu \phi^* \rightarrow e^{-iq\theta(x_\mu)} D^\mu \phi^* \quad (9.9)$$

$$(9.10)$$

613 Since ϕ and ϕ^* transform with the opposite phase, this will lead to the invariance
614 of the Lagrangian under our local gauge transformation. This D^μ is of the following
615 form

$$D^\mu = \partial_\mu - igqA^\mu \quad (9.11)$$

616 where A^μ is a vector field we introduce with the transformation law

$$A^\mu \rightarrow A^\mu - \frac{1}{g} \partial_\mu \theta \quad (9.12)$$

617 and g is the coupling constant associated to vector field. This vector field A^μ is
618 also known as a “gauge” field.

619 Since we need to add all allowed terms to the Lagrangian, we define

$$F^{\mu\nu} = A^\mu A^\nu - A^\nu A^\mu \quad (9.13)$$

620 and then we must also add the kinetic term :

$$\mathcal{L}_{\text{gauge}} = -\frac{1}{4} F^{\mu\nu} F_{\mu\nu} \quad (9.14)$$

621 The most general renormalizable Lagrangian with fermion and scalar fields can
622 be written in the following form

$$\mathcal{L} = \mathcal{L}_{kin} + \mathcal{L}_\phi + \mathcal{L}_\psi + \mathcal{L}_{Yukawa} \quad (9.15)$$

623 Symmetry breaking and the Higgs mechanism

624 Here we view some examples of symmetry breaking. We investigate breaking of a
625 global $U(1)$ symmetry and a local $U(1)$ symmetry. The SM will break the electroweak
626 symmetry $SU(2) \times U(1)$, and in Chapter 3 we will see how supersymmetry must also
627 be broken.

628 There are two ideas of symmetry breaking

- 629 • Explicit symmetry breaking by a small parameter - in this case, we have a small
630 parameter which breaks an “approximate” symmetry of our Lagrangian. An
631 example would be the theory of the single scalar field [9.2](#), when $\mu \ll m^2$ and

632 $\mu \ll \lambda$. In this case, we can often ignore the small term when considering
633 low-energy processes.

634 • Spontaneous symmetry breaking (SSB) - spontaneous symmetry breaking
635 occurs when the Lagrangian is symmetric with respect to a given symmetry
636 transformation, but the ground state of the theory is *not* symmetric with respect
637 to that transformation. This can have some fascinating consequences, as we
638 will see in the following examples

639 Symmetry breaking a

640 **U(1) global symmetry breaking**

Consider the theory of a complex scalar field under the $U(1)$ symmetry, or the transformation

$$\phi \rightarrow e^{i\theta} \phi \quad (9.16)$$

The Lagrangian for this theory is

$$\mathcal{L} = \partial^\mu \phi^\dagger \partial_\mu \phi + \frac{\mu^2}{2} \phi^\dagger \phi + \frac{\lambda}{4} (\phi^\dagger \phi)^2 \quad (9.17)$$

Let us write this theory in terms of two scalar fields, h and ξ : $\phi = (h + i\xi)/\sqrt{2}$.

The Lagrangian can then be written as

$$\mathcal{L} = \partial^\mu h \partial_\mu h + \partial^\mu \xi \partial_\mu \xi - \frac{\mu^2}{2} (h^2 + \xi^2) - \frac{\lambda}{4} (h^2 + \xi^2)^2 \quad (9.18)$$

First, note that the theory is only stable when $\lambda > 0$. To understand the effect of SSB, we now enforce that $\mu^2 < 0$, and define $v^2 = -\mu^2/\lambda$. We can then write the scalar potential of this theory as :

$$V(\phi) = \lambda(\phi^\dagger \phi - v^2/2)^2 \quad (9.19)$$

Minimizing this equation with respect to ϕ , we can see that the “vacuum expectation value” of the theory is

$$2 \langle \phi^\dagger \phi \rangle = \langle h^2 + \xi^2 \rangle = v^2 \quad (9.20)$$

641 We now reach the “breaking” point of this procedure. In the (h, ξ) plane, the
642 minima form a circle of radius v . We are free to choose any of these minima to expand
643 our Lagrangian around; the physics is not affected by this choice. For convenience,
644 choose $\langle h \rangle = v, \langle \xi^2 \rangle = 0$.

Now, let us define $h' = h - v, \xi' = \xi$ with VEVs $\langle h' \rangle = 0, \langle \xi' \rangle = 0$. We can then write our spontaneously broken Lagrangian in the form

$$\mathcal{L} = \frac{1}{2} \partial_\mu h' \partial^\mu h' + \frac{1}{2} \partial_\mu \xi' \partial^\mu \xi' - \lambda v^2 h'^2 - \lambda v h' (h'^2 + \xi'^2) - \lambda (h'^2 + \xi'^2)^2 \quad (9.21)$$