1	A search for sparticles in zero lepton final states
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12	ABSTRACT
13	A search for sparticles in zero lepton final states
14	Russell W. Smith
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#### Introduction

Particle physics is a remarkably successful field of scientific inquiry. The ability to precisely predict the properties of a exceedingly wide range of physical phenomena, such as the description of the cosmic microwave background [1, 2], the understanding 67 of the anomalous magnetic dipole moment of the electron [3, 4], and the measurement of the number of weakly-interacting neutrino flavors [5] is truly amazing. 69 The theory that has allowed this range of predictions is the Standard Model 70 of particle physics (SM). The Standard Model combines the electroweak theory of 71 Glashow, Weinberg, and Salam [6–8] with the theory of the strong interactions, as 72 first envisioned by Gell-Mann and Zweig [9, 10]. This quantum field theory (QFT) 73 contains a tiny number of particles, whose interactions describe phenomena up to at 74 least the TeV scale. These particles are manifestations of the fields of the Standard 75 Model, after application of the Higgs Mechanism. The particle content of the SM 76 consists only of the six quarks, the six leptons, the four gauge bosons, and the scalar 77 Higgs boson. 78 Despite its impressive range of described phenomena, the Standard Model has 79 some theoretical and experimental deficiencies. The SM contains 26 free parameters 80 It would be more theoretically pleasing to understand these free parameters in 81 terms of a more fundamental theory. The major theoretical concern of the Standard Model, as it pertains to this thesis, is the  $hierarchy\ problem[11-15]$ . The light mass

 $<sup>^1{\</sup>rm This}$  is the Standard Model corrected to include neutrino masses. These parameters are the fermion masses (6 leptons, 6 quarks), CKM and PMNS mixing angles (8 angles, 2 CP-violating phases), W/Z/Higgs masses (3), the Higgs field expectation value, and the couplings of the strong, weak, and electromagnetic forces (3  $\alpha_{force}$ ) .

of the Higgs boson (125 GeV) should be quadratically dependent on the scale of UV physics, due to the quantum corrections from high-energy physics processes. The most perplexing experimental issue is the existence of dark matter, as demonstrated by galactic rotation curves [16-22]. This data has shown that there exists additional 87 matter which has not yet been seen interacting with the particles of the Standard 88 Model. There is no particle in the SM which can act as a candidate for dark matter. 89 Both of these major issues, as well as numerous others, can be solved by the 90 introduction of supersymmetry (SUSY) [15, 23–35]. In supersymmetric theories, each SM particles has a so-called *superpartner*, or sparticle partner, differing from given SM 92 particle by 1/2 in spin. These theories solve the hierarchy problem, since the quantum corrections induced from the superpartners exactly cancel those induced by the SM 94 particles. In addition, these theories are usually constructed assuming R-parity, 95 which can be thought of as the "charge" of supersymmetry, with SM particles having 96 R=1 and sparticles having R=-1. In collider experiments, since the incoming 97

SM particles have total R=1, the resulting sparticles are produced in pairs. This

produces a rich phenomenology, which is characterized by significant hadronic activity

and large missing transverse energy  $(E_{\rm T}^{\rm miss})$ , which provide significant discrimination

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against SM backgrounds [36].

Despite the power of searches for supersymmetry where  $E_{\mathrm{T}}^{\mathrm{miss}}$  is a primary 102 discriminating variable, there has been significant interest in the use of other variables 103 to discriminate against SM backgrounds. These include searches employing variables 104 such as  $\alpha T$ ,  $M_{T,2}$ , and the razor variables  $(M_R, R^2)$  [37–47]. In this thesis, we 105 will present the first search for supersymmetry using the novel Recursive Jigsaw 106 Reconstruction (RJR) technique. RJR can be considered the conceptual successor 107 of the razor variables. We impose a particular final state "decay tree" on an events, 108 which roughly corresponds to a simplified Feynmann diagram in decays containing 109 weakly-interacting particles. We account for the missing degrees of freedom associated 110

to the weakly-interacting particles by a series of simplifying assumptions, which allow us to calculate our variables of interest at each step in the decay tree. This allows an unprecedented understanding of the internal structure of the decay and the ability to construct additional variables to reject Standard Model backgrounds.

This thesis details a search for the superpartners of the gluon and quarks, the 115 gluino and squarks, in final states with zero leptons, with  $13.3~{\rm fb^{-1}of}$  data using the 116 ATLAS detector. We organzie the thesis as follows. The theoretical foundations of 117 the Standard Model and supersymmetry are described in Chapters 2 and 3. The 118 Large Hadron Collider and the ATLAS detector are presented in Chapters 4 and 5. 119 120 Chapter 5 provides a detailed description of Recursive Jigsaw Reconstruction and a description of the variables used for the particular search presented in this thesis. 121 Chapter 6 presents the details of the analysis, including details of the dataset, object 122 reconstruction, and selections used. In Chapter 7, the final results are presented; 123 since there is no evidence of a supersymmetric signal in the analysis, we present the 124 final exclusion curves in simplified supersymmetric models. 125

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## The Standard Model

## $_{28}$ 2.1 Overview

A Standard Model is another name for a theory of the internal symmetry group 129  $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$ , with its associated set of parameters. The Standard 130 Model refers specifically to a Standard Model with the proper parameters to describe 131 The SM is the culmination of years of work in both theoretical the universe. 132 and experimental particle physics. In this thesis, we take the view that theorists 133 construct a model with the field content and symmetries as inputs, and write down the 134 most general Lagrangian consistent with those symmetries. Assuming this model is 135 compatible with nature (in particular, the predictions of the model are consistent with 136 previous experiments), experimentalists are responsible measuring the parameters of 137 this model This will be applicable for this chapter and the following one. 138 Additional theoretical background is in 9.6. The philosophy and notations are 139 inspired by [48, 49]. 140

# 41 2.2 Field Content

The Standard Model field content is

Fermions : 
$$Q_L(3,2)_{+1/3}$$
,  $U_R(3,1)_{+4/3}$ ,  $D_R(3,1)_{-2/3}$ ,  $L_L(1,2)_{-1}$ ,  $E_R(1,1)_{-2}$   
Scalar (Higgs) :  $\phi(1,2)_{+1}$  (2.1)

Vector Fields :  $G^{\mu}(8,1)_0, W^{\mu}(1,3)_0, B^{\mu}(1,1)_0$ 

where the  $(A, B)_Y$  notation represents the irreducible representation under SU(3)

and SU(2), with Y being the electroweak hypercharge. Each of these fermion fields

has an additional index, representing the three generation of fermions.

We observed that  $Q_L, U_R$ , and  $D_R$  are triplets under  $SU(3)_C$ ; these are the quark

fields. The color group,  $SU(3)_C$  is mediated by the gluon field  $G^{\mu}(8,1)_0$ , which has

8 degrees of freedom. The fermion fields  $L_L(1,2)_{-1}$  and  $E_R(1,1)_{-2}$  are singlets under

148  $SU(3)_C$ ; we call them the *lepton* fields.

Next, we note the "left-handed" ("right-handed") fermion fields, denoted by L(R)

subscript, The left-handed fields form doublets under  $SU(2)_L$ . These are mediated

by the three degrees of freedom of the "W" fields  $W^{\mu}(1,3)_0$ . These fields only act

on the left-handed particles of the Standard Model. This is the reflection of the

treated differently by the electroweak forces. The right-handed fields,  $U_R, D_R$ , and

155  $E_R$ , are singlets under  $SU(2)_L$ .

The  $U(1)_Y$  symmetry is associated to the  $B^{\mu}(1,1)_0$  boson with one degree of

157 freedom. The charge Y is known as the electroweak hypercharge.

To better understand the phenomenology of the Standard Model, let us investigate

each of the *sectors* of the Standard Model separately.

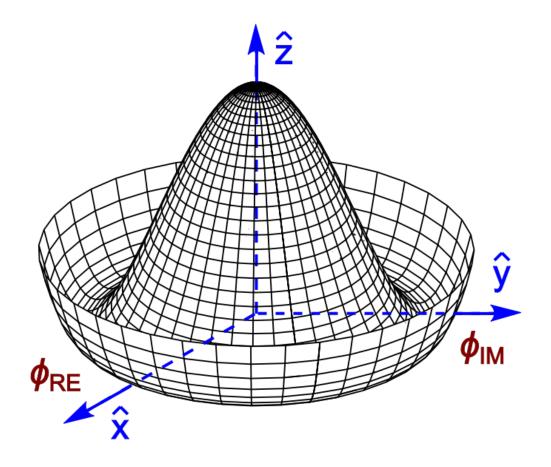
#### $_{160}$ Electroweak sector

The electroweak sector refers to the  $SU(2)_L \otimes U(1)_Y$  portion of the Standard Model gauge group. Following our philosophy of writing all gauge-invariant and renormalizable terms, the electroweak Lagrangian can be written as

$$\mathcal{L} = W_a^{\mu\nu} W_{\mu\nu}^a + B^{\mu\nu} B_{\mu\nu} + (D^{\mu}\phi)^{\dagger} D_{\mu}\phi - \mu^2 \phi^{\dagger}\phi - \lambda (\phi^{\dagger}\phi)^2. \tag{2.2}$$

where  $W_a^{\mu\nu}$  are the three (a=1,2,3) gauge bosons associated to the  $SU(2)_L$  gauge group,  $B^{\mu\nu}$  is the one gauge boson of the  $U(1)_Y$  gauge group, and  $\phi$  is the complex

Figure 2.1: Sombrero potential



Higgs multiplet. The covariant derivative  $D^{\mu}$  is given by

$$D^{\mu} = \partial^{\mu} + \frac{ig}{2} W_a^{\mu} \sigma_a + \frac{ig'}{2} B^{\mu} \tag{2.3}$$

where  $i\sigma_a$  are the Pauli matrices times the imaginary constant, which are the generators for  $SU(2)_L$ , and g and g' are the  $SU(2)_L$  and  $U(1)_Y$  coupling constants, respectively. The field strength tensors  $W_a^{\mu\nu}$  and  $B^{\mu\nu}$  are given by the commutator of the covariant derivative associated to each field

$$B^{\mu\nu} = \partial^{\mu}B^{\nu} - \partial^{\nu}B^{\mu}$$

$$W_{a}^{\mu\nu} = \partial^{\mu}W_{a}^{\nu} - \partial^{\nu}W_{a}^{\mu} - g\epsilon_{abc}W_{a}^{\mu}W_{b}^{\nu}, \qquad i = 1, 2, 3$$

$$(2.4)$$

The terms in the Lagrangian 2.2 proportional to  $\mu^2$  and  $\lambda$  make up the "Higgs potential" [50]. As normal (see Appendix 9.6), we restrict  $\lambda > 0$  to guarantee our potential is bounded from below, and we also require  $\mu^2 < 0$ , which gives us the standard "sombrero" potential shown in 2.1.

This potential has infinitely many minima at  $\langle \phi \rangle = \sqrt{2m/\lambda}$ ; the ground state is spontaneously broken by the choice of ground state, which induces a vacuum expection value (VEV). Without loss of generality, we can choose the Higgs field  $\phi$  to point in the real direction, and write the Higgs field  $\phi$  in the following form:

$$\phi = \frac{1}{\sqrt{2}} \exp(\frac{i}{v} \sigma_a \theta_a) \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}. \tag{2.5}$$

We choose a gauge to rotate away the dependence on  $\theta_a$ , such that we can write simply

$$\phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}. \tag{2.6}$$

Now, we can see how the masses of the vector bosons are generated from the application of the Higgs mechanism. We plug Eq.2.6 back into the electroweak Lagrangian, and only showing the relevant mass terms in the vacuum state where h(x) = 0 see that (dropping the Lorentz indices):

$$\mathcal{L}_{M} = \frac{1}{8} \left| \begin{pmatrix} gW_{3} + g'B & g(W_{1} - iW_{2}) \\ g(W_{1} + iW_{2}) & -gW_{3} + g'B \end{pmatrix} \begin{pmatrix} 0 \\ v \end{pmatrix} \right|^{2}$$

$$= \frac{g^{2}v^{2}}{8} \left[ W_{1}^{2} + W_{2}^{2} + (\frac{g'}{g}B - W_{3})^{2} \right]$$
(2.7)

Defining the Weinberg angle  $tan(\theta_W) = g'/g$  and the following physical fields:

$$W^{\pm} = \frac{1}{\sqrt{2}} (W_1 \mp iW_2)$$

$$Z^0 = \cos \theta_W W_3 - \sin \theta_W B$$

$$A^0 = \sin \theta_W W_3 + \cos \theta_W B$$
(2.8)

we can write the piece of the Lagrangian associated to the vector boson masses as

$$\mathcal{L}_{M_V} = \frac{1}{4}g^2 v^2 W^+ W^- + \frac{1}{8}(g^2 + g'^2)v^2 Z^0 Z^0.$$
 (2.9)

and we have the following values of the masses for the vector bosons:

$$m_W^2 = \frac{1}{4}v^2g^2$$

$$m_Z^2 = \frac{1}{4}v^2(g^2 + g'^2)$$

$$m_A^2 = 0$$
(2.10)

We thus see how the Higgs mechanism gives rise to the masses of the  $W^{\pm}$  and Z boson in the Standard Model; the mass of the photon is zero, as expected. The  $SU(2)_L \otimes U(1)_Y$  symmetry of the initially massless  $W_{1,2,3}$  and B fields is broken to the  $U(1)_{EM}$ . Of the four degrees of freedom in the complex Higgs doublet, three are "eaten" when we give mass to the  $W^{\pm}$  and  $Z_0$ , while the other degree of freedom is the Higgs particle, as found in 2012 by the ATLAS and CMS collaborations [51, 52].

## 172 Quantum Chromodynamics

Quantum chromodynamics (or the theory of the *strong* force) characterizes the behavior of *colored* particles, collectively known as *partons*. The partons of the Standard Model are the (fermionic) quarks, and the (bosonic) gluons. The strong force is governed by  $SU(3)_C$ , an unbroken symmetry in the Standard Model, which implies the gluon remains massless. Defining the covariant derivative for QCD as

$$D^{\mu} = \partial^{\mu} + ig_s G_a^{\mu} L_a, a = 1, ..., 8$$
 (2.11)

where  $L_a$  are the generators of  $SU(3)_C$ , and  $g_s$  is the coupling constant of the strong force. The QCD Lagrangian then is given by

$$\mathcal{L}_{\text{QCD}} = i\bar{\psi}_f D_\mu \gamma^\mu \psi_f - \frac{1}{4} G_{a,\mu\nu} G_a^{\mu\nu}$$
 (2.12)

where the summation over f is for quarks families, and  $G_a^{\mu\nu}$  is the gluon field strength tensor, given by

$$G_a^{\mu\nu} = \partial^{\mu} G_a^{\nu} - \partial^{\nu} G_a^{\mu} - g_s f^{abc} G_b^{\mu} G_c^{\nu}, a, b, c = 1, ..., 8$$
 (2.13)

where  $f^{abc}$  are the structure constants of  $SU(3)_C$ , which are analogous to  $\epsilon_{abc}$  for  $SU(2)_L$ . The kinetic term for the quarks is contained in the standard  $\partial_{\mu}$  term, while the field strength term contains the interactions between the quarks and gluons, as well as the gluon self-interactions.

Written down in this simple form, the QCD Lagrangian does not seem much 177 different from the QED Lagrangian, with the proper adjustments for the different 178 group structures. The gluon is massless, like the photon, so one could näively expect 179 an infinite range force, and it pays to understand why this is not the case. The 180 reason for this fundamental difference is the gluon self-interactions arising in the 181 field strength tensor term of the Lagrangian. This leads to the phenomena of color 182 confinement, which describes how one only observes color-neutral particles alone in 183 nature. In contrast to the electromagnetic force, particles which interact via the 184 strong force experience a *greater* force as the distance between the particles increases. 185 At long distances, the potential is given by V(r) = -kr. At some point, it is more 186 energetically favorable to create additional partons out of the vacuum than continue 187 pulling apart the existing partons, and the colored particles undergo fragmentation. 188 This leads to hadronization. Bare quarks and gluons are actually observed as sprays 189 of hadrons (primarly kaons and pions); these sprays are known as jets, which are 190 what are observed by experiments. 191

It is important to recognize the importance of understanding these QCD interactions in high-energy hadron colliders such as the LHC. Since protons are hadrons, proton-proton collisions such as those produced by the LHC are primarily governed by the processes of QCD. In particular, by far the most frequent process observed in LHC experiments is dijet production from gluon-gluon interactions (see Fig.2.2). These

**Standard Model Production Cross Section Measurements** Status: August 2016  $\sigma$  [pb] **ATLAS** Preliminary Theory  $\sqrt{s} = 7, 8, 13 \text{ TeV}$ Run 1,2 10<sup>6</sup> 10<sup>5</sup> *p*<sub>T</sub> > 25 GeV Data 20.3 fb-1  $10^{4}$ LHC pp  $\sqrt{s} = 13 \text{ TeV}$  $10^{3}$ Data 0.08 - 14.8 fb  $10^{2}$  $10^{1}$ 1 10- $10^{-2}$  $10^{-3}$ 

w

fid.

fid.

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Z

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tot.

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Figure 2.2: Cross-sections of various Standard Model processes

gluons that interact are part of the sea particles inside the proton; the simple p = uud197 model does not apply. The main valence uud quarks are constantly interacting via 198 gluons, which can themselves radiate gluons or split into quarks, and so on. A more 199 useful understanding is given by the colloquially-known baq model [53, 54], where the 200 proton is seen as a "bag" of (in principle) infinitely many partons, each with energy 201  $E < \sqrt{s} = 6.5$  TeV. One then collides this (proton) bag with another, and views the 202 products of this very complicated collision, where calculations include many loops in 203 nonpertubative QCD calculations. 204

ttWttZ tty Zjj ww Zyy Wyy VVjj tot. tot. fid. fid. tot. fid. fid. fid. fid.

tot. tot. fid. fid.

tot. fid. fid.

Vγ

fid.

Fortunately, we are generally saved by the QCD factorization theorems [55]. This allows one to understand the hard (i.e. short distance or high energy)  $2 \rightarrow 2$  parton process using the tools of perturbative QCD, while making series of approximations known as a parton shower model to understand the additional corrections from nonpertubative QCD. We will discuss the reconstruction of jets by experiments in Ch.5.

#### 211 Fermions

We will now look more closely at the fermions in the Standard Model [56].

As noted earlier in Sec.2.2, the fermions of the Standard Model can be first distinguished between those that interact via the strong force (quarks) and those which do not (leptons).

There are six leptons in the Standard Model, which can be placed into three generations.

 $\begin{pmatrix} e \\ \nu_e \end{pmatrix}, \begin{pmatrix} \mu \\ \nu_{\mu} \end{pmatrix}, \begin{pmatrix} \tau \\ \nu_{\tau} \end{pmatrix}$  (2.14)

There is the electron (e), muon  $(\mu)$ , and tau  $(\tau)$ , each of which has an associated neutrino  $(\nu_e, \nu_\mu, \nu_\tau)$ . Each of the so-called charged ("electron-like") leptons has electromagnetic charge -1, while the neutrinos all have  $q_{EM}=0$ .

Often in an experimental context, lepton is used to denote the stable electron and metastable muon, due to their striking experimental signatures. Taus are often treated separately, due to their much shorter lifetime of  $\tau_{\tau} \sim 10^{-13} s$ ; these decay through hadrons or the other leptons, so often physics analyses at the LHC treat them as jets or leptons, as will be done in this thesis.

As the neutrinos are electrically neutral, nearly massless, and only interact via the weak force, it is quite difficult to observe them directly. Since LHC experiments rely overwhelmingly on electromagnetic interactions to observe particles, the presence of neutrinos is not observed directly. Neutrinos are instead observed by the conservation of four-momentum in the plane transverse to the proton-proton collisions, known as missing transverse energy.

There are six quarks in the Standard Model: up, down, charm, strange, top, and bottom. Quarks are similar organized into three generations:

$$\begin{pmatrix} u \\ d \end{pmatrix}, \begin{pmatrix} c \\ s \end{pmatrix}, \begin{pmatrix} t \\ b \end{pmatrix} \tag{2.15}$$

230 where we speak of "up-like" quarks and "down-like" quarks.

Each up-like quark has charge  $q_{up} = 2/3$ , while the down-like quarks have  $q_{down} =$ 231 -1/3. At the high energies of the LHC, one often makes the distinction between 232 the light quarks (u, d, c, s), the bottom quark, and top quark. In general, due to 233 the hadronization process described above, the light quarks, with masses  $m_q < \sim$ 234 1.5GeV are indistinguishable by LHC experiments. Their hadronic decay products 235 generally have long lifetimes and they are reconstructed as jets.<sup>1</sup>. The bottom quark 236 hadronizes primarly through the B-mesons, which generally travels a short distance 237 before decaying to other hadrons. This allows one to distinguish decays via b-quarks 238 form other jets; this procedure is known as b-tagging and will be discussed more in 239 Ch.5. Due to its large mass, the top quark decays before it can hadronize; there 240 are no bound states associated to the top quark. The top is of particular interest at 241 the LHC; it has a striking signature through its most common decay mode  $t \to Wb$ . Decays via tops, especially  $t\bar{t}$  are frequently an important signal decay mode, or an 243 important background process. 244

#### 245 Interactions in the Standard Model

We briefly overview the entirety of the fundamental interactions of the Standard Model; these can also be found in 2.3.

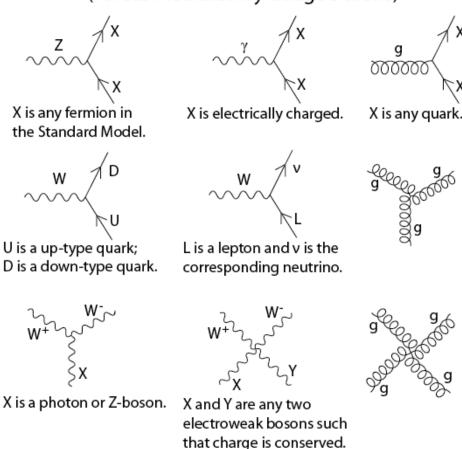
The electromagnetic force, mediated by the photon, interacts with via a threepoint coupling all charged particles in the Standard Model. The photon thus interacts with all the quarks, the charged leptons, and the charged  $W^{\pm}$  bosons.

The weak force is mediated by three particles: the  $W^{\pm}$  and the  $Z^0$ . The  $Z^0$  can interacts with all fermions via a three-point coupling. A real  $Z_0$  can thus decay to a fermion-antifermion pair of all SM fermions except the top quark, due to its large

<sup>&</sup>lt;sup>1</sup>In some contexts, charm quarks are also treated as a separate category, although it is quite difficult to distinguish charm quarks from the other light quarks.

Figure 2.3: The interactions of the Standard Model

# Standard Model Interactions (Forces Mediated by Gauge Bosons)



mass. The  $W^{\pm}$  has two important three-point interactions with fermions. First, the 254  $W^{\pm}$  can interact with an up-like quark and a down-like quark; an important example 255 in LHC experiments is  $t \to Wb$  The coupling constants for these interactions are 256 encoded in the unitary matrix known as the Cabibbo–Kobayashi–Maskawa (CKM) 257 matrix [57, 58], and are generally known as flavor-changing interactions. Secondly, 258 the  $W^{\pm}$  interacts with a charged lepton and its corresponding neutrino. In this case, 259 the unitary matrix that corresponds to CKM matrix for quarks is the identity matrix, 260 which forbids (fundamental) vertices such as  $\mu \to We$ . For leptons, instead this is 261 a two-step process:  $\mu \to \nu_m uW \to \nu_m u\bar{\nu_e}e$ . Finally, there are the self-interactions 262

of the weak gauge bosons. There is a three-point and four-point interaction; all combinations are allowed which conserve electric charge.

The strong force is mediated by the gluon, which as discussed above also carries the strong color charge. There is the fundamental three-point interaction, where a quark radiates a gluon. Additionally, there are the three-point and four-point gluononly interactions.

#### 2.3 Deficiencies of the Standard Model

At this point, it is quite easy to simply rest on our laurels. This relatively simple theory is capable of explaining a very wide range of phenomenom, which ultimately break down only to combinations of nine diagrams shown in Fig.2.3. Unfortunately, there are some unexplained problems with the Standard Model. We cannot go through all of the potential issues in this thesis, but we will motivate the primary issues which naturally lead one to *supersymmetry*, as we will see in Ch.3.

The Standard Model has many free parameters; see Table 2.1 In general, we prefer models with less free parameters. A great example of this fact, and the primary experimental evidence for EWSB, is the relationship between the couplings of the weak force and the masses of the gauge bosons of the weak force:

$$\rho \equiv \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} \stackrel{?}{=} 1 \tag{2.16}$$

where ? indicates that this is a testable prediction of the Standard Model (in particular, that the gauge bosons gain mass through EWSB). This relationship has been measured within experimental and theoretical predictions. We would like to produce additional such relationships, which would exist if the Standard Model is a low-energy approximation of some other theory.

An additional issue is the lack of gauge coupling unification. The couplings of any quantum field theory "run" as a function of the distance scales (or inversely,

Table 2.1: Parameters of the Standard Model. For values dependent on the renormalization scheme, we use a combination of the on-shell normalization scheme [59–62] and modified minimal subtraction scheme with  $m_{\bar{M}S}$  as indicated in the table [63]

$m_e$	Electron mass	511 keV
$m_{\mu}$	Muon mass	105.7  MeV
$m_{ au}$	Tau mass	1.78 GeV
$m_u$	Up quark mass	$1.9 \text{ MeV } (m_{\bar{MS}} = 2GeV)$
$m_d$	Down quark mass	$4.4 \text{ MeV } (m_{\bar{M}S} = 2GeV)$
$m_s$	Strange quark mass	$87 \text{ MeV } (m_{\bar{M}S} = 2GeV)$
$m_c$	Charm quark mass	1.32 GeV $(m_{\bar{M}S} = m_c)$
$m_b$	Bottom quark mass	$4.24 \text{ GeV } (m_{\bar{M}S} = m_b)$
$m_t$	Top quark mass	172.7 GeV (on-shell renormalization)
$\theta_{12}$ CKM	12-mixing angle	13.1°
$\theta_{23}$ CKM	23-mixing angle	2.4°
$\theta_{13}$ CKM	13-mixing angle	0.2°
$\delta$ CKM	CP-violating Phase	0.995
g'	U(1) gauge coupling	$0.357 \ (m_{\bar{MS}} = m_Z)$
g	SU(2) gauge coupling	$0.652 \ (m_{\bar{M}S} = m_Z)$
$g_s$	SU(3) gauge coupling	$1.221 \ (m_{\bar{M}S} = m_Z)$
$\theta QCD$	QCD vacuum angle	~0
VEV	Higgs vacuum expectation value	$246~{\rm GeV}$
$m_H$	Higgs mass	125 GeV

energy scales) of the theory. The idea is closely related to the unification of the electromagnetic and weak forces at the so-called *electroweak scale* of O(100 GeV). One would hope this behavior was repeated between the electroweak forces and the strong force at some suitable energy scale. The Standard Model does automatically not exhibit this behavior, as we can see in Fig.2.4.

The most significant problem with the Standard Model is the hierarchy problem. In its most straightforward incarnation, the Higgs scalar field is subject to quantum corrections through loop diagrams, as shown in Fig.2.5. For demonstration, we use the contributions from the top quark, since the top quark has the largest Higgs Yukawa coupling due to its large mass. In general, we should expect these corrections to quadratically dependent on the scale of the ultraviolet physics,  $\Lambda$ . Briefly assume there is no new physics before the Planck scale of gravity,  $\Lambda_{\rm Planck} = 10^{19}$  GeV. In this

Figure 2.4: The running of Standard Model gauge couplings. The Standard Model couplings do not unify at high energies, which indicates it cannot completely describe nature through the Planck scale.

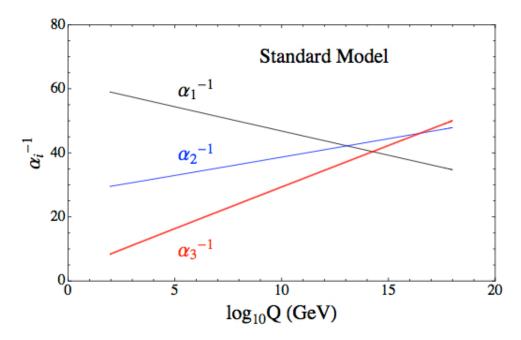
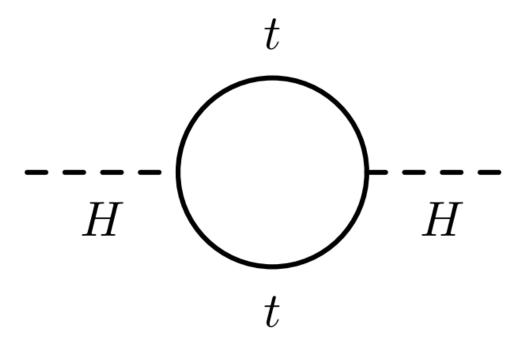


Figure 2.5: The dominant quantum loop correction to the Higgs mass in the Standard Model.



case, we expect the corrections to the Higgs mass like

$$\delta m_H^2 \approx \left(\frac{m_t}{8\pi^2 < \phi >_{VEV}}\right)^2 \Lambda_{Planck}^2.$$
 (2.17)

To achieve the miraculous cancellation required to get the observed Higgs mass of 125 GeV, one needs to then set the bare Higgs mass  $m_0$ , our input to the Standard Model Lagrangian, itself to a *precise* value  $\sim 10^{19}$  GeV. This extraordinary level of parameter finetuning is quite undesirable, and within the framework of the Standard Model, there is little that can be done to alleviate this issue.

An additional concern, of a different nature, is the lack of a dark matter candidate 293 in the Standard Model. Dark matter was discovered by observing galactic rotation 294 curves, which showed that much of the matter that interacted gravitionally was 295 invisible to our (electromagnetic) telescopes [16-22]. The postulation of the existence 296 of dark matter, which interacts at least through gravity, allows one to understand 297 these galatic rotation curves. Unfortunately, no particle in the Standard Model could 298 possibly be the dark matter particle. The only candidate truly worth another look is 299 the neutrino, but it has been shown that the neutrino content of the universe is simply 300 too small to explain the galatic rotation curves [22, 64]. The experimental evidence 301 from the galactic rotations curves thus show there must be additional physics beyond 302 the Standard Model, which is yet to be understood. 303

In the next chapter, we will see how these problems can be alleviated by the theory of supersymmetry.

mass → \*2.3 MeV/ic² ~173.07 GeV/c² ≈126 GeV/ic² charge → 2/3 1/2 Higgs boson gluon up charm top =4.8 MeV/10<sup>2</sup> \*4.18 GeWol QUARKS -103 1/2 1/2 1/2 down strange bottom photon 0.511 MeV/c\* 91.2 GeWc\* 1/2 1/2 Z boson electron tau muon <2.2 eV/c² <0.17 MeW/c<sup>2</sup> <15.5 MeV/c<sup>2</sup> 80.4 GeV/c<sup>2</sup> LEPTONS 1/2 electron neutrino muon neutrino tau neutrino W boson

Figure 2.6: Particles of the Standard Model

#### Chapter 3

307

306

## Supersymmetry

This chapter will introduce supersymmetry (SUSY) [15, 23–35]. We will begin by 308 introducing the concept of a *superspace*, and discuss some general ingredients of 309 supersymmetric theories. This will include a discussion of how the problems with the 310 Standard Model described in Ch.2 are naturally fixed by these theories. 311 The next step is to discuss the particle content of the Minimally Supersymmetric 312 Standard Model (MSSM). As its name implies, this theory contains the minimal 313 additional particle content to make Standard Model supersymmetric. We then discuss 314 the important phenomonological consequences of this theory, especially as it would 315 be observed in experiments at the LHC. 316

# 3.1 Supersymmetric theories: from space to

# superspace

# 319 Coleman-Mandula "no-go" theorm

We begin the theoretical motivation for supersymmetry by citing the "no-go" theorem of Coleman and Mandula [65]. This theorem forbids *spin-charge unification*; it states that all quantum field theories which contain nontrivial interactions must be a direct product of the Poincarégroup of Lorentz symmetries, the internal product from of gauge symmetries, and the discrete symmetries of parity, charge conjugation, and time reversal. The assumptions which go into building the Coleman-Mandula

theorem are quite restrictive, but there is one unique way out, which has become known as supersymmetry [26, 66]. In particular, we must introduce a spinorial group generator Q. Alternatively, and equivalently, this can be viewed as the addition of anti-commuting coordinates; space plus these new anti-commuting coordinates is then called superspace [67]. We will not investigae this view in detail, but it is also a quite intuitive and beautiful way to construct supersymmetry [15].

#### 332 Supersymmetry transformations

A supersymmetric transformation Q transforms a bosonic state into a fermionic state, and vice versa:

$$Q|\text{Fermion}\rangle = |\text{Boson}\rangle \tag{3.1}$$

$$Q|Boson\rangle = |Fermion\rangle$$
 (3.2)

To ensure this relation holds, Q must be an anticommuting spinor. Additionally, since spinors are inherently complex,  $Q^{\dagger}$  must also be a generator of the supersymmetry transformation. Since Q and  $Q^{\dagger}$  are spinor objects (with s=1/2), we can see that supersymmetry must be a spacetime symmetry. The Haag-Lopuszanski-Sohnius extension [66] of the Coleman-Mandula theorem [65] is quite restrictive about the forms of such a symmetry. Here, we simply write the (anti-) commutation relations [15]:

$$Q_{\alpha}, Q_{\dot{\alpha}}^{\dagger} = -2\sigma_{\alpha\dot{\alpha}^{\mu}}P_{\mu} \tag{3.3}$$

$$Q_{\alpha}, Q_{\dot{\beta}} = Q_{\dot{\alpha}}^{\dagger}, Q_{\dot{\beta}}^{\dagger} = 0 \tag{3.4}$$

$$[P^{\mu}, Q_{\alpha}] = [P^{\mu}, Q_{\dot{\alpha}}^{\dagger}] = 0$$
 (3.5)

#### 335 Supermultiplets

In a supersymmetric theory, we organize single-particle states into irreducible 336 representations of the supersymmetric algebra which are known as *supermultiplets*. 337 Each supermultiplet contains a fermion state  $|F\rangle$  and a boson state  $|B\rangle$ ; these two 338 states are the known as *superpartners*. These are related by some combination of 339 Q and  $Q^{\dagger}$ , up to a spacetime transformation. Q and  $Q^{\dagger}$  commute with the mass-340 squared operator  $-P^2$  and the operators corresponding to the gauge transformations 341 [15]; in particular, the gauge interactions of the Standard Model. In an unbroken 342 supersymmetric theory, this means the states  $|F\rangle$  and  $|B\rangle$  have exactly the same mass, 343 electromagnetic charge, electroweak isospin, and color charges. One can also prove 344 [15] that each supermultiplet contains the exact same number of bosonic  $(n_B)$  and 345 fermion  $(n_F)$  degrees of freedom. We now explore the possible types of supermultiples 346 one can find in a renormalizable supersymmetric theory. 347

Since each supermultiplet must contain a fermion state, the simplest type of supermultiplet contains a single Weyl fermion state  $(n_F = 2)$  which is paired with  $n_B = 2$  scalar bosonic degrees of freedom. This is most conveniently constructed as single complex scalar field. We call this construction a scalar supermultiplet or chiral supermultiplet. The second name is indicative; only chiral supermultiplets can contain fermions whose right-handed and left-handed components transform differently under the gauge interactions (as of course happens in the Standard Model).

The second type of supermultiplet we construct is known as a gauge supermultiplet. We take a spin-1 gauge boson (which must be massless due to the gauge symmetry, so  $n_B = 2$ ) and pair this with a single massless Weyl spinor<sup>1</sup>. The gauge bosons transform as the adjoint representation of the their respective gauge groups; their fermionic partners, which are known as gauginos, must also. In particular, the left-handed and right-handed components of the gaugino fermions have the same

<sup>&</sup>lt;sup>1</sup>Choosing an s = 3/2 massless fermion leads to nonrenormalizable interactions.

361 gauge transformation properties.

Excluding gravity, this is the entire list of supermultiplets which can participate 362 in renormalizable interactions in what is known as N=1 supersymmetry. This 363 means there is only one copy of the supersymmetry generators Q and  $Q^{\dagger}$ . This is 364 essentially the only "easy" phenomenological choice, since it is the only choice in four 365 dimensions which allows for the chiral fermions and parity violations built into the 366 Standard Model, and we will not look further into N > 1 supersymmtry in this thesis. 367 The primary goal, after understanding the possible structures of the multiplets 368 above, is to fit the Standard Model particles into a multiplet, and therefore make 369 predictions about their supersymmetric partners. We explore this in the next section. 370

# 3.2 Minimally Supersymmetric Standard Model

To construct what is known as the MSSM [susyPrimer, 68–71], we need a few ingredients and assumptions. First, we match the Standard Model particles with their corresponding superpartners of the MSSM. We will also introduce the naming of the superpartners (also known as sparticles). We discuss a very common additional restraint imposed on the MSSM, known as R-parity. We also discuss the concept of soft supersymmetry breaking and how it manifests itself in the MSSM.

# 8 Chiral supermultiplets

The first thing we deduce is directly from Sec.??. The bosonic superpartners associated to the quarks and leptons *must* be spin 0, since the quarks and leptons must be arranged in a chiral supermultiplet. This is essentially the note above, since the chiral supermultiplet is the only one which can distinguish between the left-handed and right-handed components of the Standard Model particles. The superpartners of the quarks and leptons are known as *squarks* and *sleptons*, or *sfermions* in aggregate.

(for "scalar quarks", "scalar leptons", and "scalar fermion"<sup>2</sup>). The "s-" prefix 385 can also be added to the individual quarks i.e. selectron, sneutrino, and stop. The 386 notation is to add a  $\sim$  over the corresponding Standard Model particle i.e.  $\tilde{e}$ , the 387 selectron is the superpartner of the electron. The two-component Weyl spinors of the 388 Standard Model must each have their own (complex scalar) partner i.e.  $e_L, e_R$  have 389 two distinct partners:  $\tilde{e_L}$ ,  $\tilde{e_R}$ . As noted above, the gauge interactions of any of the 390 391 sfermions are identical to those of their Standard Model partners.

Due to the scalar nature of the Higgs, it must obviously lie in a chiral supermultiplet. To avoid gauge anomolies and ensure the correct Yukawa couplings to the quarks and leptons [15], we must add additional Higgs bosons to any supersymmetric theory. In the MSSM, we have two chiral supermultiplets. The SM (SUSY) parts of the multiplets are denoted  $H_u(\tilde{H}_u)$  and  $H_d(\tilde{H}_d)$ . Writing out  $H_u$  and  $H_d$  explicitly:

$$H_{u} = \begin{pmatrix} H_{u}^{+} \\ H_{u}^{0} \end{pmatrix}$$

$$H_{d} = \begin{pmatrix} H_{d}^{0} \\ H_{d}^{-} \end{pmatrix}$$

$$(3.6)$$

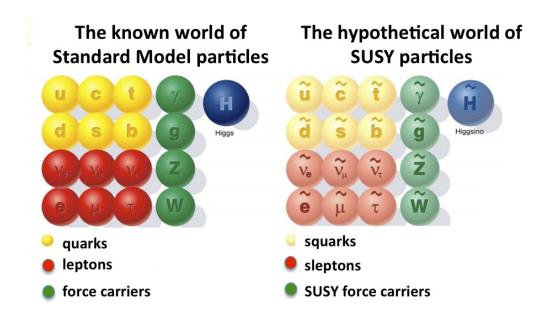
$$H_d = \begin{pmatrix} H_d^0 \\ H_d^- \end{pmatrix} \tag{3.7}$$

(3.8)

we see that  $H_u$  looks very similar to the SM Higgs with Y=1, and  $H_d$  is symmetric 392 to this with  $+ \rightarrow -$ , with Y = -1. The SM Higgs boson,  $h_0$ , is a linear superposition 393 of the neutral components of these two doublets. The SUSY parts of the Higgs 394 multiplets,  $\tilde{H}_u$  and  $\tilde{H}_d$ , are each left-handed Weyl spinors. For generic spin-1/2 395 sparticles, we add the "-ino" suffix. We then call the partners of the two Higgs 396 collectively the *Higgsinos*. 397

<sup>&</sup>lt;sup>2</sup>The last one should probably have bigger scare quotes.

Figure 3.1: Particles of the MSSM



#### 398 Gauge supermultiplets

410

The superpartners of the gauge bosons must all be in gauge supermultiplets since they contain a spin-1 particle. Collectively, we refer to the superpartners of the gauge bosons as the gauginos.

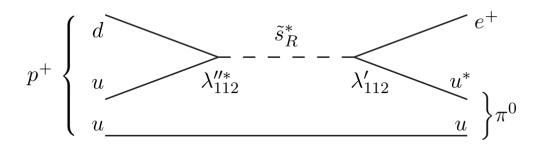
The first gauge supermultiplet contains the gluon, and its superpartner, which is 402 known as the *qluino*, denoted  $\tilde{q}$ . The gluon is of course the SM mediator of  $SU(3)_C$ ; 403 the gluino is also a colored particle, subject to  $SU(3)_C$ . From the SM before EWSB, 404 we have the four gauge bosons of the electroweak symmetry group  $SU(2)_L \otimes U(1)_Y$ : 405  $W^{1,2,3}$  and  $B^0$ . The superpartners of these particles are thus the winos  $W^{\tilde{1},2,3}$  and 406 bino  $\tilde{B}^0$ , where each is placed in another gauge supermultiplet with its corresponding 407 SM particle. After EWSB, without breaking supersymmetry, we would also have the 408 zino  $\tilde{Z}^0$  and photino  $\tilde{\gamma}$ . 409

The entire particle content of the MSSM can be seen in Fig.3.1.

At this point, it's important to take a step back. Where are these particles?

As stated above, supersymmetric theories require that the masses and all quantum

Figure 3.2: This Feynmann diagram shows how proton decay is induced in the MSSM, if one does not impose R-parity.



numbers of the SM particle and its corresponding sparticle are the same. Of course, we have not observed a selectron, squark, or wino. The answer, as it often is, is that supersymmetry is *broken* by the vacuum state of nature [15].

#### 416 $R{ m -parity}$

This section is a quick aside to the general story. R-parity refers to an additional discrete symmetry which is often imposed on supersymmetric models. For a given particle state, we define

$$R = (-1)^{3(B-L)+2s} (3.9)$$

where B, L is the baryon (lepton) number and s is the spin. The imposition of this symmetry forbids certain terms from the MSSM Lagrangian that would violate baryon and/or lepton number. This is required in order to prevent proton decay, as shown in Fig.3.2<sup>3</sup>. . In supersymmetric models, this is a  $\mathbb{Z}_2$  symmetry, where SM particles have R=1and sparticles have R=-1. We will take R-parity as part of the definition of

the MSSM. We will discuss later the drastic consequences of this symmetry on SUSY

424 phenomenology

 $<sup>^3</sup>$ Proton decay can actually be prevented by allowing only one of the four potential R-parity violating terms to survive.

#### 425 Soft supersymmetry breaking

The fundamental idea of *soft* supersymmetry breaking[15, 34, 35, 72, 73] is that we would like to break supersymmetry without reintroducing the quadratic divergences we discussed at the end of Chapter 2. We write the Lagrangian in a form:

$$\mathcal{L}_{\text{MSSM}} = \mathcal{L}_{\text{SUSY}} + \mathcal{L}_{\text{soft}} \tag{3.10}$$

In this sense, the symmetry breaking is "soft", since we have separated out the completely symmetric terms from those soft terms which will not allow the quadratic divergences to the Higgs mass.

- The explicitly allowed terms in the soft-breaking Lagrangian are [35].
- Mass terms for the scalar components of the chiral supermultipletss
- Mass terms for the Weyl spinor components of the gauge supermultipletss
- Trilinear couplings of scalar components of chiral supermultiplets

In particular, using the field content described above for the MSSM, the softly-broken portion of the MSSM Lagrangian can be writen

$$\mathcal{L}_{\text{soft}} = -\frac{1}{2} \left( M_3 \tilde{g} \tilde{g} + M_2 \tilde{W} \tilde{W} + M_1 \tilde{B} \tilde{B} + c.c. \right)$$
(3.11)

$$-\left(\tilde{u}a_u\tilde{Q}H_u - \tilde{d}a_d\tilde{Q}H_d - \tilde{e}a_e\tilde{L}H_d + c.c.\right)$$
(3.12)

$$-\tilde{Q}^{\dagger}m_{Q}^{2}\tilde{Q} - \tilde{L}^{\dagger}m_{L}^{2}\tilde{L} - \tilde{u}m_{u}^{2}\tilde{u}^{\dagger} - \tilde{d}m_{d}^{2}\tilde{d}^{\dagger} - \tilde{e}m_{e}^{2}\tilde{e}^{\dagger}$$
(3.13)

$$-m_{H_u}^2 H_u^* H_u - m_{H_d}^2 H_d^* H_d - (bH_u H_d + cc). (3.14)$$

where we have introduced the following notations:

- 1.  $M_3, M_2, M_1$  are the gluino, wino, and bino masses.
- 2.  $a_u, a_d, a_e$  are complex  $3 \times 3$  matrices in family space.
- 3.  $m_Q^2, m_u^2, m_d^2, m_L^2, m_e^2$  are hermitian  $3 \times 3$  matrices in family space.

4.  $m_{H_u}^2, m_{H_u}^2, b$  are the SUSY-breaking contributions to the Higgs potential.

We have written matrix terms without any sort of additional notational decoration 438 to indicate their matrix nature, and we now show why. The first term 1 are 439 straightforward; these are just the straightforward mass terms for these fields. There 440 are strong constraints on the off-diagonal terms for the matrices of 2 [74, 75]; for 441 simplicity, we will assume that each  $a_i, i = u, d, e$  is proportional to the Yukawa 442 coupling matrix:  $a_i = A_{i0}y_i$ . The matrices in ?? can be similarly constrained by 443 experiments [68, 75–82] Finally, we assume that the elements 4 contributing to the 444 Higgs potential as well as all of the 1 terms must be real, which limits the possible 445 CP-violating interactions to those of the Standard Model. We thus only consider 446 flavor-blind, CP-conserving interactions within the MSSM. 447

The important mixing for mass and gauge interaction eigenstates in the MSSM occurs within electroweak sector, in a process akin to EWSB in the Standard Model. The neutral portions of the Higgsinos doublets and the neutral gauginos  $(\tilde{H}_u^0, \tilde{H}_d^0, \tilde{B}^0, \tilde{W}^0)$  of the gauge interaction basis mix to form what are known as the neutralinos of mass basis:

$$M_{\tilde{\chi}} = \begin{pmatrix} M_1 & 0 & -c_{\beta}s_W m_Z & s_{\beta}s_W m_Z \\ 0 & M_2 & c_{\beta}c_W m_Z & -s_{\beta}c_W m_Z \\ -c_{\beta}s_W m_Z & c_{\beta}c_W m_Z & 0 & -\mu \\ s_{\beta}s_W m_Z & -s_{\beta}c_W m_Z & -\mu & 0 \end{pmatrix}$$
(3.15)

where s(c) are the sine and cosine of angles related to EWSB, which introduced masses to the gauginos and higgsinos. Diagonalization of this matrix gives the four neutralino mass states, listed without loss of generality in order of increasing mass:  $\chi_{1,2,3,4}^{0}$ .

The neutralinos, especially the lightest neutralino  $c\tilde{h}i_1^0$ , are important ingredients in SUSY phenomenology.

The same process can be done for the electrically charged gauginos with the charged portions of the Higgsino doublets along with the charged winos  $(\tilde{H}_u^+, \tilde{H}_d^+, \tilde{W}^+, \tilde{W}^-)$ . This leads to the *charginos*, again in order of increasing mass  $\tilde{\chi}_{1,2}^{\pm}$ .

#### $_{ ext{\tiny 458}}$ 3.3 Phenomenology

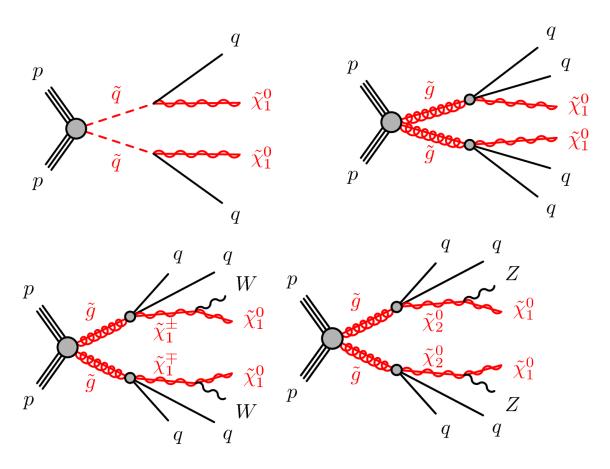
We are finally at the point where we can discuss the phenomenology of the MSSM, in particular as it manifests itself at the energy scales of the LHC.

As noted above in Sec.3.2, the assumption of R-parity has important conse-461 quences for MSSM phenomenology. The SM particles have R=1, while the sparticles 462 all have R = -1. Simply, this is the "charge" of supersymmetry. Since the particles of 463 LHC collisions (pp) have total incoming R=1, we must expect that all sparticles will 464 be produced in pairs. An additional consequence of this symmetry is the fact that the 465 lightest supersymmetric particle (LSP) is stable. Off each branch of the Feynmann 466 diagram shown in Fig., we have R = -1, and this can only decay to another sparticle 467 and a SM particle. Once we reach the lightest sparticle in the decay, it is absolutely 468 stable. This leads to the common signature  $E_{\mathrm{T}}^{\mathrm{miss}}$  for a generic SUSY signal. 469

For this thesis, we will be presenting an inclusive search for squarks and gluinos 470 with zero leptons in the final state. This is a very interesting decay channel<sup>4</sup>, due 471 to the high cross-sections of  $\tilde{g}\tilde{g}$  and  $\tilde{q}\tilde{q}$  decays, as can be seen in Fig.?? [83]. 472 is a direct consequence of the fact that these are the colored particles of the MSSM. 473 Since the sparticles interact with the gauge groups of the SM in the same way as their 474 SM partners, the colored sparticles, the squarks and gluinos, are produced and decay 475 as governed by the color group  $SU(3)_C$  with the strong coupling  $g_S$ . The digluino 476 production is particularly copious, due to color factor corresponding to the color octet 477

<sup>&</sup>lt;sup>4</sup>Prior to Run1, probably the most most interesting SUSY decay channel.

Figure 3.3: SUSY signals considered in this thesis



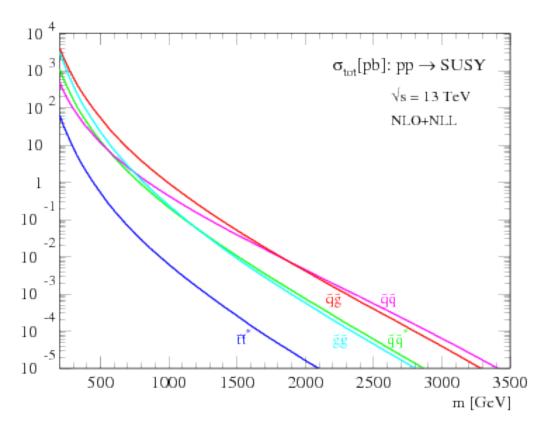
478 of SU(3)C.

489

In the case of disquark production, the most common decay mode of the squark in 479 the MSSM is a decay directly to the LSP plus a single SM quark [15]. This means the 480 basic search strategy of disquark production is two jets from the final state quarks, 481 plus missing transverse energy for the LSPs. There are also cascade decays, the most 482 common of which, and the only one considered in this thesis, is  $\tilde{q} \to q \chi^{\pm} \to q W^{\pm} \chi^0$ . 483 For digluino production, the most common decay is  $\tilde{g} \rightarrow g\tilde{q}$ , due to the large 484  $g_S$  coupling. The squark then decays as listed above. In this case, we generically 485 search for four jets and missing transverse energy from the LSPs. We can also have 486 the squark decay in association with a  $W^{\pm}$  or  $Z^{0}$ ; in this thesis, we are interested in 487 those cases where this vector boson goes hadronically. 488

In the context of experimental searches for SUSY, we often consider *simplified* 

Figure 3.4: SUSY production cross-sections as a function of sparticle mass at  $\sqrt{s} = 13$  TeV.



models. These models make certain assumptions which allow easy comparisons of results by theorists and rival experimentalists. In the context of this thesis, the simplified models will make assumptions about the branching ratios described in the preceding paragraphs. In particular, we will often choose a model where the decay of interest occurs with 100% branching ratio. This is entirely for ease of interpretation by other physicists<sup>5</sup>, but it is important to recognize that these are more a useful comparison tool, especially with limits, than a strict statement about the potential masses of sought-after beyond the Standard Model particle.

<sup>&</sup>lt;sup>5</sup>In the author's opionion, this often leads to more confusion than comprehension. We will revisit the shortcomings of simplified models in the Conclusion to this thesis.

Figure 3.5: Loop diagrams correct the Higgs mass in the MSSM

$$\Delta(m_{h^0}^2) = h^0 - \begin{pmatrix} t \\ - - \end{pmatrix} + h^0 - \begin{pmatrix} \tilde{t} \\ - - \end{pmatrix} + h^0 - \begin{pmatrix} \tilde{t} \\ \tilde{t} \end{pmatrix} - - + h^0 - \begin{pmatrix} \tilde{t} \\ \tilde{t} \end{pmatrix} - - \end{pmatrix}$$

## 498 3.4 How SUSY solves the problems with the SM

We now return to the issues with the Standard Model as described in Ch.2 to see how these issues are solved by supersymmetry.

#### $_{501}$ Quadratic divergences to the Higgs mass

The quadratic divergences induced by the loop corrections to the Higgs mass, for example from the top Yukawa coupling, goes as

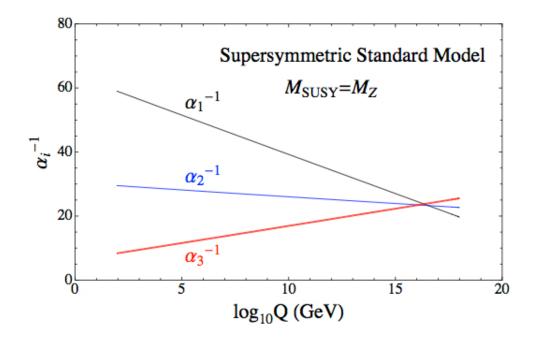
$$\delta m_H^2 \approx \left(\frac{m_t}{8\pi^2 < \phi >_{VEV}}\right)^2 \Lambda_{Planck}^2.$$
 (3.16)

The miraculous thing about SUSY is each of these terms *automatically* comes with a term which exactly cancels this contribution[15]. The fermions and bosons have opposite signs in this loop diagram to all orders in pertubation theory, which completely solves the hierarchy problem. This is the most well-motivated reason for supersymmetry.

#### 507 Gauge coupling unification

An additional motivation for supersymmetry is seen by the gauge coupling unification high scales. In the Standard Model, as we saw the gauge couplings fail to unify at high energies. In the MSSM and many other forms of supersymmetry, the gauge couplings unify at high energy, as can be seen in Fig.??. This provides additional aesthetic motivation for supersymmetric theories.

Figure 3.6: The running of Standard Model gauge couplings; compare to Fig.2.4. The MSSM gauge couplings nearly intersect at high energies.



#### $_{513}$ Dark matter

As we discussed previously, the lack of any dark matter candidate in the Standard 514 Model naturally leads to beyond the Standard Model theories. In the Standard Model, 515 there is a natural dark matter candidate in the lightest supersymmetric particle [15] 516 The LSP would in dark matter experiments be called a weakly-interacting massive 517 particle (WIMP), which is a type of cold dark matter [22, 84]. These WIMPS would 518 only interact through the weak force and gravity, which is exactly as a model like the 519 MSSM predicts for the neutralino. In Fig. 3.7, we can see the current WIMP exclusions 520 for a given mass. The range of allowed masses which have not been excluded for LSPs 521 and WIMPs have significant overlap. This provides additional motivation outside of 522 the context of theoretical details. 523

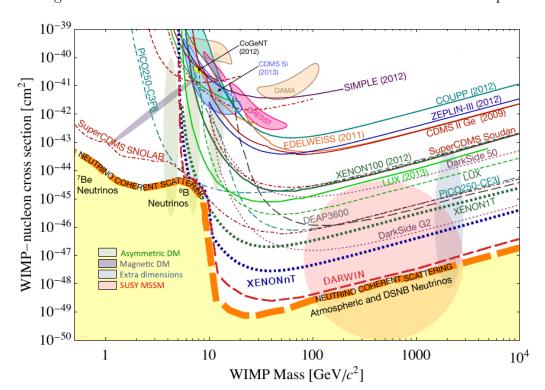


Figure 3.7: WIMP exclusions from direct dark matter detection experiments.

## 524 3.5 Conclusions

Supersymmetry is the most well-motivated theory for physics beyond the Standard 525 Model. It provides a solution to the hierarchy problem, leads to gauge coupling 526 unification, and provides a dark matter candidate consistent with galatic rotation 527 curves. As noted in this chapter, due to the LSPs in the final state, most SUSY 528 searches require a significant amount of missing transverse energy in combination 529 with jets of high transverse momentum. However, there is some opportunity to do 530 better than this, especially in final states where one has two weakly-interacting LSPs 531 on opposite sides of some potentially complicated decay tree. We will see how this is 532 done in Ch.??. 533

#### Chapter 4

535

534

# The Large Hadron Collider

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- 537 sentence its own line.
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# Magnets 4.1

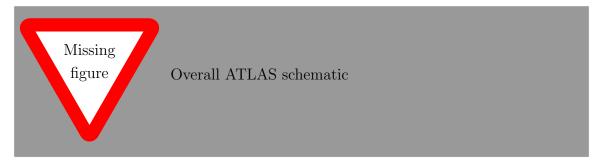
- 540 By using the asterisk to start a new section, I keep the section from appearing in the
- table of contents. If you want your sections to be numbered and to appear in the
- table of contents, remove the asterisk.

544

## The ATLAS detector

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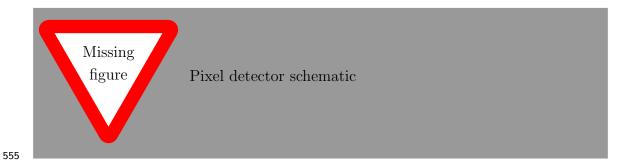
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#### 5.1 Inner Detector

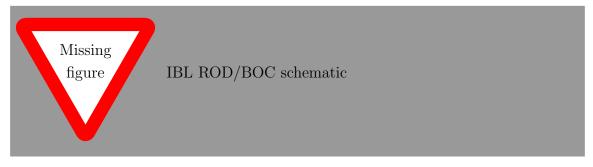
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#### 554 Pixel Detector

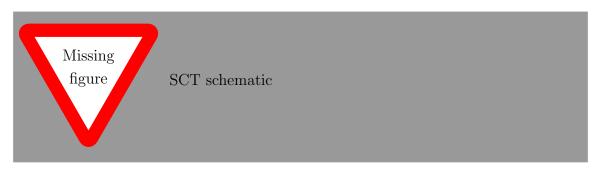


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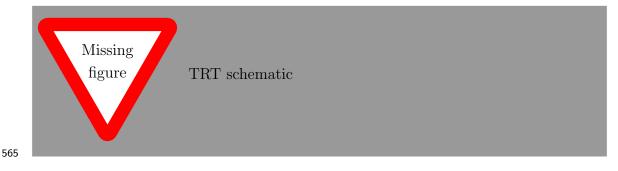
Qualification task, so add a bit more. 



## Semiconductor Tracker

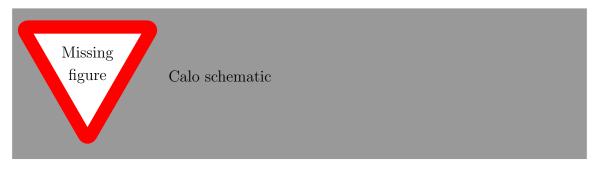


#### 564 Transition Radiation Tracker



566

# 567 5.2 Calorimeter

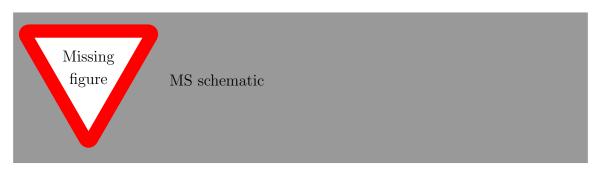


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# 570 Electromagnetic Calorimeter

#### 571 Hadronic Calorimeter

# 572 5.3 Muon Spectrometer



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#### Chapter 6

575

576

## The Recursive Jigsaw Technique

Here you can write some introductory remarks about your chapter. I like to give each sentence its own line.

When you need a new paragraph, just skip an extra line.

#### 6.1 Razor variables

By using the asterisk to start a new section, I keep the section from appearing in the table of contents. If you want your sections to be numbered and to appear in the table of contents, remove the asterisk.

# SuperRazor variables

## 585 6.3 The Recursive Jigsaw Technique

# Variables used in the search for zero lepton

## SUSY

588	Chapter 7		
589	Title of Chapter 1		

591

# Title of Chapter 1

- Here you can write some introductory remarks about your chapter. I like to give each sentence its own line.
- When you need a new paragraph, just skip an extra line.

# 595 8.1 Object reconstruction

596 Photons, Muons, and Electrons

597 **Jets** 

#### Missing transverse momentum

Probably longer, show some plots from the PUB note that we worked on

# 8.2 Signal regions

- 601 Gluino signal regions
- 602 Squark signal regions
- 603 Compressed signal regions

# 8.3 Background estimation

- 605 **Z** vv
- 606 **W** ev
- 607 ttbar

Chapter 9

608

609

Title of Chapter 1

610 Here you can write some introductory remarks about your chapter. I like to give each

- 611 sentence its own line.
- When you need a new paragraph, just skip an extra line.

# 9.1 Statistical Analysis

614 maybe to be moved to an appendix

# 9.2 Signal Region distributions

- 9.3 Pull Plots
- 9.4 Systematic Uncertainties
- 9.5 Exclusion plots

## Conclusion

- $\,$  Here you can write some introductory remarks about your chapter. I like to give each
- 621 sentence its own line.

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When you need a new paragraph, just skip an extra line.

# 9.6 New Section

- 624 By using the asterisk to start a new section, I keep the section from appearing in the
- 625 table of contents. If you want your sections to be numbered and to appear in the
- table of contents, remove the asterisk.

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#### The Standard Model

In this appendix, we provide a brief overview of the basic ingredients involved in construction of the Standard Model Lagrangian: quantum field theory, symmetries, and symmetry breaking.

## Quantum Field Theory

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In this section, we provide a brief overview of the necessary concepts from lectures

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Quantum Field Theory (QFT).

In modern physics, the laws of nature are described by the "action" S, with the imposition of the principle of minimum action. The action is the integral over the spacetime coordinates of the "Lagrangian density"  $\mathcal{L}$ , or Lagrangian for short. The Lagrangian is a function of "fields"; general fields will be called  $\phi(x^{\mu})$ , where the indices  $\mu$  run over the space-time coordinates. We can then write the action S as

$$S = \int d^4x \mathcal{L}[\phi_i(x^\mu), \partial_\mu \phi_i(x^\mu)]$$
 (9.1)

somehow

where we have an additional summation over i (of the different fields). Generally, we impose the following constraints on the Lagrangian:

- 1. Translational invariance The Lagrangian is only a function of the fields  $\phi$  and their derivatives  $\partial_{\mu}\phi$ 
  - 2. Locality The Lagrangian is only a function of one point  $x_{\mu}$  in spacetime.

- 3. Reality condition The Lagrangian is real to conserve probability.
- 4. Lorentz invariance The Lagrangian is invariant under the Poincarégroup of spacetime.
- 5. Analyticity The Lagrangian is an analytical function of the fields; this is to allow the use of pertubation theory.
- 6. Invariance and Naturalness The Lagrangian is invariant under some internal symmetry groups; in fact, the Lagrangian will have *all* terms allowed by the imposed symmetry groups.

# 7. Renormalizabilty - The Lagrangian will be renormalizable - in practice, this means there will not be terms with more than power 4 in the fields.

The key item from the point of view of this thesis is that of "Invariance and Natural". We impose a set of "symmetries" and then our Lagragian is the most general which is allowed by those symmetries.

#### 881 Symmetries

- Symmetries can be seen as the fundamental guiding concept of modern physics.
- Symmetries are described by "groups". To illustrate the importance of symmetries
- and their mathematical description, groups, we start here with two of the simplest
- and most useful examples:  $\mathbb{Z}_2$  and U(1).

#### 886 $\mathbb{Z}_2$ symmetry

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887  $\mathbb{Z}_2$ symmetry is the simplest example of a "discrete" symmetry. Consider the most 888 general Lagrangian of a single real scalar field  $\phi(x_{\mu})$ 

$$\mathcal{L}_{\phi} = \frac{1}{2} \partial_{\mu} \phi \partial^{\mu} \phi - \frac{m^2}{2} \phi^2 - \frac{\mu}{2\sqrt{2}} \phi^3 - \lambda \phi^4$$
 (9.2)

Now we *impose* the symmetry

$$\mathcal{L}(\phi) = \mathcal{L}(-\phi) \tag{9.3}$$

This has the effect of restricting the allowed terms of the Lagrangian. In particular, we can see the term  $\phi^3 \to -\phi^3$  under the symmetry transformation, and thus must be disallowed by this symmetry. This means under the imposition of this particular symmetry, our Lagrangian should be rewritten as

$$\mathcal{L}_{\phi} = \frac{1}{2} \partial_{\mu} \phi \partial^{\mu} \phi - \frac{m^2}{2} \phi^2 - \lambda \phi^4 \tag{9.4}$$

The effect of this symmetry is that the total number of  $\phi$  particles can only change by even numbers, since the only interaction term  $\lambda \phi^4$  is an even power of the field. This symmetry is often imposed in supersymmetric theories, as we will see in Chapter 3.

#### 897 U(1) symmetry

898 U(1) is the simplest example of a continuous (or Lie) group. Now consider a theory 899 with a single complex scalar field  $\phi = \text{Re } \phi + i \text{Im } \phi$ 

$$\mathcal{L}_{\phi} = \delta_{i,j} \frac{1}{2} \partial_{\mu} \phi_i \partial^{\mu} \phi_j - \frac{m^2}{2} \phi_i \phi_j - \frac{\mu}{2\sqrt{2}} \phi_i \phi_j \phi_k - \lambda \phi_i \phi_j \phi_k \phi_l$$
 (9.5)

where i, j, k, l = Re, Im. In this case, we impose the following U(1) symmetry  $\phi \to e^{i\theta}, \phi^* \to e^{-i\theta}$ . We see immediately that this again disallows the third-order terms, and we can write a theory of a complex scalar field with U(1) symmetry as

$$\mathcal{L}_{\phi} = \partial_{\mu}\phi \partial^{\mu}\phi^* - \frac{m^2}{2}\phi\phi^* - \lambda(\phi\phi^*)^2$$
(9.6)

#### 903 Local symmetries

The two examples considered above are "global" symmetries in the sense that the symmetry transformation does not depends on the spacetime coordinate  $x_{\mu}$ . We know look at local symmetries; in this case, for example with a local U(1) symmetry, the transformation has the form  $\phi(x_{\mu}) \to e^{i\theta(x_m u)}\phi(x_{\mu})$ . These symmetries are also known as "gauge" symmetries; all symmetries of the Standard Model are gauge symmetries.

There are wide-ranging consequences to the imposition of local symmetries. To begin, we note that the derivative terms of the Lagrangian 9.2 are *not* invariant under a local symmetry transformation

$$\partial_{\mu}\phi(x_{\mu}) \to \partial_{\mu}(e^{i}i\theta(x_{\mu})\phi(x_{\mu})) = (1 + i\theta(x_{\mu}))e^{i}i\theta(x_{\mu})\phi(x_{\mu}) \tag{9.7}$$

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This leads us to note that the kinetic terms of the Lagrangian are also not invariant under a gauge symmetry. This would lead to a model with no dynamics, which is clearly unsatisfactory.

Let us take inspiration from the case of global symmetries. We need to define a so-called "covariant" derivative  $D^{\mu}$  such that

$$D^{\mu}\phi \to e^{iq\theta(x^{\mu})D^{\mu}\phi} \tag{9.8}$$

$$D^{\mu}\phi^* \to e^{-iq\theta(x^{\mu})D^{\mu}\phi} \tag{9.9}$$

(9.10)

Since  $\phi$  and  $\phi^*$  transforms with the opposite phase, this will lead the invariance of the Lagrangian under our local gauge transformation. This  $D^{\mu}$  is of the following form

$$D^{\mu} = \partial_{\mu} - igqA^{\mu} \tag{9.11}$$

where  $A^{\mu}$  is a vector field we introduce with the transformation law

$$A^{\mu} \to A^{\mu} - \frac{1}{g} \partial_{\mu} \theta \tag{9.12}$$

and g is the coupling constant associated to vector field. This vector field  $A^{\mu}$  is also known as a "gauge" field.

Since we need to add all allowed terms to the Lagrangian, we define

$$F^{\mu\nu} = A^{\mu}A^{\nu} - A^{\nu}A^{\mu} \tag{9.13}$$

and then we must also add the kinetic term:

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$$\mathcal{L}_{\text{gauge}} = -\frac{1}{4} F^{\mu\nu} F_{\mu\nu} \tag{9.14}$$

The most general renormalizable Lagrangian with fermion and scalar fields can be written in the following form

$$\mathcal{L} = \mathcal{L}_{kin} + \mathcal{L}_{\phi} + \mathcal{L}_{\psi} + \mathcal{L}Yukawa \tag{9.15}$$

#### 925 Symmetry breaking and the Higgs mechanism

Here we view some examples of symmetry breaking. We investigate breaking of a global U(1) symmetry and a local U(1) symmetry. The SM will break the electroweak symmetry SU(2)xU(1), and in Chapter 3 we will see how supersymmetry must also be broken.

There are two ideas of symmetry breaking

• Explicit symmetry breaking by a small parameter - in this case, we have a small parameter which breaks an "approximate" symmetry of our Lagrangian. An example would be the theory of the single scalar field 9.2, when  $\mu << m^2$  and

 $\mu << \lambda$ . In this case, we can often ignore the small term when considering low-energy processes.

• Spontaneous symmetry breaking (SSB) - spontaneous symmetry breaking occurs when the Lagrangian is symmetric with respect to a given symmetry transformation, but the ground state of the theory is *not* symmetric with respect to that transformation. This can have some fascintating consequences, as we will see in the following examples

941 Symmetry breaking a

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#### $_{ m 942}$ m ~U(1) global symmetry breaking

Consider the theory of a complex scalar field under the U(1) symmetry, or the transformation

$$\phi \to e^{i\theta} \phi$$
 (9.16)

The Lagrangian for this theory is

$$\mathcal{L} = \partial^{\mu} \phi^{\dagger} \partial_{\mu} \phi + \frac{\mu^2}{2} \phi^{\dagger} \phi + \frac{\lambda}{4} (\phi^{\dagger} \phi)^2$$
 (9.17)

Let us write this theory in terms of two scalar fields, h and  $\xi$ :  $\phi = (h+i\xi)/\sqrt(2)$ . The Lagrangian can then be written as

$$\mathcal{L} = \partial^{\mu} h \partial_{\mu} h + \partial^{\mu} \xi dm u \xi - \frac{\mu^{2}}{2} (h^{2} + \xi^{2}) - \frac{\lambda}{4} (h^{2} + \xi^{2})^{2}$$
 (9.18)

First, note that the theory is only stable when  $\lambda > 0$ . To understand the effect of SSB, we now enforce that  $\mu^2 < 0$ , and define  $v^2 = -\mu^2/\lambda$ . We can then write the scalar potential of this theory as:

$$V(\phi) = \lambda (\phi^{\dagger} \phi - v^2/2)^2 \tag{9.19}$$

Minimizing this equation with respect to  $\phi$ , we can see that the "vacuum expectation value" of the theory is

$$2 < \phi^{\dagger} \phi > = < h^2 + \xi^2 > = v^2 \tag{9.20}$$

We now reach the "breaking" point of this procedure. In the  $(h, \xi)$  plane, the minima form a circle of radius v. We are free to choose any of these minima to expand our Lagrangian around; the physics is not affected by this choice. For convenience, choose  $< h >= v, < \xi^2 >= 0$ .

Now, let us define  $h' = h - v, \xi' = \xi$  with VEVs  $< h' >= 0, < \xi' >= 0$ . We can then write our spontaneously broken Lagrangian in the form

$$\mathcal{L} = \frac{1}{2} \partial_{\mu} h' \partial^{\mu} h' + \frac{1}{2} \partial_{\mu} \xi' \partial^{\mu} \xi' - \lambda v^2 h'^2 - \lambda v h' (h'^2 + \xi'^2) - \lambda (h'^2 + \xi'^2)^2$$
 (9.21)