

1 A search for sparticles in zero lepton final states

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## ABSTRACT

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A search for sparticles in zero lepton final states

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*Acknowledgements*



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*Dedication*



*Introduction*

67 Particle physics is a remarkably successful field of scientific inquiry. The ability to  
 68 precisely predict the properties of a exceedingly wide range of physical phenomena,  
 69 such as the description of the cosmic microwave background [1, 2], the understanding  
 70 of the anomalous magnetic dipole moment of the electron [3, 4], and the measurement  
 71 of the number of weakly-interacting neutrino flavors [5] is truly amazing.

72 The theory that has allowed this range of predictions is the *Standard Model*  
 73 of particle physics (SM). The Standard Model combines the electroweak theory of  
 74 Glashow, Weinberg, and Salam [6–8] with the theory of the strong interactions, as  
 75 first envisioned by Gell-Mann and Zweig [9, 10]. This quantum field theory (QFT)  
 76 contains a tiny number of particles, whose interactions describe phenomena up to at  
 77 least the TeV scale. These particles are manifestations of the fields of the Standard  
 78 Model, after application of the Higgs Mechanism. The particle content of the SM  
 79 consists only of the six quarks, the six leptons, the four gauge bosons, and the scalar  
 80 Higgs boson.

81 Despite its impressive range of described phenomena, the Standard Model has  
 82 some theoretical and experimental deficiencies. The SM contains 26 free parameters  
 83 <sup>1</sup>. It would be more theoretically pleasing to understand these free parameters in  
 84 terms of a more fundamental theory. The major theoretical concern of the Standard  
 85 Model, as it pertains to this thesis, is the *hierarchy problem*[11–15]. The light mass

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<sup>1</sup>This is the Standard Model corrected to include neutrino masses. These parameters are the fermion masses (6 leptons, 6 quarks), CKM and PMNS mixing angles (8 angles, 2 CP-violating phases), W/Z/Higgs masses (3), the Higgs field expectation value, and the couplings of the strong, weak, and electromagnetic forces (3  $\alpha_{force}$  ).

86 of the Higgs boson (125 GeV) should be quadratically dependent on the scale of UV  
87 physics, due to the quantum corrections from high-energy physics processes. The  
88 most perplexing experimental issue is the existence of *dark matter*, as demonstrated  
89 by galactic rotation curves [16–22]. This data has shown that there exists additional  
90 matter which has not yet been seen interacting with the particles of the Standard  
91 Model. There is no particle in the SM which can act as a candidate for dark matter.

92 Both of these major issues, as well as numerous others, can be solved by the  
93 introduction of *supersymmetry* (SUSY) [15, 23–35]. In supersymmetric theories, each  
94 SM particles has a so-called *superpartner*, or sparticle partner, differing from given SM  
95 particle by 1/2 in spin. These theories solve the hierarchy problem, since the quantum  
96 corrections induced from the superpartners exactly cancel those induced by the SM  
97 particles. In addition, these theories are usually constructed assuming *R*–parity,  
98 which can be thought of as the “charge” of supersymmetry, with SM particles having  
99  $R = 1$  and sparticles having  $R = -1$ . In collider experiments, since the incoming  
100 SM particles have total  $R = 1$ , the resulting sparticles are produced in pairs. This  
101 produces a rich phenomenology, which is characterized by significant hadronic activity  
102 and large missing transverse energy ( $E_T^{\text{miss}}$ ), which provide significant discrimination  
103 against SM backgrounds [36].

104 Despite the power of searches for supersymmetry where  $E_T^{\text{miss}}$  is a primary  
105 discriminating variable, there has been significant interest in the use of other variables  
106 to discriminate against SM backgrounds. These include searches employing variables  
107 such as  $\alpha T$ ,  $M_{T,2}$ , and the razor variables ( $M_R, R^2$ ) [37–47]. In this thesis, we  
108 will present the first search for supersymmetry using the novel Recursive Jigsaw  
109 Reconstruction (RJR) technique. RJR can be considered the conceptual successor  
110 of the razor variables. We impose a particular final state “decay tree” on an events,  
111 which roughly corresponds to a simplified Feynmann diagram in decays containing  
112 weakly-interacting particles. We account for the missing degrees of freedom associated

113 to the weakly-interacting particles by a series of simplifying assumptions, which allow  
114 us to calculate our variables of interest at each step in the decay tree. This allows an  
115 unprecedented understanding of the internal structure of the decay and the ability to  
116 construct additional variables to reject Standard Model backgrounds.

117 This thesis details a search for the superpartners of the gluon and quarks, the  
118 gluino and squarks, in final states with zero leptons, with  $13.3 \text{ fb}^{-1}$  of data using the  
119 ATLAS detector. We organize the thesis as follows. The theoretical foundations of  
120 the Standard Model and supersymmetry are described in Chapters 2 and 3. The  
121 Large Hadron Collider and the ATLAS detector are presented in Chapters 4 and 5.  
122 Chapter 5 provides a detailed description of Recursive Jigsaw Reconstruction and a  
123 description of the variables used for the particular search presented in this thesis.  
124 Chapter 6 presents the details of the analysis, including details of the dataset, object  
125 reconstruction, and selections used. In Chapter 7, the final results are presented;  
126 since there is no evidence of a supersymmetric signal in the analysis, we present the  
127 final exclusion curves in simplified supersymmetric models.



*The Standard Model***130 2.1 Overview**

131 A Standard Model is another name for a theory of the internal symmetry group  
 132  $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$ , with its associated set of parameters. *The Standard*  
 133 Model refers specifically to a Standard Model with the proper parameters to describe  
 134 the universe. The SM is the culmination of years of work in both theoretical  
 135 and experimental particle physics. In this thesis, we take the view that theorists cite

136 construct a model with the field content and symmetries as inputs, and write down the  
 137 most general Lagrangian consistent with those symmetries. Assuming this model is  
 138 compatible with nature (in particular, the predictions of the model are consistent with  
 139 previous experiments), experimentalists are responsible measuring the parameters of  
 140 this model. This will be applicable for this chapter and the following one.

141 Additional theoretical background is in ?? . The philosophy and notations are  
 142 inspired by [48, 49].

**143 2.2 Field Content**

The Standard Model field content is

$$\begin{aligned}
 \text{Fermions} &: Q_L(3, 2)_{+1/3}, U_R(3, 1)_{+4/3}, D_R(3, 1)_{-2/3}, L_L(1, 2)_{-1}, E_R(1, 1)_{-2} \\
 \text{Scalar (Higgs)} &: \phi(1, 2)_{+1} \\
 \text{Vector Fields} &: G^\mu(8, 1)_0, W^\mu(1, 3)_0, B^\mu(1, 1)_0
 \end{aligned} \tag{2.1}$$

144 where the  $(A, B)_Y$  notation represents the irreducible representation under  $SU(3)$   
145 and  $SU(2)$ , with  $Y$  being the electroweak hypercharge. Each of these fermion fields  
146 has an additional index, representing the three generation of fermions.

147 We observed that  $Q_L, U_R$ , and  $D_R$  are triplets under  $SU(3)_C$ ; these are the *quark*  
148 fields. The *color* group,  $SU(3)_C$  is mediated by the *gluon* field  $G^\mu(8, 1)_0$ , which has  
149 8 degrees of freedom. The fermion fields  $L_L(1, 2)_{-1}$  and  $E_R(1, 1)_{-2}$  are singlets under  
150  $SU(3)_C$ ; we call them the *lepton* fields.

151 Next, we note the “left-handed” (“right-handed”) fermion fields, denoted by  $L$  ( $R$ )  
152 subscript, The left-handed fields form doublets under  $SU(2)_L$ . These are mediated  
153 by the three degrees of freedom of the “W” fields  $W^\mu(1, 3)_0$ . These fields only act  
154 on the left-handed particles of the Standard Model. This is the reflection of the  
155 “chirality” of the Standard Model; the left-handed and right-handed particles are  
156 treated differently by the electroweak forces. The right-handed fields,  $U_R, D_R$ , and  
157  $E_R$ , are singlets under  $SU(2)_L$ .

158 The  $U(1)_Y$  symmetry is associated to the  $B^\mu(1, 1)_0$  boson with one degree of  
159 freedom. The charge  $Y$  is known as the electroweak hypercharge.

160 To better understand the phenomenology of the Standard Model, let us investigate  
161 each of the *sectors* of the Standard Model separately.

## 162 Electroweak sector

The electroweak sector refers to the  $SU(2)_L \otimes U(1)_Y$  portion of the Standard  
Model gauge group. Following our philosophy of writing all gauge-invariant and  
renormalizable terms, the electroweak Lagrangian can be written as

$$\mathcal{L} = W_a^{\mu\nu} W_{\mu\nu}^a + B^{\mu\nu} B_{\mu\nu} + (D^\mu \phi)^\dagger D_\mu \phi - \mu^2 \phi^\dagger \phi - \lambda (\phi^\dagger \phi)^2. \quad (2.2)$$

where  $W_a^{\mu\nu}$  are the three ( $a = 1, 2, 3$ ) gauge bosons associated to the  $SU(2)_L$  gauge  
group,  $B^{\mu\nu}$  is the one gauge boson of the  $U(1)_Y$  gauge group, and  $\phi$  is the complex

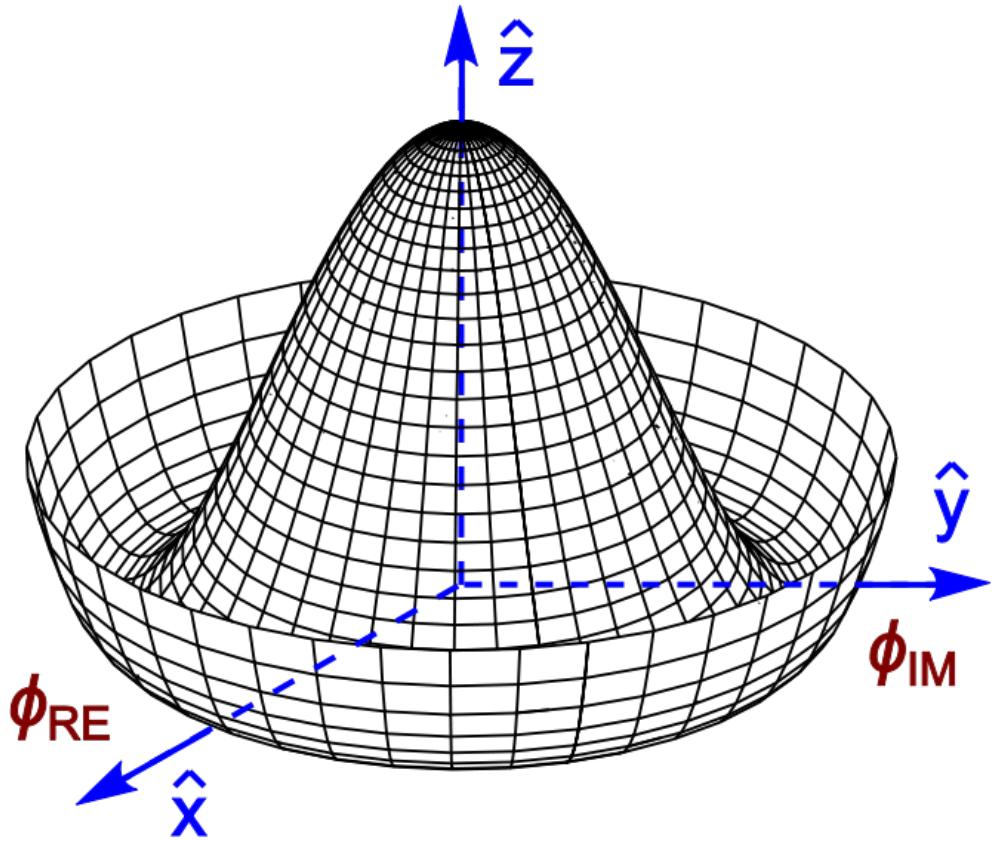


Figure 2.1: Sombrero potential

Higgs multiplet. The covariant derivative  $D^\mu$  is given by

$$D^\mu = \partial^\mu + \frac{ig}{2}W_a^\mu\sigma_a + \frac{ig'}{2}B^\mu \quad (2.3)$$

where  $i\sigma_a$  are the Pauli matrices times the imaginary constant, which are the generators for  $SU(2)_L$ , and  $g$  and  $g'$  are the  $SU(2)_L$  and  $U(1)_Y$  coupling constants, respectively. The field strength tensors  $W_a^{\mu\nu}$  and  $B^{\mu\nu}$  are given by the commutator of the covariant derivative associated to each field

$$B^{\mu\nu} = \partial^\mu B^\nu - \partial^\nu B^\mu \quad (2.4)$$

$$W_a^{\mu\nu} = \partial^\mu W_a^\nu - \partial^\nu W_a^\mu - g\epsilon_{abc}W_a^\mu W_b^\nu, \quad i = 1, 2, 3$$

164      The terms in the Lagrangian 2.2 proportional to  $\mu^2$  and  $\lambda$  make up the “Higgs  
 165 potential” [50]. As normal (see Appendix ??), we restrict  $\lambda > 0$  to guarantee our  
 166 potential is bounded from below, and we also require  $\mu^2 < 0$ , which gives us the  
 167 standard “sombrero” potential shown in 2.1.

This potential has infinitely many minima at  $\langle \phi \rangle = \sqrt{2m/\lambda}$ ; the ground state is *spontaneously* broken by the choice of ground state, which induces a vacuum expectation value (VEV). Without loss of generality, we can choose the Higgs field  $\phi$  to point in the real direction, and write the Higgs field  $\phi$  in the following form :

$$\phi = \frac{1}{\sqrt{2}} \exp\left(\frac{i}{v} \sigma_a \theta_a\right) \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}. \quad (2.5)$$

We choose a gauge to rotate away the dependence on  $\theta_a$ , such that we can write simply

$$\phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}. \quad (2.6)$$

Now, we can see how the masses of the vector bosons are generated from the application of the Higgs mechanism. We plug Eq.2.6 back into the electroweak Lagrangian, and only showing the relevant mass terms in the vacuum state where  $h(x) = 0$  see that (dropping the Lorentz indices) :

$$\begin{aligned} \mathcal{L}_M &= \frac{1}{8} \left| \begin{pmatrix} gW_3 + g'B & g(W_1 - iW_2) \\ g(W_1 + iW_2) & -gW_3 + g'B \end{pmatrix} \begin{pmatrix} 0 \\ v \end{pmatrix} \right|^2 \\ &= \frac{g^2 v^2}{8} \left[ W_1^2 + W_2^2 + \left( \frac{g'}{g} B - W_3 \right)^2 \right] \end{aligned} \quad (2.7)$$

Defining the Weinberg angle  $\tan(\theta_W) = g'/g$  and the following *physical* fields :

$$W^\pm = \frac{1}{\sqrt{2}} (W_1 \mp iW_2) \quad (2.8)$$

$$Z^0 = \cos \theta_W W_3 - \sin \theta_W B$$

$$A^0 = \sin \theta_W W_3 + \cos \theta_W B$$

we can write the piece of the Lagrangian associated to the vector boson masses as

$$\mathcal{L}_{MV} = \frac{1}{4}g^2 v^2 W^+ W^- + \frac{1}{8}(g^2 + g'^2)v^2 Z^0 Z^0. \quad (2.9)$$

and we have the following values of the masses for the vector bosons :

$$\begin{aligned} m_W^2 &= \frac{1}{4}v^2 g^2 \\ m_Z^2 &= \frac{1}{4}v^2(g^2 + g'^2) \\ m_A^2 &= 0 \end{aligned} \quad (2.10)$$

We thus see how the Higgs mechanism gives rise to the masses of the  $W^\pm$  and  $Z$  boson in the Standard Model; the mass of the photon is zero, as expected. The  $SU(2)_L \otimes U(1)_Y$  symmetry of the initially massless  $W_{1,2,3}$  and  $B$  fields is broken to the  $U(1)_{EM}$ . Of the four degrees of freedom in the complex Higgs doublet, three are “eaten” when we give mass to the  $W^\pm$  and  $Z_0$ , while the other degree of freedom is the Higgs particle, as found in 2012 by the ATLAS and CMS collaborations [51, 52].

## **174 Quantum Chromodynamics**

Quantum chromodynamics (or the theory of the *strong* force) characterizes the behavior of *colored* particles, collectively known as *partons*. The partons of the Standard Model are the (fermionic) quarks, and the (bosonic) gluons. The strong force is governed by  $SU(3)_C$ , an unbroken symmetry in the Standard Model, which implies the gluon remains massless. Defining the covariant derivative for QCD as

$$D^\mu = \partial^\mu + ig_s G_a^\mu L_a, a = 1, \dots, 8 \quad (2.11)$$

where  $L_a$  are the generators of  $SU(3)_C$ , and  $g_s$  is the coupling constant of the strong force. The QCD Lagrangian then is given by

$$\mathcal{L}_{QCD} = i\bar{\psi}_f D_\mu \gamma^\mu \psi_f - \frac{1}{4}G_{a,\mu\nu} G_a^{\mu\nu} \quad (2.12)$$

where the summation over  $f$  is for quarks *families*, and  $G_a^{\mu\nu}$  is the gluon field strength tensor, given by

$$G_a^{\mu\nu} = \partial^\mu G_a^\nu - \partial^\nu G_a^\mu - g_s f^{abc} G_b^\mu G_c^\nu, a, b, c = 1, \dots, 8 \quad (2.13)$$

175 where  $f^{abc}$  are the structure constants of  $SU(3)_C$ , which are analogous to  $\epsilon_{abc}$  for  
 176  $SU(2)_L$ . The kinetic term for the quarks is contained in the standard  $\partial_\mu$  term, while  
 177 the field strength term contains the interactions between the quarks and gluons, as  
 178 well as the gluon self-interactions.

179 Written down in this simple form, the QCD Lagrangian does not seem much  
 180 different from the QED Lagrangian, with the proper adjustments for the different  
 181 group structures. The gluon is massless, like the photon, so one could naïvely expect  
 182 an infinite range force, and it pays to understand why this is not the case. The  
 183 reason for this fundamental difference is the gluon self-interactions arising in the  
 184 field strength tensor term of the Lagrangian. This leads to the phenomena of *color*  
 185 *confinement*, which describes how one only observes color-neutral particles alone in  
 186 nature. In contrast to the electromagnetic force, particles which interact via the  
 187 strong force experience a *greater* force as the distance between the particles increases.  
 188 At long distances, the potential is given by  $V(r) = -kr$ . At some point, it is more  
 189 energetically favorable to create additional partons out of the vacuum than continue  
 190 pulling apart the existing partons, and the colored particles undergo *fragmentation*.  
 191 This leads to *hadronization*. Bare quarks and gluons are actually observed as sprays  
 192 of hadrons (primarily kaons and pions); these sprays are known as *jets*, which are  
 193 what are observed by experiments.

194 It is important to recognize the importance of understanding these QCD inter-  
 195 actions in high-energy hadron colliders such as the LHC. Since protons are hadrons,  
 196 proton-proton collisions such as those produced by the LHC are primarily governed by  
 197 the processes of QCD. In particular, by far the most frequent process observed in LHC  
 198 experiments is dijet production from gluon-gluon interactions (see Fig.2.2). These

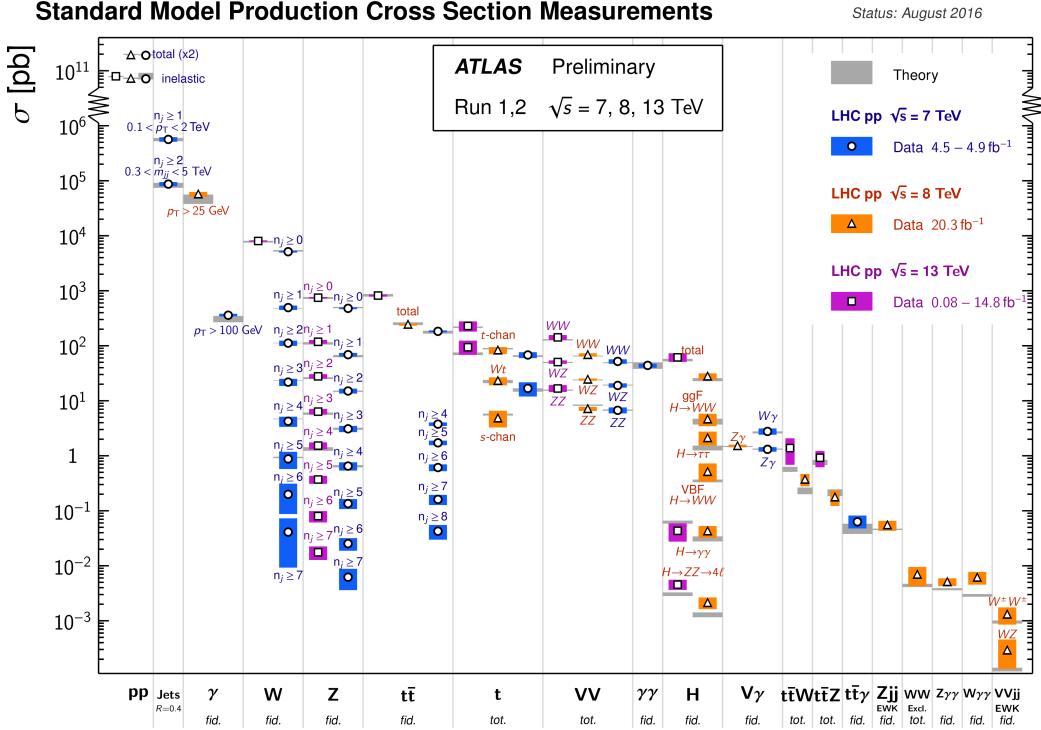


Figure 2.2: Cross-sections of various Standard Model processes

199 gluons that interact are part of the *sea* particles inside the proton; the simple  $p = uud$   
 200 model does not apply. The main *valence*  $uud$  quarks are constantly interacting via  
 201 gluons, which can themselves radiate gluons or split into quarks, and so on. A more  
 202 useful understanding is given by the colloquially-known *bag* model [53, 54], where the  
 203 proton is seen as a “bag” of (in principle) infinitely many partons, each with energy  
 204  $E < \sqrt{s} = 6.5$  TeV. One then collides this (proton) bag with another, and views the  
 205 products of this very complicated collision, where calculations include many loops in  
 206 nonperturbative QCD calculations.

207 Fortunately, we are generally saved by the QCD factorization theorems [55]. This  
 208 allows one to understand the hard (i.e. short distance or high energy)  $2 \rightarrow 2$  parton  
 209 process using the tools of perturbative QCD, while making series of approximations  
 210 known as a *parton shower* model to understand the additional corrections from  
 211 nonperturbative QCD. We will discuss the reconstruction of jets by experiments in  
 212 Ch.5.

213 **Fermions**

214 We will now look more closely at the fermions in the Standard Model [56].

215 As noted earlier in Sec.2.2, the fermions of the Standard Model can be first  
 216 distinguished between those that interact via the strong force (quarks) and those  
 217 which do not (leptons).

There are six leptons in the Standard Model, which can be placed into three  
*generations*.

$$\begin{pmatrix} e \\ \nu_e \end{pmatrix}, \begin{pmatrix} \mu \\ \nu_\mu \end{pmatrix}, \begin{pmatrix} \tau \\ \nu_\tau \end{pmatrix} \quad (2.14)$$

218 There is the electron ( $e$ ), muon ( $\mu$ ), and tau ( $\tau$ ), each of which has an associated  
 219 neutrino ( $\nu_e, \nu_\mu, \nu_\tau$ ). Each of the so-called charged (“electron-like”) leptons has  
 220 electromagnetic charge  $-1$ , while the neutrinos all have  $q_{EM} = 0$ .

221 Often in an experimental context, lepton is used to denote the stable electron  
 222 and metastable muon, due to their striking experimental signatures. Taus are often  
 223 treated separately, due to their much shorter lifetime of  $\tau_\tau \sim 10^{-13}s$ ; these decay  
 224 through hadrons or the other leptons, so often physics analyses at the LHC treat  
 225 them as jets or leptons, as will be done in this thesis.

226 As the neutrinos are electrically neutral, nearly massless, and only interact via the  
 227 weak force, it is quite difficult to observe them directly. Since LHC experiments rely  
 228 overwhelmingly on electromagnetic interactions to observe particles, the presence of  
 229 neutrinos is not observed directly. Neutrinos are instead observed by the conservation  
 230 of four-momentum in the plane transverse to the proton-proton collisions, known as  
 231 *missing transverse energy*.

There are six quarks in the Standard Model : up, down, charm, strange, top, and  
 bottom. Quarks are similar organized into three generations :

$$\begin{pmatrix} u \\ d \end{pmatrix}, \begin{pmatrix} c \\ s \end{pmatrix}, \begin{pmatrix} t \\ b \end{pmatrix} \quad (2.15)$$

232 where we speak of “up-like” quarks and “down-like” quarks.

233 Each up-like quark has charge  $q_{up} = 2/3$ , while the down-like quarks have  $q_{down} =$   
234  $-1/3$ . At the high energies of the LHC, one often makes the distinction between  
235 the light quarks ( $u, d, c, s$ ), the bottom quark, and top quark. In general, due to  
236 the hadronization process described above, the light quarks, with masses  $m_q < \sim$   
237  $1.5\text{GeV}$  are indistinguishable by LHC experiments. Their hadronic decay products  
238 generally have long lifetimes and they are reconstructed as jets.<sup>1</sup>. The bottom quark  
239 hadronizes primarily through the  $B$ -mesons, which generally travels a short distance  
240 before decaying to other hadrons. This allows one to distinguish decays via  $b$ -quarks  
241 from other jets; this procedure is known as *b-tagging* and will be discussed more in  
242 Ch.5. Due to its large mass, the top quark decays before it can hadronize; there  
243 are no bound states associated to the top quark. The top is of particular interest at  
244 the LHC; it has a striking signature through its most common decay mode  $t \rightarrow Wb$ .  
245 Decays via tops, especially  $t\bar{t}$  are frequently an important signal decay mode, or an  
246 important background process.

## 247 **Interactions in the Standard Model**

248 We briefly overview the entirety of the fundamental interactions of the Standard  
249 Model; these can also be found in 2.3.

250 The electromagnetic force, mediated by the photon, interacts with via a three-  
251 point coupling all charged particles in the Standard Model. The photon thus interacts  
252 with all the quarks, the charged leptons, and the charged  $W^\pm$  bosons.

253 The weak force is mediated by three particles : the  $W^\pm$  and the  $Z^0$ . The  $Z^0$  can  
254 interacts with all fermions via a three-point coupling. A real  $Z_0$  can thus decay to  
255 a fermion-antifermion pair of all SM fermions except the top quark, due to its large

---

<sup>1</sup>In some contexts, charm quarks are also treated as a separate category, although it is quite difficult to distinguish charm quarks from the other light quarks.

## Standard Model Interactions (Forces Mediated by Gauge Bosons)



Figure 2.3: The interactions of the Standard Model

mass. The  $W^\pm$  has two important three-point interactions with fermions. First, the  $W^\pm$  can interact with an up-like quark and a down-like quark; an important example in LHC experiments is  $t \rightarrow Wb$ . The coupling constants for these interactions are encoded in the unitary matrix known as the Cabibbo–Kobayashi–Maskawa (CKM) matrix [57, 58], and are generally known as flavor-changing interactions. Secondly, the  $W^\pm$  interacts with a charged lepton and its corresponding neutrino. In this case, the unitary matrix that corresponds to CKM matrix for quarks is the identity matrix, which forbids (fundamental) vertices such as  $\mu \rightarrow We$ . For leptons, instead this is a two-step process :  $\mu \rightarrow \nu_m u W \rightarrow \nu_m u \bar{\nu}_e e$ . Finally, there are the self-interactions

265 of the weak gauge bosons. There is a three-point and four-point interaction; all  
266 combinations are allowed which conserve electric charge.

267 The strong force is mediated by the gluon, which as discussed above also carries  
268 the strong color charge. There is the fundamental three-point interaction, where a  
269 quark radiates a gluon. Additionally, there are the three-point and four-point gluon-  
270 only interactions.

## 271 2.3 Deficiencies of the Standard Model

272 At this point, it is quite easy to simply rest on our laurels. This relatively simple  
273 theory is capable of explaining a very wide range of phenomena, which ultimately  
274 break down only to combinations of nine diagrams shown in Fig.2.3. Unfortunately,  
275 there are some unexplained problems with the Standard Model. We cannot go  
276 through all of the potential issues in this thesis, but we will motivate the primary  
277 issues which naturally lead one to *supersymmetry*, as we will see in Ch.3.

The Standard Model has many free parameters; see Table 2.1 In general, we prefer models with less free parameters. A great example of this fact, and the primary experimental evidence for EWSB, is the relationship between the couplings of the weak force and the masses of the gauge bosons of the weak force :

$$\rho \equiv \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} \stackrel{?}{=} 1 \quad (2.16)$$

278 where ? indicates that this is a testable prediction of the Standard Model (in  
279 particular, that the gauge bosons gain mass through EWSB). This relationship has  
280 been measured within experimental and theoretical predictions. We would like to  
281 produce additional such relationships, which would exist if the Standard Model is a  
282 low-energy approximation of some other theory.

283 An additional issue is the lack of *gauge coupling unification*. The couplings of  
284 any quantum field theory “run” as a function of the distance scales (or inversely,

$m_e$	Electron mass	511 keV
$m_\mu$	Muon mass	105.7 MeV
$m_\tau$	Tau mass	1.78 GeV
$m_u$	Up quark mass	1.9 MeV ( $m_{\bar{MS}} = 2\text{GeV}$ )
$m_d$	Down quark mass	4.4 MeV ( $m_{\bar{MS}} = 2\text{GeV}$ )
$m_s$	Strange quark mass	87 MeV ( $m_{\bar{MS}} = 2\text{GeV}$ )
$m_c$	Charm quark mass	1.32 GeV ( $m_{\bar{MS}} = m_c$ )
$m_b$	Bottom quark mass	4.24 GeV ( $m_{\bar{MS}} = m_b$ )
$m_t$	Top quark mass	172.7 GeV (on-shell renormalization)
$\theta_{12}$ CKM	12-mixing angle	13.1°
$\theta_{23}$ CKM	23-mixing angle	2.4°
$\theta_{13}$ CKM	13-mixing angle	0.2°
$\delta$ CKM	CP-violating Phase	0.995
$g'$	U(1) gauge coupling	0.357 ( $m_{\bar{MS}} = m_Z$ )
$g$	SU(2) gauge coupling	0.652 ( $m_{\bar{MS}} = m_Z$ )
$g_s$	SU(3) gauge coupling	1.221 ( $m_{\bar{MS}} = m_Z$ )
$\theta_{QCD}$	QCD vacuum angle	~0
VEV	Higgs vacuum expectation value	246 GeV
$m_H$	Higgs mass	125 GeV

Table 2.1: Parameters of the Standard Model. For values dependent on the renormalization scheme, we use a combination of the on-shell normalization scheme [59–62] and modified minimal subtraction scheme with  $m_{\bar{MS}}$  as indicated in the table[63]

285 energy scales) of the theory. The idea is closely related to the unification of the  
 286 electromagnetic and weak forces at the so-called *electroweak scale* of  $O(100 \text{ GeV})$ .  
 287 One would hope this behavior was repeated between the electroweak forces and the  
 288 strong force at some suitable energy scale. The Standard Model does automatically  
 289 not exhibit this behavior, as we can see in Fig.2.4.

The most significant problem with the Standard Model is the *hierarchy problem*. In its most straightforward incarnation, the Higgs scalar field is subject to quantum corrections through loop diagrams, as shown in Fig.2.5. For demonstration, we use the contributions from the top quark, since the top quark has the largest Higgs Yukawa coupling due to its large mass. In general, we should expect these corrections to quadratically depend on the scale of the ultraviolet physics,  $\Lambda$ . Briefly assume there is no new physics before the Planck scale of gravity,  $\Lambda_{\text{Planck}} = 10^{19} \text{ GeV}$ . In this

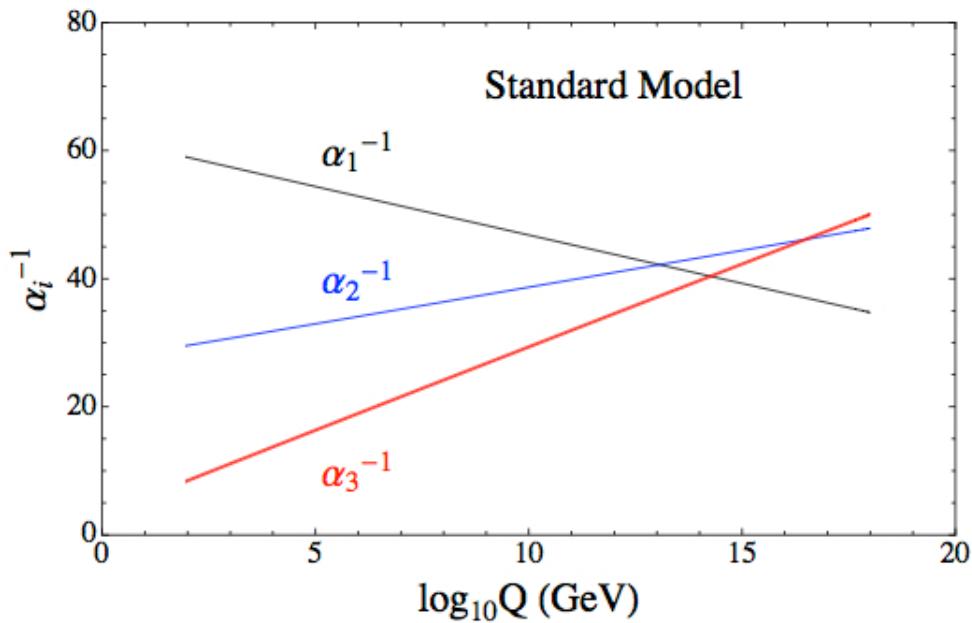


Figure 2.4: The running of Standard Model gauge couplings. The Standard Model couplings do not unify at high energies, which indicates it cannot completely describe nature through the Planck scale.

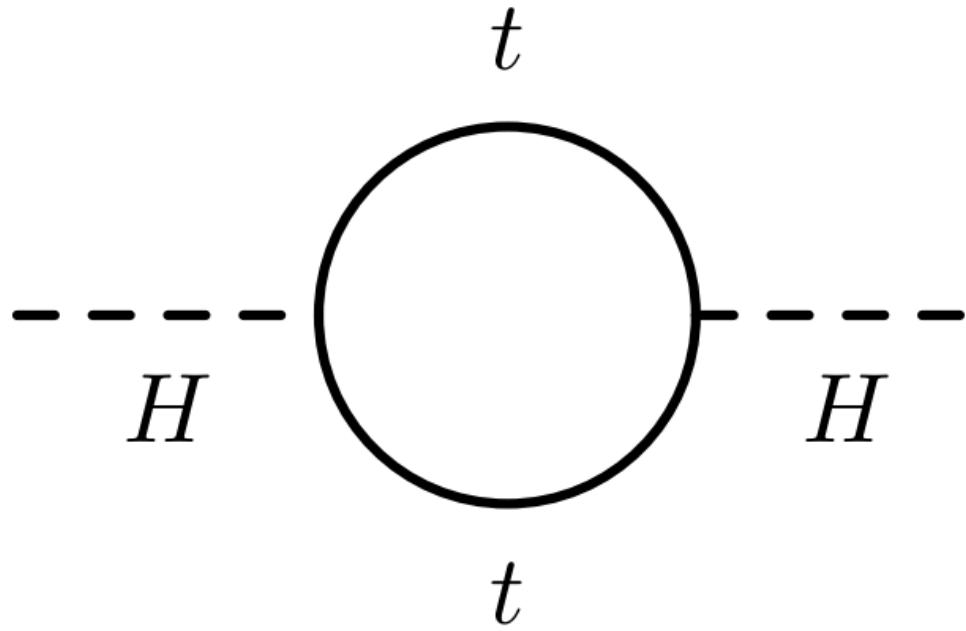


Figure 2.5: The dominant quantum loop correction to the Higgs mass in the Standard Model.

case, we expect the corrections to the Higgs mass like

$$\delta m_H^2 \approx \left( \frac{m_t}{8\pi^2 \langle \phi \rangle_{VEV}} \right)^2 \Lambda_{Planck}^2. \quad (2.17)$$

To achieve the miraculous cancellation required to get the observed Higgs mass of 125 GeV, one needs to then set the bare Higgs mass  $m_0$ , our input to the Standard Model Lagrangian, itself to a *precise* value  $\sim 10^{19}$  GeV. This extraordinary level of parameter finetuning is quite undesirable, and within the framework of the Standard Model, there is little that can be done to alleviate this issue.

An additional concern, of a different nature, is the lack of a *dark matter* candidate in the Standard Model. Dark matter was discovered by observing galactic rotation curves, which showed that much of the matter that interacted gravitationally was invisible to our (electromagnetic) telescopes [16–22]. The postulation of the existence of dark matter, which interacts at least through gravity, allows one to understand these galactic rotation curves. Unfortunately, no particle in the Standard Model could possibly be the dark matter particle. The only candidate truly worth another look is the neutrino, but it has been shown that the neutrino content of the universe is simply too small to explain the galactic rotation curves [22, 64]. The experimental evidence from the galactic rotations curves thus show there *must* be additional physics beyond the Standard Model, which is yet to be understood.

In the next chapter, we will see how these problems can be alleviated by the theory of supersymmetry.

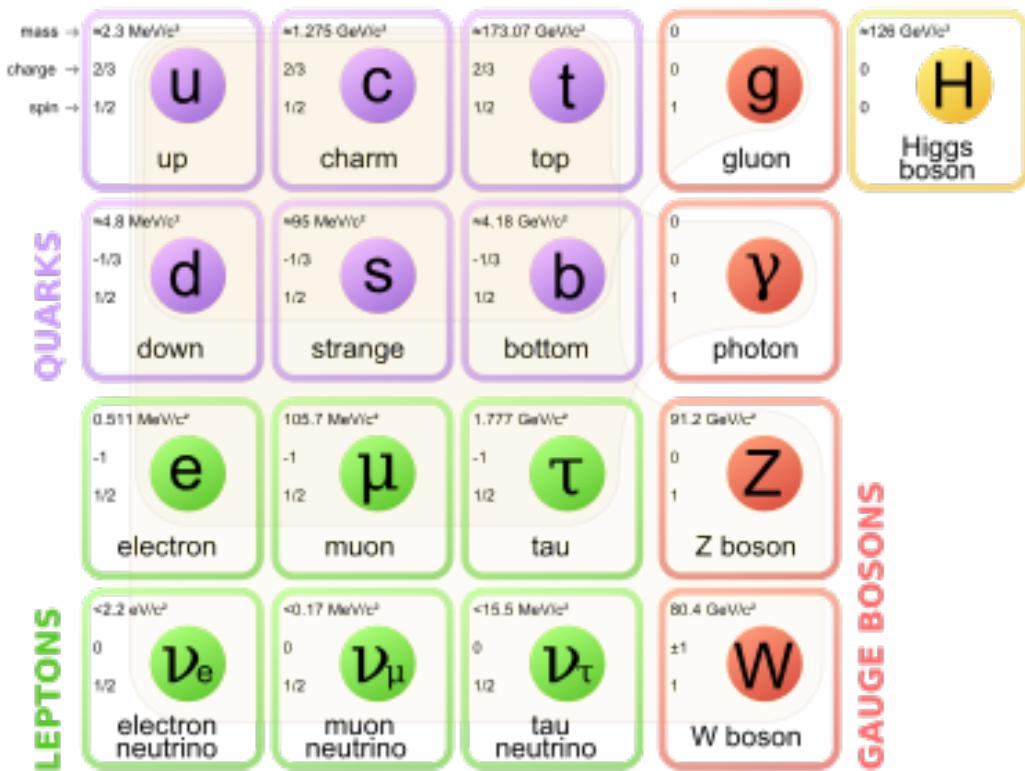


Figure 2.6: Particles of the Standard Model



*Supersymmetry*

310 This chapter will introduce supersymmetry (SUSY) [15, 23–35]. We will begin by  
 311 introducing the concept of a *superspace*, and discuss some general ingredients of  
 312 supersymmetric theories. This will include a discussion of how the problems with the  
 313 Standard Model described in Ch.2 are naturally fixed by these theories.

314 The next step is to discuss the particle content of the *Minimally Supersymmetric*  
 315 *Standard Model* (MSSM). As its name implies, this theory contains the minimal  
 316 additional particle content to make Standard Model supersymmetric. We then discuss  
 317 the important phenomenological consequences of this theory, especially as it would  
 318 be observed in experiments at the LHC.

319 **3.1 Supersymmetric theories : from space to  
 320 superspace**

321 **Coleman-Mandula “no-go” theorem**

322 We begin the theoretical motivation for supersymmetry by citing the “no-go” theorem  
 323 of Coleman and Mandula [65]. This theorem forbids *spin-charge unification*; it  
 324 states that all quantum field theories which contain nontrivial interactions must be  
 325 a direct product of the Poincaré group of Lorentz symmetries, the internal product  
 326 from of gauge symmetries, and the discrete symmetries of parity, charge conjugation,  
 327 and time reversal. The assumptions which go into building the Coleman-Mandula

328 theorem are quite restrictive, but there is one unique way out, which has become  
 329 known as *supersymmetry* [26, 66]. In particular, we must introduce a *spinorial* group  
 330 generator  $Q$ . Alternatively, and equivalently, this can be viewed as the addition  
 331 of anti-commuting coordinates; space plus these new anti-commuting coordinates is  
 332 then called *superspace* [67]. We will not investiage this view in detail, but it is also a  
 333 quite intuitive and beautiful way to construct supersymmetry[15].

### 334 Supersymmetry transformations

335 A *supersymmetric* transformation  $Q$  transforms a bosonic state into a fermionic state,  
 336 and vice versa :

$$Q |\text{Fermion}\rangle = |\text{Boson}\rangle \quad (3.1)$$

$$Q |\text{Boson}\rangle = |\text{Fermion}\rangle \quad (3.2)$$

To ensure this relation holds,  $Q$  must be an anticommuting spinor. Additionally, since spinors are inherently complex,  $Q^\dagger$  must also be a generator of the supersymmetry transformation. Since  $Q$  and  $Q^\dagger$  are spinor objects (with  $s = 1/2$ ), we can see that supersymmetry must be a spacetime symmetry. The Haag-Lopuszanski-Sohnius extension [66] of the Coleman-Mandula theorem [65] is quite restrictive about the forms of such a symmetry. Here, we simply write the (anti-) commutation relations [15] :

$$Q_\alpha, Q_{\dot{\alpha}}^\dagger = -2\sigma_{\alpha\dot{\alpha}\mu} P_\mu \quad (3.3)$$

$$Q_\alpha, Q_{\dot{\beta}} = Q_{\dot{\alpha}}^\dagger, Q_{\dot{\beta}}^\dagger = 0 \quad (3.4)$$

$$[P^\mu, Q_\alpha] = [P^\mu, Q_{\dot{\alpha}}^\dagger] = 0 \quad (3.5)$$

337 **Supermultiplets**

338 In a supersymmetric theory, we organize single-particle states into irreducible  
339 representations of the supersymmetric algebra which are known as *supermultiplets*.  
340 Each supermultiplet contains a fermion state  $|F\rangle$  and a boson state  $|B\rangle$ ; these two  
341 states are the known as *superpartners*. These are related by some combination of  
342  $Q$  and  $Q^\dagger$ , up to a spacetime transformation.  $Q$  and  $Q^\dagger$  commute with the mass-  
343 squared operator  $-P^2$  and the operators corresponding to the gauge transformations  
344 [15]; in particular, the gauge interactions of the Standard Model. In an unbroken  
345 supersymmetric theory, this means the states  $|F\rangle$  and  $|B\rangle$  have exactly the same mass,  
346 electromagnetic charge, electroweak isospin, and color charges. One can also prove  
347 [15] that each supermultiplet contains the exact same number of bosonic ( $n_B$ ) and  
348 fermion ( $n_F$ ) degrees of freedom. We now explore the possible types of supermultiples  
349 one can find in a renormalizable supersymmetric theory.

350 Since each supermultiplet must contain a fermion state, the simplest type of  
351 supermultiplet contains a single Weyl fermion state ( $n_F = 2$ ) which is paired with  
352  $n_B = 2$  scalar bosonic degrees of freedom. This is most conveniently constructed as  
353 single complex scalar field. We call this construction a *scalar supermultiplet* or *chiral*  
354 *supermultiplet*. The second name is indicative; only chiral supermultiplets can contain  
355 fermions whose right-handed and left-handed components transform differently under  
356 the gauge interactions (as of course happens in the Standard Model).

357 The second type of supermultiplet we construct is known as a *gauge* supermul-  
358 tiplet. We take a spin-1 gauge boson (which must be massless due to the gauge  
359 symmetry, so  $n_B = 2$ ) and pair this with a single massless Weyl spinor<sup>1</sup>. The gauge  
360 bosons transform as the adjoint representation of the their respective gauge groups;  
361 their fermionic partners, which are known as gauginos, must also. In particular,  
362 the left-handed and right-handed components of the gaugino fermions have the same

---

<sup>1</sup>Choosing an  $s = 3/2$  massless fermion leads to nonrenormalizable interactions.

363 gauge transformation properties.

364 Excluding gravity, this is the entire list of supermultiplets which can participate  
365 in renormalizable interactions in what is known as  $N = 1$  supersymmetry. This  
366 means there is only one copy of the supersymmetry generators  $Q$  and  $Q^\dagger$ . This is  
367 essentially the only “easy” phenomenological choice, since it is the only choice in four  
368 dimensions which allows for the chiral fermions and parity violations built into the  
369 Standard Model, and we will not look further into  $N > 1$  supersymmetry in this thesis.

370 The primary goal, after understanding the possible structures of the multiplets  
371 above, is to fit the Standard Model particles into a multiplet, and therefore make  
372 predictions about their supersymmetric partners. We explore this in the next section.

## 373 **3.2 Minimally Supersymmetric Standard Model**

374 To construct what is known as the MSSM [15, 68–71], we need a few ingredients and  
375 assumptions. First, we match the Standard Model particles with their corresponding  
376 superpartners of the MSSM. We will also introduce the naming of the superpartners  
377 (also known as *sparticles*). We discuss a very common additional restraint imposed on  
378 the MSSM, known as  $R$ –parity. We also discuss the concept of soft supersymmetry  
379 breaking and how it manifests itself in the MSSM.

### 380 **Chiral supermultiplets**

381 The first thing we deduce is directly from Sec.???. The bosonic superpartners  
382 associated to the quarks and leptons *must* be spin 0, since the quarks and leptons must  
383 be arranged in a chiral supermultiplet. This is essentially the note above, since the  
384 chiral supermultiplet is the only one which can distinguish between the left-handed  
385 and right-handed components of the Standard Model particles. The superpartners of  
386 the quarks and leptons are known as *squarks* and *sleptons*, or *sfermions* in aggregate.

387 (for “scalar quarks”, “scalar leptons”, and “scalar fermion”<sup>2</sup>). The “s-” prefix  
 388 can also be added to the individual quarks i.e. *selectron*, *sneutrino*, and *stop*. The  
 389 notation is to add a  $\sim$  over the corresponding Standard Model particle i.e.  $\tilde{e}$ , the  
 390 selectron is the superpartner of the electron. The two-component Weyl spinors of the  
 391 Standard Model must each have their own (complex scalar) partner i.e.  $e_L, e_R$  have  
 392 two distinct partners :  $\tilde{e}_L, \tilde{e}_R$ . As noted above, the gauge interactions of any of the  
 393 sfermions are identical to those of their Standard Model partners.

Due to the scalar nature of the Higgs, it must obviously lie in a chiral supermultiplet. To avoid gauge anomalies and ensure the correct Yukawa couplings to the quarks and leptons[15], we must add additional Higgs bosons to any supersymmetric theory. In the MSSM, we have two chiral supermultiplets. The SM (SUSY) parts of the multiplets are denoted  $H_u(\tilde{H}_u)$  and  $H_d(\tilde{H}_d)$ . Writing out  $H_u$  and  $H_d$  explicitly:

$$H_u = \begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix} \quad (3.6)$$

$$H_d = \begin{pmatrix} H_d^0 \\ H_d^- \end{pmatrix} \quad (3.7)$$

(3.8)

394 we see that  $H_u$  looks very similar to the SM Higgs with  $Y = 1$ , and  $H_d$  is symmetric  
 395 to this with  $+ \rightarrow -$ , with  $Y = -1$ . The SM Higgs boson,  $h_0$ , is a linear superposition  
 396 of the neutral components of these two doublets. The SUSY parts of the Higgs  
 397 multiplets,  $\tilde{H}_u$  and  $\tilde{H}_d$ , are each left-handed Weyl spinors. For generic spin-1/2  
 398 sparticles, we add the “-ino” suffix. We then call the partners of the two Higgs  
 399 collectively the *Higgsinos*.

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<sup>2</sup>The last one should probably have bigger scare quotes.

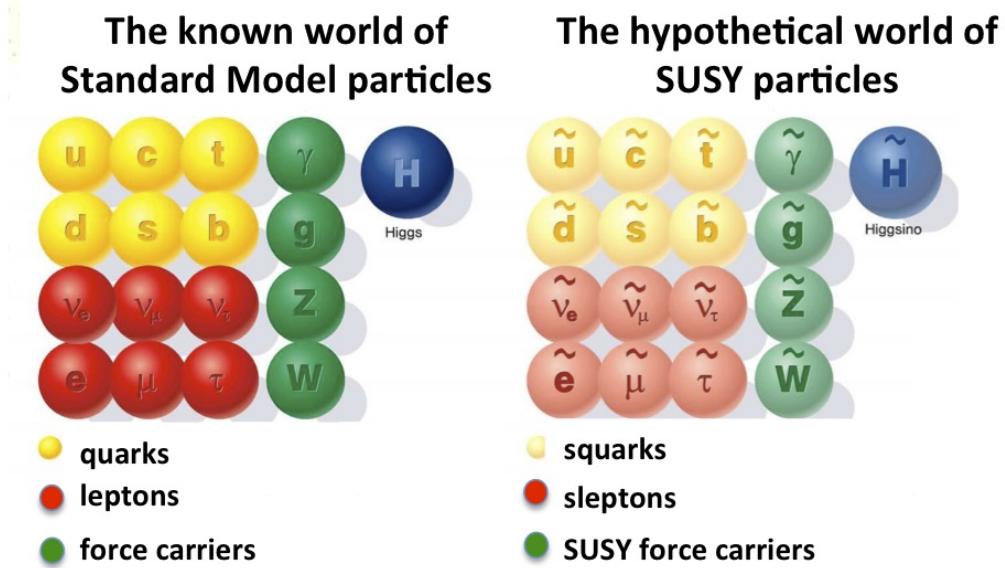


Figure 3.1: Particles of the MSSM

## 400 Gauge supermultiplets

401 The superpartners of the gauge bosons must all be in gauge supermultiplets since  
 402 they contain a spin-1 particle. Collectively, we refer to the superpartners of the  
 403 gauge bosons as the gauginos.

404 The first gauge supermultiplet contains the gluon, and its superpartner, which is  
 405 known as the *gluino*, denoted  $\tilde{g}$ . The gluon is of course the SM mediator of  $SU(3)_C$ ;  
 406 the gluino is also a colored particle, subject to  $SU(3)_C$ . From the SM before EWSB,  
 407 we have the four gauge bosons of the electroweak symmetry group  $SU(2)_L \otimes U(1)_Y$  :  
 408  $W^{1,2,3}$  and  $B^0$ . The superpartners of these particles are thus the *winos*  $W^{\tilde{1},\tilde{2},\tilde{3}}$  and  
 409 *bino*  $\tilde{B}^0$ , where each is placed in another gauge supermultiplet with its corresponding  
 410 SM particle. After EWSB, without breaking supersymmetry, we would also have the  
 411 zino  $\tilde{Z}^0$  and photino  $\tilde{\gamma}$ .

412 The entire particle content of the MSSM can be seen in Fig.3.1.

413 At this point, it's important to take a step back. Where are these particles?  
 414 As stated above, supersymmetric theories require that the masses and all quantum



Figure 3.2: This Feynmann diagram shows how proton decay is induced in the MSSM, if one does not impose  $R$ -parity.

415 numbers of the SM particle and its corresponding sparticle are the same. Of course,  
 416 we have not observed a selectron, squark, or wino. The answer, as it often is, is that  
 417 supersymmetry is *broken* by the vacuum state of nature [15].

418  **$R$ -parity**

This section is a quick aside to the general story.  $R$  – parity refers to an additional discrete symmetry which is often imposed on supersymmetric models. For a given particle state, we define

$$R = (-1)^{3(B-L)+2s} \quad (3.9)$$

419 where  $B, L$  is the baryon (lepton) number and  $s$  is the spin. The imposition of  
 420 this symmetry forbids certain terms from the MSSM Lagrangian that would violate  
 421 baryon and/or lepton number. This is required in order to prevent proton decay, as  
 422 shown in Fig.3.2<sup>3</sup>. .

423 In supersymmetric models, this is a  $\mathbb{Z}_2$  symmetry, where SM particles have  $R = 1$   
 424 and sparticles have  $R = -1$ . We will take  $R$  – parity as part of the definition of  
 425 the MSSM. We will discuss later the *drastic* consequences of this symmetry on SUSY  
 426 phenomenology

---

<sup>3</sup>Proton decay can actually be prevented by allowing only one of the four potential R-parity violating terms to survive.

427 **Soft supersymmetry breaking**

The fundamental idea of *soft* supersymmetry breaking[15, 34, 35, 72, 73] is that we would like to break supersymmetry without reintroducing the quadratic divergences we discussed at the end of Chapter 2. We write the Lagrangian in a form :

$$\mathcal{L}_{\text{MSSM}} = \mathcal{L}_{\text{SUSY}} + \mathcal{L}_{\text{soft}} \quad (3.10)$$

428 In this sense, the symmetry breaking is “soft”, since we have separated out the  
 429 completely symmetric terms from those soft terms which will not allow the quadratic  
 430 divergences to the Higgs mass.

431 The explicitly allowed terms in the soft-breaking Lagrangian are [35].

- 432 • Mass terms for the scalar components of the chiral supermultipletss  
 433 • Mass terms for the Weyl spinor components of the gauge supermultipletss  
 434 • Trilinear couplings of scalar components of chiral supermultiplets

In particular, using the field content described above for the MSSM, the softly-broken portion of the MSSM Lagrangian can be written

$$\mathcal{L}_{\text{soft}} = -\frac{1}{2} \left( M_3 \tilde{g} \tilde{g} + M_2 \tilde{W} \tilde{W} + M_1 \tilde{B} \tilde{B} + c.c. \right) \quad (3.11)$$

$$- \left( \tilde{u} a_u \tilde{Q} H_u - \tilde{d} a_d \tilde{Q} H_d - \tilde{e} a_e \tilde{L} H_d + c.c. \right) \quad (3.12)$$

$$- \tilde{Q}^\dagger m_Q^2 \tilde{Q} - \tilde{L}^\dagger m_L^2 \tilde{L} - \tilde{u} m_u^2 \tilde{u}^\dagger - \tilde{d} m_d^2 \tilde{d}^\dagger - \tilde{e} m_e^2 \tilde{e}^\dagger \quad (3.13)$$

$$- m_{H_u}^2 H_u^* H_u - m_{H_d}^2 H_d^* H_d - (b H_u H_d + cc). \quad (3.14)$$

435 where we have introduced the following notations :

436 1.  $M_3, M_2, M_1$  are the gluino, wino, and bino masses.

437 2.  $a_u, a_d, a_e$  are complex  $3 \times 3$  matrices in family space.

438 3.  $m_Q^2, m_u^2, m_d^2, m_L^2, m_e^2$  are hermitian  $3 \times 3$  matrices in family space.

439        4.  $m_{H_u}^2, m_{H_d}^2, b$  are the SUSY-breaking contributions to the Higgs potential.

440 We have written matrix terms without any sort of additional notational decoration  
 441 to indicate their matrix nature, and we now show why. The first term 1 are  
 442 straightforward; these are just the straightforward mass terms for these fields. There  
 443 are strong constraints on the off-diagonal terms for the matrices of 2 [74, 75]; for  
 444 simplicity, we will assume that each  $a_i, i = u, d, e$  is proportional to the Yukawa  
 445 coupling matrix :  $a_i = A_{i0}y_i$ . The matrices in ?? can be similarly constrained by  
 446 experiments [68, 75–82] Finally, we assume that the elements 4 contributing to the  
 447 Higgs potential as well as all of the 1 terms must be real, which limits the possible  
 448 CP-violating interactions to those of the Standard Model. We thus only consider  
 449 flavor-blind, CP-conserving interactions within the MSSM.

The important mixing for mass and gauge interaction eigenstates in the MSSM occurs within electroweak sector, in a process akin to EWSB in the Standard Model. The neutral portions of the Higgsinos doublets and the neutral gauginos ( $\tilde{H}_u^0, \tilde{H}_d^0, \tilde{B}^0, \tilde{W}^0$ ) of the gauge interaction basis mix to form what are known as the *neutralinos* of mass basis :

$$M_{\tilde{\chi}} = \begin{pmatrix} M_1 & 0 & -c_\beta s_W m_Z & s_\beta s_W m_Z \\ 0 & M_2 & c_\beta c_W m_Z & -s_\beta c_W m_Z \\ -c_\beta s_W m_Z & c_\beta c_W m_Z & 0 & -\mu \\ s_\beta s_W m_Z & -s_\beta c_W m_Z & -\mu & 0 \end{pmatrix} \quad (3.15)$$

450 where  $s(c)$  are the sine and cosine of angles related to EWSB, which introduced  
 451 masses to the gauginos and higgsinos. Diagonalization of this matrix gives the four  
 452 neutralino mass states, listed without loss of generality in order of increasing mass :  
 453  $\tilde{\chi}_{1,2,3,4}^0$ .

454        The neutralinos, especially the lightest neutralino  $\tilde{\chi}_1^0$ , are important ingredients  
 455 in SUSY phenomenology.

456      The same process can be done for the electrically charged gauginos with  
457      the charged portions of the Higgsino doublets along with the charged winos  
458      ( $\tilde{H}_u^+, \tilde{H}_d^+, \tilde{W}^+, \tilde{W}^-$ ). This leads to the *charginos*, again in order of increasing mass  
459      :  $\tilde{\chi}_{1,2}^\pm$ .

460      

### 3.3 Phenomenology

461      We are finally at the point where we can discuss the phenomenology of the MSSM,  
462      in particular as it manifests itself at the energy scales of the LHC.

463      As noted above in Sec.3.2, the assumption of *R*–parity has important conse-  
464      quences for MSSM phenomenology. The SM particles have  $R = 1$ , while the sparticles  
465      all have  $R = -1$ . Simply, this is the “charge” of supersymmetry. Since the particles of  
466      LHC collisions ( $pp$ ) have total incoming  $R = 1$ , we must expect that all sparticles will  
467      be produced in *pairs*. An additional consequence of this symmetry is the fact that the  
468      lightest supersymmetric particle (LSP) is *stable*. Off each branch of the Feynmann  
469      diagram shown in Fig., we have  $R = -1$ , and this can only decay to another sparticle  
470      and a SM particle. Once we reach the lightest sparticle in the decay, it is absolutely  
471      stable. This leads to the common signature  $E_T^{\text{miss}}$  for a generic SUSY signal.

472      For this thesis, we will be presenting an inclusive search for squarks and gluinos  
473      with zero leptons in the final state. This is a very interesting decay channel<sup>4</sup>, due  
474      to the high cross-sections of  $\tilde{g}\tilde{g}$  and  $\tilde{q}\tilde{q}$  decays, as can be seen in Fig.?? [83]. This  
475      is a direct consequence of the fact that these are the colored particles of the MSSM.  
476      Since the sparticles interact with the gauge groups of the SM in the same way as their  
477      SM partners, the colored sparticles, the squarks and gluinos, are produced and decay  
478      as governed by the color group  $SU(3)_C$  with the strong coupling  $g_S$ . The digluino  
479      production is particularly copious, due to color factor corresponding to the color octet

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<sup>4</sup>Prior to Run1, probably the most *most* interesting SUSY decay channel.

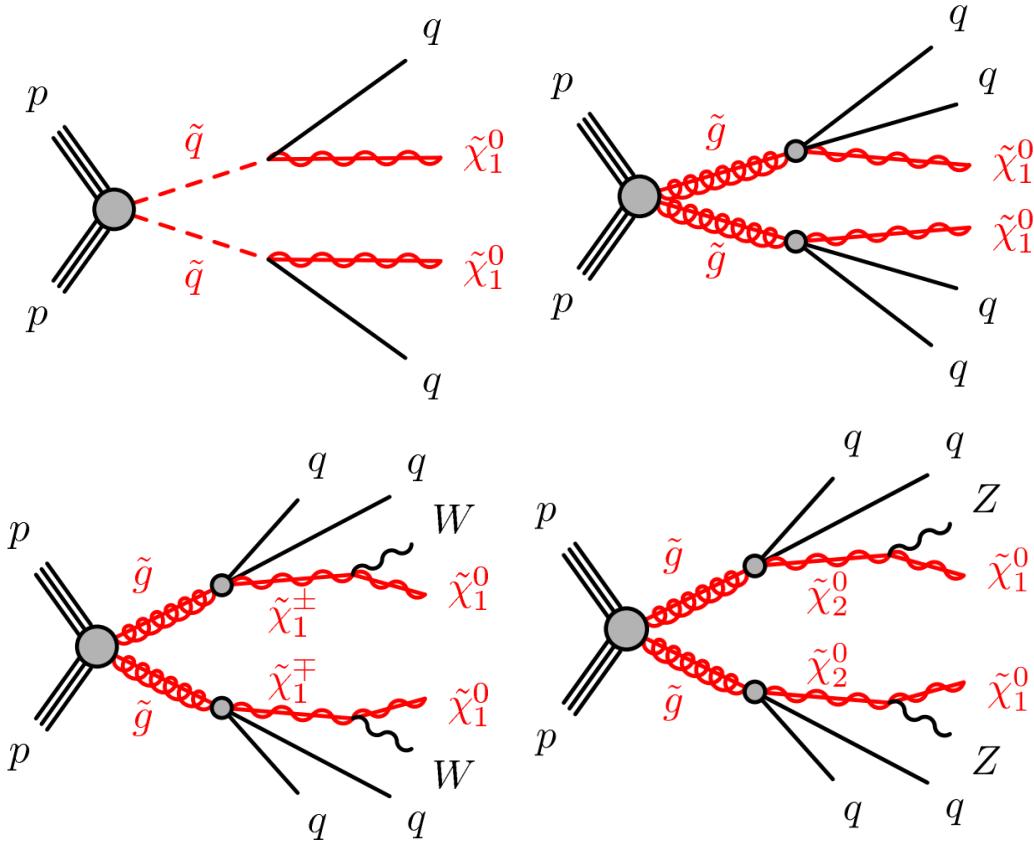


Figure 3.3: SUSY signals considered in this thesis

480 of  $SU(3)C$ .

481 In the case of disquark production, the most common decay mode of the squark in  
 482 the MSSM is a decay directly to the LSP plus a single SM quark [15]. This means the  
 483 basic search strategy of disquark production is two jets from the final state quarks,  
 484 plus missing transverse energy for the LSPs. There are also cascade decays, the most  
 485 common of which, and the only one considered in this thesis, is  $\tilde{q} \rightarrow q\chi_1^\pm \rightarrow qW^\pm\chi_1^0$ .

486 For digluino production, the most common decay is  $\tilde{g} \rightarrow g\tilde{q}$ , due to the large  
 487  $g_S$  coupling. The squark then decays as listed above. In this case, we generically  
 488 search for four jets and missing transverse energy from the LSPs. We can also have  
 489 the squark decay in association with a  $W^\pm$  or  $Z^0$ ; in this thesis, we are interested in  
 490 those cases where this vector boson goes hadronically.

491 In the context of experimental searches for SUSY, we often consider *simplified*

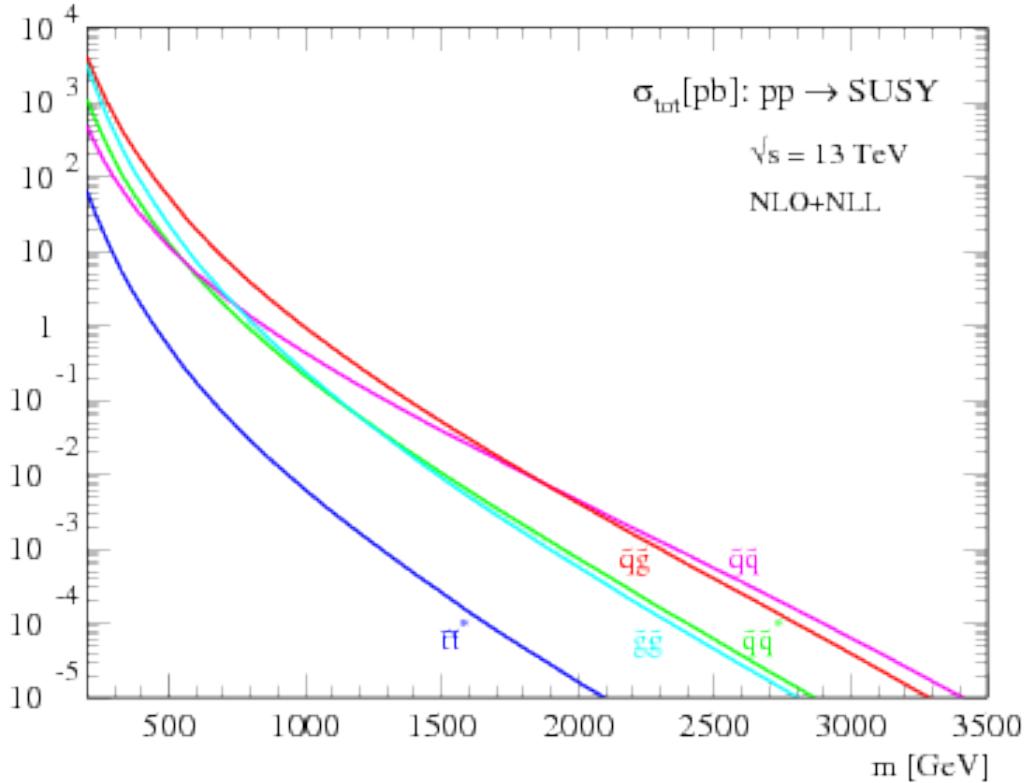


Figure 3.4: SUSY production cross-sections as a function of sparticle mass at  $\sqrt{s} = 13$  TeV.

492 *models*. These models make certain assumptions which allow easy comparisons of  
 493 results by theorists and rival experimentalists. In the context of this thesis, the  
 494 simplified models will make assumptions about the branching ratios described in the  
 495 preceding paragraphs. In particular, we will often choose a model where the decay of  
 496 interest occurs with 100% branching ratio. This is entirely for ease of interpretation  
 497 by other physicists<sup>5</sup>, but it is important to recognize that these are more a useful  
 498 comparison tool, especially with limits, than a strict statement about the potential  
 499 masses of sought-after beyond the Standard Model particle.

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<sup>5</sup>In the author's opinion, this often leads to more confusion than comprehension. We will revisit the shortcomings of simplified models in the Conclusion to this thesis.

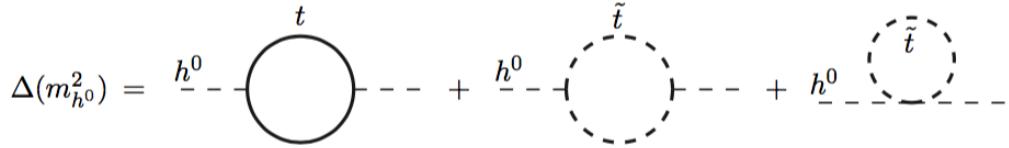


Figure 3.5: Loop diagrams correct the Higgs mass in the MSSM

## 500 3.4 How SUSY solves the problems with the SM

501 We now return to the issues with the Standard Model as described in Ch.2 to see  
 502 how these issues are solved by supersymmetry.

### 503 Quadratic divergences to the Higgs mass

The quadratic divergences induced by the loop corrections to the Higgs mass, for example from the top Yukawa coupling, goes as

$$\delta m_H^2 \approx \left( \frac{m_t}{8\pi^2 \langle \phi \rangle_{VEV}} \right)^2 \Lambda_{Planck}^2. \quad (3.16)$$

504 The miraculous thing about SUSY is each of these terms *automatically* comes  
 505 with a term which exactly cancels this contribution[15]. The fermions and bosons  
 506 have opposite signs in this loop diagram to all orders in perturbation theory, which  
 507 completely solves the hierarchy problem. This is the most well-motivated reason for  
 508 supersymmetry.

### 509 Gauge coupling unification

510 An additional motivation for supersymmetry is seen by the gauge coupling unification  
 511 high scales. In the Standard Model, as we saw the gauge couplings fail to unify at  
 512 high energies. In the MSSM and many other forms of supersymmetry, the gauge  
 513 couplings unify at high energy, as can be seen in Fig.???. This provides additional  
 514 aesthetic motivation for supersymmetric theories.



Figure 3.6: The running of Standard Model gauge couplings; compare to Fig.2.4. The MSSM gauge couplings nearly intersect at high energies.

## 515 Dark matter

516 As we discussed previously, the lack of any dark matter candidate in the Standard  
 517 Model naturally leads to beyond the Standard Model theories. In the Standard Model,  
 518 there is a natural dark matter candidate in the lightest supersymmetric particle[15]  
 519 The LSP would in dark matter experiments be called a *weakly-interacting massive*  
 520 *particle* (WIMP), which is a type of cold dark matter [22, 84]. These WIMPS would  
 521 only interact through the weak force and gravity, which is exactly as a model like the  
 522 MSSM predicts for the neutralino. In Fig.3.7, we can see the current WIMP exclusions  
 523 for a given mass. The range of allowed masses which have not been excluded for LSPs  
 524 and WIMPs have significant overlap. This provides additional motivation outside of  
 525 the context of theoretical details.



Figure 3.7: WIMP exclusions from direct dark matter detection experiments.

### 526 3.5 Conclusions

527 Supersymmetry is the most well-motivated theory for physics beyond the Standard  
 528 Model. It provides a solution to the hierarchy problem, leads to gauge coupling  
 529 unification, and provides a dark matter candidate consistent with galactic rotation  
 530 curves. As noted in this chapter, due to the LSPs in the final state, most SUSY  
 531 searches require a significant amount of missing transverse energy in combination  
 532 with jets of high transverse momentum. However, there is some opportunity to do  
 533 better than this, especially in final states where one has two weakly-interacting LSPs  
 534 on opposite sides of some potentially complicated decay tree. We will see how this is  
 535 done in Ch.??.



*The Large Hadron Collider*

538 The Large Hadron Collider (LHC) produces high-energy protons which are collided  
 539 at the center of multiple large experiments at CERN on the outskirts of Geneva,  
 540 Switzerland [85]. The LHC produces the highest energy collisions in the world,  
 541 with design center-of-mass energy of  $\sqrt{s} = 14$  TeV, which allows the experiments  
 542 to investigate physics far beyond the reach of previous colliders. This chapter will  
 543 summarize the basics of accelerator physics, especially with regards to discovering  
 544 physics beyond the Standard Model. We will describe the CERN accelerator complex  
 545 and the LHC.

546 **4.1 Basics of Accelerator Physics**

547 This section follows closely the presentation of [86].

Simple particle accelerators simply rely on the acceleration of charged particles in a static electric field. Given a field of strength  $E$ , charge  $q$ , and mass  $m$ , this is simply

$$a = \frac{qE}{m}. \quad (4.1)$$

548 For a given particle with a given mass and charge, this is limited by the static electric  
 549 field which can be produced, which in turn is limited by electrical breakdown at high  
 550 voltages.

551 There are two complementary solutions to this issue. First, we use the *radio*  
 552 *frequency acceleration* technique. We call the devices used for this *RF cavities*. The

553    cavities produce a time-varied electric field, which oscillate such that the charged  
 554    particles passing through it are accelerated towards the design energy of the RF  
 555    cavity. This oscillation also induces the particles into *bunches*, since particles which  
 556    are slightly off in energy from that induced by the RF cavity are accelerated towards  
 557    the design energy.

Second, one bends the particles in a magnetic field, which allows them to pass through the same RF cavity over and over. This second process is often limited by *synchrotron radiation*, which describes the radiation produced when a charged particle is accelerated. The power radiated is

$$P \sim \frac{1}{r^2} \left( E/m \right)^4 \quad (4.2)$$

558    where  $r$  is the radius of curvature and  $E, m$  is the energy (mass) of the charged  
 559    particle. Given an energy which can be produced by a given set of RF cavities (which  
 560    is *not* limited by the mass of the particle), one then has two options to increase the  
 561    actual collision energy : increase the radius of curvature or use a heavier particle.  
 562    Practically speaking, the easiest options for particles in a collider are protons and  
 563    electrons, since they are (obviously) copious in nature and do not decay<sup>1</sup>. Given the  
 564    dependence on mass, we can see why protons are used to reach the highest energies.  
 565    The tradeoff for this is that protons are not point particles, and we thus we don't  
 566    know the exact incoming four-vectors of the protons, as discussed in Ch.2.

The particle *beam* refers to the bunches all together. An important property of a beam of a particular energy  $E$ , moving in uniform magnetic field  $B$ , containing particles of momentum  $p$  is the *beam rigidity* :

$$R \equiv rB = p/c. \quad (4.3)$$

567    The linear relation between  $r$  and  $p$ , or alternatively  $B$  and  $p$  have important  
 568    consequences for LHC physics. For hadron colliders, this is the limiting factor on

---

<sup>1</sup>Muon colliders are a really cool option at high energies, since the relativistic  $\gamma$  factor gives them a relatively long lifetime in the lab frame.

569 going to higher energy scales; one needs a proportionally larger magnetic field to  
570 keep the beam accelerating in a circle.

571 Besides the rigidity of the beam, the most important quantities to characterize  
572 a beam are known as the (normalized) *emittance*  $\epsilon_N$  and the *betatron function*  $\beta$ .  
573 These quantities determine the transverse size  $\sigma$  of a relativistic beam  $v \gtrsim c$  beam :  
574  $\sigma^2 = \beta^* \epsilon_N / \gamma_{\text{rel}}$ , where  $\beta^*$  is the value of the betatron function at the collision point  
575 and  $\gamma_{\text{rel}}$  is the Lorentz factor.

These quantities determine the *instantaneous luminosity*  $L$  of a collider, which combined with the cross-section  $\sigma$  of a particular physics process, give the rate of this physics process :

$$R = L\sigma. \quad (4.4)$$

The instantaneous luminosity  $L$  is given by :

$$L = \frac{f_{\text{rev}} N_b^2 F}{4\pi\sigma^2} = \frac{f_{\text{rev}} n N_b^2 \gamma_{\text{rel}} F}{4\pi\beta^* \epsilon_N}. \quad (4.5)$$

576 Here we have introduced the frequency of revolutions  $f_{\text{rev}}$ , the number of bunches  $n$ ,  
577 the number of protons per bunch  $N_b^2$ , and a geometric factor  $F$  related to the crossing  
578 angle of the beams.

The *integrated luminosity*  $\int L$  gives the total number of a particular physics process  $P$ , with cross-section  $\sigma_P$ .

$$N_P = \sigma_P \int L. \quad (4.6)$$

579 Due to this simple relation, one can also quantify the “amount of data delivered” by  
580 a collider simply by  $\int L$ .

## 581 4.2 Accelerator Complex

582 The Large Hadron Collider is the last accelerator in a chain of accelerators which  
583 together form the CERN accelerator complex, which can be seen in 4.1. The protons



Figure 4.1: The CERN accelerator complex.

begin their journey to annihilation in a hydrogen source, where they are subsequently ionized. The first acceleration occurs in the Linac 2, a linear accelerator composed of RF cavities. The protons leave the Linac 2 at an energy of 50 MeV and enter the Proton Synchrotron Booster (PSB). The PSB contains four superimposed rings, which accelerate the protons to 1.4 GeV. The protons are then injected into the Proton Synchrotron (PS). This synchrotron increases the energy up to 25 GeV. After leaving the PS, the protons enter the Super Proton Synchrotron (SPS). This is the last step before entering the LHC ring, and the protons are accelerated to 450 GeV. From the SPS, the protons are injected into the beam pipes of the LHC. The process to fill the LHC rings with proton bunches from start to finish typically takes about four minutes.

595 **4.3 Large Hadron Collider**

The Large Hadron Collider is the final step in the CERN accelerator complex, and produces the collisions analyzed in this thesis. From the point of view of experimentalists on the general-purpose ATLAS and CMS experiments, the main goal of the LHC is to deliver collisions at the highest possible energy, with the highest possible instantaneous luminosity. The LHC was installed in the existing 27 km tunnel used by the Large Electron Positron (LEP) collider [87]. This allowed the existing accelerator complex at CERN, described in the previous section, to be used as the injection system to prepare the protons up to 450 GeV. Many aspects of the LHC design were decided by this very fact, and specified the options allowed to increase the energy or luminosity. In particular, the radius of the tunnel was already specified; from Eq.4.3, this implies the momentum (or energy) of the beam is entirely determined by the magnetic field. Given the 27 km circumference of the LEP tunnel, one can calculate the required magnetic field to reach the 7 TeV per proton design energy of the LHC :

$$r = C/2\pi = 4.3 \text{ km} \quad (4.7)$$

$$\rightarrow B = \frac{p}{rc} = 5 \text{ T} \quad (4.8)$$

596 In fact, the LHC consists of 8 528 m straight portions consisting of RF cavities, used  
597 to accelerate the particles, and 8 circular portions which bend the protons around the  
598 LHC ring. These circular portions actually have a slightly smaller radius of curvature  
599  $r = 2804 \text{ m}$ , and we require  $B = 8.33 \text{ T}$ . To produce this large field, we need to use  
600 superconducting magnets, as discussed in the next section.

601 **Magnets**

602 There are many magnets used by the LHC machine, but the most important are the  
603 1232 dipole magnets; a schematic is shown in Fig.4.2 and a photograph is shown in



Figure 4.2: Schematic of an LHC dipole magnet.

604 Fig.4.3.

605 The magnets are made of Niobium and Titanium. The maximum field strength is  
 606 10 T when cooled to 1.9 Kelvin. The magnets are cooled by superfluid helium, which  
 607 is supplied by a large cryogenic system. Due to heating between the eight helium  
 608 refrigerators and the beampipe, the helium is cooled in the refrigerators to 1.8 K.

609 A failure in the cooling system can cause what is known as a *quench*. If the  
 610 temperature goes above the critical superconducting temperature, the metal loses its  
 611 superconducting properties, which leads to a large resistance in the metal. This leads  
 612 to rapid temperature increases, and can cause extensive damages if not controlled.

613 The dipole magnets are 16.5 meters long with a diameter of 0.57 meters. There  
 614 are two individual beam pipes inside each magnet, which allows the dipoles to house  
 615 the beams travelling in both directions around the LHC ring. They curve slightly,  
 616 at an angle of 5.1 mrad, which carefully matches the curvature of the ring. The

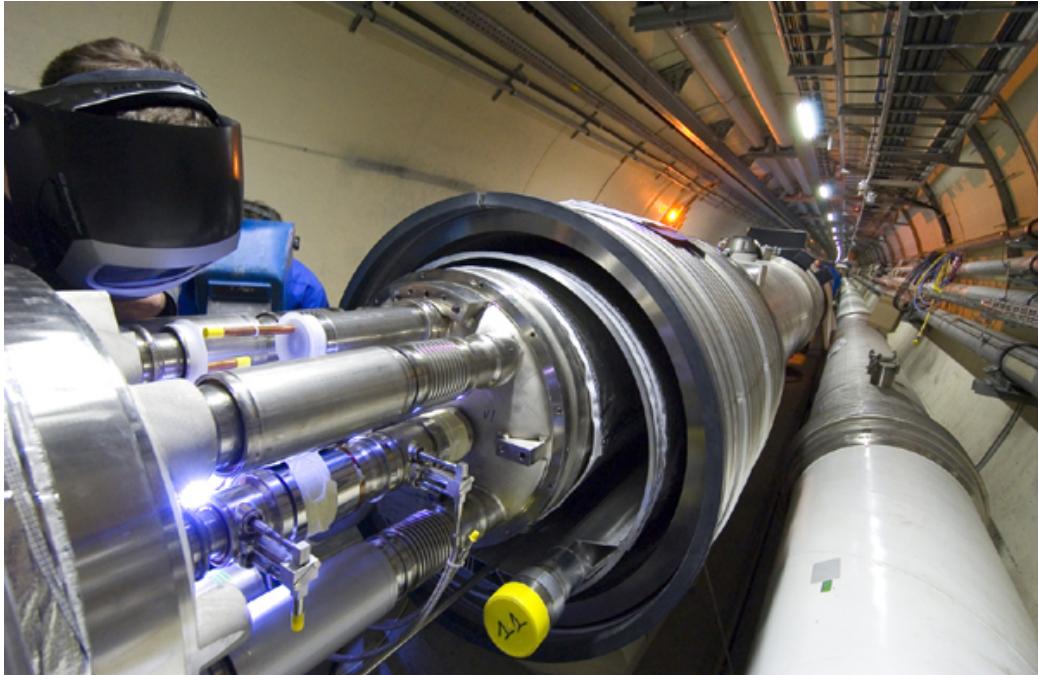


Figure 4.3: Photograph of a technician connecting an LHC dipole magnet.

617 beampipes inside of the magnets are held in high vacuum, to avoid stray particles  
618 interacting with the beam.

## 619 **4.4 Dataset Delivered by the LHC**

620 In this thesis, we analyze the data delivered by the LHC to ATLAS in the 2015 and  
621 2016 datasets. The beam parameters relevant to this dataset are available in Table  
622 [4.1](#).

623 The peak instantaneous luminosity delivered in 2015 (2016) was  $L =$   
624  $5.2(11) \text{ cm}^{-2}\text{s}^{-1} \times 10^{33}$ . One can note that the instantaneous luminosity delivered in  
625 the 2016 dataset exceeds the design luminosity of the LHC. The total integrated  
626 luminosity delivered was  $13.3 \text{ fb}^{-1}$ . In Figure [4.4](#), we display the integrated luminosity  
627 as a function of day for 2015 and 2016.

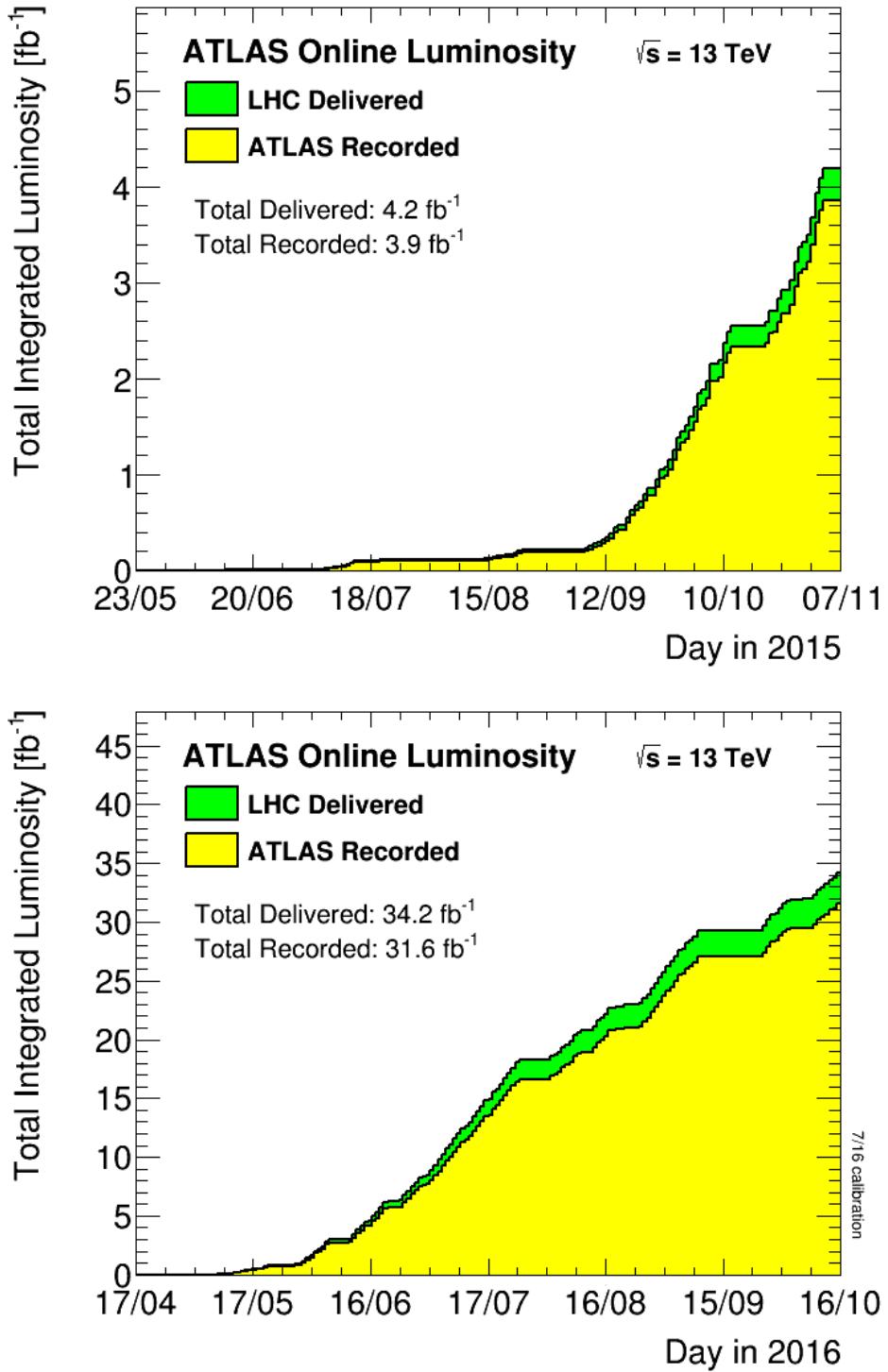


Figure 4.4: Integrated Luminosity delivered by the LHC and collected by ATLAS in the 2015 and 2016 datasets.

Parameter	Injection	Extraction
Energy (GeV)	450	7000
Rigidity (T-m)	3.8	23353
Bunch spacing (ns)	25	25
Design Luminosity ( $\text{cm}^{-2}\text{s}^{-1} \times 10^3$ )	-	1.0
Bunches per proton beam	2808	2808
Protons per bunch	1.15 e11	1.15 e11
Beam lifetime (hr)	-	10
Normalized Emittance $\epsilon_N$ (mm $\mu\text{rad}$ )	3.3	3.75
Betatron function at collision point $\beta^*$ (cm)	-	55

Table 4.1: Beam parameters of the Large Hadron Collider.

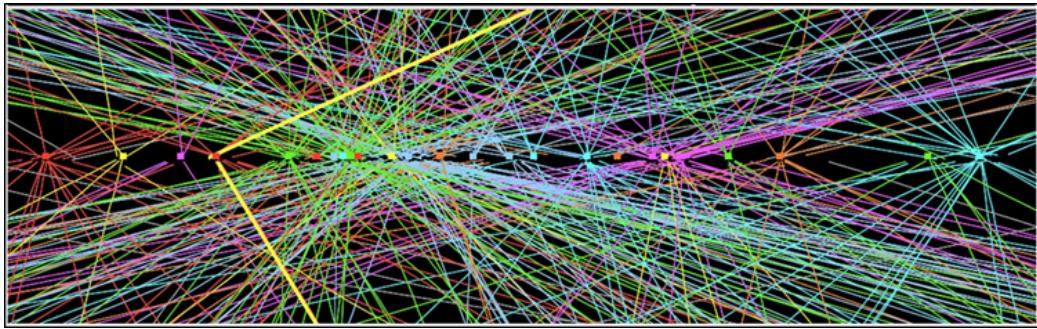


Figure 4.5: Simulated event with many pileup vertices.

## 628 Pileup

629 *Pileup* is the term for the additional proton-proton interactions which occur during  
 630 each bunch crossing of the LHC. At the beginning of the LHC physics program, there  
 631 had not been a collider which averaged more than a single interaction per bunch  
 632 crossing. In the LHC, each bunch crossing (or *event*) generally contains multiple  
 633 proton-proton interactions. An simulated event with many *vertices* can be seen in  
 634 Fig.4.5. The so-called *primary vertex* (or *hard scatter vertex*) refers to the vertex  
 635 which has the highest  $\Sigma p_T^2$ ; this summation occurs over the *tracks* in the detector,  
 636 which we will describe later[**ATL-INDET-PUB-2009-001**]. We then distinguish  
 637 between *in-time* pileup and *out-of-time* pileup. In-time pileup refers to the additional  
 638 proton-proton interactions which occur in the event. Out-of-time pileup refers to  
 639 effects related to proton-proton interactions previous bunch crossings.

640        We quantify in-time pileup by the number of “primary”<sup>2</sup> vertices in a particular  
641    event. To quantify the out-of-time pileup, we use the average number of interactions  
642    per bunch crossing  $\langle \mu \rangle$  over some human-scale time. In Figure 4.6, we show the  
643    distribution of  $\mu$  for the dataset used in this thesis.

---

<sup>2</sup>The primary vertex is as defined above, but we unfortunately use the same name here.



Figure 4.6: Mean number of interactions per bunch crossing in the 2015 and 2016 datasets.



*The ATLAS detector*

646 The dataset analyzed in this thesis was taken by the ATLAS detector [88], which is  
 647 located at the “Point 1” cavern of the LHC beampipe, just across the street from  
 648 the main CERN campus. The much-maligned acronym stands for *A Toroidal LHC*  
 649 *ApparatuS*. ATLAS is a massive cylindrical detector, with a radius of 12.5 m and a  
 650 length of 44 m, with nearly hermitic coverage around the collision point. It consists  
 651 of multiple subdetectors; each plays a role in ATLAS’s ultimate purpose of measuring  
 652 the energy, momentum, and type of the particles produced in collisions delivered by  
 653 the LHC. These subdetectors are immersed in a hybrid solenoid-toroid magnet system  
 654 whichs forces charged particles to curve, which allows for precise measurements of  
 655 their momenta. These magnetic fields are maximized in the central solenoid magnet,  
 656 which contains a magnetic field of 2 T. A schematic of the detector can be seen in  
 657 [5.1](#).

658 The *inner detector* (ID) lies closest to the collision point, and contains three  
 659 separate subdetectors. It provides pseudorapidity<sup>1</sup>coverage of  $|\eta| < 2.5$  for charged  
 660 particles to interact with the tracking material. The tracks reconstructed from the  
 661 inner detector hits are used to reconstruct the primary vertices, as noted in Ch.??,

---

<sup>1</sup>ATLAS uses a right-handed Cartesian coordinate system; the origin is defined by the nominal beam interaction point. The positive- $z$  direction is defined by the incoming beam travelling counterclockwise around the LHC. The positive- $x$  direction points towards the center of the LHC ring from the origin, and the positive- $y$  direction points upwards towards the sky. For particles of transverse (in the  $x - y$  plane) momentum  $p_T = \sqrt{p_x^2 + p_y^2}$  and energy  $E$ , it is generally most convenient fully describe this particle’s kinematics as measured by the detector in the  $(p_T, \phi, \eta, E)$  basis. The angle  $\phi = \arctan(p_y/p_x)$  is the standard azimuthal angle, and  $\eta = \ln \tan(\theta/2)$  is known as the pseudorapidity, and defined based on the standard polar angle  $\theta = \arccos(p_z/p_T)$ . For locations of i.e. detector elements, both  $(r, \phi, \eta)$  and  $(z, \phi, \eta)$  can be useful.



Figure 5.1: The ATLAS detector

and to determine the momenta of charged particles. The ATLAS *calorimeter* consists of two subdetectors, known as the *electromagnetic* and *hadronic* calorimeters. These detectors stop particles in their detector material, and measure the energy deposition inside, which measures the energy of the particles deposited. The calorimeters provide coverage out to pseudorapidity of  $|\eta| < 4.9$ . The muon spectrometer is aptly named; it is specifically used for muons, which are the only particles which generally reach the outer portions of the detector. In this region, we have the large tracking systems of the muon spectrometer, which provide precise measurements of muon momenta. The muon spectrometer has pseudorapidity coverage of  $|\eta| < 2.7$ .

## 5.1 Magnets

ATLAS contains multiple magnetic systems; primarily, we are concerned with the solenoid, used by the inner detector, and the toroids located outside of the ATLAS calorimeter. A schematic is shown in Fig.5.2. These magnetic fields are used to bend

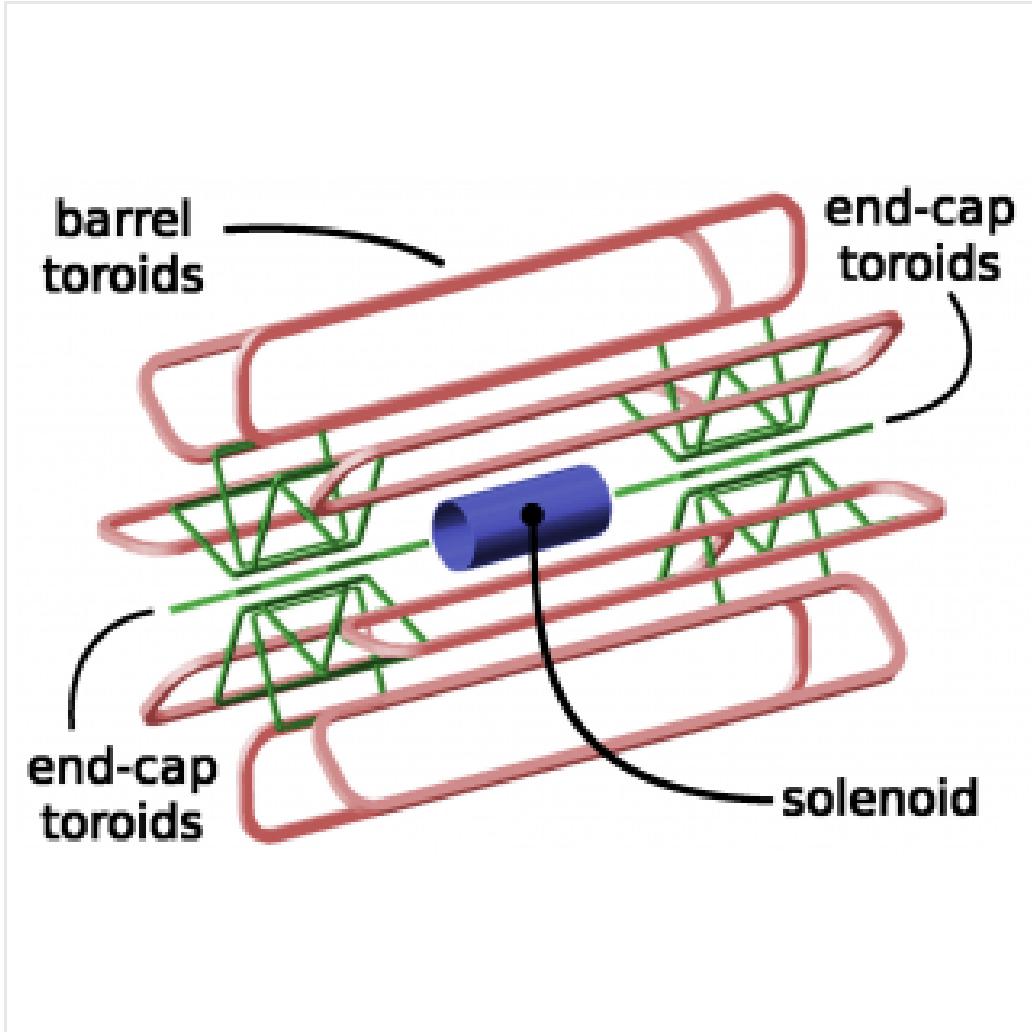


Figure 5.2: The ATLAS magnet system

675 charged particles under the Lorentz force, which subsequently allows one to measure  
676 their momentum.

677 The ATLAS central solenoid is a 2.3 m diameter, 5.3 m long solenoid at the center  
678 of the ATLAS detector. It produces a uniform magnetic field of 2 T; this strong field  
679 is necessary to accurately measure the charged particles in this field. An important  
680 design constraint for the central solenoid was the decision to place it in between the  
681 inner detector and the calorimeters. To avoid excessive impacts on measurements in  
682 the calorimetry, the central solenoid must be as transparent as possible<sup>2</sup>.

---

<sup>2</sup>This is also one of the biggest functional differences between ATLAS and CMS; in CMS, the



Figure 5.3: The ATLAS inner detector

683     The toroid system consists of eight air-core superconducting barrel loops; these  
 684    give ATLAS its distinctive shape. There are also two endcap air-core magnets. These  
 685    produce a magnetic field in a region of approximately 26 m in length and 10 m of  
 686    radius. The magnetic field in this region is non-uniform, due to the prohibitive costs  
 687    of a solenoid magnet of that size.

## 688    **5.2 Inner Detector**

689    The ATLAS inner detector consists of three separate tracking detectors, which are  
 690    known as, in order of increasing distance from the interaction point, the Pixel  
 691    Detector, Semiconductor Tracker (SCT), and the Transition Radiation Tracker  
 692    (TRT). When charged particles pass through these tracking layers, they produce  
 693    *hits*, which using the known 2 T magnetic field, allows the reconstruction of *tracks*.  
 694    Tracks are used as inputs for reconstruction of many higher-level physics objects,

---

solenoid is outside of the calorimeters.

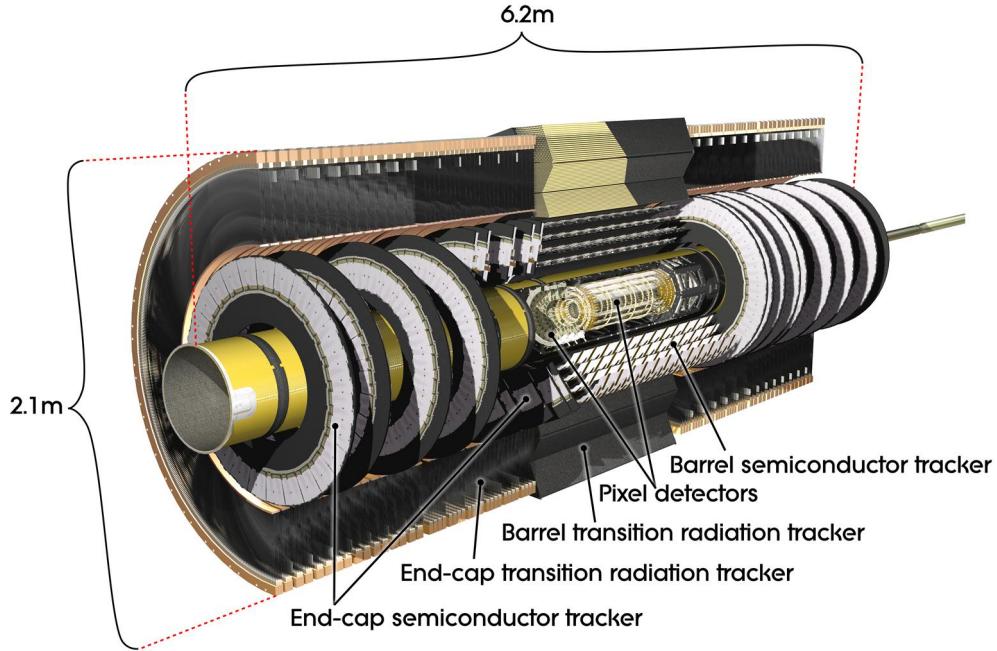


Figure 5.4: The ATLAS pixel detector

695 such as electrons, muons, photons, and  $E_T^{\text{miss}}$ . Accurate track reconstruction is thus  
 696 crucial for precise measurements of charged particles.

## 697 Pixel Detector

698 The ATLAS pixel detector consists four layers of silicon “pixels”. This refers to the  
 699 segmentation of the active medium into the pixels; compare to the succeeding silicon  
 700 detectors, which will use silicon “strips”. This provides precise 3D hit locations. The  
 701 layers are known as the “Insertable”<sup>3</sup>B-Layer (IBL), the B-Layer (or Layer-0), Layer-  
 702 1, and Layer-2, in order of increasing distance from the interaction point. These  
 703 layers are very close to the interaction point, and therefore experience a large amount  
 704 of radiation.

705 Layer-1, Layer-2, and Layer-3 were installed with the initial construction of  
 706 ATLAS. They contain front-end integrated electronics (FEI3s) bump-bonded to 1744

---

<sup>3</sup>Very often, the IBL is mistakenly called the Inner B-Layer, which would have been a much more sensible name.

707 silicon modules; each module is  $250 \mu\text{m}$  in thickness and contains 47232 pixels. These  
708 pixels have planar sizes of  $50 \times 400 \mu\text{m}^2$  or  $50 \times 600 \mu\text{m}^2$ , to provide highly accurate  
709 location information. The FEI3s are mounted on long rectangular structures known  
710 as staves, which encircle the beam pipe. A small tilt to each stave allows full coverage  
711 in  $\phi$  even with readout systems which are installed. These layers are at radia of 50.5  
712 mm, 88.5 mm, and 122.5 mm from the interaction point.

713 The IBL was added to ATLAS after Run1 in 2012 at a radius of 33 mm from the  
714 interaction point. The entire pixel detector was removed from the center of ATLAS  
715 to allow an additional pixel layer to be installed. The IBL was required to preserve  
716 the integrity of the pixel detector as radiation damage leads to inoperative pixels in  
717 the other layers. The IBL consists of 448 FEI4 chips, arranged onto 14 staves. Each  
718 FEI4 has 26880 pixels, of planar size  $50 \times 250 \mu\text{m}$ . This smaller granularity was  
719 required due to the smaller distance to the interaction point.

720 In total, a charged particle passing through the inner detector would expect to  
721 leave four hits in the pixel detector.

## 722 Semiconductor Tracker

723 The SCT is directly beyond Layer-2 of the pixel detector. This is a silicon strip  
724 detector, which do not provide the full 3D information of the pixel detector. The  
725 dual-sensors of the SCT contain  $2 \times 768$  individual strips; each strip has area  $6.4$   
726  $\text{cm}^2$ . The SCT dual-sensor is then double-layered, at a relative angle of 40 mrad;  
727 together these layers provide the necessary 3D information for track reconstruction.  
728 There are four of these double-layers, at radia of 284 mm, 355 mm, 427 mm, and 498  
729 mm. These double-layers provide hits comparable to those of the pixel detector, and  
730 we have four additional hits to reconstruct tracks for each charged particle.

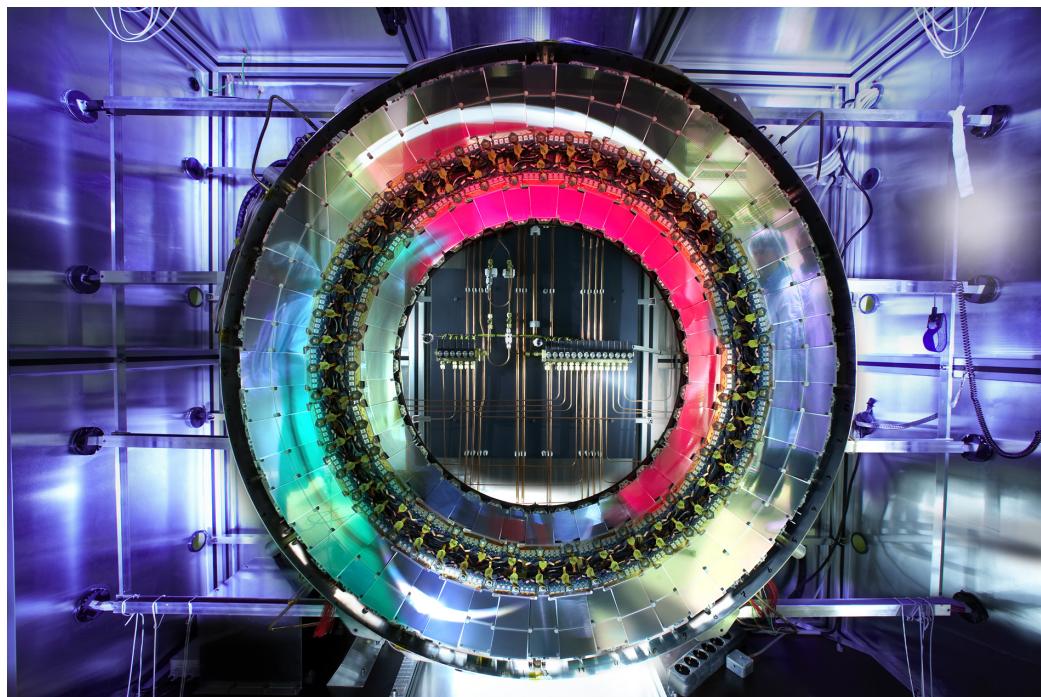


Figure 5.5: A ring of the Semiconductor Tracker

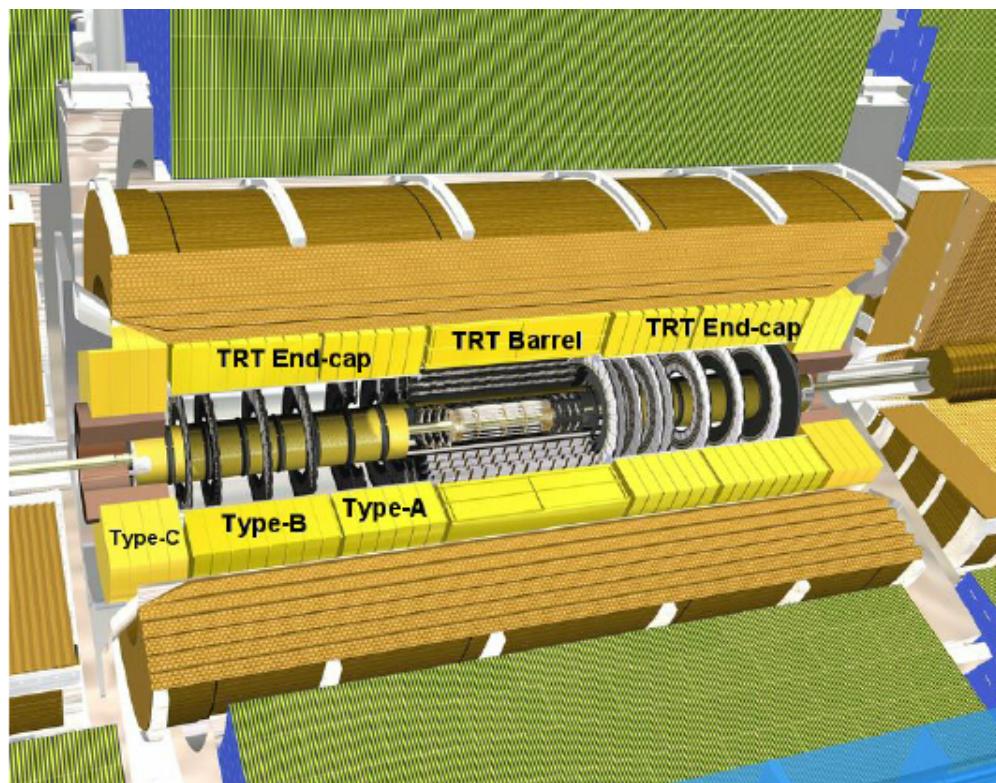


Figure 5.6: A schematic of the Transition Radiation Tracker

731 **Transition Radiation Tracker**

732 The Transition Radiation Tracker is the next detector radially outward from the SCT.  
733 It contains straw drift tubes; these contain a tungsten gold-plated wire of  $32 \mu\text{m}$   
734 diameter held under high voltage (-1530 V) with the edge of the Kapton-aluminum  
735 tube. They are filled with a gas mixture of primarily xenon that is ionized when  
736 a charged particle passes through the tube. The ions are collected by the “drift”  
737 due to the voltage inside the tubes, which is read out by the electronics. This gives  
738 so-called “continuous tracking” throughout the tube, due to the large number of ions  
739 produced.

740 The TRT is so-named due to the *transition radiation* (TR) it induces. Due to  
741 the dielectric difference between the gas and tubes, TR is induced. This is important  
742 for distinguishing electrons from their predominant background of minimum ionizing  
743 particles. Generally, electrons have a much larger Lorentz factor than minimum  
744 ionizing particles, which leads to additional TR. This can be used as an additional  
745 handle for electron reconstruction.

746 **5.3 Calorimetry**

747 The calorimetry of the ATLAS detector also includes multiple subdetectors; these sub-  
748 detectors allow precise measurements of the electrons, photons, and hadrons produced  
749 by the ATLAS detector. Generically, calorimeters work by stopping particles in their  
750 material, and measuring the energy deposition. This energy is deposited as a cascade  
751 particles induce from interactions with the detector material known *showers*. ATLAS  
752 uses *sampling* calorimeters; these alternate a dense absorbing material, which induces  
753 showers, with an active layer which measures energy depositions by the induced  
754 showers. Since some energy is deposited into the absorption layers as well, the energy  
755 depositions must be properly calibrated for the detector.

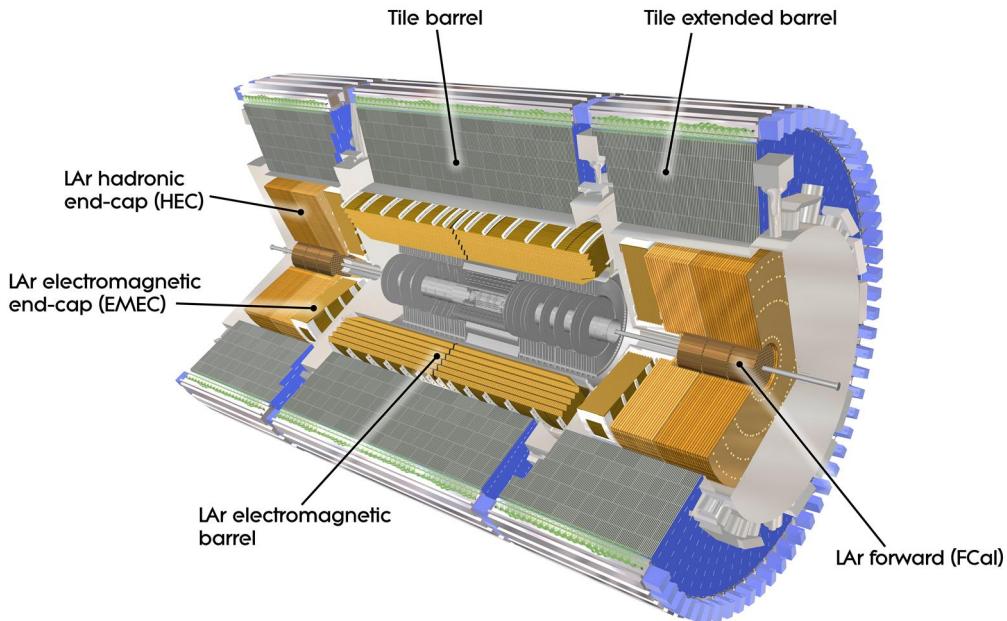


Figure 5.7: The ATLAS calorimeter

756 Electromagnetic objects (electrons and photons) and hadrons have much different  
 757 interaction properties, and thus we need different calorimeters to accurately measure  
 758 these different classes of objects; we can speak of the *electromagnetic* and *hadronic*  
 759 calorimeters. ATLAS contains four separate calorimeters : the liquid argon (LAr)  
 760 electromagnetic barrel calorimeter, the Tile barrel hadronic calorimeter, the LAr  
 761 endcap electromagnetic calorimeter, the LAr endcap hadronic calorimeter, and the  
 762 LAr Forward Calorimeter (FCal). Combined, these provide full coverage in  $\phi$  up to  
 763  $|\eta| < 4.9$ , and can be seen in Fig.5.7.

## 764 **Electromagnetic Calorimeters**

765 The electromagnetic calorimeters of the ATLAS detector consist of the barrel and  
 766 endcap LAr calorimeters. These are arranged into an ingenious “accordion” shape,  
 767 shown in 5.8, which allows full coverage in  $\phi$  and exceptional coverage in  $\eta$  while  
 768 still allowing support structures for detector operation. The accordion is made of



Figure 5.8: A schematic of a subsection of the barrel LAr electromagnetic calorimeter

769 layers with liquid argon (active detection material) and lead (absorber) to induce  
 770 electromagnetic showers. The LAr EM calorimeters are each more than 20 radiation  
 771 lengths deep, which provides the high stopping power necessary to properly measure  
 772 the electromagnetic showers.

773 The barrel component of the LAr EM calorimeter extends from the center of the  
 774 detector out to  $|\eta| < 1.475$ . The calorimeter has a presampler, which measures the  
 775 energy of any EM shower induced before the calorimeter. This has segmentation of  
 776  $\Delta\eta = 0.025, \Delta\phi = .01$ . There are three “standard” layers in the barrel, which have  
 777 decreasing segmentation into calorimeter *cells* as one travels radially outward from  
 778 the interaction point. The first layer has segmentation of  $\Delta\eta = 0.003, \Delta\phi = .1$ , and  
 779 is quite thin relative to the other layers at only 4 radiation lengths deep. It provides  
 780 precise  $\eta$  and  $\phi$  measurements for incoming EM objects. The second layer is the  
 781 deepest at 16 radiation lengths, with a segmentation of  $\Delta\eta = 0.025, \Delta\phi = 0.025$ . It



Figure 5.9: A schematic of Tile hadronic calorimeter

is primarily responsible for stopping the incoming EM particles, which dictates its large relative thickness, and measures most of the energy of the incoming particles. The third layer is only 2 radiation lengths deep, with a rough segmentation of  $\Delta\eta = 0.05$ ,  $\Delta\phi = .025$ . The deposition in this layer is primarily used to distinguish hadrons interacting electromagnetically and entering the hadronic calorimeter from the strictly EM objects which are stopped in the second layer.

The barrel EM calorimeter has a similar overall structure, but extends from  $1.4 < |\eta| < 3.2$ . The segmentation in  $\eta$  is better in the endcap than the barrel; the  $\phi$  segmentation is the same. In total, the EM calorimeters contain about 190000 individual calorimeter cells.

## Hadronic Calorimeters

The hadronic calorimetry of ATLAS sits directly outside the EM calorimetry. It contains three subdetectors : the barrel Tile calorimeter, the endcap LAr calorimeter,

795 and the Forward LAr Calorimeter. Similar to the EM calorimeters, these are  
796 sampling calorimeters that alternate steel (dense material) with an active layer  
797 (plastic scintillator).

798 The barrel Tile calorimeter extends out to  $|\eta| < 1.7$ . There are again three layers,  
799 which combined give about 10 interactions length of distance, which provides excellent  
800 stopping power for hadrons. This is critical to avoid excess *punchthrough* to the muon  
801 spectrometer beyond the hadronic calorimeters. The first layer has a depth of 1.5  
802 interaction lengths. The second layer is again the thickest at a depth of 4.1 interaction  
803 lengths; most of the energy of incoming particle is deposited here. Both the first and  
804 second layer have segmentation of about  $\Delta\eta = 0.1, \Delta\phi = 0.1$ . Generally, one does not  
805 need as fine of granularity in the hadronic calorimeter, since the energy depositions  
806 in the hadronic calorimeters will be summed into the composite objects we know as  
807 jets. The third layer has a thickness of 1.8 interaction lengths, with a segmentation of  
808  $\Delta\eta = 0.2, \Delta\phi = 0.1$ . The use of multiple layers allows one to understand the induced  
809 hadronic shower as it propagates through the detector material.

810 The endcap LAr hadronic calorimeter covers the region  $1.5 < |\eta| < 3.2$ . It is  
811 again a sampling calorimeter; the active material is LAr with a copper absorbed. It  
812 does not use the accordion shape of the other calorimeters; it has a “standard” flat  
813 shape perpendicular to the interaction point. The segmentation varies with  $\eta$ . For  
814  $1.5 < |\eta| < 2.5$ , the cells are  $\Delta\eta = 0.1, \Delta\phi = 0.1$ ; in the region  $2.5 < |\eta| < 3.2$ , the  
815 cells are  $\Delta\eta = 0.2, \Delta\phi = 0.2$  in size.

816 The final calorimeter in ATLAS is the forward LAr calorimeter. Of those  
817 subdetectors which are used for standard reconstruction techniques, the FCal sits  
818 at the most extreme values of  $3.1 < |\eta| < 4.9$ . The FCal itself is made of three  
819 subdetectors; FCal1 is actually an electromagnetic module, while FCal2 and FCal3  
820 are hadronic. The absorber in FCal1 is copper, with a liquid argon active medium.  
821 FCal2 and FCal3 also use a liquid argon active medium, with a tungsten absorber.

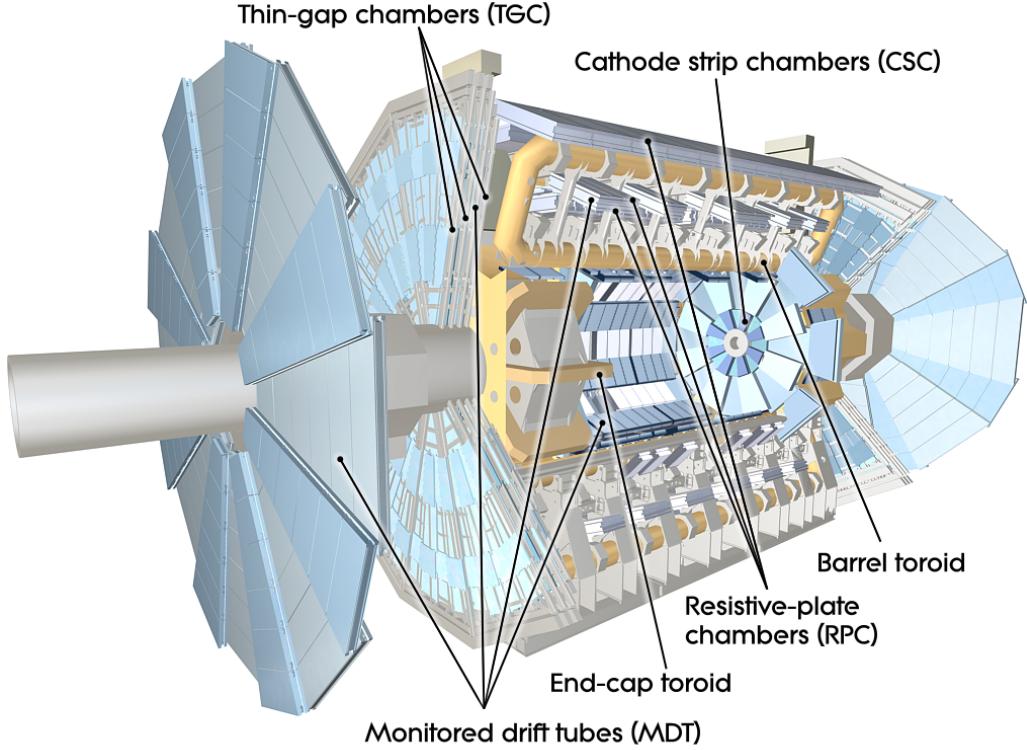


Figure 5.10: The ATLAS muon spectrometer

## 822 5.4 Muon Spectrometer

823 The muon spectrometer is the final major subdetector of the ATLAS detector.  
824 The muon spectrometer sits outside the hadronic calorimetry, with pseudorapidity  
825 coverage out to  $|\eta| < 2.7$ . The MS is a huge detector, with some detector elements  
826 existing as far as 11 m in radius from the interaction point. This system is used  
827 almost exclusively to measure the momenta of muons; these are the only measured  
828 SM particles which consistently exit the hadronic calorimeters. These systems provide  
829 a rough measurement, which is used in triggering (described in Ch.5.5), and a precise  
830 measurement to be used in offline event reconstruction as described in Ch.???. The  
831 MS produces tracks in a similar way to the ID; the hits in each subdetector are  
832 recorded and then tracks are produced from these hits. Muon spectrometer tracks are  
833 largely independent of the ID tracks due to the independent solenoidal and toroidal  
834 magnet systems used in the ID and MS respectively. The MS consists of four separate

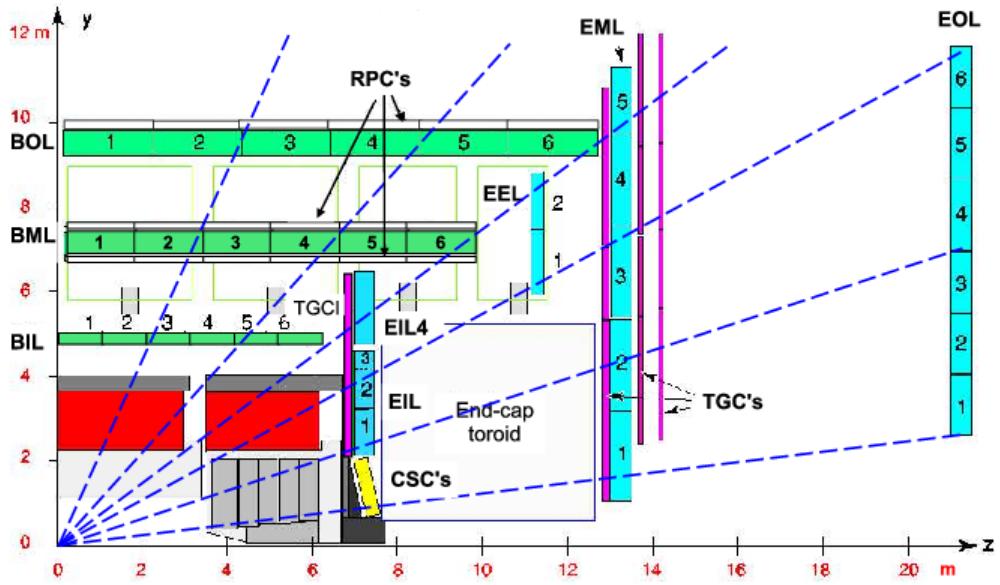


Figure 5.11: A schematic in  $z/\eta$  showing the location of the subdetectors of the muon spectrometer

835 subdetectors: the barrel region is covered by the Resistive Plate Chambers (RPCs)  
 836 and Monitored Drift Tubes (MDTs) while the endcaps are covered by MDTs, Thin  
 837 Gap Chambers (TGCs), and Cathode Strip Chambers (CSCs).

## 838 Monitored Drift Tubes

839 The MDT system is the largest individual subdetector of the MS. MDTs provide  
 840 precision measurements of muon momenta as well as fast measurements used for  
 841 triggers. There are 1088 MDT chambers providing coverage out to pseudorapidity  
 842  $|\eta| < 2.7$ ; each consists of an aluminum tube containing an argon- $\text{CO}_2$  gas mixture.  
 843 In the center of each tube there  $50\mu\text{m}$  diameter tungsten-rhenium wire at a voltage of  
 844 3080 V. A muon entering the tube will induce ionization in the gas, which will “drift”  
 845 towards the wire due to the voltage. One measures this ionization as a current in the  
 846 wire; this current comes with a time measurement related to how long it takes the  
 847 ionization to drift to the wire.

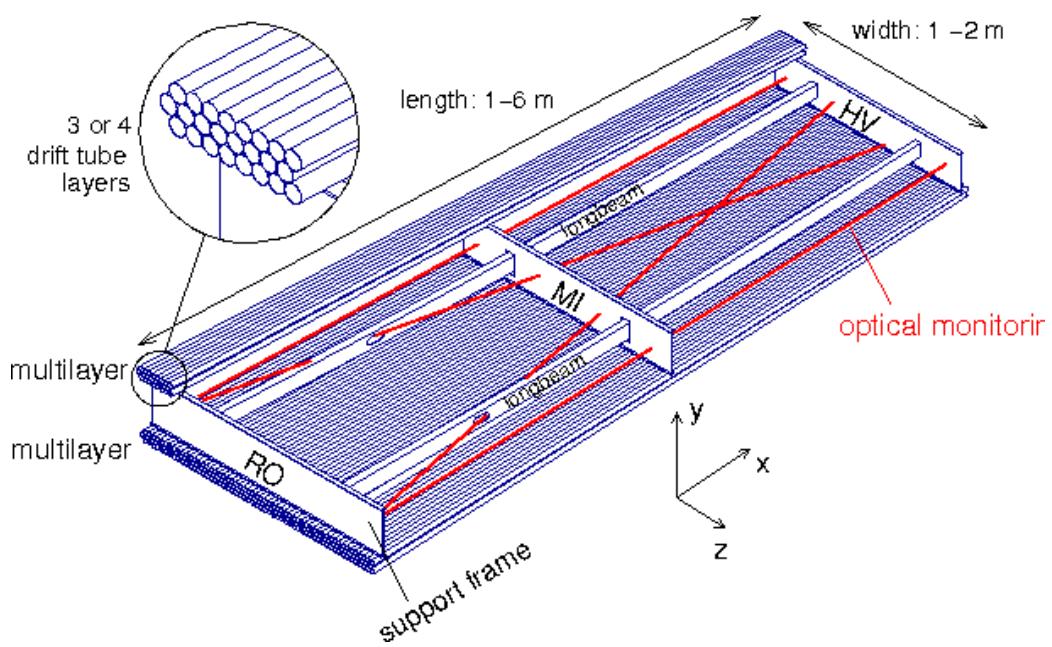


Figure 5.12: Schematic of a Muon Drift Tube chamber

848 These tubes are layered in a pattern shown in Fig.5.12. Combining the measure-  
849 ments from the tubes in each layer gives good position resolution. The system consists  
850 of three subsystems of these layers, at 5 m, 7m, and 9 m from the interaction point.  
851 The innermost layer is directly outside the hadronic calorimeter. The combination of  
852 these three measurements gives precise momenta measurements for muons.

## 853 Resistive Plate Chambers

854 The RPC system is alternated with the MDT system in the barrel; the first two layers  
855 of RPC detectors surround the second MDT layer while the third is outside the final  
856 MDT layer. The RPC system covers pseudorapidity  $|\eta| < 1.05$ . Each RPC consists  
857 of two parallel plates at a distance of 2 mm surrounding a  $\text{C}_2\text{H}_2\text{F}_4$  mixture. The  
858 electric field between these plates is 4.9k kV/mm. Just as in the MDTs, an incoming  
859 muon ionizes the gas, and the deposited ionization is collected by the detector (in this  
860 case on the plates). It is quite fast, but with a relatively poor spatial resolution of  
861 1 cm. Still, it can provide reasonable  $\phi$  resolution due to its large distance from the  
862 interaction point. This is most useful in triggering, where the timing requirements are  
863 quite severe. The RPCs are also complement the MDTs by providing a measurement  
864 of the non-bending coordinate.

## 865 Cathode Strip Chambers

866 The CSCs are used in place of MDTs in the first layer of the endcaps. This region, at  
867  $2.0 < |\eta| < 2.7$ , has higher particle multiplicity at the close distance to the interaction  
868 point from low-energy photons and neutrons. The MDTs were not equip to deal with  
869 the higher particle rate of this region, so the CSCs were designed to deal with this  
870 deficiency.

871 Each CSC consists multiwire proportional chambers, oriented radially outward  
872 from the interaction point. These chambers overlap partially in  $\phi$ . The wires contain



Figure 5.13: Photo of the installation of Cathode Strip Chambers and Monitored Drift Tubes

873 a gas mixture of argon and CO<sub>2</sub>, which is ionized when muons enter. The detectors  
874 operate with a voltage of 1900 V, with much lower drift times than the MDTs. They  
875 provide less hits than MDTs, but their lower drift times lower uptime and reduce the  
876 amount of detector overload.

877 The CSCs are arranged into four planes on the wheels of the muon spectrometer,  
878 as seen in Fig.???. There are 32 CSCs in total, with 16 on each side of the detector  
879 in  $\eta$ .

## 880 Thin Gap Chambers

881 The TGCs serve the purpose of the RPCs in the endcap at pseudorapidity of  $1.05 <$   
882  $|\eta| < 2.4$ ; they provide fast measurements used in triggering. The TGCs are also  
883 multiwire proportional chambers a la the CSCs. The fast readouts necessary for  
884 trigger are provided by a high electric field and a small wire-to-wire distance of 1.8  
885 mm. These detectors provide both  $\eta$  and  $\phi$  information, allowing the trigger to use  
886 as much information as possible when selecting events.



Figure 5.14: Photo of a muon Big Wheel, consisting of Thin Gap Chambers

## 887 5.5 Trigger System

888 The data rate delivered by the LHC is staggering [89]. In the 2016 dataset, the  
889 collision rate was 40 MHz, meaning a *bunch spacing* of 25 ns. In each of the event,  
890 as we saw in Ch.??, there are many proton-proton collisions. Most of the collisions  
891 are uninteresting, such as elastic scattering of protons, or even inelastic scattering  
892 leading to low-energy dijet events. These types of events have been studied in detail  
893 in previous experiments.

894 Even if one is genuinely interested in these events, it's *impossible* to save all of  
895 the information available in each event. If all events were written "to tape" (as the  
896 jargon goes), ATLAS would store terabytes of data per second. We are limited to only  
897 about 1000 Hz readout by computing processing time and storage space. We thus  
898 implement a *trigger* which provides fast inspection of events to drastically reduce  
899 the data rate from the 40 MHz provided by the LHC to the 1000 Hz we can write to  
900 tape for further analysis.

901     The ATLAS trigger system consists of a two-level trigger, known as the Level-  
902     1 trigger (L1 trigger) and the High-Level Trigger (HLT)<sup>4</sup>. Trigger selections are  
903     organized into *trigger chains*, where events passing a particular L1 trigger are passed  
904     to a corresponding HLT trigger. For example, one would require a particular high- $p_T$   
905     muon at L1, with additional quality requirements at HLT. One can also use HLT  
906     triggers as prerequisites for each other, as is done in some triggers requiring both jets  
907     and  $E_T^{\text{miss}}$ .

## 908     **Level-1 Trigger**

909     The L1 trigger is hardware-based, and provides the very fast rejection needed to  
910     quickly select events of interest. The L1 trigger uses only what is known as *prompt*  
911     data to quickly identify interesting events. Only the calorimeters and the triggering  
912     detectors (RPCs and TGCs) of the MS are fast enough to be considered at L1,  
913     since the tracking reconstruction algorithms used by the ID and the more precise  
914     MS detectors are very slow. This allows quick identification of events with the  
915     most interesting physical objects : large missing transverse momentum and high-  
916      $p_T$  electrons, muons, and jets.

917     L1 trigger processing is done locally. This means that events are selected without  
918     considering the entire available event. Energy deposits over some threshold are  
919     reconstructed as *regions of interest*. These RoIs are then compared using pattern  
920     recognition hardware to “expected” patterns for the given RoIs. Events with RoIs  
921     matching these expected patterns are then handed to the HLT through the Central  
922     Trigger Processor. This step alone lowers the data rate down by about three orders  
923     of magnitude.

---

<sup>4</sup>In Run1, ATLAS ran with a three-level trigger system. The L1 was essentially as today; the HLT consisted of two separate systems known as the L2 trigger and the Event Filter (EF). This was changed to the simpler system used today during the shutdown between Run1 and Run2.

924 **High-Level Trigger**

925 The HLT performs the next step, taking the incoming data rate from the L1 trigger  
926 of  $\sim 75$  kHz down to the  $\sim 1$  kHz that can be written to tape. The HLT really  
927 performs much like a simplified offline reconstruction, using many common quality  
928 and analysis cuts to eliminate uninteresting events. This is done by using computing  
929 farms located close to the detector, which process events in parallel. Individually, each  
930 event which enters the computing farms takes about 4 seconds to reconstruct; the  
931 HLT reconstruction time also has a long tail, which necessitates careful monitoring  
932 of the HLT to ensure smooth operation.

933 HLT triggers are targetted to a particular physics process, such as a  $E_T^{\text{miss}}$  trigger,  
934 single muon trigger, or multijet trigger. The collection of all triggers is known as  
935 the trigger *menu*. Since many low-energy particles are produced in collisions, it is  
936 necessary to set a *trigger threshold* on the object of interest; this is really just a fancy  
937 naming for a trigger  $p_T$  cut. Due to the changing luminosity conditions of the LHC,  
938 these thresholds change constantly, mostly by increasing thresholds with increasing  
939 instantaneous luminosity. This allows an approximately constant number of events to be  
940 written for further analysis. Triggers which have rates higher than those designated  
941 by the menu are *prescaled*. This means writing only some fraction of the triggered  
942 events. Of course, for physics analyses, one wishes to investigate all data events  
943 passing some set of analysis cuts, so often one uses the “lowest threshold unprescaled  
944 trigger”. *Turn-on curves* allow one to select the needed offline analysis cut to ensure  
945 the trigger is fully efficient. An example turn-on curve for the  $E_T^{\text{miss}}$  triggers used in  
946 the signal region of this analysis is shown in ??.

947 The full set of the lowest threshold unprescaled triggers considered here can be  
948 found in Table 5.1. These are the lowest unprescaled triggers associated to the SUSY  
949 signal models and Standard Model backgrounds considered in this thesis. More  
950 information can be found in [89].

Physics Object	Trigger	$p_T$ (GeV)	Threshold	Level-1 Seed	Additional Requirements	Approximate Rate (Hz)
<b>2015 Data</b>						
$E_T^{\text{miss}}$	HLT_xe70	70	L1_XE50	-	60	
Muon	HLT_mu24_iloose_L1MU15	50	L1_MU15	isolated, loose	130	
Muon	HLT_mu50	50	L1_MU15	-	30	
Electron	HLT_e24_1hmedium_ll2base_L1EM20VH		L1_EM20VH	medium OR isolated, loose	140	
Electron	HLT_e60_1hmedium	60	L1_EM20VH	medium	10	
Electron	HLT_e120_1hloose	120	L1_EM20VH	loose	<10	
Photon	HLT_g120_loose	120	L1_EM20VH	loose	20	
<b>2016 Data</b>						
$E_T^{\text{miss}}$	HLT_xe100_mht_L1XE5000		L1_XE50	-	180	
Muon	HLT_mu24_ivarmedium4		L1_MU20	medium	120	
Muon	HLT_mu50	50	L1_MU20	-	40	
Electron	HLT_e24_1htight_noD1ivarloose		L1_EM22VHI	tight with no $d_0$ or loose	110	
Electron	HLT_e60_1hmedium_nd60		L1_EM22VHI	medium with no $d_0$	10	
Electron	HLT_e140_1hloose_noD0		L1_EM22VHI	loose with no $d_0$	<10	
Photon	HLT_g140_loose	140	L1_EM22VHI	loose	20	

Table 5.1: High-Level Triggers used in this thesis. Descriptions of loose, medium, tight, and isolated can be found in [89]. The  $d_0$  cut refers to a quality cut on the vertex position; this was removed from many triggers in 2016 to increase sensitivity to displaced vertex signals. For most triggers, the increased thresholds in 2016 compared to 2016 were designed to keep the rate approximately equal. The exception is the  $E_T^{\text{miss}}$  triggers; see 5.5.

951 **Razor Triggers**

952 For the analysis presented in this thesis, the *razor triggers* were developed. These are  
953 topological triggers, combining both jet and  $E_T^{\text{miss}}$  information to select interesting  
954 events. In particular, they use the razor variable  $M_{\Delta}^R$  which will be described in  
955 Chapter ??.

956 Based on 2015 run conditions, these triggers would have allowed the use of a lower  
957 offline  $E_T^{\text{miss}}$  cut with a similar rate to the nominal  $E_T^{\text{miss}}$  triggers. This can be seen  
958 in the turn-on curves shown in Figure 5.15. The razor triggers are fully efficient at  
959 nearly 100 GeV lower than the corresponding  $E_T^{\text{miss}}$  triggers in  $M_{\Delta}^R$ .

960 There was a quite big change in the 2016 menu, which increased the rate given to  
961  $E_T^{\text{miss}}$  triggers drastically. This can be seen in the difference in rate shown between  
962  $E_T^{\text{miss}}$  triggers in 2015 and 2016 in Table 5.1. This allowed the  $E_T^{\text{miss}}$  triggers to  
963 maintain a lower threshold throughout the dataset used in this thesis.

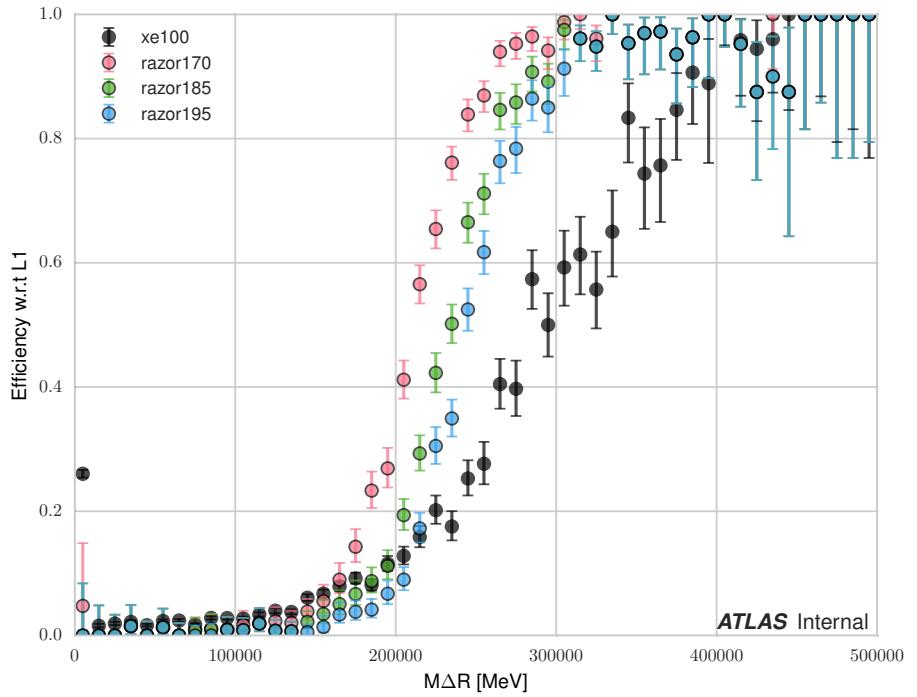
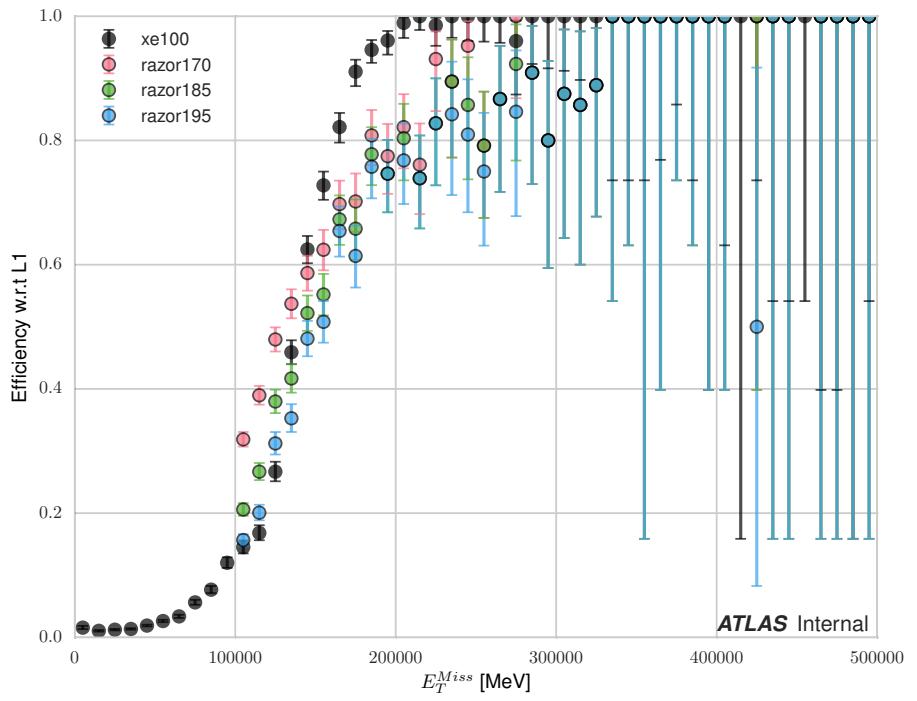


Figure 5.15: Turn-on curves for the razor triggers and nominal  $E_T^{\text{miss}}$  trigger. The razor triggers show a much sharper turn-on in  $M_D^R$  relative to the  $E_T^{\text{miss}}$  trigger. The converse is true for the  $E_T^{\text{miss}}$  triggers.



## Object Reconstruction

966 This chapter describes the reconstruction algorithms used within ATLAS. We will  
967 make the distinction between the “primitive” objects which are reconstructed from  
968 the detector signals from the “composite” physics objects we use in measurements  
969 and searches for new physics.

### 970 6.1 Primitive Object Reconstruction

971 The primitive objects reconstructed by ATLAS are *tracks* and (calorimeter) *clusters*.  
972 These are reconstructed directly from tracking hits and calorimeter energy deposits  
973 into cells. Tracks can be further divided into inner detector and muon spectrom-  
974 eter tracks. Calorimeter clusters can be divided into sliding-window clusters and  
975 topological clusters (topoclusters).

#### 976 Inner Detector Tracks

977 Inner detector tracks are reconstructed from hits in the inner detector [90, 91] These  
978 hits indicate that a charged particle has passed through the detector material. Due  
979 to the 2 T solenoid in the inner detector, the hits associated with any individual  
980 particle will be curved. The amount of curvature determines the momentum of the  
981 particle. In any given event, there are upwards of  $10^4$  hits, making it impossible to do  
982 any sort of combinatorics to reconstruct tracks. There are two algorithms used by  
983 ATLAS track reconstruction, known as *inside-out* and *outside-in*.

984     ATLAS first employs the inside-out algorithm. One assumes the track begins  
985 at the interaction point. Moving out from the interaction point, one creates track  
986 seeds. Track seeds are proto-tracks constructed from three hits. These hits can be  
987 distributed as three pixel hits, two pixel hits and one SCT hit, or three SCT hits.  
988 One extrapolates the track and uses a combinatorial Kalman filter[90], which adds  
989 the rest of the pixel and SCT hits to the seeds. This is done seed by seed, so it  
990 avoids the combinatorial complexity involved with checking all hits with all seeds.  
991 At this point, the algorithm applies an additional filter to avoid ambiguities from  
992 nearby tracks. The TRT hits are added to the seeds using the same method. After  
993 this procedure, all hits are associated to a track.

994     The next step is to figure out the correct kinematics of the track. This is  
995 done by applying a fitting algorithm which outputs the best-fit track parameters  
996 by minimizing the track distance from hits, weighted by each hit's resolution. These  
997 parameters are  $(d_0, z_0, \eta, \phi, q/p)$  where  $d_0$  ( $z_0$ ) is the transverse (longitudinal) impact  
998 parameter and  $q/p$  is the charge over the track momenta. This set of parameters  
999 uniquely defines the measurement of the trajectory of the charged particle associated  
1000 to the track. An illustration of a track with these parameters is shown in Fig.6.1.

1001    The other track reconstruction algorithm is the outside-in algorithm. As the  
1002 name implies, we start from the outside of the inner detector, in the TRT, and  
1003 extend the tracks in toward the interaction point. One begins by seeding from  
1004 TRT hits, and extending the track back towards the center of the detector. The  
1005 same fitting procedure is used as in the inside-out algorithm to find the optimal  
1006 track parameters. This algorithm is particularly important for finding tracks which  
1007 originate from interactions with the detector material, especially the SCT. For tracks  
1008 from primary vertices, this often finds the same tracks as the inside-out algorithm,  
1009 providing an important check on the consistency of the tracking procedure.

1010    In the high luminosity environment of the LHC, even the tracks reconstructed

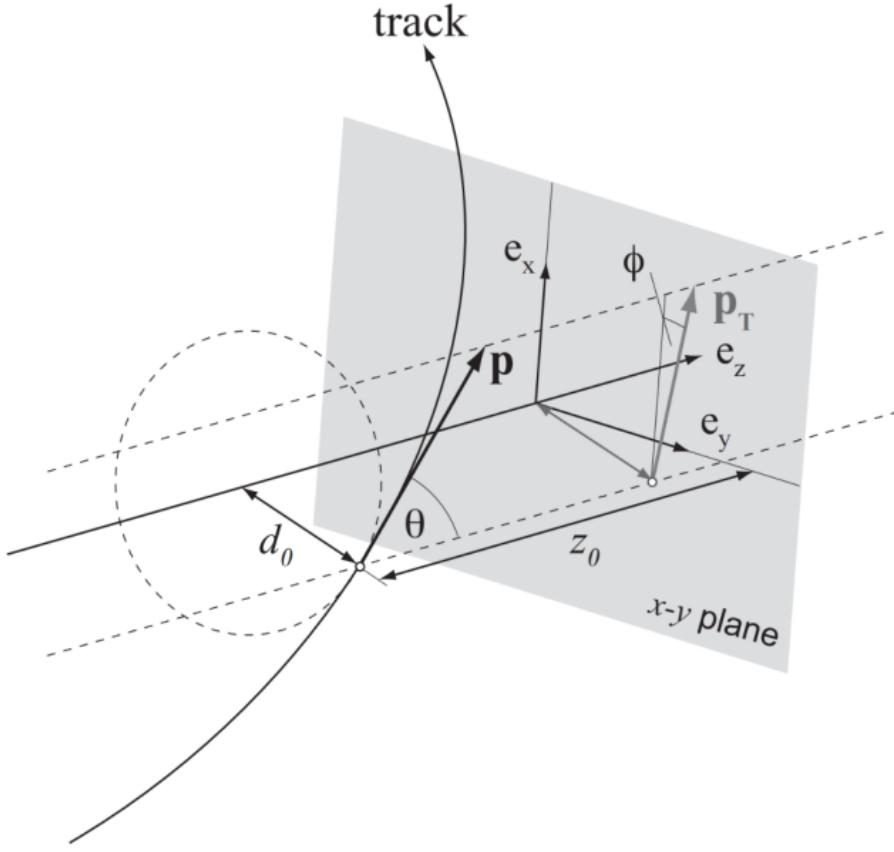


Figure 6.1: The parameters associated to a track.

from precision detectors such as those of ATLAS inner detector can sometimes lead to fake tracks from simple combinatoric chance. Several quality checks are imposed after track fitting which reduce this background. Seven silicon (pixel + SCT) hits are required for all tracks. No more than two *holes* are allowed in the pixel detector. Holes are expected measurements from the track that are missing in the pixel detector. Finally, tracks with poor fit quality, as measured by  $\chi^2/ndf$ , are also rejected. Due to the high quality of the silicon measurements in the pixel detector and SCT, these requirements give good track reconstruction efficiency, as seen in Fig.6.2 for simulated events[92].



(a) Track reconstruction as a function of  $p_T$ . (b) Track reconstruction as a function of  $\eta$ .

Figure 6.2: Track reconstruction efficiency as a function of track  $p_T$  and  $\eta$ . The efficiency is defined as the number of reconstructed tracks divided by the number of generate charged particles.

## 1020 Sliding-window clusters

1021 The sliding-window algorithm is a way to combine calorimeter cells into composite  
 1022 objects (clusters) to be used as inputs for other algorithms[93]. Sliding-window  
 1023 clusters are the primary inputs to electron and photon reconstruction, as described  
 1024 below. The electromagnetic calorimeter has high granularity, with a cell size of  
 1025  $(\eta, \phi) = (.025, .025)$  in the coarsest second layer throughout most of the calorimeter.  
 1026 The “window” consists of 3 by 5 cells in the  $(\eta, \phi)$  space. All layers are added on  
 1027 this same 2D space. One translates this window over the space and seeds a cluster  
 1028 whenever the energy sum of the cells is maximized. If the seed energy is greater  
 1029 than 2.5 GeV, this seed is called a sliding-window cluster. This choice was motivated  
 1030 to optimize the reconstruction efficiency of proto-electrons and proto-photons while  
 1031 rejecting fakes from electronic noise and additional particles from pileup vertices.

## 1032 Topological clusters

1033 Topoclusters are the output of the algorithm used within ATLAS to combine  
1034 hadronic and electromagnetic calorimeter cells in a way which extracts signal from  
1035 a background of significant electronic noise[94]. They are the primary input to the  
1036 algorithms which reconstruct jets.

1037 Topological clusters are reconstructed from calorimeter cells in the following way.  
1038 First, one maps all cells onto a single  $\eta - \phi$  plane so one can speak of *neighboring*  
1039 cells. Two cells are considered neighboring if they are in the same layer and directly  
1040 adjacent, or if they are in adjacent layers and overlap in  $\eta - \phi$  space. The *significance*  
1041  $\xi_{\text{cell}}$  of a cell during a given event is

$$\xi_{\text{cell}} = \frac{E_{\text{cell}}}{\sigma_{\text{noise},\text{cell}}} \quad (6.1)$$

1042 where  $\sigma_{\text{noise},\text{cell}}$  is measured for each cell in ATLAS and  $E_{\text{cell}}$  measures the current  
1043 energy level of the cell. One thinks of this as the measurement of the energy *over*  
1044 *threshold* for the cell.

1045 Topocluster *seeds* are defined as calorimeter cells which have a significance  $\xi_{\text{cell}} >$   
1046 4. These are the inputs to the algorithm. One iteratively tests all cells adjacent  
1047 to these seeds for  $\xi_{\text{cell}} > 2$ . Each cells passing this selection is then added to the  
1048 topocluster, and the procedure is repeated. When the algorithm reaches the point  
1049 where there are no additional adjacent cells with  $\xi_{\text{cell}} > 2$ , every positive-energy cell  
1050 adjacent to the current proto-cluster is added. The collection of summed cells is a  
1051 topocluster. An example of this procedure for a simulation dijet event is shown in  
1052 Fig.6.3.

1053 There are two calibrations used for clusters[95]. These are known as the  
1054 electromagnetic (EM) scale and the local cluster weighting (LCW) scale. The EM  
1055 scale is the energy read directly out of the calorimeters as described. This scale  
1056 is appropriate for electromagnetic processes. The LCW scale applies additional



Figure 6.3: Example of topoclustering on a simulated dijet event.

1057 scaling to the clusters based on the shower development. The cluster energy can be  
1058 corrected for calorimeter non-compensation and the differences in the hadronic and  
1059 electromagnetic calorimeters’ responses. This scale provides additional corrections  
1060 that improve the accuracy of hadronic energy measurements. This thesis only uses  
1061 the EM scale corrections. LCW scaling requires additional measurements that only  
1062 became available with additional data. Due to the jet calibration procedure that  
1063 we will describe below, it is also a relatively complicated procedure to rederive the  
1064 “correct” jet energy.

## 1065 Muon Spectrometer Tracks

1066 Muon spectrometer tracks are fit using the same algorithms as the ID tracks, but  
1067 different subdetectors. The tracks are seeded by hits in the MDTs or CSCs. After  
1068 seeding in the MDTs and CSCs, the hits from all subsystems are refit as the final  
1069 MS track. These tracks are used as inputs to the muon reconstruction, as we will see  
1070 below.

## 1071 6.2 Physics Object Reconstruction and Quality

### 1072 Identification

1073 There are essentially six objects used in ATLAS searches for new physics: electrons,  
1074 photons, muons,  $\tau$ -jets, jets, and  $E_T^{\text{miss}}$ . The reconstruction of these objects is  
1075 described here. In this thesis,  $\tau$  lepton jets are not treated differently from other  
1076 hadronic jets, and we will not consider their reconstruction algorithms. A very  
1077 convenient summary plot is shown in Fig.6.4.

1078 One often wishes to understand “how certain” we are that a particular object  
1079 is truly the underlying physics object. In ATLAS, we often generically consider, in



Figure 6.4: The interactions of particles with the ATLAS detector. Solid lines indicate the particle is interacting with the detector, while dashed lines are shown where the particle does not interact.

1080 order, *very loose*, *loose*, *medium*, and *tight* objects<sup>1</sup>. These are ordered in terms of  
 1081 decreasing object efficiency, or equivalently, decreasing numbers of fake objects. We  
 1082 will also describe briefly the classification of objects into these categories.

1083 In this thesis, since we present a search for new physics in a zero lepton final state,  
 1084 we will provide additional details about jet and  $E_T^{\text{miss}}$  reconstruction.

---

<sup>1</sup> These are not all used for all objects, but it's conceptually useful to think of these different categories.

## 1085 Electrons and Photons

### 1086 Reconstruction

1087 The reconstruction of electrons and photons (often for brevity called “electromagnetic  
1088 objects”) is very similar [93, 96, 97]. This is because the reconstruction begins with  
1089 the energy deposit in the calorimeter in the form of an electromagnetic shower. For  
1090 any incoming  $e/\gamma$ , this induces many more electrons and photons in the shower. The  
1091 measurement in the calorimeter is similar for these two objects.

1092 One begins the reconstruction of electromagnetic objects from the sliding-window  
1093 clusters reconstructed from the EM calorimeter. These  $E > 2.5$  GeV clusters the  
1094 the primary seed for electrons and photons. One then looks for all ID tracks within  
1095  $\Delta R < 0.3$ , where  $\Delta R = \sqrt{\Delta\eta^2 + \Delta\phi^2}$ . We “match” the track and cluster if they are  
1096 within  $\Delta\phi < 0.2$  in the direction of track curvature, or  $\Delta\phi < 0.05$  in the direction  
1097 opposite the track curvature. Those track-cluster seeds with tracks pointing to the  
1098 primary vertex are reconstructed as electrons.

1099 For photons, we have two options to consider, known as *converted* and *unconverted*  
1100 photons. Due to the high energy of the LHC collisions, typical photons have energy  
1101  $>\sim 1$  GeV. At this scale, photons interact almost exclusively via pair-production in  
1102 the presence of the detector material, as shown in Fig.6.5 [56]. If the track-cluster seed  
1103 has a track which does not point at the primary vertex, we reconstruct this object as a  
1104 converted photon. This happens since the photon travels a distance before decay into  
1105 two electrons, and see the tracks coming from this secondary vertex. Those clusters  
1106 which do not have any associated tracks are then reconstruced as an unconverted  
1107 photon.

1108 The final step in electromagnetic object reconstruction is the final energy value  
1109 assigned to these objects. This process is different between electrons and photons due  
1110 to their differing signatures in the EM calorimeter. In the barrel, electrons energies

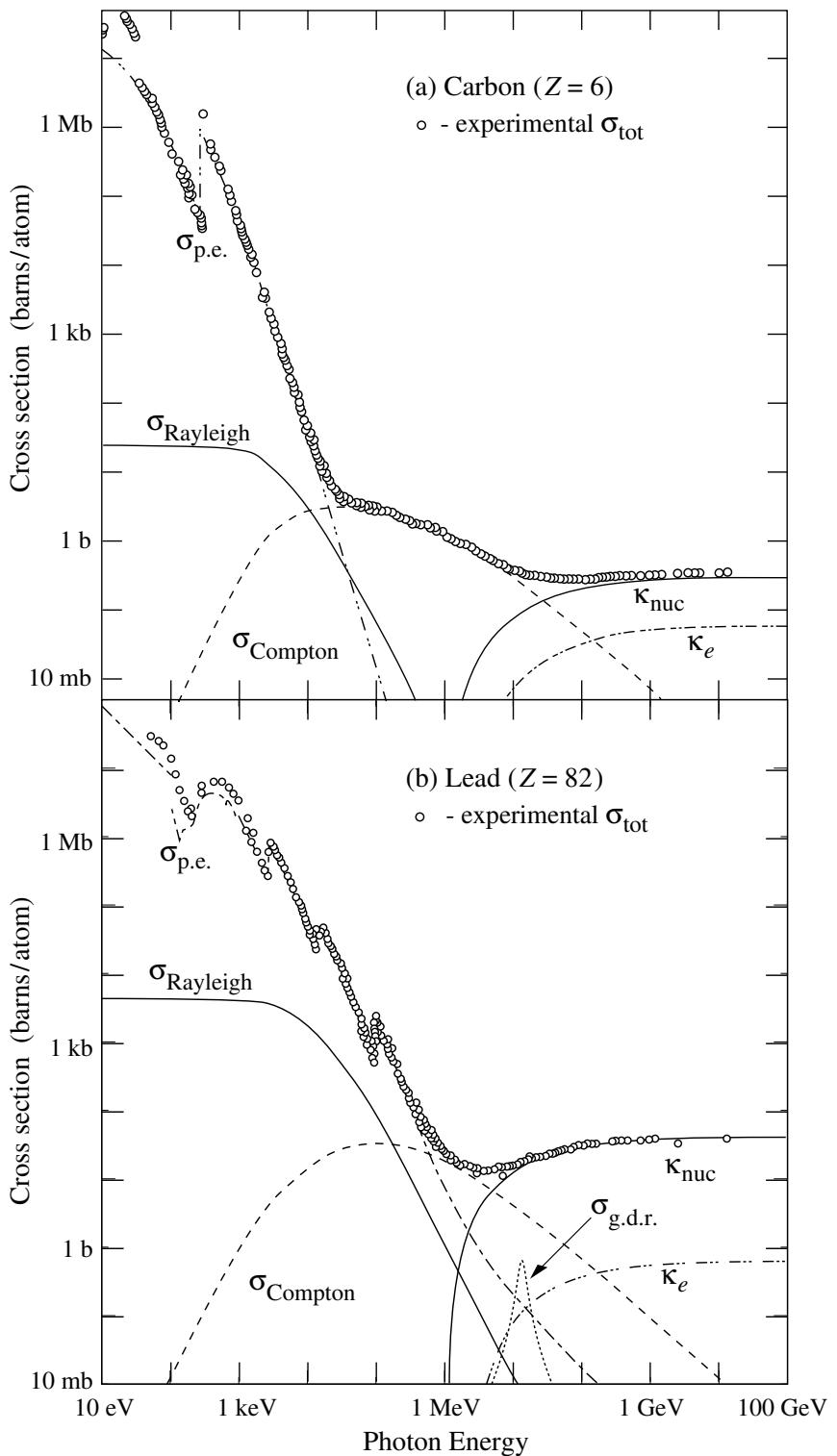


Figure 6.5: Photon total cross sections as a function of energy in carbon and lead, showing the contributions of different processes[56].

1111 are assigned as the sum of the 3 clusters in  $\eta$  and 7 clusters in  $\phi$  to account for the  
1112 electron curving in the  $\phi$  direction. Barrel photons are assigned the energy sum of  
1113 (3, 5) clusters in  $(\eta, \phi)$  space. In the endcap, the effect of the magnetic field on the  
1114 electrons is smaller, and there is a coarser granularity. Both objects sum the (5, 5)  
1115 clusters for their final energy value.

## 1116 Quality Identification

1117 Electrons have a number of important backgrounds which can give fakes. Fake  
1118 electrons come primarily from secondary vertices in hadron decays or misidentified  
1119 hadronic jets. To reduce these backgrounds, quality requirements are imposed on  
1120 electron candidates. Loose electrons have requirements imposed on the shower  
1121 shapes in the electromagnetic calorimeter and on the quality of the associated ID  
1122 track. There is also a requirement that there is a small energy deposition in the  
1123 hadronic calorimeter behind the electron, to avoid jets being misidentified as electrons  
1124 (low hadronic leakage). Medium and tight electrons have increasingly stronger  
1125 requirements on these variables, and additional requirements on the isolation (as  
1126 measured by  $\Delta R$ ) and matching of the ID track momentum and the calorimeter  
1127 energy deposit.

1128 Photons are relatively straightforward to measure, since there are few background  
1129 processes[98]. The primary one is pion decays to two photons, which can cause a jet  
1130 to be misidentified as photon. Loose photons have requirements on the shower shape  
1131 and hadronic leakage. Tight photons have tighter shower shape cuts, especially on  
1132 the high granularity first layer of the EM calorimeter. The efficiency for unconverted  
1133 tight photons as a function of  $p_T$  is shown in

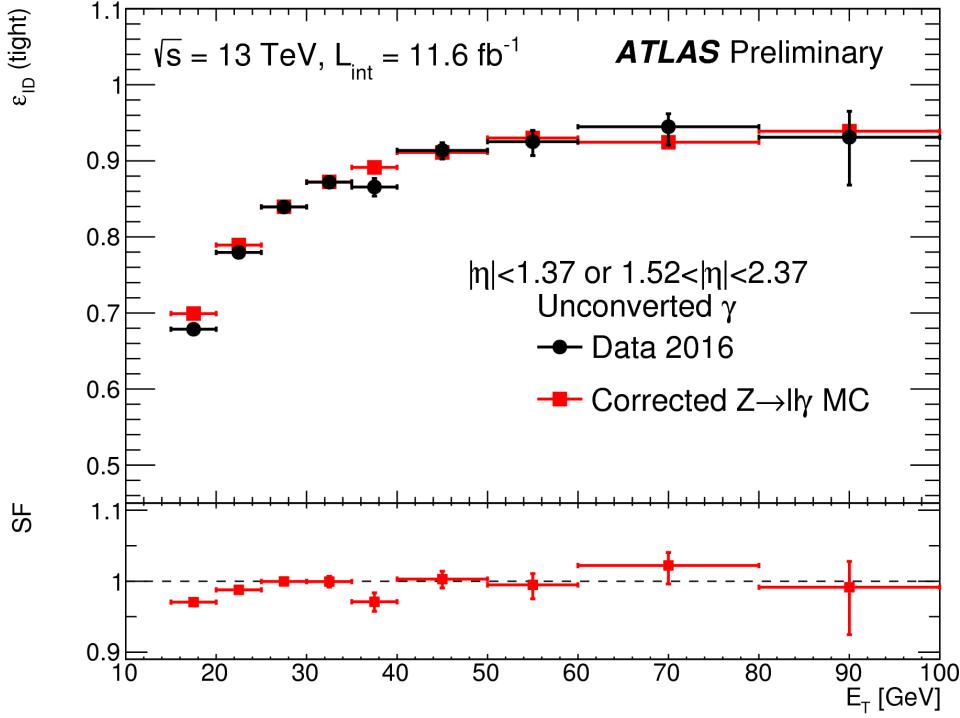


Figure 6.6: Unconverted photon efficiency as measured in [98].

## 1134 Muons

### 1135 Reconstruction

1136 Muons are reconstructed using measurements from all levels of the ATLAS detec-  
 1137 tor[99]. They leave a ID track, a small, characteristic deposition in the EM calorime-  
 1138 ter, and then a track in the muon spectrometer. The primary reconstruction technique  
 1139 produces a so-called *combined* muon. “Combined” means using a combination of the  
 1140 ID and MS tracks to produce the final reconstructed muon kinematics. This is done  
 1141 by refitting the hits associated to both tracks, and using this refit track for the muon  
 1142 kinematics. This process produces the best measured muons, although several other  
 1143 worse algorithms are used when the full detector information is missing. An example  
 1144 is in the region  $2.5 < |\eta| < 2.7$  outside the ID acceptance, where MS tracks are used  
 1145 without the corresponding ID tracks.

1146 **Quality Identification**

Several additional criteria are used to assure muon measurements are free of significant background contributions, especially from pion and kaon decays to muons. Muons produced via these decay processes are often characterized by a “kink”. Candidate muons with a poor fit quality, characterized by  $\chi^2/\text{n.d.f.}$ , are thus rejected. Additionally, the absolute difference in momentum measurements between the ID and MS provide another handle, since the other decay products from hadron decays carry away some amount of the initial hadron momentum. This is measured by

$$\rho' = \frac{|p_T^{\text{ID}} - p_T^{\text{MS}}|}{p_T^{\text{Combined}}}. \quad (6.2)$$

Additionally, there is a requirement on the  $q/p$  significance, defined as

$$S_{q/p} = \frac{|(q/p)^{\text{ID}} - (q/p)^{\text{MS}}|}{\sqrt{\sigma_{\text{ID}}^2 + \sigma_{\text{MS}}^2}}. \quad (6.3)$$

1147 The  $\sigma_{\text{ID,MS}}$  in the denominator of Eq.6.3 are the uncertainties on the corresponding  
1148 quantity from the numerator. Finally, cuts are placed on the number of hits in the  
1149 various detector elements.

1150 Subsequently tighter cuts on these variables allow one to define the different muon  
1151 identification criteria. Loose muons have the highest reconstruction efficiency, but  
1152 the highest number of fake muons, since there are no requirements on the number  
1153 of subdetector hits and the loosest requirements on the suite of quality variables.  
1154 Medium muons consist of Loose muons with tighter cuts on the quality variables.  
1155 They also require more than three MDT hits in at least two MDT layers. These are  
1156 the default used by ATLAS analyses. Tight muons have stronger cuts than those of  
1157 the medium selection, and reducing the reconstruction efficiency. The reconstruction  
1158 efficiency as a function of  $p_T$  can be seen for Medium muons in Fig.6.7.

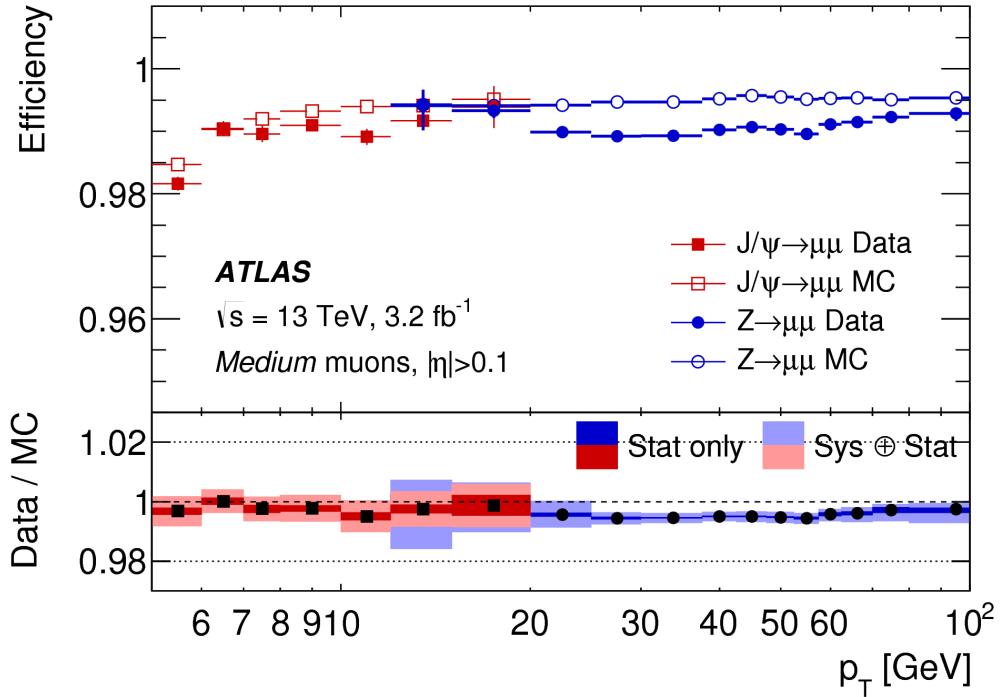


Figure 6.7: Medium muon efficiency as measured in [99].

## 1159 Jets

1160 Jets are composite objects corresponding to many physical particles [56, 100, 101]  
 1161 This is a striking difference from the earlier particles. Fortunately, we normally (and  
 1162 in this thesis) care about the original particle produced in primary collision. In the  
 1163 SM, this corresponds to quarks and gluons. Due to the hadronization process, free  
 1164 quarks and gluons spontaneously hadronize and produce a hadronic shower, which  
 1165 we call a jet. These showers can be measured by the EM and hadronic calorimeters,  
 1166 and the charged portions can be measured in the ID. The first question is how to  
 1167 combine these measurements into a composite object representing the underlying  
 1168 physical parton. This is done via jet algorithms.

## 1169 Jet Algorithms

1170 It might seem straightforward to combine the underlying physical particles into a  
1171 jet. There are three important characteristics required for any jet reconstruction  
1172 algorithm to be used by ATLAS.

- 1173     • Collinear safety - if any particle with four-vector  $p$  is replaced by two particles  
1174       of  $p_1, p_2$  with  $p = p_1 + p_2$ , the subsequent jet should not change  
  
1175     • Radiative (infrared) safety - if any particle with four-vector  $p$  radiates a particle  
1176       of energy  $\alpha \rightarrow 0$ , the subsequent jet should not change  
  
1177     • Fast - the jet algorithm should be “fast enough” to be useable by ATLAS  
1178       computing resources

1179 The first two requirements can be seen in terms of requirements on soft gluon emission.  
1180 Since partons emit arbitrarily soft gluons freely, one should expect the algorithms  
1181 to not be affected by this emission. The final requirement is of course a practical  
1182 limitation.

The algorithms in use by ATLAS (and CMS) which satisfies these requirements are collectively known as the  $k_T$ algorithms [102–104]. These algorithms iteratively combine the “closest” objects, defined using the following distance measures :

$$d_{ij} = \min(k_{T,i}^{2p}, k_{T,j}^{2p}) \frac{\Delta_{ij}^2}{R^2} \quad (6.4)$$
$$d_{iB} = k_{Ti}^{2p}$$

1183 In Eq.6.4,  $k_T, i$  is the transverse momentum of  $i$ -th jet *constituent*,  $\Delta_{ij}$  is the angular  
1184 distance between the constituents. Both  $R$  and  $p$  are adjustable parameters:  $R$  is  
1185 known as the (jet) *cone size* and  $p$  regulates the power of the energy versus the  
1186 geometrical scales. The algorithm sequence, for a given set of objects  $i$  with four-  
1187 vector  $k$  :

- 1188     1. Find the minimum distance in the set of all  $d_{ij}$  and  $d_{iB}$ .

1189     2. If the distance is one of the  $d_{ij}$ , combine the input pair of object  $i, j$  and return  
1190         to (1). If the distance is one of the  $d_{iB}$ , remove the object from the list, call it  
1191         a jet, and return to (1).

1192 This process ends when all objects  $i$  have been added to a jet.

1193 Any choice of  $(p, R)$  has the requirements of collinear and radiative safety. In  
1194 essence, the choice is then to optimize based on speed and the potential for new  
1195 physics discoveries. In ATLAS, we make the choice of  $p = -1$  which is also known  
1196 as the *anti- $k_T$*  algorithm. The choice of  $R = 0.4$  is used for the distance parameter of  
1197 the jets.

1198 The primary “nice” quality of this algorithm can be seen with the following  
1199 example. Consider three inputs to an anti- $k_T$  algorithm, all with  $\eta = 0$  :

- 1200     • Object 1 :  $(p_T, \phi) = (30 \text{ GeV}, 0)$   
1201     • Object 2 :  $(p_T, \phi) = (20 \text{ GeV}, -0.2)$   
1202     • Object 3 :  $(p_T, \phi) = (10 \text{ GeV}, 0.2)$   
1203     • Object 4 :  $(p_T, \phi) = (1 \text{ GeV}, 0.5)$

1204 . In the case shown, it seems natural to first combine the “bigger” objects 1 and 2.  
1205 These then pick up the extra small object 3, and object 4 is not included in the jet.  
1206 This is exactly what is done by the anti- $k_T$  algorithm. The (normal)  $k_T$  algorithm with  
1207  $p = 1$  instead combines the smallest objects, 3 and 4, first. Object 1 and 2 combine  
1208 to form their own jet, instead of these jets picking up object 3. This behavior is not  
1209 ideal due to the effects of pileup, as we will see in the next section.

## 1210 Jet Reconstruction

1211 In ATLAS, jets are reconstructed using multiple different objects as inputs, including  
1212 tracks, “truth” objects, calorimeter clusters, and *particle flow objects* (PFOs). For

1213 physics analyses, ATLAS primarily uses jets reconstructed from calorimeter clusters,  
1214 but we will describe the others here, as they are often used for derivations of  
1215 systematic uncertainties or future prospects.

1216 Calorimeter jets are reconstructed using topoclusters using the anti- $k_T$  algorithm  
1217 with  $R = 0.4$ . The jet reconstruction algorithm is run on the collection of all  
1218 topoclusters reconstructed as in Sec.6.1. Both EM and LCW scale clusters are used  
1219 in the ATLAS reconstruction software and produce two sets of jets for analysis. As  
1220 stated above, this thesis presents an analysis using jets reconstructed using EM scale  
1221 clusters, which we refer to these as *EM jets*.

1222 Tracks can be used as inputs to jet reconstruction algorithms. Jets reconstructed  
1223 from tracks are known as *track jets*. Since the ID tracks do not measure neutral  
1224 objects, these jets measure an incorrect energy. However, these are still useful for  
1225 checks and derivations of systematic uncertainties.

1226 *Truth* jets are reconstructed from *truth* particles. In this case, truth is jargon for  
1227 simulation. In simulation, the actual simulated particles are available and used as  
1228 inputs to the jet reconstruction algorithms. Similarly to track jets, these are not useful  
1229 in and of themselves. Instead, truth jets are used for comparisons and derivations of  
1230 systematic uncertainties.

1231 The last object used as inputs to jet reconstruction algorithms are *particle flow*  
1232 *objects* (PFOs). These are used extensively as the primary input to jet particle  
1233 reconstruction algorithms by the CMS collaboration[105]. Particle flow objects are  
1234 reconstructed by associating tracks and clusters through a combination of angular  
1235 distance measures and detector response measurements to create a composite object  
1236 which contains information from both the ID and the calorimeters. For calorimeter  
1237 clusters which do not have any associated ID track, the cluster is simply the PFO.  
1238 The natural association between tracks and clusters provides easy pileup subtraction  
1239 since tracks are easily associated to the primary vertex. This technique is generally

1240 used in CMS, and ATLAS has been slow to adopt the same. As pileup has increased,  
1241 the utility of using PFOs as inputs to jet reconstruction has increased as well.

## 1242 Jet Calibration

1243 Jets as described in the last section are still *uncalibrated*. Even correcting the cluster  
1244 energies using the LCW does not fully correct the jet energy, due to particles losing  
1245 energy in the calorimeters. The solution to this is the *jet energy scale* (JES). The  
1246 JES is a series of calibrations which on average restore the correct truth jet energy  
1247 for a given reconstructed jet. These steps are shown in Fig.6.8 and described here.

1248 The first step is the origin correction. This adjusts the jet to point at the  
1249 primary vertex. Next, is the jet-area based pileup correction. This step subtracts  
1250 the “average” pileup as measured by the energy density  $\rho$  outside of the jets and  
1251 assumes this is a good approximation for the pileup inside the jet. One then removes  
1252 energy  $\Delta E = \rho \times A_{\text{jet}}$  in this step. The residual pileup correction makes a final offset  
1253 correction by parametrizing the change in jet energy as a function of the number of  
1254 primary vertices  $N_{\text{PV}}$  and the average number of interactions  $\mu$ .

1255 The next step is the most important single correction, known as the AbsoluteEta-  
1256 JES step. Due to the use of non-compensation and sampling calorimeters in ATLAS,  
1257 the measured energy of a jet is a fraction of the true energy of the outgoing parton.  
1258 Additionally, due to the use of different technologies and calorimeters throughout the  
1259 detector, there are directional biases induced by these effects. The correction bins a  
1260 multiplicative factor in  $p_{\text{T}}$  and  $\eta$  which scales the reconstructed jets to corresponding  
1261 truth jet  $p_{\text{T}}$ . This step does not entirely correct the jets, since it is entirely a  
1262 simulation-based approach.

1263 The final steps are known as the global sequential calibration (GSC) and the  
1264 residual in-situ calibration. The GSC uses information about the jet showering shape  
1265 to apply additional corrections based on the expected shape of gluon or quark jets.

1266 The final step is the residual in-situ calibration, which is only applied to data. This  
1267 step uses well-measured objects recoiling off a jet to provide a final correction to the  
1268 jets in data. In the low  $p_T$  region ( $20 \text{ GeV} \sim < p_{T,\text{jet}} \sim < 200 \text{ GeV}$ ),  $Z \rightarrow ll$  events are  
1269 used as a reference object. In the middle  $p_T$  region ( $100 \text{ GeV} \sim < p_{T,\text{jet}} \sim < 600 \text{ GeV}$ ),  
1270 the reference object is a photon, while in the high  $p_T$  region ( $p_{T,\text{jet}} \sim > 200 \text{ GeV}$ ),  
1271 the high  $p_T$  jet is compared to multiple smaller  $p_T$  jets. The reference object is this  
1272 group of multijets. After this final correction, the data and MC scales are identical  
1273 up to the corresponding uncertainties. The combined JES uncertainty as a function  
1274 of  $p_T$  is shown in Fig.6.9.

## 1275 Jet Vertex Tagger

1276 The *jet vertex tagger* (JVT) technique is used to separate pileup jets from those  
1277 associated to the hard primary vertex[106]. The technique for doing so first involves  
1278 *ghost association*[107]. Ghost association runs the anti- $k_T$ jet clustering algorithm on  
1279 a combined collection of the topoclusters and tracks. The tracks *only* momenta are  
1280 set to zero<sup>2</sup>, with only the directional information is included. As discussed above,  
1281 the anti- $k_T$ algorithm is “big to small”; tracks are associated to the “biggest” jet near  
1282 them in  $(\eta, \phi)$ . This method uniquely associates each track to a jet, without changing  
1283 the final jet kinematics.

1284 The JVT technique uses a combination of these track variables to determine the  
1285 likelihood that the jet originated at the primary vertex. For jets which have associated  
1286 tracks from ghost association, this value ranges from 0 (likely pileup jet) to 1 (likely  
1287 hard scatter jet). Jets without associated tracks are assigned  $\text{JVT} = -.1$ . The  
1288 working point of  $\text{JVT} > .59$  is used for jets in this thesis.

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<sup>2</sup>Well, not exactly zero, since zero momentum tracks wouldn’t have a well-defined  $(\eta, \phi)$  coordinate, but set to a value obeying  $p_{T,\text{track}} << 400 \text{ MeV} = p_{\text{track,min}}$ . This is the minimum momentum for a track to reach the ATLAS inner detector.

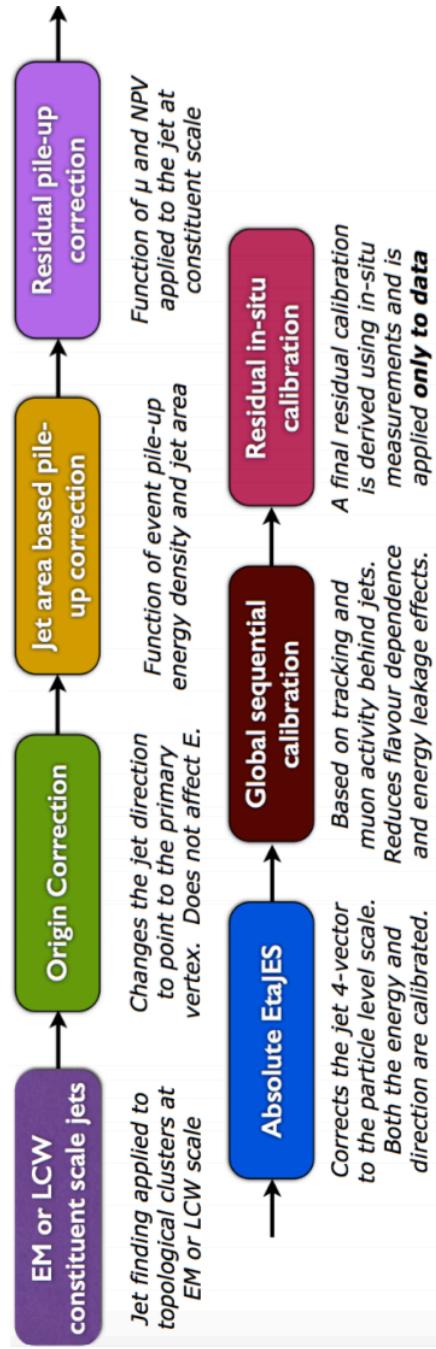


Figure 6.8: The steps used by ATLAS to calibrate jets

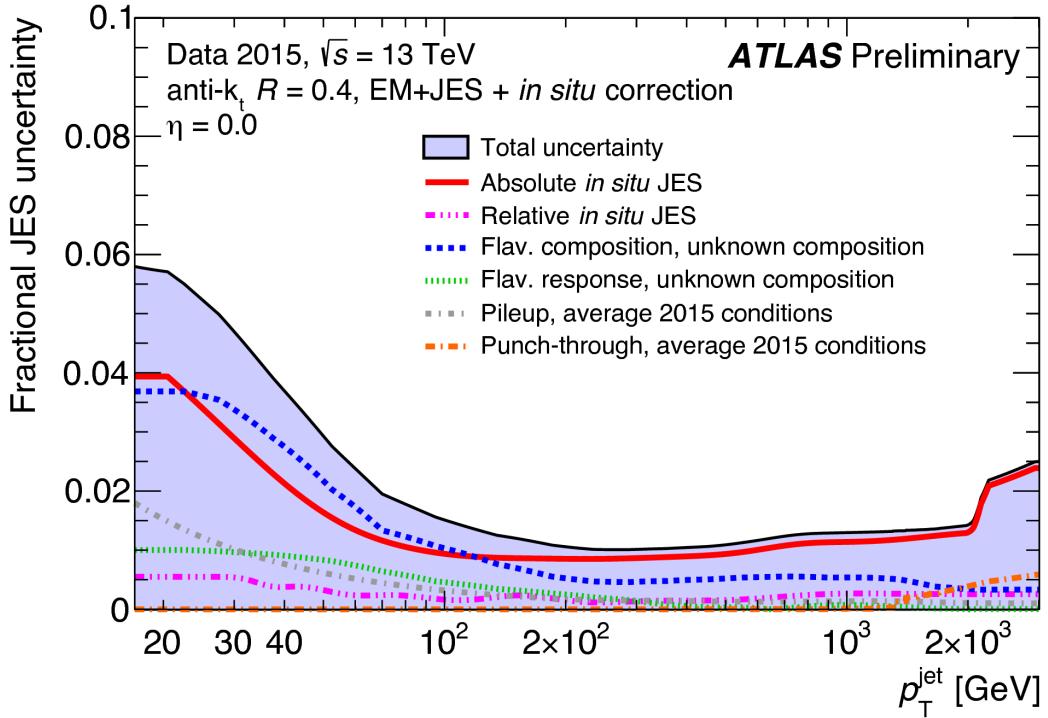


Figure 6.9: Combined jet energy scale uncertainty as a function of  $p_T$  at  $\eta = 0$ .

## 1289 B-jets

1290 Jets originating from bottom quarks (b-jets) are interesting physical phenomena that  
 1291 can be *tagged* by the ATLAS detector[Aad:2015ydr, 108]. B-hadrons, which have  
 1292 a comparatively long lifetime compared to hadrons consisting of lighter quarks, can  
 1293 travel a macroscopic distance inside the ATLAS detector. The high-precision tracking  
 1294 detectors identify the secondary vertices from these decays and the jet matched to  
 1295 that vertex is called a *b-jet*. The “MV2c10” algorithm, based on boosted decision  
 1296 trees, identifies these jets using a combination of variables sensitive to the difference  
 1297 between light-quark and b-quark jets. The efficiency of this tagger is 77%, with a  
 1298 rejection factor of 134 for light-quarks and 6 for charm jets.

1299 **Missing Transverse Momentum**

1300 Missing transverse momentum  $E_T^{\text{miss}}$  [109] is a key observable in searches for new  
1301 physics, especially in SUSY searches[110, 111]. However,  $E_T^{\text{miss}}$  is not a uniquely  
1302 defined object when considered from the detector perspective (as compared to the  
1303 Feynammn diagram), and it is useful to understand the choices that affect the  
1304 performance of this observable in searches for new physics.

1305  **$E_T^{\text{miss}}$  Definitions**

*Hard* objects refers to all physical objects as defined in the previous sections. The  
 $E_T^{\text{miss}}$  reconstruction procedure uses these hard objects and the *soft term* to provide  
a value and direction of the missing transverse momentum. The  $E_{x(y)}^{\text{miss}}$  components  
are calculated as:

$$E_{x(y)}^{\text{miss}} = E_{x(y)}^{\text{miss, } e} + E_{x(y)}^{\text{miss, } \gamma} + E_{x(y)}^{\text{miss, jets}} + E_{x(y)}^{\text{miss, } \mu} + E_{x(y)}^{\text{miss, soft}}, \quad (6.5)$$

1306 where each value  $E_{x(y)}^{\text{miss, } i}$  is the negative vectorial sum of the calibrated objects defined  
1307 in the previous sections.

1308 For purposes of  $E_T^{\text{miss}}$  reconstruction, we must assign an ordering of *overlap*  
1309 *removal*. This is to avoid double counting of the underlying primitive objects (clusters  
1310 and tracks) which are inputs to the reconstruction of the physics objects. We resolve  
1311 this in the following order : electrons, photons , jets and muons. This is motivated  
1312 by the performance of the reconstruction of these objects in the calorimeters.

1313 The soft term  $E_{x(y)}^{\text{miss, soft}}$  contains all of the primitive objects which are not  
1314 associated to any of the reconstructed physics objects. Of course, we need to choose  
1315 which primitive object to use. The primary choices which have been used within  
1316 ATLAS are the *calorimeter-based soft term* (CST) and the *track-based soft term*  
1317 (TST). Based on the soft term choice, we then call  $E_T^{\text{miss}}$  built with a CST (TST)

1318 soft term simply CST (TST)  $E_T^{\text{miss}}$ . An additional option, which will be important  
1319 as pileup continues to increase, particle flow  $E_T^{\text{miss}}$  (PFlow  $E_T^{\text{miss}}$ ).

1320 The CST  $E_T^{\text{miss}}$  was used for much of the early ATLAS data-taking. CST  $E_T^{\text{miss}}$  is  
1321 built from the calibrated hard objects, combined with the calorimeter clusters which  
1322 are *not* assigned to any of those hard objects. In the absence of pileup, it provides the  
1323 best answer for the “true”  $E_T^{\text{miss}}$  in a given event, due to the impressive hermiticity of  
1324 the calorimeters. Unfortunately, the calorimeters do not know “where” from where  
1325 their energy deposition came, and thus CST is susceptible to drastically reduced  
1326 performance as pileup is increased.

1327 TST  $E_T^{\text{miss}}$  is the standard for ATLAS searches as currently performed by ATLAS.  
1328 TST  $E_T^{\text{miss}}$  is built by using the calibrated hard objects and the soft term is built from  
1329 the tracks which are not assigned to any of those hard objects. In particular, due  
1330 to the impressive track-vertex association efficiency, one chooses tracks which only  
1331 come from the primary vertex. This drastically reduces the pileup contributions to  
1332 the  $E_T^{\text{miss}}$  measurement. However, since the ID tracking system is unable to measure  
1333 neutral objects, the TST  $E_T^{\text{miss}}$  is “wrong”. This bias is important to understand for  
1334 many measurements. However, in most searches for new physics, the soft  $E_T^{\text{miss}}$  is  
1335 generally a small fraction of the total  $E_T^{\text{miss}}$ , and thus this bias is not particularly  
1336 hurtful.

1337 PFlow  $E_T^{\text{miss}}$  uses the PFOs described above to build the  $E_T^{\text{miss}}$ . The PFOs which  
1338 are assigned to hard objects are calibrated, and the PFOs which are not assigned  
1339 to any hard object are added to the soft term. In this context, it is convenient to  
1340 distinguish between “charged” and “neutral” PFOs. Charged PFOs can be seen as a  
1341 topocluster which has an associated track, while neutral PFOs do not. This charged  
1342 PFO is essentially a topocluster that we are “sure” comes from the primary vertex.  
1343 The neutral PFOs are in the same status as the original topoclusters. Thus a “full”  
1344 PFlow  $E_T^{\text{miss}}$  should have performance somewhere between TST  $E_T^{\text{miss}}$  and CST  $E_T^{\text{miss}}$ <sup>3</sup>.

1345 A *charged* PFlow  $E_T^{\text{miss}}$  should for sanity be the same as TST.

1346 **Measuring  $E_T^{\text{miss}}$  Performance : event selection**

1347 The question is now straightforward: how do we compare these different algorithms?  
1348 We compare these algorithms in  $Z \rightarrow \ell\ell + \text{jets}$  and  $W \rightarrow \ell\nu + \text{jets}$  events. Due to  
1349 the presence of leptons, these events are well-measured “standard candles”. Here  
1350 we present the results in early 2015 data with  $Z \rightarrow \mu\mu$  and  $W \rightarrow e\nu$  events, as  
1351 shown in [112, 113]. This result was important to assure the integrity of the  $E_T^{\text{miss}}$   
1352 measurements at the higher energy and pileup environment of Run-2.

1353 The  $Z \rightarrow \ell\ell$  selection is used to measure the intrinsic  $E_T^{\text{miss}}$  resolution of the  
1354 detector. The only possible source of neutrinos in these decays is from heavy-flavor  
1355 decays inside of jets, and thus  $Z \rightarrow \ell\ell$  events they have very low  $E_T^{\text{miss}}$ . This provides  
1356 an ideal event topology to understand the modelling of  $E_T^{\text{miss}}$  mismeasurement.  
1357 Candidate  $Z \rightarrow \mu\mu$  events are first required to pass a muon or electron trigger, as  
1358 described in Table 5.1. Offline, the selection of  $Z \rightarrow \mu\mu$  events requires exactly two  
1359 medium muons. The muons are required to have opposite charge and  $p_T > 25 \text{ GeV}$ ,  
1360 and mass of the dimuon system is required to be consistent with the  $Z$  mass  
1361  $|m_{ll} - m_Z| < 25 \text{ GeV}$ .

$W \rightarrow \ell\nu$  events are an important topology to evaluate the  $E_T^{\text{miss}}$  modelling in  
an event with real  $E_T^{\text{miss}}$ . This  $E_T^{\text{miss}}$  is from the neutrino, which is not detected.  
The  $E_T^{\text{miss}}$  in these events has a characteristic distribution with a peak at  $\frac{1}{2}m_W$ . The  
selection of  $W \rightarrow e\nu$  events begins with the selection of exactly one electron of medium  
quality. A selection on TST  $E_T^{\text{miss}} > 25 \text{ GeV}$  drastically reduces the background from  
multijet events where the jet fakes an electron. The transverse mass is used to select

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<sup>3</sup>Naively, due to approximate isospin symmetry, about 2/3 of the hadrons will be charged and 1/3 will be neutral.

the  $W \rightarrow e\nu$  events :

$$m_T = \sqrt{2p_T^\ell E_T^{\text{miss}}(1 - \cos \Delta\phi)}, \quad (6.6)$$

1362 where  $\Delta\phi$  is the difference in the  $\phi$  between the  $E_T^{\text{miss}}$  and the electron.  $m_T$  is required  
1363 to be greater than 50 GeV.

1364 There are two main ingredients to investigate : the  $E_T^{\text{miss}}$  resolution and the  $E_T^{\text{miss}}$   
1365 scale.

1366 **Measuring  $E_T^{\text{miss}}$  Performance in early 2015 data : metrics**

1367 To compare these algorithms we use the  $E_T^{\text{miss}}$  resolution,  $E_T^{\text{miss}}$  scale, and the  
1368 linearity. Representative distributions of TST  $E_x^{\text{miss}}$ ,  $E_y^{\text{miss}}$ , and  $E_T^{\text{miss}}$  from early  
1369 2015 datataking are shown in Fig.6.10.

The  $E_T^{\text{miss}}$  resolution is an important variable due to the fact that the bulk of the distributions associated to  $E_{x(y)}^{\text{miss}}$  are Gaussian distributed [Aad2012]. However, to properly measure the tails of this distribution, especially when considering non-calorimeter based soft terms, it is important to use the root-mean square as the proper measure of the resolution. This is strictly larger than a resolution as measured using a fit to a Gaussian, due to the long tails from i.e. track mismeasurements. The resolution is measured with respect to two separate variables :  $\sum E_T$  and  $N_{\text{PV}}$ .  $\sum E_T$  is an important measure of the “total event activity”. It is defined as

$$\sum E_T = \sum p_T^e + \sum p_T^\gamma + \sum p_T^\tau + \sum p_T^{\text{jets}} + \sum p_T^\mu + \sum p_T^{\text{soft}}. \quad (6.7)$$

1370 The measurement as a function of  $N_{\text{PV}}$  is useful to understand the degradation of  
1371  $E_T^{\text{miss}}$  performance with increasing pileup. Figure 6.11 shows the  $E_T^{\text{miss}}$  resolution in  
1372 the early 2015 data. The degradation of the  $E_T^{\text{miss}}$  performance is shown as a function  
1373 of pileup  $N_{\text{PV}}$  and total event activity  $\sum E_T$ .

Another important performance metric is the  $E_T^{\text{miss}}$  scale, or how “right” we are in our  $E_T^{\text{miss}}$  calculation. This can be off in various directions, as CST  $E_T^{\text{miss}}$  contains

additional particles from pileup, while soft neutral particles<sup>4</sup> are ignored by TST  $E_T^{\text{miss}}$ .

To measure this in data, we again use  $Z \rightarrow \mu\mu$  events, where the  $Z \rightarrow \mu\mu$  system is treated as a well-measured reference object. The component of  $E_T^{\text{miss}}$  which is in the same direction as the reconstructed  $Z \rightarrow \mu\mu$  system is sensitive to potential biases in the detector response. The unit vector  $\mathbf{A}_Z$  of the  $Z$  system is defined as

$$\mathbf{A}_Z = \frac{\vec{p}_T^{\ell^+} + \vec{p}_T^{\ell^-}}{|\vec{p}_T^{\ell^+} + \vec{p}_T^{\ell^-}|}, \quad (6.8)$$

where  $\vec{p}_T^{\ell^+}$  and  $\vec{p}_T^{\ell^-}$  are the transverse momenta of the leptons from the  $Z$  boson decay. The relevant scale metric is then the mean value of the  $\vec{E}_T^{\text{miss}}$  projected onto  $\mathbf{A}_Z$ :  $\langle \vec{E}_T^{\text{miss}} \cdot \mathbf{A}_Z \rangle$ . In Figure 6.12, the scale is shown for the early 2015 dataset. The negative bias, which is maximized at about 5 GeV, is a reflection of two separate effects. The soft neutral particles are missed by the tracking system, and thus ignored in TST  $E_T^{\text{miss}}$ . Missed particles due to the limited ID acceptance can also affect the scale.

For events with real  $E_T^{\text{miss}}$ , one can also look at the *linearity* in simulation. This is defined as

$$\text{linearity} = \left\langle \frac{E_T^{\text{miss}} - E_T^{\text{miss,Truth}}}{E_T^{\text{miss,Truth}}} \right\rangle. \quad (6.9)$$

$E_T^{\text{miss,Truth}}$  refers to “truth” particles as defined before, or the magnitude of the vector sum of all noninteracting particles. The linearity is expected to be zero if the  $E_T^{\text{miss}}$  is reconstructed at the correct scale.

## 1384 Particle Flow Performance

As described above, the resolution, scale, and linearity are the most important metrics to understand the performance of the different  $E_T^{\text{miss}}$  algorithms. In this section, we present comparisons of the different algorithms, including particle flow, in simulation

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<sup>4</sup>“Soft” here means those particles which are not hard enough to be reconstructed as their own particle, using the reconstruction algorithms above.

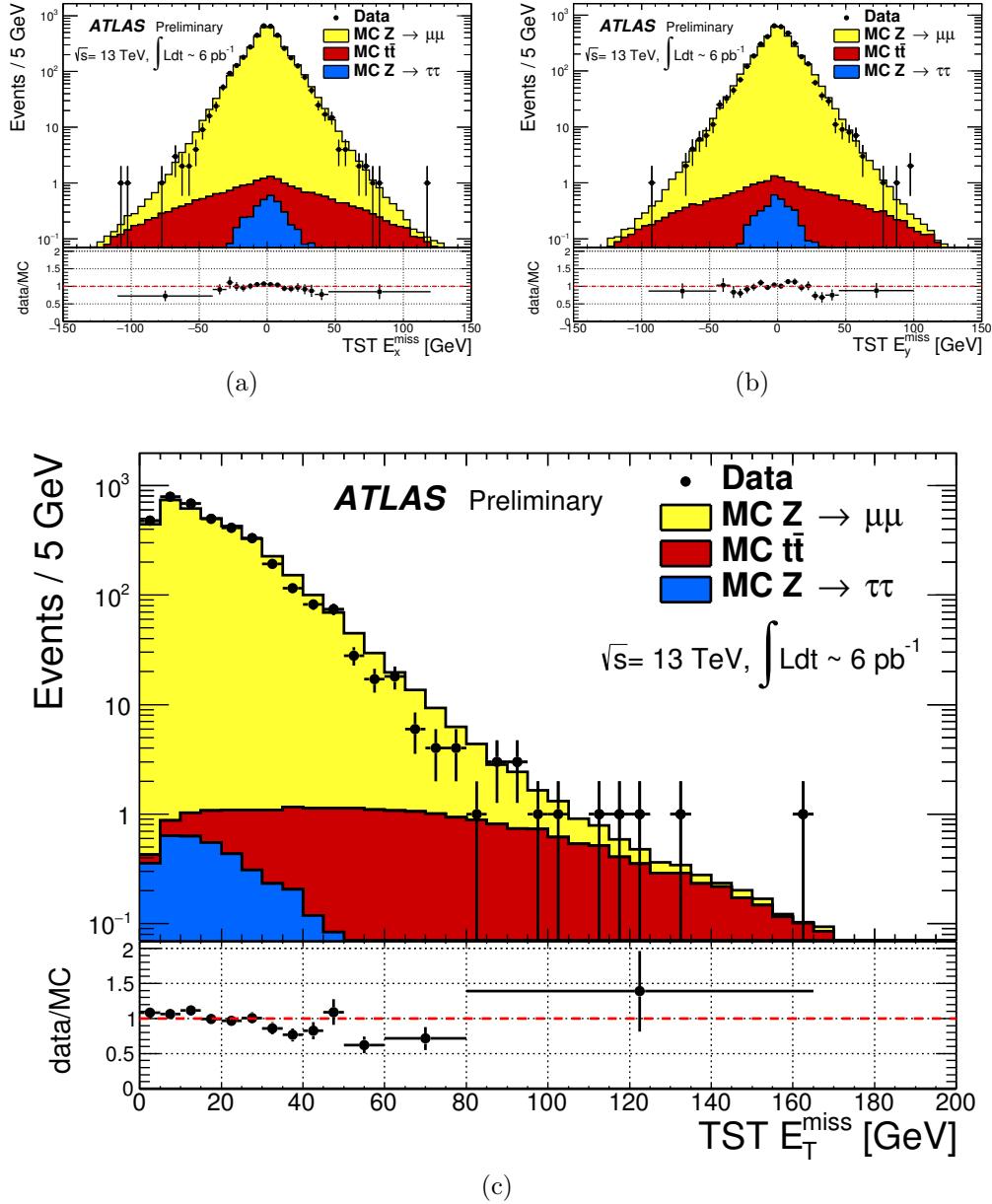


Figure 6.10: TST  $E_x^{\text{miss}}$ ,  $E_y^{\text{miss}}$ , and  $E_T^{\text{miss}}$  distributions of early  $\sqrt{s} = 13$  TeV data compared with simulation after the  $Z \rightarrow \mu\mu$  selection described in Sec. 6.2. The data sample consists of  $6 \text{ pb}^{-1}$ .

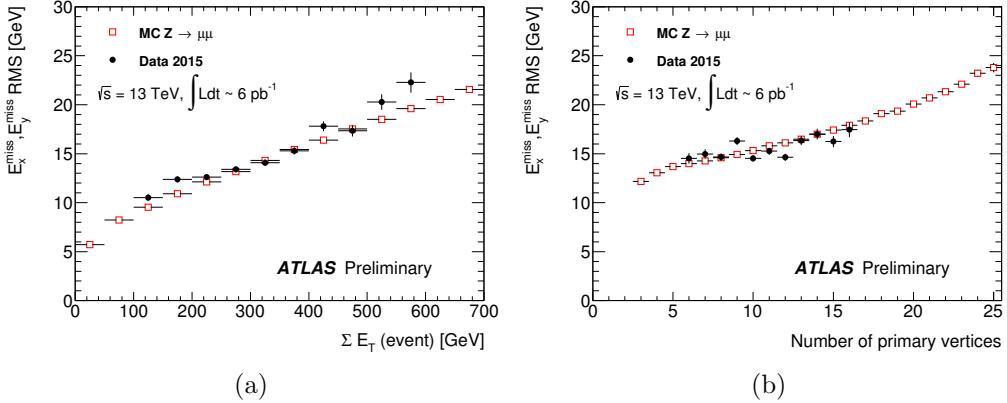


Figure 6.11: Resolution of TST  $E_T^{\text{miss}}$  of early  $\sqrt{s} = 13$  TeV data compared with simulation after the  $Z \rightarrow \mu\mu$  selection described in Sec.6.2. The data sample consists of  $6 \text{ pb}^{-1}$ .

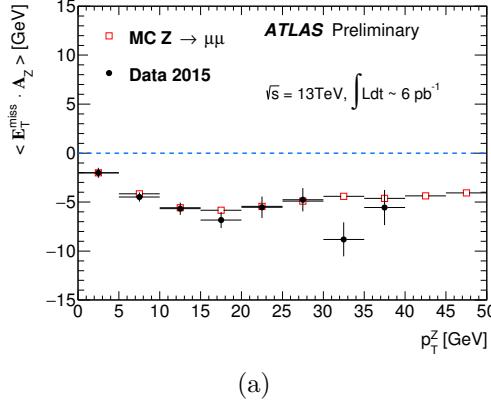


Figure 6.12: Scale of TST  $E_T^{\text{miss}}$  of early  $\sqrt{s} = 13$  TeV data compared with simulation after the  $Z \rightarrow \mu\mu$  selection described in Sec.6.2. The data sample consists of  $6 \text{ pb}^{-1}$ .

1388 and using a data sample from 2015 of  $80 \text{ pb}^{-1}$ . In these plots, ‘‘MET\_PFlow-TST’’  
 1389 refers to charged PFlow  $E_T^{\text{miss}}$ , while the other algorithms are as described above.

1390 Figures ?? show the resolution and scale in simulated  $Z \rightarrow \mu\mu$  events. The  
 1391 resolution curves follow the ‘‘intuitive’’ behavior discussed before. Due to the high  
 1392 pileup in 2015 run conditions, the CST  $E_T^{\text{miss}}$  resolution is poor, and becomes even  
 1393 poorer with increasing pileup and event activity. The ‘‘regular’’ PFlow  $E_T^{\text{miss}}$  shows  
 1394 reduces pileup and event activity dependence as compared to the CST. As stated  
 1395 earlier, the  $E_T^{\text{miss}}$  from the PFlow algorithm can be seen as a hybrid of TST  $E_T^{\text{miss}}$

1396 and CST  $E_T^{\text{miss}}$ . The charged PFOs ( $\sim 2/3$ ) are pileup suppressed, while the neutral  
1397 PFOs (or topoclusters) are not. Both charged PFlow and TST  $E_T^{\text{miss}}$  show only a  
1398 small residual dependence on  $N_{\text{PV}}$  and  $\sum E_T$ , since they have fully pileup suppressed  
1399 inputs through the track associations.

1400 The scale plots are shown for  $Z + \text{jets}$  events and  $Z$  events with no jets. For the  
1401 nonsuppressed CST, the scale continues to worsen with increasing  $p_T^Z$ . It is almost  
1402 always the worst performing algorithm. The standard PFlow algorithm performs the  
1403 second worst in the region of high  $p_T^Z$ , but is the best at low  $p_T^Z$ . The most exciting note  
1404 in this plot is the improved scale of the charged PFlow  $E_T^{\text{miss}}$  compared to the TST  
1405  $E_T^{\text{miss}}$ . Considering the resolution is essentially identical, the PFlow algorithm is better  
1406 picking up the contributions from additional neutral particles. In events with no jets,  
1407 the soft term is essentially the only indication of the  $E_T^{\text{miss}}$  mismeasurement, since  
1408 the muons will be well-measured. In this case, the pileup effects cancel, on average,  
1409 due to the  $U(1)_\phi$  symmetry of the ATLAS detector, and CST performs rather well  
1410 compared to the more complicated track-based algorithms. The full PFlow algorithm  
1411 performs best, since it provides a small amount of pileup suppression on the neutral  
1412 components from CST.

1413 The resolution and linearity are shown in simulated  $W \rightarrow e\nu$  events in Figure ???.  
1414 The resolution in  $W \rightarrow e\nu$  events shows a similar qualitative behavior to that shown  
1415 in  $Z \rightarrow \mu\mu$  events. The CST  $E_T^{\text{miss}}$  has the worst performance, with charged PFlow  
1416  $E_T^{\text{miss}}$  performing best. The surprise here is that the scale associated to TST  $E_T^{\text{miss}}$  in  
1417 these events is best throughout the space parameterized by  $E_T^{\text{miss,Truth}}$ , except for one  
1418 bin at  $40 \text{ GeV} < E_T^{\text{miss,Truth}} < 50 \text{ GeV}$ . The scale in these events is best measured  
1419 using a track-based soft term.

1420 The resolution also investigated in real data passing the  $Z \rightarrow \mu\mu$  selection  
1421 described above. A comparison of the  $E_T^{\text{miss}}$  between real data and simulation for  
1422 each algorithm is presented in Figure 6.16. The resolution as a function of  $\sum E_T$  and

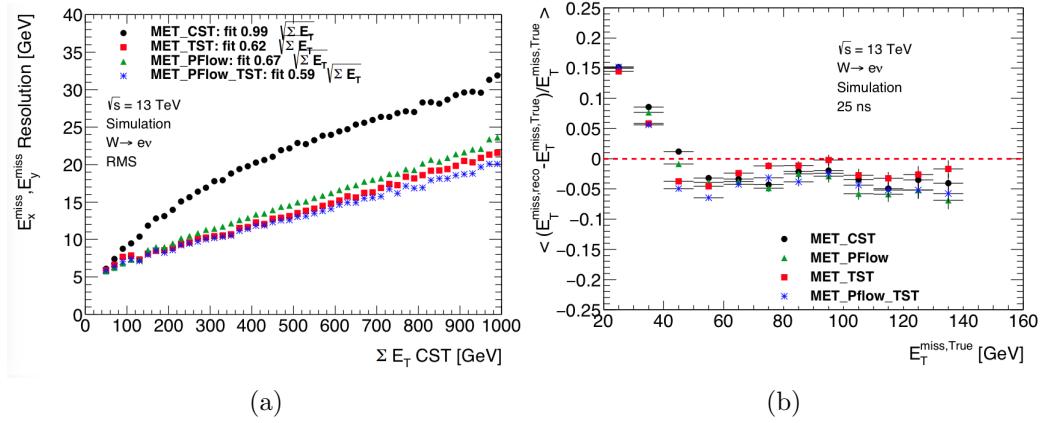


Figure 6.13: Comparison of  $E_T^{\text{miss}}$  resolution and linearity using different  $E_T^{\text{miss}}$  algorithms with simulated  $W \rightarrow e\nu$  events.

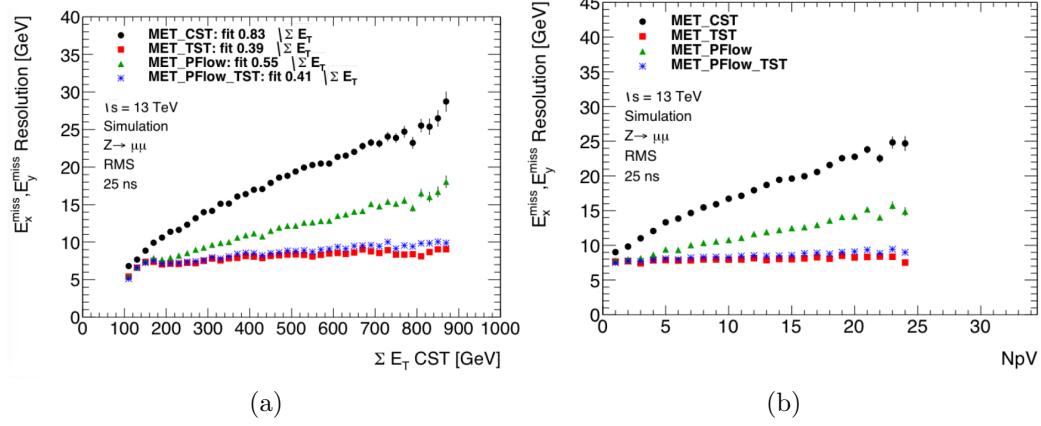


Figure 6.14: Comparison of  $E_T^{\text{miss}}$  resolution using different  $E_T^{\text{miss}}$  algorithms with simulated  $Z \rightarrow \mu\mu$  events.

1423  $N_{\text{PV}}$  is shown in Figure 6.17 for this dataset. Overall, this plot shows the same general  
 1424 features as the simulation dataset in terms of algorithm performance. However, the  
 1425 performance of all algorithms seems to be significantly worse in data. This is likely due  
 1426 to simplifications made in the simulation: soft interactions that cannot be simulated  
 1427 can have a significant effect on an event level variable such as the  $E_T^{\text{miss}}$  resolution.

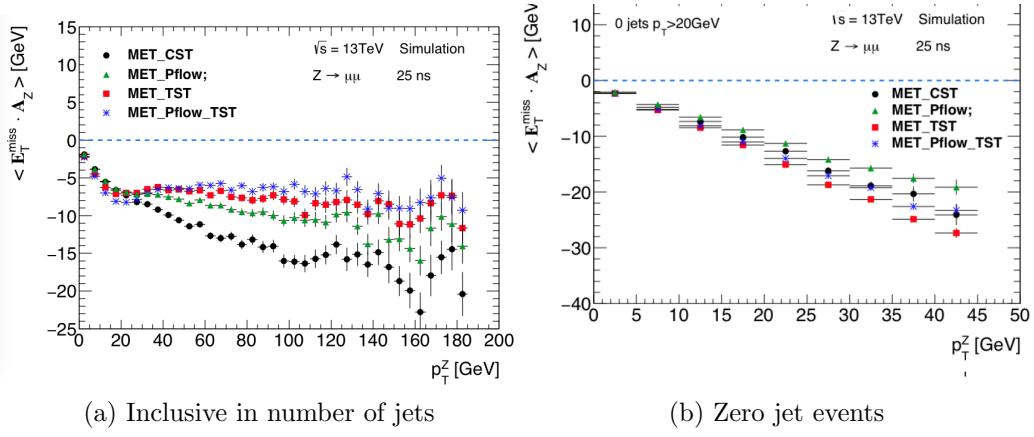


Figure 6.15: Comparison of  $E_T^{\text{miss}}$  scale using different  $E_T^{\text{miss}}$  algorithms with simulated  $Z \rightarrow \mu\mu$  events.

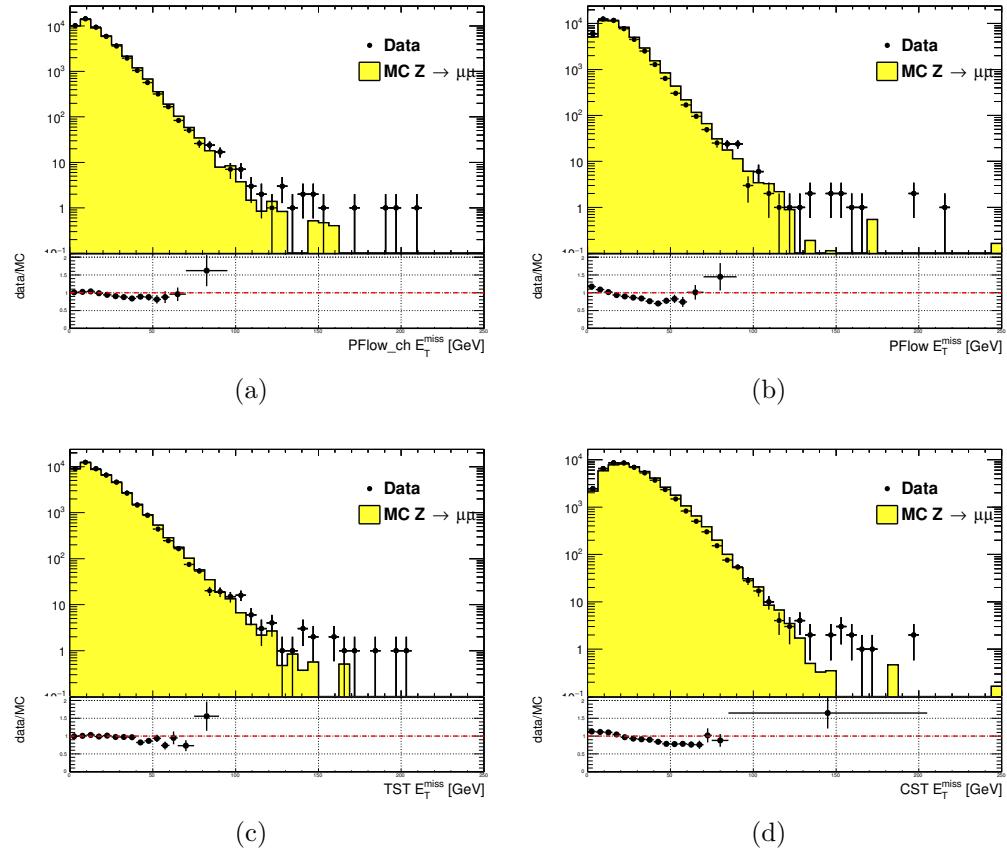


Figure 6.16: Comparison of  $E_T^{\text{miss}}$  distributions using different  $E_T^{\text{miss}}$  algorithms with a data sample of  $80 \text{ pb}^{-1}$  after the  $Z \rightarrow \mu\mu$  selection described in Sec.6.2

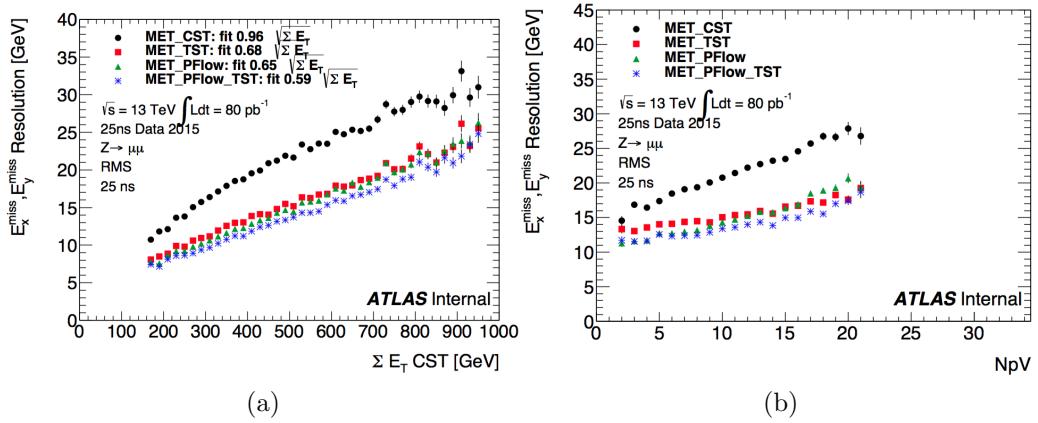


Figure 6.17: Comparison of  $E_T^{\text{miss}}$  resolution using different  $E_T^{\text{miss}}$  algorithms with a data sample of  $80 \text{ pb}^{-1}$  after the  $Z \rightarrow \mu\mu$  selection described in Sec. 6.2

*Recursive Jigsaw Reconstruction*

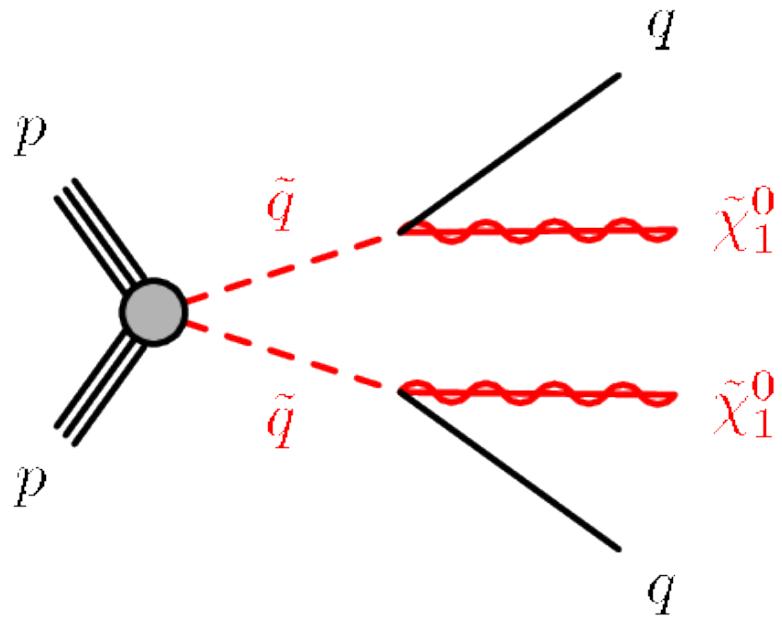
1430 *Recursive Jigsaw Reconstruction* (RJR) [114, 115] is a novel algorithm used for the  
 1431 analysis presented in this thesis. RJR is the conceptual successor to the razor  
 1432 technique [116, 117], which has been used successfully in many new physics searches  
 1433 [37, 38, 40, 41, 47, 118]. In this chapter, we will first present the razor technique,  
 1434 and describe the razor variables. We will then present the RJR algorithm. After the  
 1435 description of the algorithm, we will describe the precise RJR variables used by this  
 1436 thesis and attempt to provide some physical intuition of what they describe.

## 7.1 Razor variables

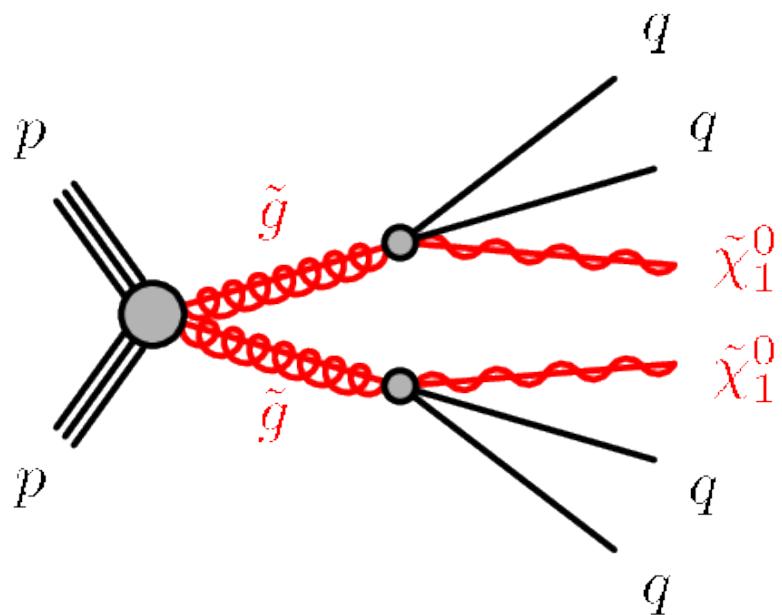
### Motivation

1439 In this thesis, we consider SUSY models where gluinos and squarks are pair-produced.  
 1440 Pair-production is a consequence of the  $R$ -parity imposed in many SUSY models.  
 1441  $R$ -parity violation is highly constrained by limits on proton decay[15], and is often  
 1442 assumed in SUSY model building. The Feynman diagrams considered are shown in  
 1443 Fig.7.1.

1444 As discussed previously, the consequences of this  $\mathbb{Z}_2$  symmetry are drastic. To un-  
 1445 derstand the utility of the razor variables, the stability of the lightest supersymmetric  
 1446 particle is very important. In many SUSY models, including the ones considered in  
 1447 this thesis, this is the lightest neutralino  $\tilde{\chi}_1^0$ . This means that on either side of a  
 1448 SUSY decay process, where we begin with disparticle production, we have a final



(a) Disquark production



(b) Digluino production

Figure 7.1: Feynman diagrams for the SUSY signals considered in this thesis

1449 state particle which is not detected. Generically, this leads to  $E_T^{\text{miss}}$ . Selections based  
1450 on  $E_T^{\text{miss}}$  are very good at reducing dominant backgrounds, for example from QCD  
1451 backgrounds.

1452 However, there are limitations to searches based on  $E_T^{\text{miss}}$ . Due to jet mismeasurements,  
1453 instrumental failures, finite detector acceptance, nongaussian tails in the  
1454 detector response, and production of neutrinos inside of jets, there are many sources of  
1455 “fake”  $E_T^{\text{miss}}$  which does not correspond to a Standard Model neutrino or new physics  
1456 object such as an LSP. An additional limitation is the complete lack of longitudinal  
1457 information. As events from i.e. QCD backgrounds tend to have higher boosts along  
1458 the  $z$ -direction, this is ignoring an important handle in searches for new physics.  
1459 Finally,  $E_T^{\text{miss}}$  is only one object, which is a measurement for *two* separate LSPs. If one  
1460 could factorize this information somehow, this would provide additional information  
1461 to potentially discriminate against backgrounds. The *razor variables* ( $M_{\Delta}^R, R^2$ ) are  
1462 more robust than standard variables against these effects[[116](#), [117](#)].

## 1463 Derivation of the razor variables

1464 To derive the razor variables ( $M_{\Delta}^R, R^2$ ), we start with a generic situation of the pair  
1465 production of heavy sparticles with mass  $m_{\text{Heavy}}$ .<sup>1</sup> Each sparticle decays to a number  
1466 of observable objects (in this thesis, jets), and an unobservable  $\tilde{\chi}_1^0$  of mass  $m_{\tilde{\chi}_1^0}$ . We  
1467 will combine all of the jets into a *megajet*; this process will be described below. We  
1468 begin by analyzing the decay in the “rough-approximation”, or in modern parlance,  
1469 *razor frame* (*R-frame*). This is the frame where each sparticle is at rest. The complete  
1470 set of frames considered in the case of the razor variables is shown in [7.2](#).

In the *R-frame*, the decay is straightforward to analyze. By construction, there  
are in fact two *R-frame* s, and they have identical kinematics. Each megajet has

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<sup>1</sup>The razor variables have undergone confusing notational changes over the years. We will be self-consistent, but the notation used here may be different from references.

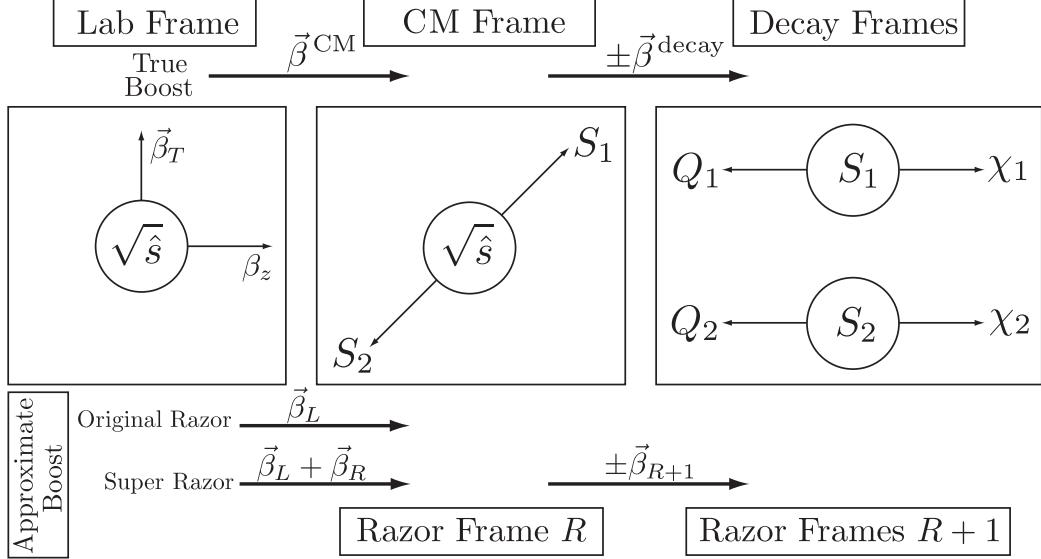


Figure 7.2: Frames considered when applying the razor technique, from [117].

energy  $E_1^R, E_2^R$  in the frame of its parent sparticle, and we define a characteristic mass  $M_R$ :

$$E_1^R = E_2^R = \frac{m_{\text{Heavy}}^2 - m_{\tilde{\chi}_1^0}^2}{2m_{\text{Heavy}}} \quad (7.1)$$

$$M_R = 2 \times E_1^R = 2 \times E_2^R = \frac{m_{\text{Heavy}}^2 - m_{\tilde{\chi}_1^0}^2}{m_{\text{Heavy}}} \quad (7.2)$$

For cases where  $m_{\text{Heavy}} \gg m_{\tilde{\chi}_1^0}$ ,  $M_R$  is an estimator of  $m_{\text{Heavy}}$ . This scenario happens in the SM, such as in  $t\bar{t}$  and  $WW$  events, where the  $\tilde{\chi}_1^0$  is instead a neutrino.

The question now is how to use this simple derivation in the lab frame, where we actually have measurements. There are two related issues: how to combine the jets into the megajets, and how to “transform” (or *boost*) to the  $R$ -frame.

To construct the megajets, the procedure is the following. For a given set of jets  $j_i, i = 0, \dots, n_{\text{jet}}$ , we construct *all* combinations of their four-momenta such that there is at least one jet inside each megajet. Among this set of possible megajets  $\{J_{1,2}\}$ , we make the following unique choice for the megajets. We minimize the following quantity:

$$m_{J_1}^2 + m_{J_2}^2. \quad (7.3)$$

1476 In modern parlance, this is known as a *jigsaw*. It is important to note, this is a  
 1477 *choice*. It may have nice physical qualities or satisfy some convenient intuition about  
 1478 the events, but as we will see later, other choices are possible.

We now describe how we translate our megajet kinematics, measured in the lab frame, to the  $R$ -frame. This is a two-step procedure. We perform two *boosts*: a longitudinal boost  $\beta_L$  and a transverse boost  $\beta_T$ . Schematically,

$$J_1^R \xrightarrow{\beta_T} J_1^{CM} \xrightarrow{\beta_L} J_1^{\text{lab}} \quad (7.4)$$

$$J_2^R \xrightarrow{-\beta_T} J_2^{CM} \xrightarrow{\beta_L} J_2^{\text{lab}} \quad (7.5)$$

$$(7.6)$$

1479 The  $J_{1,2}^{\text{lab}}$  correspond directly to those in the megajet construction. We drop the  
 1480 “lab” designation for the rest of the discussion. The question is how to compute the  
 1481 magnitudes of these boosts, given the missing degrees of freedom.

For the transverse boost  $\beta_T$ , recall the two megajets have equal energies in their  $R$ -frame by construction. This constraint can be reexpressed as a constraint on the magnitude of this boost, in terms of the boost velocity  $\beta_L$  (and Lorentz factor  $\gamma_L$ ):

$$\beta_T = \frac{\gamma_L(E_1 - E_2) - \gamma_L\beta_L(p_{1,z} - p_{2,z})}{\hat{\beta}_T \cdot (\vec{p}_{1,T} + \vec{p}_{2,T})} \quad (7.7)$$

where we have denoted the lab frame four-vectors as  $p_i = (E_i, \vec{p}_{i,T}, p_z)$ . We now make the *choice* for the direction of the transverse boost  $\hat{\beta}_T$ :

$$\hat{\beta}_T = \frac{\vec{p}_{1,T} + \vec{p}_{2,T}}{|\vec{p}_{1,T} + \vec{p}_{2,T}|}. \quad (7.8)$$

1482 This choice forces the denominator of 7.7 to unity, and corresponds to aligning the  
 1483 transverse boost direction with the sum of the two megajets transverse directions.

For the longitudinal boost, we choose  $\vec{\beta}_L$  along the  $z$ -direction, with magnitude:

$$\beta_L = \frac{p_{1,z} + p_{2,z}}{E_1 + E_2}. \quad (7.9)$$

1484 Viewed in terms of the original parton-parton interactions, this is the choice which  
 1485 “on average” gives  $p_{z,\text{CM}} = 0$ , as we would expect. This well-motivated choice due to  
 1486 the total  $z$  symmetry.

We now have well-motivated guesses for both boosts, which allow us write our original characteristic mass  $M_R$  in terms of the lab frame variables, by application of these two Lorentz boosts to the energies of 7.1:

$$M_R^2 \xrightarrow{\beta_T} M_{R,\text{CM}}^2 \xrightarrow{\beta_L} M_{R,\text{lab}}^2 = (E_1 + E_2)^2 - (p_{1,z} + p_{2,z})^2. \quad (7.10)$$

Finally, we define an additional mass variable, which include the missing transverse energy  $E_{\text{T}}^{\text{miss}}$ . Importantly, note that we did not use the  $E_{\text{T}}^{\text{miss}}$  in the definition of  $M_R$ , which depends only on the energies of the megajets. Backgrounds with no invisible particles (such as multijet events) must have  $J_1$  and  $J_2$  back to back. Thus, we define the transverse mass:

$$(M_R^T)^2 = \frac{1}{2} \left[ E_{\text{T}}^{\text{miss}}(p_{1,T} + p_{2,T}) - \vec{E}_{\text{T}}^{\text{miss}} \cdot (\vec{p}_{1,T} + \vec{p}_{2,T}) \right]. \quad (7.11)$$

Generally, we have  $M_R^T < M_R$ , so we define a dimensionless ratio (“the razor”):

$$R^2 = \left( \frac{M_R^T}{M_R} \right)^2. \quad (7.12)$$

1487 For signal events, we expect  $R$  to peak around  $R \sim 1/4$ , while backgrounds without  
 1488 real  $E_{\text{T}}^{\text{miss}}$  are expected to have  $R \sim 0$ .

## 1489 7.2 Recursive Jigsaw Reconstruction

1490 Recursive Jigsaw Reconstruction is an algorithm allowing the imposition of a decay  
 1491 tree interpretation on an particular event[114, 115]. The idea is to construct the  
 1492 underlying kinematic variables (the masses and decay angles) on an event-by-event  
 1493 level. This is done “recursively” through a decay tree which corresponds (sometimes  
 1494 approximately) to the Feynmann diagram for the signal process of interest. After

1495 each step of the recursive procedure, the objects are “placed” into one bucket (or  
1496 branch) of the decay tree, and the process is repeated on each frame we have imposed.  
1497 The imposition of these decay trees is done by *jigsaw* rule: a procedure to resolve  
1498 combinatoric or kinematic ambiguities while traversing the decay tree. This procedure  
1499 is performed by the `RestFrames` software packages [119]

1500 In events where all objects are fully reconstructed, this is straightforward, and  
1501 of course has been used for many years in particle physics experiments. Events  
1502 which contain  $E_T^{\text{miss}}$  are more difficult, due to the loss of information: the potential  
1503 for multiple mismeasured or simply unmeasureable objects, such as neutrinos or the  
1504 LSP in SUSY searches. There can also be combinatoric ambiguities in deciding how  
1505 to group objects of the same type; specifically here, we will be concerned with the  
1506 jigsaw rule to associate jets to a particular branch of a decay tree. The jigsaw rules  
1507 we impose will remove these ambiguities. First, we will describe the decay trees used  
1508 in this thesis, and then describe the jigsaw rules we will use. Finally, we will describe  
1509 the variables used in the all-hadronic SUSY search presented in this thesis.

## 1510 Decay Trees

1511 The decay trees imposed in this thesis are shown in 7.3. Leaving temporarily the  
1512 question of “how” we apply the jigsaw rules, let us compare these trees to the signal  
1513 processes of interest. In particular, we want to compare the Feynman diagrams of 7.1  
1514 with the decay trees of 7.3. The decay tree in ?? corresponds exactly to that expected  
1515 from disquark production, and matches very closely with the principles of the razor  
1516 approach. We first apply a jigsaw rule, indicated by a line, to the kinematics of the  
1517 objects in the *lab* frame. This outputs the kinematics of our event in the *parent-parent*  
1518 (*PP*) frame, or in the razor terminology, the CM frame. That is, the kinematics of  
1519 this frame are an estimator for the kinematics in the center of mass frame of the  
1520 disquark system. We apply another jigsaw, which splits the objects in the *PP* frame

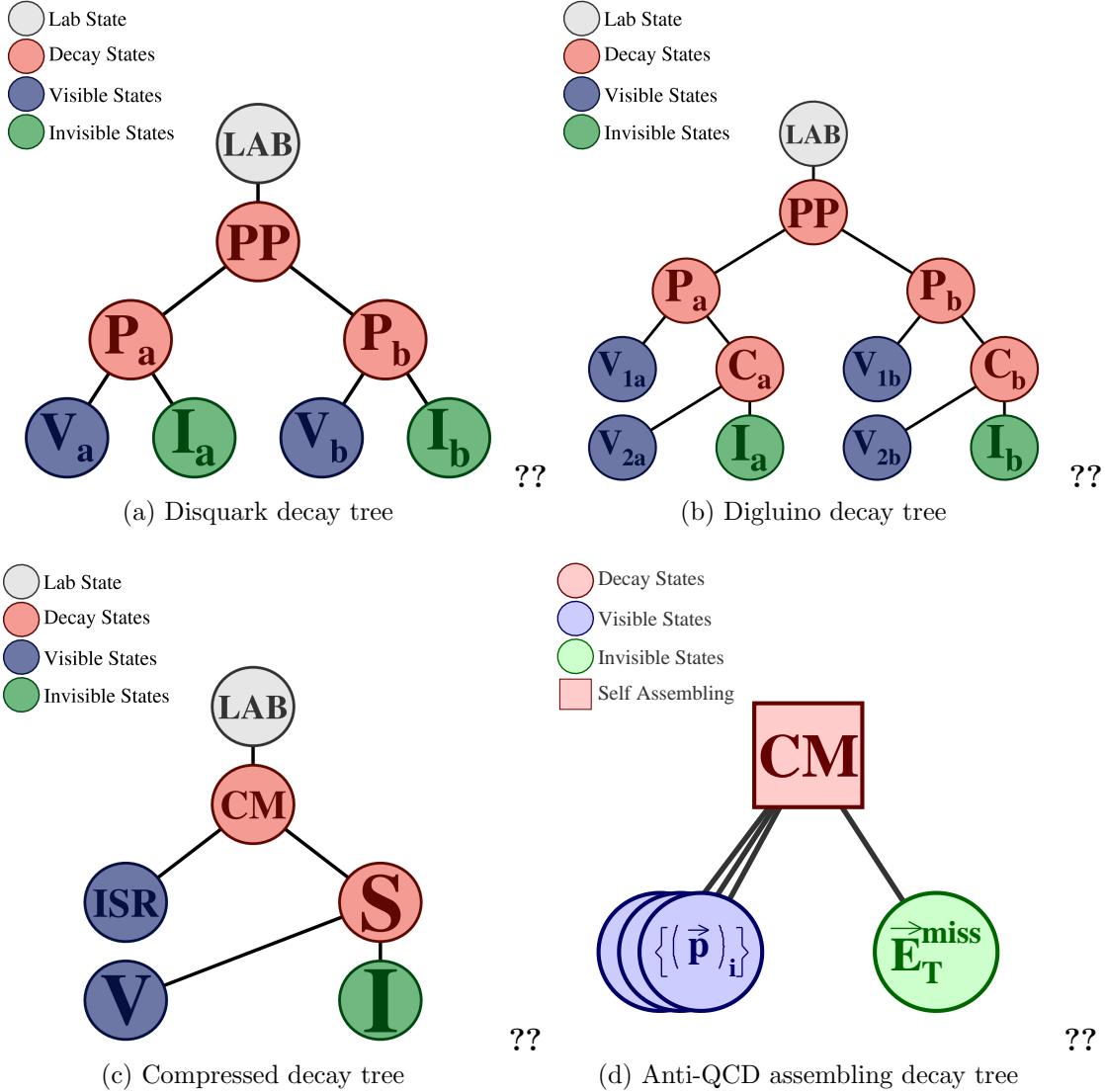


Figure 7.3: RJR decay trees imposed in this thesis

1521 into two new frames, known as the  $P_a$  and  $P_b$  systems. These are equivalent to the  
 1522 razor frames of the razor technique, and represent proxy frames where each squark  
 1523 is at rest. In  $P_a(P_b)$ , the decay is symmetric between the visible  $V_a(V_b)$  objects and  
 1524 the invisible system  $I_a(I_b)$ . To generate the estimator of the kinematics of the  $V_a$ ,  $V_b$ ,  
 1525  $I_a$ , and  $I_b$  systems in the  $P_a$  and  $P_b$  systems, we apply another jigsaw rule to split the  
 1526 total  $E_T^{\text{miss}}$  between  $P_a$  and  $P_b$ , which allows calculations of these kinematics in these  
 1527 frames. For the case of disquark production, this is the expected decay tree, and we

1528 stop the recursive calculation at that level.

1529 In the case of digluino production, we expect two additional jets, and we can  
1530 perform an additional boost in each of  $P_a$  and  $P_b$ , to what we call the  $C_a$  and  $C_b$  frames.  
1531 The decay tree is shown in ?? . In this case we apply a jigsaw at the level of  $P_a(P_b)$   
1532 which separates a single visible object  $V_{1a}$  ( $V_{2a}$ ) from the child frame  $C_a(C_b)$ . This  
1533 child frame represents the hypothesized squark after the decay  $\tilde{g} \rightarrow g\tilde{q}$ , which then  
1534 decays as in the squark case. This gives additional information which will be exploited  
1535 for the gluino specific search regions.

The third decay tree used in this thesis is the *compressed* decay tree. Compressed refers to signal models which have a small splitting between the mass of the proposed sparticle and the  $\tilde{\chi}_1^0$ . In this case, the sparticle decay products (i.e. the jets and  $E_T^{\text{miss}}$ ) do not generally have large scale[114]. Instead, the strategy is generally to look for a large-scale initial state radiation (ISR) jet which is recoiling off the disparticle system. In the case where the LSPs receive no momentum from the sparticle decays, the following approximation holds:

$$E_T^{\text{miss}} \sim -p_T^{\text{ISR}} \times \frac{m_{\tilde{\chi}_1^0}}{m_{\text{sparticle}}} \quad (7.13)$$

1536 where  $p_T^{\text{ISR}}$  is the transverse momentum associated to the entire ISR system.

1537 RJR offers a natural and straightforward way to exploit this feature in events  
1538 containing ISR. One imposes the simple decay tree in ?? with associated jigsaw rules.  
1539 With suitable jigsaw rules, this decay tree “picks out” the large  $p_T$  ISR jet, recoiling  
1540 off the  $E_T^{\text{miss}}$  and additional radiation from the sparticle decays. This provides a  
1541 convenient set of variables to understand compressed scenarios.

1542 There is one other decay tree, shown in ?? . This is special, as it is only used for  
1543 the purpose of QCD rejection, and does not directly map to a sparticle decay chain.  
1544 Due to the large production cross-sections of QCD events, even very rare large jet  
1545 mismeasurements can lead to significant  $E_T^{\text{miss}}$  which can enter the signal region. To  
1546 reduce these backgrounds, one usually rejects events which contain jets which are

1547 “too close” by some distance metric to the  $E_T^{\text{miss}}$  in the event. Generally, in the past,  
1548 the distance metric has been defined as simply the angular distance  $\Delta R$ .

1549 The *self-assembling tree* can be seen as defining a distance metric which depends  
1550 on the magnitudes of the  $E_T^{\text{miss}}$  and jets rather than simply their distance in angular  
1551 space. Depending on the exact kinematics, the one or two closest jets are found, and  
1552 label the  $E_T^{\text{miss}}$  *siblings*.

1553 In this section, we have seen how one imposes particular decay trees on an event  
1554 to produce a basis of kinematic variables in the approximated frames relevant to  
1555 the hypothesized sparticle decay chain. This explains why we call this procedure  
1556 “recursive”: we can continue the procedure through as many steps of a decay tree as  
1557 we want, and each application of a jigsaw rule is dependent on the variables produced  
1558 in the last step. The question, of course, is *what are these jigsaw rules?*.

## 1559 Jigsaw Rules

1560 Jigsaw rules are the fundamental step that allow the recursive definitions of the  
1561 variables of interest. We want rules which allow us to fully define kinematic variables  
1562 at each step in a decay tree. The only possible solution to fully define the event  
1563 kinematics in terms of the frames of the hypothesized decays is the imposition of  
1564 external constraints to eliminate additional degrees of freedom. In principle, these  
1565 need not have any particular physical motivation. Instead, the jigsaw rules are a  
1566 way to resolve the mathematical ambiguities to fully reconstruct the full decay chain  
1567 kinematics. However, most practical jigsaw rules also have some reasonable physical  
1568 motivation, which we will also elucidate.

1569 In the original razor point of view, some jigsaw rules can be seen as the definitions  
1570 of the boosts which relate the different frames of interest, while other rules allow one  
1571 to combine multiple objects and place them into a particular hemisphere (previously  
1572 megajet). These are the two forms of jigsaw rules: combinatoric and kinematic. As

1573 we have stressed before, the jigsaw rules are a *choice*; as long as a particular jigsaw  
1574 rule allows the definition of variables at each step in a decay tree, it is “as valid” as  
1575 any other rule.

Practically speaking, in this thesis we use only a small subset of possible jigsaw rules. The combinatoric jigsaw rule we use has already been introduced as megajet construction above. The minimization of

$$m_{J_1}^2 + m_{J_2}^2. \quad (7.14)$$

1576 is a jigsaw rule to deal with the combinatoric ambiguity implicit in which jets go in  
1577 which hemisphere. This is the jigsaw rule used in the decay trees when going from  
1578 one frame to two frames such as  $PP \rightarrow P_a, P_b$ .

1579 We will use three other jigsaw rules, which are both kinematic jigsaw rules. One  
1580 has already been used in the razor technique. The minimization of  $\beta_L$  will be used  
1581 as the jigsaw rule in the first step of each decay tree: the lab frame to the  $PP/\text{CM}$   
1582 frame. This is in effect the imposition of longitudinal boost invariance, as we expect  
1583 on average  $p_{z,PP,\text{CM}} = 0$ . One defines a unique longitudinal boost by imposition of  
1584 this external constraint.

1585 The final two jigsaw rules used in this thesis was not used in the razor technique.  
1586 We describe them here.

The first kinematic ambiguity is the total mass of the invisible system  $M_I$ . We guess this to be:

$$M_I^2 = M_V^2 - 4M_{V_a}M_{V_b}. \quad (7.15)$$

1587 As we stated above, there is no need to “justify” the jigsaw rules, as they are in some  
1588 ways a mathematical trick to fully resolve the event kinematics. However in this case,  
1589 there is a nice property of this guess. The symmetry of the production mechanism,  
1590 where we have two decay products  $V_i$  and  $I_i$  produced from the decay of the same  
1591 heavy sparticle, is explicit with this jigsaw choice.

1592 The final jigsaw rule we employ in this thesis is used to resolve the “amount” of  
1593  $E_T^{\text{miss}}$  that “belongs” to each hemisphere, and therefore how to impose the transverse  
1594 boost onto each of i.e.  $P_a$  and  $P_b$  from  $PP$ . Equivalently, it can be seen as the  
1595 resolution of the kinematics of the  $I_a$  and  $I_b$  objects in the disquark and digluino  
1596 decay trees. Recall that at this point, we have already approximated the boost  
1597 of the  $PP$  frame. The choice we use is to minimize the masses  $P_a$  and  $P_b$ , while  
1598 simultaneously constraining  $P_a = P_b$ . As is the case in the last step, there is a  
1599 straightforward physical interpretation of this choice. In the signal models we are  
1600 considering,  $P_a$  and  $P_b$  are the estimated frames of the squark or gluino pair-produced  
1601 as a heavy resonance. We then of course expect  $M_{P_a} = M_{P_b}$ .

1602 The imposition of the decay trees, with ambiguities resolved through the jigsaw  
1603 rules, give a full set of boosts relating the frames of each decay tree. In each frame,  
1604 we have estimates for the frame mass and decay angles, which can be used in searches  
1605 for new physics. In the next section, we describe the variables that are used in this  
1606 thesis in more details.

## 1607 7.3 Variables used in the search for zero lepton

### 1608 SUSY

1609 We describe here the variables used in the search described in ???. These were  
1610 reconstructed using the RJR algorithm as just described, using the RestFrames  
1611 packages[119]. In these frames, the momenta of all objects placed into that branch  
1612 of the decay tree are available (after application of the approximated boost), and in  
1613 principle we can calculate any variable of interest such as invariant masses or the  
1614 angles between these objects. The truly useful set of variables are highly dependent  
1615 on the signal process, and we leave their discussion to the subsequent chapters. It is  
1616 useful to understand the philosophy employed in the construction of these variables.

1617 In general, we can split variables useful for searches for new physics into two  
1618 categories: *scaleful* and *scaleless* variables. In this search, we will use a set of scaleful  
1619 variables called the  $H$  variables. The scaleless variables will consists of ratios and  
1620 angles. In general, we want to limit the number of scaleful cuts we apply, for two  
1621 reasons. Different scaleful variables are often highly correlated, and this of course  
1622 limits the utility of additional cuts. Addtionally, selections based on many scaleful  
1623 variables often “over-optimize” for particular signal model of interest, especially as  
1624 related to the mass difference chosen between the sparticle and the LSP. To avoid  
1625 this, each decay tree will only use two scale variables, one of which quantifies the  
1626 overall mass scale of the event, and another which acts as a measure of the event  
1627 balance.

## 1628 **Squark and gluino variables**

1629 Taking our general philosophy to a particular case, we here describe the variables  
1630 used by the squark and gluino searches. We have a suite of scale variables which we  
1631 will call the  $H$  variables, and a suite of angles and ratios.

1632 As we have described above, the RJR algorithm gives us access to the masses of  
1633 each frame of interest. It maybe seem natural, then, that these variables would be the  
1634 most useful for discrimination of the signal from background processes. However, due  
1635 to the all hadronic state considered in this thesis, the that can be constructed such  
1636 as  $M_{PP}$  can be affected by extra QCD radiation, which can promote the background  
1637 processes to large scales. The  $H$  variables show a resilience to this effect. They  
1638 take their name from the commonly used variable  $H_T$ , which is the scalar sum of  
1639 the visible momentum. However, due to the RJR technique, we can evaluate these  
1640 variables in the non-lab frame, including longitudinal information. They are also  
1641 constructed with *aggregate* momenta using a similar mass minimization procedure  
1642 as we have already described.

We label these variables as  $H_{n,m}^F$ . The frame from where they are evaluated is denoted  $F$ ; practically, this means  $F \in \{\text{lab}, PP, P_a, P_b\}$ . When the discussion applies to both  $P_a$  and  $P_b$ , we will write  $P_i$ . The subscripts  $n$  and  $m$  denote the number of visible and invisible vectors considered, respectively. When there are more vectors available than  $n$  or  $m$ , we add up vectors using the hemisphere (megajet) jigsaw rule until there are  $n$  ( $m$ ) objects.<sup>2</sup> In the opposite case, where  $n$  or  $m$  is greater than the number of available objects, one simply considers the available objects. The  $H_{n,m}^F$  variables are then defined as

$$H_{n,m}^F = \sum_i^n |\vec{p}_{\text{vis},i}^F| + \sum_j^m |\vec{p}_{\text{inv},i}^F|. \quad (7.16)$$

It may not be clear that these variables encode independent information. Fundamentally, this is just an expression of the triangle inequality  $\sum |\vec{p}| \geq |\sum \vec{p}|$ . The different combinations can then include independent information. The final note on the  $H$  variables is that we can also consider purely transverse versions of these variables, which we will denote  $H_{T,n,m}^F$ . Including this view, it is easy to see how the  $H$  variables are extensions of the normal  $H_T$  variables, as

$$H_T = H_{T,\infty,0}^{\text{lab}}. \quad (7.17)$$

1643     Although the  $H$  variables are interesting in their own right, the true power of the  
 1644     RJR technique comes from the construction of scaleless variables with the technique.  
 1645     This is because the scaleless ratios and angles are in fact measured in the “right”  
 1646     frame, where right here means an approximation of the correct frame. This provides  
 1647     a less correlated set of variables than those measured in the lab frame, due to the  
 1648     corrections to the disparticle or sparticle system boosts from the RJR technique.  
 1649     For the search for noncompressed disquark production, we use will use the  
 1650     following set of RJR variables.

---

<sup>2</sup>Recall that these vectors are constructed by the imposition of the decay tree with the relevant jigsaw rules.

- 1651     •  $H_{1,1}^{PP}$  - scale variable useful for discrimination against QCD backgrounds and  
 1652        used in a similar way to  $E_T^{\text{miss}}$

- 1653     •  $H_{T,2,1}^{PP}$  - scale variable providing information on the overall mass scale of the  
 1654        event for disquark signal production. We will often call this the *full* scale  
 1655        variable.

- 1656     •  $H_{T,1,1}^{PP}/H_{2,1}^{PP}$  - ratio used to prevent imbalanced events where the scale variable  
 1657        is dominated by one high  $p_T$  jet or high  $E_T^{\text{miss}}$

- 1658     •  $p_{PP,z}^{\text{LAB}}/(p_{PP,z}^{\text{LAB}} + H_{T,2,1}^{PP})$  - ratio used to prevent significant boosts in the  
 1659         $z$ -direction.  $p_{PP,z}^{\text{LAB}}$  is a measure of the total boost of the  $PP$  system from the lab  
 1660        frame

- 1661     •  $p_{T,j2}^{PP}/H_{T,2,1}^{PP}$  - ratio to force the second leading jet in the  $PP$  frame to carry a  
 1662        significant portion of the total scalar sum in that frame. This requirement is  
 1663        another balance requirement, on the total  $p_T$  of that second jet in the  $PP$  frame.

1664 First, we note that there is an implicit requirement that each hemisphere has at least  
 1665 one jet (to even reconstruct the  $P_a$  and  $P_b$  frames), these variables are implicitly using  
 1666 two or more jets, as we expect in disquark production. The other important thing  
 1667 to note is that all of the ratios use the full scale variable as the denominator. This  
 1668 is sensible, as we expect all of these effects to be scaled with the full scale variable  
 1669  $H_{T,2,1}^{PP}$ . We will see a similar behavior for the gluino regions, with a new full scale  
 1670 variable.

1671 For the search for noncompressed digluino production, we use will use the following  
 1672 set of RJR variables. Due to the increased complexity of the event topology with four  
 1673 jets, there are additional handles we can exploit:

- 1674     •  $H_{1,1}^{PP}$  - same as disquark production

- 1675     •  $H_{T,4,1}^{PP}$  - scale variable providing information on the overall mass scale of the  
 1676       event for digluino signal production. As before, we often call this the *full* scale  
 1677       variable. Since this variable allows the jets to be separated in the *PP* frame, it  
 1678       is more appropriate for digluino production.
- 1679     •  $H_{T,1,1}^{PP}/H_{4,1}^{PP}$  - ratio used to prevent imbalanced events where the scale variable  
 1680       is dominated by one high  $p_T$  jet or high  $E_T^{\text{miss}}$
- 1681     •  $H_{T,4,1}^{PP}/H_{4,1}^{PP}$  - ratio used to measure the fraction of the total scalar sum of the  
 1682       momentum in the transverse plane. Digluino production is expected to be fairly  
 1683       central
- 1684     •  $p_{PP,z}^{\text{LAB}}/(p_{PP,z}^{\text{LAB}} + H_{T,4,1}^{PP})$  - ratio used to prevent significant boosts in the  
 1685        $z$ -direction
- 1686     •  $\min(p_{T,j2_i}^{PP}/H_{T,2,1_i}^{PP})$ - ratio to require the second leading jet in *both* squark-like  
 1687       hemispheres  $C_a$ and  $C_b$ to contain a significant portion of *that frame's* momenta.  
 1688       This is similar to the  $p_{T,j2}^{PP}/H_{T,2,1}^{PP}$  disquark discriminator, but applied to both  
 1689       hemispheres  $C_a$ and  $C_b$ .
- 1690     •  $\max(H_{1,0}^{P_i}/H_{2,0}^{P_i})$ - ratio requiring one jet in each of the  $P_i$  to not take too much  
 1691       of the total momentum of that frame. This ratio is generally a very loose cut.

## 1692 Compressed variables

1693 As we saw above, the decay tree imposed for compressed spectra is simpler. We do  
 1694 not attempt to fully reconstruct the details of the system recoiling of the ISR system,  
 1695 but use a straightforward set of variables in this case. One additional simplification  
 1696 is that all variables are force to be transverse in this case; we simply do not include  
 1697 the  $\eta/z$  information of the objects as inputs to the RJR reconstruction. We still use  
 1698 the philosophy of limiting our scaleful variables to just two. The compressed scenario  
 1699 uses the following set of RJR variables:

1700 •  $p_{T,S}^{\text{ISR}}$ - scale variable that is the magnitude of the total transverse momenta of all  
 1701 jets associated to the ISR system, as evaluated in the CM frame

1702 •  $R_{\text{ISR}} \equiv p_I^{\hat{\text{CM}}} \cdot p_{T,S}^{\hat{\text{CM}}} / p_{T,S}^{\text{CM}}$  - this ratio is our measurement for the ratio of the LSP  
 1703 mass to the compressed sparticle mass. These are the values in the CM frame  
 1704 In compressed cases, this should be large, as this estimates the amount of the  
 1705 total  $\text{CM} \rightarrow S$  boost is carried by the invisible system.

1706 •  $M_{T,S}$ - the transverse mass of the  $S$  system

1707 •  $N_{\text{jet}}^V$ - the number of jets associated to the visible system  $V$

1708 •  $\Delta\phi_{\text{ISR},I}$ - the opening angle between the ISR system and the invisible system  
 1709 measured in the lab frame. As the invisible system is expected to carry much  
 1710 of the total  $S$  system momentum, this should be large, as we expect the ISR  
 1711 system to recoil directly opposite the  $I$  system in that case.

## 1712 Anti-QCD variables

1713 For the self-assembling tree, we construct two variables, which we combine to form a  
 1714 single variable which rejects QCD events. In this case, we use the mass minimization  
 1715 jigsaw, with a fully transverse version of the event (i.e. we set all jet  $z/\eta$  components  
 1716 to 0). This jigsaw defines the distance metric, and provides us with one or two jets  
 1717 known as the  $E_{\text{T}}^{\text{miss}}$  siblings. We define  $\vec{p}_{\text{sib}}$  as the sum of these jets, and define the  
 1718 following quantities.

We calculate a ratio observable which examines the relative magnitude of the sibling vector  $\vec{p}_{\text{sib}}$  and  $E_{\text{T}}^{\text{miss}}$ , and an angle relating  $\vec{p}_{\text{sib}}$  and  $E_{\text{T}}^{\text{miss}}$ :

$$R(\vec{p}_{\text{sib}}, E_{\text{T}}^{\text{miss}}) \equiv \frac{\vec{p}_{\text{sib}} \cdot \hat{E}_{\text{T}}^{\text{miss}}}{\vec{p}_{\text{sib}} \cdot \hat{E}_{\text{T}}^{\text{miss}} + |\vec{E}_{\text{T}}^{\text{miss}}|} \quad (7.18)$$

$$\cos \theta(\vec{p}_{\text{sib}}, E_{\text{T}}^{\text{miss}}) \equiv \frac{(\vec{p}_{\text{sib}} + \vec{E}_{\text{T}}^{\text{miss}}) \cdot \vec{p}_{\text{sib}}^{\text{miss}}}{|\vec{p}_{\text{sib}}| + E_{\text{T}}^{\text{miss}}} \quad (7.19)$$

These observables are highly correlated, but taking the following fractional difference provides strong discrimination between SUSY signal and QCD background events:

$$\Delta_{\text{QCD}} \equiv \frac{1 + \cos \theta(\vec{p}_{\text{sib}}, E_{\text{T}}^{\text{miss}}) - 2R(\vec{p}_{\text{sib}}, E_{\text{T}}^{\text{miss}})}{1 + \cos \theta(\vec{p}_{\text{sib}}, E_{\text{T}}^{\text{miss}}) + 2R(\vec{p}_{\text{sib}}, E_{\text{T}}^{\text{miss}})}. \quad (7.20)$$

<sup>1719</sup> We will use this variable in the next chapter.

1721 *A search for supersymmetric particles in zero lepton final  
 1722 states with the Recursive Jigsaw Technique*

1723 This section presents the details of the first search employing RJR variables as  
 1724 discriminating variables, as described in [115]. We will describe the simulation  
 1725 samples used, and then define the selections where we search for new SUSY  
 1726 phenomena, which we call the *signal regions* (SRs) Afterwards, we describe the  
 1727 background estimation techniques used in the analysis. Finally, we discuss the  
 1728 treatment of systematic uncertainties, and how we combine them using a likelihood  
 1729 method[120].

1730 **8.1 Simulation samples**

1731 We discussed the collision data sample provided by the LHC for the analysis in this  
 1732 thesis. We analyze a dataset of  $13.3 \text{ fb}^{-1}$  of collision data, at  $\sqrt{s} = 13 \text{ TeV}$ . To select  
 1733 events in data, we use the trigger system as previously discussed, and use the lowest  
 1734 unprescaled trigger which is available for a particular Standard Model background.  
 1735 We now discuss the simulation samples used for this search.

1736 Simulated data is fundamentally important to the ATLAS physics program.  
 1737 Calibrations, measurements, and searches use Monte Carlo (MC) simulations<sup>1</sup> to  
 1738 compare with collision data. In this thesis, MC samples are used to optimize the  
 1739 signal region selections, assist in background estimation, and assess the sensitivity to

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<sup>1</sup>In jargon, often just called “Monte Carlo” or MC.

1740 specific SUSY signal models. The details of Monte Carlo production, accuracy, and  
1741 utility are far beyond the scope of this thesis, but we provide a short description here.

1742 The first step is MC *generation*. A program is run which does a matrix-element  
1743 calculation, sometimes with additional corrections, which produces a set of output  
1744 particles from the parton interactions. These output particles are then decayed via  
1745 another (or the same) simulation program. This produces a set of *truth* particles,  
1746 which are the output of event generation. The details of which generator to use are  
1747 the subject of much discussion, and generally (many) comparisons are made between  
1748 them, for different processes of interest. Additionally, differences between generators  
1749 are often a starting point for the calculation of systematic uncertainties.

1750 The next step is the *simulation*. The detector response to the truth particles  
1751 is simulated, and simulated hits are produced. After simulation, the standard  
1752 reconstruction algorithms described previously are run with the simulated hits. This  
1753 procedure ensures “as close as possible” treatment of simulation and collision data.

1754 We give a brief description of which samples use which generators; additional  
1755 details are available in [115].

MAKE 1756 Signal (diguino and disquark) samples are generated with up to two ex-  
BETTER 1757 tra partons in the matrix element using MG5\_aMC@NLO 2.2.2 event genera-  
1758 tor [Alwall:2014hca] interfaced to PYTHIA 8.186 [Sjostrand:2014zea]. The  
1759 nominal cross-section is taken from an envelope of cross-section predictions using  
1760 different PDF sets and factorization and renormalization scales, as described in  
1761 Ref. [Kramer:2012bx], considering only light-flavour quarks ( $u, d, s, c$ ). For the  
1762 light-flavour squarks (gluinos) in case of gluino- (squark-) pair production, cross-  
1763 sections are evaluated assuming masses of 450 TeV. The free parameters are  $m_{\tilde{\chi}_1^0}$  and  
 $m_{\tilde{g}} (m_{\tilde{s}})$  for gluino-pair (squark-pair) production models.

explain 1764 Boson ( $W, Z, \gamma$ ) plus jet events are simulated using different SHERPAGenerators,  
we have a 1765 with COMIX and OPENLOOPS matrix-element generators[comix, openloops, 121].  
“grid” of 1766 these signal  
models  
samples

1767 Photons are required to have transverse momentum of  $> 35$  GeV. Importantly, the  
1768  $W(Z)$ +jet events are calculated at NLO while the the  $\gamma$ +jet events are calculated  
1769 at LO. The  $W/Z +$  jets events are normalized to their NNLO cross-sections  
1770 [Catani:2009sm]. The  $\gamma$ +jets LO cross-section is taken directly from **SHERPA**; we  
1771 will apply a correction factor to be described later.

1772 The various  $t\bar{t}$  and single-top processes[122] are generated using two versions of  
1773 **POWHEG-Box** [**powheg-box**, 122]. These are calculated at NLO and normalized  
1774 to various orders ranging from NLO to NNLO+NNLL in the different processes,  
1775 which can be seen in 8.1[Czakon:2013goa, Czakon:2011xx, Aliev:2010zk,  
1776 Kant:2014oha, Kidonakis:2010ux, Kidonakis:2011wy].

1777 Diboson processes ( $WW$ ,  $WZ$ ,  $ZZ$ ) [123] are simulated using the **SHERPA** 2.1.1  
1778 generator. For processes with four charged leptons ( $4\ell$ ), three charged leptons and  
1779 a neutrino ( $3\ell+1\nu$ ) or two charged leptons and two neutrinos ( $2\ell+2\nu$ ), the matrix  
1780 elements contain all diagrams with four electroweak vertices, and are calculated for  
1781 up to one ( $4\ell$ ,  $2\ell+2\nu$ ) or no partons ( $3\ell+1\nu$ ) at NLO and up to three partons at LO  
1782 using the **COMIX** and **OPENLOOPS** matrix-element generators, and merged with the  
1783 **SHERPA** parton shower using the ME+PS@NLO prescription. For processes in which  
1784 one of the bosons decays hadronically and the other leptonically, matrix elements  
1785 are calculated for up to one ( $ZZ$ ) or no ( $WW$ ,  $WZ$ ) additional partons at NLO  
1786 and for up to three additional partons at LO using the **COMIX** and **OPENLOOPS**  
1787 matrix-element generators, and merged with the **SHERPA** parton shower using the  
1788 ME+PS@NLO prescription. In all cases, the CT10 PDF set is used in conjunction  
1789 with a dedicated parton-shower tuning developed by the authors of **SHERPA**. The  
1790 generator cross-sections are used in this case.

1791 The multi-jet background is generated with **PYTHIA** 8.186 using the A14  
1792 underlying-event tune and the NNPDF2.3LO parton distribution functions.

1793 A summary of the SM background processes together with the MC generators,

1794 cross-section calculation orders in  $\alpha_s$ , PDFs, parton shower and tunes used is given  
 1795 in Table 8.1.

Physics process	Generator	Cross-section normalization	PDF set	Parton shower	Tune
$W(\rightarrow \ell\nu) + \text{jets}$	SHERPA 2.2.0	NNLO	NNPDF3.0NNLO	SHERPA	SHERPA default
$Z/\gamma^*(\rightarrow \ell\bar{\ell}) + \text{jets}$	SHERPA 2.2.0	NNLO	NNPDF3.0NNLO	SHERPA	SHERPA default
$\gamma + \text{jets}$	SHERPA 2.1.1	LO	CT10	SHERPA	SHERPA default
$t\bar{t}$	Powheg-Box v2	NNLO+NNLL	CT10	PYTHIA 6.428	PERUGIA2012
Single top ( $Wt$ -channel)	Powheg-Box v2	NNLO+NNLL	CT10	PYTHIA 6.428	PERUGIA2012
Single top ( $s$ -channel)	Powheg-Box v2	NLO	CT10	PYTHIA 6.428	PERUGIA2012
Single top ( $t$ -channel)	Powheg-Box v1	NLO	CT10f4	PYTHIA 6.428	PERUGIA2012
$t\bar{t} + W/Z/WW$	MG5_aMC@NLO 2.2.3	NLO	NNPDF2.3LO	PYTHIA 8.186	A14
$WW, WZ, ZZ$	SHERPA 2.1.1	NLO	CT10	SHERPA	SHERPA default
Multi-jet	PYTHIA 8.186	LO	NNPDF2.3LO	PYTHIA 8.186	A14

Table 8.1: The Standard Model background Monte Carlo simulation samples used in this thesis. The generators, the order in  $\alpha_s$  of cross-section calculations used for yield normalization, PDF sets, parton showers and tunes used for the underlying event are shown.

1796 For all SM background samples the response of the detector to particles is  
 1797 modelled with a full ATLAS detector simulation [:2010wqa] based on GEANT4  
 1798 [Agostinelli:2002hh]. Signal samples are prepared using a fast simulation based on  
 1799 a parameterization of the performance of the ATLAS electromagnetic and hadronic  
 1800 calorimeters [ATLAS:2010bfa] and on GEANT4 elsewhere.

1801 All simulated events are overlaid with multiple  $pp$  collisions simulated with  
 1802 the soft QCD processes of PYTHIA 8.186 using the A2 tune [A14tune] and the  
 1803 MSTW2008LO parton distribution functions [Martin:2009iq]. The simulations are  
 1804 reweighted to match the distribution of the mean number of interactions observed in  
 1805 data.

1806 **8.2 Event selection**

1807 This section describes the selection of the signal region events. We begin by describing  
1808 the *preselection*, which is used to remove problematic events and reduce the dataset  
1809 to a manageable size. We then describe the signal region strategy, and present the  
1810 signal regions used in the analysis.

1811 **Preselection**

1812 The preselection is used to reduce the dataset to that of interest in this thesis. The  
1813 table containing the preselection cuts is shown in 8.2. This selection is also used for  
1814 the samples used for background estimation, except for the lepton veto.

1815 The cuts [1] and [4] are a set of cleaning cuts to remove problematic events.  
1816 The *Good Runs List* is a centrally-maintained list of data runs which have been  
1817 determined to be “good for physics”. This determination is made by analysis of the  
1818 various subdetectors, and monitoring of their status. Event cleaning is used to veto  
1819 events which could be affected by noncollision background, noise bursts, or cosmic  
1820 rays.

1821 We require the lowest unprescaled  $E_T^{\text{miss}}$  trigger for the data run of interest, as  
1822 described previously, in cut [2]. The lepton veto is applied in cut [5]. These two cuts  
1823 are only used for the signal region selection.

1824 The rest of the preselection is used for the signal region and control regions used  
1825 for background estimation. These cuts on scaleful variables used by previous searches  
1826 are mostly used for the reduction of the dataset to a manageable size. Signal models  
1827 with sensitivity to lower values of these scaleful variables have been ruled out by  
1828 previous searches[124]. The final cut is on  $m_{\text{eff}}$ , which is the scalar sum of all jets and  
1829  $E_T^{\text{miss}}$ . This is the final discriminating variable used in the complementary search to  
1830 this thesis, which is also presented in [115].

Cut	Description	
1	Good Runs List	Veto events with intolerable detector errors
2	Trigger	HLT_xe70 (2015), HLT_xe80_tclcw_L1XE50, or HLT_xe100_mht_L1XE50 (2016)
3	Event cleaning	Veto for noncollision background, noise bursts, and cosmic rays
4	Lepton veto	No leptons with $p_T > 10$ GeV after overlap removal
5	$E_T^{\text{miss}}$ [GeV] >	250
6	$p_T(j_1)$ [GeV] >	200
7	$p_T(j_2)$ [GeV] >	50
8	$m_{\text{eff}}$ [GeV] >	800

Table 8.2: Preselection for the various event topologies used in the analysis.

## 1831 Signal regions

1832 We define a set of signal regions using the RJR variables previously described.  
 1833 These signal regions are split into three general categories: squark pair production  
 1834 SRs, gluino pair production SRs, and compressed production SRs. Within these  
 1835 general SRs, we have a set of signal regions targetting different mass splittings of the  
 1836 sparticle and LSP.

1837 A schematic of this strategy is shown in 8.1. This type of plane is how most  
 1838 ( $R$ -parity conserving) SUSY searches are organized in both ATLAS and CMS. The  
 1839 horizontal axis is the mass of the sparticle considered. In the case of this thesis,  
 1840 this will be the squark or gluino mass. On the horizontal axis, we place the LSP mass.  
 1841 These are the two free parameters of the simplified models considered here. Our  
 1842 search occurs in this two-parameter space. Each signal region targets some portion  
 1843 of this plane. As shown in the figure, a new iteration of a search will use a set of  
 1844 signal regions which have sensitivity just beyond those of the previous exclusions.  
 1845 The choice of how many signal regions to use to fully cover this plane is in many  
 1846 ways a matter of judgment, as it is important to avoid over or under/over-fitting  
 1847 to the signal models of interest. To take the extreme examples, One signal region

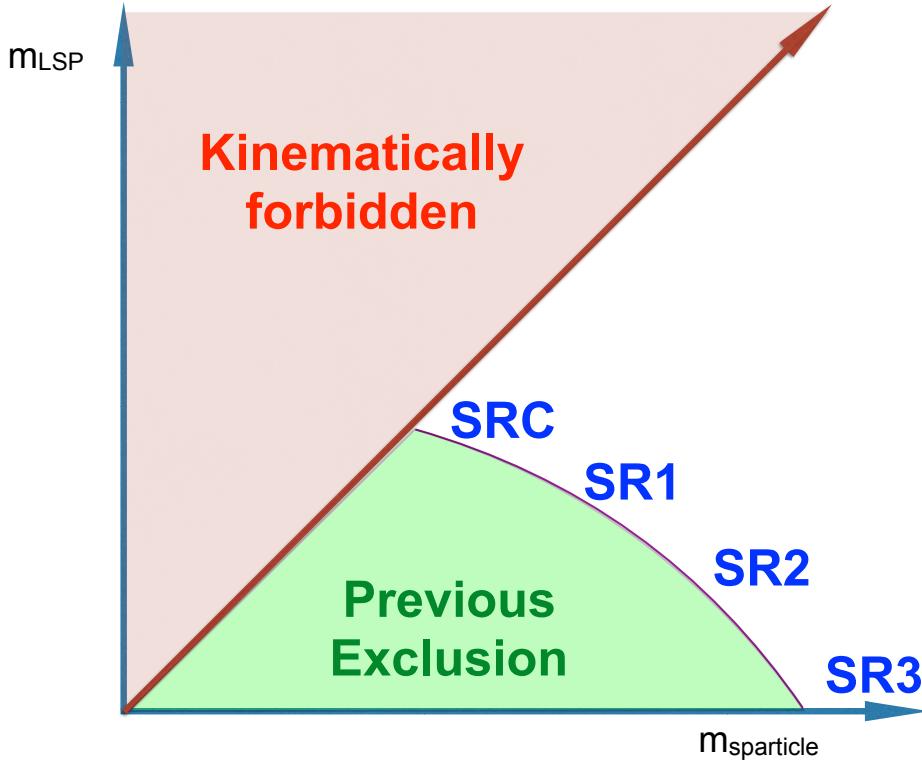


Figure 8.1: Schematic leading the development of the SUSY signal regions in this thesis. A variant of this schematic is used for most SUSY searches on ATLAS and CMS.

1848 will obscure the different phenomena in signal events with large versus small mass  
 1849 splittings, leading to underfitting. Binning as finely as possible<sup>2</sup> leads to overfitting  
 1850 due to the fluctuations present in the signal and background events passing the various  
 1851 selections selection. In this thesis, we use six squark signal regions, six gluino signal  
 1852 regions, and five compressed regions.

1853 The full table defining all signal regions is shown in 8.3. In all cases, the signal  
 1854 region selections contain a combination of scaleful and scaleless cuts. Emphasis  
 1855 on cuts on scaleful variables provide stronger sensitivity to larger mass splittings,  
 1856 while additional sensitivity to smaller mass splittings is found using stronger cuts on  
 1857 scaleless variables. One envisions walking from SR1 (with tight scaleless cuts and

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<sup>2</sup>This can be defined as having a signal region for each simulated signal sample, which for this analysis is  $\sim 100$ .

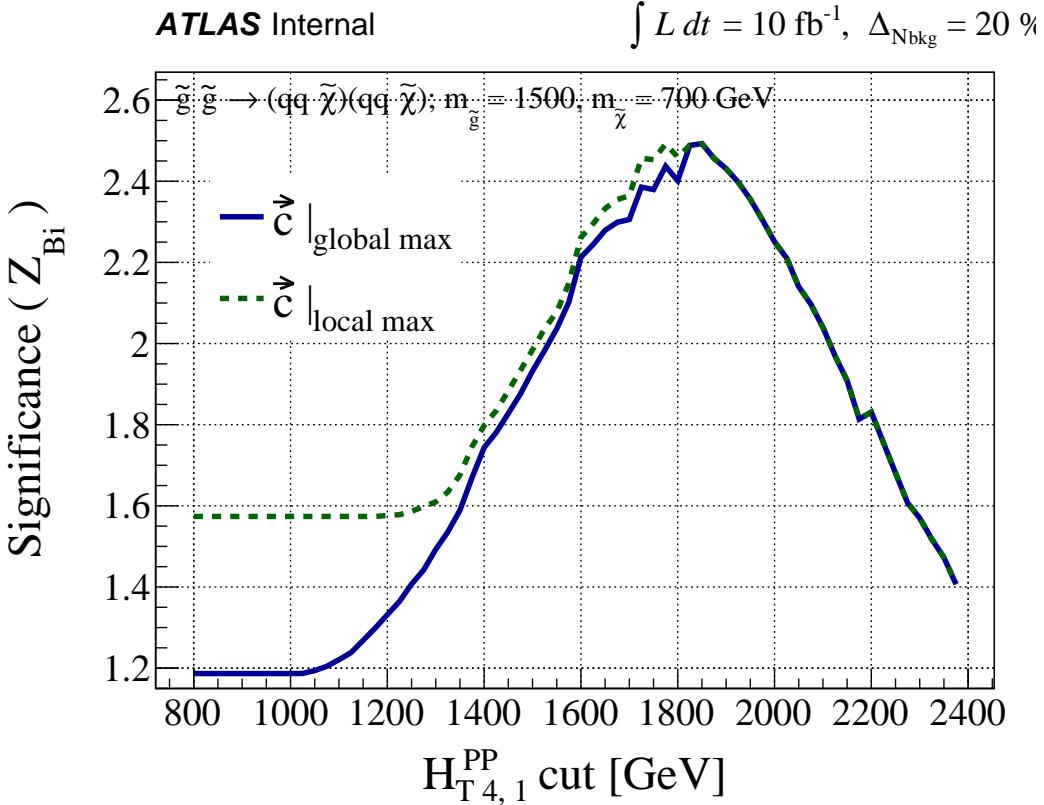


Figure 8.2: Optimization of the  $H_{T,4,1}^{PP}$  cut for a gluino signal model with  $(m_{\tilde{g}}, m_{\tilde{\chi}_1^0}) = (1500, 700)$  GeV assuming  $10 \text{ fb}^{-1}$  and an uncertainty of 20% on the background estimate.

1858 loose scaleful cuts) in 8.1 towards SR3 by loosening the scaleless cuts and tightening  
 1859 the scaleful cuts. We will see this strategy at work in each set of signal regions.

1860 We have already described the useful variables in the previous chapter. The  
 1861 question is how to choose the optimal cuts for a given set of signal models, which are  
 1862 grouped in the mass splitting space. This was done by a brute force scan over the  
 1863 cut values, using a guess of integrated luminosity with a fixed systematic uncertainty  
 1864 scenario; the value of the systematic uncertainty is motivated by that from previous  
 1865 analyses. We choose the lowest cut value that maximizes the  $Z_{Bi}$ , as described in  
 1866 [125]. This figure of merit gives conservative estimates, as compared to i.e.  $S/\sqrt{B}$ .  
 1867 A figure showing an example of this selection tuning procedure is shown in 8.2.

1868 The compressed selections are split into five regions (SRC1-5), and due to the

1869 simplified nature of the compressed decay tree, has sensitivity in both the gluino  
1870 and squark planes. The compressed regions target mass splittings with  $m_{\text{sparticle}} -$   
1871  $m_{\text{LSP}} \tilde{<} 200 \text{ GeV}$ . For the compressed region,  $M_{T,S}$  is the primary scaleful variable.  
1872 We can see the general strategy of lowering increasing scale cuts while decreasing the  
1873 scaleless cuts here. SRC1 targets the most compressed scenarios, with mass splittings  
1874 of less than 25 GeV, and has the loosest  $M_{T,S}$  cut coupled with the tightest  $R_{\text{ISR}}$  and  
1875  $\Delta\phi_{\text{ISR},I}$  cuts. SRC4 and SRC5 target mass splittings of  $\sim 200$  GeV, and are coupled  
1876 with the loosest scaleless cuts on  $R_{\text{ISR}}$  and  $\Delta\phi_{\text{ISR},I}$ . We also note that SRC4 and  
1877 SRC5 have differing cuts on  $N_{\text{jet}}^V$ , since these SRs are closest to the noncompressed  
1878 regions, and can be seen as the “crossover” where the differences between squark and  
1879 gluino production begins to become manifest.

1880 The squark regions (for noncompressed spectra) are organized into six signal  
1881 regions. These are labeled by a numeral 1-3 and letter a/b. SRs sharing a common  
1882 numeral i.e. SRS1a and SRS1b share a common set of scaleless cuts, while differing in  
1883 the main scale variable  $H_{T,2,1}^{PP}$ . The two SRs for each set of scaleless cuts, only differing  
1884 in the main scale variable, can be seen in a naïve way as providing sensitivity to a  
1885 range of luminosity scenarios<sup>3</sup>. As before, we see that the scaleless cuts are loosened  
1886 as we tighten the scaleful cuts, as we move across the table from SRS1a to SRS3b.  
1887 This provides strong sensitivity to signal models with intermediate mass splittings with  
1888 SRS1a to large mass splittings with SR3b.

1889 The gluino signal regions are organized entirely analogously to the squark signal  
1890 regions. There are six gluino signal regions, again labeled via a numeral 1-3 and letter  
1891 a/b. Those SRs sharing a common numeral have a common set of scaleless cuts, but  
1892 differ in their main scale variable  $H_{T,4,1}^{PP}$ . The SRs follow scaleless vs scaleful strategy,  
1893 with SRG1 having the loosest scaleful cut cuts coupled with the strongest scaleless

---

<sup>3</sup>These SRs were defined before the entire collision dataset was produced, and thus needed to be robust in cases where the LHC provided significantly different than expected performance.

1894 cuts, and the converse being true in SRG3. As in the squark case, this strategy  
1895 provides strong expected sensitivity throughout the gluino-LSP plane.

Targeted signal	$\tilde{s}\tilde{s}, \tilde{s} \rightarrow q\tilde{\chi}_1^0$									
Requirement	Signal Region									
	<b>RJR-S1</b>		<b>RJR-S2</b>		<b>RJR-S3</b>					
$H_{1,1}^{PP}/H_{2,1}^{PP} \geq$	0.6		0.55		0.5					
$H_{1,1}^{PP}/H_{2,1}^{PP} \leq$	0.95		0.96		0.98					
$p_{PP, z}/(p_{PP, z}^{lab} + H_{T, 2,1}^{PP}) \leq$	0.5		0.55		0.6					
$p_{j2, T}^{PP}/H_{T, 2,1}^{PP} \geq$	0.16		0.15		0.13					
$\Delta_{QCD} >$	0.001									
	<b>RJR-S1a</b>	<b>RJR-S1b</b>	<b>RJR-S2a</b>	<b>RJR-S2b</b>	<b>RJR-S3a</b>	<b>RJR-S3b</b>				
$H_{T, 2,1}^{PP}$ [GeV] >	1000	1200	1400	1600	1800	2000				
$H_{1,1}^{PP}$ [GeV] >	1000		1400		1600					
Targeted signal	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow q\bar{q}\tilde{\chi}_1^0$									
Requirement	Signal Region									
	<b>RJR-G1</b>		<b>RJR-G2</b>		<b>RJR-G3</b>					
$H_{1,1}^{PP}/H_{4,1}^{PP} \geq$	0.35		0.25		0.2					
$H_{T, 4,1}^{PP}/H_{4,1}^{PP} \geq$	0.8		0.75		0.65					
$p_{PP, z}/(p_{PP, z}^{lab} + H_{T, 4,1}^{PP}) \leq$	0.5		0.55		0.6					
$\min(p_{j2, T, i}^{PP}/H_{T, 2,1}^{PP}) \geq$	0.12		0.1		0.08					
$\max(H_{1,0}^{Pi}/H_{2,0}^{Pi}) \leq$	0.95		0.97		0.98					
$  \frac{2}{3}\Delta\phi_{V,P}^{PP} - \frac{1}{3}\cos\theta_p   \leq$	0.5		—		—					
$\Delta_{QCD} >$	0									
	<b>RJR-G1a</b>	<b>RJR-G1b</b>	<b>RJR-G2a</b>	<b>RJR-G2b</b>	<b>RJR-G3a</b>	<b>RJR-G3b</b>				
$H_{T, 4,1}^{PP}$ [GeV] >	1000	1200	1500	1900	2300	2700				
$H_{1,1}^{PP}$ [GeV] >	600		800		900					
Targeted signal	compressed spectra in $\tilde{s}\tilde{s}$ ( $\tilde{s} \rightarrow q\tilde{\chi}_1^0$ ); $\tilde{g}\tilde{g}$ ( $\tilde{g} \rightarrow q\bar{q}\tilde{\chi}_1^0$ )									
Requirement	Signal Region									
	<b>RJR-C1</b>	<b>RJR-C2<sub>133</sub></b>	<b>RJR-C3</b>	<b>RJR-C4</b>	<b>RJR-C5</b>					
$R_{ISR} \geq$	0.9	0.85	0.8	0.75	0.70					
$\Delta\phi_{ISR, I} >$	3.1	3.07	2.95	2.95	2.95					

Requirement	Signal Region				
	<b>RJR-C1</b>	<b>RJR-C2<sub>133</sub></b>	<b>RJR-C3</b>	<b>RJR-C4</b>	<b>RJR-C5</b>
$R_{ISR} \geq$	0.9	0.85	0.8	0.75	0.70
$\Delta\phi_{ISR, I} >$	3.1	3.07	2.95	2.95	2.95

## 1896 8.3 Background estimation

1897 We describe here the method of background estimation. In this thesis, we detail what  
 1898 is colloquially called a “cut-and-count” analysis. This is in contrast to a “shape fit”  
 1899 analysis, where one needs to consider the details of the variable distribution shapes.  
 1900 Instead, we must ensure the overall normalization of the Standard Model backgrounds  
 1901 are correct in the regions of phase space considered in the analysis. In order to  
 1902 do this, we define a set of *control regions* which are free of SUSY contamination  
 1903 based on the previously excluded analysis. We compare the number of events present  
 1904 in the control regions in simulation with that in data to define a *transfer factor*  
 1905 (TF). We extrapolate the number of expected events from each background using  
 1906 this transfer factor to translate from the , which provides our final estimate of the  
 1907 SM background in the corresponding signal region. To be explicit, each signal region  
 1908 SR has a corresponding set of control regions.

More precisely, for a given signal region, we are attempting to estimate the value  $N_{\text{SR}}^{\text{data}}$  for a given background. This value is estimated using the following equation:

$$N_{\text{SR}}^{\text{data,est}} = N_{\text{CR}}^{\text{data,obs}} \times \text{TF}_{\text{CR}} \equiv N_{\text{CR}}^{\text{data,obs}} \times \left( \frac{N_{\text{SR}}^{\text{MC}}}{N_{\text{CR}}^{\text{MC}}} \right) \quad (8.1)$$

1909 where the transfer factor TF is taken directly from MC. The two ingredients to our  
 1910 estimation of  $N_{\text{SR}}^{\text{data,obs}}$  is thus  $N_{\text{CR}}^{\text{data,obs}}$  and the transfer factor taken from MC.

The transfer factor method is potentially more straightforward written in the following way:

$$N_{\text{SR}}^{\text{data,est}} = N_{\text{SR}}^{\text{MC}} \times \left( \frac{N_{\text{CR}}^{\text{data,obs}}}{N_{\text{CR}}^{\text{MC}}} \right) \equiv N_{\text{SR}}^{\text{MC}} \times \mu_{\text{CR}}. \quad (8.2)$$

1911 In this form, the correction to the overall normalization is explicit. The ratio  $\frac{N_{\text{CR}}^{\text{data,obs}}}{N_{\text{CR}}^{\text{MC}}}$   
 1912 which we call  $\mu$  informs us how to scale  $N_{\text{SR}}^{\text{MC}}$  in order to get the right overall  
 1913 normalization. The assumption made with this method is that the overall shape of  
 1914 the distribution should not change “that much” as one extrapolates to the signal  
 1915 region.

1916        The CR definitions are motivated and designed according to two (generally  
1917 competing) requirements:

- 1918        1. Statistical uncertainties due to low CR statistics  
1919        2. Systematic uncertainties related to the extrapolation from the CR to the SR.

1920        This motivates the desire to make the control regions as similar as possible  
1921        to the signal regions without risking signal contamination while ensuring high  
1922        purity in the targeted SM background.

1923        In principle, one can also apply data-driven corrections to the TF obtained for each  
1924        CR.

1925        In order to validate the transfer factors obtained from MC, we also develop a series  
1926        of *validation regions* (VRs). These regions are generally designed to be “in between”  
1927        the control region and signal region selections in phase space, and thus provide a  
1928        check on the extrapolation from the control regions into the signal regions. Despite  
1929        their closeness in phase space to the signal regions, they are also designed to have  
1930        low signal contamination.

1931        In practice, we perform this estimation procedure simultaneously across all control  
1932        regions; we describe this later. We only note this here since we can also apply  
1933        Eq.8.1 to measure the contamination of a control region with another background as  
1934        well. This procedure accounts for the correlations between regions due to correlated  
1935        systematic uncertainties. We next describe the control region selection for the major  
1936        SM backgrounds for the analysis.

## 1937        **Control Regions**

1938        As was hinted at in the discussion of Monte Carlo generators, the primary back-  
1939        grounds of note in this analysis are  $Z + \text{jets}$ ,  $W + \text{jets}$ ,  $t\bar{t}$ , and QCD events. There is  
1940        also a minor background from diboson events which is taken directly from MC with an

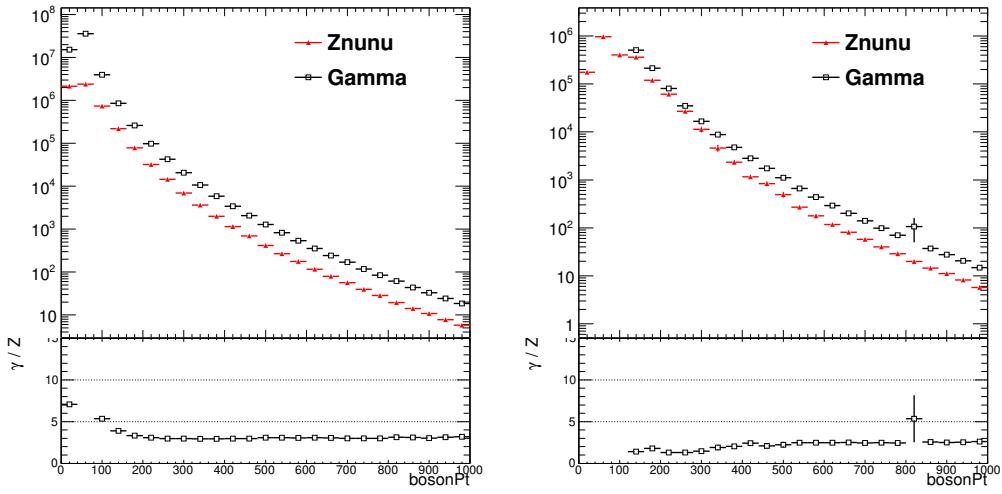
1941 uncertainty of 50%. We describe the strategy to estimate these various backgrounds  
 1942 here. A summary table is shown in 8.4. All distributions shown in this section use  
 1943 the scaling factors  $\mu$  from the background fits, which we describe later.

CR	SM background	CR process	CR event selection
Meff/RJR-CR $\gamma$	$Z(\rightarrow \nu\bar{\nu}) + \text{jets}$	$\gamma + \text{jets}$	Isolated photon
Meff/RJR-CRQ	Multi-jet	Multi-jet	$\Delta_{\text{QCD}} < 0$ reversed requirement on $H_{1,1}^{PP}$ (RJR-S/G) or $R_{\text{ISR}} < 0.5$ (RJR-C)
Meff/RJR-CRW	$W(\rightarrow \ell\nu) + \text{jets}$	$W(\rightarrow \ell\nu) + \text{jets}$	$30 \text{ GeV} < m_T(\ell, E_T^{\text{miss}}) < 100 \text{ GeV}$ , $b$ -veto
Meff/RJR-CRT	$t\bar{t}(\text{+EW})$ and single top	$t\bar{t} \rightarrow b\bar{b}qq'\ell\nu$	$30 \text{ GeV} < m_T(\ell, E_T^{\text{miss}}) < 100 \text{ GeV}$ , $b$ -tag

Table 8.4: Control regions used in this thesis.

1944 Events with a  $Z$  boson decaying to neutrinos in association with jets are the  
 1945 primary irreducible background in the analysis. These events have true  $E_T^{\text{miss}}$  from  
 1946 the decaying neutrinos, and can have significant values of the scaleful variables of  
 1947 interest. Naively, one might expect us to use  $Z \rightarrow \ell\ell$  as the control process of interest,  
 1948 as  $Z \rightarrow \ell\ell$  events are quite well-measured. Unfortunately, the  $Z \rightarrow \ell\ell$  branching ratio  
 1949 is about half of from  $Z \rightarrow \nu\nu$ , which necessitates loosening the control region selection  
 1950 significantly. This leads to unacceptably large systematic uncertainties in the transfer  
 1951 factor.

1952 Instead, photon events are used as the control region for the  $Z \rightarrow \nu\nu$  events. We  
 1953 label this photon control region as CRY. The photon is required to have  $p_T > 150 \text{ GeV}$   
 1954 to ensure the trigger is fully efficient. The kinematic properties of photon events  
 1955 strongly resemble those of  $Z$  events when the boson  $p_T$  is significantly above the  
 1956 mass of the  $Z$  boson. In this regime, the neutral bosons are both scaleless, and can be  
 1957 treated interchangeably, up to the differences in coupling strengths. Additionally, the



(a) Boson  $p_T$  ratio as a function of true boson  $p_T$   
(b) Boson  $p_T$  ratio as a function of reconstructed boson  $p_T$

Figure 8.3

1958 cross-section for  $\gamma + \text{jets}$  events is significantly larger than  $Z + \text{jets}$  events above the  $Z$   
1959 mass. These features are shown in 8.3 in simulated  $Z \rightarrow \nu\nu$  truth and reconstructed  
1960 events. The reconstructed  $Z \rightarrow \nu\nu$  events define the boson  $p_T$  as simply the  $E_T^{\text{miss}}$ .  
1961 In truth events, one clearly sees the effect of the  $Z$  mass below  $\sim 100$  GeV, with a  
1962 flattening of the ratio above  $\sim 300$  GeV. In reconstructed events, the effects are less  
1963 clear at low boson  $p_T$ , primarily due to cut sculpting from i.e. the trigger requirement  
1964 on photon events, which necessitates a higher  $p_T$  cut on photon events for the trigger  
1965 to remain fully efficient. Still, it is clear that the ratio flattens out at high boson  $p_T$ ,  
1966 and we are justified in the use of CRY to model the  $Z + \text{jets}$  background.

1967 The CRY kinematic selection is slightly looser in the scaleful variables for the  
1968 noncompressed regions to provide sufficient control region statistics. This is chosen  
1969 to be  $H_{1,1}^{PP} > 900$  GeV ( $H_{1,1}^{PP} > 550$  GeV) for the squark (gluino) regions to minimize  
1970 the corresponding statistical and systematic uncertainties.

1971 One additional correction scale factor is applied to  $\gamma + \text{jets}$  events before calculat-  
1972 ing the transfer factors. This is known as the  $\kappa$  method, which is used to determine  
1973 the disagreement arising from the use of a LO generator for photon events vs. a NLO

1974 generator for  $Z$ +jets events, which can reduce the theoretical uncertainties from  
 1975 this disagreement. One can see this as a measurement of the k-factor for the LO  
 1976  $\gamma$ +jets sample. This is effectively done with an auxiliary CRZ region, defined using  
 1977 two leptons with an invariant mass close with 25 GeV of the Z mass. The correction  
 1978 factor derived for this purpose is  $\kappa = 1.39 \pm 0.05$ .

1979 Distributions of CRY in squark, gluino, and compressed regions are shown in ??.  
 1980 One can see the quite high purity of CRY in photon events from these plots.

Event with a  $W$  boson decaying leptonically via  $W \rightarrow \ell\nu$  can also enter the signal region. In this case, we use leptonically to include all leptons ( $e, \mu, \tau$ ). The  $W$ +jets events passing the event selection either have a hadronically-decaying  $\tau$ , with a neutrino supplying  $E_T^{\text{miss}}$ , or the case where a muon or electron is misidentified as a jet or missed completely due to the limited detector acceptance. To model this background, we use a sample of one-lepton events with a veto on b-jets, which we label CRW. The lepton is required to have  $p_T > 27$  GeV to guarantee a fully efficient trigger. We then treat this single lepton as a jet for purposes of the RJR variable calculations. We apply a kinematic selection on the transverse mass:

$$m_T = \sqrt{2p_{T,\ell}E_T^{\text{miss}}(1 - \cos\phi_e - E_\phi^{\text{miss}})}, \quad (8.3)$$

1981 around the  $W$  mass:  $30 \text{ GeV} < m_T < 100 \text{ GeV}$ . Checks in simulation shows that  
 1982 these requirements give a sample of high purity  $W \rightarrow \ell\nu$  background. Due to low  
 1983 statistics using the kinematic cuts imposed in the signal regions, the control region  
 1984 kinematic cuts are slightly loosened with respect to the signal region cuts. We use  
 1985 the loosest cut in any signal region as the control region selection for all signal  
 1986 regions. More clearly, the control region selection corresponding to each signal region  
 1987 is the *same*. As discussed above, this leads to a tolerable increase in the systematic  
 1988 uncertainty from the extrapolation from the CR to the SR when compared to the  
 1989 resulting statistical uncertainty.

1990      Distributions of CRW in squark, gluino, and compressed regions are shown in ??.

1991      There is high purity in  $W+\text{jets}$  events in the control region corresponding to all

1992      signal regions.

1993      Top events are also an important background, for the same reasons as the

1994       $W+\text{jets}$  background, due to the dominant top decay channel of  $t \rightarrow Wb$ . For a

1995      top event to be selected by the analysis criteria, as in the case of  $W+\text{jets}$ , we expect

1996      a  $W$  to decay via a  $\tau$  lepton which decays hadronically or one a muon or electron to

1997      be misidentified as a jet or be outside the detector acceptance. We are not so worried

1998      about hadronic or all dileptonic tops: hadronic  $t\bar{t}$  events generally have low  $E_T^{\text{miss}}$

1999      (and  $H_{1,1}^{PP}$ ) so they will not pass the kinematic cuts, while dileptonic  $t\bar{t}$  events have a

2000      lower cross-section and good reconstruction efficiency from the two leptons. We are

2001      thus primarily concerned with semileptonic  $t\bar{t}$  events with  $E_T^{\text{miss}}$  from the neutrino.

2002      To model this background, we use the same selection as the  $W$  selection, but require

2003      that one of the jets chosen by the analysis has at least one  $b$ -tag. This selection has

2004      quite high purity, as we expect the  $t\bar{t}$  background to have two  $b$ -jets. Thus with

2005      the 70%  $b$ -tagging efficiency working point used in this analysis, ignoring (small)

2006      correlations between the two  $b$ -tags, we expect to tag one of the  $b$ -jets greater than

2007      90% of the time. As with CRW, we need to loosen the cuts applied to CRT with

2008      respect to the signal region in order to gain sufficient expected data statistics. We

2009      use exactly the same scheme; the CRT corresponding to each SR is identical, due to

2010      using the loosest set of cuts among the SRs. This comes at the cost of an increased

2011      systematic uncertainty for this extrapolation, but it was determined that this tradeoff

2012      resulted in the lowest overall uncertainty.

2013      Distributions of CRT in squark, gluino, and compressed regions are shown in ??.

2014      There is high purity in top events in the control region corresponding to all signal

2015      regions.

2016      The final important background is the QCD background. As briefly discussed in

2017 the previous chapter, QCD backgrounds are difficult, for a few reasons we describe  
2018 here. The large cross-section for QCD events means that even very rare extreme  
2019 mismeasurements can be seen in our signal regions. However, as these events are  
2020 very rare, one requires extreme confidence in the tails of the distributions to use  
2021 simulation as an input for background estimation. To avoid this, the strategy in  
2022 these cases is to apply a strong enough cut to expect *zero* QCD events in the signal  
2023 regions to avoid this issue. To produce a sample enriched in QCD, which we call CRQ,  
2024 we reverse the  $\Delta_{\text{QCD}}$  and  $H_{1,1}^{PP}$  cuts. This analysis uses the jet smearing method, as  
2025 described in [126]. This is a data-driven method which applies a resolution function  
2026 to well-measured QCD events, which also an estimate of the impact of the jet energy  
2027 mismeasurement on  $E_{\text{T}}^{\text{miss}}$  and subsequently the RJR variables.

2028 Distributions of CRQ in squark, gluino, and compressed regions are shown in ??.  
2029 There is high purity in top events in the control region corresponding to all signal  
2030 regions.

2031 The final background of note in this background is the diboson background. This  
2032 background is estimated directly from simulation. Due to the low cross-section of  
2033 electroweak processes, this background is not significant in the signal regions. We  
2034 assign a large ad-hoc 50% systematic on the cross-section, and do not attempt to  
2035 define a control region for this background.

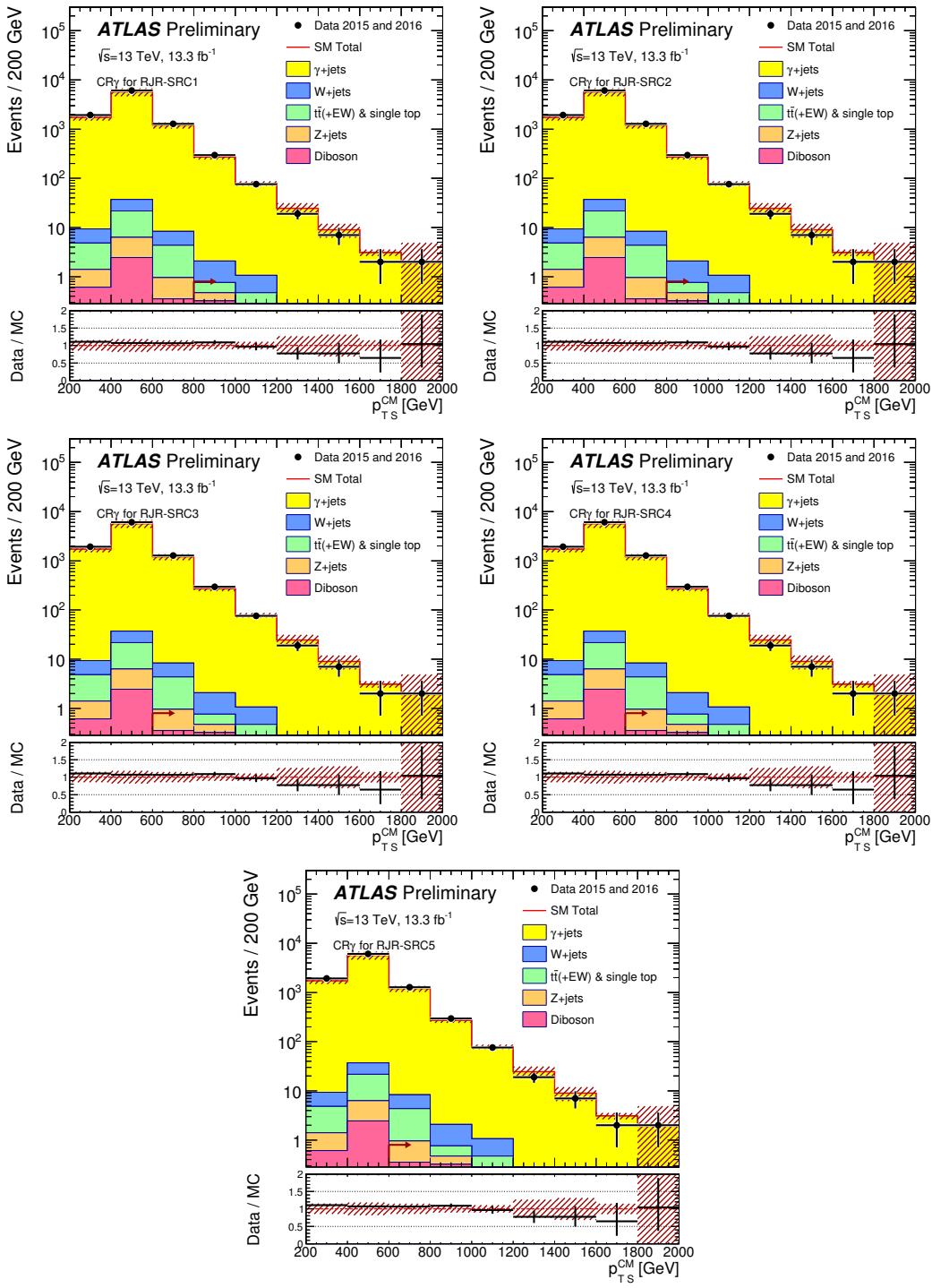


Figure 8.4: Scale variable distributions for the compressed CRY regions.

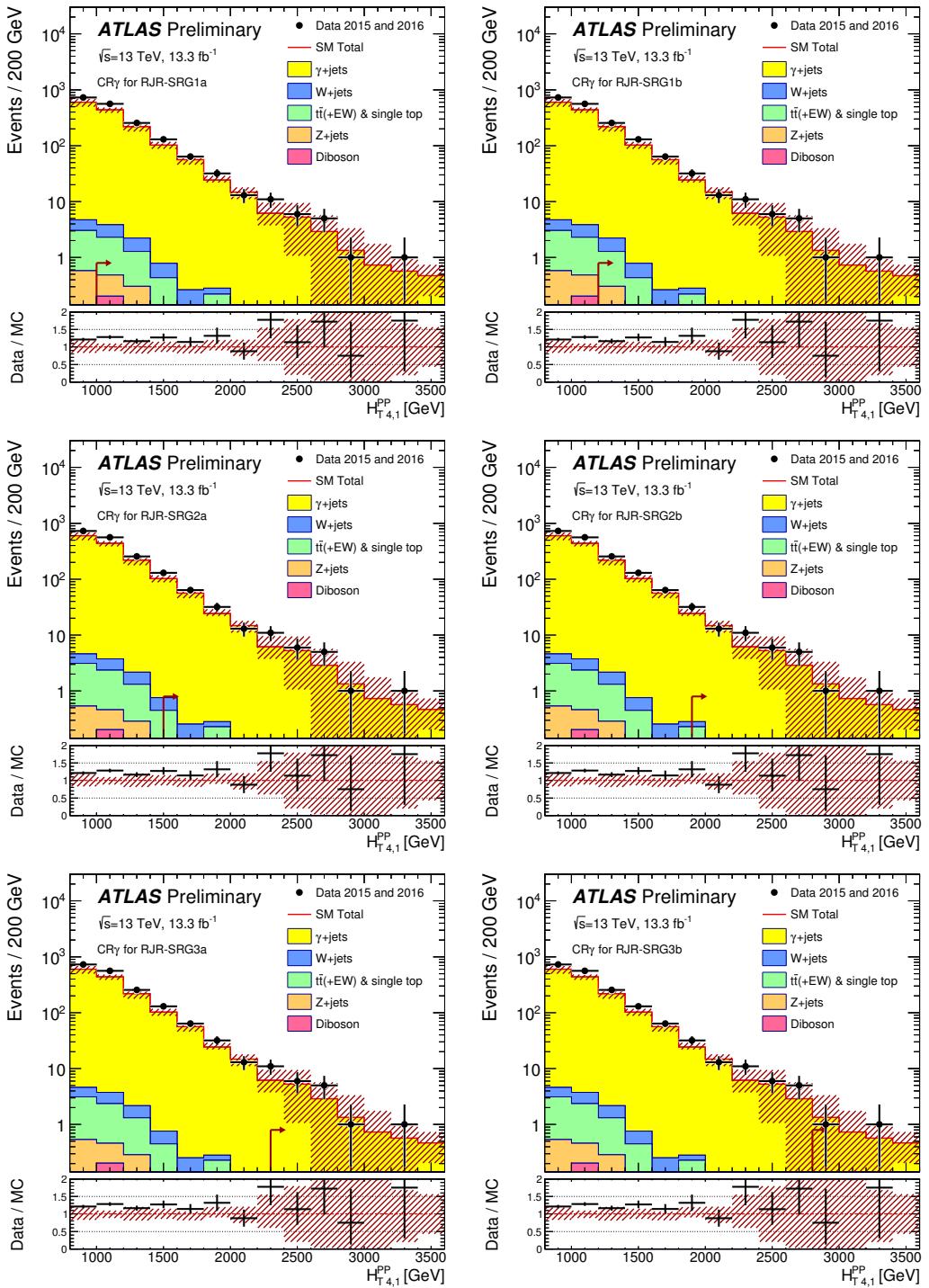


Figure 8.5: Scale variable distributions for the gluino CRY regions.

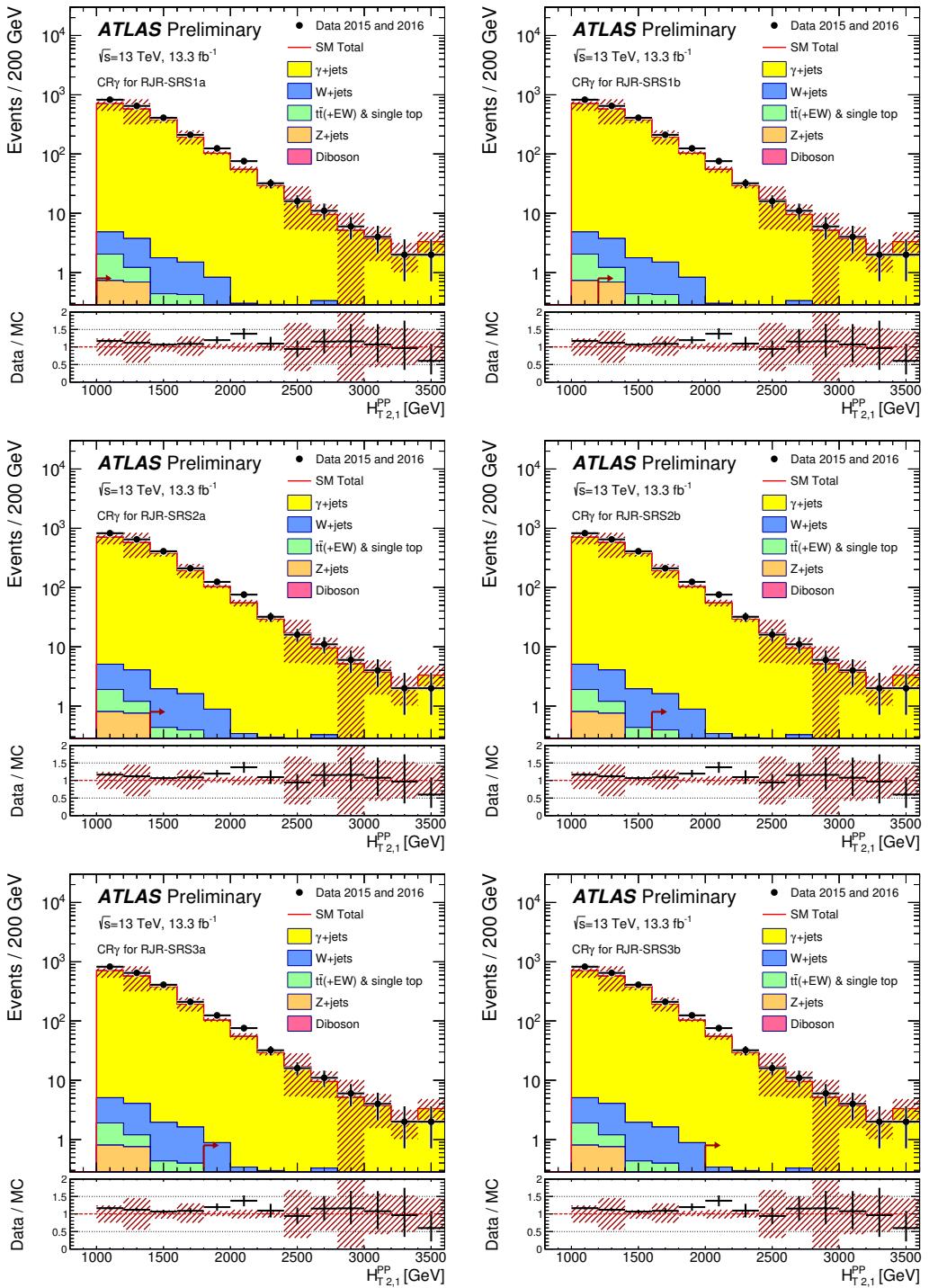


Figure 8.6: Scale variable distributions for the squark CRY regions.

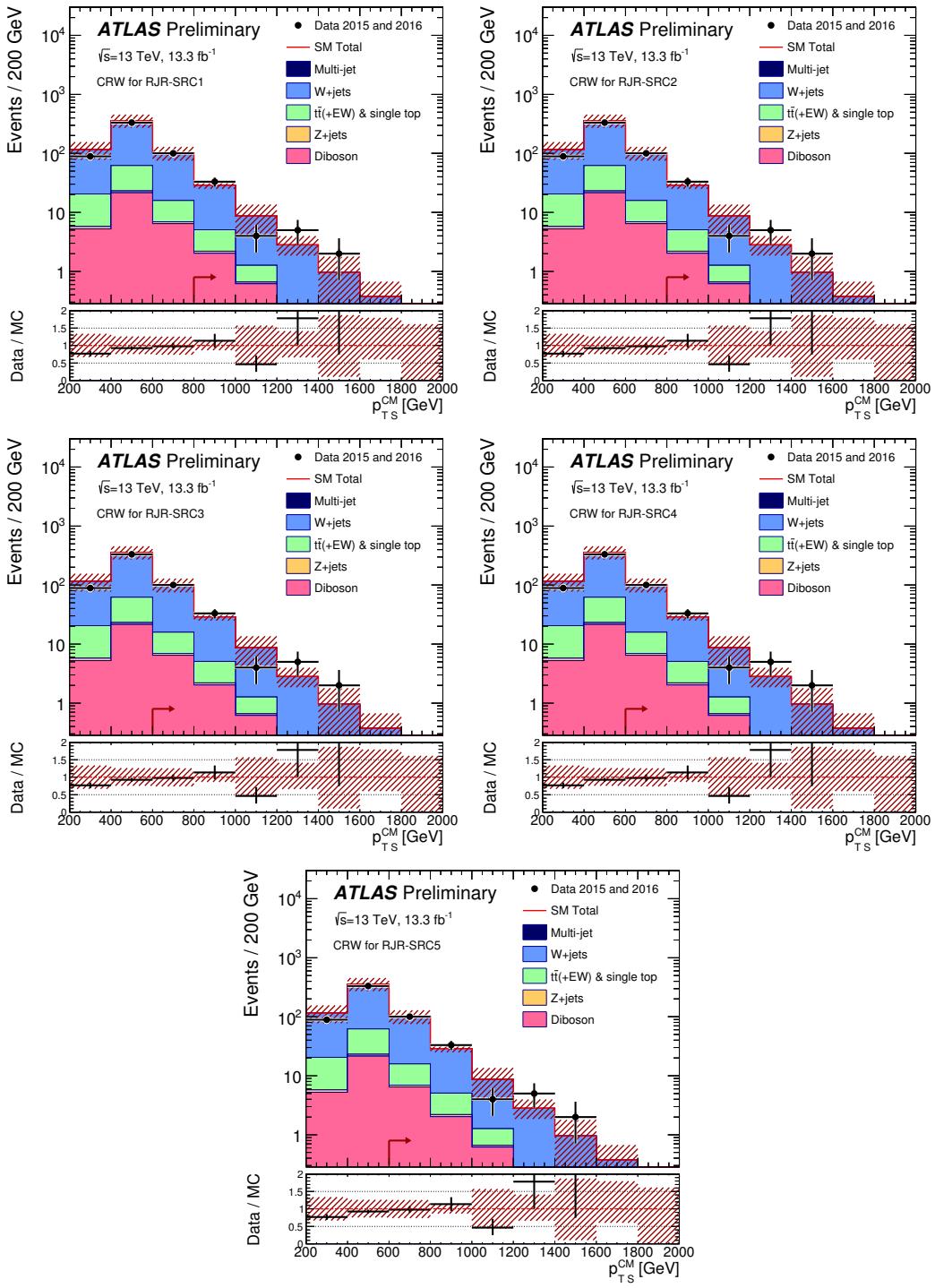


Figure 8.7: Scale variable distributions for the compressed CRW regions.

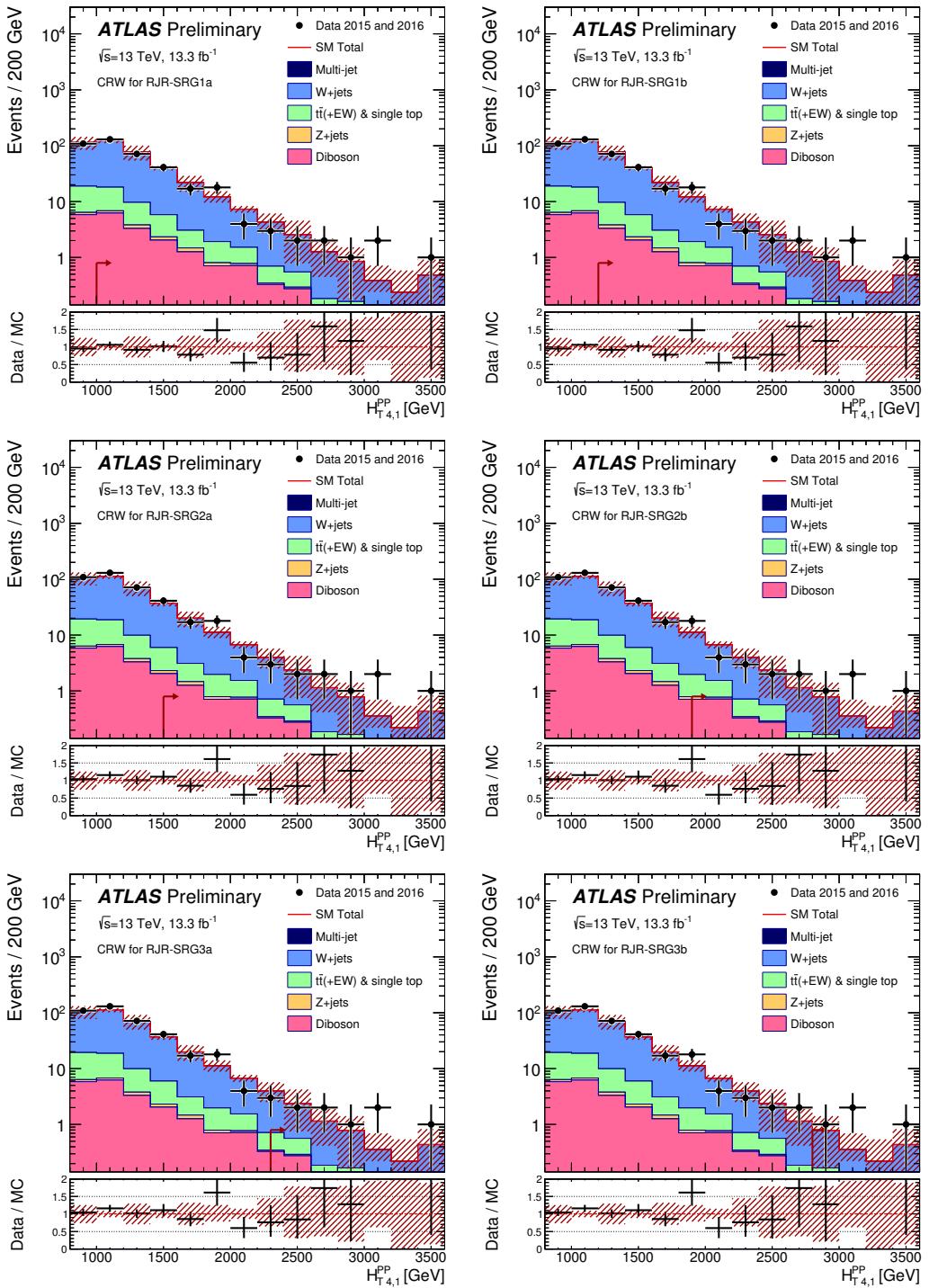


Figure 8.8: Scale variable distributions for the gluino CRW regions.

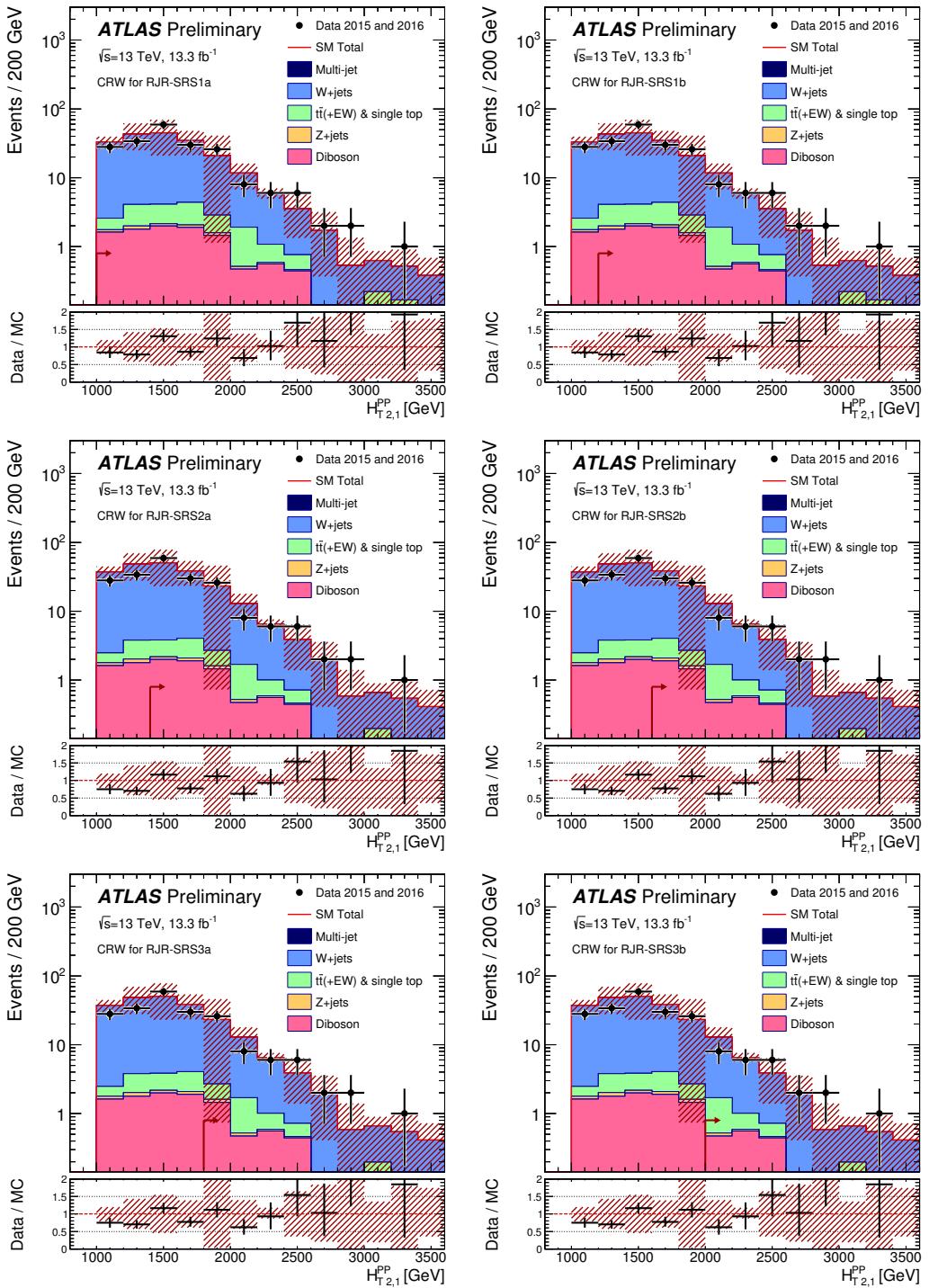


Figure 8.9: Scale variable distributions for the squark CRW regions.

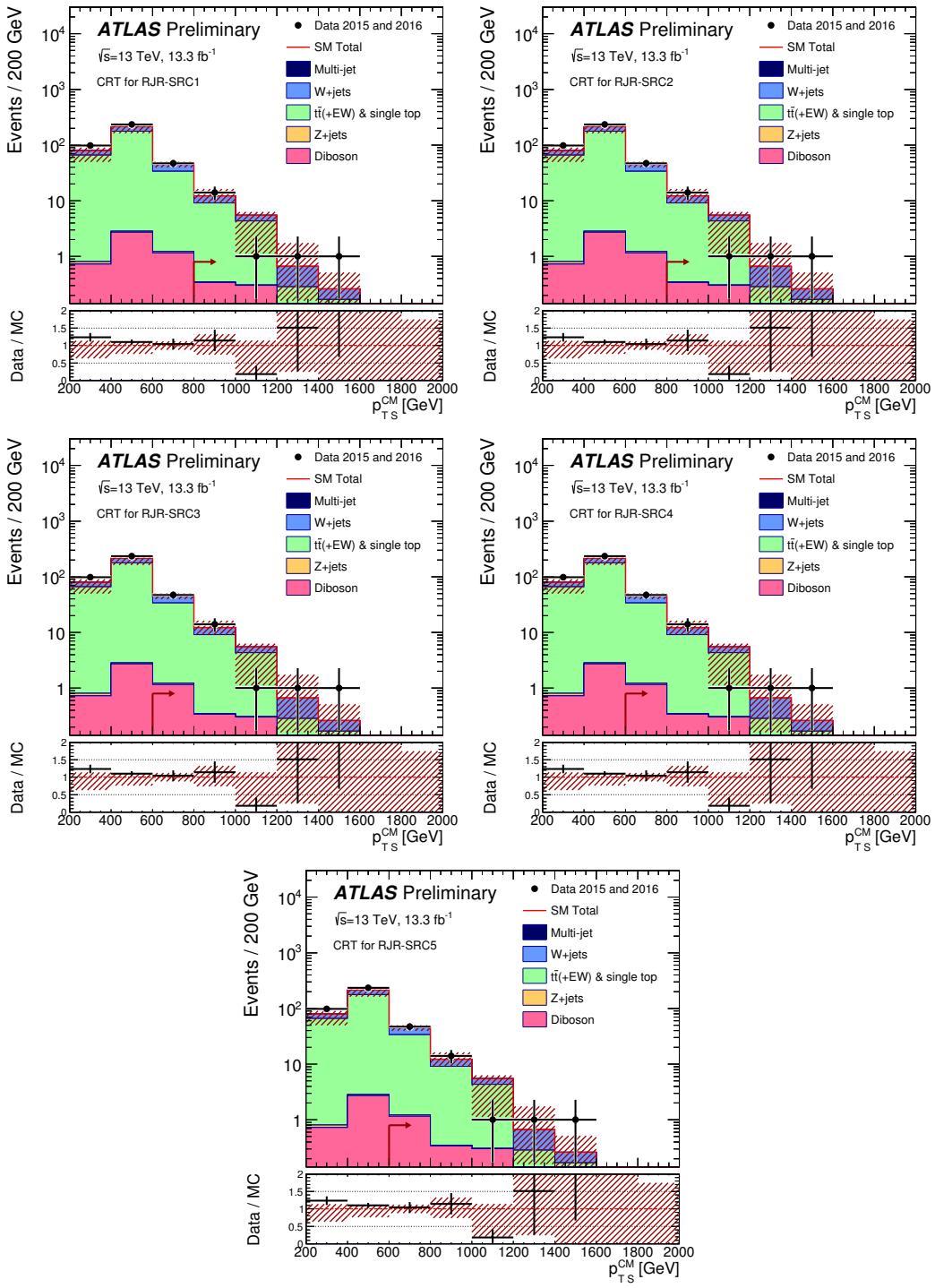


Figure 8.10: Scale variable distributions for the compressed CRT regions.

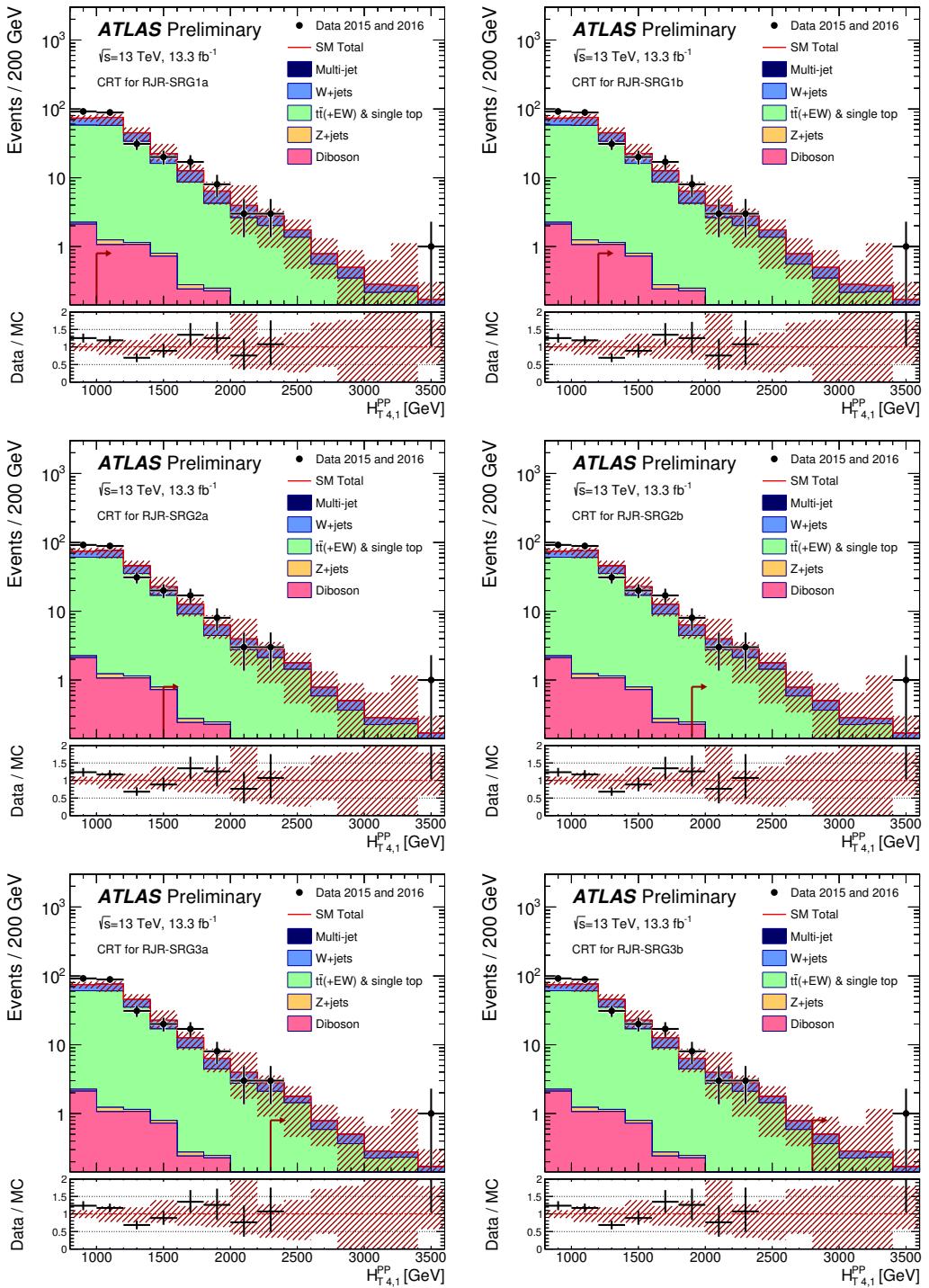


Figure 8.11: Scale variable distributions for the gluino CRT regions.

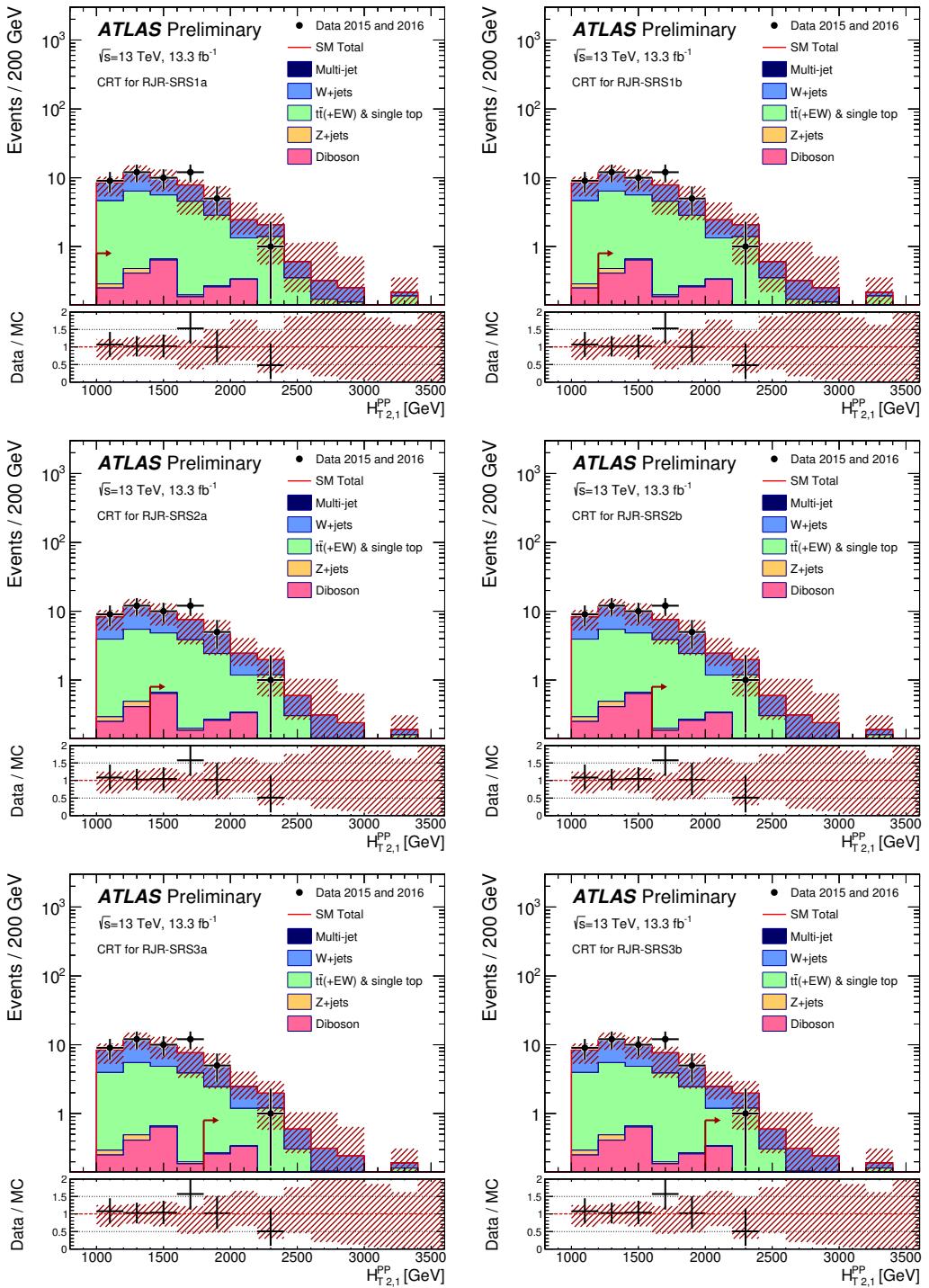


Figure 8.12: Scale variable distributions for the squark CRT regions.

2036 **Validation Regions**

2037 As discussed in general terms above, we define a set of validation regions to ensure  
2038 we can properly model the particular backgrounds as we move closer to the SRs in  
2039 phase space. We define at least one validation region for each major background.

2040 For the most important background  $Z \rightarrow \nu\nu$ , we use a series of validation regions.  
2041 The primary validation region, which we label as VRZ, is defined by selecting lepton  
2042 pairs of opposite sign and identical flavor which lie within  $\pm 25$  GeV of the Z boson mass.  
2043 This selection has high purity for  $Z \rightarrow \ell\ell$  events as seen in simulation. We treat the  
2044 two leptons as contributions to the  $E_T^{\text{miss}}$  (as we did with the photon in CRY). This  
2045 selection uses the same kinematic cuts as the signal region. We also define two VRs  
2046 using the same event selection but looser kinematic cuts, which we label VRZa and  
2047 VRZb. VRZa has a loosened selection on  $H_{1,1}^{PP}$ , again to the loosest value among the  
2048 signal regions, as was done for CRW and CRt. VRZa has a loosened selection on  
2049 the primary scaleful variable ( $H_{T,2,1}^{PP}$  or  $H_{T,4,1}^{PP}$ ), again to the loosest value among the  
2050 signal regions, as was done for CRW and CRT. These two validation regions allow us  
2051 to test the modeling of each of these variables individually, as well as allowing more  
2052 validation region statistics in the signal regions with tighter cuts on these variables.

2053 For the compressed regions, these  $Z$  validation region were found lacking. The  
2054 leptons are highly boosted in the compressed case, and the lepton acceptance was  
2055 quite low due to lepton isolation requirements in  $\Delta R$ . Instead, two fully hadronic  
2056 validation region were developed for the compressed regions. The first, VRZc has  
2057 identical requirements to the signal regions with an inverted requirement on  $\Delta\phi_{ISR,I}$ .  
2058 From simulation, this region was found to be at least 50% pure in  $Z$  events, which  
2059 was considered enough to validate this background in this extreme portion of phase  
2060 space. For additional validation region statistics, we also developed VRZca, which  
2061 takes again uses the loosest set of cuts from each signal region. Note this means that  
2062 each compressed signal region has an identical VRZca.

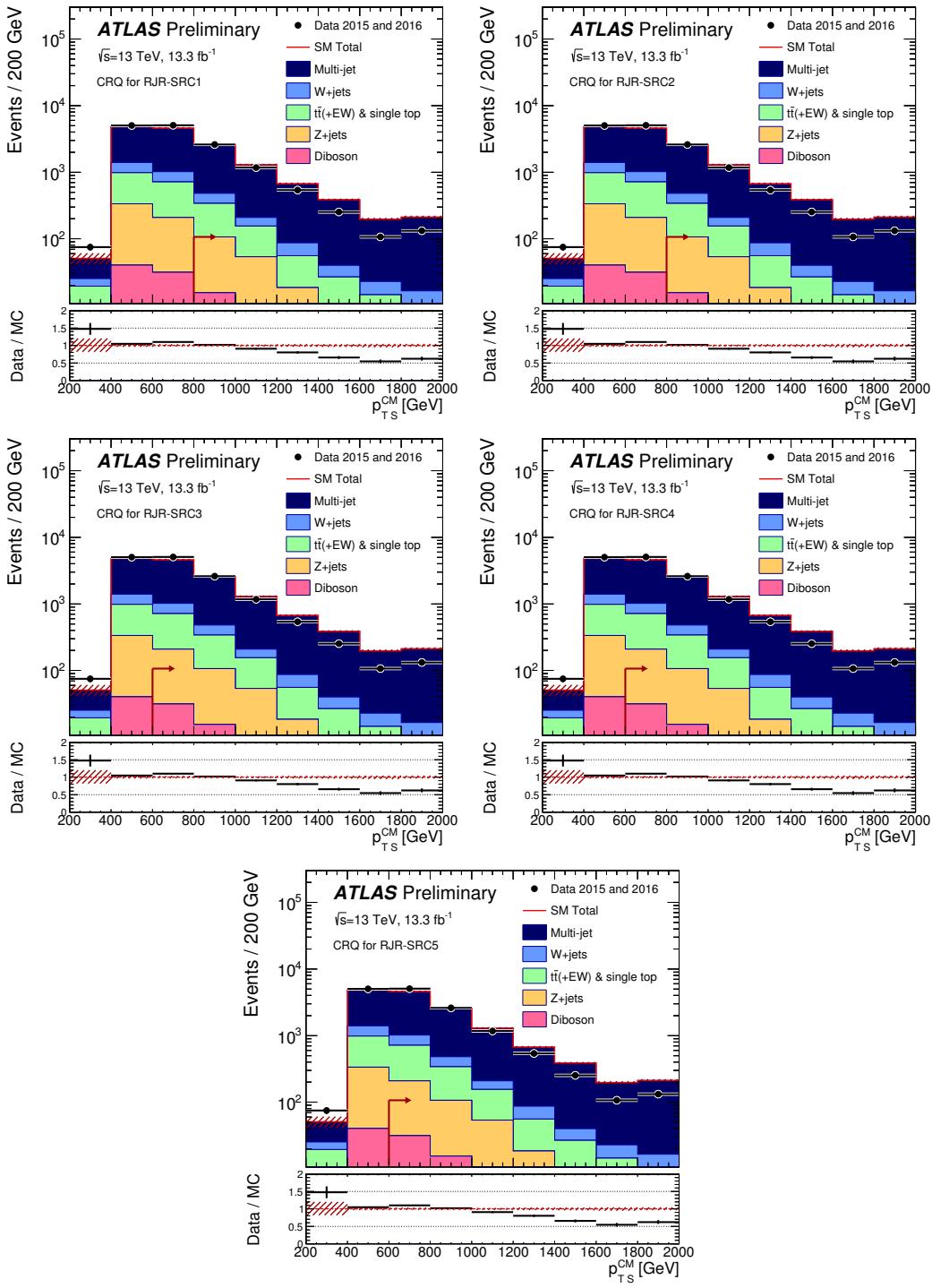


Figure 8.13: Scale variable distributions for the compressed CRQ regions.

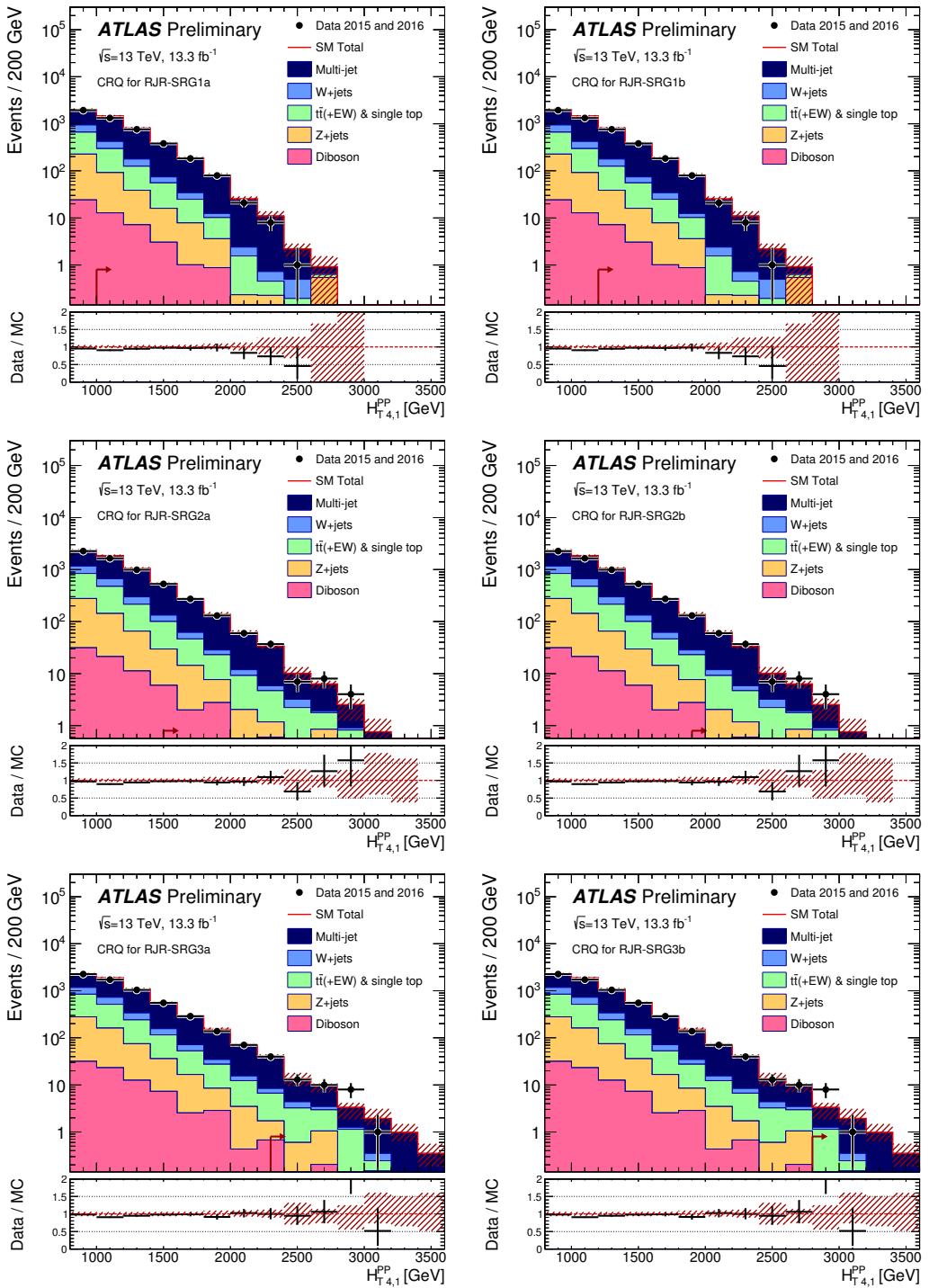


Figure 8.14: Scale variable distributions for the gluino CRQ regions.

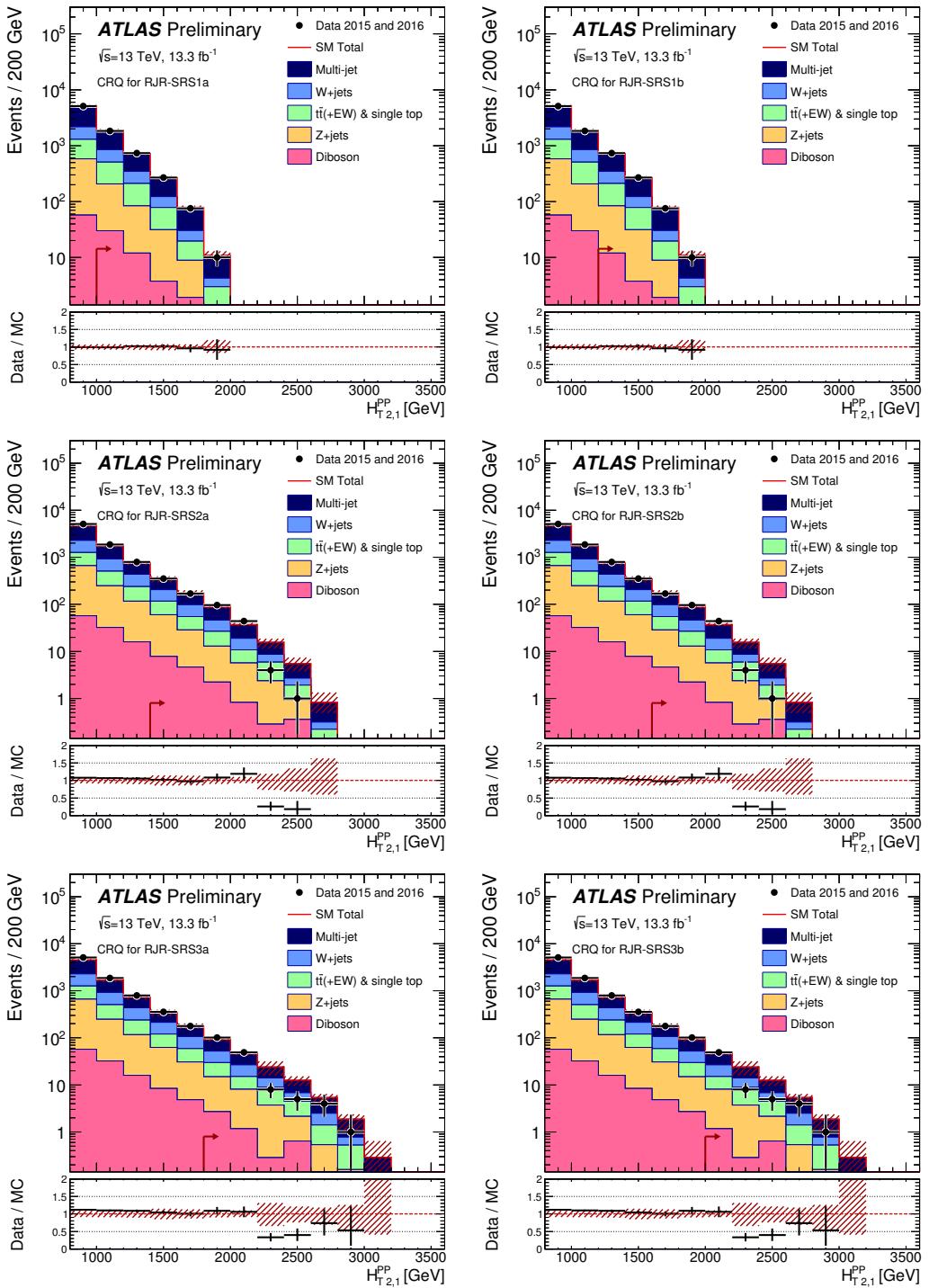


Figure 8.15: Scale variable distributions for the squark CRQ regions.

2063        The top and  $W$  validation regions use the same event selection as the correspond-  
 2064        ing control regions, as described above. However, unlike the control regions, these  
 2065        validation regions reimpose the SR scaleful variable selections, to be closer in phase  
 2066        space to the hadronic signal regions. In the same way as we did for VRZa and  
 2067        VRZb, we also define auxiliary VRs which loosen the cuts on the scale variables. We  
 2068        define VRTa (VRWa) as VRT (VRW) with the same loosened cut on  $H_{1,1}^{PP}$  and VRTb  
 2069        (VRWb) as VRT (VRW) with the same loosened cut on the primary scale variable.

2070        The final set of validation regions are those defined to check the estimation of  
 2071        the QCD background. VRQ is defined to be identical to the corresponding CRQ,  
 2072        but again we use the full SR region cuts for the scaleful variables. This selection is  
 2073        then closer to the corresponding signal region to validate the CRQ estimate. We also  
 2074        define the auxiliary validation regions VRQa and VRQb for the noncompressed signal  
 2075        regions. In this case, we reimpose one of the two inverted cuts in CRQ with respect  
 2076        to the signal regions, to make each one even closer to the SRs. In CRQa (CRQb), we  
 2077        reimpose the  $H_{1,1}^{PP}$  ( $\Delta_{\text{QCD}}$ ).

2078        For the compressed case, we again define a separate validation region, due to  
 2079        the special kinematics probed. We construct a validation region which is the same as  
 2080        CRQ, with  $.5 < R_{\text{ISR}} < R_{\text{ISR, SR}}$ , where  $R_{\text{ISR, SR}}$  is the cut on  $R_{\text{ISR}}$  in the corresponding  
 2081        SR. Again, this can be seen as probing “in between” the CR and SR in phase space.

The results of this validation can be seen in 8.16. Each bin is *pull* of the validation  
 region corresponding to a particular signal region. This is defined

$$\text{Pull} = \frac{N_{\text{obs}} - N_{\text{pred}}}{\sigma_{\text{tot}}} \quad (8.4)$$

2082        where  $\sigma_{\text{tot}}$  is the total uncertainty folding in all systematic uncertainties, which we  
 2083        will describe later. Assuming we have well-measured our backgrounds, we expect a  
 2084        Gaussian distribution of the pulls around 0, with a standard deviation of 1, as this  
 2085        is measuring the number of standard deviations around the mean. We can see there  
 2086        are few positive pulls (indicating an underestimation of the background), indicating

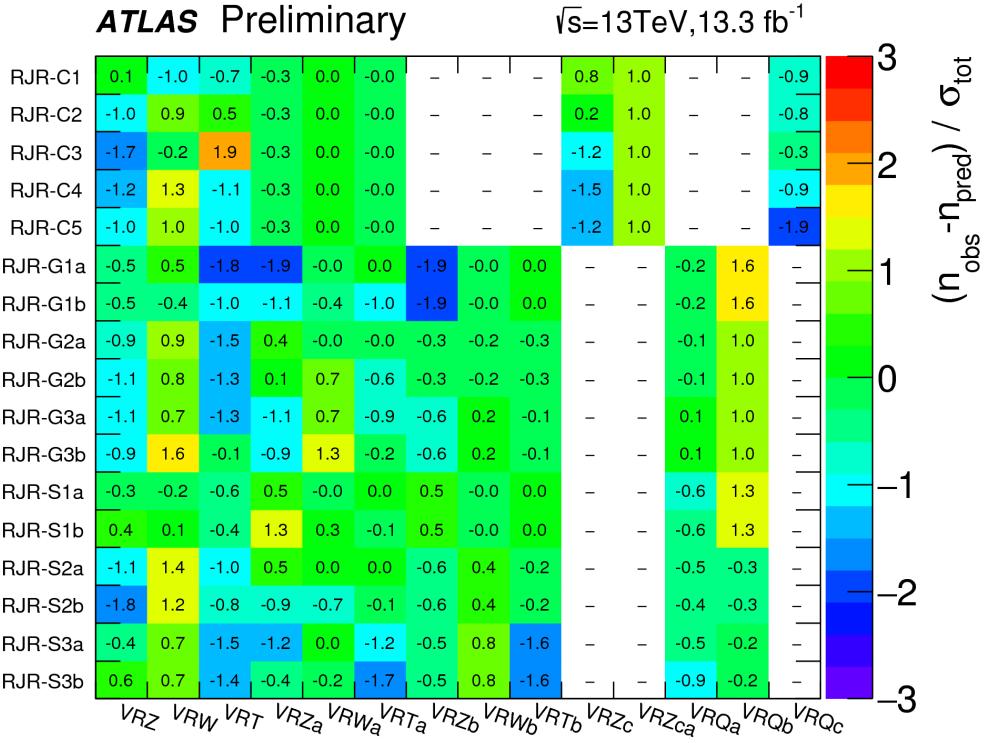


Figure 8.16: Summary of the validation region pulls

2087 we have conservatively measured the Standard Model backgrounds with our control  
 2088 regions.

## 2089 Systematic Uncertainties

2090 In this section, we discuss the uncertainties considered. These generally fall into  
 2091 four categories: theoretical generator uncertainties, uncertainties on the CR to SR  
 2092 extrapolations, uncertainties on the data-driven transfer factor corrections, and object  
 2093 reconstruction uncertainties. We discuss each of these categories here. A table  
 2094 summarizing this section is in 8.5

Systematic	Uncertainty Description
alpha_GeneratorZ	Theoretical on $Z$ cross-section
alpha_generatorW	Theoretical on $W$ cross-section
alpha_generatorTop	Theoretical on $t$ cross-section
alpha_radiationTop	Theoretical on $t$ radiation tune
alpha_Pythia8Top	Theoretical on $t$ fragmentation tune
alpha_FlatDiboson	Flat on diboson cross-section
mu_Zjets	CRY extrapolation to SR
mu_Wjets	CRW extrapolation to SR
mu_Top	CRT extrapolation to SR
mu_Multijets	CRQ extrapolation to SR
alpha_Kappa	$\kappa$ factor
alpha_QCDError	Jet smearing
alpha_JET_GroupedNP_1	JES NP group 1
alpha_JET_GroupedNP_2	JES NP group 2
alpha_JET_GroupedNP_3	JES NP group 3
alpha_JER	JER
alpha_MET_SoftTrk_ResoPerp	Soft $E_T^{\text{miss}}$ resolution perpendicular to hard object system
alpha_MET_SoftTrk_ResoPara	Soft $E_T^{\text{miss}}$ resolution parallel to hard object system
alpha_MET_SoftTrk_Scale	Soft $E_T^{\text{miss}}$ scale

Table 8.5: Description of the systematic uncertainties in the analysis.

2095        The theoretical generator uncertainties are evaluated by using alternative sim-  
 2096 ulation samples or varying scale uncertainties. In the case of the  $Z+jets$  and  
 2097  $W+jets$  backgrounds, the related theoretical uncertainties are estimated by varying  
 2098 the renormalization, factorization, and resummation scales by two, and decreasing  
 2099 the nominal CKKW matching scale by 5 GeV and 10 GeV respectively. In  
 2100 the case of  $t\bar{t}$  production, we compare the nominal POWHEG-Box generator with  
 2101 MG5\_aMC@NLO, as well as comparing different radiation and generator tunes. As  
 2102 stated above, we account for the uncertainty on the small diboson background by  
 2103 imposition of a flat 50% uncertainty.

2104        The CR to SR extrapolation uncertainties, or what could be called the transfer

2105 factor uncertainties, are listed in 8.5 as  $\mu_-$ . There is one normalization factor  $\mu$  for  
2106 each major background, and their uncertainties, especially  $\mu_Z$ , are often dominant  
2107 for the measurement in many signal regions. This uncertainty is generally dominated  
2108 by the statistical uncertainty in the CR.

2109 There are two uncertainties from the data-driven corrections to the transfer  
2110 factors. The first is the uncertainty on  $\kappa$ , which is measured using an auxiliary  $Z \rightarrow \ell\ell$   
2111 control region. This is labeled alpha\_Kappa. The other is the uncertainty is that  
2112 assigned to the jet smearing method, which is seen in the table as alpha\_QCDError.

2113 The final set of uncertainties are those related to object reconstruction. In the  
2114 case of the hadronic search presented, the important uncertainties are those assigned  
2115 to the jet energy and  $E_T^{\text{miss}}$ . The uncertainties on the lepton reconstruction and  
2116  $b$ -tagging uncertainties were found to be negligible in all SRs. The measurement  
2117 of the jet energy scale (JES) uncertainty is quite complicated, and described in  
2118 [Aad:2011he, Aad:2012vm, 127]. After a complicated procedure to decorrelate  
2119 the various components of the JES uncertainty, there are three components which  
2120 remain, which are labeled as alpha\_JET\_GroupedNP\_1,2,3. The jet energy resolution  
2121 uncertainty is estimated using the methods discussed in Refs. [Aad:2012ag, 127],  
2122 and is labeled alpha\_JER.

2123 The  $E_T^{\text{miss}}$  soft term uncertainties are described in [112, 113, 128]. The  
2124 uncertainty on the  $E_T^{\text{miss}}$  soft term resolution is parameterized into a component  
2125 parallel to direction of the rest of the event (the sum of the hard objects  $p_T$ )  
2126 and a component perpendicular to this direction. There is also an uncertainty  
2127 on the  $E_T^{\text{miss}}$  soft term scale. These are labeled as alpha\_MET\_SoftTrk\_ResoPara,  
2128 alpha\_MET\_SoftTrk\_ResoPerp, and alpha\_MET\_SoftTrk\_Scale.

2129 **Fitting procedure**

2130 In this section, we describe the fitting procedure employed, which properly accounts  
2131 for the correlations between the uncertainties through the use of a likelihood fit  
2132 as described in [120]. We use three classes of likelihood fits: *background-only*,  
2133 *model-independent*, and *model-dependent* fits. The background-only fits estimate the  
2134 background yields in each signal region. These fits use only the control region event  
2135 yields as inputs; they do not include the information from the signal regions besides  
2136 the simulation event yield. The cross-contamination between CRs is also fit by this  
2137 procedure. The systematic uncertainties described in the previous section are used as  
2138 nuisance parameters. This background only fit also estimates the background event  
2139 yields in the validation regions. When designing the analysis (before unblinding  
2140 the signal regions), checking the validation region agreement is the primary way to  
2141 validate the consistency and accuracy of the background estimation procedure.

2142 In the case no excess is observed, we use a model-independent fit to set upper  
2143 limits on the possible number of possible beyond the Standard Model events in each  
2144 SR. The fitting procedure has one difference from the background-only fit: we add  
2145 the number of observed events as an input to the fit, and we fit the signal strength as  
2146 a new non-negative free parameter. Using the  $CL_s$  procedure[129] and neglecting the  
2147 possible (small) signal contamination in control regions, we derive the the observed  
2148 and expected limits on the number of events from BSM phenomena in each signal  
2149 region.

2150 Model-dependent fits are used to set exclusion limits on the specific SUSY  
2151 models considered in this thesis, particular the gluino or squark pair production  
2152 with various mass splittings. This can be seen as identical to the background-only  
2153 fit with an additional simulation input from the particular model of interest, with its  
2154 corresponding systematic uncertainties from detector effects accounted for as in the  
2155 background-only fit. As noted when we introduced 8.1, the exclusion contours from

2156 previous model-dependent fits are the primary motivating factor in the design of our  
2157 signal regions. If no excess is found, we set limits on each of the simplified signal  
2158 models with various mass splittings.



*Title of Chapter 1*

2161 This chapter presents the results of the analysis presented in the previous chapter.  
2162 We present the full set of signal region distributions after applying the  $\mu$  factors  
2163 derived from the fitting procedure. We also present the systematic uncertainties in  
2164 each signal region properly accounting for the correlations of the uncertainties. As  
2165 no excess is observed, we show exclusion limits in the sparticle- $\tilde{\chi}_1^0$  plane based on the  
2166 results of the model-dependent fits and present the model-independent limits.

2167 **9.1 Signal region distributions**

2168 In ??, we can see the unblinded distributions of the last scale cut used for each  
2169 signal region. These distributions include the  $\mu$  scale factors as well as the systematic  
2170 uncertainties after the fitting procedure. Each plot shows the distribution from a  
2171 signal model which is targetted by the given signal region.

2172 These distributions have all cuts applied except for the cut on this scale variable,  
2173 which allows us to see the additional discrimination provided by the given variable.  
2174 Since signal regions with the same numeral have identical cuts on all cuts other than  
2175 the main scale variable, we show (a) and (b) on the same figure. The left-most (right-  
2176 most) arrow shown is the location of the a (b) cut applied in the analysis. We call  
2177 these plots  $N - 1$  plots, where  $N$  refers to the number of cuts applied in the analysis.  
2178 The full set of  $N - 1$  plots in the signal regions for the other variables used in the  
2179 analysis are shown in 9.4.

2180 A figure showing a summary of the pulls in all of the SRs is shown in 9.4. This  
2181 figure shows the integrated data and simulation values above the cut values in the N-1  
2182 plots, with the corresponding statistical and systematic uncertainties, for all signal  
2183 regions simultaneously. The systematic uncertainties will be discussed in the next  
2184 section. From this plot, we can see there is no significant excess of events over the  
2185 Standard Model background.

2186 This information is also presented in 9.1. The table includes the expectations  
2187 from simulation before applying the  $\mu$  scaling factor. SRG3b shows a small excess,  
2188 but this is not significant.

2189 In this case, we set both simplified model-dependent limits and model-independent  
2190 limits on the possible cross-sections from BSM physics.

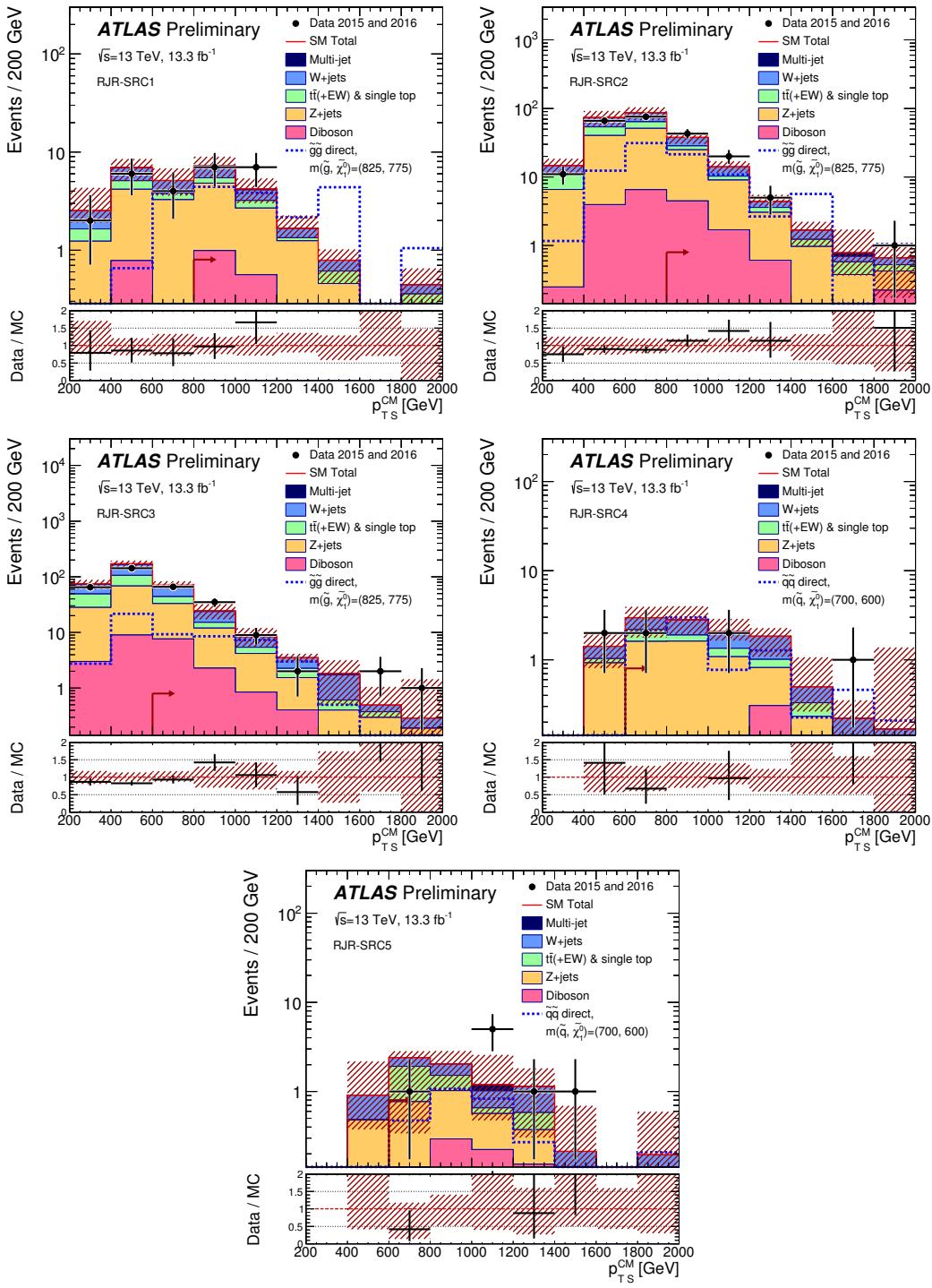


Figure 9.1: Scale variable distributions for the compressed signal regions.

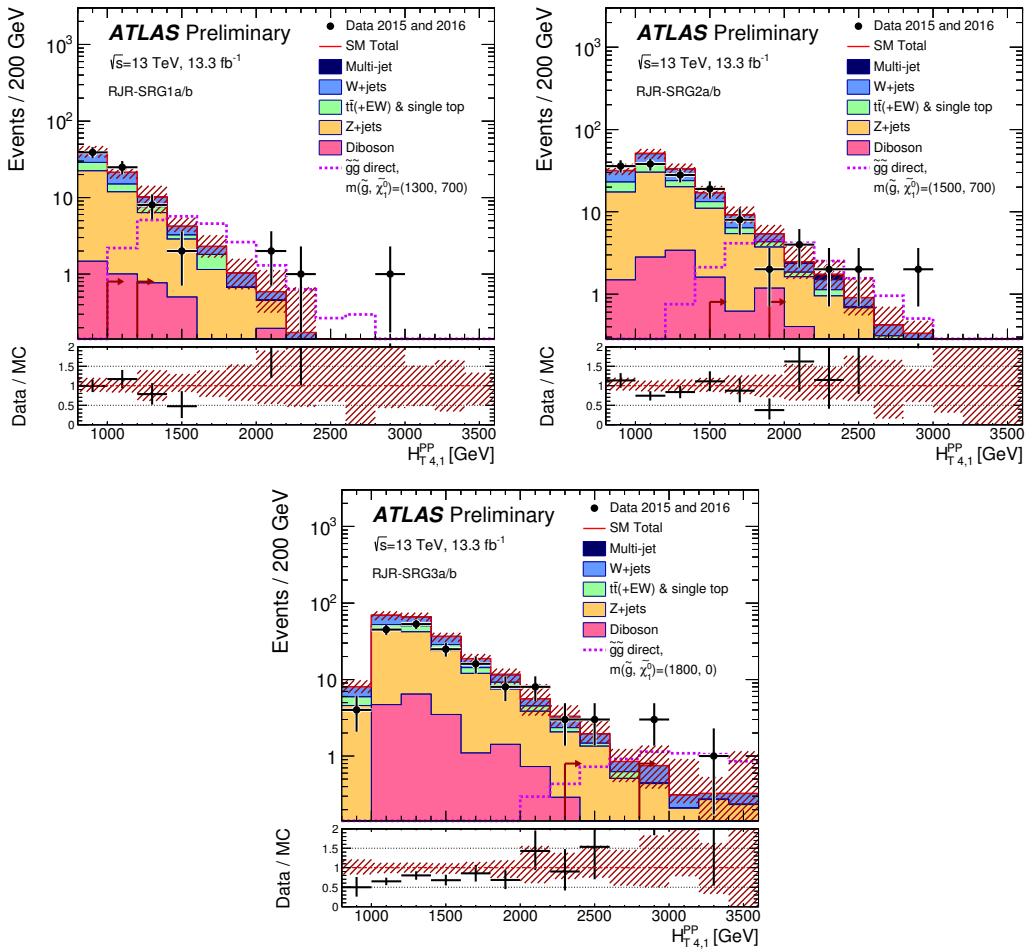


Figure 9.2: Scale variable distributions for the gluino signal regions.

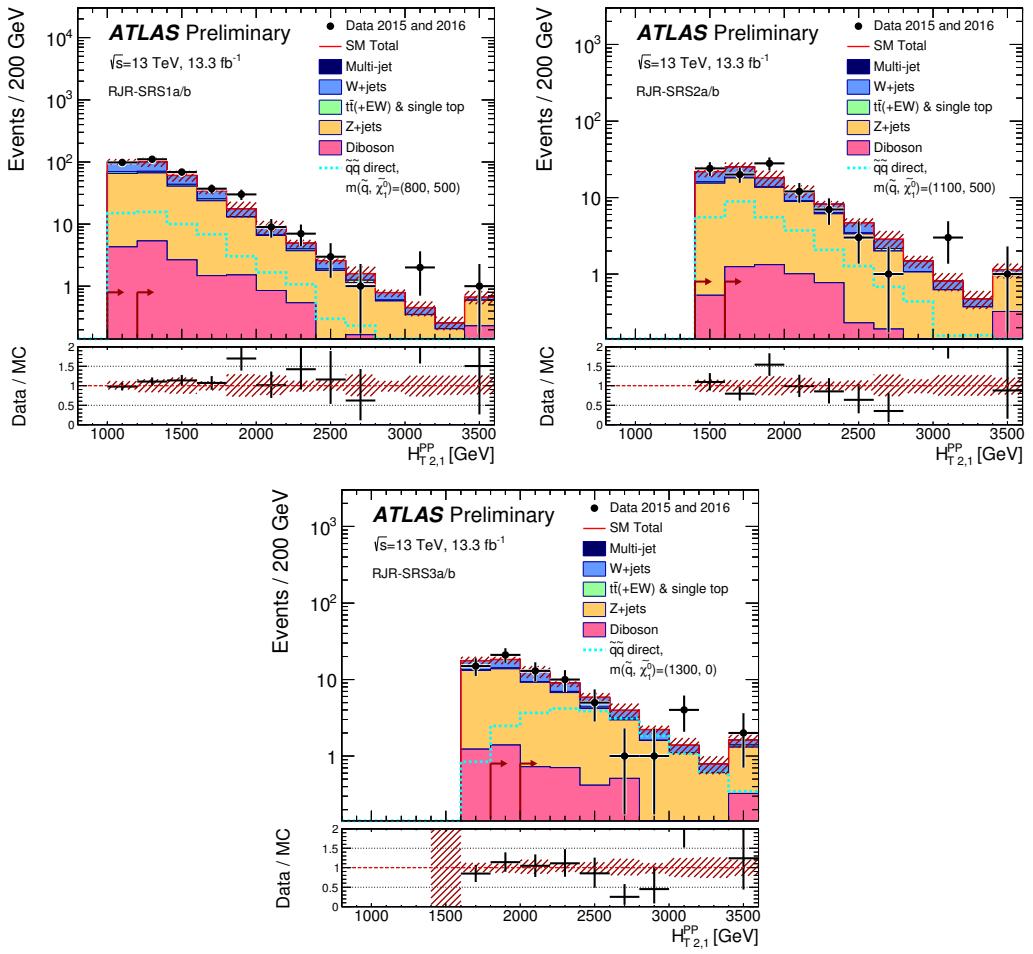


Figure 9.3: Scale variable distributions for the squark signal regions.

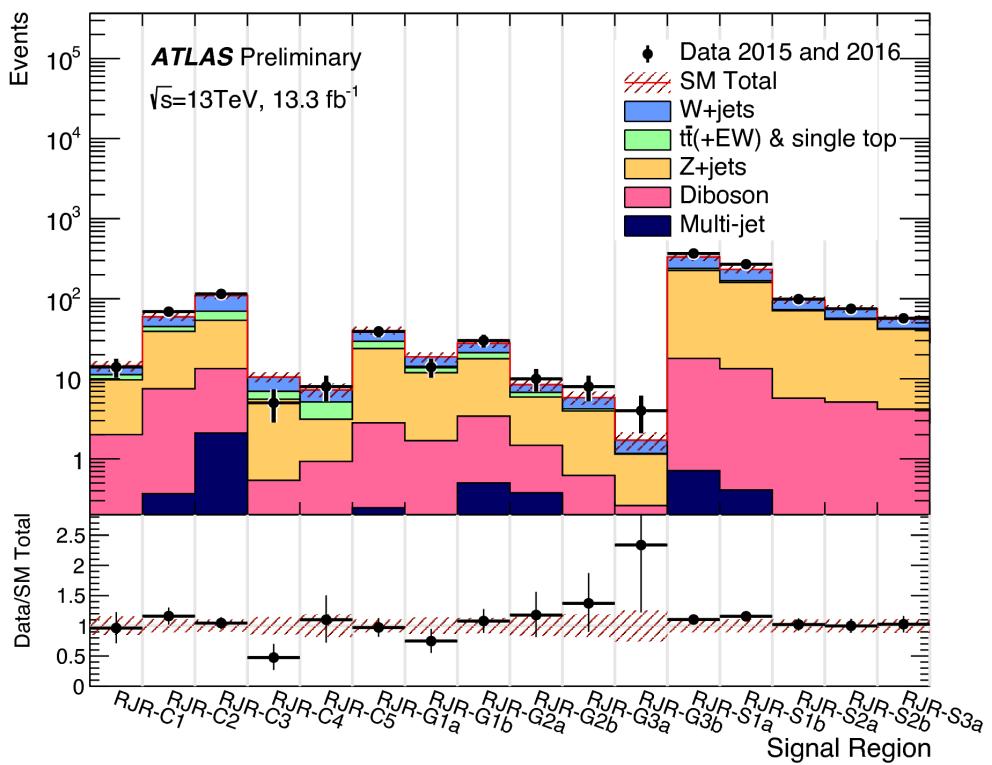


Figure 9.4: Summary of the signal region pulls



Signal Region	RJR-S1a	RJR-S1b	RJR-S2a	RJR-S2b	RJR-S3a	RJR-S3b
MC expected events						
Diboson	17	13	5.6	5.1	4.2	2.8
Z/ $\gamma^*$ +jets	231	163	63	48	36	24
W+jets	97	66	22	16	11	7.8
t $\bar{t}$ (+EW) + single top	15	10	2.9	2.1	1.7	1.1
Fitted background events						
Diboson	17 $\pm$ 9	13 $\pm$ 7	5.6 $\pm$ 2.8	5.1 $\pm$ 2.6	4.2 $\pm$ 2.1	2.8 $\pm$ 1.4
Z/ $\gamma^*$ +jets	207 $\pm$ 33	146 $\pm$ 23	65 $\pm$ 9	50 $\pm$ 7	37 $\pm$ 5	25.0 $\pm$ 3.5
W+jets	95 $\pm$ 9	65 $\pm$ 7	24.1 $\pm$ 2.9	18.3 $\pm$ 2.3	12.8 $\pm$ 2.8	8.7 $\pm$ 2.0
t $\bar{t}$ (+EW) + single top	14 $\pm$ 7	9 $\pm$ 5	2.1 $\pm$ 1.7	1.6 $\pm$ 1.3	1.3 $\pm$ 1.0	0.8 $\pm$ 0.7
Multi-jet	0.71 <sup>+0.71</sup> <sub>-0.71</sub>	0.41 <sup>+0.41</sup> <sub>-0.41</sub>	0.08 <sup>+0.09</sup> <sub>-0.08</sub>	—	—	—
Total Expected MC	362	253	93	72	53	36
Total Fitted bkg	334 $\pm$ 35	233 $\pm$ 25	96 $\pm$ 10	75 $\pm$ 8	56 $\pm$ 6	37 $\pm$ 4
Observed	368	270	99	75	57	36
$\langle\epsilon\sigma\rangle_{\text{obs}}^{95}$ [fb]	7.6	6.5	2.2	1.7	1.6	1.1
$S_{\text{obs}}^{95}$	101	86	29	23	22	15
$S_{\text{exp}}^{95}$	78 <sup>+27</sup> <sub>-21</sub>	61 <sup>+22</sup> <sub>-16</sub>	28 <sup>+11</sup> <sub>-8</sub>	23 <sup>+9</sup> <sub>-7</sub>	20 <sup>+8</sup> <sub>-6</sub>	16 <sup>+7</sup> <sub>-5</sub>
$p_0$ (Z)	0.20 (0.84)	0.12 (1.17)	0.44 (0.15)	0.50 (0.00)	0.44 (0.14)	0.50 (0.00)

Signal Region	RJR-G1a	RJR-G1b	RJR-G2a	RJR-G2b	RJR-G3a	RJR-G3b
MC expected events						
Diboson	2.6	1.6	2.9	1.1	0.62	0.26
Z/ $\gamma^*$ +jets	18	8.8	13	4.2	3.1	0.83
W+jets	11	4.7	7.7	2.0	1.9	0.63
t $\bar{t}$ (+EW) + single top	7.4	3.1	4.4	1.1	0.34	0.03
Fitted background events						
Diboson	2.6 $\pm$ 1.3	1.6 $\pm$ 0.8	2.9 $\pm$ 1.5	1.1 $\pm$ 0.6	0.6 $\pm$ 0.4	0.26 $\pm$ 0.14
Z/ $\gamma^*$ +jets	21.1 $\pm$ 3.1	10.2 $\pm$ 1.6	14.3 $\pm$ 2.5	4.5 $\pm$ 0.8	3.3 $\pm$ 0.6	0.88 $\pm$ 0.19
W+jets	10.8 $\pm$ 1.7	4.6 $\pm$ 1.4	6.7 $\pm$ 1.3	1.7 $\pm$ 0.7	1.6 $\pm$ 0.7	0.55 $\pm$ 0.2
t $\bar{t}$ (+EW) + single top	5.4 $\pm$ 1.6	2.3 $\pm$ 0.9	3.4 $\pm$ 1.4	0.8 $\pm$ 0.5	0.26 <sup>+0.45</sup> <sub>-0.26</sub>	0.02 <sup>+0.26</sup> <sub>-0.02</sub>
Multi-jet	0.24 $\pm$ 0.24	0.12 $\pm$ 0.12	0.5 $\pm$ 0.5	0.4 $\pm$ 0.4	—	—
Total Expected MC	39	18	29	8.7	5.9	1.7
Total Fitted bkg	40 $\pm$ 4	18.8 $\pm$ 2.5	27.8 $\pm$ 3.4	8.5 $\pm$ 1.4	5.8 $\pm$ 1.1	1.7 $\pm$ 0.4
Observed	39	14	30	10	8	4
$\langle\epsilon\sigma\rangle_{\text{obs}}^{95}$ [fb]	1.1	0.56	1.1	0.71	0.64	0.55
$S_{\text{obs}}^{95}$	15	7.5	15	9.4	8.5	7.3
$S_{\text{exp}}^{95}$	16 <sup>+7</sup> <sub>-4</sub>	10 <sup>+5</sup> <sub>-3</sub>	14 <sup>+6</sup> <sub>-4</sub>	7.6 <sup>+3.5</sup> <sub>-2.0</sub>	7.0 <sup>+2.5</sup> <sub>-2.1</sub>	4.2 <sup>+1.9</sup> <sub>-0.5</sub>
$p_0$ (Z)	0.50 (0.00)	0.50 (0.00)	0.36 (0.35)	0.31 (0.50)	0.21 (0.81)	0.06 (1.55)

Signal Region	RJR-C1	RJR-C2	RJR-C3	RJR-C4	RJR-C5
MC expected events					
Diboson	1.9	7.1	11	0.54	0.75
Z/ $\gamma^*$ +jets	8.8	36	46	5.8	2.5
W+jets	3.5	16	43	3.8	2.3
t $\bar{t}$ (+EW) + single top	1.9	16 <sup>+8</sup> <sub>-7.2</sub>	20	1.7	2.5
Fitted background events					
Diboson	1.9 $\pm$ 1.0	7 $\pm$ 4	11 $\pm$ 6	0.54 $\pm$ 0.29	0.8 $\pm$ 0.5

2191 **9.2 Fitting procedure checks and systematic**

2192 **uncertainties**

2193 This section

2194 **9.3 Exclusion plots**

Figure 9.5: Exclus.



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2195

## *Conclusion*

2196 Here you can write some introductory remarks about your chapter. I like to give each  
2197 sentence its own line.

2198 When you need a new paragraph, just skip an extra line.

2199 **9.4 New Section**

2200 By using the asterisk to start a new section, I keep the section from appearing in the  
2201 table of contents. If you want your sections to be numbered and to appear in the  
2202 table of contents, remove the asterisk.



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2578

## *The Standard Model*

2579

2580 **Compressed region N-1 plots**

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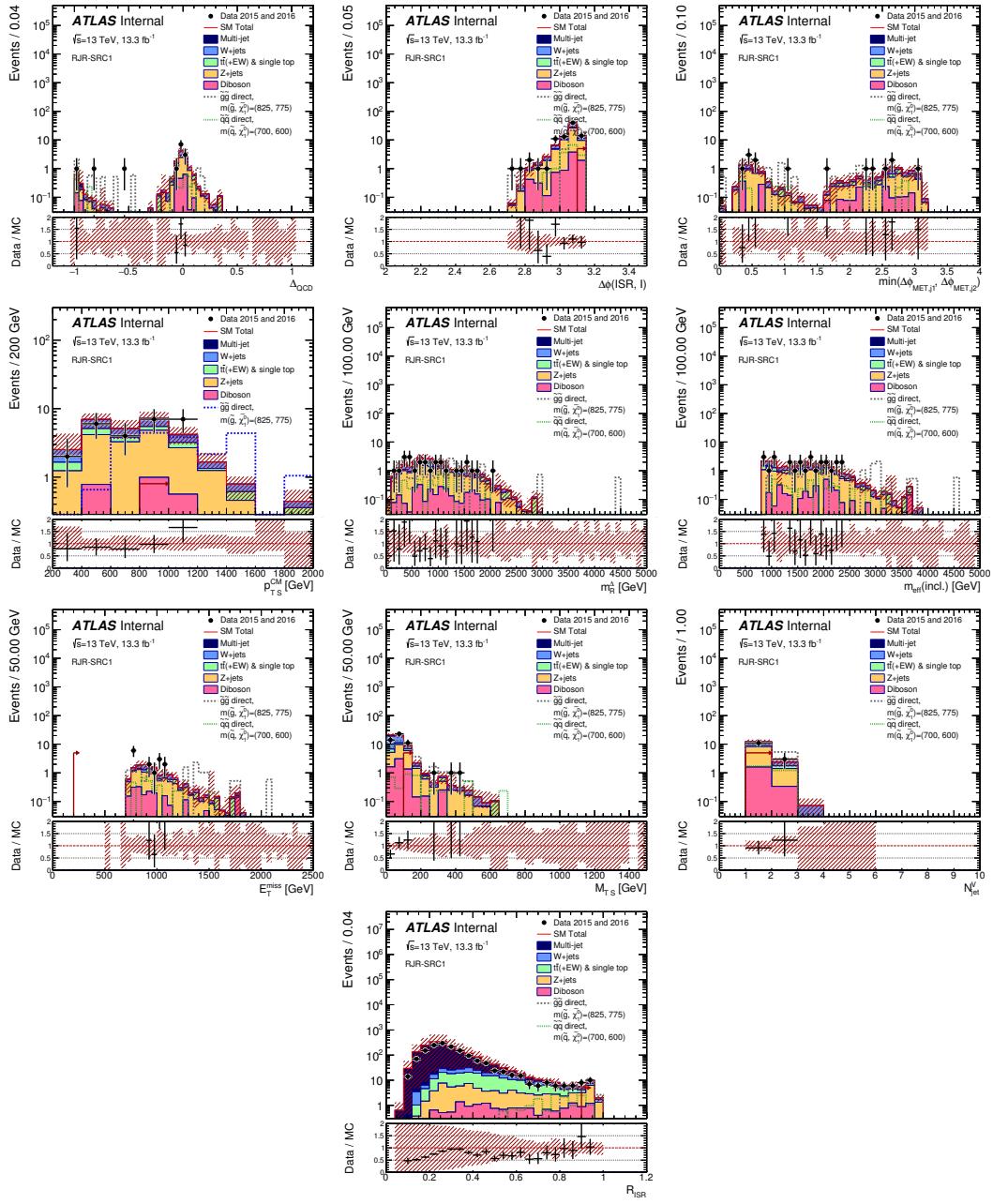


Figure 1

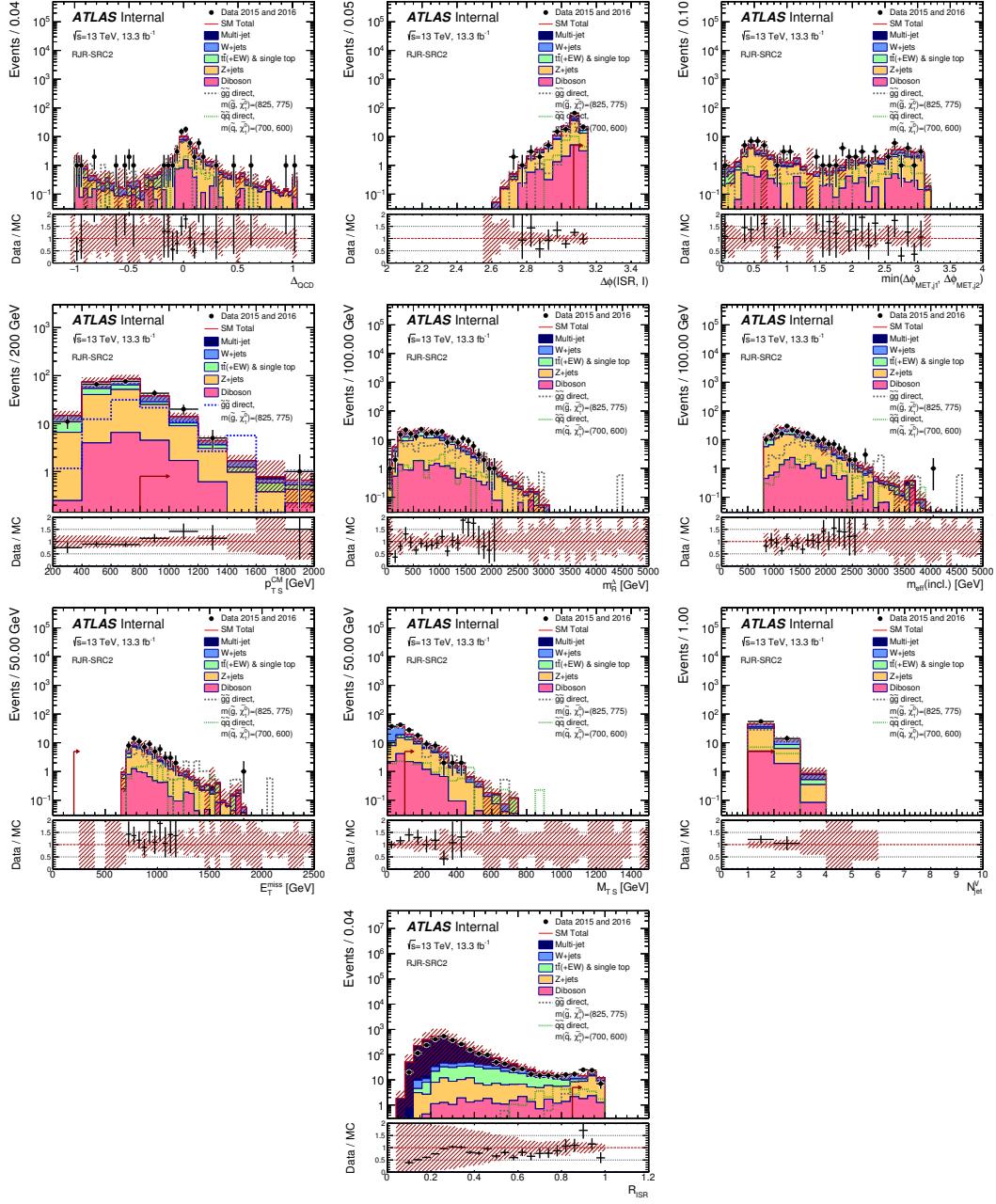


Figure 2

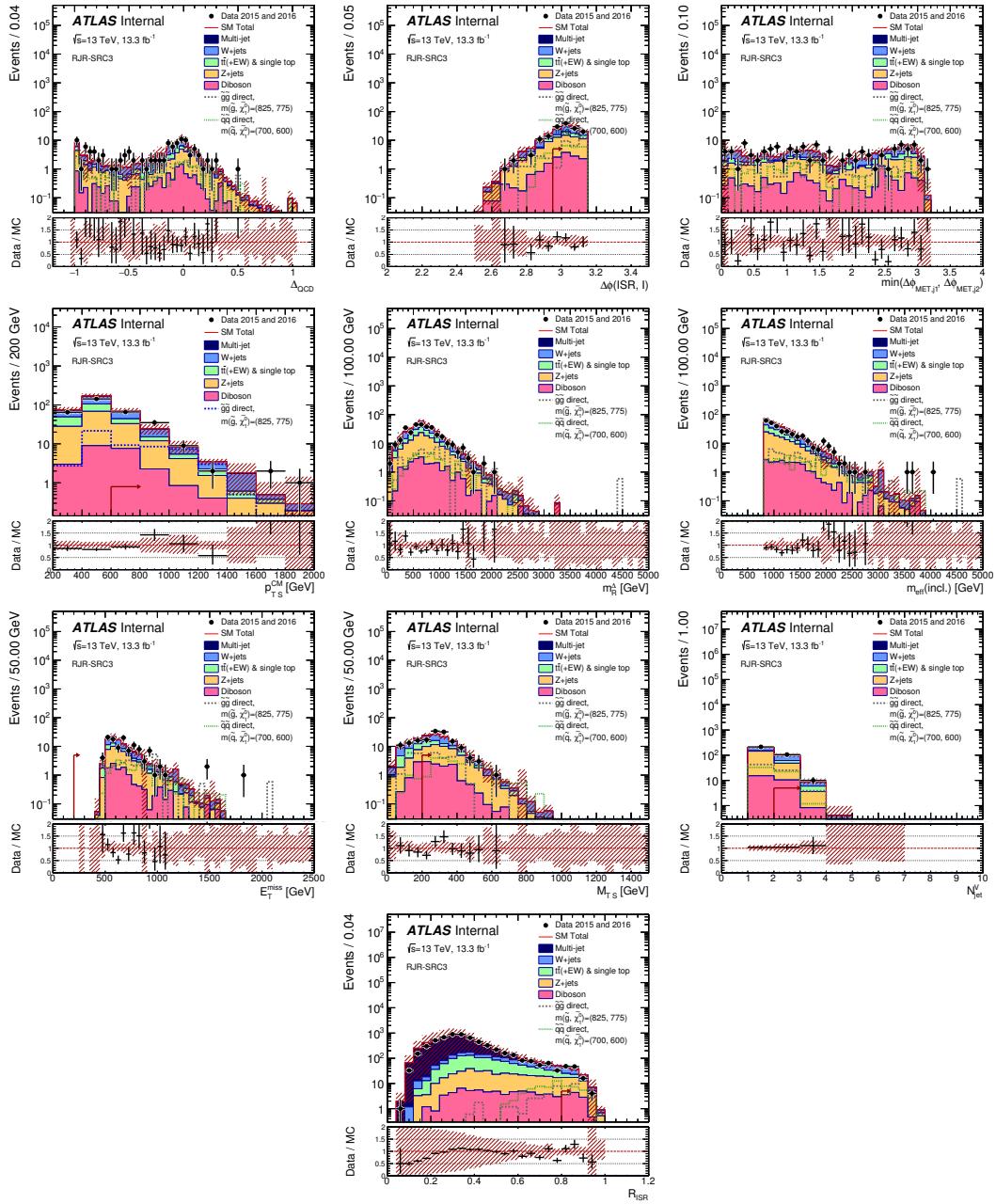


Figure 3

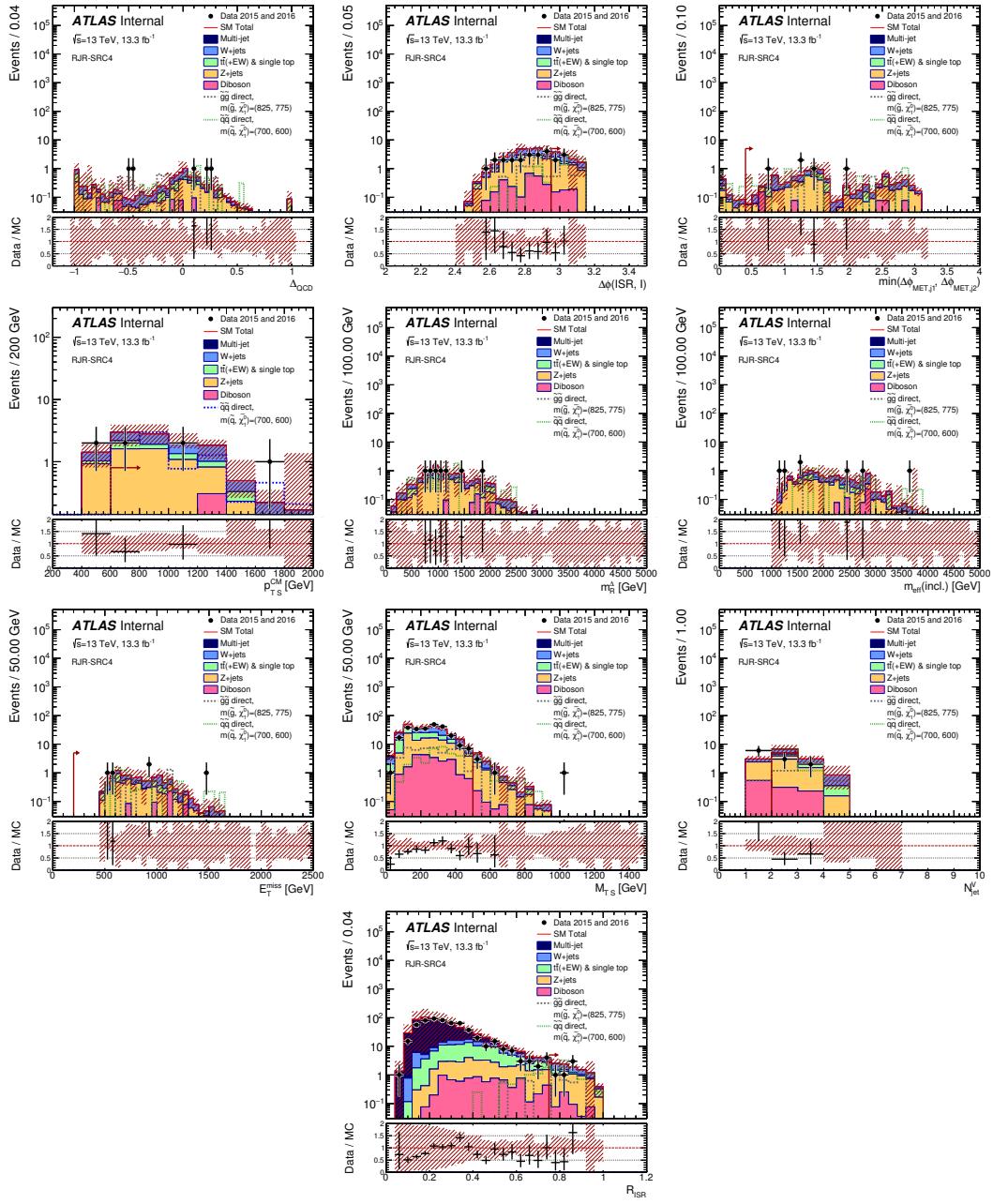


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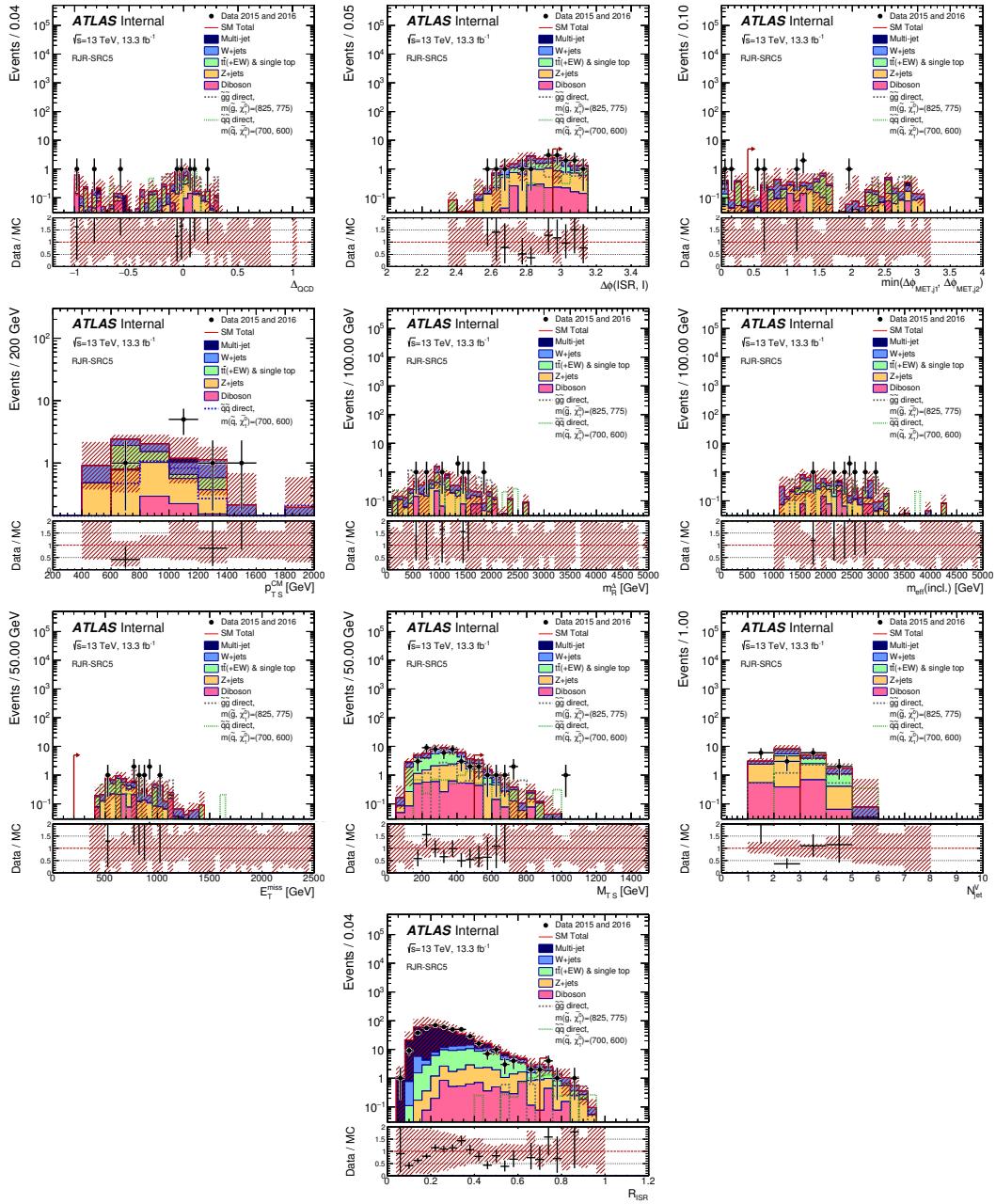


Figure 5

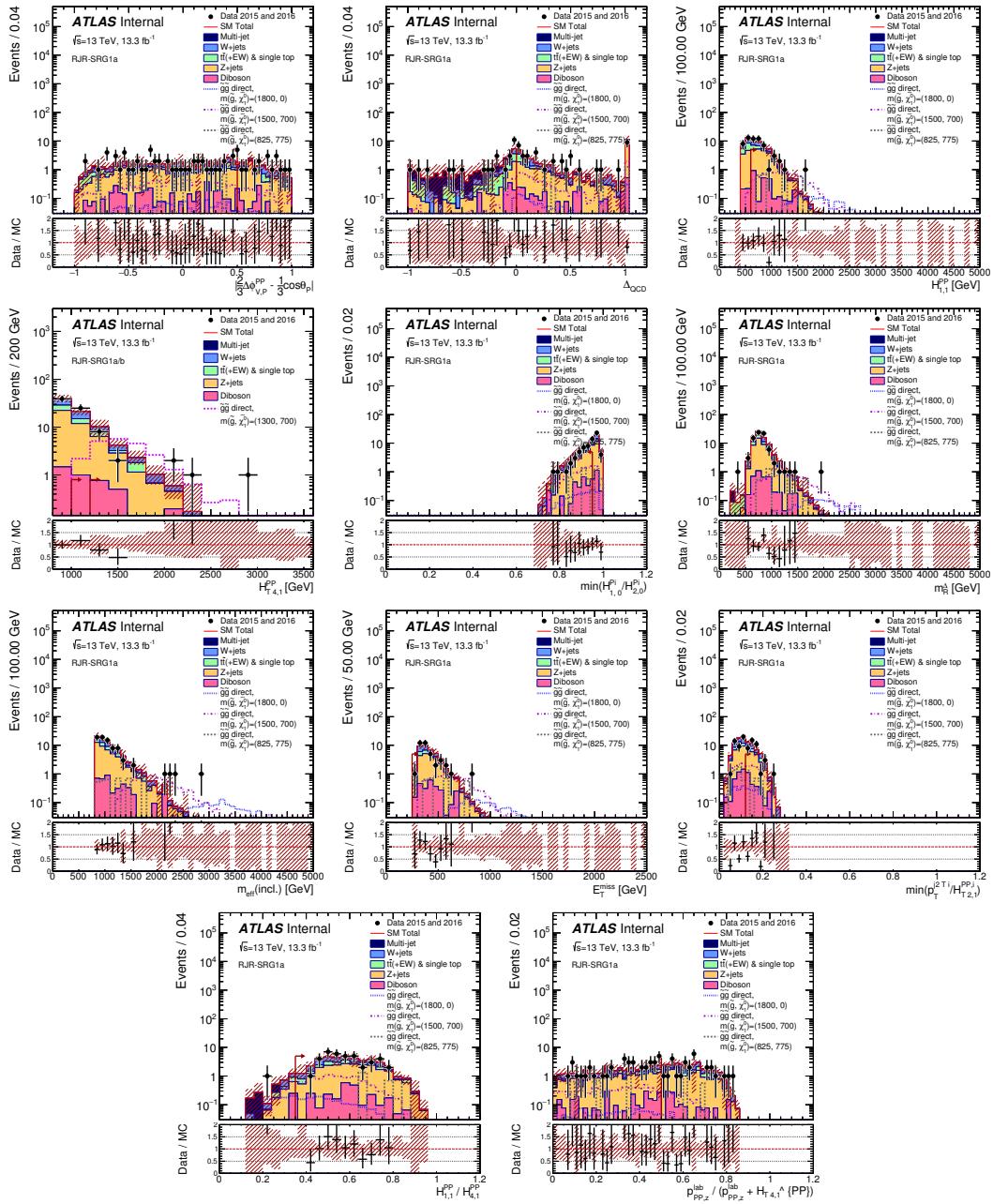


Figure 6

Figure 7

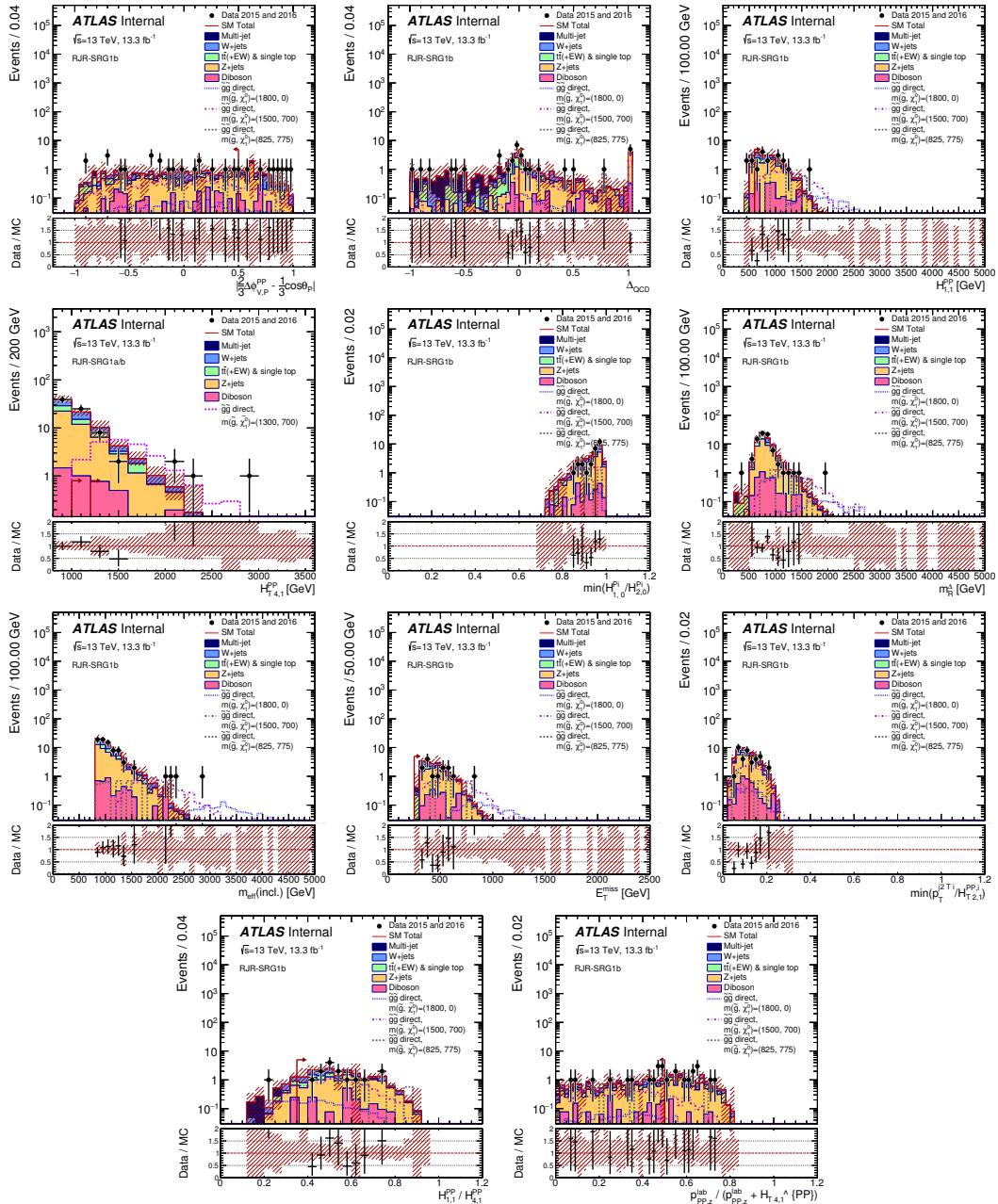


Figure 8

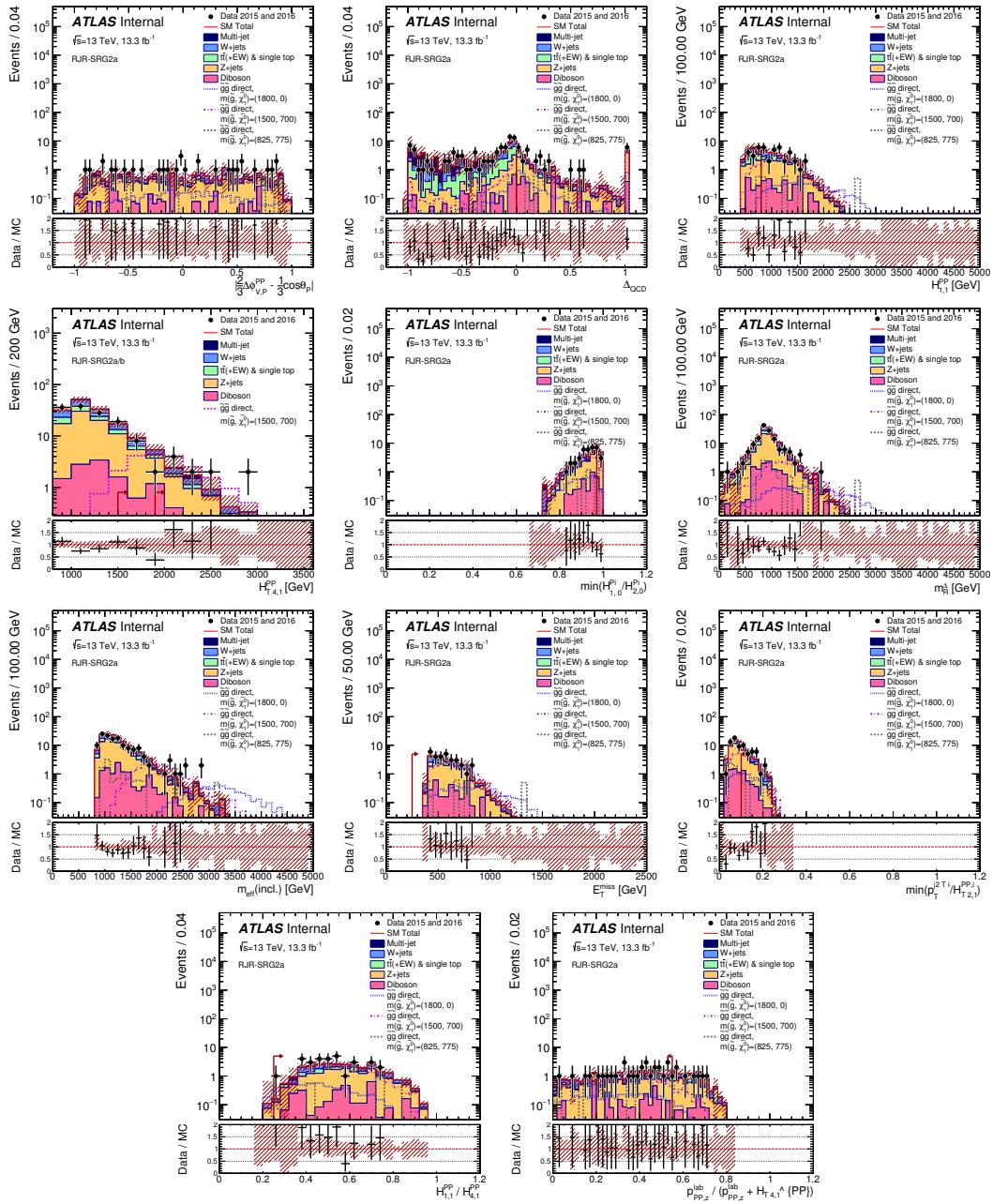


Figure 9

Figure 10

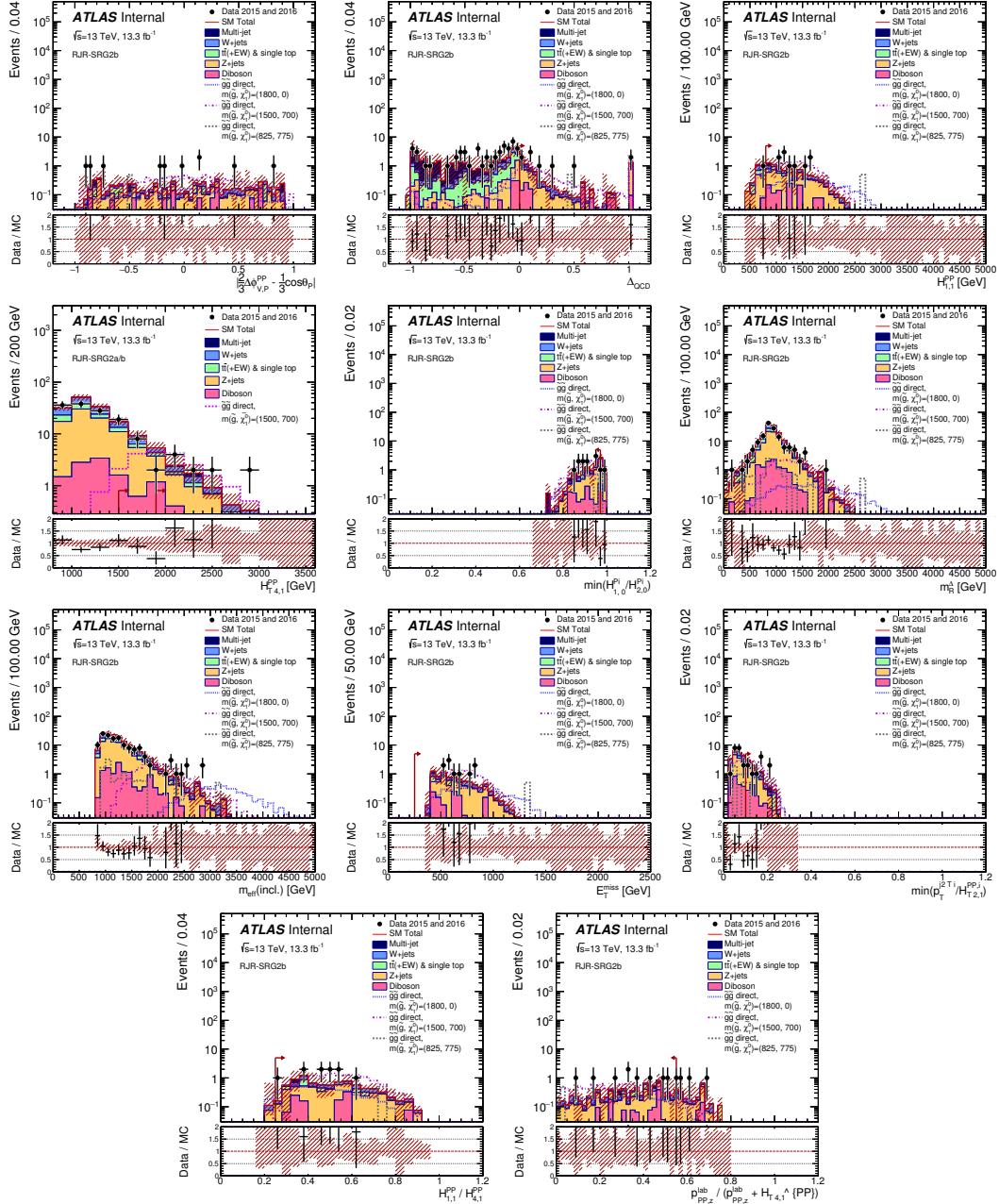


Figure 11

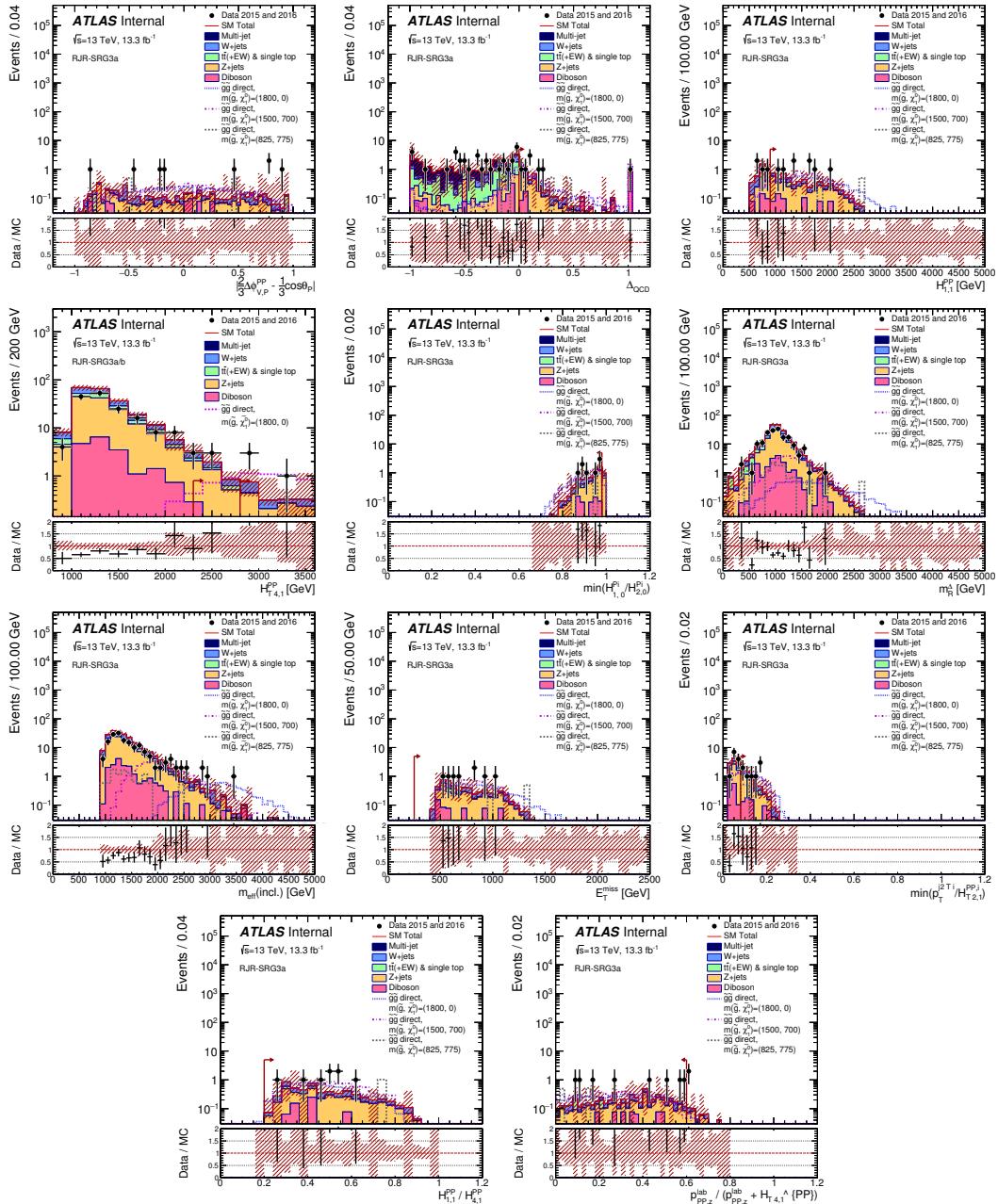


Figure 12

Figure 13

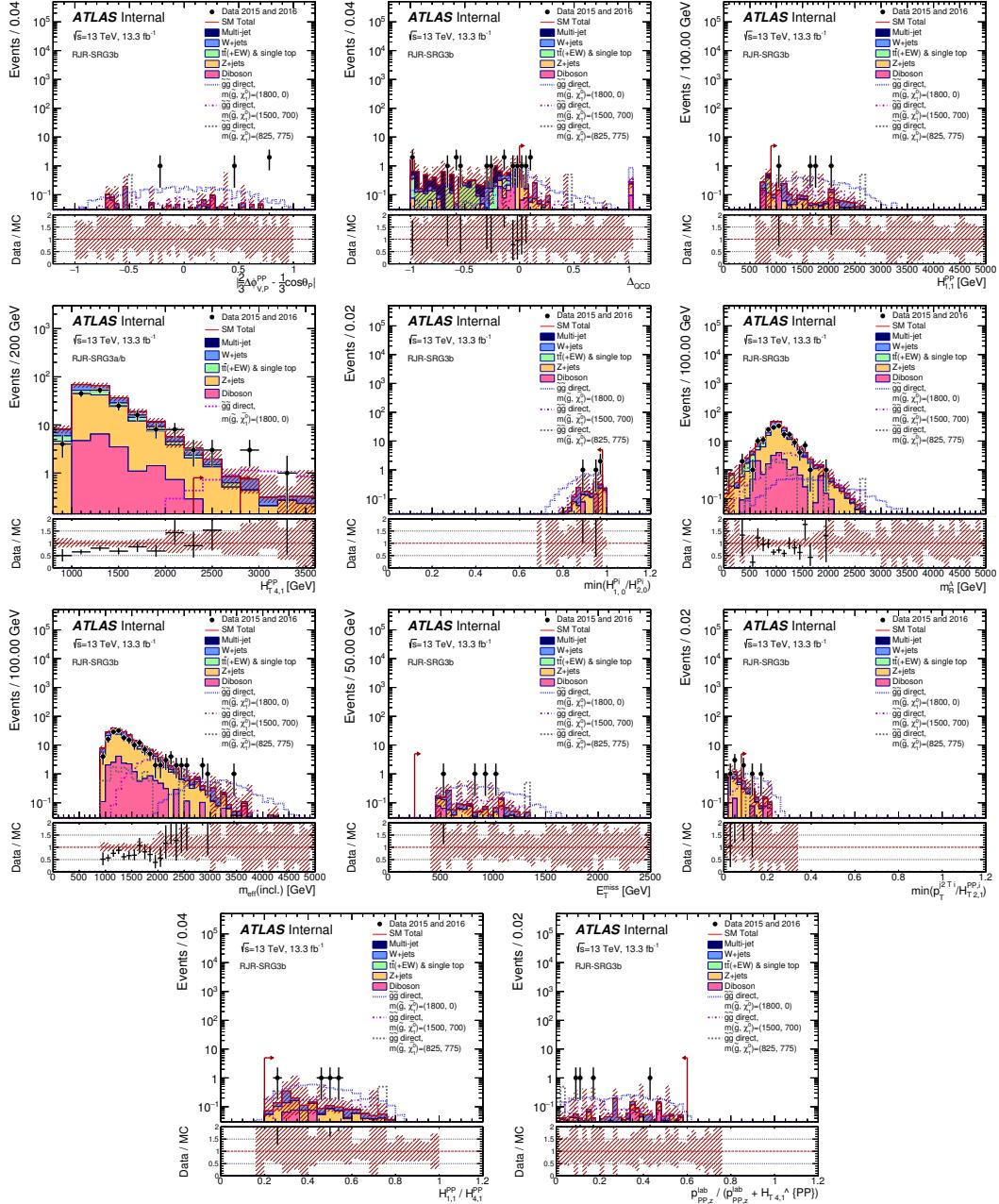


Figure 14

Figure 15

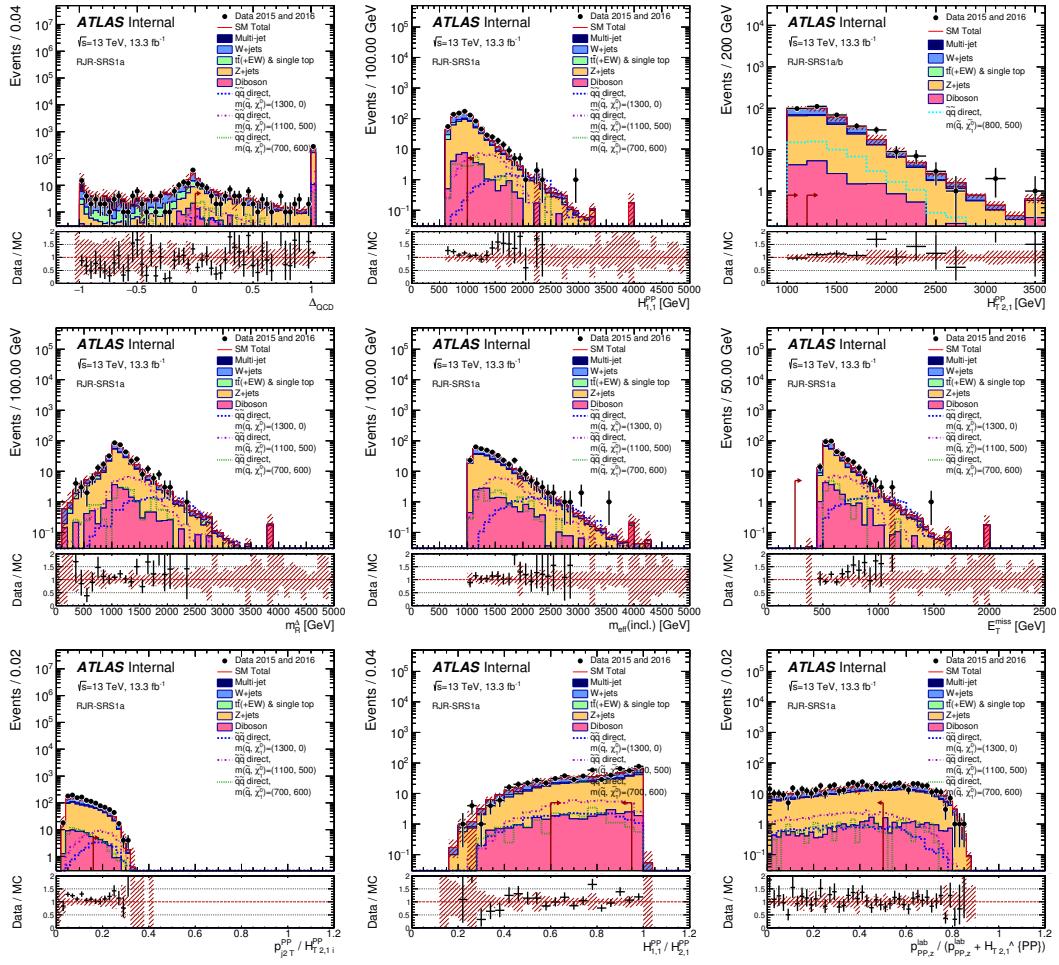


Figure 16

Figure 17

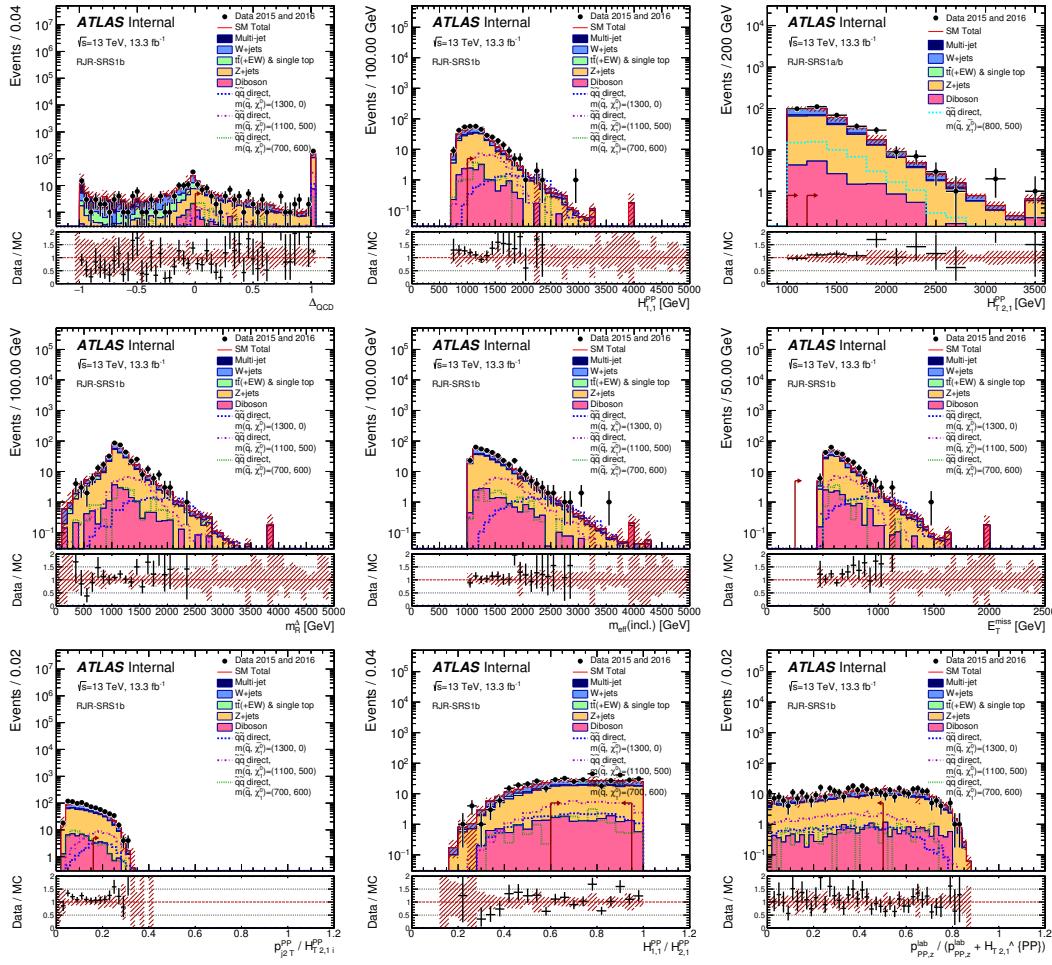


Figure 18

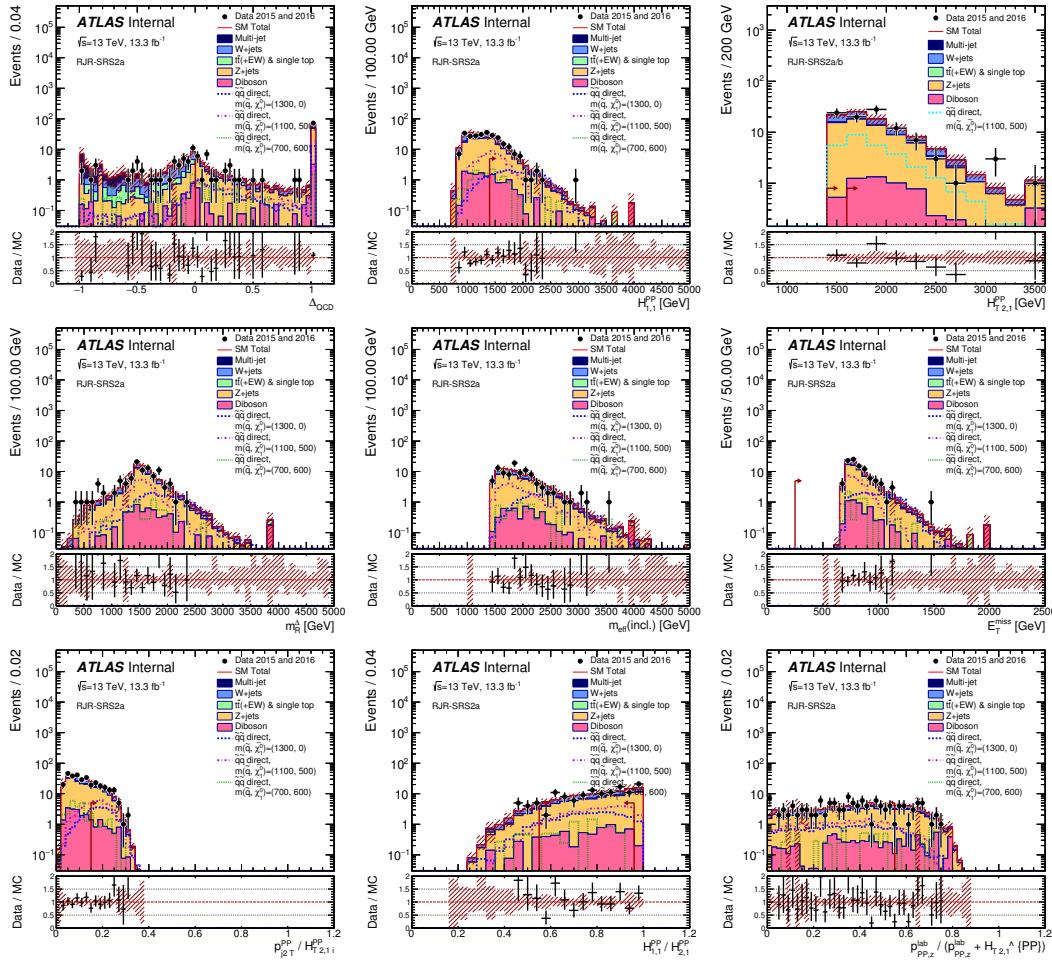


Figure 19

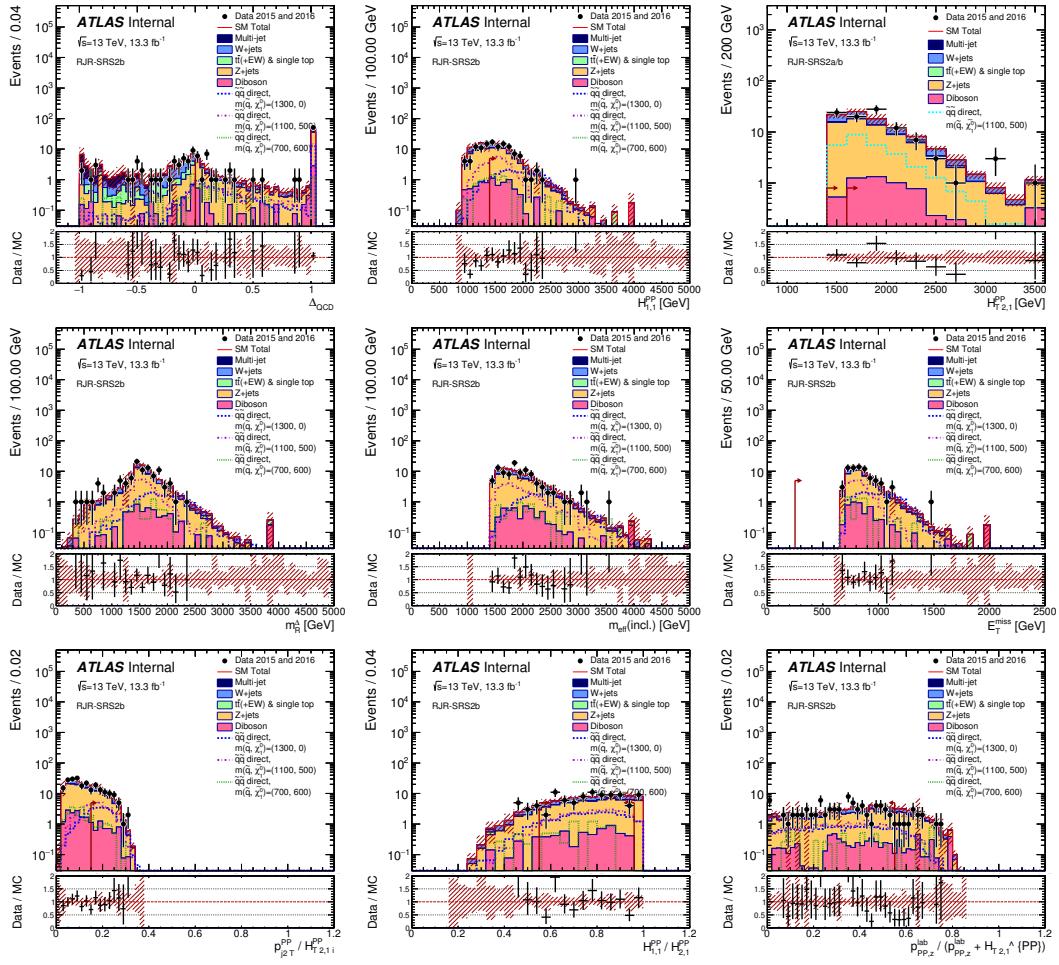


Figure 20

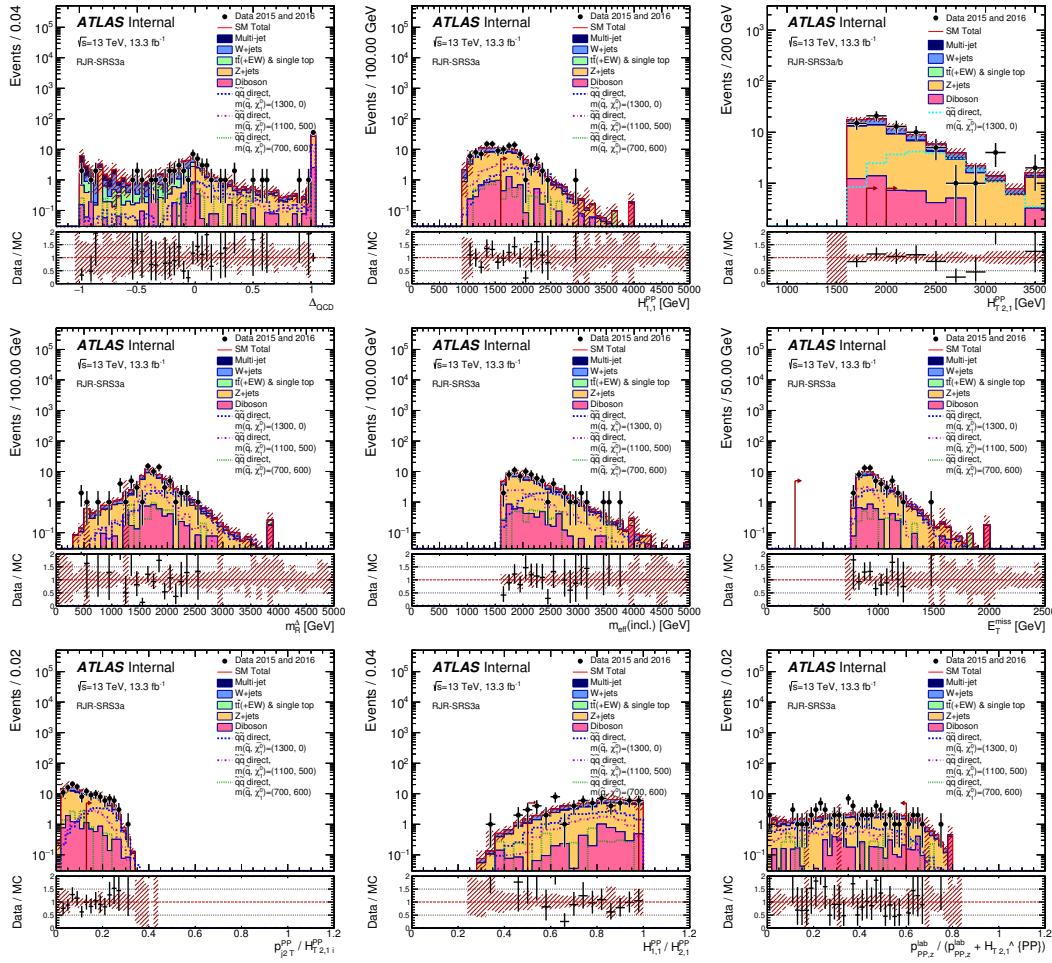


Figure 21

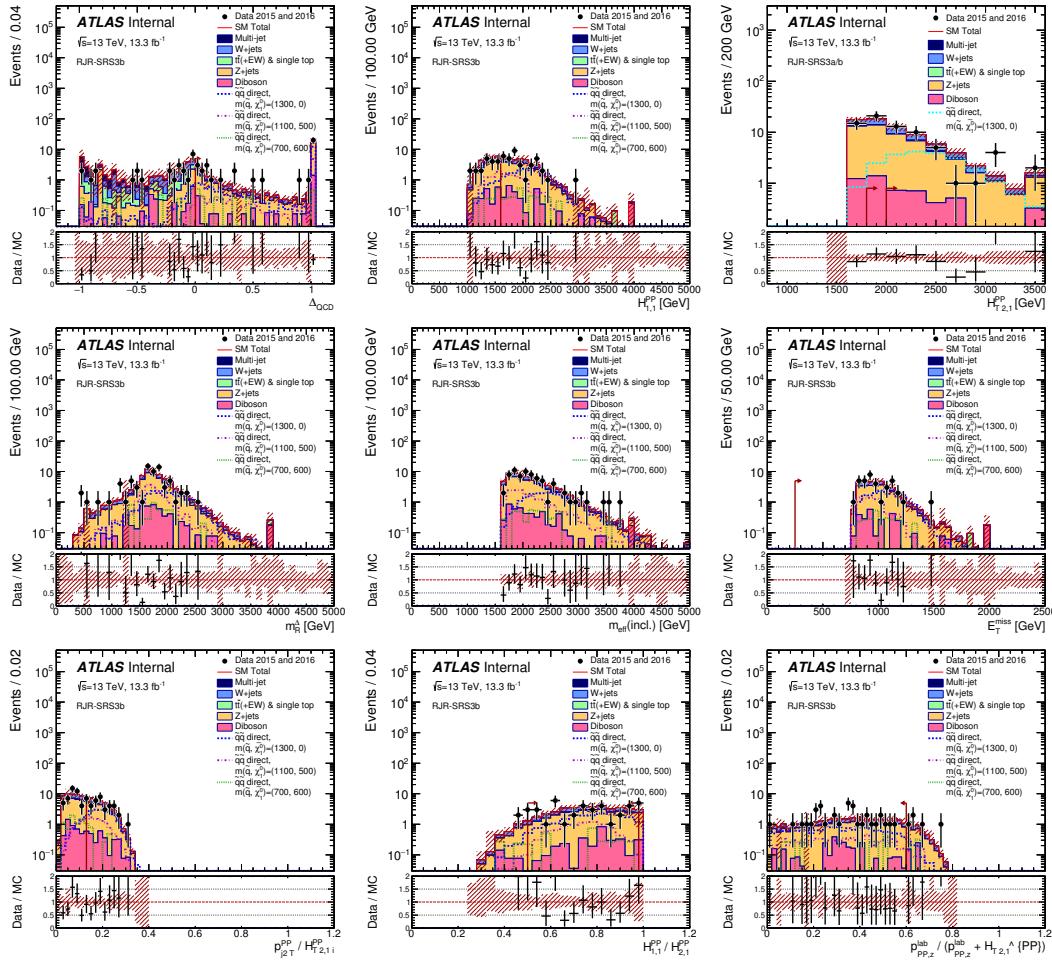


Figure 22