### Homework 1

Ryan, Soeyadi

rs4163

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#### Question 1

A Pythagorean triple consists of three positive integers a, b, and c, such that

$$a^2 + b^2 = c^2$$

### Question 2

Given a quadratic equation  $ax^2 + bx + c = 0$  where x is an unknown variable, a, b, and c are constants. The solution to the quadratic equation is called quadratic formula and is given by:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

#### Question 3

$$1 + 2 + 3 + 4 + \dots + 98 + 99 + 100 = \sum_{x=1}^{100} x$$
$$x_1 + x_2 + x_3 + \dots + x_n = \sum_{i=1}^n x_i$$
$$x_1 \times x_2 \times x_3 \times \dots \times x_n = \prod_{i=1}^n x_i$$
$$f(x) = \int_b^a x^2 dx$$

### Question 4

 $f \colon \mathbb{Z} \mapsto \mathbb{N}$  defined by

$$f(x) = \begin{cases} 2x & \text{if } x \ge 0\\ -2x - 1 & \text{if } x < 0 \end{cases}$$

## Question 5

$$V = \{x \in \mathbb{Z} | x < 100\} \cap \{x \in \mathbb{Z} | \text{x is prime}\}$$
 
$$V \subset W$$

### Question 6

$$((\alpha \to \beta) \land (\beta \to \gamma)) \to (\alpha \to \gamma)$$

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# Question 7

Consider the following statements about integers:

- 1. For every x, there is a y, such that x + y = 0
- 2. There is a y, such that for every x, we have x + y = 0

In symbols, these statements are written respectively:

1. 
$$\forall x \exists y x + y = 0$$

$$2. \ \forall \ y \ \exists \ x \ x + y = 0$$

# Question 8

If x is even, then  $x^2$  is even

Proof. x is an even number.

$$\exists a \in \mathbb{Z} \text{ such that } x = 2a$$

Troop. 
$$x$$
 is an even number:
$$\exists a \in \mathbb{Z} \text{ such that } x = 2a$$

$$x^2 = (2a)^2 = 4a^2 = 2(2a^2)$$
Let  $c = 2a^2, c \in \mathbb{Z}$ 

$$x^2 = 2c$$

Let 
$$c = 2a^2, c \in \mathbb{Z}$$

$$x^2 = 2c$$

Therefore,  $x^2$  is even.

### Question 9

x	y	$x \lor y$
TRUE	TRUE	TRUE
TRUE	FALSE	TRUE
FALSE	TRUE	TRUE
FALSE	FALSE	FALSE