



Week 7

السنة الخامسة – هندسة المعلوماتية / الذكاء الصناعي

مقرر التعلم التلقائي

Practical Concerns for Machine Learning 1 Generalization (Bias-Variance Tradeoff)

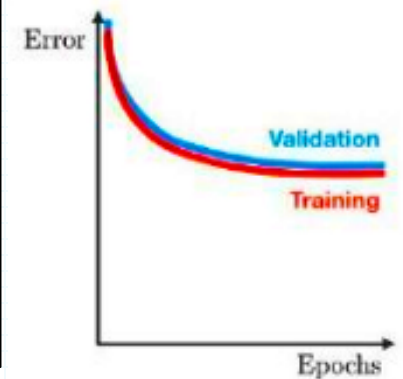
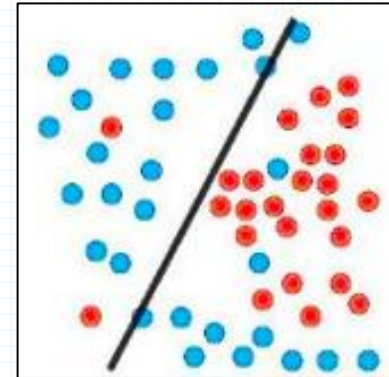
د. رياض سنبل

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Generalization

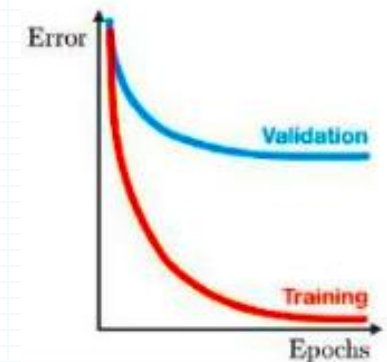
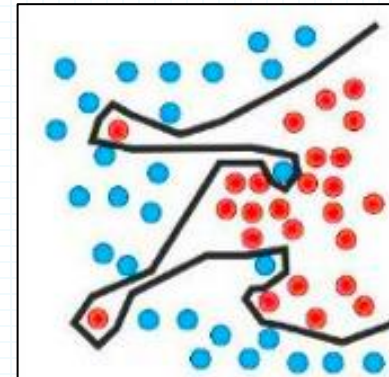
■ **Underfitting**

- The model is **too “simple”** to represent all the relevant class characteristics
- E.g., model with too few parameters produces high error on the training set and high error on the validation set

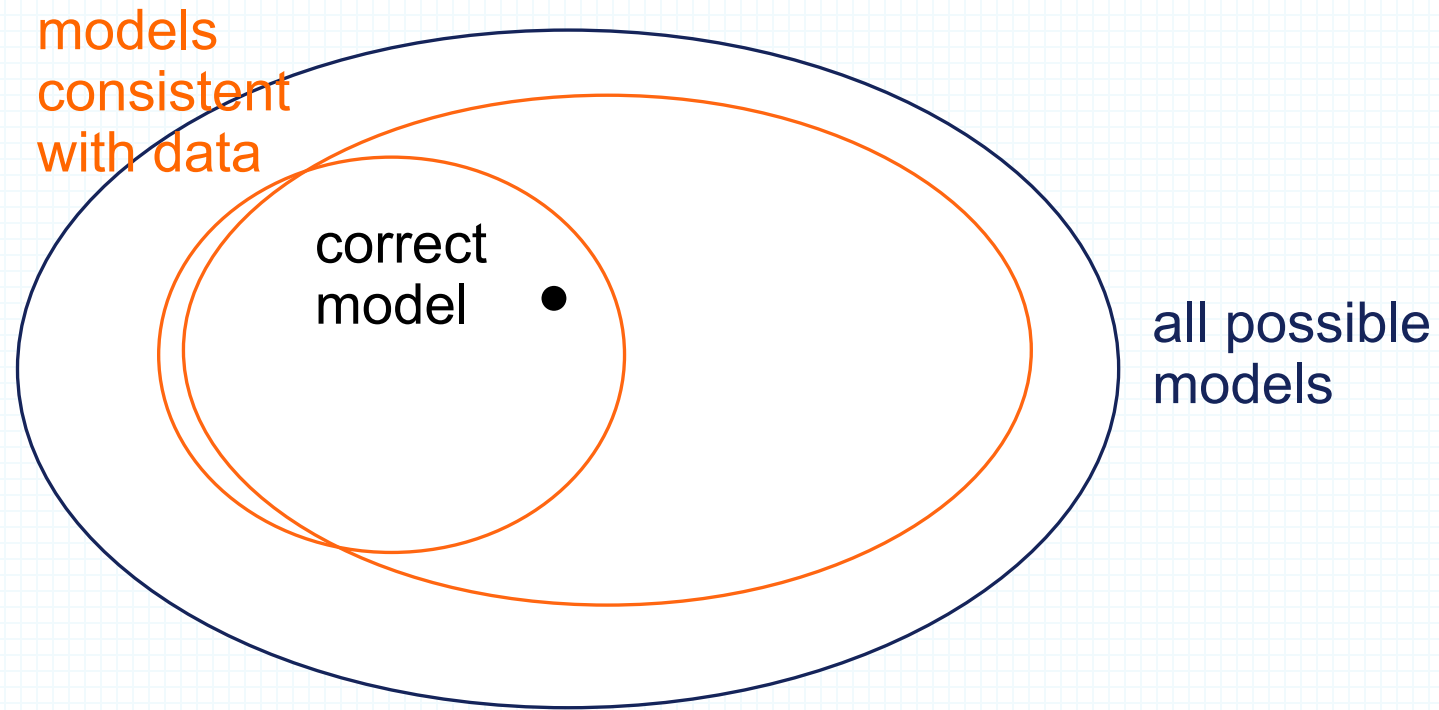


■ **Overfitting**

- The model is **too “complex”** and fits irrelevant characteristics (noise) in the data
- E.g., model with too many parameters produces low error on the training set and high error on the validation set

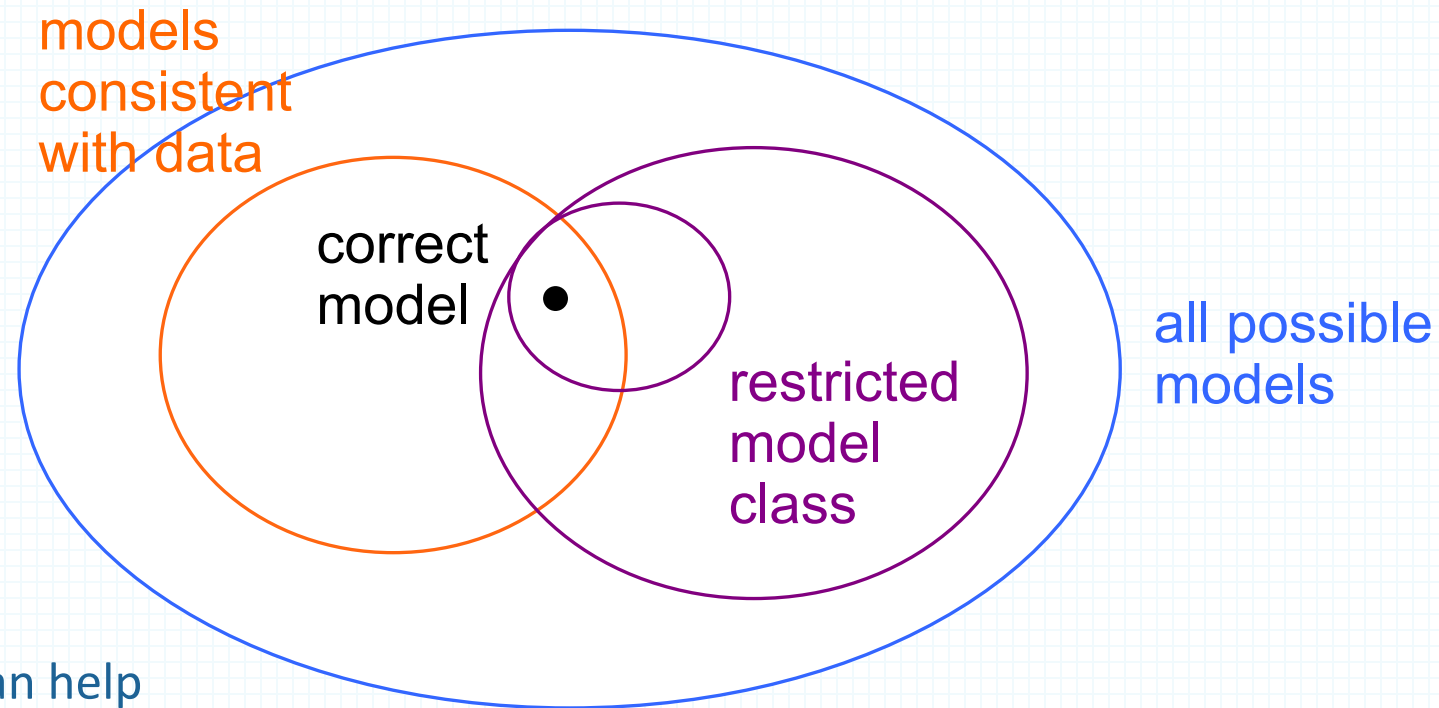


Back to the core idea in ML 😊



More data can help!

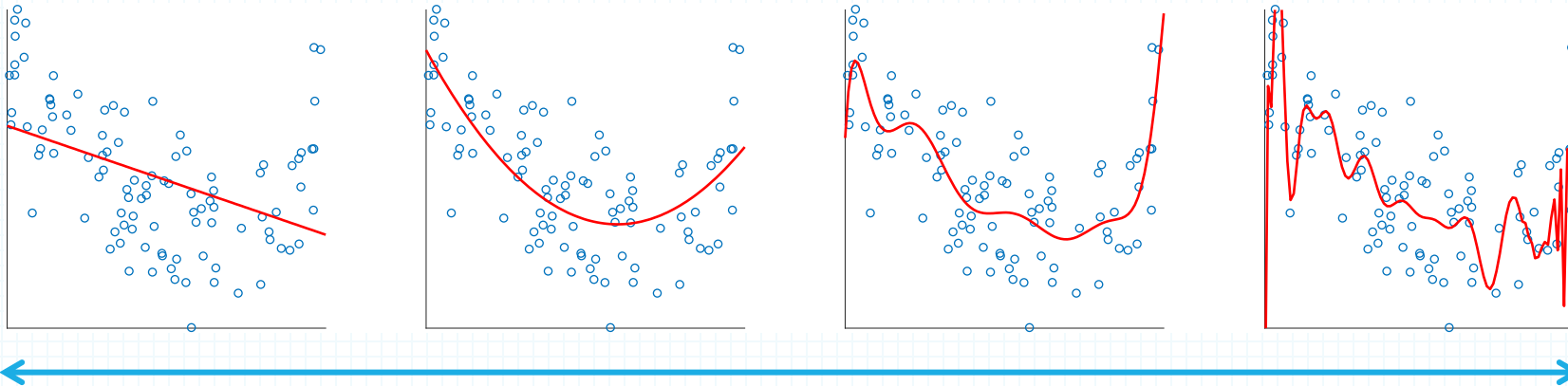
Back to the core idea in ML 😊



- Restricting model class can help
- Or it can hurt
- Depends on whether restrictions are domain appropriate

Restricting Models

- Models range in their flexibility to fit arbitrary data



simple model

constrained

*small capacity may prevent it
from representing all structure
in data*

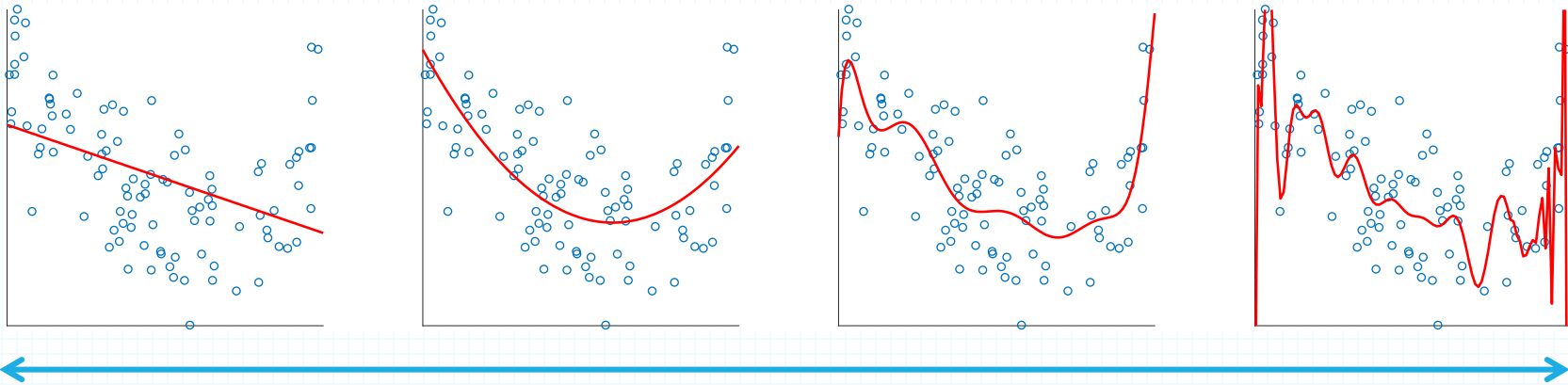
complex model

unconstrained

*large capacity may allow it to
fit quirks in data and fail to
capture regularities*

Bias vs Variance

- Models range in their flexibility to fit arbitrary data



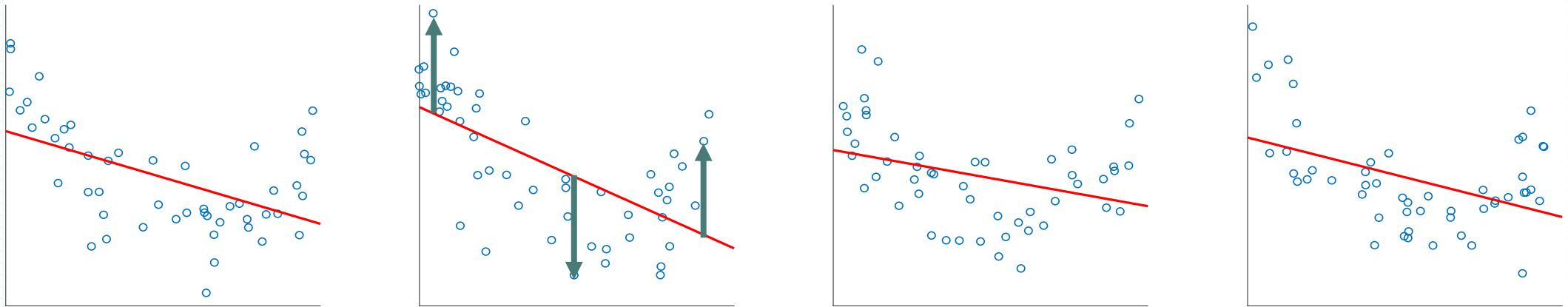
high bias

low variance

low bias

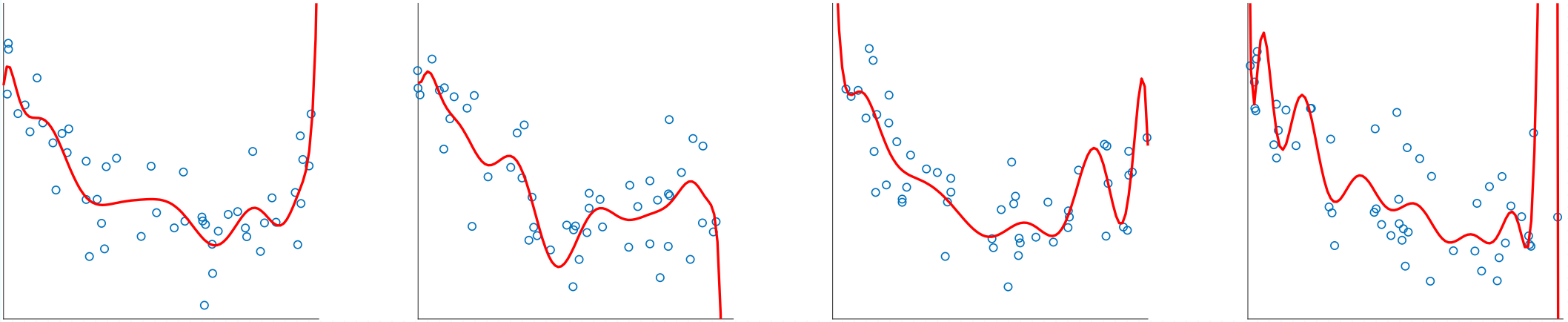
high variance

Bias



- Bias is the amount that a model's prediction differs from the target value, compared to the **training data**.
- Bias error **results from** simplifying the assumptions used in a model so the target functions are easier to approximate.
- Regardless of training sample, or size of training sample, model will produce consistent errors

Variance

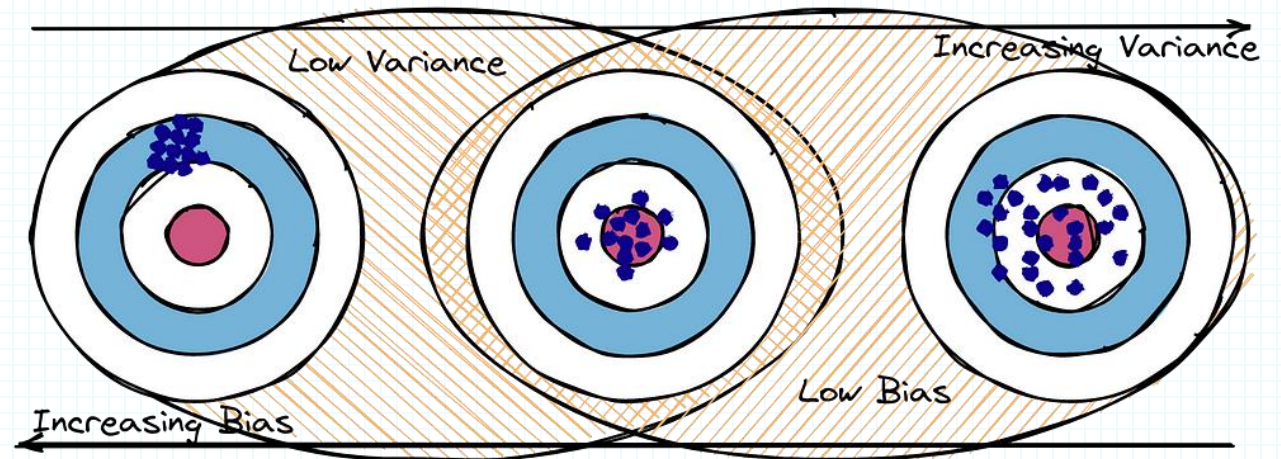
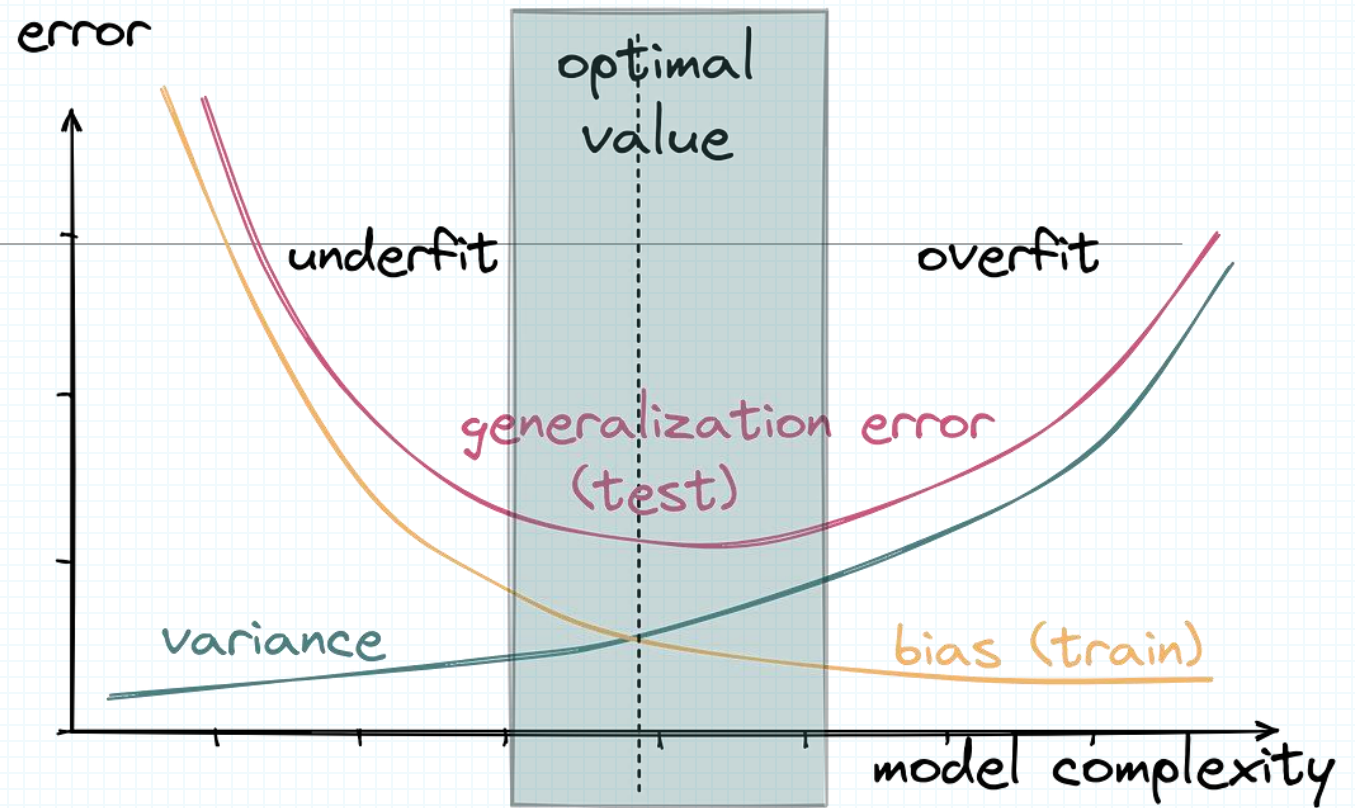


- Variance refers to **the changes in the model** when using different portions of the training data set.
- Simply stated, variance is the **variability in the model prediction**
- Different samples of training data yield different model fits

Bias-Variance Trade off

What does tons of training data do for us in terms of bias-variance trade off?

- ✓ Doesn't affect bias
- ✓ Reduces variance
- ✓ Allows more complex model to be used [shift of optimal complexity to the right]



Bias-Variance Trade off

Training set Error	1%	15%	15%	0.5%
Testing set Error	11%	16%	30%	1%
Bias				
Variance				

DOG vs. CAT

Bias-Variance Trade off

Training set Error	1%	15%	15%	0.5%
Testing set Error	11%	16%	30%	1%
Bias	Low	High	High	Low
Variance	High	Low	High	Low

DOG vs. CAT

$\text{Error} = \text{Irreducible Error} + \text{Bias} + \text{Variance}$

Solutions!

- **High Bias:**

- Bigger Network?
- Train Longer?

- **High Variance:**

- More Data
- Regularization.

$$Err(x) = E \left[(Y - \hat{f}(x))^2 \right]$$

$$Err(x) = \left(E[\hat{f}(x)] - f(x) \right)^2 + E \left[\left(\hat{f}(x) - E[\hat{f}(x)] \right)^2 \right] + \sigma_e^2$$

$$Err(x) = \text{Bias}^2 + \text{Variance} + \text{Irreducible Error}$$
