

The Revolution of the Moons of Jupiter

Student Manual

A Manual to Accompany Software for the
Introductory Astronomy Lab Exercise
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Contemporary Laboratory
Experiences in Astronomy

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Equipment

This experiment uses a Windows computer, the **CLEA** program *The Revolution of the Moons of Jupiter*, and a scientific calculator. (Note that the computer mentioned above may provide such a calculator.)

Historical Background

Astronomers cannot directly measure many of the things they study, such as the masses and distances of the planets and their moons. Nevertheless, we can deduce some properties of celestial bodies from their motions despite the fact that we cannot directly measure them. In 1543 Nicolaus Copernicus hypothesized that the planets revolve in circular orbits around the sun. Tycho Brahe (1546-1601) carefully observed the locations of the planets and 777 stars over a period of 20 years using a sextant and compass. These observations were used by Johannes Kepler, a student of Brahe's, to deduce three empirical mathematical laws governing the orbit of one object around another. Kepler's Third Law is the one that applies to this lab. For a moon orbiting a much more massive parent body, it states the following:

$$M = \frac{a^3}{p^2}$$

where

M is the mass of the parent body in units of the mass of the sun

a is the length of the semi-major axis in units of the mean Earth-Sun distance, 1 A.U. (astronomical unit). If the orbit is circular (as we assume in this lab), the semi-major axis is equal to the radius of the orbit.

p is the period of the orbit in Earth years. The period is the amount of time required for the moon to orbit the parent body once.

In 1609, the telescope was invented, allowing the observation of objects not visible to the naked eye. Galileo used a telescope to discover that Jupiter had four moons orbiting it and made exhaustive studies of this system, which was especially remarkable because the Jupiter system is a miniature version of the solar system. Studying such a system could open a way to understand the motions of the solar system as a whole. Indeed, the Jupiter system provided clear evidence that Copernicus' heliocentric model of the solar system was physically possible. Unfortunately for Galileo, the inquisition took issue with his findings; he was tried and forced to recant.

Introduction

We will observe the four moons of Jupiter that Galileo saw through his telescope, known today as the Gallilean moons. They are named Io, Europa, Ganymede and Callisto, in order of distance from Jupiter. You can remember the order by the mnemonic “**I Eat Green Carrots.**”

If you looked at Jupiter through a small telescope, you might see the following:



Figure 1
JUPITER AND MOONS THROUGH A SMALL TELESCOPE

The moons appear to be lined up because we are looking edge-on at the orbital plane of the moons of Jupiter. If we watched, as Galileo did, over a succession of clear nights, we would see the moons shuttle back and forth, more or less in a line. While the moons actually move in roughly circular orbits, you can only see the perpendicular distance of the moon to the line of sight between Jupiter and Earth. If you could view Jupiter from “above” (see Figure 2), you would see the moons traveling in apparent circles.

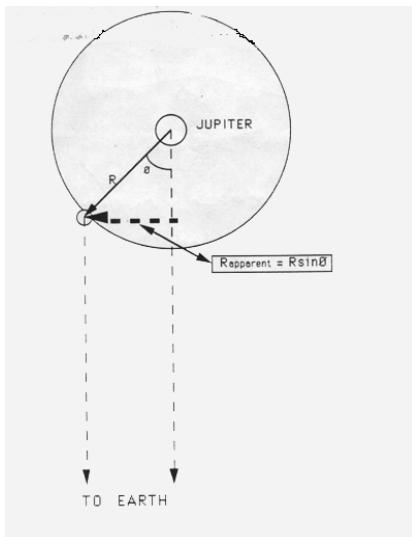


Figure 2

VIEW FROM ABOVE THE PLANE OF ORBIT

R_{apparent} shows the apparent distance between the moon and Jupiter that would be seen from earth.

As you can see from Figure 3 on the next page, the perpendicular distance of the moon should be a sinusoidal curve if you plot it versus time. By taking enough measurements of the position of a moon, you can fit a sine curve to the data and determine the radius of the orbit (the amplitude of the sine curve) and the period of the orbit (the period of the sine curve). Once you know the radius and period of the orbit of that moon and convert them into appropriate units, you can determine the mass of Jupiter by using Kepler’s Third Law. You will determine Jupiter’s mass using measurements of each of the four moons; there will be errors of measurement associated with each moon, and therefore your Jupiter masses may not be exactly the same.

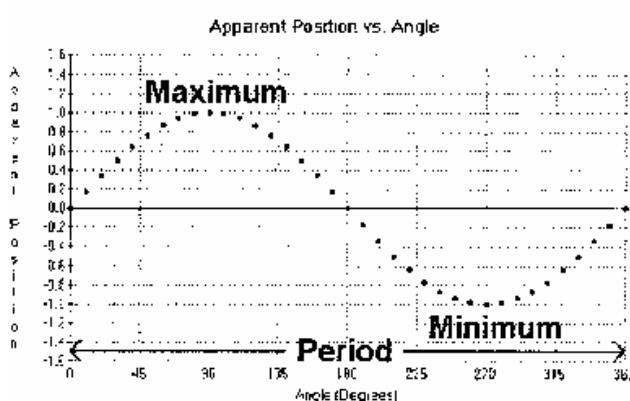


Figure 3

GRAPH OF APPARENT POSITION OF A MOON

The apparent position of a moon varies sinusoidally with the changing angle from the line of sight, θ , as it orbits Jupiter. Here the apparent position is measured in units of the radius of the moon’s orbit, R , and the angle measured in degrees.

This program simulates the operation of an automatically controlled telescope with a charge-coupled device (CCD) camera that provides a video image to a computer screen. It also allows convenient measurements to be made at a computer console, as well as adjustment of the telescope's magnification. The computer simulation is realistic in all important ways, and using it will give you a good understanding of how astronomers collect data and control their telescopes. Instead of using a telescope and actually observing the moons for many days, the computer simulation shows the moons to you as they would appear if you were to look through a telescope at the specified time.

Overall Strategy

This is the overall plan of action for this laboratory exercise.

- Start up the program and use it to familiarize yourself with the Jupiter system.
- Set up observing sessions.
- Measure positions of Jupiter's moons over successive clear nights.
- Plot a graph of your observations for each moon, using the ***Revolution of Jupiter's Moons*** program.
- Using this program to help you, fit a sine curve to each graph.
- Determine the period and semi-major axis for the orbit of each moon from its graph, then convert the values to years and AU, respectively.
- Calculate the mass of Jupiter from your observations of each moon, then determine the average value for Jupiter's mass from your individual values.

Before You Start

Now is an ideal time to have a little fun with the program and in the process visualize what you will be doing and why. Start up the **Jupiter's Moons** lab; then select **Log in . . .** from the **File** menu. Enter your name(s) and table number in the dialogue box that appears and select **OK**. Now select **File . . . > Run . . .**; when the next window pops up, simply select **OK** to accept the defaults for the **Start Date & Time**; you will be going back to change these after you've familiarized yourself with the program and the motions of the Jupiter system. Now the window pictured below appears, showing Jupiter much as it would appear in a telescope. Jupiter appears in the center of the screen, while the small, point-like moons are on either side. Sometimes a moon is hidden behind Jupiter and sometimes it appears in front of the planet and is difficult to see. You can display the screen at four levels of magnification by clicking on the **100X**, **200X**, **300X**, and **400X** buttons. The screen also displays the date, Universal Time (the time at Greenwich, England), the Julian Date (a running count of days used by astronomers; the decimal is an expression of the time), and the interval between observations (or animation step interval if **Animation** is selected).



Figure 4
OBSERVATION SCREEN

To do something you can't do with the real sky, select **File > Preferences > Animation**, then click on the **Cont.** (Continuous) button on the main screen. Watch the moons zip back and forth as the time and date scroll by. With this animation, it's fairly easy to see that what the moons are really doing is circling the planet while you view their orbits edge-on. To reinforce this, stop the motion by selecting **Cont.** again, select **File > Preferences > Top View**, and start the motion again (**Cont.**). Note that under the **Preferences** menu you can also choose **ID Color** and avoid confusing the four moons.

When you are satisfied that you understand the motions of Jupiter's moons and why they appear the way they do, you are ready to start the lab. At any time you may select **Help** in the upper right corner of the main screen to view help screens on a wide variety of topics.

Turn off the Animation feature before going on to the next section.

Procedure

Data Collection

If you have already logged in as described above, stop the motion of the moons (if you have not already) and select **Run . . .** again. The **Start Date & Time** window will appear, and now you will change the defaults. Each table will perform a *different set* of observing sessions. The starting dates of observations for each table, as well as the interval between observations, will be given to you by your instructor. (A typical approach is to observe at twelve-hour intervals until you have successfully observed 18 times.) Fill in the table below first; then enter the information into the program. It is good scientific practice to keep both paper and computer records when possible. (Note that this time you will be replacing the defaults, which are for the current date and time.)

Table Number	_____
Year	_____
Month	_____
Day	_____
Time Zone	_____
Number of Observations	_____
Interval Between Obs.	_____

In order to measure the position of a moon, move the pointer to the moon and left-click the mouse. The lower right-hand corner of the screen will display the name of the moon (for example, **II. Europa**), the X and Y coordinates of its position in pixels on your screen, and its X coordinate expressed in diameters of Jupiter (**Jup. Diam.**) to the east or west of the planet's center. This is the crucial figure for our purposes. Note that if the name of the moon does not appear, you may not have clicked exactly on the moon, so try again. To measure each moon's position accurately, switch to the highest magnification that will keep the moon on the screen.

Column 1:	Date
Column 2:	Universal Time
Column 3:	Day - number of day (e.g. 1.0, 1.5, 2.0, . . .), including cloudy days.
Columns 4-7:	Record each moon's position under the column for that moon. Be sure to note both distance and direction, for example, 2.75W.

You will also use the computer to record your data for later analysis. After taking a measurement, select **Record Measurements . . .** and enter the data in the dialog box that appears. You can go back and add to or edit this data later using **File > Data > Review . . .**, but for the sake of convenience, you may want to enter the data for all four moons before you go on to the next observing session. To be safe, use **File > Data > Save . . .** to save your data. Otherwise it will be lost if the program closes. If the program is closed, use **Load . . .** under the same menu to retrieve the saved file.

Data Analysis

You now need to analyze your data. By plotting position versus time, you will use the data to obtain a graph similar to the one below. (The data shown are for an imaginary moon named CLEA, not one of the moons in the laboratory exercise.)

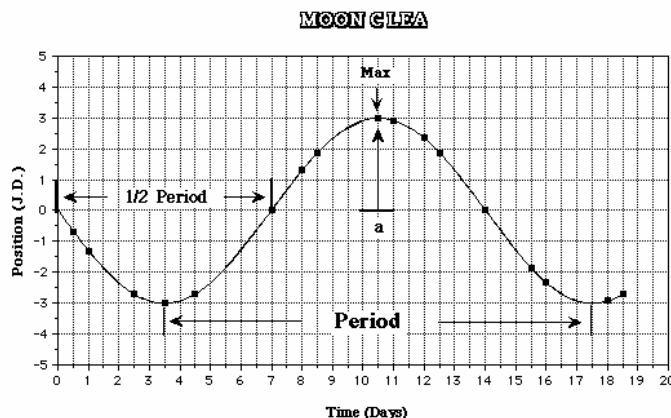


Figure 5

SAMPLE GRAPH FOR MOON CLEA

$$p = 14 \text{ days} = 0.0383 \text{ years}$$

$$a = 3 \text{ J.D.} = 0.00286 \text{ A.U.}$$

We know the following: (1) the orbits of the moons are regular, that is, they do not speed up or slow down from one period to the next, and (2) the radius of each orbit does not change from one period to the next. The sine curve should therefore also be regular. It should go through all of the points, and not have a varying maximum height nor a varying width from peak to peak.

Taking as an example the imaginary Moon CLEA, we can determine the radius and period of the orbit. The period is the time it takes for the moon to circle the planet and return to the same point in the orbit. Thus the time between two maxima is the period. The time between crossings at 0 J.D., is equal to half the period because this is the time it takes to get from the front of Jupiter to the back of Jupiter, or half way around. For some of your moons, you may not get data from your observations for a full period. You may find the time between crossings at 0 J.D. to be of use to you in determining the period, even though the moon has not gone through a complete orbit.

The radius of an orbit is equal to the maximum position eastward or westward, that is, the largest apparent distance from the planet. Remember that the orbits of the moon are nearly circular, but since we see the orbits edge on, we can only determine the radius when the moon is at its maximum position eastward or westward.

When you have completed the specified number of successful observing sessions (typically 18, not counting cloudy nights), you are ready to analyze the data as we've done for Moon CLEA.

Fortunately, this program will help you create the appropriate sine curve. Select **File > Data > Analyze ...** and then choose **Callisto IV** from the **Select** menu. (Start with the more distant, slower moving moons because the time interval between observing sessions represents a smaller portion of their orbits, and thus their curves are easier to fit.) When the graph of data points appears, try to find a pattern by eye, and take note of any data points that seem to be out of place. To better see the pattern, select **Plot > Plot Type > Connect Points**. This will display a jagged, "connect-the-dots" version of your graph. Click on a point at which the line connecting the points crosses from negative to positive. (If this happens several times, choose a point toward the left of the screen.) A date and a value very close to zero should appear in the box marked **Cursor Value**. Now select **Plot > Fit Sine Curve > Set Initial Parameters** and enter the date you just found as **T-zero**. Go back to the graph and find the next point at which the line passes *from negative to positive* (that is, when the moon has completed one orbit.) Subtract the earlier date from the later date and enter this as **Period** in the dialog box. If the line does not cross from negative to positive twice, you could use the interval between any two crossings as a good estimate of half the period and then double it. Similarly, in the case of a fast moving moon, you could measure the time taken to complete several periods and then divide the total time by the number of periods for a more accurate figure. Finally, estimate the **Amplitude** of the sine curve by clicking on the peaks and valleys of your graph and reading the **Value** in the **Cursor Position** box. The **Amplitude** is equal to the absolute value (i.e., ignore a – sign) of the highest peak or the lowest valley of your graph.

When **T-Zero**, **Period**, and **Amplitude** are all entered, click **OK**. Now a blue sine curve will appear. It should be a rough fit for all your data points. If not, you may need to repeat the **Set Initial Parameters** step. If only one or two points are significantly off the blue line, they may represent inaccurate measurements. If your instructor allows, you may remove these.

Now you will begin adjusting the fit with the three scroll bars that have appeared. First adjust the **T-Zero** point. As you adjust this value, the entire curve will slide to the left or right. Try to achieve the best fit *for the data points closest to the T-zero value you selected above*. At this stage, pay no attention to the number labeled **RMS Residual**; just use your eyes. After you've adjusted the **T-zero** value, you may notice that the points farther away from your **T-zero** point no longer fit as well. Now use the **Period** scroll bar to stretch or shrink the curve and achieve a better fit. If at any time you cannot scroll far enough to get a good fit, select **Plot > Reset Scrollbars > Normal Sensitivity** to re-center the bars. Next adjust the **Amplitude** bar to better fit the points near the peaks and valleys. You may wish to return to the other scroll bars for further adjustment, but the goal at this point is a good, though not necessarily perfect, fit.

Now it is time to fine tune the curve. Return to adjusting the **T-zero** scroll bar, this time observing the **RMS Residual**. The smaller the value of this number is (note that it's expressed in scientific notation), the better the fit. Move the scroll bar with the arrows until this number is smallest, that is, when one click in either direction would make it larger. Continue this process with the **Period** and **Amplitude** bars. Because the three adjustments affect each other, you should then return to the **T-zero** bar and repeat the scroll bar adjustments until all three yield the lowest **RMS Residual**. When you have achieved the lowest value, select **Plot > Reset Scrollbars > Fine Sensitivity**. Then repeat the adjustments for the three scroll bars at this more sensitive level. These last adjustments should result in a highly accurate sine curve drawn to fit the data you gathered.

Write down the **Period** and **Amplitude** in the table provided on page X. (Recall that the amplitude is equal to the radius, which, since we are assuming the orbit is circular, is equal to the semi-major axis.) Then select **Plot > Print Current Display** to print the graph. After the graph has been successfully printed, choose a different moon from the **Select** menu. As mentioned before, it is a good idea to start with the slow-moving Callisto and then move on to Ganymede, Europa, and finally Io. Hint: you may find it easier to fit a curve for the fast-moving Io if you use a short **Data Span** of 10 days, even if your data covers a longer period of time. This setting can be found under the **Plot** menu.

When you have printed all four graphs and recorded all the appropriate data you may close the CLEA Jupiter's Moons exercise and begin answering the questions on the next page.

Calculating Jupiter's Mass

You now have all the information you need to use Kepler's Third Law to find the mass of Jupiter. But note that values you obtained from the graphs have units of days for **p**, and J.D. for **a**. In order to use Kepler's Third Law, you need to convert the period into years by dividing by the number of days in a year (365), and the orbital radius into A.U. by dividing by the number of Jupiter diameters in an A.U. (1050). Enter your converted values in the spaces provided in the data table on page X. With **p** and **a** in the correct units, calculate a mass of Jupiter using data from each of the four moons. If one of the values differs significantly from the other three, look for a source of error. If no error is found, the data may not be adequate for a better result, in which case you should leave the data as you found it.

where **M_J** the mass of Jupiter in units of the solar mass

$$\mathbf{M} = \frac{\mathbf{a}^3}{\mathbf{p}^2}$$

a is the radius of the orbit in units of A.U.

p is the period of the orbit in Earth years

From Callisto $M_J = \underline{\hspace{2cm}}$

From Ganymede $M_J = \underline{\hspace{2cm}}$

From Europa $M_J = \underline{\hspace{2cm}}$ **in units of solar masses**

From Io $M_J = \underline{\hspace{2cm}}$

Average $M_J = \underline{\hspace{2cm}}$ solar masses

Questions and Discussion

1. Express the mass of Jupiter in earth units by dividing it by 3.00×10^{-6} , which is the mass of Earth in solar mass units.

Average $M_J = \underline{\hspace{2cm}}$ earth masses

2. There are moons beyond the orbit of Callisto. Will they have larger or smaller periods than Callisto? Why?

Extra Credit

1. Which do you think would cause the larger error in : a ten percent error in **p** or a ten percent error in **a**? Why?
 2. The orbit of earth's moon has a period of 27.3 days and a radius (semi-major axis) of 2.56×10^{-3} A.U. ($= 3.84 \times 10^5$ km). What is the mass of Earth? What are the units? Show your work.

Data Sheet A

Collect 18 lines of data, not counting cloudy nights. Mark cloudy sessions as in the sample below. Remember to enter “E” or “W.”

(1) Date	(2) Time	(3) Day	(4) Io	(5) Europa	(6) Ganymede	(7) Calisto
7/24	0.0	1.0	2.95W	2.75W	7.43E	13.15W
7/24	12.0	1.5	CLOUDY-	-----	-----	-----

Data Sheet B

Moon	Period (days)	Period (years)	Semi-major Axis (J.D.)	Semi-major Axis (A.U.)
IV Callisto				
III Ganymede				
II Europa				
I Io				