



# Lecture 7: Sorting algorithm (Part. 1)

## Algorithm

Jeong-Hun Kim

# Remind

- ❖ Knapsack Problems
  - 0-1 knapsack
  - Fractional knapsack
- ❖ Interval scheduling
  - Maximum number of tasks that can be processed
- ❖ Scheduling all requests
  - Minimum number of classrooms required to conduct all lectures
- ❖ Huffman encoding
  - Minimization of binary string length

# Table of Contents

- ❖ Part 1
  - Data Sorting
- ❖ Part 2
  - Representative Basic Sorting Algorithms

Part 1

# **DATA SORTING**

# Data Sorting

## ❖ Sorting problem

- Input: A list consisting of  $n$  numbers  $\langle a_1, a_2, a_3, \dots, a_{n-1}, a_n \rangle$
- Output: A list rearranged in ascending order  $\langle a'_1, a'_2, a'_3, \dots, a'_{n-1}, a'_n \rangle$ , where  $a'_1 \leq a'_2 \leq \dots \leq a'_n$

## ❖ What is the sorting algorithm?

- Arranging  $n$  elements in order
  - E.g., Sorted by height, sorted by name, sorted by number, etc.
- Time complexity: typically between  $O(n^2)$  and  $O(n \log n)$ 
  - When the input satisfies specific conditions, time complexity is  $O(n)$

# Data Sorting

- ❖ Representative sorting algorithms
  - Basic sorting algorithms
    - Sorting algorithms that have an time complexity of  $\Theta(n^2)$ 
      - $n$  is the number of elements
    - E.g., Selection sort, Bubble sort, Insertion sort
  - Advanced sorting algorithms
    - Sorting algorithms that have an time complexity of  $O(n \log n)$
    - E.g., Shell sort, Merge sort, Quick sort, Heap sort, Radix sort, Bucket sort, Tim sort

Part 2

# **REPRESENTATIVE BASIC SORTING ALGORITHMS**

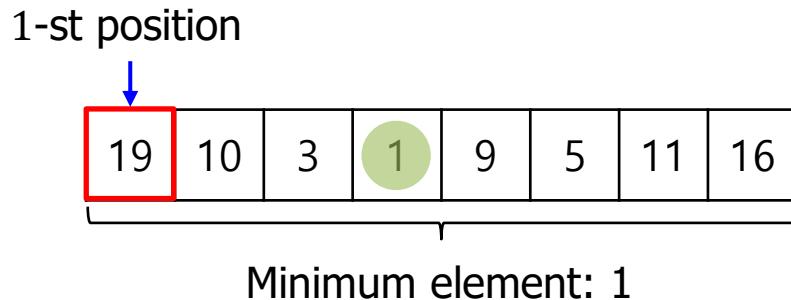
# Representative Basic Sorting Algorithms

- ❖ Selection sort
  - The **simplest** sorting algorithm
  - **In-place** comparison sort
    - In-place: no need for a new list ( $\leftrightarrow$  out-of-place)
    - Useful when memory space is **limited**
  - Time complexity:  $O(n^2)$
  - Methodology:
    - 1) Move to the  $i$ -th position in the list
    - 2) Find the **minimum** element among elements from  $i$  to  $n$
    - 3) **Swap** the  $i$ -th element with the minimum element
    - 4) Repeat 1) – 3) steps until  $i = n$

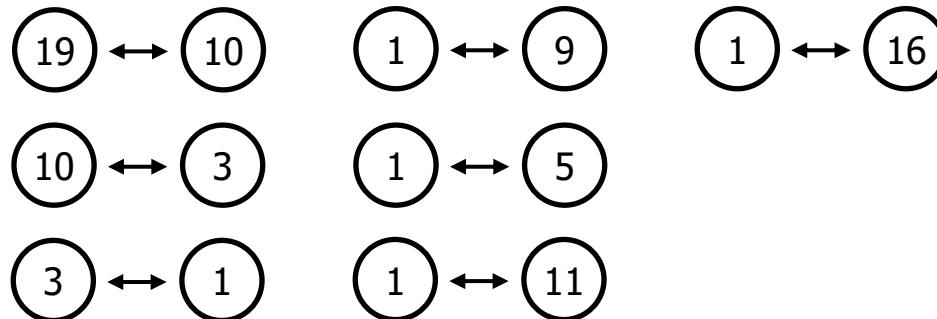
# Representative Basic Sorting Algorithms

## ❖ Selection sort

- Example)



Comparisons:

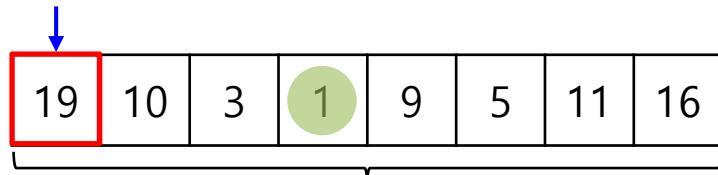


# Representative Basic Sorting Algorithms

## ❖ Selection sort

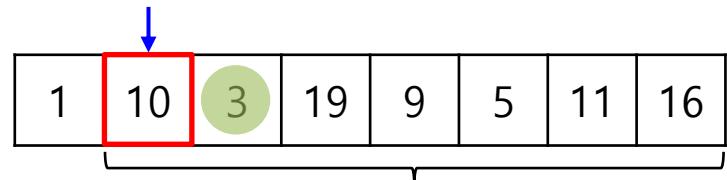
- Example (cont'd)

1-st position



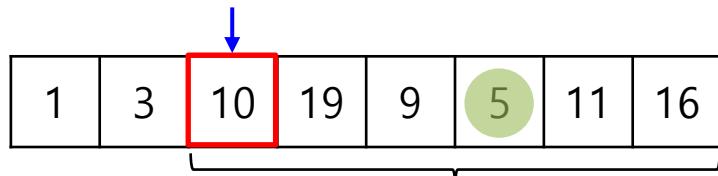
Minimum element: 1

2-nd position



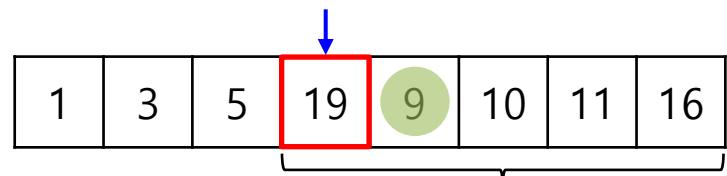
Minimum element: 3

3-rd position



Minimum element: 5

4-th position

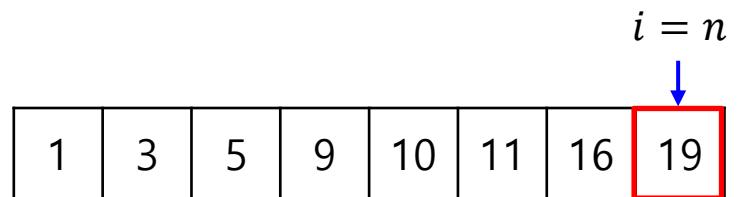
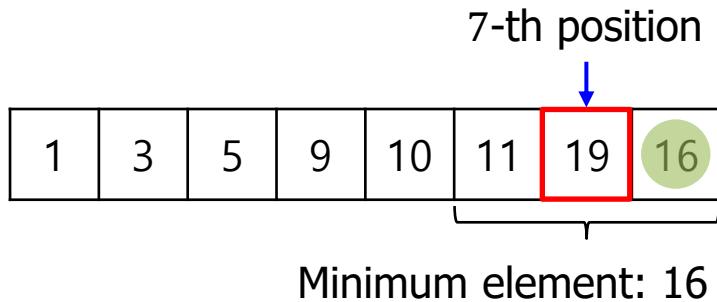
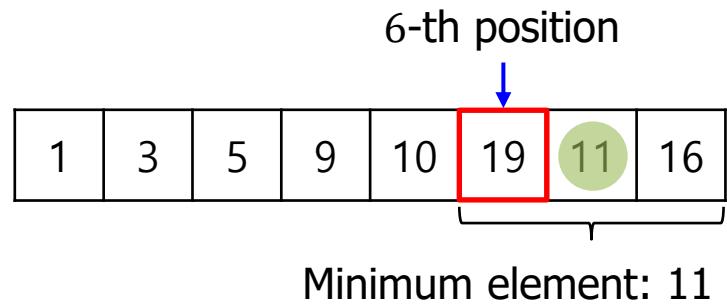
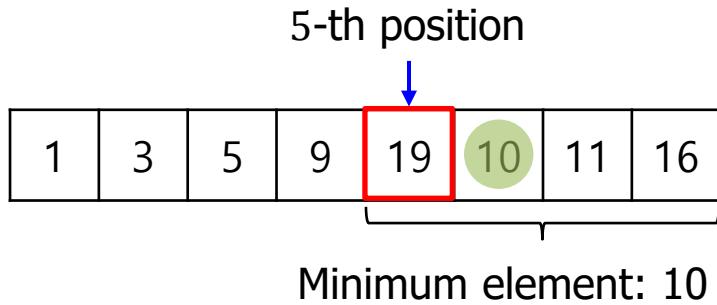


Minimum element: 9

# Representative Basic Sorting Algorithms

## ❖ Selection sort

- Example (cont'd)



# Representative Basic Sorting Algorithms

## ❖ Selection sort

- Psuedo code)

```
#include <stdio.h>

void swap(int *a, int *b){
    int temp = *a;
    *a = *b;
    *b = temp;
}

void selection_sort(int arr[], int n){
    int i, j, min_idx;
    for (i = 0; i < n - 1; i++){
        min_idx = i;
        for (j = i + 1; j < n; j++){
            if (arr[j] < arr[min_idx])
                min_idx = j;
        }
        if (min_idx != i)
            swap(arr[min_idx], arr[i])
    }
}
```

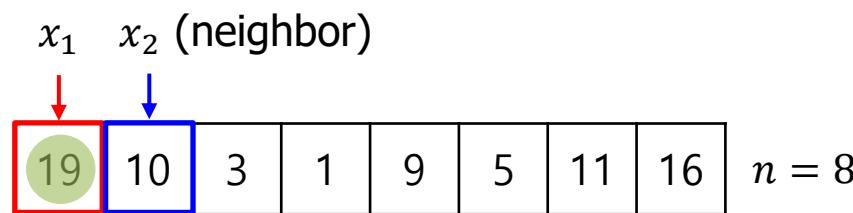
# Representative Basic Sorting Algorithms

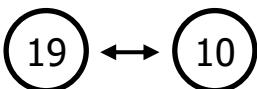
## ❖ Bubble sort

- Traverse method
- In-place comparison sort
- It uses neighbor element
- Time complexity:  $O(n^2)$
- Methodology:
  - 1) Compare  $i$ -th element  $x_i$  with its neighbor ( $i + 1$ -th) element  $x_{i+1}$
  - 2) If  $x_i > x_{i+1}$ , swap the positions of  $x_i$  and  $x_{i+1}$
  - 3) Repeat 1-2) steps until  $i + 1 = n$
  - 4) Decrease  $n$  by 1, then repeat steps 1) – 3)
  - 5) Terminate when  $n = 1$

# Representative Basic Sorting Algorithms

- ❖ Bubble sort
  - Example)



Comparisons: 

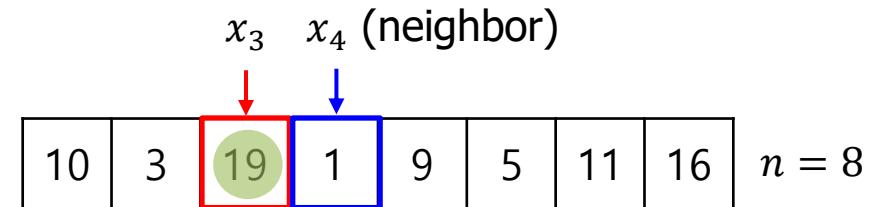
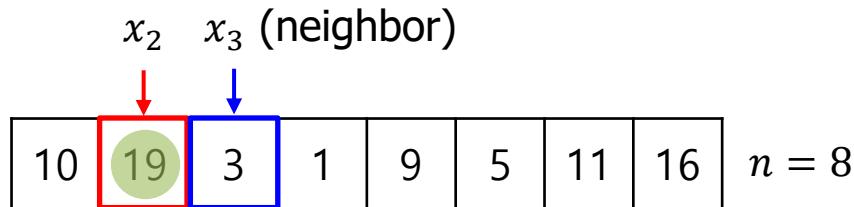
↓ Swap  $x_1$  and  $x_2$

10	19	3	1	9	5	11	16
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# Representative Basic Sorting Algorithms

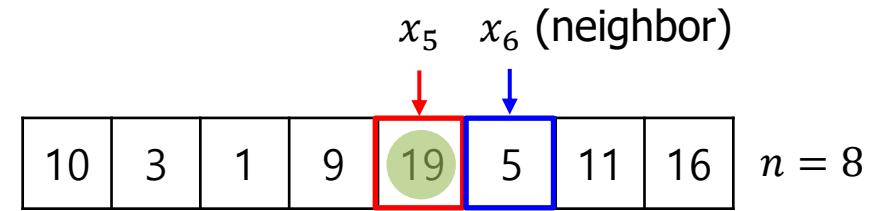
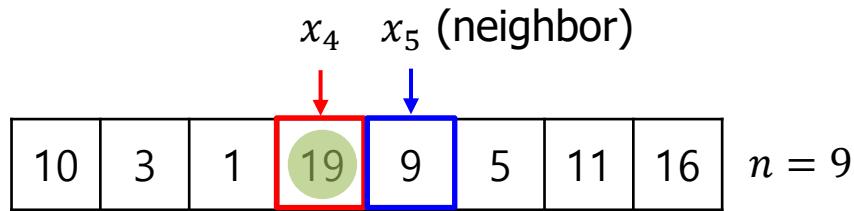
## ❖ Bubble sort

- Example)



Comparisons:  $\leftrightarrow$

Comparisons:  $\leftrightarrow$

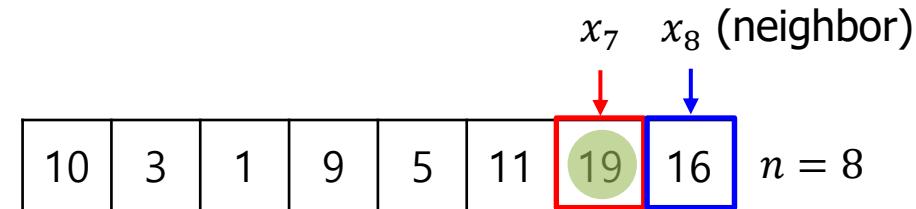
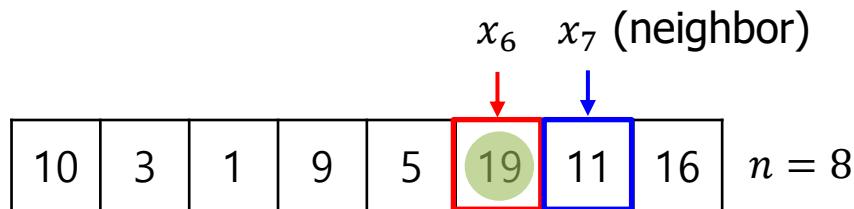


Comparisons:  $\leftrightarrow$

Comparisons:  $\leftrightarrow$

# Representative Basic Sorting Algorithms

- ❖ Bubble sort
  - Example)



Comparisons: 19 ↔ 11

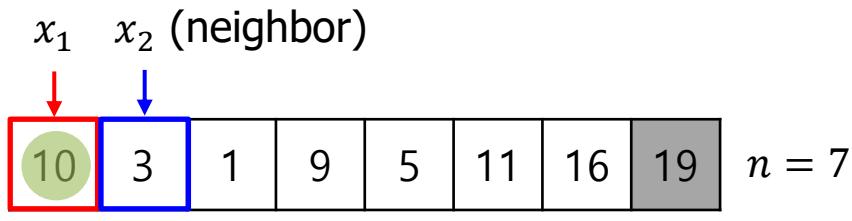
Comparisons: 19 ↔ 16

10	3	1	9	5	11	16	19
----	---	---	---	---	----	----	----

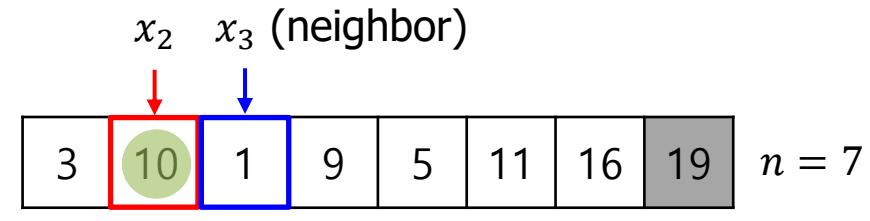
# Representative Basic Sorting Algorithms

## ❖ Bubble sort

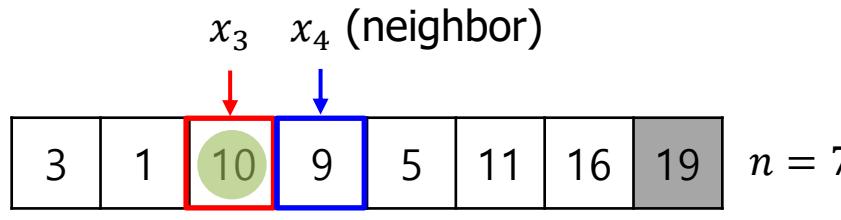
- Example)



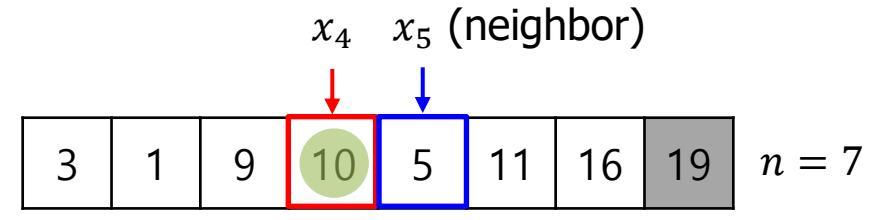
Comparisons:  $10 \leftrightarrow 3$



Comparisons:  $10 \leftrightarrow 1$



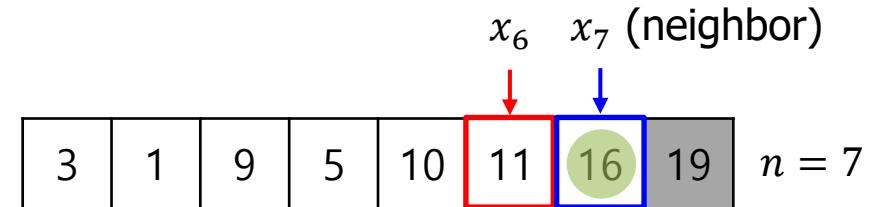
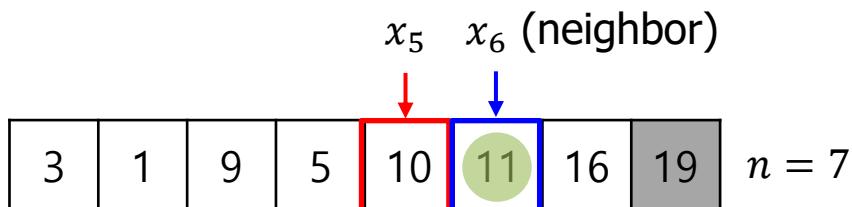
Comparisons:  $10 \leftrightarrow 9$



Comparisons:  $10 \leftrightarrow 5$

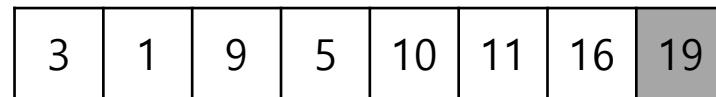
# Representative Basic Sorting Algorithms

- ❖ Bubble sort
  - Example)



Comparisons: 10 ↔ 11

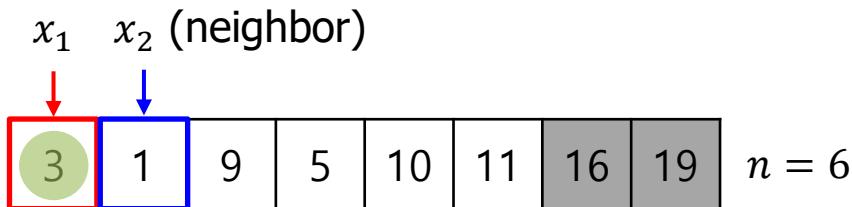
Comparisons: 11 ↔ 16



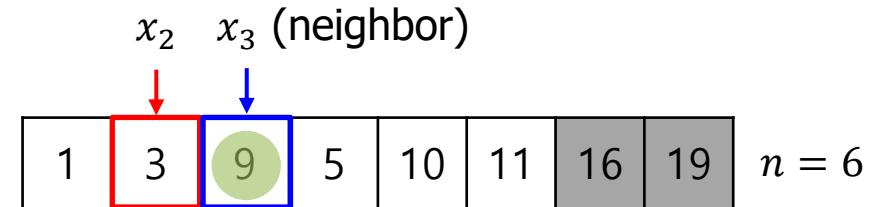
# Representative Basic Sorting Algorithms

## ❖ Bubble sort

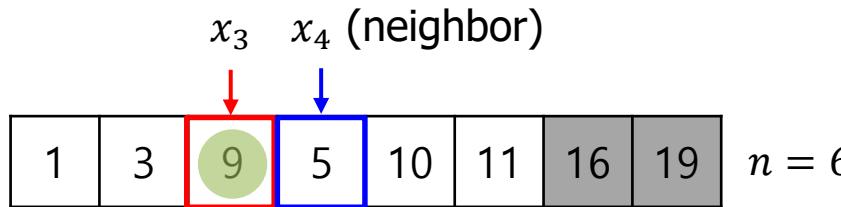
- Example)



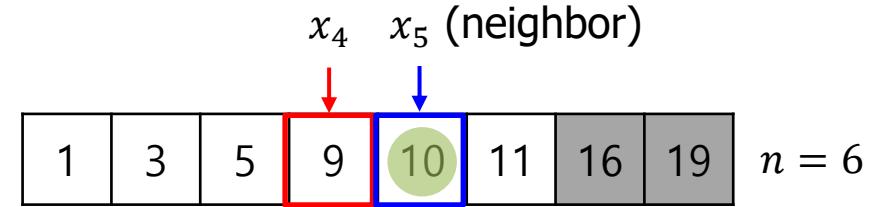
Comparisons:  $3 \leftrightarrow 1$



Comparisons:  $3 \leftrightarrow 9$



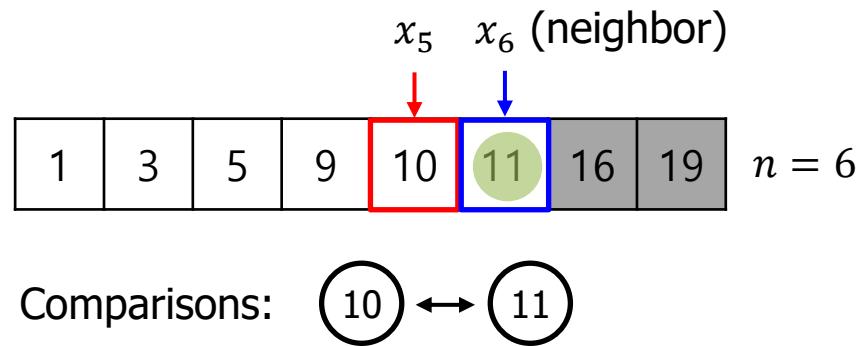
Comparisons:  $9 \leftrightarrow 5$



Comparisons:  $9 \leftrightarrow 10$

# Representative Basic Sorting Algorithms

- ❖ Bubble sort
  - Example)

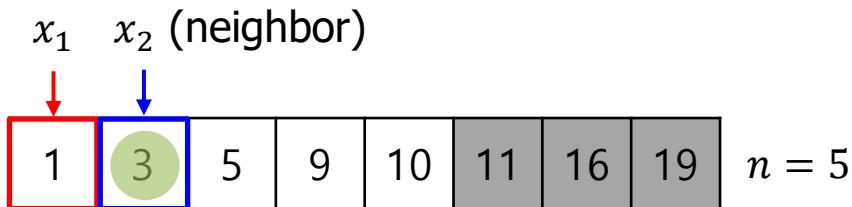


1	3	5	9	10	11	16	19
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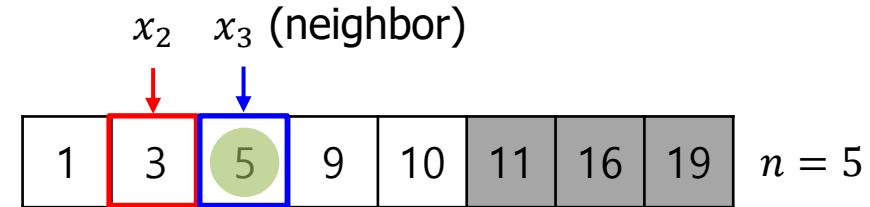
# Representative Basic Sorting Algorithms

## ❖ Bubble sort

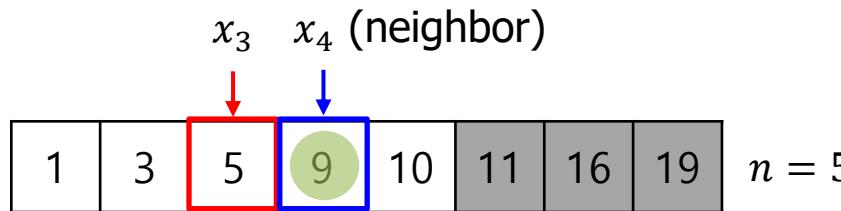
- Example)



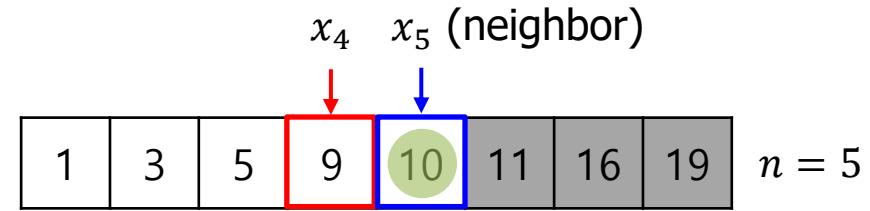
Comparisons:  $1 \leftrightarrow 3$



Comparisons:  $3 \leftrightarrow 5$



Comparisons:  $5 \leftrightarrow 9$

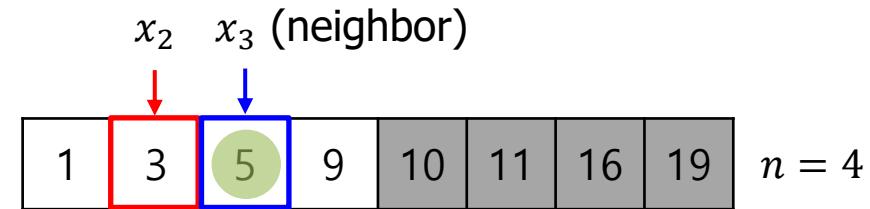
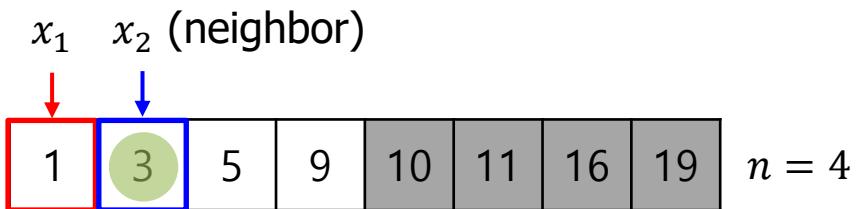


Comparisons:  $9 \leftrightarrow 10$

# Representative Basic Sorting Algorithms

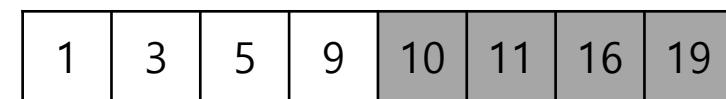
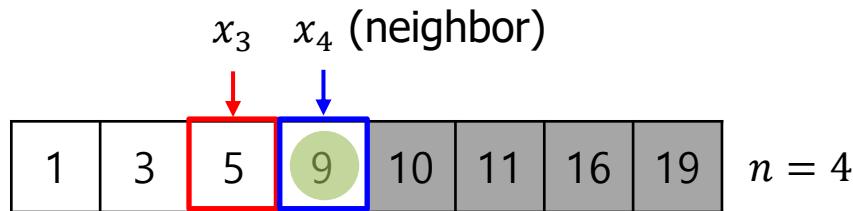
## ❖ Bubble sort

- Example)



Comparisons: 1 ↔ 3

Comparisons: 3 ↔ 5

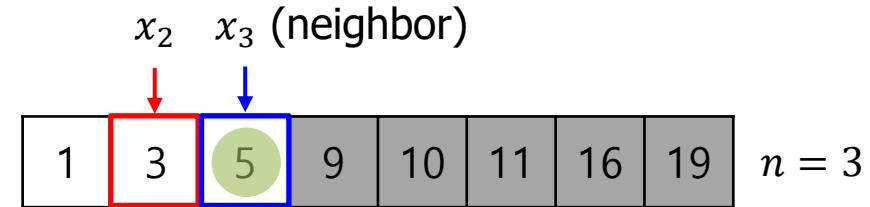
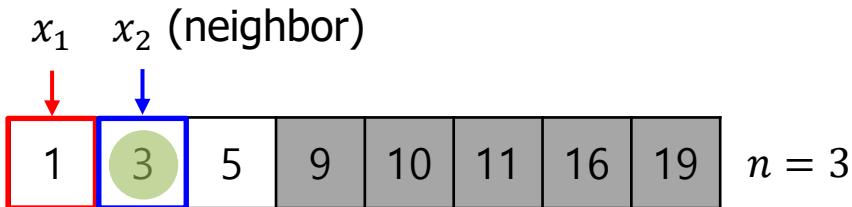


Comparisons: 5 ↔ 9

# Representative Basic Sorting Algorithms

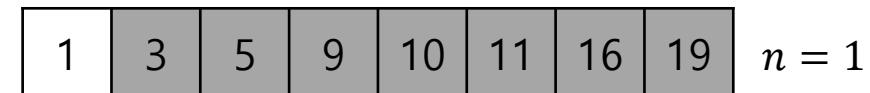
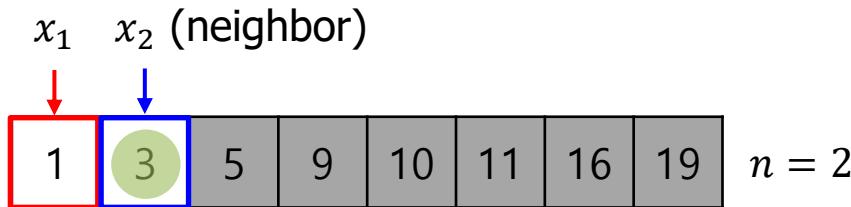
## ❖ Bubble sort

- Example)



Comparisons:  $1 \leftrightarrow 3$

Comparisons:  $3 \leftrightarrow 5$



Comparisons:  $1 \leftrightarrow 3$

# Representative Basic Sorting Algorithms

## ❖ Bubble sort

- Psuedo code)

```
#include <stdio.h>
#include <stdbool.h>

void swap(int *a, int *b){
    int temp = *a;
    *a = *b;
    *b = temp;
}
```

```
void bubble_sort(int arr[], int n){
    int i, j;
    bool swapped;
    for (i = 0; i < n - 1; i++){
        swapped = false;
        for (j = 0; j < n - i - 1; j++){
            if (arr[j] < arr[j + 1]){
                swap(&arr[j], &arr[j + 1]);
                swapped = true;
            }
        }
        if (swapped == false)
            break;
    }
}
```

# Representative Basic Sorting Algorithms

## ❖ Insertion sort

- It uses **two virtual subsets**:
  - Sorted subset  $S$
  - Unsorted subset  $U$
- **In-place** comparison sort
- Time complexity:  $O(n^2)$
- Methodology:

1)  $i = |S|$

2)  $key = (i + 1)\text{-th element } x_{i+1}$

3) Find the insertion position of  $key$ :

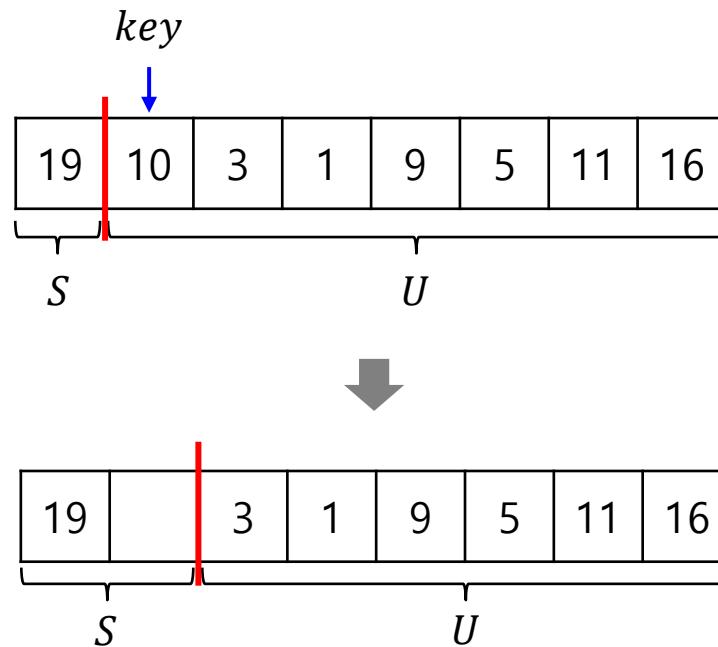
- Compare  $i$ -th element  $x_i$  and  $key$
- If  $x_i > key$ , then  $x_{i+1} = x_i$  and  $i$  is decreased by 1
- Otherwise,  $x_{i+1} = key$
- Repeat 3) step

4) Repeat 1) – 4) steps until  $U = \emptyset$

# Representative Basic Sorting Algorithms

## ❖ Insertion sort

- Example)

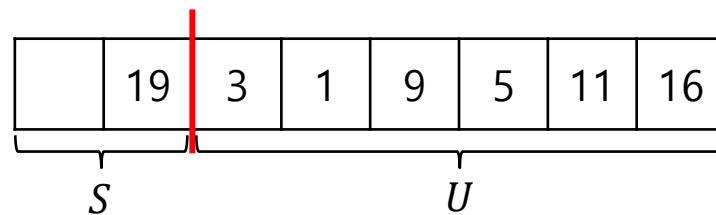
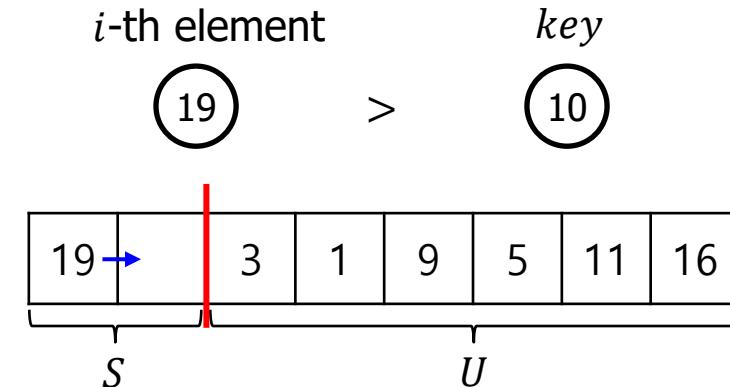


i-th element                      key  
Comparisons:     $\leftrightarrow$     19     $\leftrightarrow$     10

# Representative Basic Sorting Algorithms

## ❖ Insertion sort

- Example)



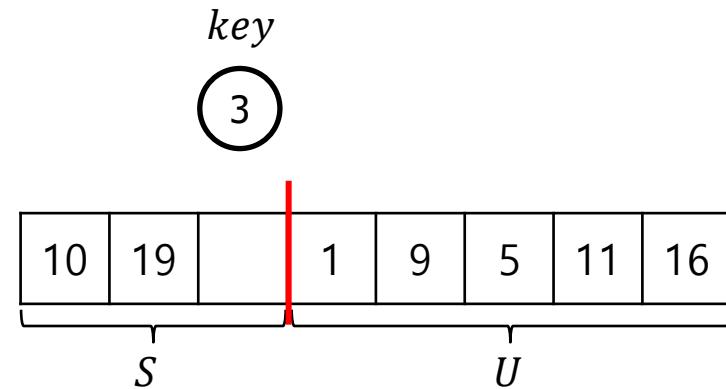
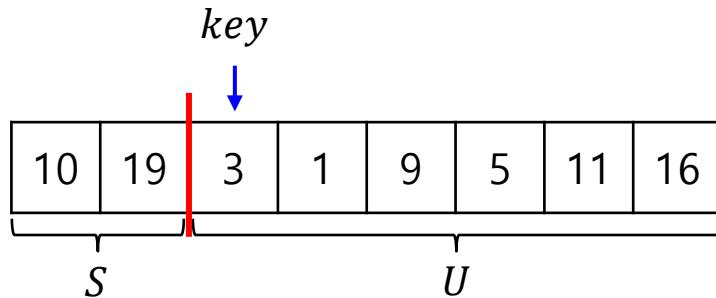
*i*-th element                      key

( )                      =                      (10)

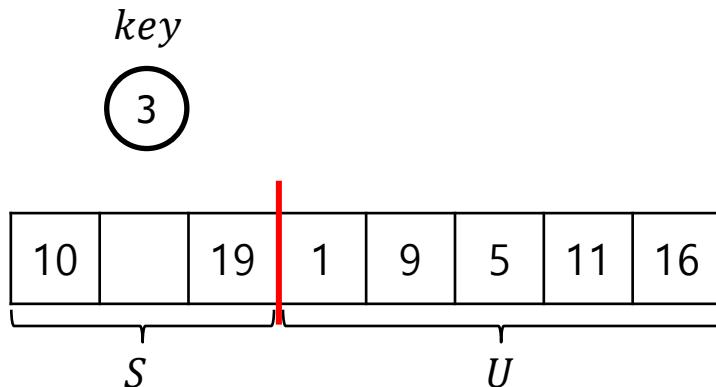
# Representative Basic Sorting Algorithms

## ❖ Insertion sort

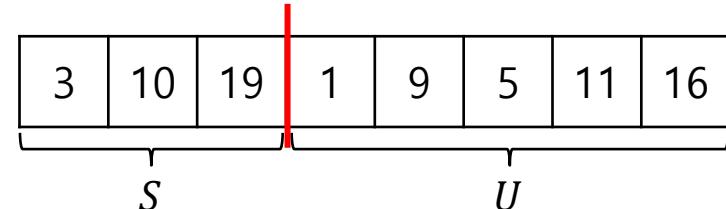
- Example)



Comparisons: 3 ↔ 19



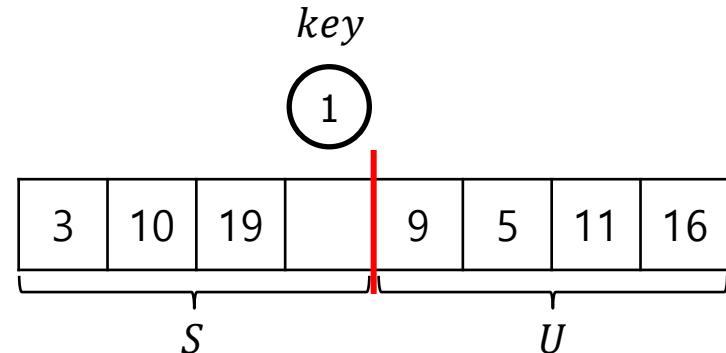
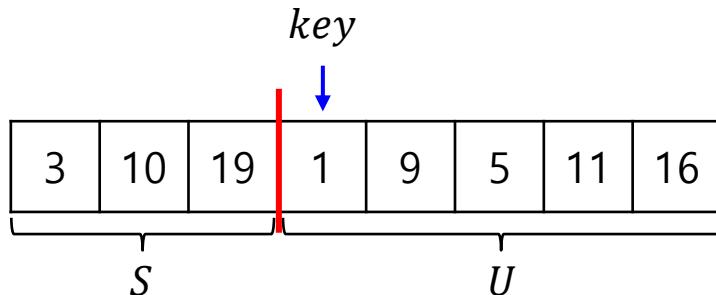
Comparisons: 3 ↔ 10



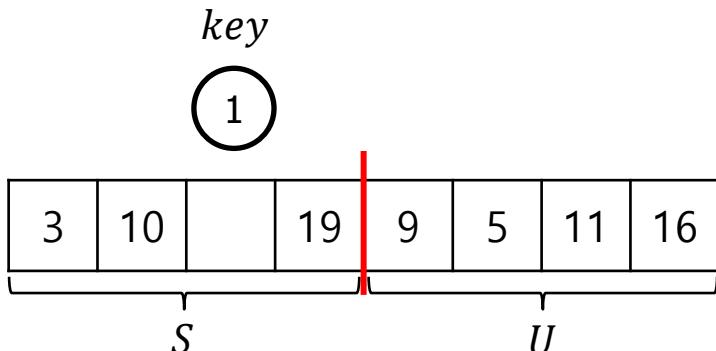
# Representative Basic Sorting Algorithms

## ❖ Insertion sort

- Example)

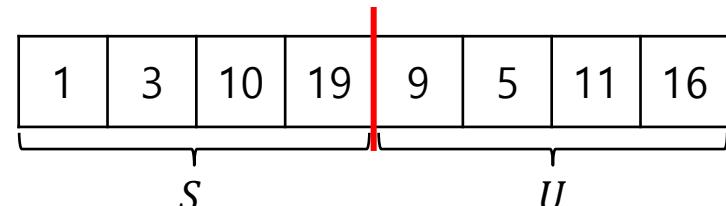


Comparisons: ↔



Comparisons: ↔

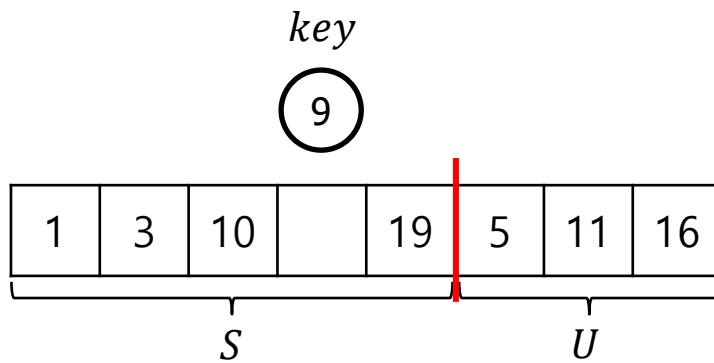
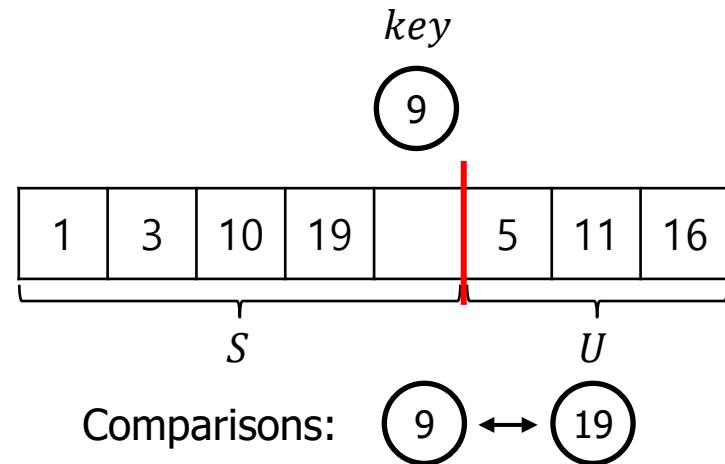
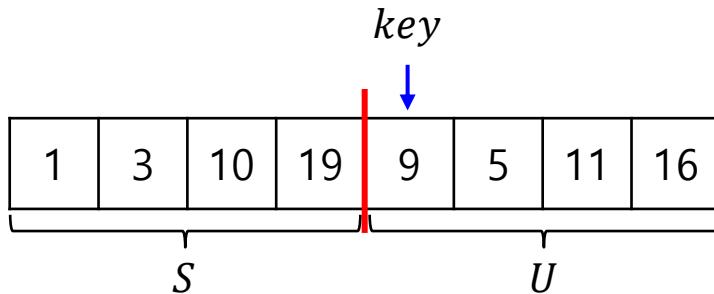
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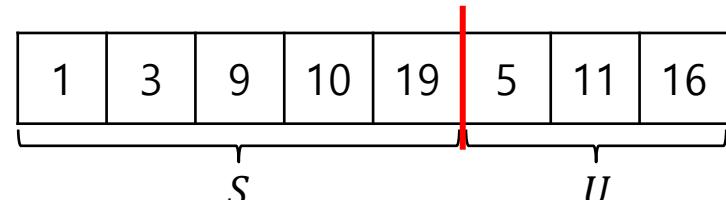
# Representative Basic Sorting Algorithms

## ❖ Insertion sort

- Example)



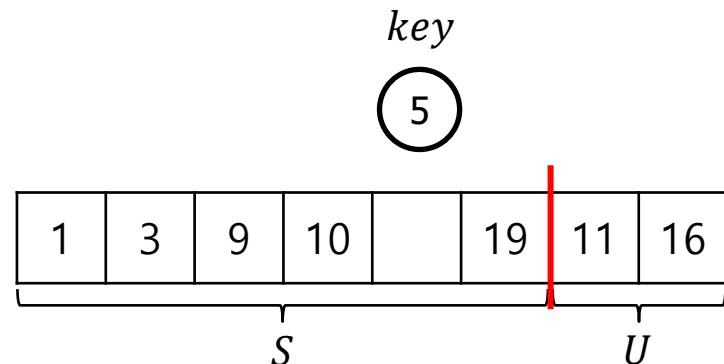
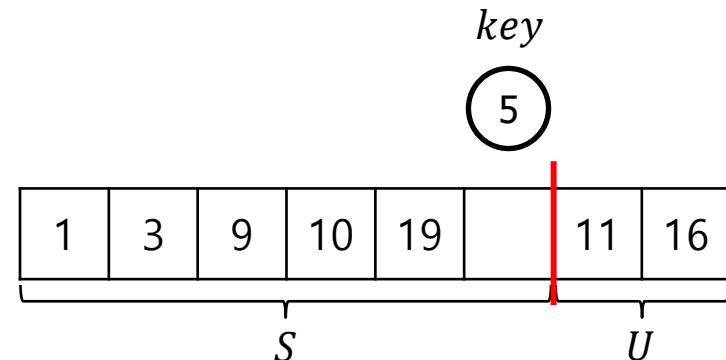
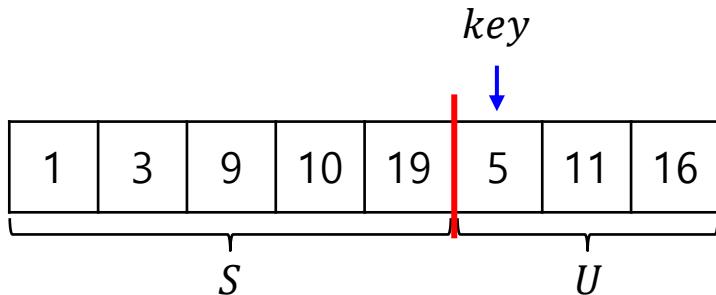
Comparisons: ↔



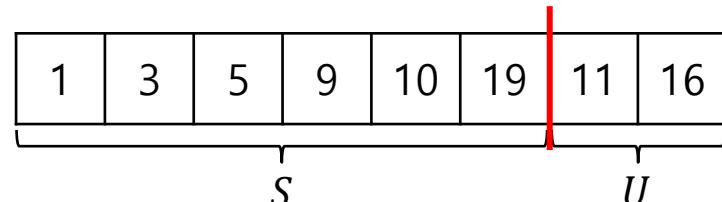
# Representative Basic Sorting Algorithms

## ❖ Insertion sort

- Example)



...

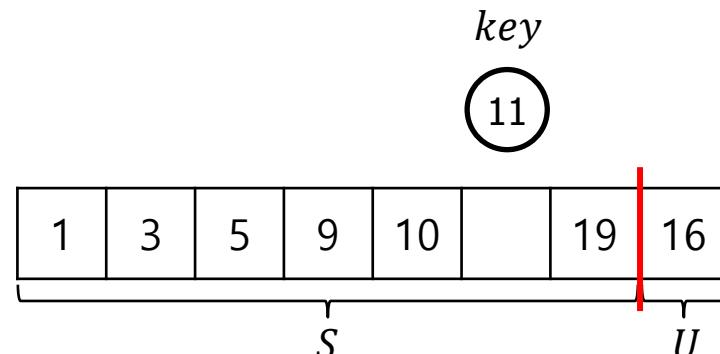
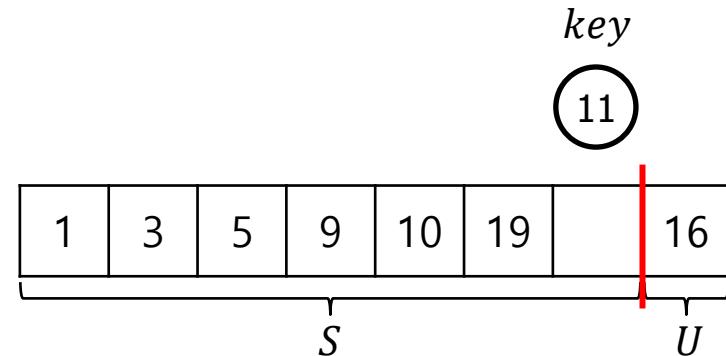
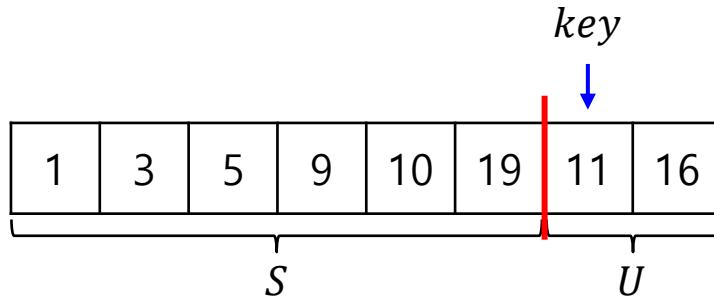


Comparisons:  5 ↔ 10

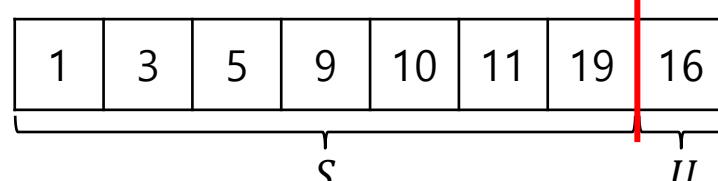
# Representative Basic Sorting Algorithms

## ❖ Insertion sort

- Example)



...

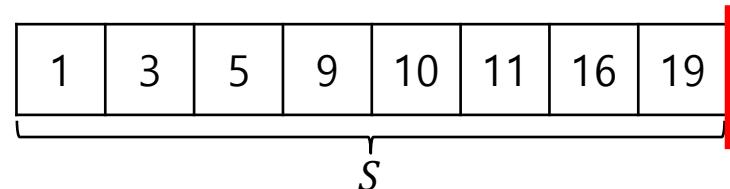
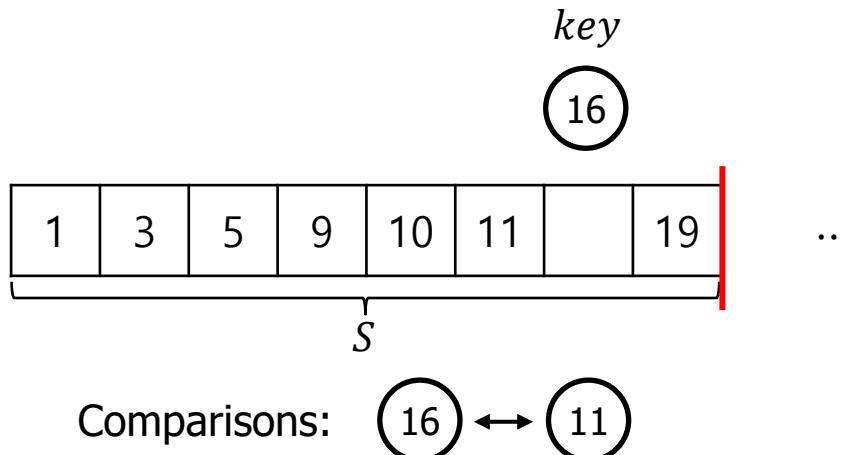
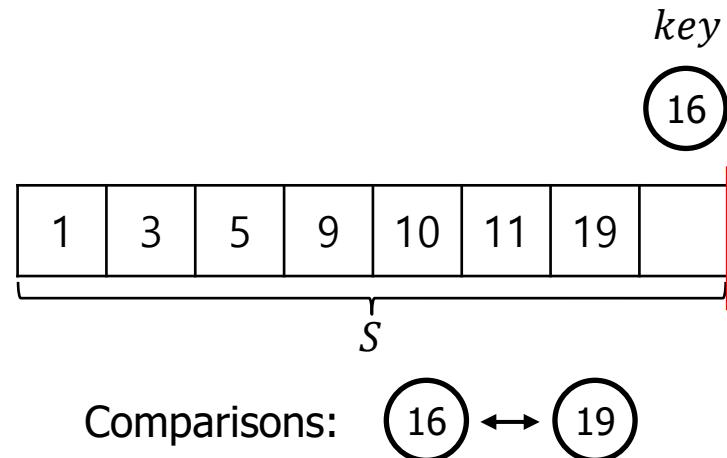
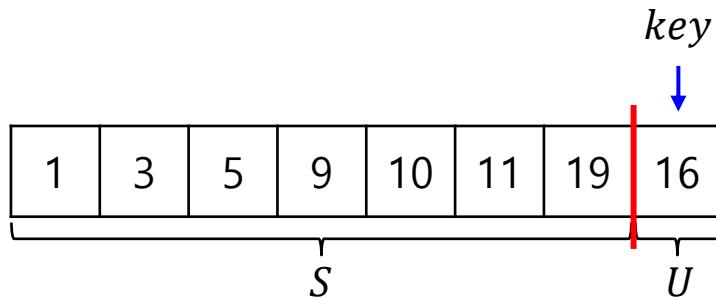


Comparisons:  

# Representative Basic Sorting Algorithms

## ❖ Insertion sort

- Example)



# Representative Basic Sorting Algorithms

## ❖ Insertion sort

- Psuedo code)

```
#include <stdio.h>
#include <math.h>

void insertion_sort(int arr[], int n){
    int i, j, key;
    for (i = 1; i < n; i++){
        key = arr[i];
        j = i - 1;
        while(j >= 0 && arr[j] > key){
            arr[j + 1] = arr[j];
            j = j - 1;
        }
        arr[j + 1] = key;
    }
}
```

# Summary

- ❖ Sorting problem
- ❖ Sorting algorithms
  - Basic sorting algorithms
    - Selection sort
    - Bubble sort
    - Insertion sort
  - Advanced sorting algorithms
    - Shell sort
    - Merge sort
    - Quick sort
    - Heap sort
    - Etc.

Questions?

**SEE YOU NEXT TIME!**