

$$\left. \begin{aligned} \frac{dV}{dx} &= -(R + j\omega L) I \\ \frac{dI}{dx} &= -(G + j\omega C) V \end{aligned} \right\} \rightarrow \begin{aligned} \frac{d^2 V}{dx^2} &= \Gamma^2 V \\ \frac{d^2 I}{dx^2} &= \Gamma^2 I \end{aligned}$$

$$\Gamma = \alpha + j\beta = \sqrt{(R + j\omega L)(G + j\omega C)}$$

$$\alpha - \text{Nepers/m}, 1 \text{ nep/m} = 0.68 \text{ dB/m}$$

$$\beta = \frac{2\pi}{\lambda}$$

$$Z_0 = \sqrt{\frac{R + j\omega L}{G + j\omega C}}$$

$$\text{Lossless: } \alpha = 0 \Rightarrow R = 0, G = 0$$

$$\Gamma = j\omega\sqrt{LC}, Z_0(\text{real}) = \sqrt{\frac{L}{C}}, v_p = 3 \times 10^8 \text{ m/s}$$

Distortion less:

- Equal rise and fall time

- series time constant = shunt time constant

$$RC = LG$$

$$\Gamma = \sqrt{RG} \left(1 + j\omega \frac{L}{R}\right); Z_0 = \sqrt{\frac{R}{G}} \text{ (real)}$$

$$v_p = \text{constant}$$

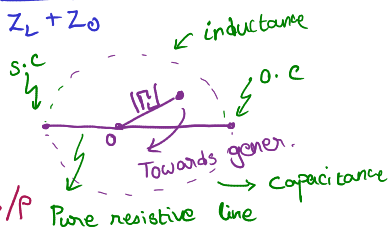
- α depends on $\omega \rightarrow$ delay distortion

β depends on $\omega \rightarrow$ freq. distortion

$$\text{Reflection coefficient } \Gamma = \frac{Z_L - Z_0}{Z_L + Z_0}$$

$$\text{VSWR: } \rho = \frac{1 + |\Gamma_L|}{1 - |\Gamma_L|}$$

$$R_{\max} = Z_0 \rho, R_{\min} = Z_0 / \rho$$



$$Z_L = \begin{cases} jZ_0 \tan \beta l & \rightarrow \text{s.c} \\ -jZ_0 \cot \beta l & \rightarrow \text{o.c} \end{cases}$$

$$Z_L \rightarrow \begin{aligned} &\xrightarrow{\lambda/4, \lambda/4} \frac{Z_0^2}{Z_L} \\ &Z_L = \frac{Z_0^2}{Z_L} \end{aligned}$$