

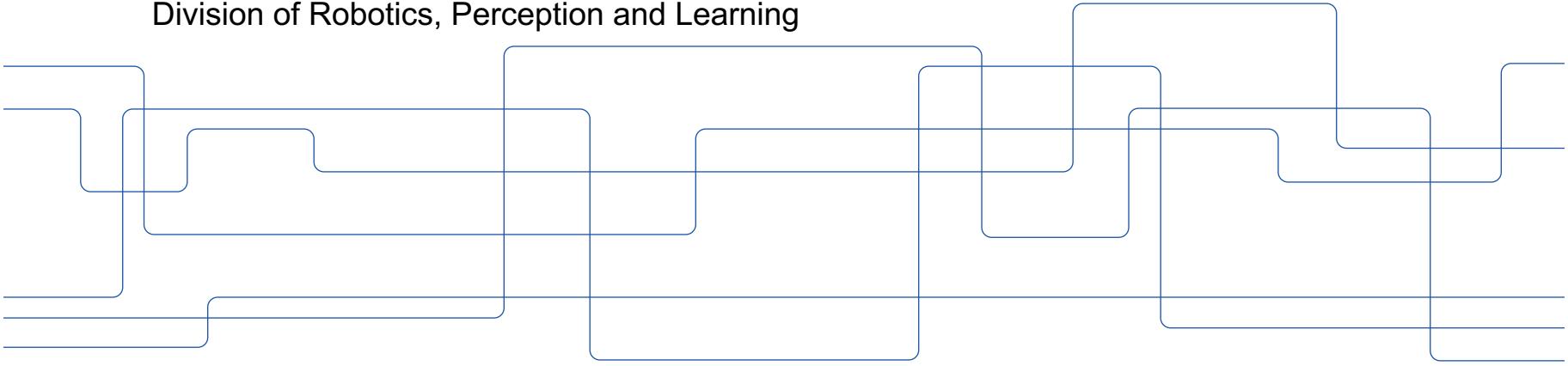


Formal methods for robot planning

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Why formal methods?

Rigorous techniques for
specification



How do we tell
robots what to do?

development,
verification,
analysis of systems



How do we ensure
that they behave
as expected?



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Why temporal logics and formal synthesis?

Temporal logics

- rich
- rigorous
- resemblance to natural language



How do we tell robots what to do?

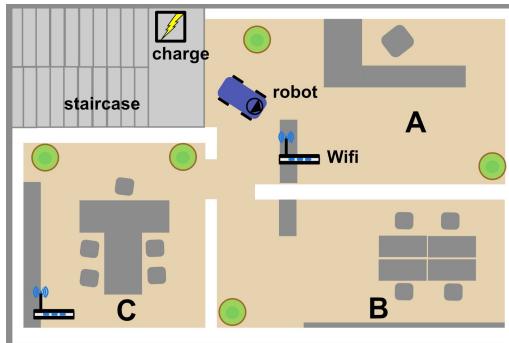
Formal synthesis



How do we ensure that they behave as expected?



Temporal logic for mission and motion objectives



- Keep patrolling the three offices.
$$GF(A) \wedge GF(B) \wedge GF(C)$$
- Whenever you spot danger, go directly to the staircase and wait for “all clear” signal before continuing.
$$G(\text{danger} \Rightarrow X(\text{staircase} U \text{all_clear}))$$
- Make sure to recharge at least every 10 minutes.
$$GF_{[0,10]} \text{recharge}$$
- At all times, stay within 5 meters from the wi-fi router.
$$G(\text{Dist}(\text{robot}, \text{router}) \leq 5)$$



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Why temporal logics and formal synthesis?

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How do we tell
robots what to do?

Formal synthesis

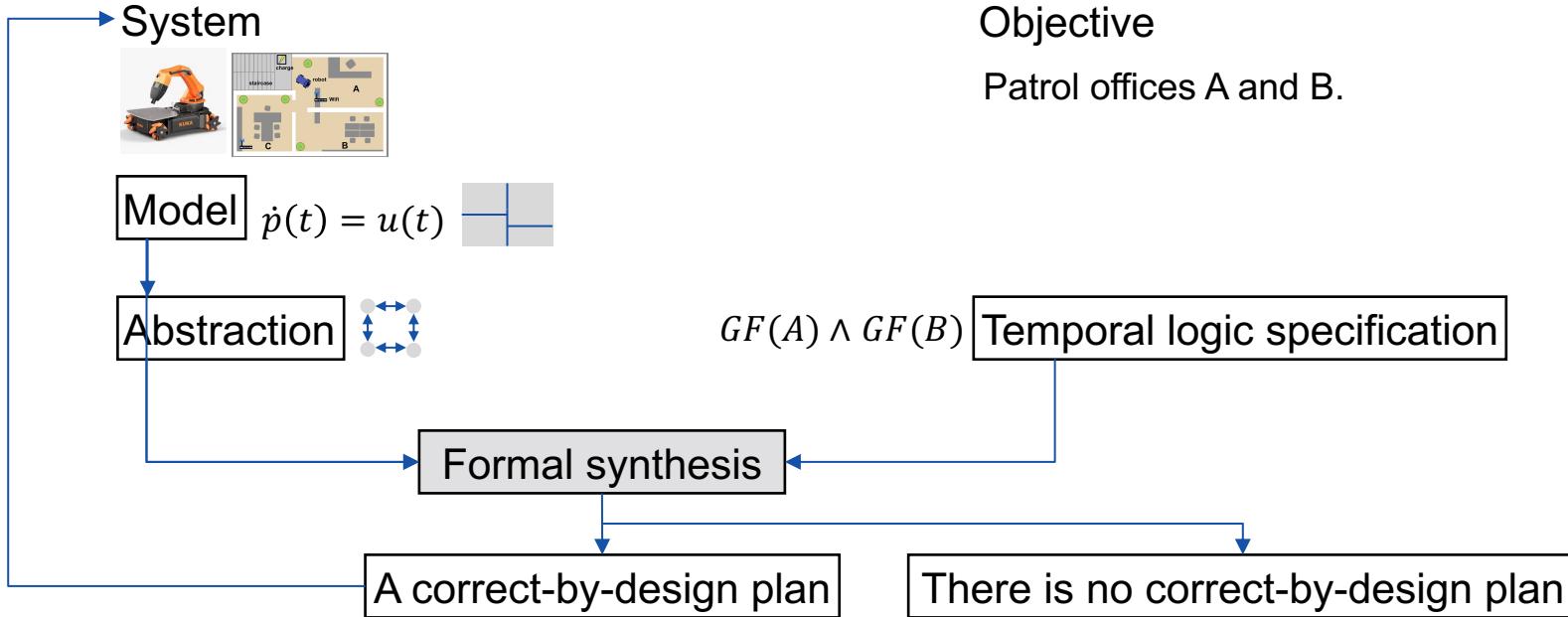
- correct-by-design plan



How do we ensure
that they behave
as expected?

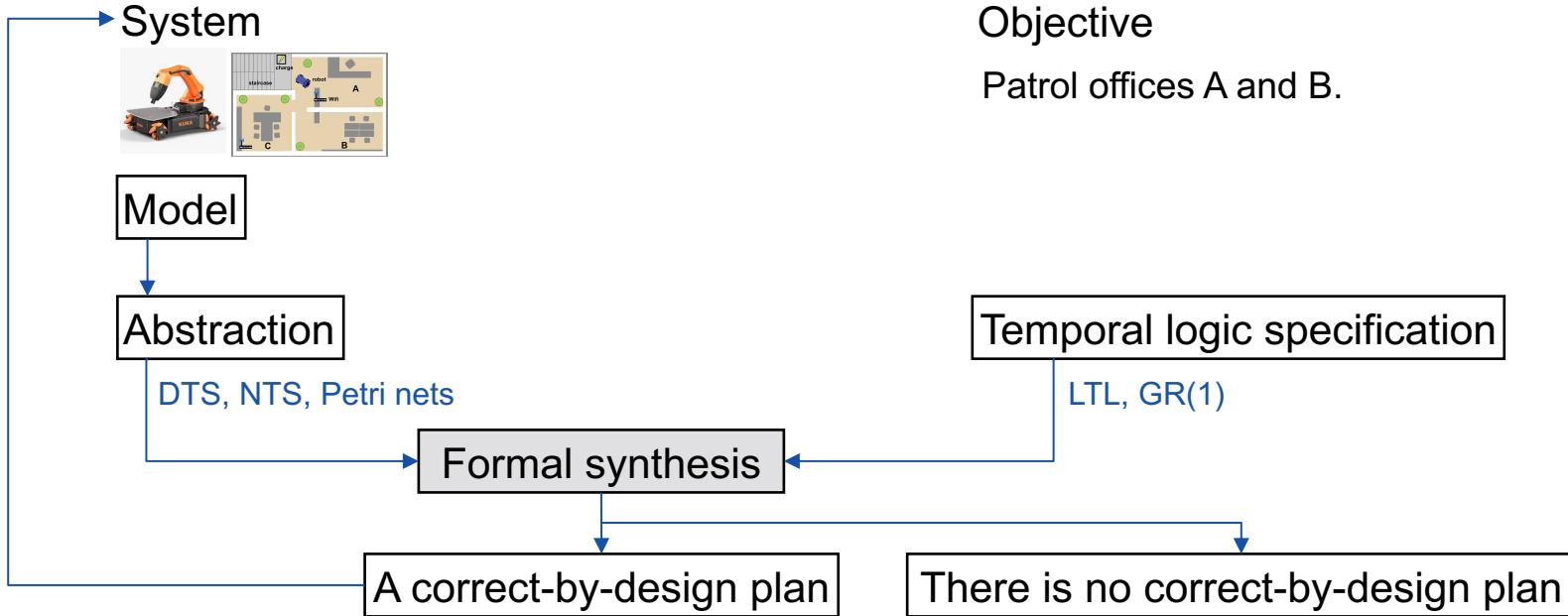


Formal synthesis





Formal synthesis (2009)

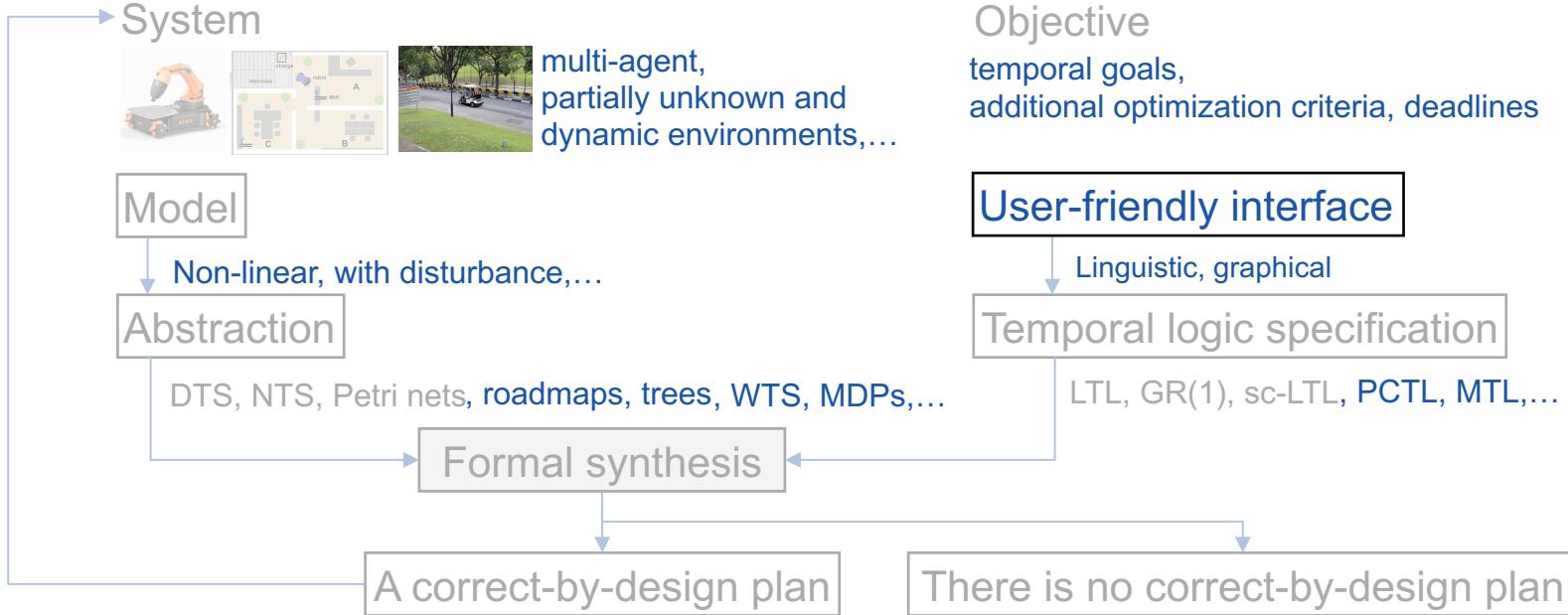


Some seminal works:

[Kress-Gazit et al, TRO 2009, Kloetzer and Belta, TAC 2008]

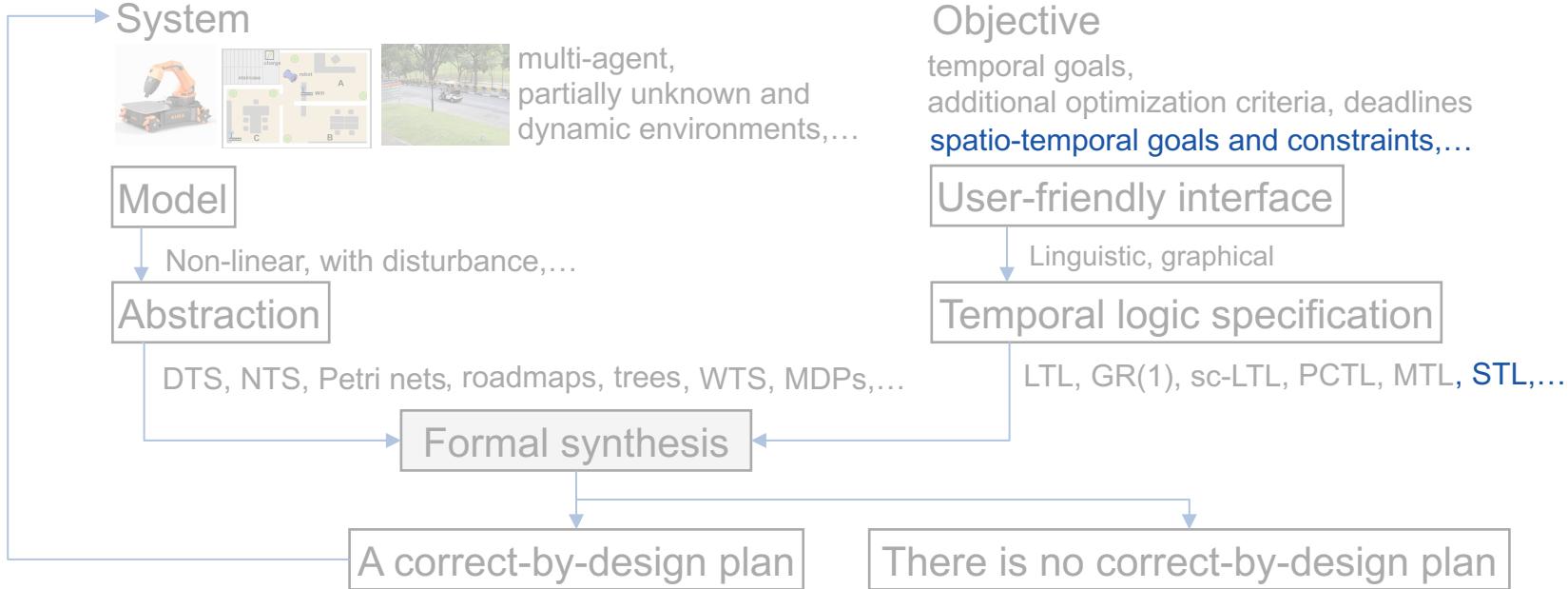


Formal synthesis (2013)





Formal synthesis (today)





Formal synthesis, integrated



Multi-robot coordination
for dynamic production assistance



BOSCH
Invented for life



National
Technical
University of
Athens

PAL
ROBOTICS



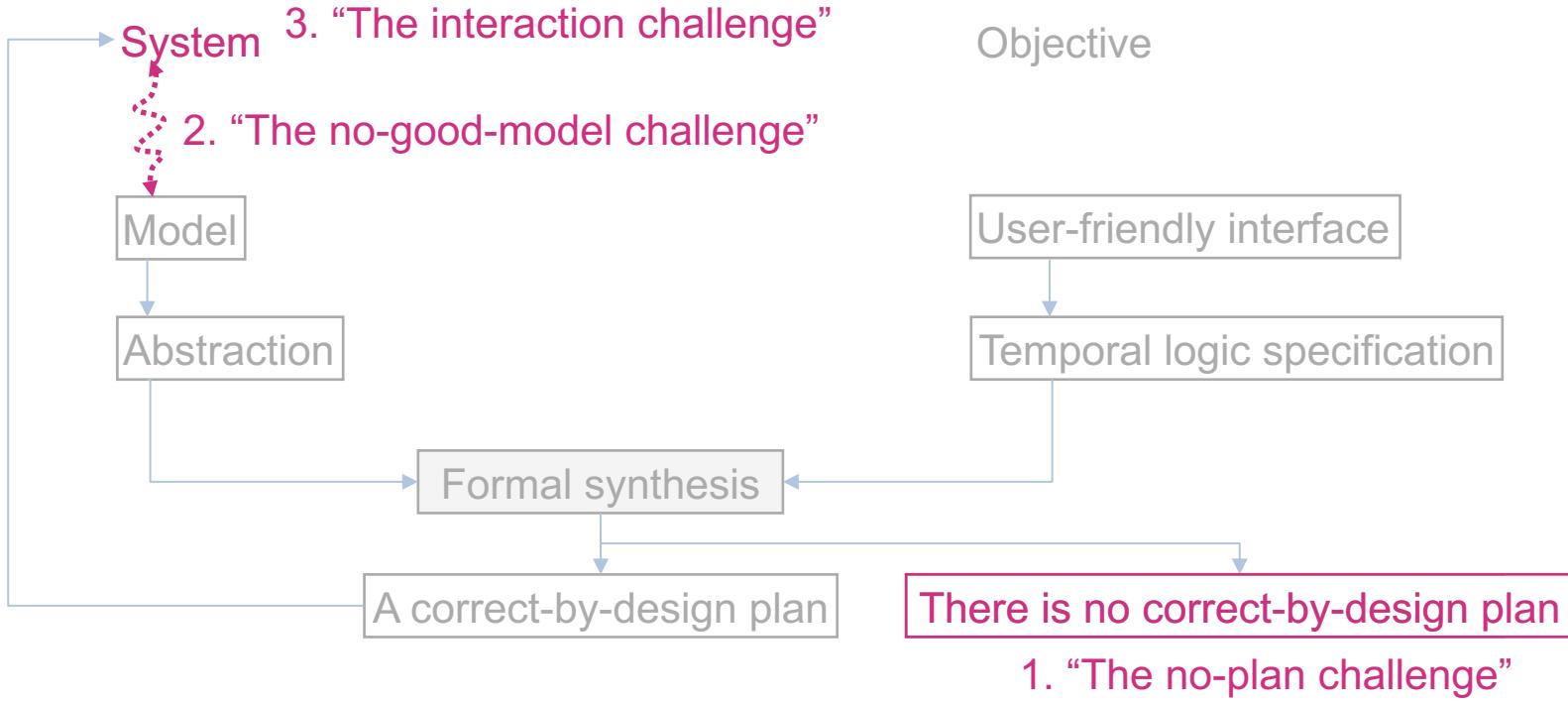
FORTH
Foundation for Research & Technology



www.co4robots.eu

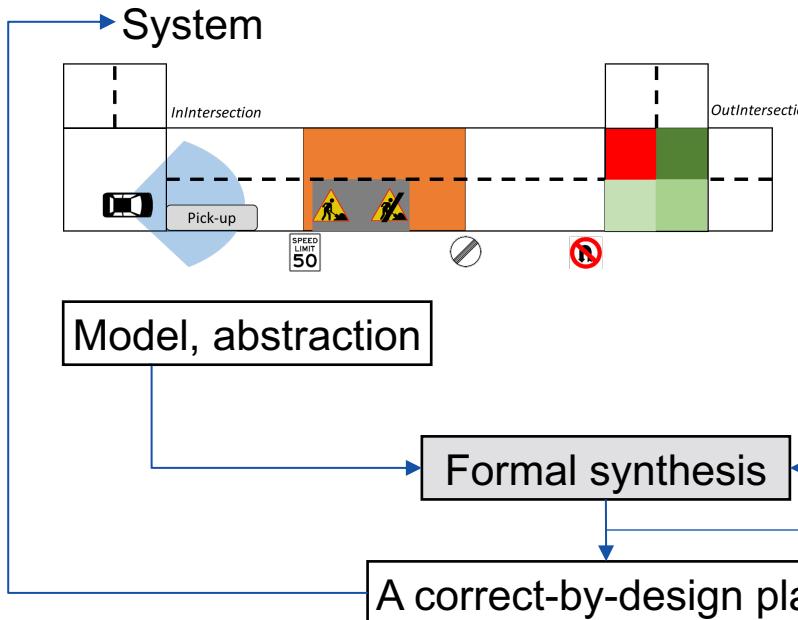


Three challenges of formal synthesis





1. The no-plan challenge



Objective

Obey the traffic rules:

- Do not cross the full lane
- Stay in the right lane
- Do not enter the construction zone
- Do not enter sidewalk

...

Temporal logic specification

LTL over finite traces

There is no correct-by-design plan

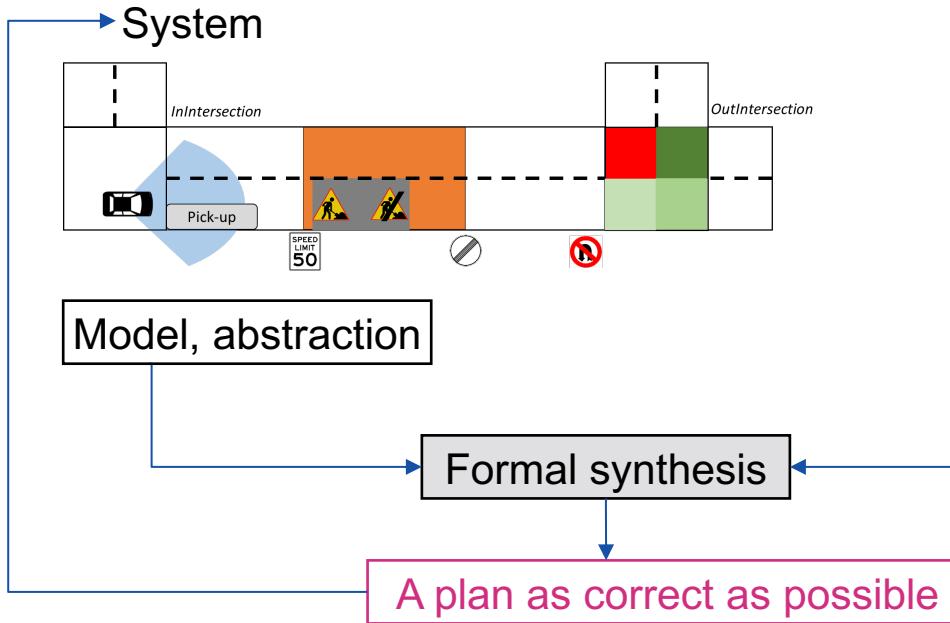
All the traffic rules cannot be obeyed simultaneously



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1. The no-plan challenge



Objective

Obey the traffic rules:

- Do not cross the full lane
- Stay in the right lane
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- Do not enter sidewalk

...

Temporal logic specification

LTL over finite traces

The traffic rules are violated only for the absolutely necessary, for the necessary time



Quantitative evaluation of LTL

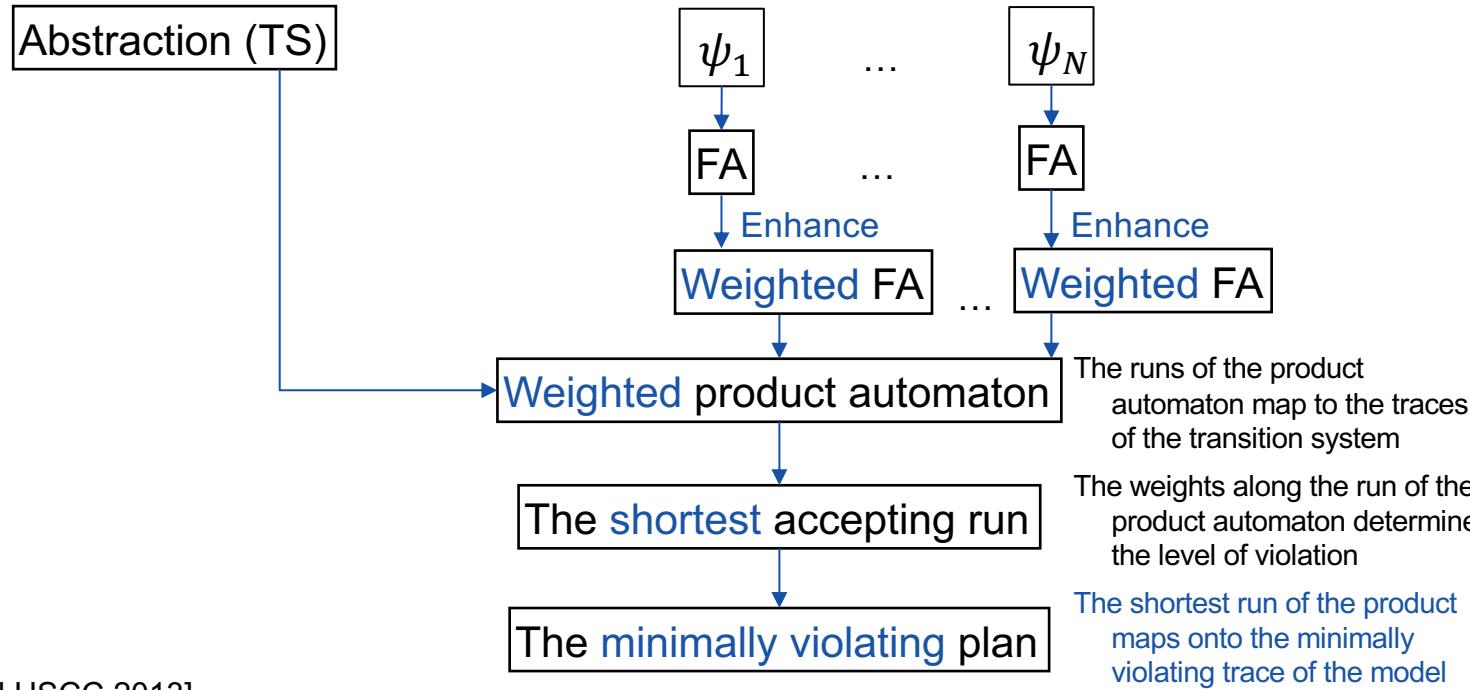
Assume a transition system from RRT* or other abstraction

Level of violation $\lambda(trace, LTL\ formula)$: the time duration associated with the discrete transitions that need to be removed to make the trace satisfy the LTL formula, weighted by the penalty





Minimum-violation automata-based FS



[Tumova et al HSCC 2013]





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MV-RRT*

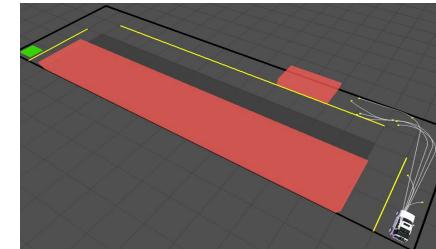
- Incrementally build
- Incrementally update
- Optimality criterion

RRT*

weighted tree
shortest path
distance

MV-RRT*

weighted product automaton
minimally violating path
primarily level of violation, then distance



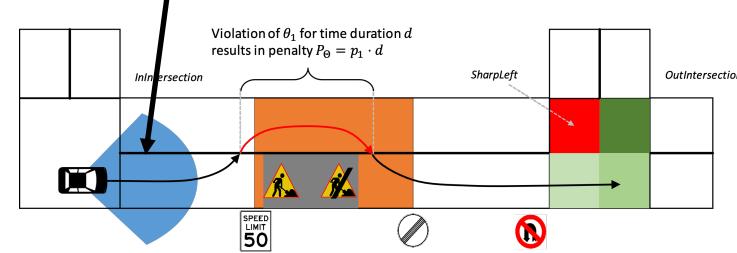
[Reyes-Castro et al CDC 2013]



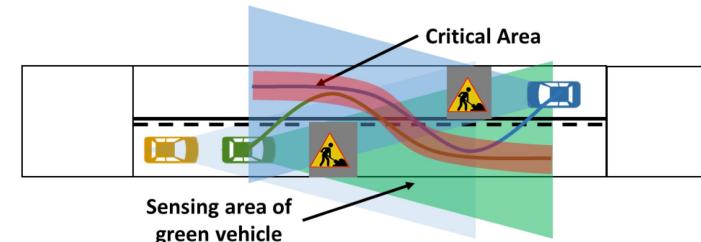
MV-RRT* in autonomous driving



Limited sensing:



Multi-vehicle settings:

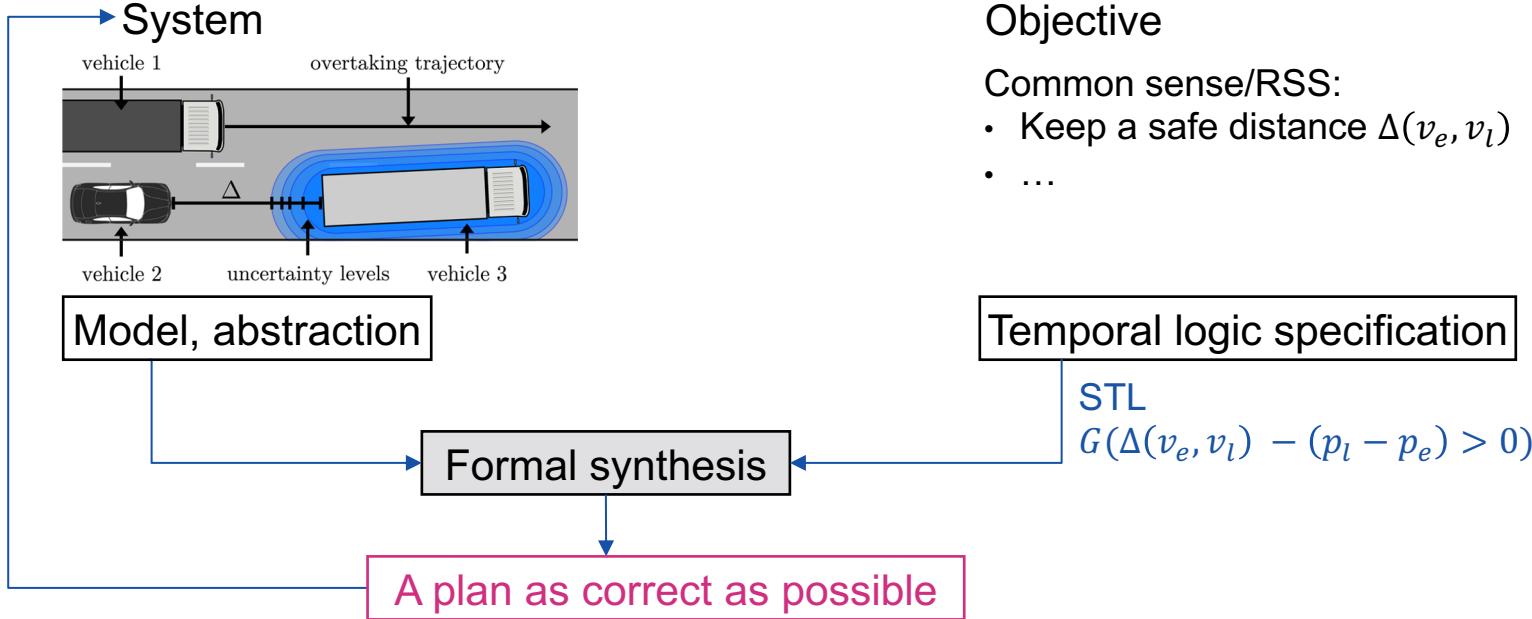


[Reyes-Castro et al HSCC 2013, Vasile et al ICRA 2017, Karlsson et al ICRA 2018, CASE 2020, ICRA 2021]





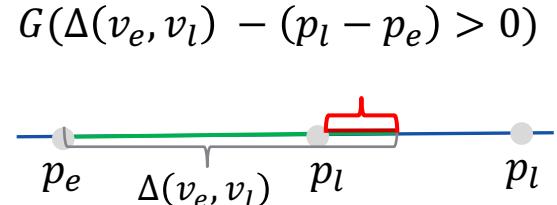
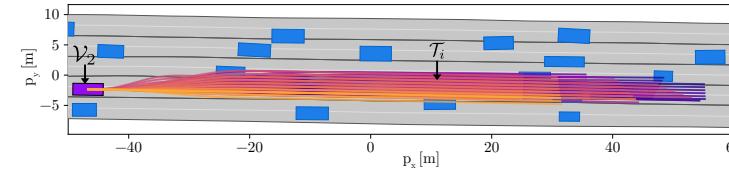
The no plan challenge under uncertainty



The severity of violation, the probability of violation, and the level of uncertainty are taken into account



Risk-aware planning in autonomous driving

- Safety specification: $G(h(x(t)) > 0)$
 - Severity function: $\ell_h(x) = \begin{cases} \ell(h(x(t))), & h(x(t)) > 0 \\ 0, & \text{otherwise} \end{cases}$
 - Severity of violation: $L = l_h(\hat{x})$
 - Risk: $E[L]$
 - Risk-aware planning
- 
- 

[Nyberg et al IV 2021]



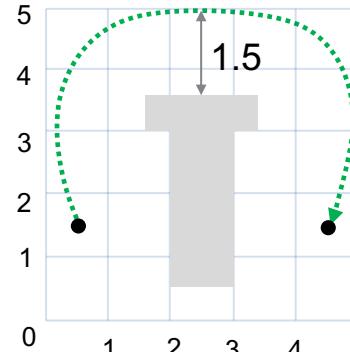


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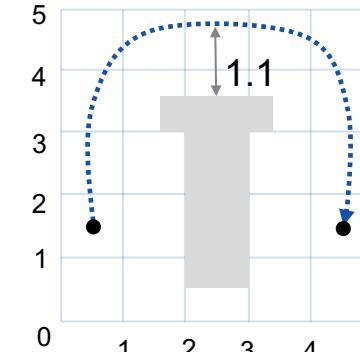


Signal Temporal Logic spatial robustness

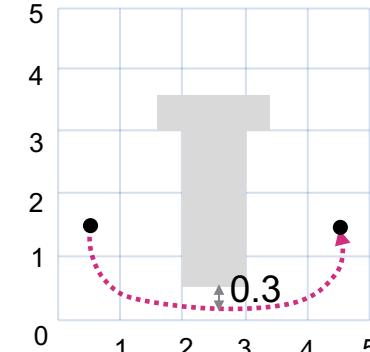
$$G(1 - \text{dist}(\sigma, M) > 0)$$



0.5



0.1



-0.7

See [Donze and Maler, LNCS, 2013]



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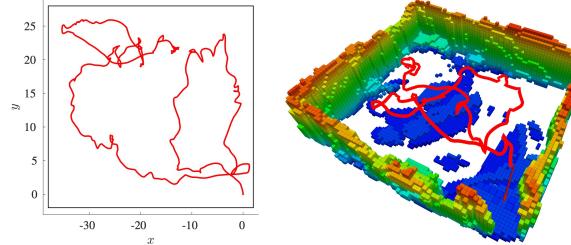
STL as a preference specification



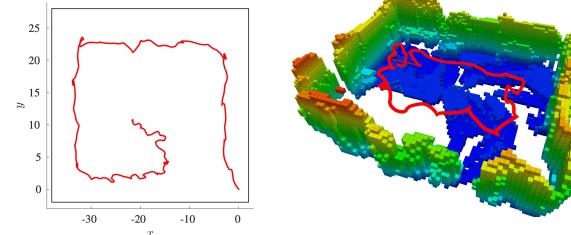


STL-guided autonomous exploration

AEP



AEP + STL $G(\text{dist}(\sigma, M) - 1 > 0)$



[Barbosa et al RA-L 2019]

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Guiding Autonomous Exploration
with Signal Temporal Logic

Fernando S. Barbosa, Daniel Duberg, Patric Jensfelt and Jana Tumova





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2. The no-good-model challenge





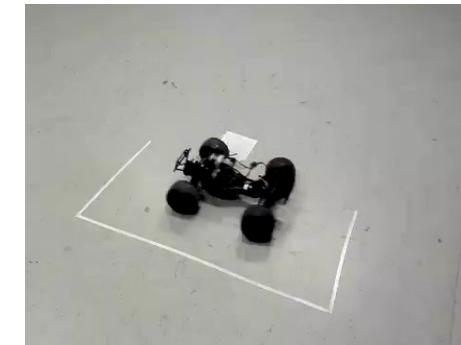
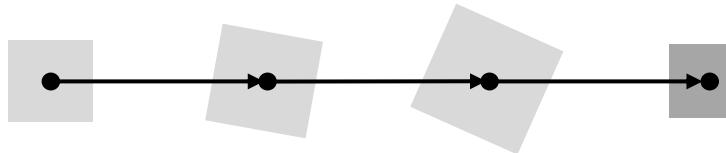
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Safe multi-step feedback motion primitives

for non-holonomic system with bounded disturbance

- Divide the input space into regions & linearize
- Linearization introduces error

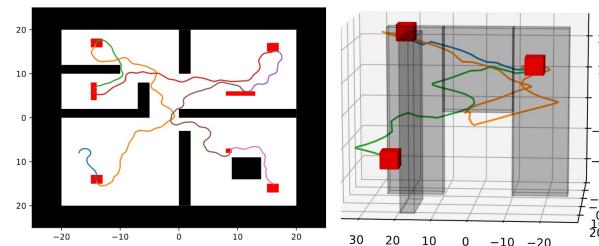
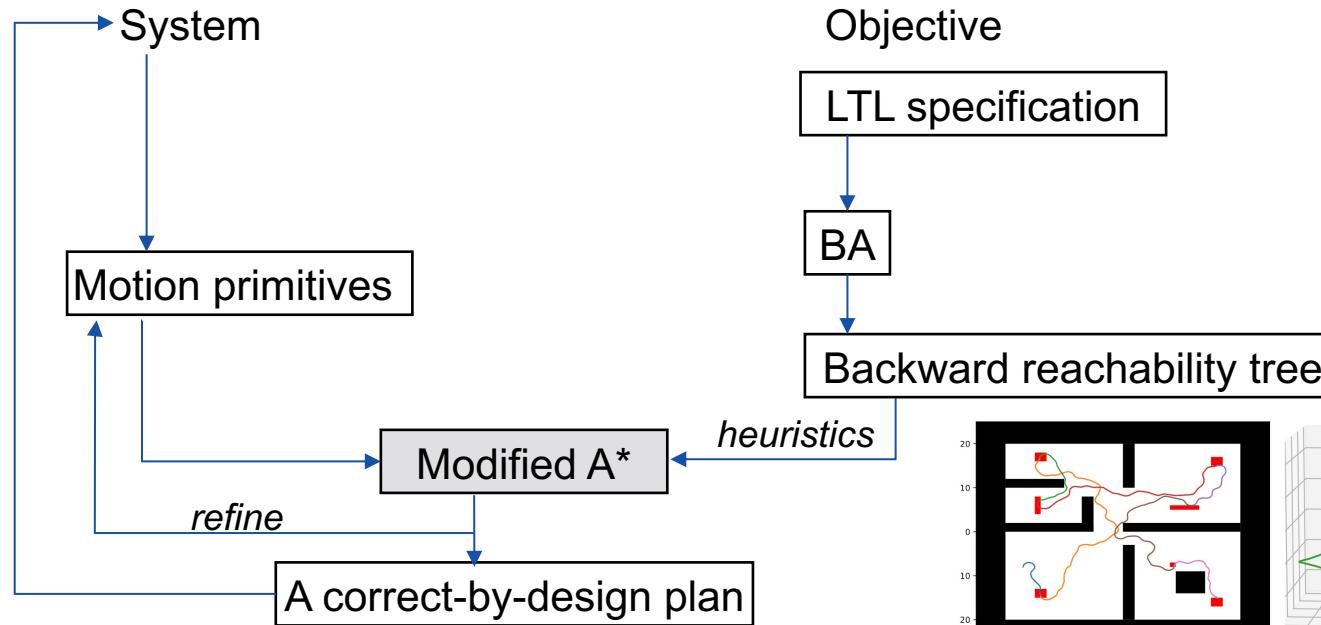


- The error can be corrected in k steps
- The motion primitives can be chained and refined





LTL planning with motion primitives



[Tajvar et al CASE 2020]

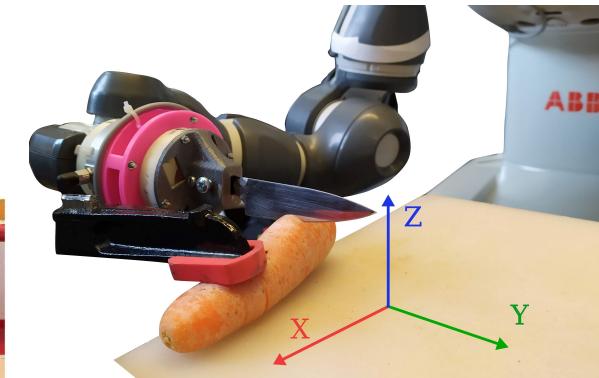
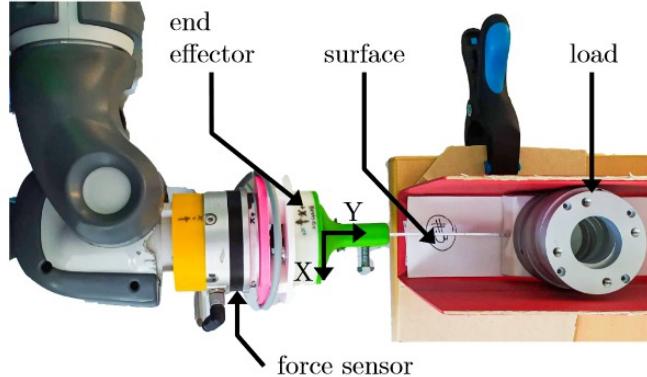




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Towards safe data-driven contact-rich manipulation



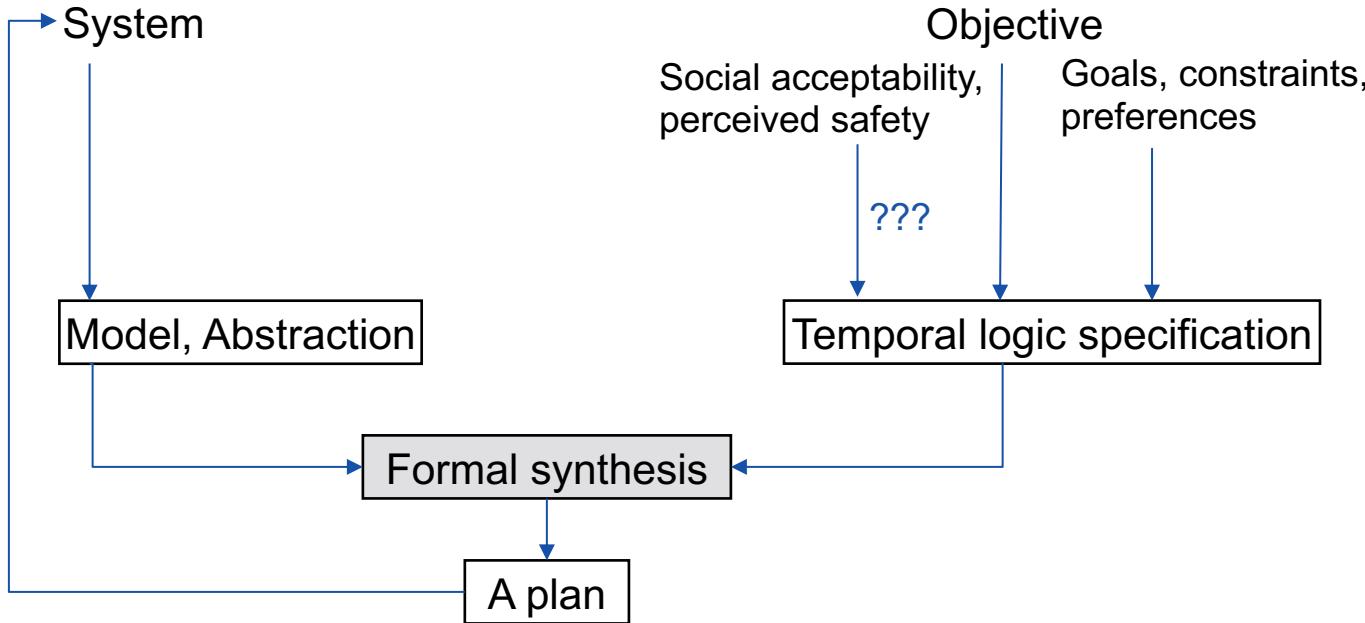


The ~~smart city~~ interactive challenge



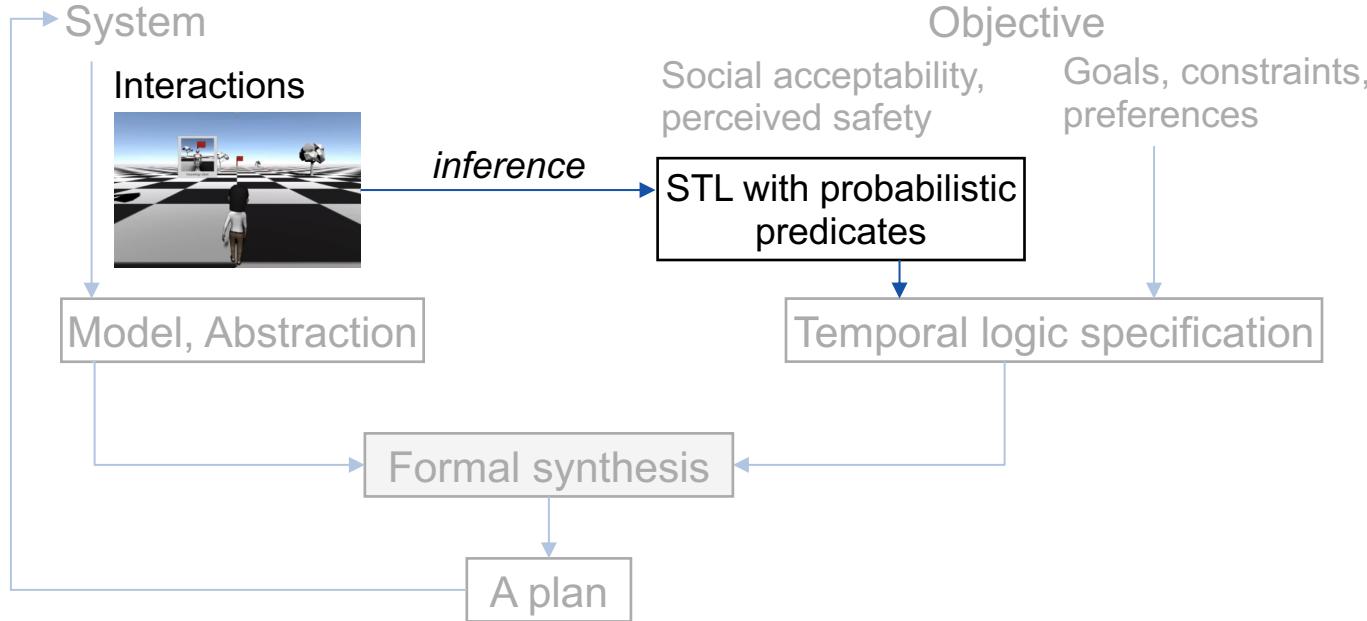


Correct-by-design and socially acceptable plan





Correct-by-design and socially acceptable plan





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I wish I had time to talk also about

- Provable safety vs. perceived safety
- Assumption-guarantee synthesis



- Decentralized multi-agent coordination with temporal logic specifications



Take-aways

- Temporal logics and formal synthesis to address
 - How do we tell robots what to do?
 - How do we ensure that they behave as expected?
- Rigorous, **but not rigid**:
 - Can be used to provide guarantees if that is desired and possible
 - No need to freeze if a correct-by-design plan does not exist
 - Support for preferences, not just mission/safety-critical goals



The future: Moving forward to the wild

- Well-defined mathematical objectives → “Soft” objectives
- Guarantees → Risk-awareness
- Manually created models → Data-driven models and specifications and specifications
- FS or learning → FS and learning
RL with TL goals, RL with TL constraints,
- Component-view → System-view



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ROBOTICS SCIENCE AND SYSTEMS



Thanks!



Pouria Tajvar, Truls Nyberg, Fernando Barbosa, Wei Wang,
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