

Control of Linear Vibrations  
Automation and Control Laboratory  
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# Chapter 1

## Model

$$\left(\frac{J}{R_d} + M\right)\ddot{x} + C\dot{x} + Kx = \frac{r(t)}{R_d} - \mu \operatorname{sign}(\dot{x})$$

$$\theta = \frac{x}{R_d}$$

$$\mathcal{L}\{r(t)\} = 2K_e \frac{1}{2R + 2sL} (\mathcal{L}\{v(t)\} - 2K_e s \mathcal{L}\{\theta\})$$

1.  $\mathcal{L}\{\cdot\}$  Laplace transform.
2.  $J$  Disk inertia.
3.  $M$  Cart+load mass
4.  $C$  Spring damping.
5.  $K$  Spring stiffness.
6.  $r(t)$  Torque.
7.  $R_d$  Disk radius.
8.  $\mu$  Coloumb friction coefficient.
9.  $\theta$  angle of the disk.
10.  $v(t)$  tension applied to the motor.
11.  $R, L$  resistance and inductance of the motor
12.  $K_e$  backemf constant.