

CIS 27: Data Structures and Algorithms

Answer to Question 1

Expressions from slowest to fastest:

$$n!, 3^n, 4n^2, 20n, n^{2/3}, \log_2 n, \log_3 n, 2$$

Answer to Question 2

(a)

$$3 \times 2^x = 64 \times 3 \times 2^n$$

$$3 \times 2^x = 3 \times 2^n \times 2^6$$

$$3 \times 2^x = 3 \times 2^{n+6}$$

$$x = n + 6$$

(b)

$$x^2 = 64 \times n^2$$

$$\sqrt{x^2} = \sqrt{64n^2}$$

$$x = 8n$$

(c)

$$8x = 64 \times 8n$$

$$x = \frac{64 \times 8n}{8}$$

$$x = 64n$$

Answer to Question 3

(n)

$$x = 100n$$

(n²)

$$x^2 = 100 \times n^2$$

$$\sqrt{x^2} = \sqrt{100n^2}$$

$$x = 10n$$

(n³)

$$x^3 = 100 \times n^3$$

$$\sqrt[3]{x^3} = \sqrt[3]{100n^3}$$

$$x = \sqrt[3]{100n}$$

(2ⁿ)

$$2^x = 100 \times 2^n$$

$$2^x = 2^n \times 2^{\log_2 100}$$

$$x = n + \log_2 100$$

