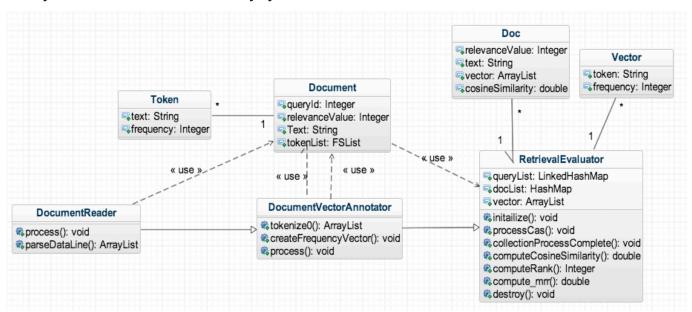
11693 - Software Method for Biotechnology

HW3- Engineering and Error Analysis with UIMA

Task 1

1. System Design

In this task, I firstly design a simple vector space retrieval system using the UIMA framework. There are three main parts of my system. The DocumentReader will read queries and documents from the input and parse the information, output it to Annotator. Then DocumentVectorAnnotator will build the vectors for every input. Finally, RetrievalEvaluator will compute the cosine similarity between each query and related candidates, output the result. You can see the UML diagram of my system below. I will describe my system in detail later.



Graph 1 – system design and general data flow of hw3-xiaomins

1.1 Type System (type):

The instructors provided two types already, the Token and the Document. The first one can store the token and frequency, which is important for building vectors. The second one stores queryId, relevance value and the text. It also has a file system to store the token lists.

I also define another two classes that be used in the RetrievalEvaluator. One is called Vector, that stores the token and its frequency, which can avoid nested HashMap or ArrayList. Another is called Doc, that stores all the information except the queryId of a single document. More specifically, it stores the tokens in a single document, the relevance value of this document, the cosine similarity value of this document and the text of this document. The reason why it does not need to store the queryId is in RetrievalEvaluator, I use a HashMap to link the queryId with the Doc, so id is not necessary in Doc. The Doc class can avoid lists of HashMap and ArrayList, and also support efficient retrieve the information during output.

1.2 Document Reader:

The Document Reader use the process() function to read the input file line by line. Then call the parseDataLine() function to parse the queryId, relevance value and the text of the sentences. By using the type called Document, the Collection Reader pass those information to Analysis Engine through JCas.

1.3 DocumentVectorAnnotator:

The Document Vector Annotator will read the document from the Document Reader Creates. Then sparse the bag of words, say tokens and related frequency, which related to two elements for building term vectors for each word. Finally, it update the tokenList and output the information to the RetrievalEvaluator

1.4 Retrieval Evaluator:

The Retrieval Evaluator is the most important part of this system. It

RetrievalEvaluator will firstly store all the information from the Document Vector Annotator into proper data structure. I use a LinkedHashMap to store all the queryId and related vectors, which can iterator as the same sequence as the input data. And I use a HashMap to store all the document queryId with self defined class Doc, which can call the document related values efficiently. Then the Retrieval Evaluator will compute the cosine similarity between query and related documents, and compute the rank of the relevant document to calculate the MRR metric. Finally, it will write the output into the report.txt in required format.

1.5 Aggregate Analysis Engine: VectorSpaceRetrieval

This class will help to run the pipeline without collection process engine (CPE).

3. Performance Evaluate:

For the first five queries and documents, I output the same result as the golden standard. For all the twenty queries and documents, I got MRR metric for 0.4375.

```
rank=2 gid=1 rank=2 gid=2 rank=3 gid=2 rank=3 gid=2 rank=3 gid=3 rank=3 gid=3 rank=3 gid=5 rank=3 gid=5 rank=3 gid=5 rank=3 gid=6 rank=3 gid=6 rank=3 gid=7 rank=3 gid=17 rank=3 gid=13 rank=3 gid=17 rank=3 g
```

Task 2

1. Error Analysis

Generally speaking, there are five main errors in the current system. Error type and their appearance times on the 20 queries are listed below in table 1.

Table 1 – statistics for error type

No.	Error Types	times
1	stop words	5
2	morphology change	4
3	additional information	7
4	tokenization	6
5	synonym	9
6	different case	4
7	misspelling	4

1.1 Stop words

The is caused by regarding and ignore dft during the calculation of frequency, which causes some unimportant and meaningless words like the, has a high weight. Then impact the cosine similarity significantly. This can be solved by implementing a stopword detector to delete the stop words from the tokens.

1.2 morphology change

This means that the answer candidate use other morphology of words. For example, from nouns to verb(describe to description), change of tense(die to died) and also abbreviation(N.J. to New Jersey). To deal with this error, more advanced algorithm is needed. For example, detect the change of tense and morphology. Also match abbreviation with the full word. In this assignment, there is a provided class called StanfordLemmatizer can do this job perfectly except for abbreviation.

1.3 additional information

This mean that the candidate answer correctly answer the query but provide additional information that not match the words in the query. This can be solved by using substring/subsentence match algorithm or change to another advanced similarity measure.

1.4 Synonym Tokenization

The system cannot detect synonyms substitution. To deal with this problem need more advanced algorithm to distinguish the synonyms.

1.5 synonym

Wrong tokenization, words with punctuations cause mismatch. This can be solved by pre-delete punctuations or use advanced tokenization algorithm.

1.6 different case

This is easy to understand, same words, different case cause mismatch. This problem can be solved by transform all the characters into lower case.

1.7 misspelling

This is straight forward, because the misspelling, the two words cannot match. This can be solve be using some spelling checking tools like that used in Microsoft office.

2. Improvement and result (including bonus)

2.1 Tokenization method improvement

2.1.1 Delete punctuations

Remove "," ";" "?" "." " $\,$ " and " $\,$ s' $\,$ " from the tokens, which enhance the mrr to 0.5608.

```
In A.D. 79, long-dormant Mount Vesuvius erupted, burying in volcanic ash the Roman city of Pompeii; an estimated 20,000 people died. When Michael Jordan—one of the greatest basketball player of all time—made what was expected to be his last trip to play in Atlanta last out to see him and the Bulls.

Alaska was purchased from Russia in year 1867.

On March 2, 1962, Wilt Chamberlain scored a record 100 points in a game against the New York Knicks.

People of China have mixed feelings about River, which they often call "sorrow of China"

Roger Bannister was the first to break the four—minute mile barrier.

And that's not even to mention the breathtaking beauty of Alaska that became, in 1959, our 49th state.

Fighting for Holyfield's WBA heavyweight title on June 28, 1997, Tyson inexplicably bit his opponent's right ear.

Luna 2 was the first spacecraft to reach the surface of the Moon.

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Devils Tower can be found in Crook County

Named the "Mendocino Tree," the 600—to 800—year—old redwood stands 367 1/2 feet tall.

Oregon's Crater Lake tops it at 1,932 feet at its greatest depth.

Lionel Richiewss was lead singer and songwriter for Commodores.

A new look at NASA satellite data revealed that Earth set a new record for coldest temperature recorded in East Antarctica.

Bob Martey died in 1981 from cancer at age 36.

Corn futures found support from forecasts for above—normal temperatures in major growing areas, including Iowa, which often is the
cosine=0.3257
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                                                                                  rank=2 gid=2
ecord 62,046 fans
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rank=1
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 cosine=0.2828
cosine=0.2261
 nation's largest producer.

cosine=0.2831 rank=1 gid=18 rel=1 From a single hamburger stand in San Bernardino, Calif., in 1948, the systematized approach that the McDonald brothers developed to offer customers reasonably priced food at a rapid pace formed the cornerstone of the fast-food business.

cosine=0.1690 rank=3 gid=19 rel=1 On May 6, 1937, the hydrogen-filled German dirigible Hindenburg burned and crashed in Lakehurst, N.J., killing 35 of the 97 people on board and a Navy crewman on the ground.

cosine=0.4104 rank=2 gid=20 rel=1 They call it the Keystone State, and in this unpredictable election year, Pennsylvania is living up to its name.
  nation's largest producer
cosine=0.2831 rank=1 o
board and a Navy
cosine=0.4104
MRR=0.5608
```

2.1.2 All tokens to lowercase

I use the system library to change all the chars into lowercase. This improve the mrr to 0.4583. This shows that tokenization with punctuation has more impact on the result.

```
In A.D. /9, long-dormant Mount vesuvius erupted, burying in voicanic asn the Roman city of Pompeil; an estimated z0,000 people died.

When Michael Jordan—one of the greatest basketball player of all time—made what was expected to be his last trip to play in Atlanta last of to to see him and the Bulls.

Alaska was purchased from Russia in year 1867.

On March 2, 1962, Wilt chamberlain scored a record 100 points in a game against the New York Knicks.

People of China have mixed feelings about River, which they often call "sorrow of China"

Roger Bannister was the first to break the four—minute mile barrier.

And that's not even to mention the breathtaking beauty of Alaska that became, in 1959, our 49th state.

Fighting for Holyfield's WBA heavyweight title on June 28, 1997, Tyson inexplicably bit his opponent's right ear.

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Oregon's Crater Lake tops it at 1,932 feet at its greatest depth.

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A new look at NASA satellite data revealed that Earth set a new record for coldest temperature recorded in East Antarctica.

Bob Marley died in 1981 from cancer at age 36.

Corn futures found support from forecasts for above—normal temperatures in major growing areas, including Iowa, which often is the
 cosine=0.2/91
March, an NBA
cosine=0.2357
cosine=0.2315
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nation's large
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cosine-0.2265 rank-2 gid=18 rel=1 From a single hamburger stand in San Bernardino, Calif., in 1948, the systematized approach that the McDonald brothers developed to offer customers reasonably priced food at a rapid pace formed the cornerstone of the fast-food business. cosine-0.1268 rank-3 gid=19 rel=1 0n May 6, 1937, the hydrogen-filled German dirigible Hindenburg burned and crashed in Lakehurst, N.J., killing 35 of the 97 people on board and a Navy crewman on the ground.
  cosine=0.3078
                                                                   rank=2 gid=20
                                                                                                                                    rel=1
                                                                                                                                                                     They call it the Keystone State, and in this unpredictable election year, Pennsylvania is living up to its name.
 MRR=0.4583
```

2.2 Stemming improvement

2.2.1 remove stop words

I wrote a class myself which reads the stop words from the given text and can return whether a token is stop word. I use this to distinguish stop words and tell the system does not store the stop words in tokenList. As a result, the mrr increases to 0.5788. While, there are some problems. One of the main reason is some of the queries and documents are too short, after remove the stop word, the queries left only a few words or even nothing left. It is not a good ideal for short queries.

```
cosine=0.8791 rank=2 gid=1 rank=2 gid=2 rgl=1 rank=2 gid=3 rank=2 gid=4 rgl=1 rank=2 gid=5 rank=3 gid=5 rgl=1 rank=2 gid=6 rgl=
```

2.2.2 Retrieve back the original word

I use the provided StanfordLemmatizer to retrieve back the original word, which enhance the performance to 0.6500. This is the best performance of improvement.

```
cosine=0.20b/
cosine=0.4003
March, an NBA
cosine=0.4714
cosine=0.3086
cosine=0.0990
cosine=0.5547
                                                                                                                                                 In A.D. /ש, long-dormant mount vesuvius erupted, burying in volcanic ash the koman city of rompell; an estimated שטש people died.
When Michael Jordan—one of the greatest basketball player of all time—made what was expected to be his last trip to play in Atlanta last out to see him and the Bulls.
Alaska was purchased from Russia in year 1867.
                                                                                                                                               Alaska was purchased from Russia in year 1867.

On March 2, 1962, Wilt Chamberlain scored a record 100 points in a game against the New York Knicks.

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Bob Marley died in 1981 from cancer at age 36.

Corn futures found support from forecasts for above-normal temperatures in major growing areas, including Iowa, which often is the
                                                                                     gid=3
gid=4
                                                                                                                   rel=1
rel=1
                                                           rank=3
                                                           rank=2
                                                         rank=2
rank=2
rank=2
rank=1
rank=2
rank=4
cosine=0.5547

cosine=0.0891

cosine=0.2750

cosine=0.5804

cosine=0.7500

cosine=0.3162

cosine=0.3162
cosine=0.1195
cosine=0.4216
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                                                                                      gid=13
                                                           rank=3
cosine=0.4216 rank=3
cosine=0.0727 rank=3
cosine=0.4243 rank=1
cosine=0.3015 rank=3
nation's largest product
cosine=0.2265 rank=2
nation's targest producer. cosine=0.2265 rank=2 gid=18 rel=1 From a single hamburger stand in San Bernardino, Calif., in 1948, the systematized approach that the McDonald brothers developed to offer customers reasonably priced food at a rapid pace formed the cornerstone of the fast-food business. cosine=0.2417 rank=3 gid=19 rel=1 On May 6, 1937, the hydrogen-filled German dirigible Hindenburg burned and crashed in Lakehurst, N.J., killing 35 of the 97 people on
board and a Navy crewman on the ground.

cosine=0.3078 rank=2 gid=20 rel=1 They call it the Keystone State, and in this unpredictable election year, Pennsylvania is living up to its name.
MRR=0.6500
```

2.3 unnormalized TF-IDF

IDF
$$(q_i) = \log \frac{N - n(q_i) + 0.5}{n(q_i) + 0.5},$$

I implemented a function in a class to calculate the TF-IDF. Although the MRR value increases, but this is because there are so many zero cosine similarity, which cause ties. Then I use the relevance value = 1, and there is only one relevance document in each query.

```
cosine=0.0000 rank=2 gid=1 ral=1 march, an NBA record 52,046 fans turned cosine=0.5858 rank=2 gid=2 rank=1 gid=3 rank=1 gid=3 rank=1 gid=3 rank=1 gid=3 rank=1 gid=5 rank=1 gid=1 rank=1 gid=5 rank=1 gid=1 rank=1 gid=5 rank=1 gid=1 rank=1 gi
```

2.4 different similarity measures (bonus)

2.4.1 Dice coefficient

$$QS = \frac{2C}{A+B} = \frac{2|A \cap B|}{|A|+|B|}$$

I implement a dice-coefficient class(edu.cmu.lti.f14.hw3.hw3_xiaomins. casconsumers package) which includes a public function that can be called to compute the dice coefficient. The result is not so much better than that of cosine similarity.

```
In A.D. 79, long-dormant Mount Vesuvius erupted, burying in volcanic ash the Roman city of Pompeii; an estimated 20,000 people died.
When Michael Jordan—one of the greatest basketball player of all time—made what was expected to be his last trip to play in Atlanta last
out to see him and the Bulls.
Alaska was purchased from Russia in year 1867.
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Corn futures found support from forecasts for above-normal temperatures in major growing areas, including Iowa, which often is the
cosine=0.3456
cosine=0.2345
March, an NBA
cosine=0.2357
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gid=15
gid=16
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  cosine=0.5547
                                                                                   rank=2
                                                                                 rank=2
rank=2
rank=2
rank=1
rank=4
   cosine=0.4657
  cosine=0.1768
  cosine=0.3162
                                                                                   rank=3
  cosine=0.1195
                                                                                  rank=3
  cosine=0.4216
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 cosine=0.0788
cosine=0.2828
cosine=0.1508
nation's largest producer.

cosine=0.2362 rank=2 gid=18 rel=1 From a single hamburger stand in San Bernardino, Calif., in 1948, the systematized approach that the McDonald brothers developed to offer customers reasonably priced food at a rapid pace formed the cornerstone of the fast-food business.

cosine=0.1268 rank=3 gid=19 rel=1 On May 6, 1937, the hydrogen-filled German dirigible Hindenburg burned and crashed in Lakehurst, N.J., killing 35 of the 97 people on board and a Navy crewman on the ground.

cosine=0.2345 rank=2 gid=20 rel=1 They call it the Keystone State, and in this unpredictable election year, Pennsylvania is living up to its name.

MRR=0.4775
```

2.4.2 Jaccard coefficient

$$J(A,B) = \frac{|A \cap B|}{|A \cup B|}.$$

I implement a jaccard-coefficient class(edu.cmu.lti.f14.hw3.hw3_xiaomins. casconsumers package) which includes a public function that can be called to compute the jaccard coefficient. The result is very similar to that of dice coefficient.

```
cosine=0.4354 rank=1 gid=1 rgl=1 merch, an NBA record 62,046 fans turned cosine=0.2345 rank=2 gid=3 rgl=1 cosine=0.2345 rank=2 gid=3 rgl=1 cosine=0.2345 rank=2 gid=3 rgl=1 cosine=0.2345 rank=2 gid=3 rgl=1 rgl=1 cosine=0.4565 rank=2 gid=3 rgl=1 rgl=1 rosine=0.4565 rank=2 gid=3 rgl=1 rgl=1 rosine=0.4565 rank=2 gid=3 rank=2 gid=3 rgl=1 rosine=0.4565 rank=2 gid=3 rank=3 gid=3 rank=2 gid=3 rank=3 gid=3 rank=3
```

2.4.3 BM25

$$score(D,Q) = \sum_{i=1}^{n} IDF(q_i) \cdot \frac{f(q_i, D) \cdot (k_1 + 1)}{f(q_i, D) + k_1 \cdot (1 - b + b \cdot \frac{|D|}{avgdl})},$$

Lastly, I implement a BM25 class(edu.cmu.lti.f14.hw3.hw3_xiaomins. casconsumers package) which includes a public function that can be called to compute the BM25. It should also call the IDF class I mentioned before. The result is not that optimistic, because not normalize, there appears many negative values and the mrr is low.

```
In A.D. 79, long-dormant Mount Vesuvius erupted, burying in volcanic ash the Roman city of Pompeii; an estimated 20,000 people died. When Michael Jordan--one of the greatest basketball player of all time--made what was expected to be his last trip to play in Atlanta
    cosine=-0.7263
    Washe with the control of the contro
                                                                                                                                                                                                                                                                                                                                                                    out to see him and the Bulls.

Alaska was purchased from Russia in year 1867.

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And that's not even to mention the breathtaking beauty of Alaska that became, in 1959, our 49th state.

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A new look at NASA satellite data revealed that Earth set a new record for coldest temperature recorded in East Antarctica.

Bob Marley died in 1981 from cancer at age 36.

Corn futures found support from forecasts for above—normal temperatures in major growing areas, including Iowa, which ofte
                                                                                                                                                                                                                                                                                                                                                                           out to see him and the
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Bulls.
                                                                                                                                                                                                                    gid=4
gid=5
gid=6
gid=7
gid=8
gid=9
gid=10
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    board and a Navy
cosine=-7.3412 r
MRR=0.4868
```

3. comparison and conclusion

I conclude all the result I tried before, the result is listed on table-2.

Table-2 result conclusion

Type of improvement	MRR	
Delete punctuations	0.5608	
To lowercase	0.4583	
Remove stop words	0.5788	(many ties)
Retrieve original word	0.6500	
Aggregate of above	0.6879	
TF-IDF	0.8285	(many ties)
Dice coefficient	0.4775	
Jaccard coefficient	0.4805	
BM25	0.4868	

As a result, The tokenization improvement and stemming improvement have more impact on the MRR result than changing into other similarity measures. Among the tokenization improvement methods, delete the punctuations improves a lot and does create many ties. And the stemming improvement method, Retrieve original word using the StanfordLemmatizer can also make a great difference to the result. On the contract, TF-IDF does run well because it almost ties all the documents. And all the three other similarity measures, Dice coefficient, Jaccard coefficient and BM25 almost perform the same result as cosine similarity does.

4. Acknowledgement

Thanks to all the TAs and my classmates who help me with this assignment. Without your kind help, I cannot finish it.