CSCI 6342: Linear Algebra: A Computational Approach. Assignment 2

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1 Pen and Paper Problems

1. I is Unique.

Let I be the identity matrix for an n by n matrix. Let A and B be n by n matrices. Assume there is a matrix J such that,

$$\mathbf{J}\mathbf{A} = \mathbf{A} \tag{1}$$

Similarly we know that,

$$\mathbf{BI} = \mathbf{B} \tag{2}$$

Replace A with I and you get:

$$\mathbf{JI} = \mathbf{I} \tag{3}$$

Replace \mathbf{B} with \mathbf{J} and you get:

$$\mathbf{JI} = \mathbf{J} \tag{4}$$

Since JI equal both J and I, then J = I

2. $AA^{-1} = I$

Let **A** be the inverse of **B** such that AB = I.

$$\mathbf{A} = \mathbf{A} \tag{5}$$

As per how identity matrices work,

$$\mathbf{A} = \mathbf{I}\mathbf{A} \tag{6}$$

By definition, AB = I.

$$\mathbf{A} = (\mathbf{A}\mathbf{B})\mathbf{A} \tag{7}$$

By associativity with matrix multiplication we get,

$$\mathbf{A} = \mathbf{A}(\mathbf{B}\mathbf{A}) \tag{8}$$

Therefore,

$$\mathbf{B}\mathbf{A} = \mathbf{I} \tag{9}$$