

# Modelling Human Uncertainty

How to teach machines when experts disagree with each other

Ryutaro Tanno

University College London, UK



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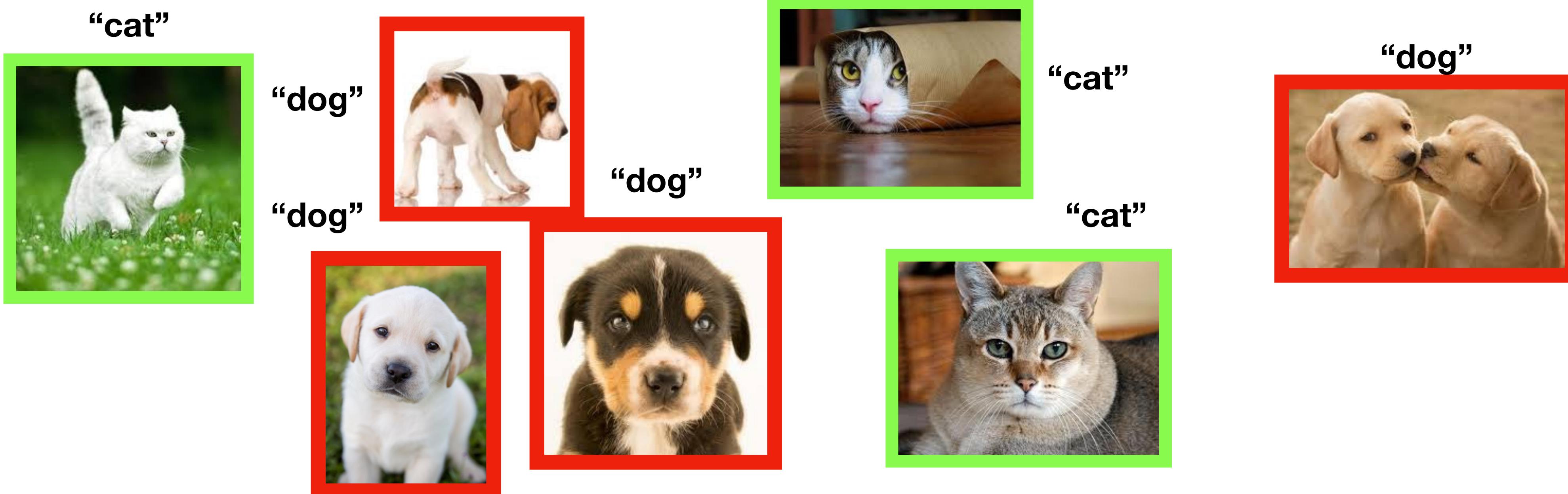
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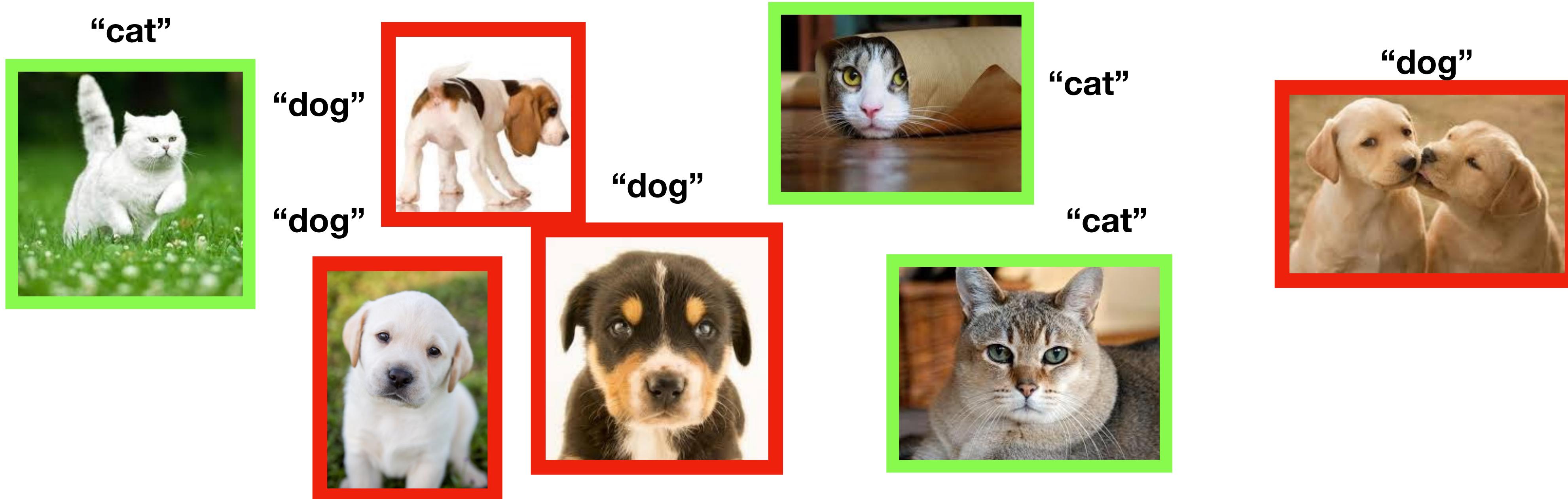
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- **Clean** data => great performance!

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**Alex**  
**(engineer)**

“Bird”

“Red-necked Grebe”

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# Deep Learning in the “wild”

- **Input** can also be noisy! e.g. hard to interpret / nebulous images

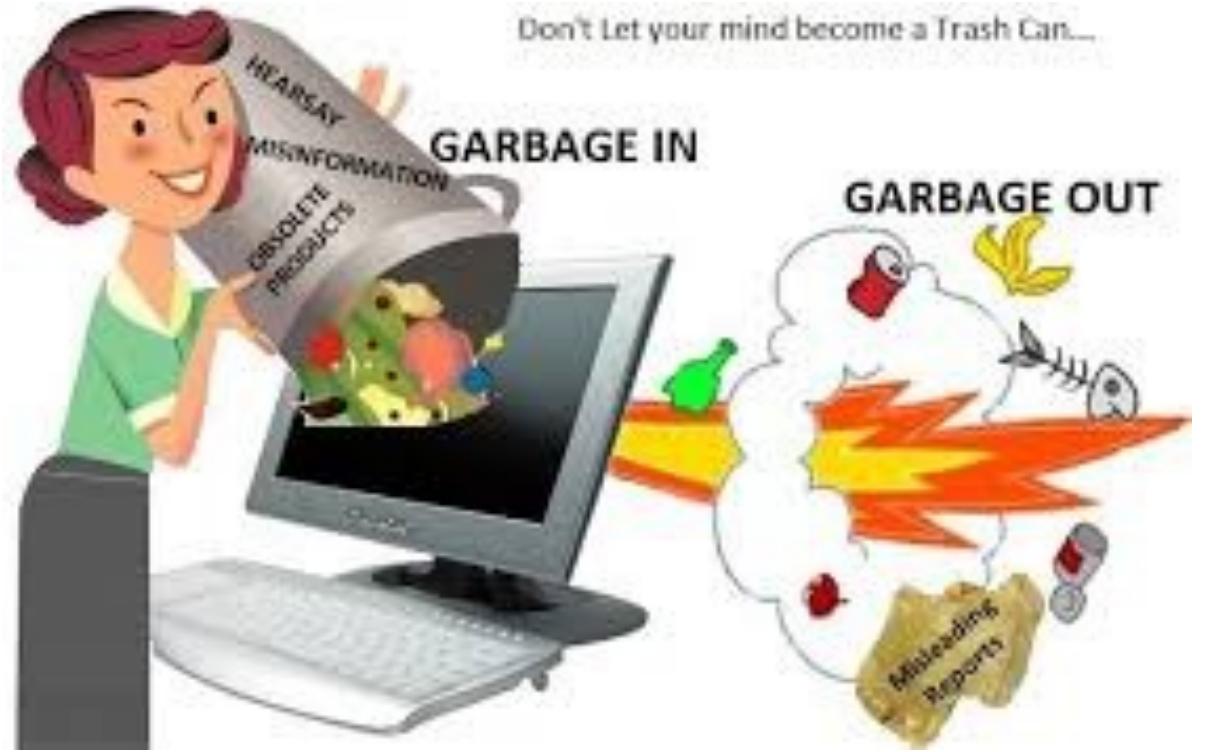


- But, not the focus of this talk.

# Problems

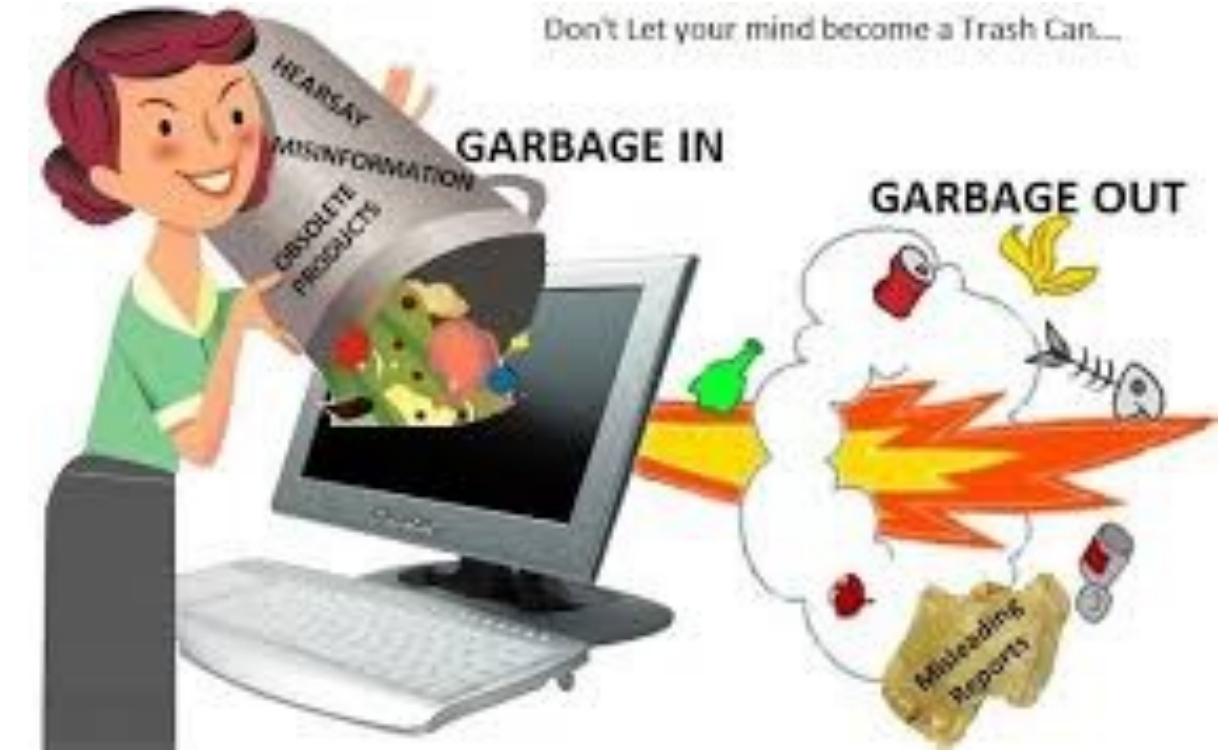
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- Data curation is time-consuming and suboptimal



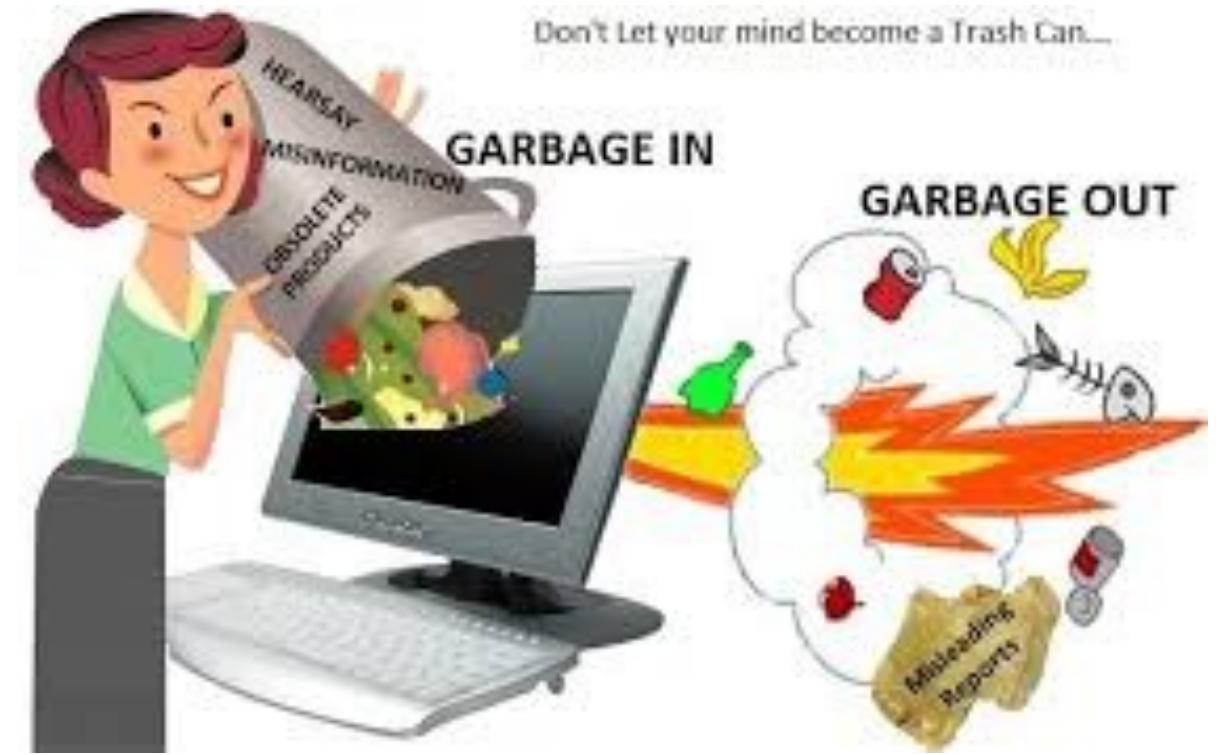
Cleaning Big Data: Most Time-Consuming, Least Enjoyable Data Science Task, Survey Says



Gil Press Contributor ⓘ  
*I write about technology, entrepreneurs and innovation.*

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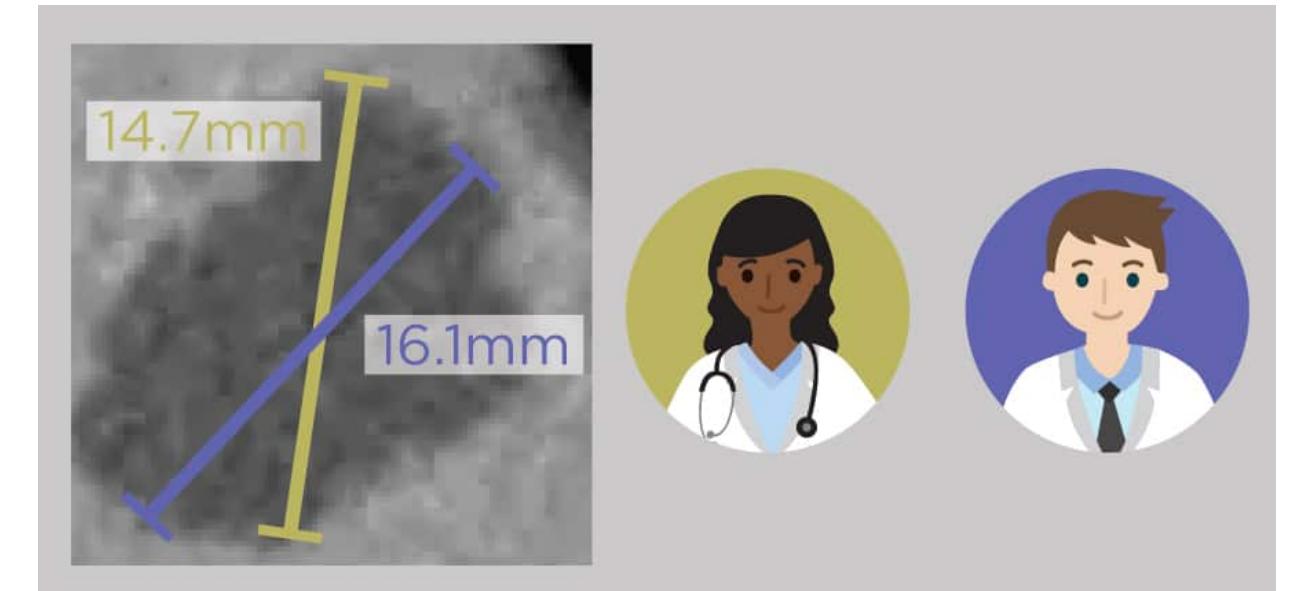
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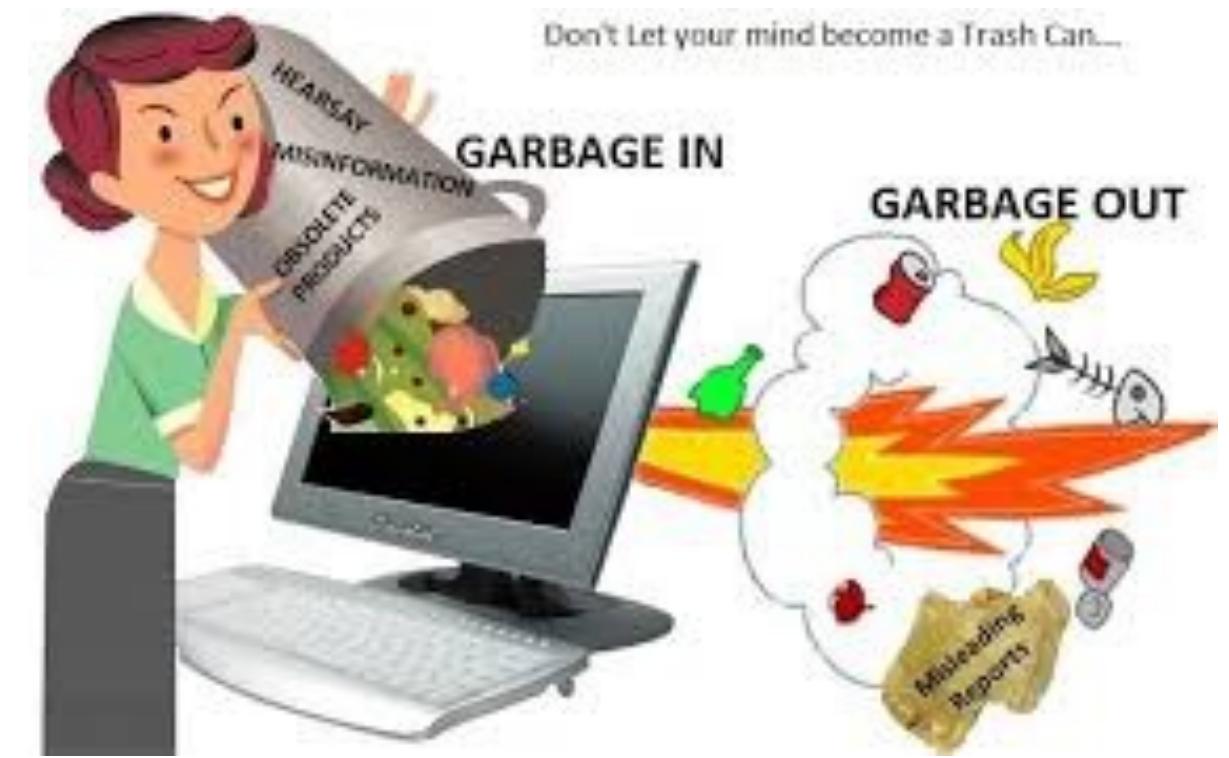
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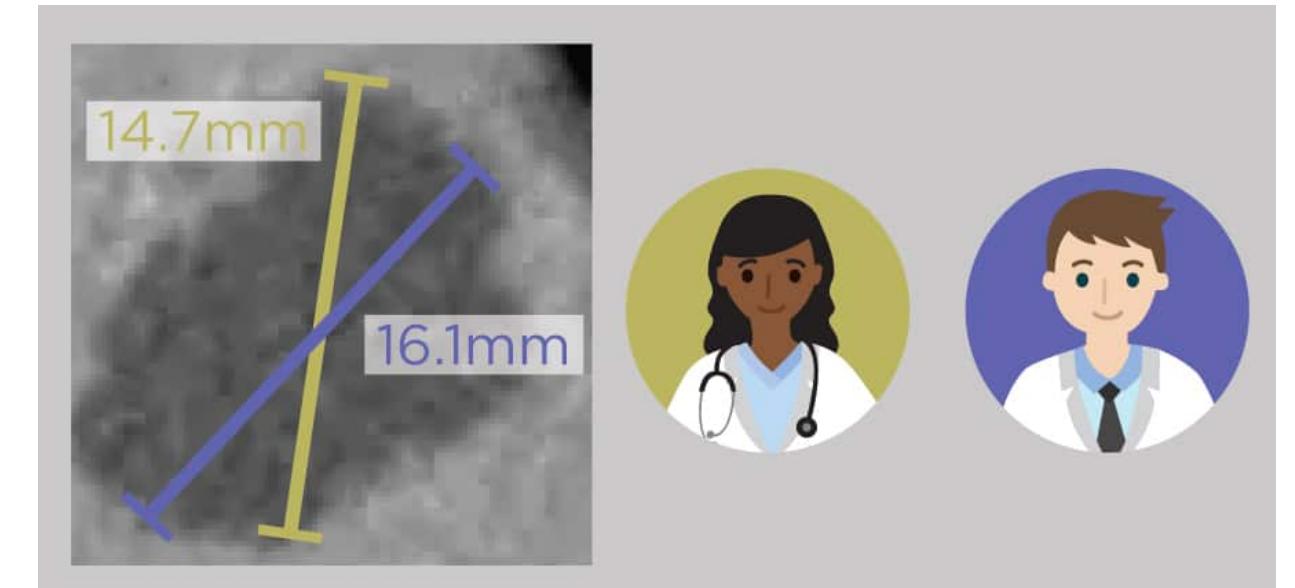
- “Garbage in, garbage out”
- Data curation is time-consuming and suboptimal
- High inter-reader variability in radiology
- Majority vote (“Wisdom of Crowds” ) is not always a solution!
  - (1) **Expensive**, (2) **Rare experts**



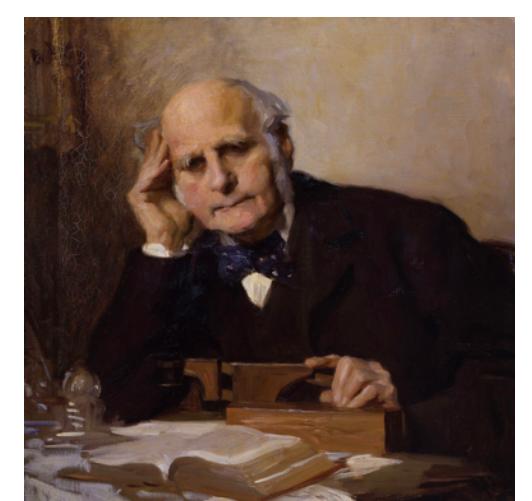
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Francis Galton, 1907

# My Goal

Simultaneously model **uncertainty of annotators & true label distribution.**

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Simultaneously model **uncertainty of annotators** & **true label distribution**.

=> Automate data curation

=> Improve future label acquisition



# Set-up

- Multiple annotators
- At least 1 label per image
- No meta-information e.g. expert level, reviews, etc
- No “golden” data
- **Task:** classification



# Our Model

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- Models the uncertainty of each annotator with a **confusion matrix**.
- Use this **confusion matrix** to “correct” noisy labels to learn **true label distribution**.

# What is a confusion matrix?



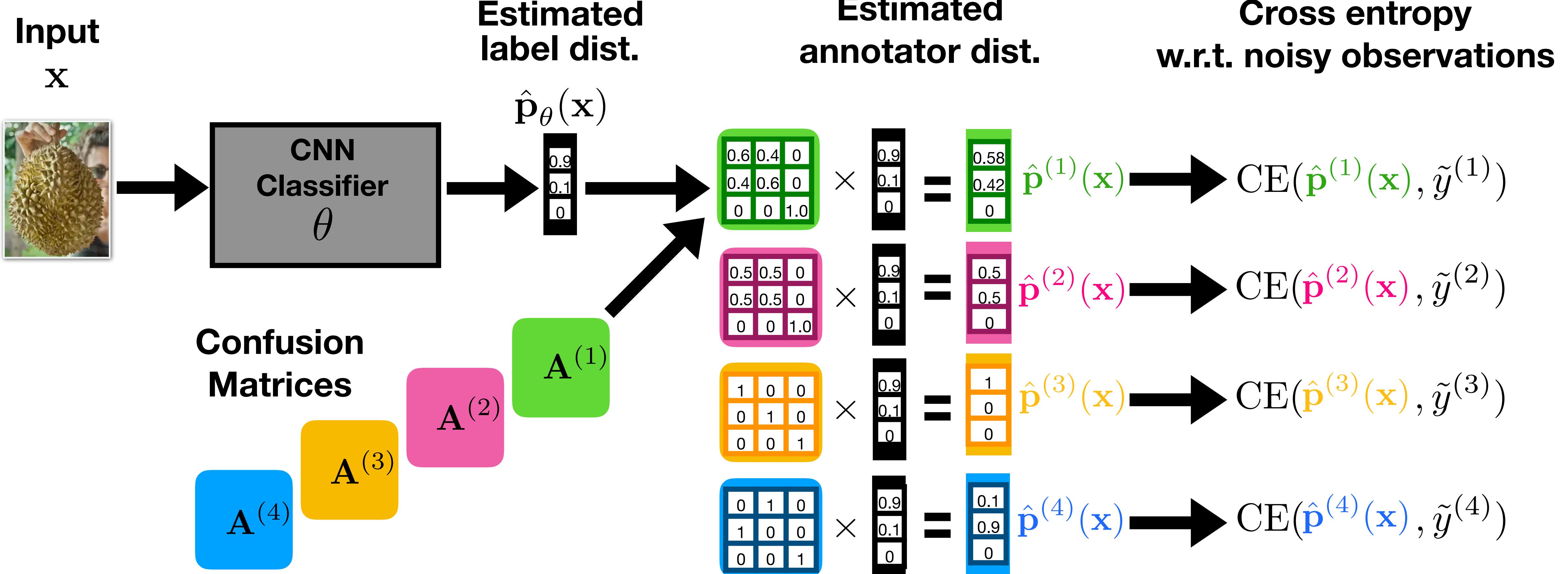
Correct

		Durian	Jack fruit	Apple
Durian	Durian	0.6	0.4	
	Jack fruit	0.5	0.5	
Apple				1.0
		Durian	Jack fruit	Apple
Predictions				

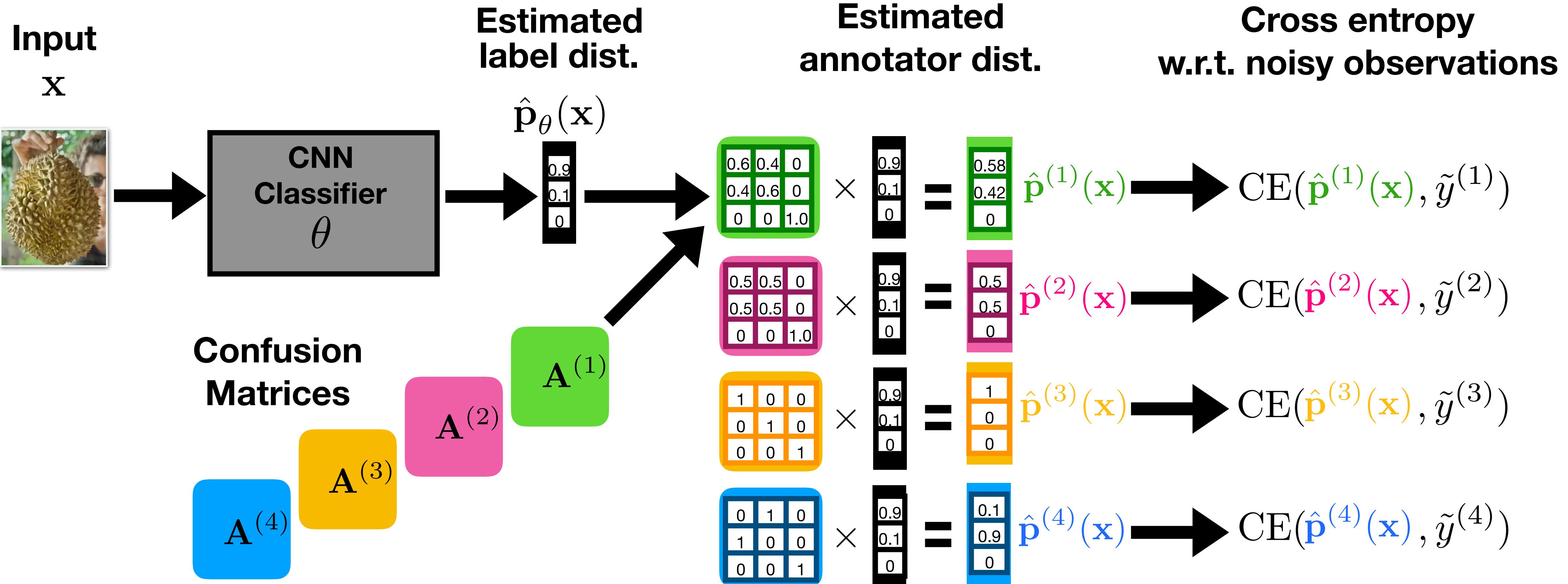


?

# Model Schematic



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**Loss Function**

$$\sum_{i=1}^N \sum_{r=1}^R \mathbb{1}(\tilde{y}_i^{(r)} \in \mathcal{S}(\mathbf{x}_i)) \cdot \text{CE}(\hat{\mathbf{A}}^{(r)} \hat{p}_\theta(\mathbf{x}_i), \tilde{y}_i^{(r)}) + \lambda \sum_{r=1}^R \text{tr}(\hat{\mathbf{A}}^{(r)})$$

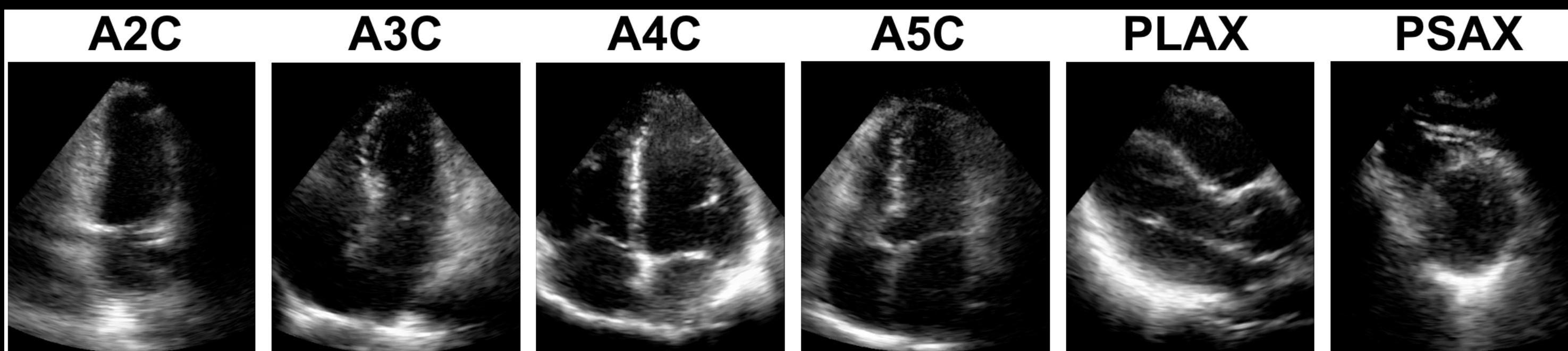
where:  
 $R$  = no. of annotators  
 $N$  = no. of samples  
 $\mathcal{S}(\mathbf{x})$  = set of available labels for  $\mathbf{x}$

# Experiments

- MNIST digit classification dataset



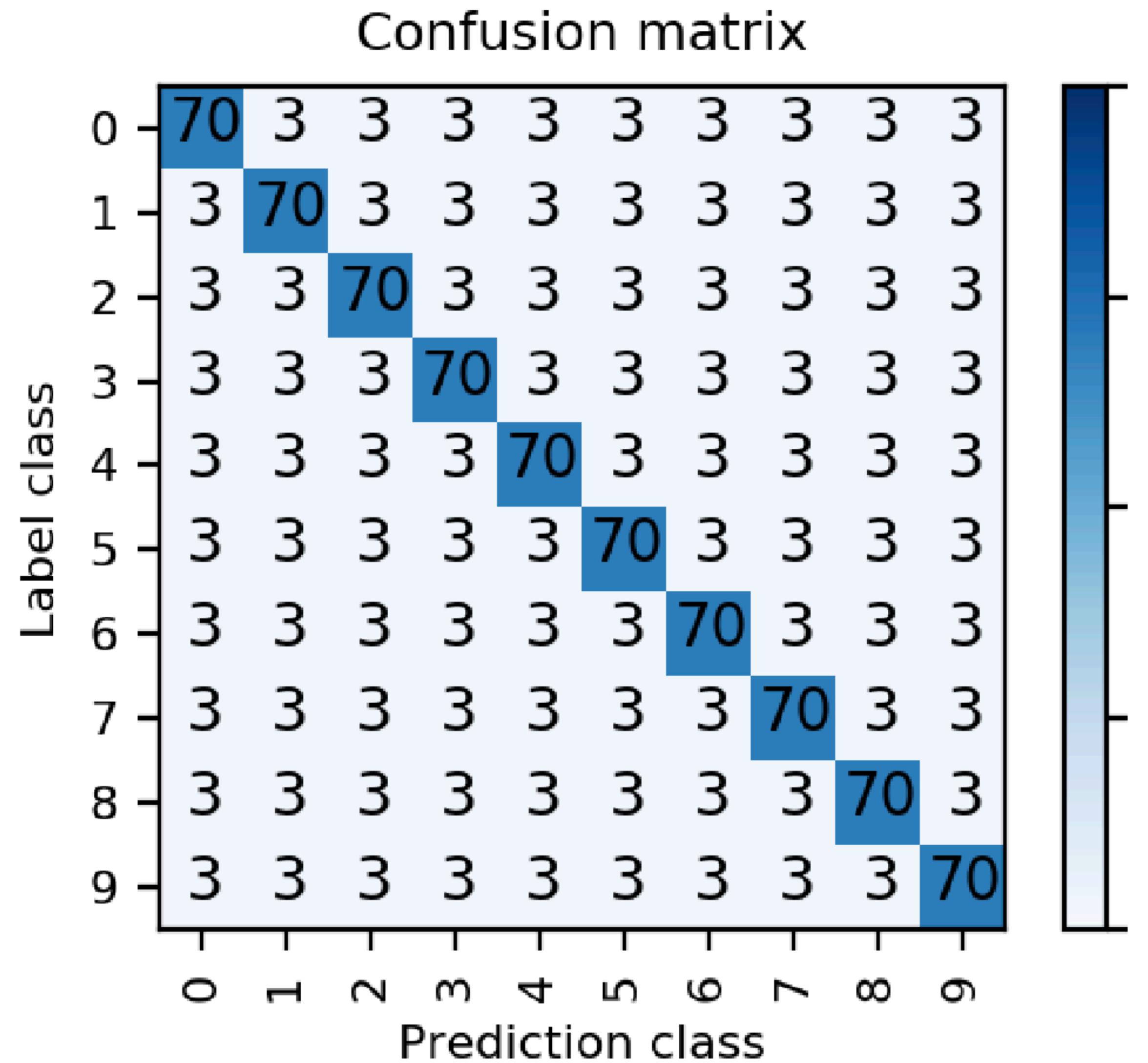
- Ultrasound Cardiac View Classification



Can the model curate and learn  
simultaneously?

# Experiment 1: demo on a diverse annotator group

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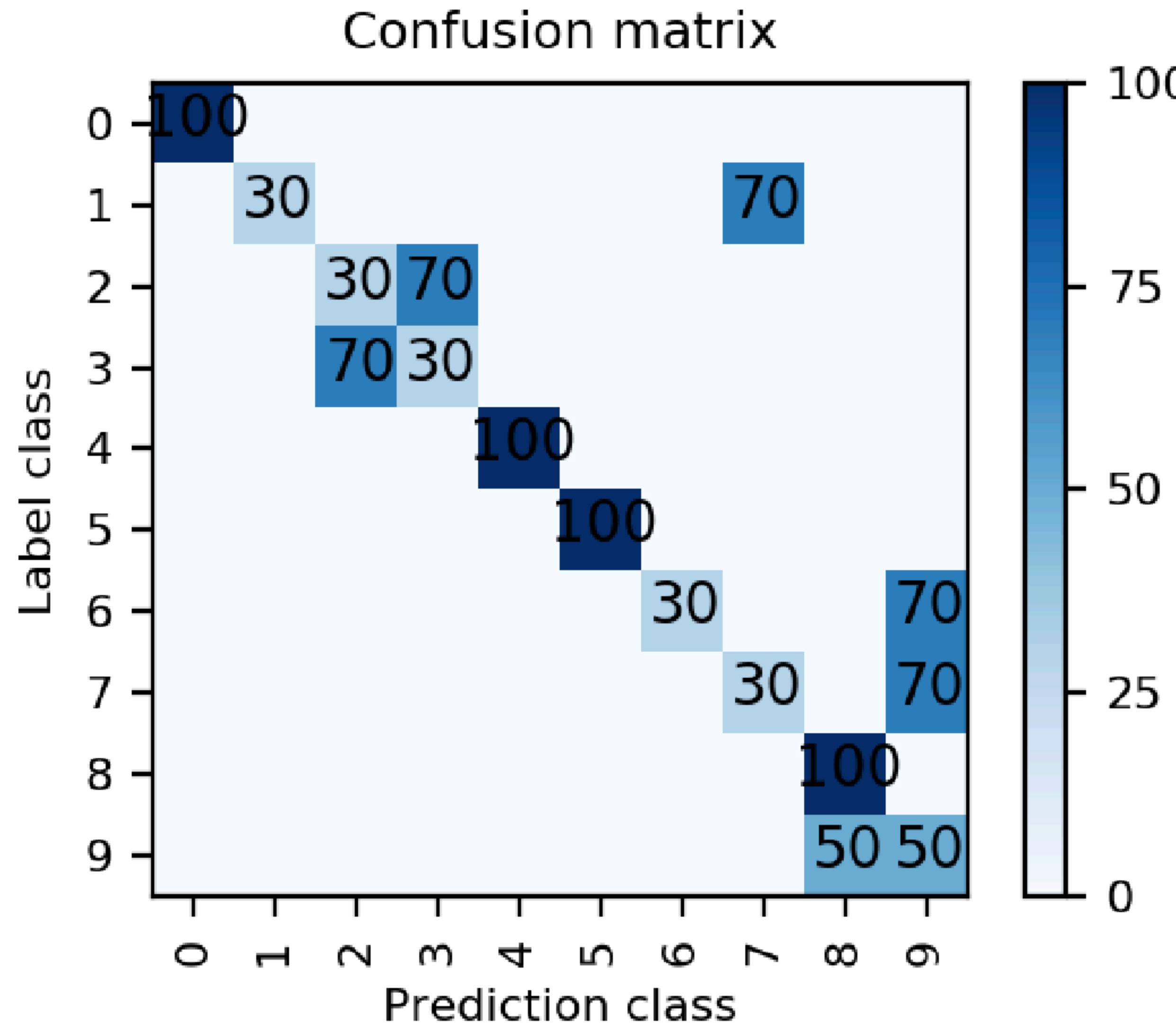
**Name:** A+ Alice

**Accuracy:** 70 %

**Characteristics:**

she whimsically assigns random labels 30% of the time.

# Experiment 1: demo on a diverse annotator group



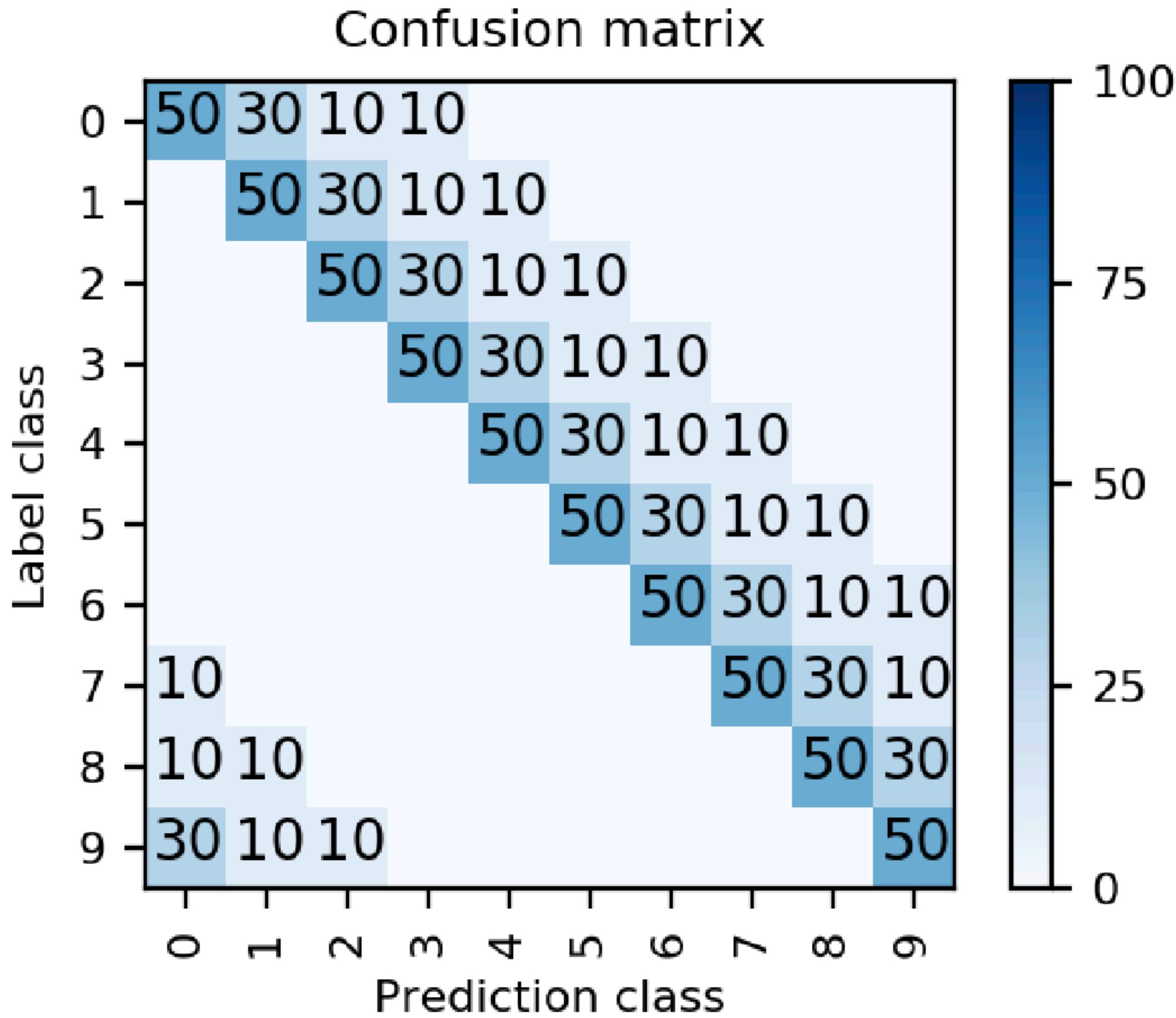
**Name:** A- Andy

**Accuracy:** 60 %

**Characteristics:**  
He is not very good at  
discriminating similar looking  
numbers.

**Flips labels as follows:**  
1 => 7, 2 <=> 3 ,  
6 => 9, 7=>9, 9 => 8

# Experiment 1: demo on a diverse annotator group



**Name:** Solid C, Carla

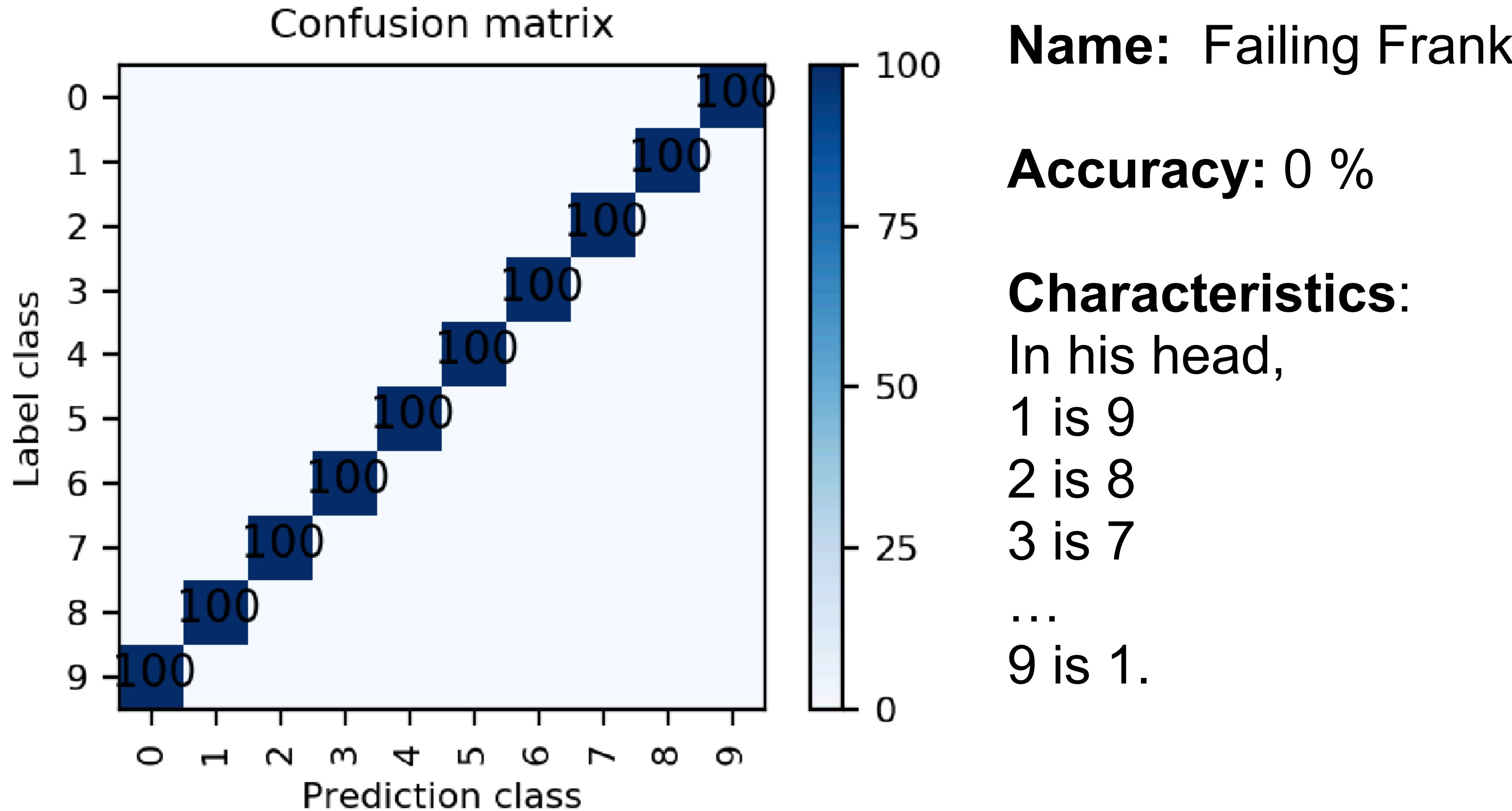
**Accuracy:** 50 %

**Characteristics:**

He is not very good at  
discriminating neighboring digits.

E.g. 1 and 2, 2 and 3, etc

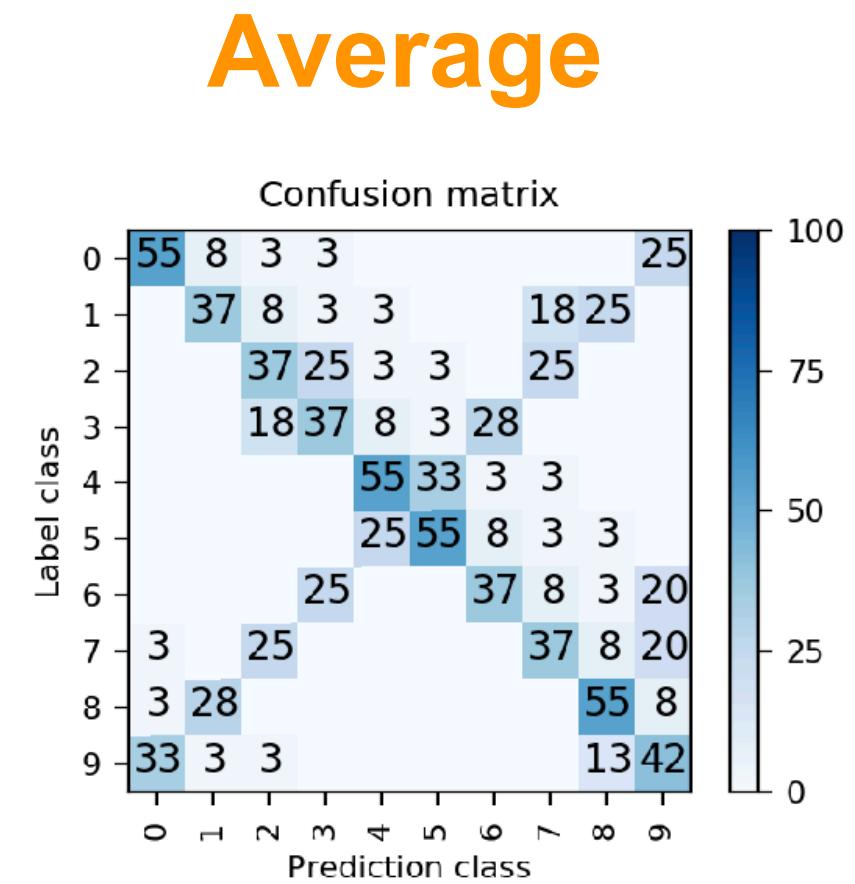
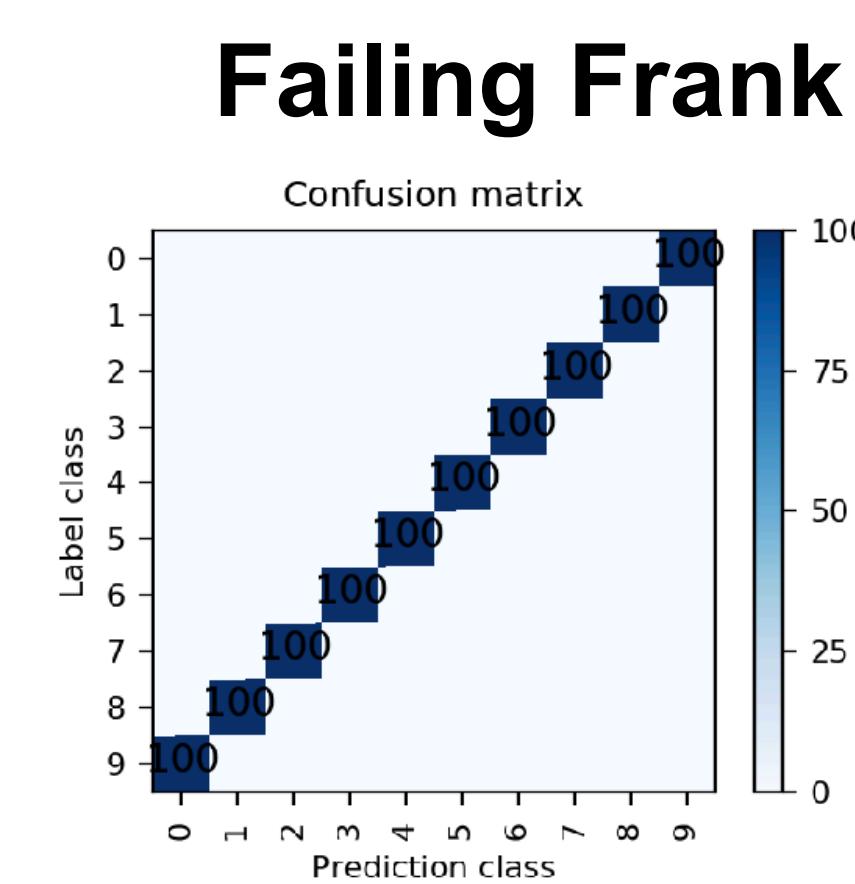
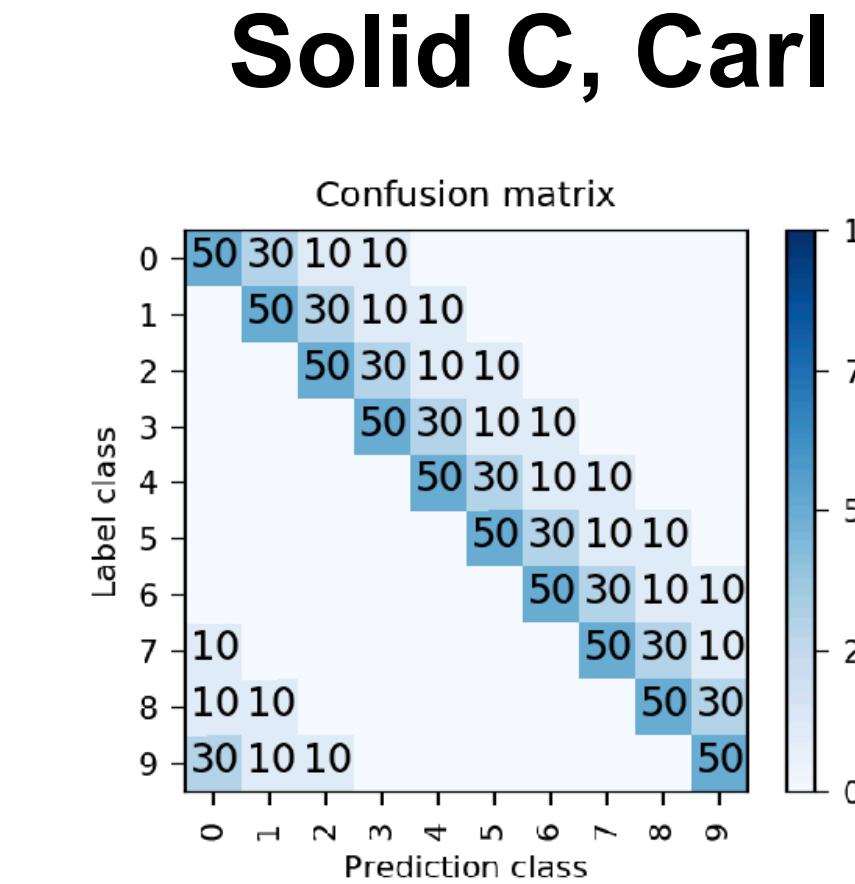
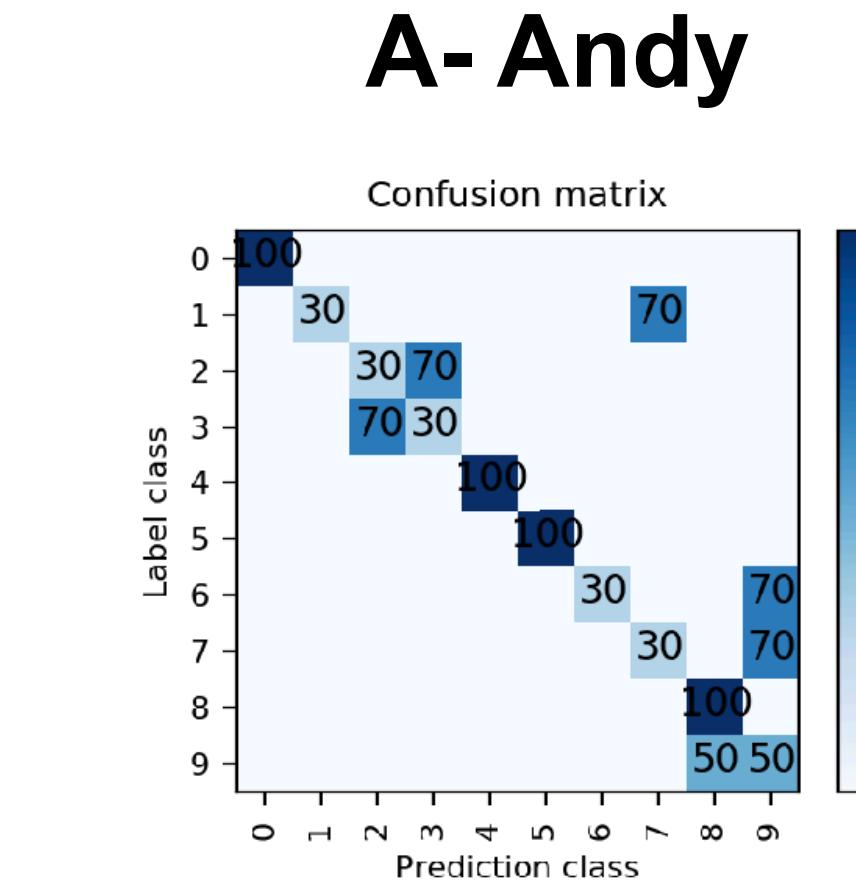
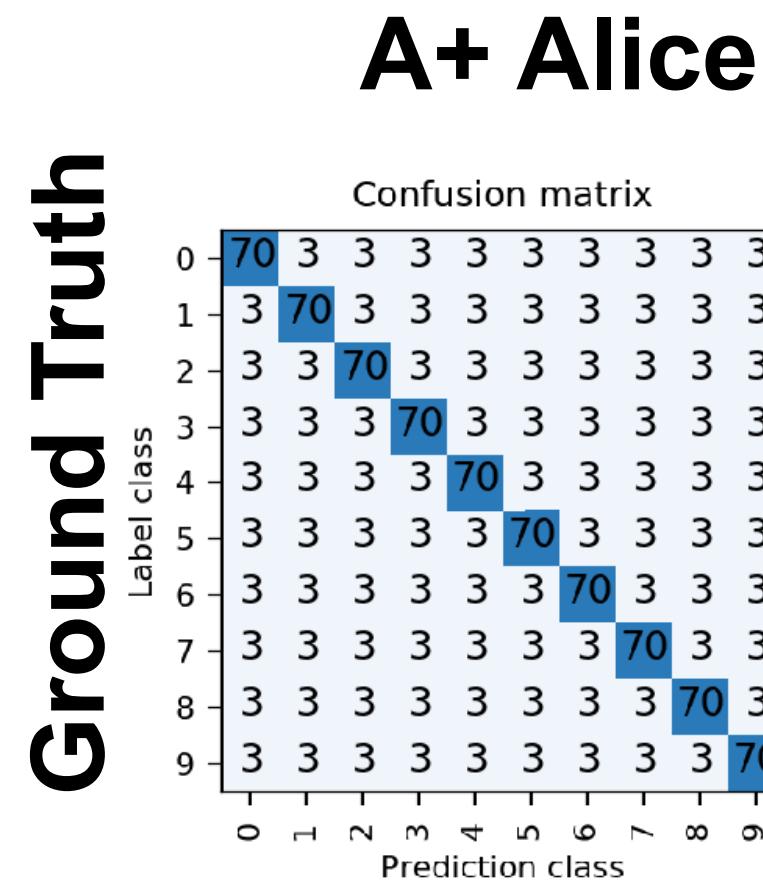
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# Curation Results

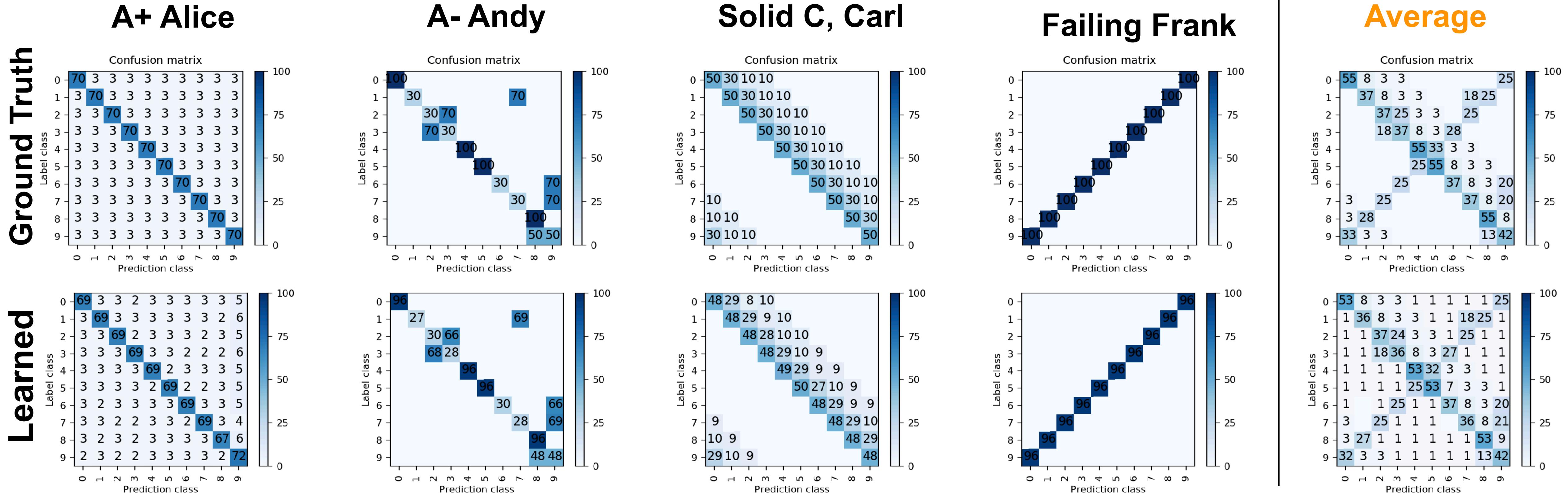
# Experiment 1: demo on a diverse annotator group

- Now train our model on labels obtained from these people ...



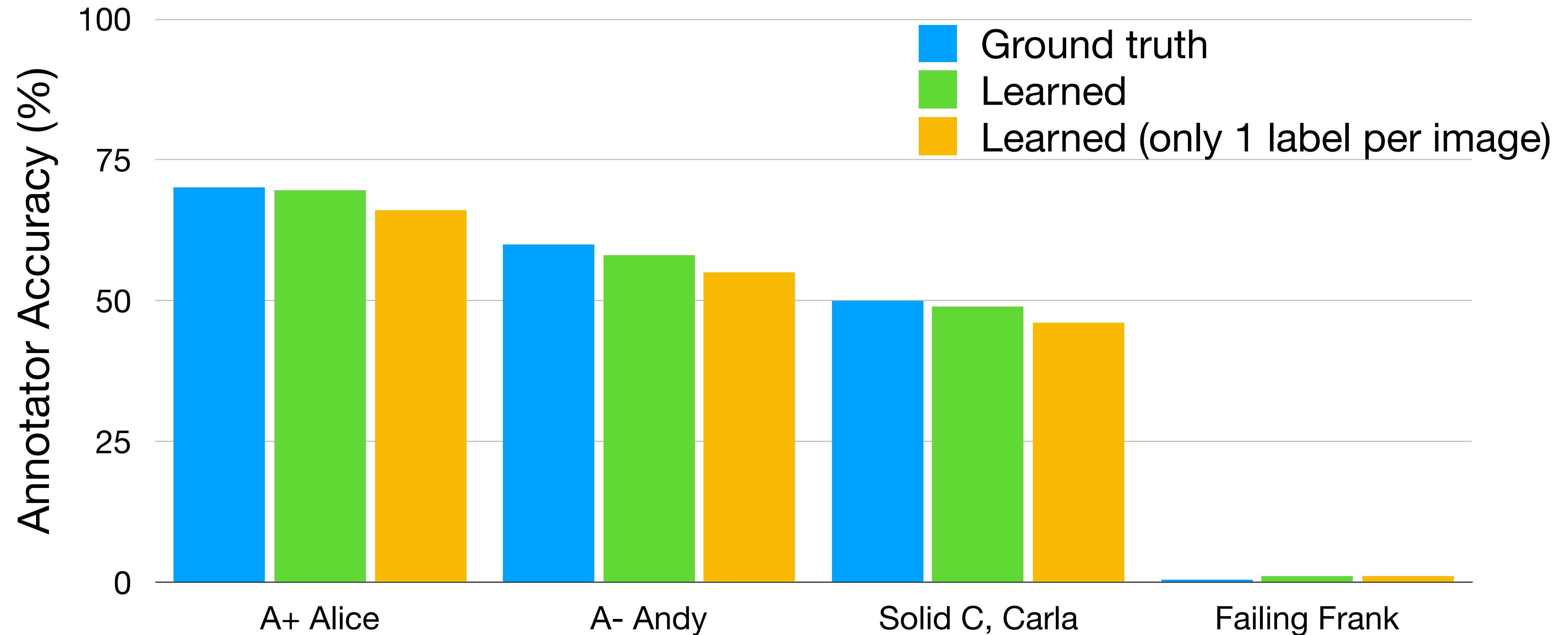
# Experiment 1: demo on a diverse annotator group

- Confusion matrices are successfully recovered!



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- Annotator accuracy are well estimated! Useful for ranking.

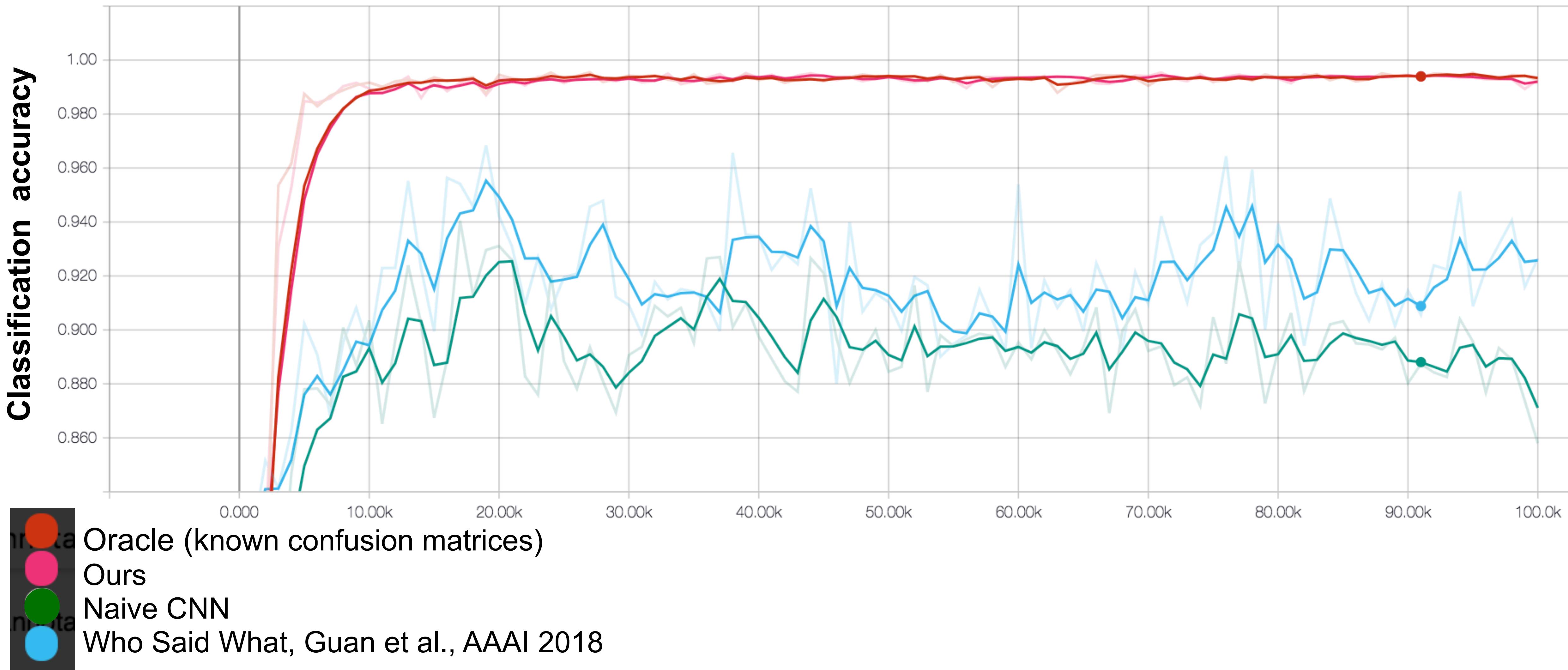


# Model Prediction Results

# Model Performance

- > 99 % classification accuracy, outperforms other models.

accuracy/model\_on\_true\_labels



# When does it work (or fail)?

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**Theorem** (motivation for the trace term).

If the average confusion matrix of annotators is **diagonally dominant (D.D.)**, and the cross-entropy term in the loss function is zero, minimising the trace of the estimated confusion matrices **uniquely** recover the true confusion matrices.

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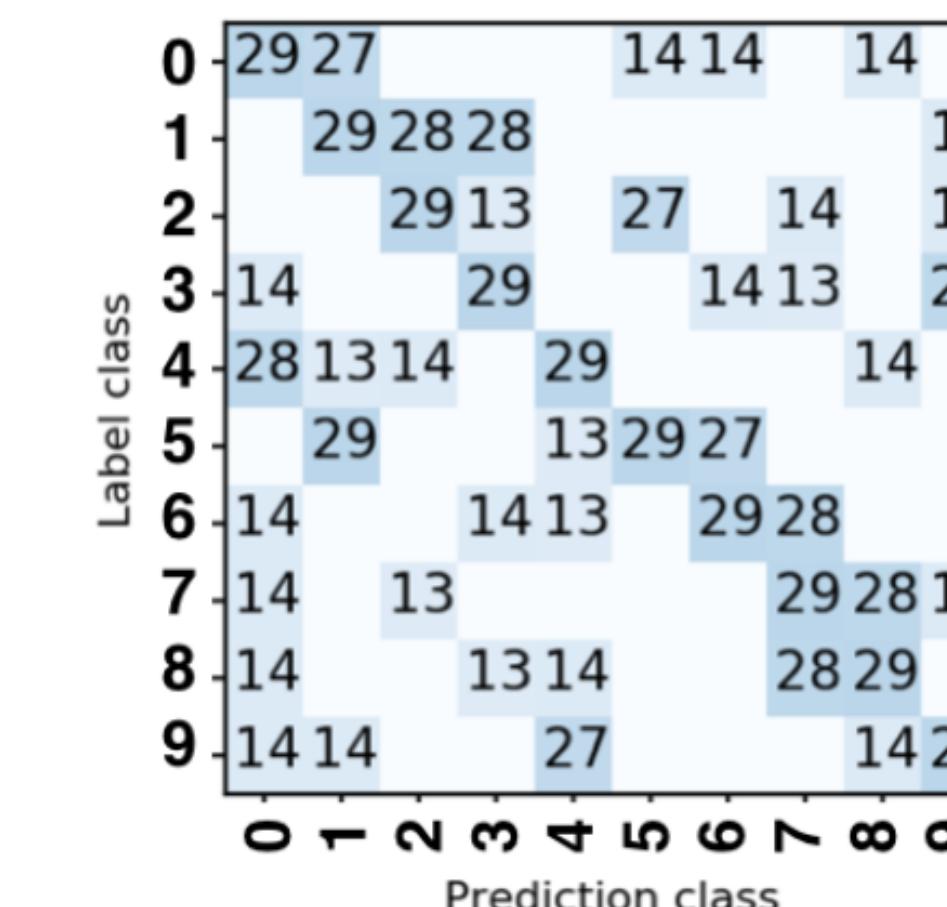
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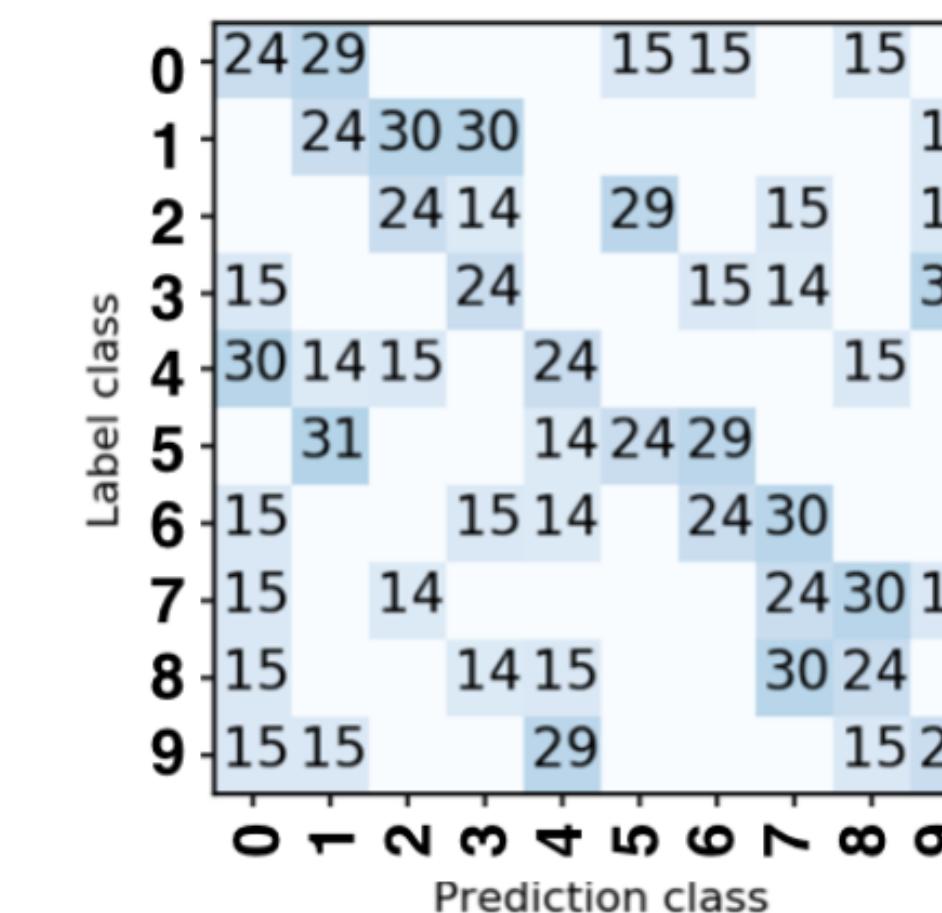
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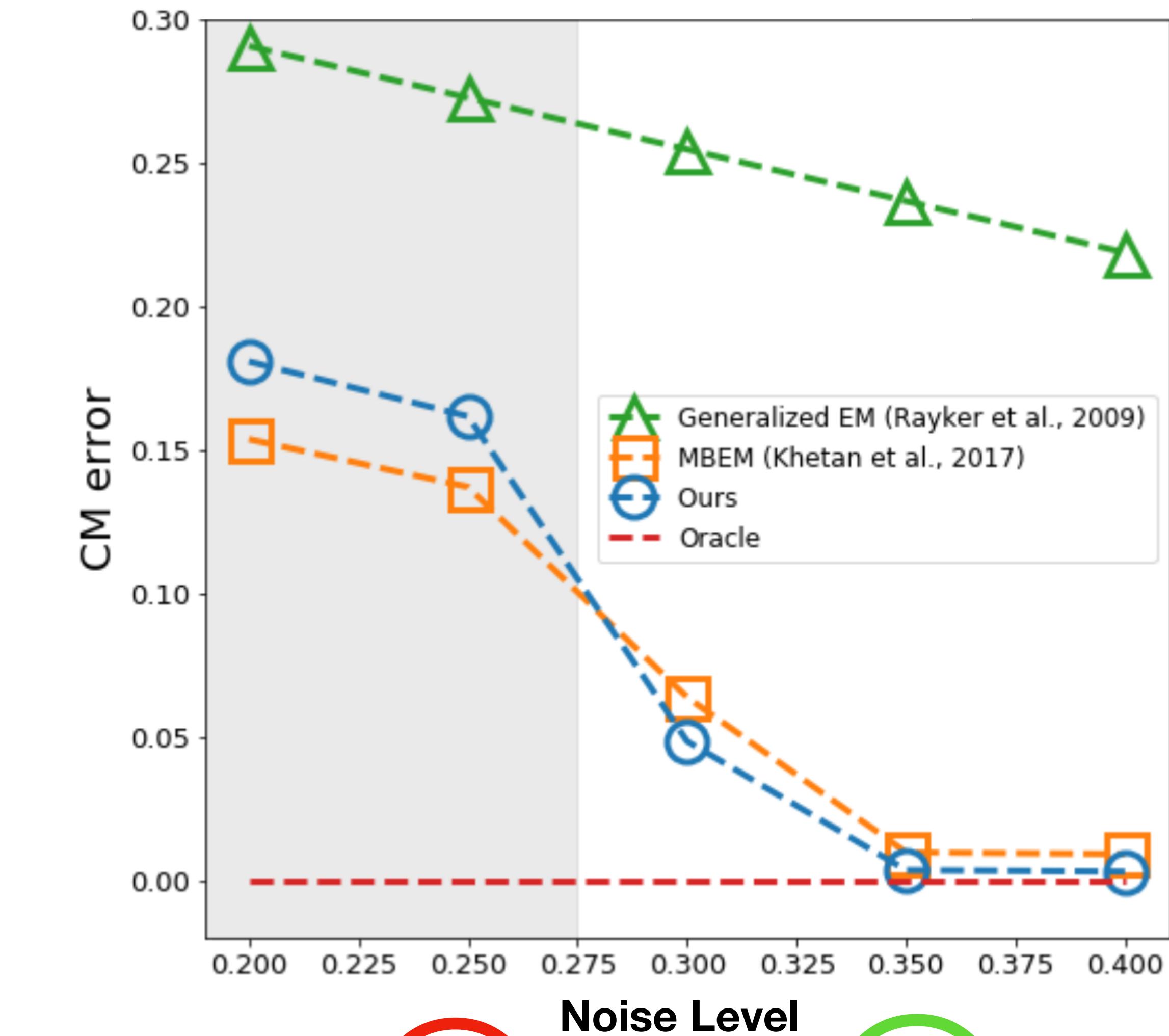
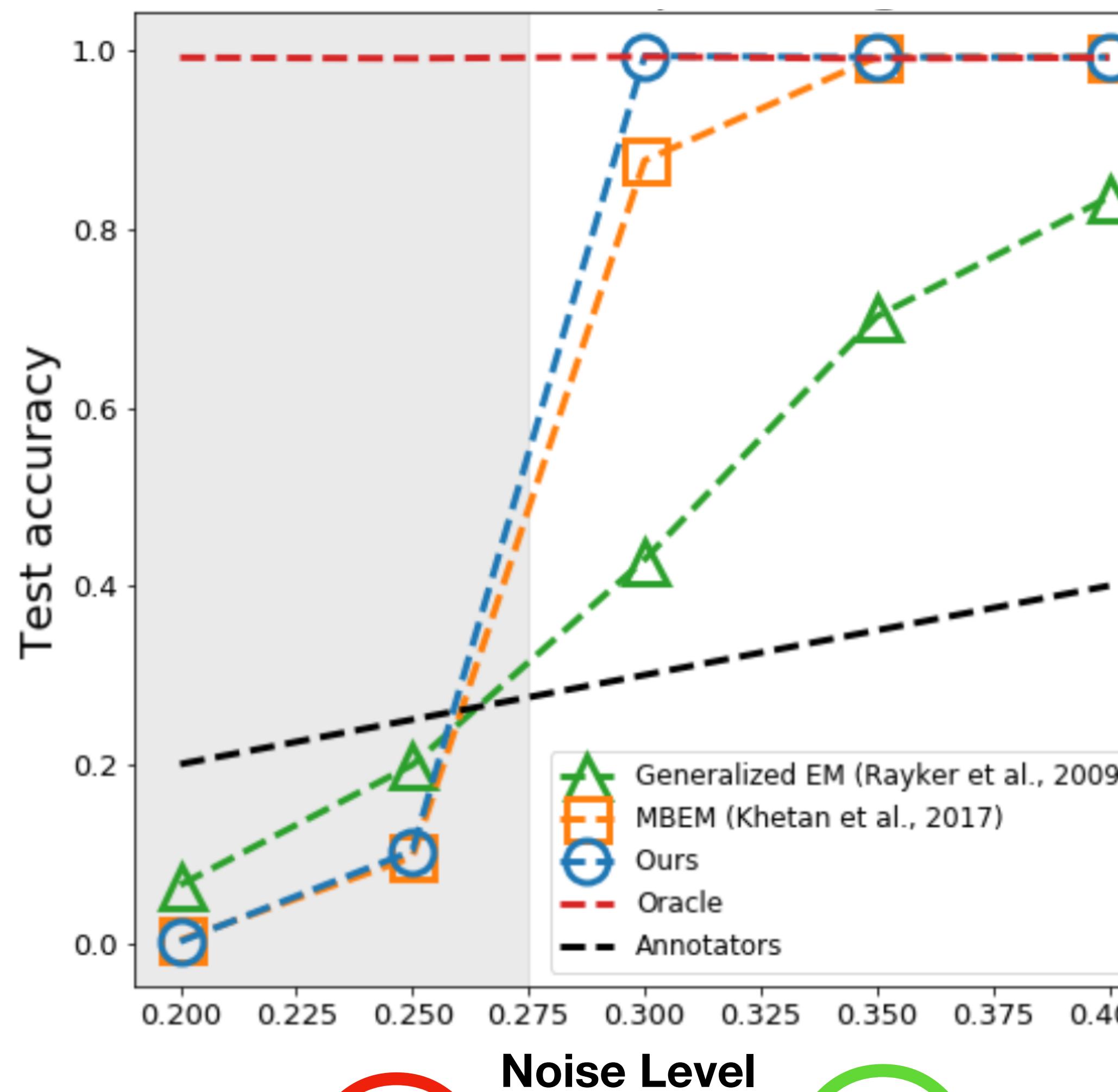
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*not diagonally dominant*

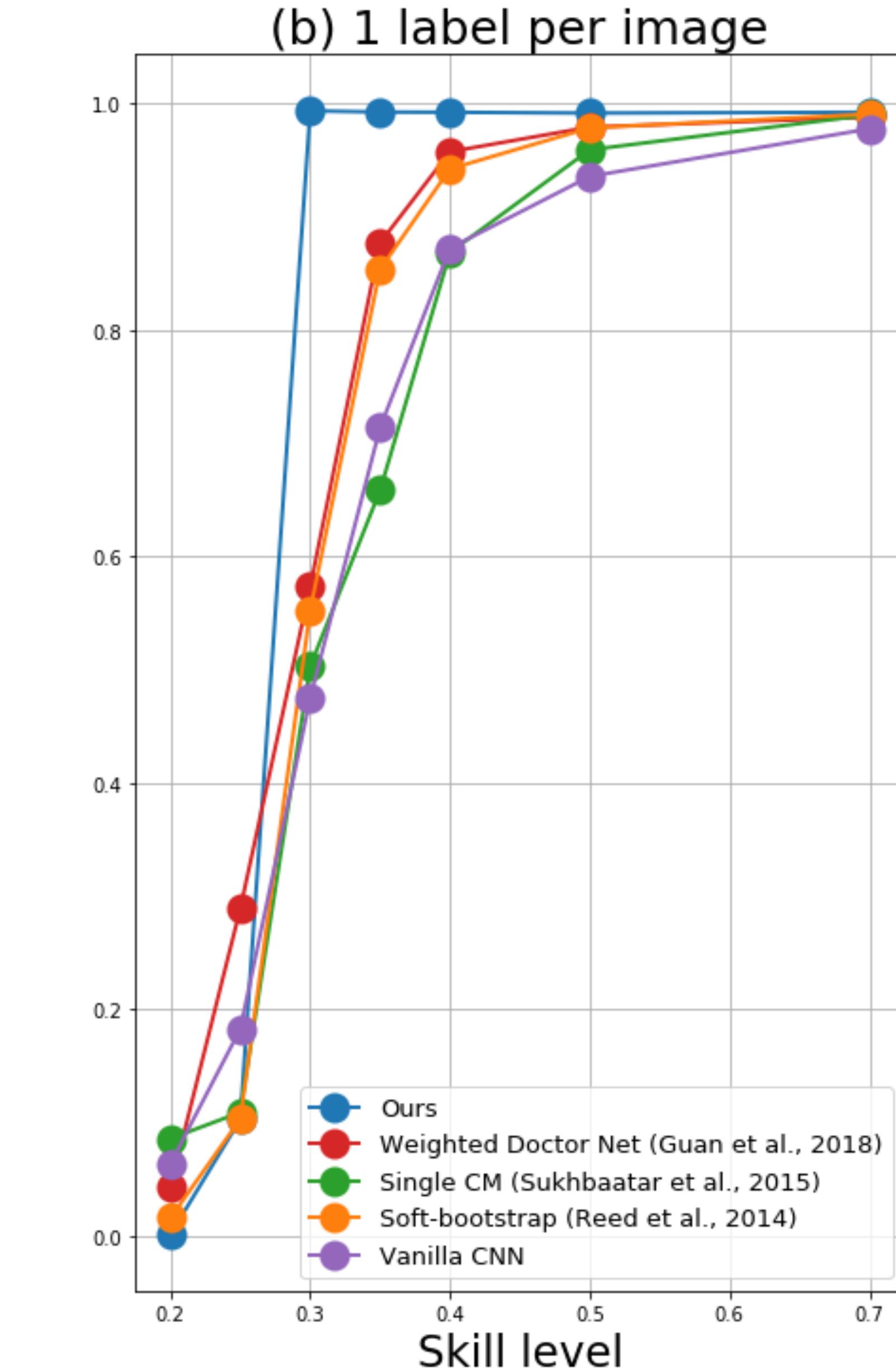
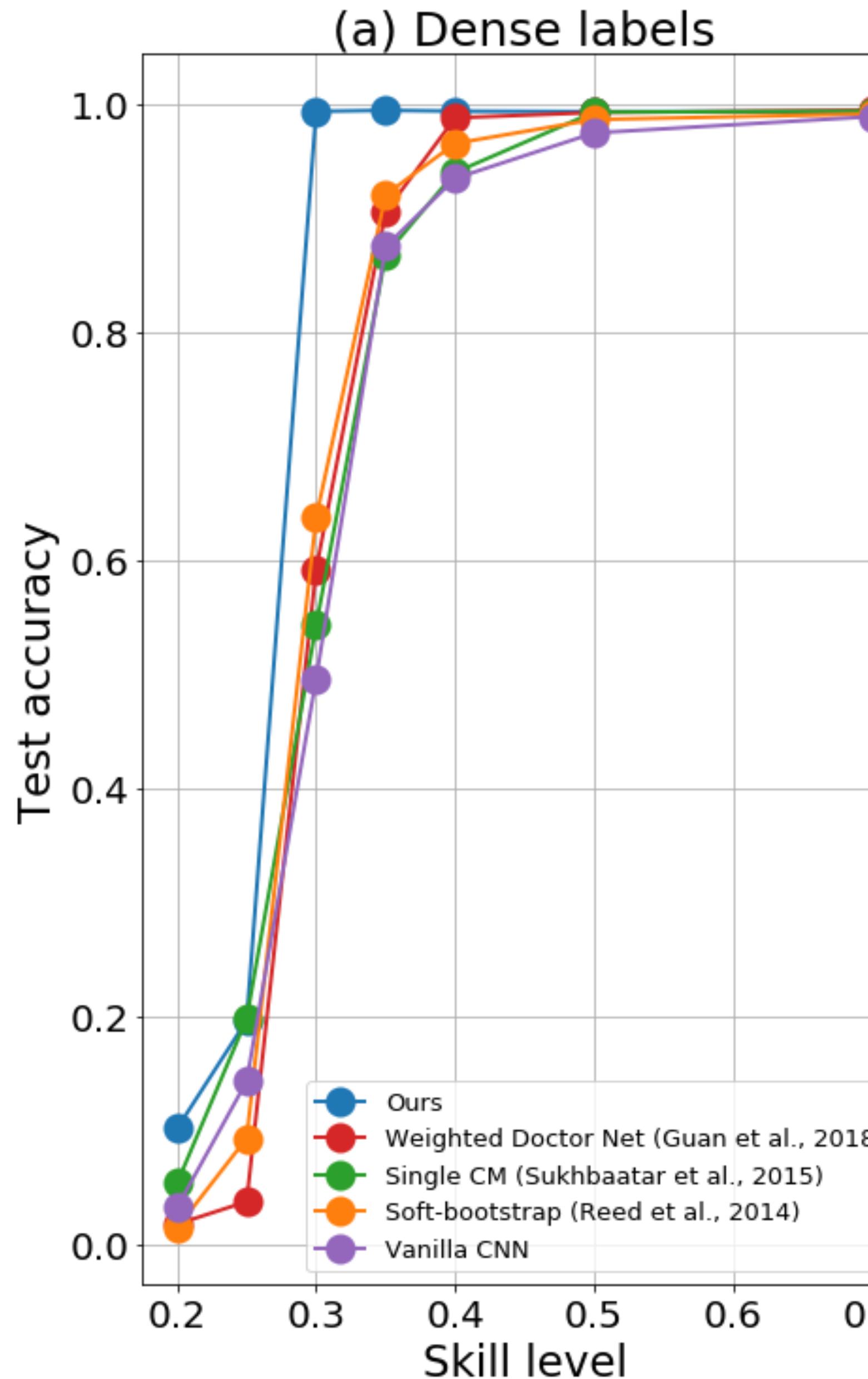


# When does it work (or fail)?



# Is it important model individual annotators?

Yes!



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---

Method	Accuracy
Our method	<b><math>81.23 \pm 0.21</math></b>
Single CM [22]	$68.82 \pm 2.27$
Weighted Doctor Net [24]	$60.11 \pm 1.80$
Soft-bootstrap [21]	$54.73 \pm 1.33$
Vanilla CNN [21]	$52.33 \pm 0.31$

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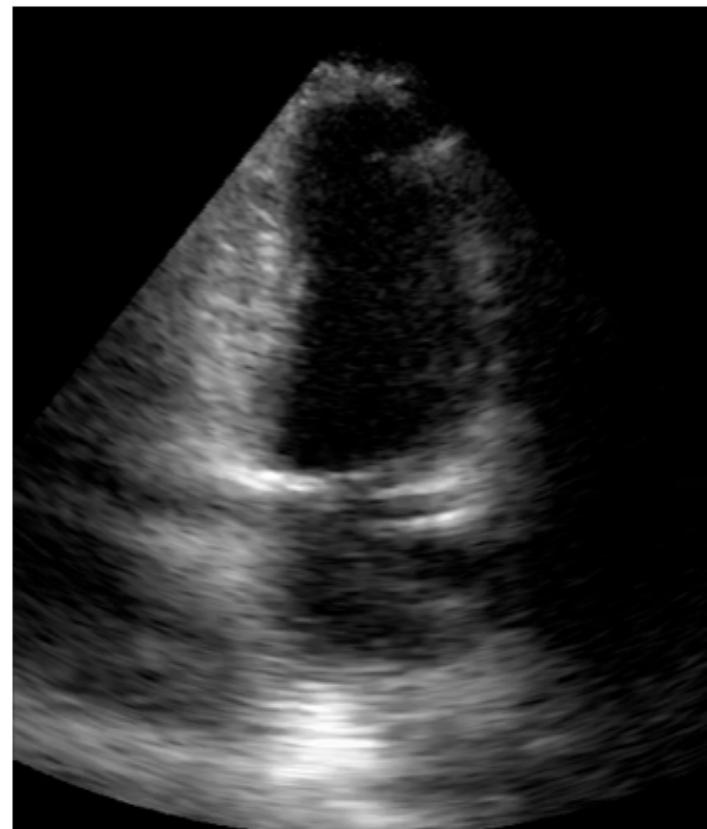


# Test on ultrasound data

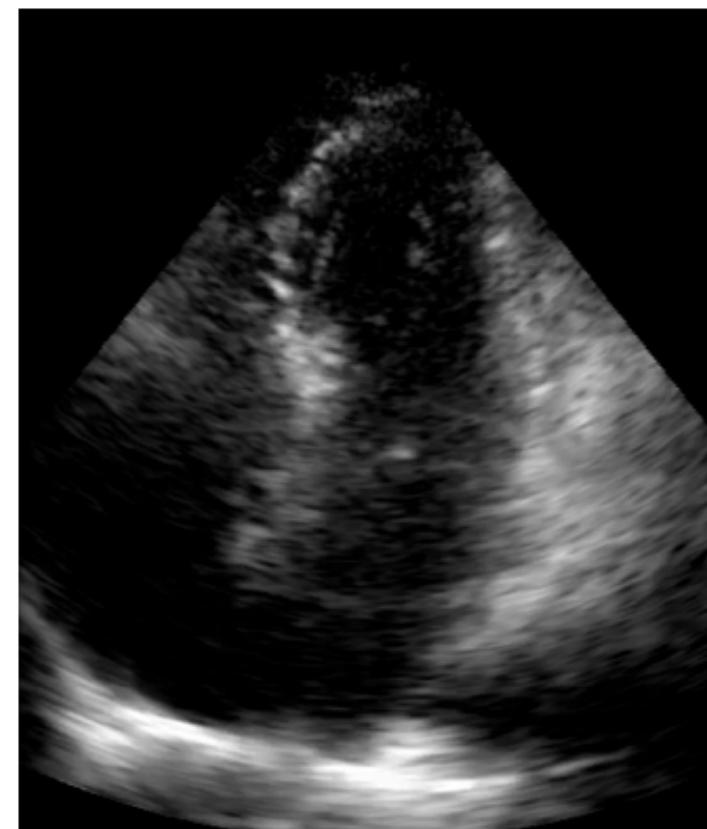
# Ultrasound Cardiac View Classification

- 6 classes
- 240,000 training images and 20, 000 test images
- Sparsely labelled by 9 experts + 2 engineers
- Ground truth generated as the unanimous labels from top 3 experts

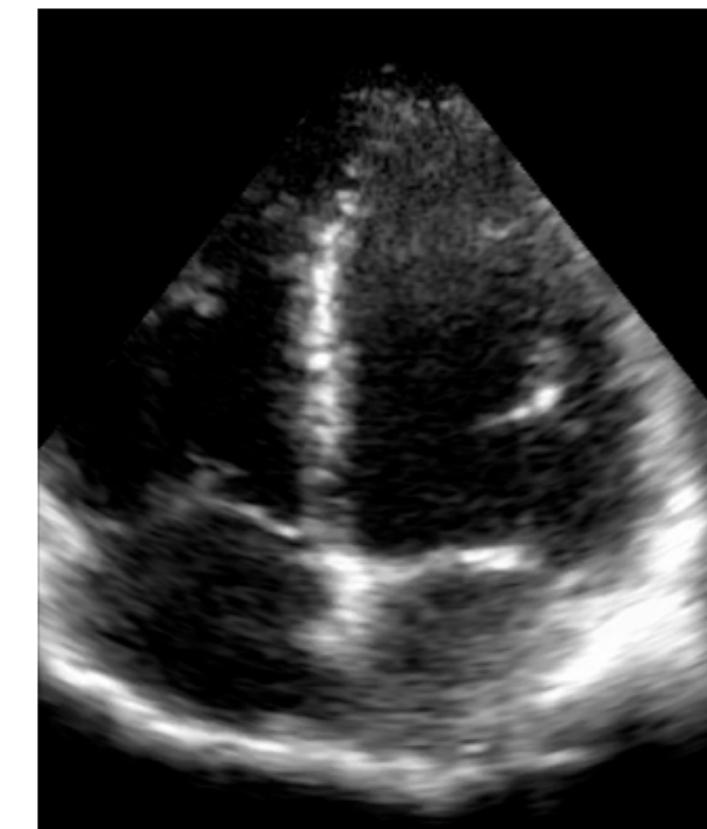
**A2C**



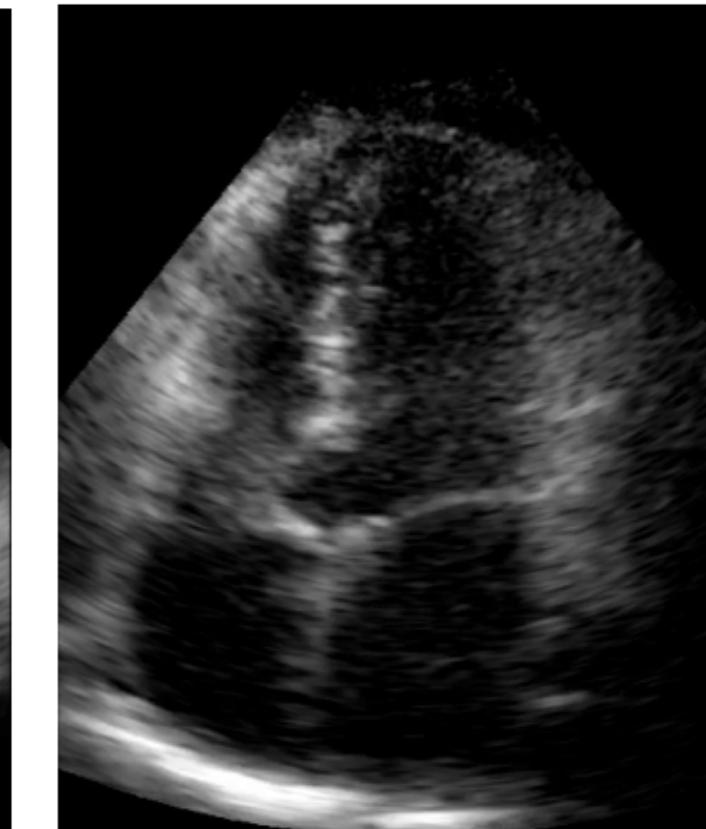
**A3C**



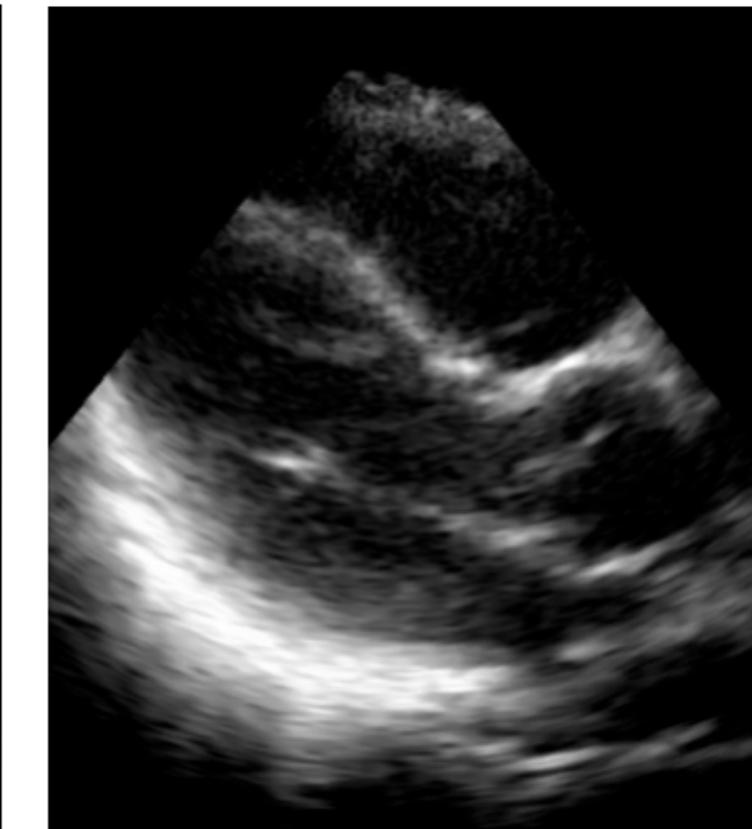
**A4C**



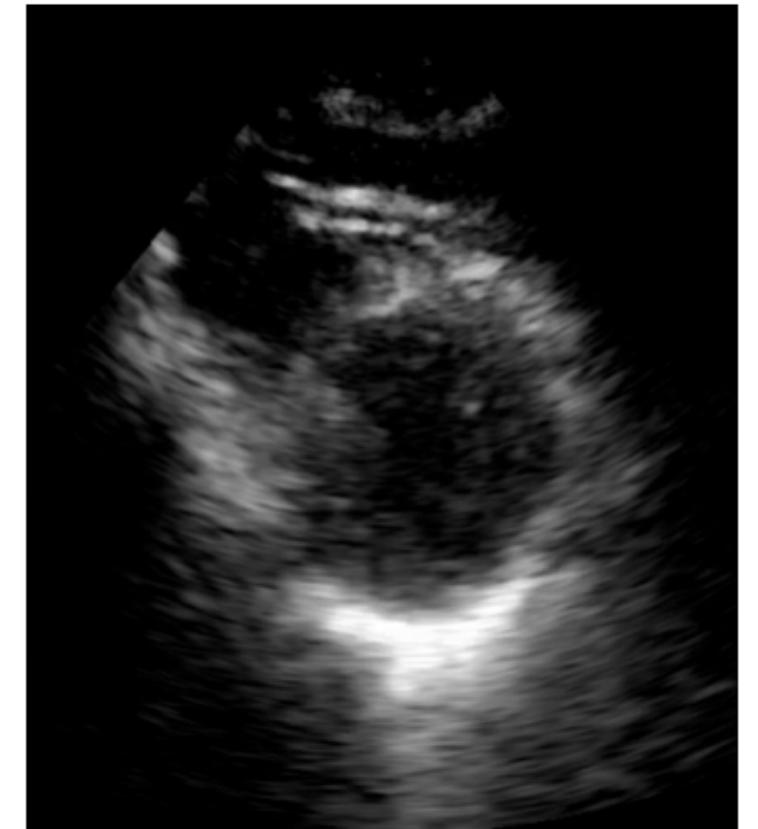
**A5C**



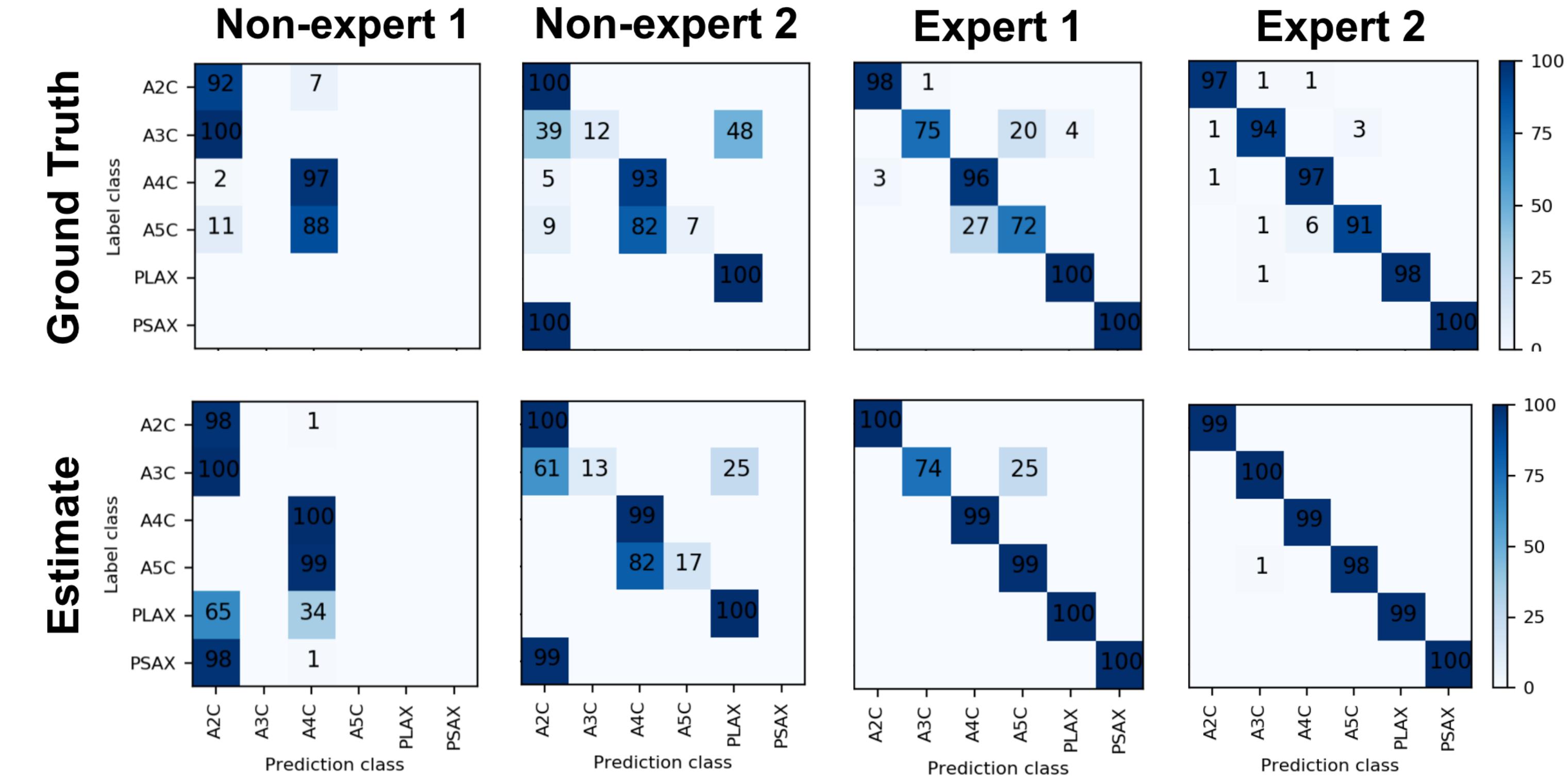
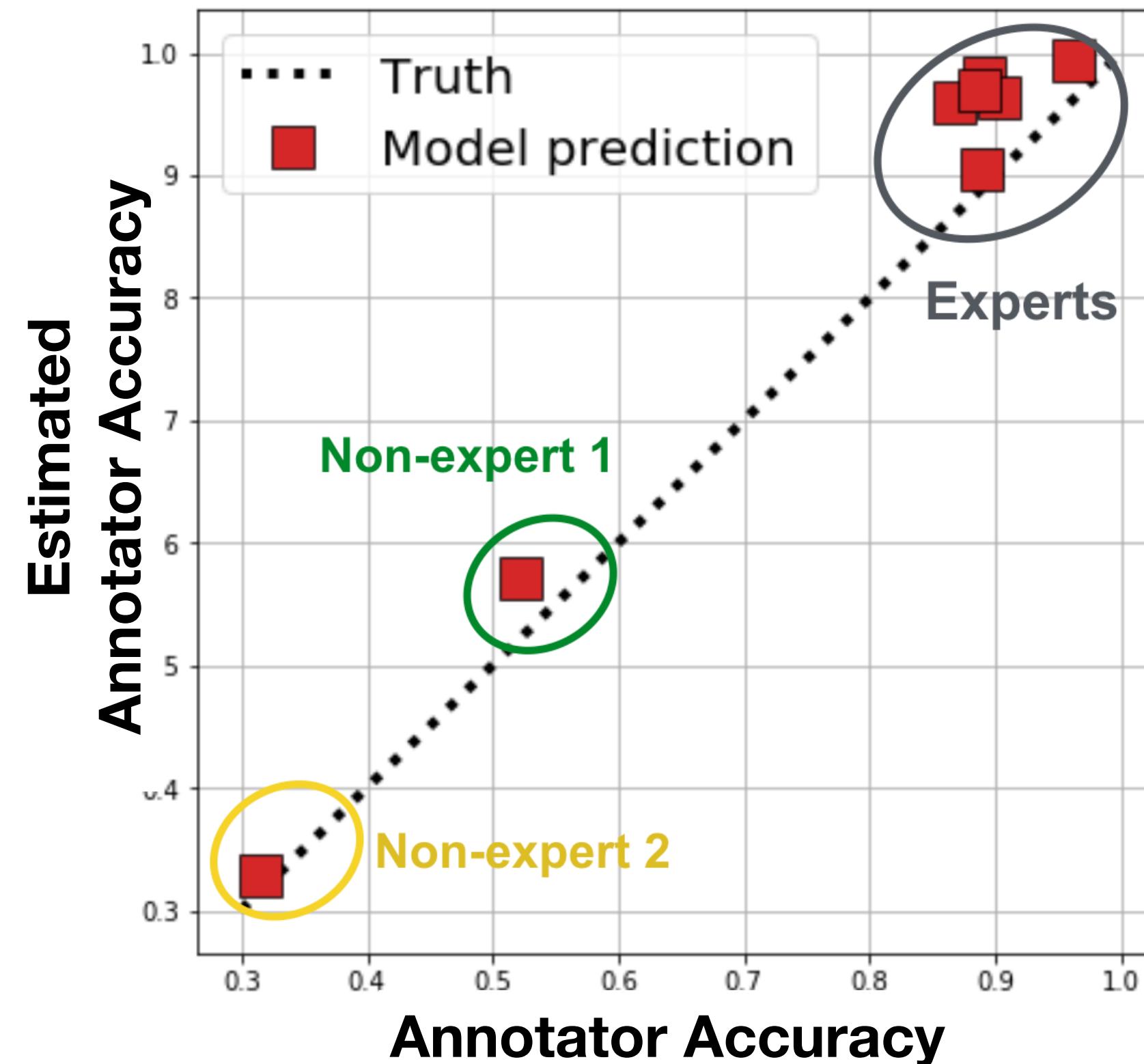
**PLAX**



**PSAX**



# Ultrasound Cardiac View Classification



Accuracy (%)	
Our method	$75.57 \pm 0.16$
Naive CNN	$70.95 \pm 0.44$

# Summary

- One model can simultaneously curate and learn from noisy data, performing better than the state-of-the-art in a very noisy mix of annotators with different skill levels.
- Successful recovery of confusion matrices, can visualise annotator mistakes.
- Robust performance with sparse labels (which is cheaper)

# Next Steps

- Account for prior knowledge e.g. expert levels
- Model image dependence of annotators
- Trying to infer different “schools of thoughts”
- Active Learning
- Extend to other tasks e.g. structured prediction?
  - ▶ Segmentation errors
  - ▶ Geometric errors e.g. misalignment
  - ▶ Artefacts in data (e.g. PVEs, motion, etc)

# Acknowledgements



Nathan Silberman



Ardavan Saeedi



Swami Sankaranarayanan



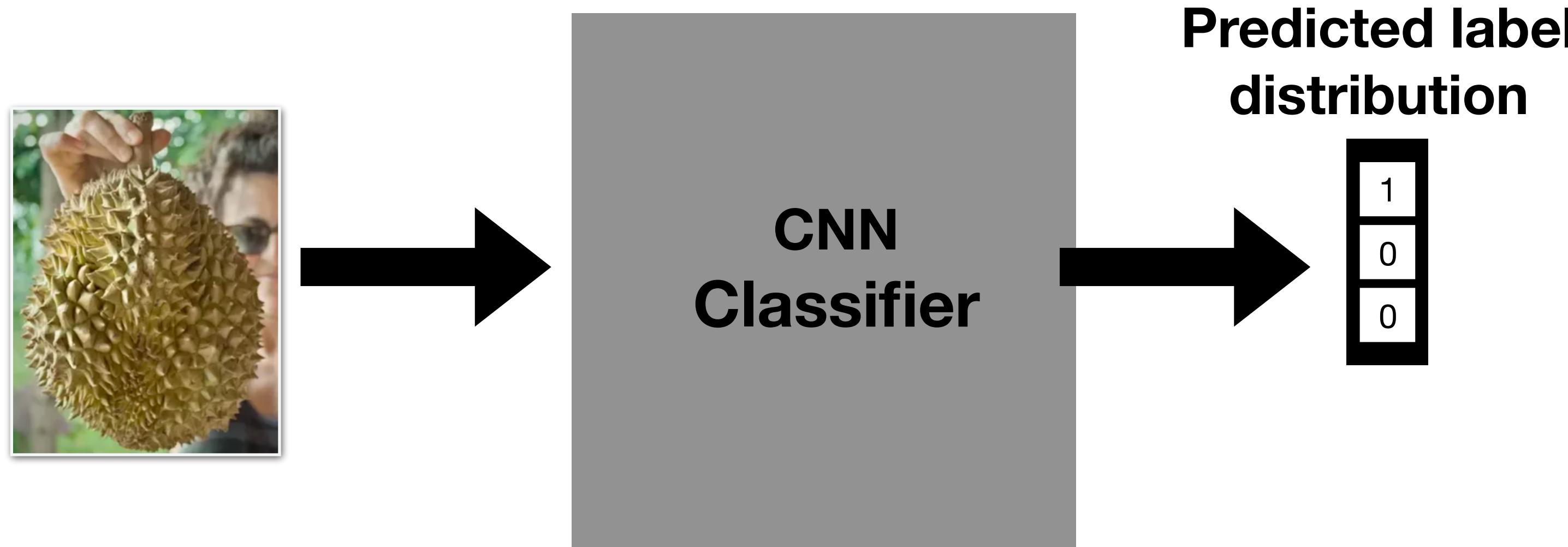
Danny C. Alexander



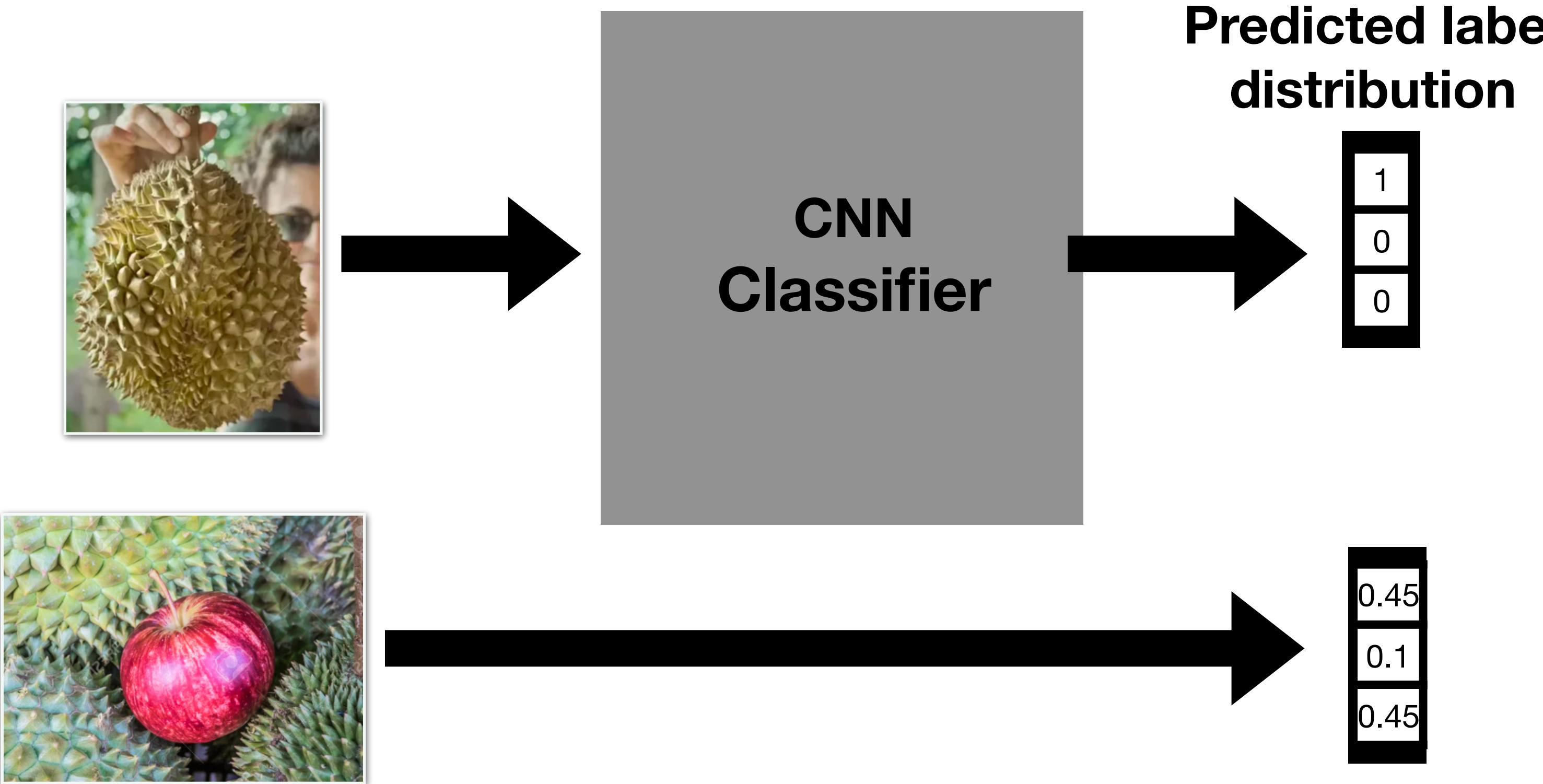
The image features a large, bold red text "thank you" at the center. Surrounding it are numerous other "thank you" expressions in various languages and colors, including blue, green, yellow, pink, purple, and orange. These include "спасибо" (Russian), "dankt" (Dutch), "dziekuje" (Polish), "obrigado" (Portuguese), "danke" (German), "sukriya" (Bengali), "terima kasih" (Indonesian), "감사합니다" (Korean), "dank je" (Afrikaans), "gracias" (Spanish), "mochchakkeram" (Burmese), "go raibh maith agat" (Irish), "arigatō" (Japanese), "merci" (French), "ngiyabonga" (Xhosa), "teşekkür ederim" (Turkish), and "dakujem" (Croatian). The background is white, and the overall design is colorful and diverse.

Can we gauge  
the difficulty of images?

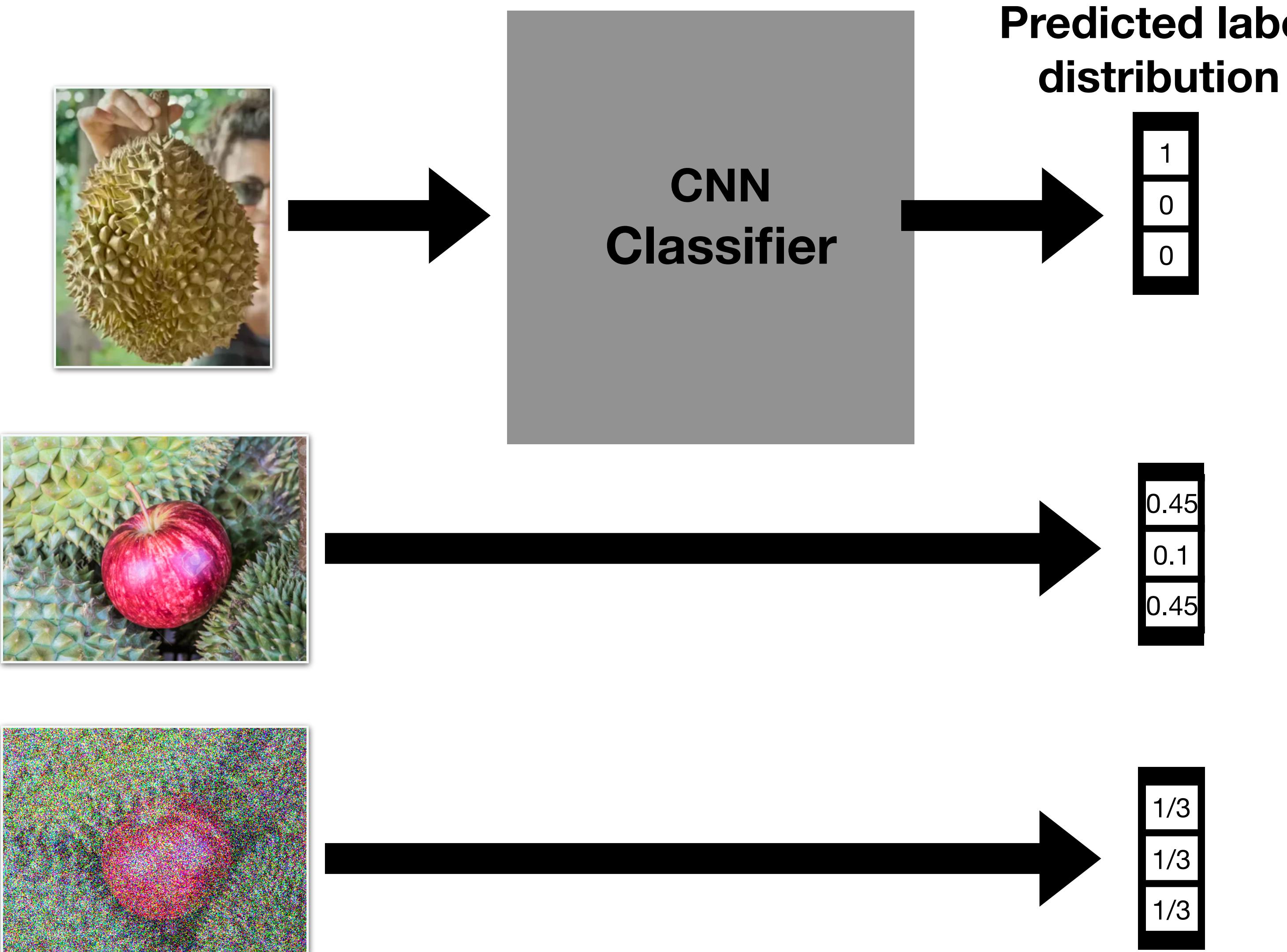
# Quantifying image difficulty



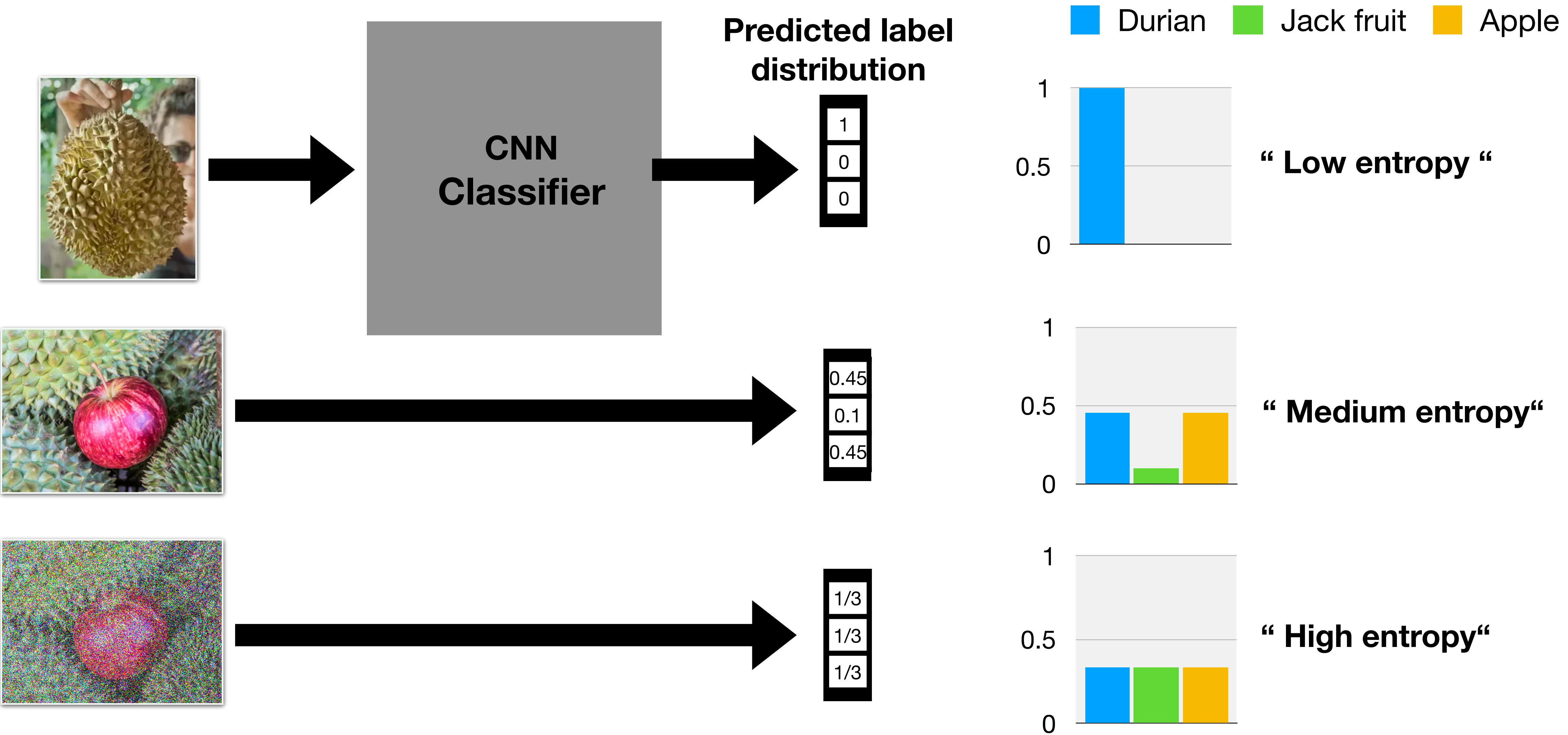
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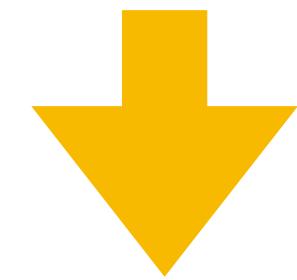
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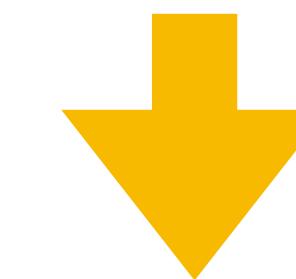
# Quantifying image noise

- Make the labelling task more difficult by corrupting images

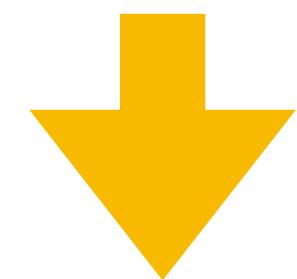
**Noise = 0 %**



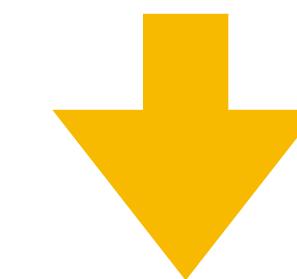
**Noise = 30 %**



**Noise = 60 %**



**Noise = 90 %**



# Quantifying image noise

- Labels are obtained from A+ Alice, A- Andy, Solid C Carl, Failing Frank
- Compare the correlation between **image noise level & entropy of label distribution**

	Naive softmax	Logit Noise	Loss Attenuation
Ours	0.72	<b>0.83</b>	0.77
Sukhbaatar et al., ICLR'15	0.80	0.81	<b>0.85</b>
Naive CNN	0.79	<b>0.87</b>	0.81