Package 'GA'

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Title Genetic Algorithms

Description Flexible general-purpose toolbox implementing genetic algorithms (GAs) for stochastic optimisation. Binary, real-valued, and permutation representations are available to optimize a fitness function, i.e. a function provided by users depending on their objective function. Several genetic operators are available and can be combined to explore the best settings for the current task. Furthermore, users can define new genetic operators and easily evaluate their performances. Local search using general-purpose optimisation algorithms can be applied stochastically to exploit interesting regions. GAs can be run sequentially or in parallel, using an explicit master-slave parallelisation or a coarse-grain islands approach.

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GA-package

Genetic Algorithms

Description

Flexible general-purpose toolbox implementing genetic algorithms (GAs) for stochastic optimisation. Binary, real-valued, and permutation representations are available to optimize a fitness function, i.e. a function provided by users depending on their objective function. Several genetic operators are available and can be combined to explore the best settings for the current task. Furthermore, users can define new genetic operators and easily evaluate their performances. Local search using general-purpose optimisation algorithms can be applied stochastically to exploit interesting regions. GAs can be run sequentially or in parallel, using an explicit master-slave parallelisation or a coarse-grain islands approach.

Details

For a quick intro to GA package see the vignette accompanying the package. Further details are provided in the papers referenced below.

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References

Scrucca, L. (2013) GA: A Package for Genetic Algorithms in R. *Journal of Statistical Software*, 53(4), 1-37. http://www.jstatsoft.org/v53/i04/

Scrucca, L. (2017) On some extensions to GA package: hybrid optimisation, parallelisation and islands evolution. *The R Journal*, 9/1, 187-206. https://journal.r-project.org/archive/2017/RJ-2017-008

Author(s)

Luca Scrucca < luca.scrucca@unipg.it>

binary2decimal

Binary encoding of decimal numbers and viceversa.

Description

Functions for computing binary to decimal conversion of numbers and viceversa.

Usage

```
decimal2binary(x, length)
binary2decimal(x)
```

Arguments

x input value.

length an optional value giving the length of binary string to return.

Details

decimal2binary converts a numerical value (which is forced to be an integer) to a binary representation, i.e. a vector of 0s and 1s. For real numerical values see the example below.

binary2binary converts a binary value, i.e. a vector of 0s and 1s, to a decimal representation.

Author(s)

Luca Scrucca

See Also

binary2gray

binary2gray

Examples

```
# for integer values
dval <- 12
(bval <- decimal2binary(dval))
binary2decimal(bval)

# for real values
dval <- 12.456
# use
(bval <- decimal2binary(dval*1000))
binary2decimal(bval)/1000</pre>
```

binary2gray

Gray encoding for binary strings

Description

Functions for computing Gray encoding from/to binary strings.

Usage

```
binary2gray(x)
gray2binary(x)
```

Arguments

Χ

the string to be evaluated

Details

Gray encoding allows to obtain binary strings not affected by the well-known Hamming cliff problem. With Gray encoding the number of bit differences between any two consecutive values is one, whereas in binary strings this is not always true.

Author(s)

Luca Scrucca

See Also

binary2decimal

Examples

```
# Consider a five-bit encoding of values 15 and 16 using the standard
# binary coding
decimal2binary(15, 5)
decimal2binary(16, 5)
# Moving from 15 to 16 (or viceversa) all five bits need to be changed,
# but using Gray encoding the two binary strings differ by one bit.
binary2gray(decimal2binary(15, 5))
binary2gray(decimal2binary(16, 5))
```

ga

Genetic Algorithms

Description

Maximization of a fitness function using genetic algorithms (GAs). Local search using general-purpose optimisation algorithms can be applied stochastically to exploit interesting regions. The algorithm can be run sequentially or in parallel using an explicit master-slave parallelisation.

Usage

```
ga(type = c("binary", "real-valued", "permutation"),
   fitness, ...,
   lower, upper, nBits,
   population = gaControl(type)$population,
   selection = gaControl(type)$selection,
   crossover = gaControl(type)$crossover,
   mutation = gaControl(type)$mutation,
   popSize = 50,
   pcrossover = 0.8,
   pmutation = 0.1,
   elitism = base::max(1, round(popSize*0.05)),
   updatePop = FALSE,
   postFitness = NULL,
   maxiter = 100,
   run = maxiter,
   maxFitness = Inf,
   names = NULL,
   suggestions = NULL,
   optim = FALSE,
   optimArgs = list(method = "L-BFGS-B",
                    poptim = 0.05,
                    pressel = 0.5,
                    control = list(fnscale = -1, maxit = 100)),
   keepBest = FALSE,
   parallel = FALSE,
   monitor = if(interactive()) gaMonitor else FALSE,
   seed = NULL)
```

Arguments

fitness

the type of genetic algorithm to be run depending on the nature of decision type variables. Possible values are:

"binary" for binary representations of decision variables.

"real-valued" for optimization problems where the decision variables are floating-point representations of real numbers.

"permutation" for problems that involves reordering of a list of objects.

the fitness function, any allowable R function which takes as input an individual

string representing a potential solution, and returns a numerical value describ-

ing its "fitness".

additional arguments to be passed to the fitness function. This allows to write

fitness functions that keep some variables fixed during the search.

lower a vector of length equal to the decision variables providing the lower bounds of

the search space in case of real-valued or permutation encoded optimizations. Formerly this argument was named min; its usage is allowed but deprecated.

a vector of length equal to the decision variables providing the upper bounds of upper

the search space in case of real-valued or permutation encoded optimizations. Formerly this argument was named max; its usage is allowed but deprecated.

nBits a value specifying the number of bits to be used in binary encoded optimizations.

population an R function for randomly generating an initial population. See ga_Population

for available functions.

an R function performing selection, i.e. a function which generates a new popselection

ulation of individuals from the current population probabilistically according to

individual fitness. See ga_Selection for available functions.

an R function performing crossover, i.e. a function which forms offsprings by crossover

combining part of the genetic information from their parents. See ga_Crossover

for available functions.

an R function performing mutation, i.e. a function which randomly alters the mutation

values of some genes in a parent chromosome. See ga_Mutation for available

functions.

popSize the population size.

updatePop a logical defaulting to FALSE. If set at TRUE the first attribute attached to the value

returned by the user-defined fitness function is used to update the population.

Be careful though, this is an experimental feature!

postFitness a user-defined function which, if provided, receives the current ga-class object

as input, performs post fitness-evaluation steps, then returns an updated version

of the object which is used to update the GA search. Be careful though, this is an experimental feature!

pcrossover the probability of crossover between pairs of chromosomes. Typically this is a

large value and by default is set to 0.8.

pmutation the probability of mutation in a parent chromosome. Usually mutation occurs

with a small probability, and by default is set to 0.1.

elitism the number of best fitness individuals to survive at each generation. By default the top 5% individuals will survive at each iteration.

maxiter the maximum number of iterations to run before the GA search is halted.

run the number of consecutive generations without any improvement in the best

fitness value before the GA is stopped.

maxFitness the upper bound on the fitness function after that the GA search is interrupted.

names a vector of character strings providing the names of decision variables.

suggestions a matrix of solutions strings to be included in the initial population. If provided the number of columns must match the number of decision variables.

a logical defaulting to FALSE determining whether or not a local search using general-purpose optimisation algorithms should be used. See argument optimArgs for further details and finer control.

a list controlling the local search algorithm with the following components:

method a string specifying the general-purpose optimisation method to be used, by default is set to "L-BFGS-B". Other possible methods are those reported in optim.

poptim a value in the range [0,1] specifying the probability of performing a local search at each iteration of GA (default 0.1).

pressel a value in the range [0,1] specifying the pressure selection (default 0.5). The local search is started from a random solution selected with probability proportional to fitness. High values of pressel tend to select the solutions with the largest fitness, whereas low values of pressel assign quasi-uniform probabilities to any solution.

control a list of control parameters. See 'Details' section in optim.

a logical argument specifying if best solutions at each iteration should be saved in a slot called bestSol. See ga-class.

An optional argument which allows to specify if the Genetic Algorithm should be run sequentially or in parallel.

For a single machine with multiple cores, possible values are:

- a logical value specifying if parallel computing should be used (TRUE) or not (FALSE, default) for evaluating the fitness function;
- a numerical value which gives the number of cores to employ. By default, this is obtained from the function detectCores;
- a character string specifying the type of parallelisation to use. This depends on system OS: on Windows OS only "snow" type functionality is available, while on Unix/Linux/Mac OSX both "snow" and "multicore" (default) functionalities are available.

In all the cases described above, at the end of the search the cluster is automatically stopped by shutting down the workers.

If a cluster of multiple machines is available, evaluation of the fitness function can be executed in parallel using all, or a subset of, the cores available to the machines belonging to the cluster. However, this option requires more work from the user, who needs to set up and register a parallel back end. In this case the cluster must be explicitly stopped with stopCluster.

optimArgs

optim

keepBest

parallel

monitor a logical or an R function which takes as input the current state of the ga-class

object and show the evolution of the search. By default, for interactive sessions the function <code>gaMonitor</code> prints the average and best fitness values at each iteration. If set to plot these information are plotted on a graphical device. Other functions can be written by the user and supplied as argument. In non interactive

sessions, by default monitor = FALSE so any output is suppressed.

seed an integer value containing the random number generator state. This argument

can be used to replicate the results of a GA search. Note that if parallel comput-

ing is required, the doRNG package must be installed.

Details

Genetic algorithms (GAs) are stochastic search algorithms inspired by the basic principles of biological evolution and natural selection. GAs simulate the evolution of living organisms, where the fittest individuals dominate over the weaker ones, by mimicking the biological mechanisms of evolution, such as selection, crossover and mutation.

The **GA** package is a collection of general purpose functions that provide a flexible set of tools for applying a wide range of genetic algorithm methods.

The ga function enables the application of GAs to problems where the decision variables are encoded as "binary", "real-valued", or "permutation" strings.

Default genetic operators are set via gaControl. To retrieve the currently set operators:

```
gaControl("binary")
gaControl("real-valued")
gaControl("permutation")
```

Value

Returns an object of class ga-class. See ga-class for a description of available slots information.

Author(s)

Luca Scrucca < luca.scrucca@unipg.it>

References

Back T., Fogel D., Michalewicz Z. (2000). *Evolutionary Computation 1: Basic Algorithms and Operators*. IOP Publishing Ltd., Bristol and Philadelphia.

Back T., Fogel D., Michalewicz Z. (2000b). *Evolutionary Computation 2: Advanced Algorithms and Operators*. IOP Publishing Ltd., Bristol and Philadelphia.

Coley D. (1999). An Introduction to Genetic Algorithms for Scientists and Engineers. World Scientific Pub. Co. Inc., Singapore.

Eiben A., Smith J. (2003). *Introduction to Evolutionary Computing*. Springer-Verlag, Berlin Heidelberg.

Goldberg D. (1989). Genetic Algorithms in Search, Optimization, and Machine Learning. Addison-Wesley Professional, Boston, MA.

Haupt R. L., Haupt S. E. (2004). *Practical Genetic Algorithms*. 2nd edition. John Wiley & Sons, New York.

Luke S. (2013) *Essentials of Metaheuristics*, 2nd edition. Lulu. Freely available at http://cs.gmu.edu/~sean/book/metaheuristics/.

Scrucca L. (2013). GA: A Package for Genetic Algorithms in R. *Journal of Statistical Software*, 53(4), 1-37, http://www.jstatsoft.org/v53/i04/.

Scrucca, L. (2017) On some extensions to GA package: hybrid optimisation, parallelisation and islands evolution. *The R Journal*, 9/1, 187-206. https://journal.r-project.org/archive/2017/RJ-2017-008

Simon D. (2013) Evolutionary Optimization Algorithms. John Wiley & Sons.

Sivanandam S., Deepa S. (2007). *Introduction to Genetic Algorithms*. Springer-Verlag, Berlin Heidelberg.

Yu X., Gen M. (2010). *Introduction to Evolutionary Algorithms*. Springer-Verlag, Berlin Heidelberg.

See Also

summary, ga-method, plot, ga-method, ga-class, ga_Population, ga_Selection, ga_Crossover, ga_Mutation, gaControl.

Examples

```
# 1) one-dimensional function
f \leftarrow function(x) abs(x) + cos(x)
curve(f, -20, 20)
fitness <- function(x) -f(x)
GA <- ga(type = "real-valued", fitness = fitness, lower = -20, upper = 20)
summary(GA)
plot(GA)
curve(f, -20, 20)
abline(v = GA@solution, lty = 3)
# 2) one-dimensional function
f < -function(x) (x^2+x)*cos(x) # -10 < x < 10
curve(f, -10, 10)
# write your own tracing function
monitor <- function(obj)</pre>
  curve(f, -10, 10, main = paste("iteration =", obj@iter))
  points(obj@population, obj@fitness, pch = 20, col = 2)
  rug(obj@population, col = 2)
  Sys.sleep(0.2)
## Not run:
```

```
GA <- ga(type = "real-valued", fitness = f, lower = -10, upper = 10, monitor = monitor)
## End(Not run)
# or if you want to suppress the tracing
GA <- ga(type = "real-valued", fitness = f, lower = -10, upper = 10, monitor = NULL)
monitor(GA)
abline(v = GA@solution, lty = 3)
# 3) two-dimensional Rastrigin function
Rastrigin <- function(x1, x2)</pre>
  20 + x1^2 + x2^2 - 10*(cos(2*pi*x1) + cos(2*pi*x2))
x1 \leftarrow x2 \leftarrow seq(-5.12, 5.12, by = 0.1)
f <- outer(x1, x2, Rastrigin)</pre>
persp3D(x1, x2, f, theta = 50, phi = 20)
filled.contour(x1, x2, f, color.palette = jet.colors)
GA <- ga(type = "real-valued", fitness = function(x) -Rastrigin(x[1], x[2]),
         lower = c(-5.12, -5.12), upper = c(5.12, 5.12),
         popSize = 50, maxiter = 100)
summary(GA)
plot(GA)
# 4) Parallel GA
# Simple example of an expensive fitness function obtained artificially by
# introducing a pause statement.
## Not run:
Rastrigin <- function(x1, x2)</pre>
  Sys.sleep(0.1)
  20 + x1^2 + x2^2 - 10*(cos(2*pi*x1) + cos(2*pi*x2))
system.time(GA1 <- ga(type = "real-valued",</pre>
                       fitness = function(x) -Rastrigin(x[1], x[2]),
                       lower = c(-5.12, -5.12), upper = c(5.12, 5.12),
                       popSize = 50, maxiter = 100, monitor = FALSE,
                       seed = 12345))
system.time(GA2 <- ga(type = "real-valued",</pre>
                      fitness = function(x) -Rastrigin(x[1], x[2]),
                       lower = c(-5.12, -5.12), upper = c(5.12, 5.12),
                       popSize = 50, maxiter = 100, monitor = FALSE,
                       seed = 12345, parallel = TRUE))
## End(Not run)
# 5) Hybrid GA
```

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ga-class

Class "ga"

Description

An S4 class for genetic algorithms

Objects from the Class

Objects can be created by calls to the ga function.

Slots

call an object of class "call" representing the matched call;

type a character string specifying the type of genetic algorithm used;

lower a vector providing for each decision variable the lower bounds of the search space in case of real-valued or permutation encoded optimisations. Formerly this slot was named min;

upper a vector providing for each decision variable the upper bounds of the search space in case of real-valued or permutation encoded optimizations. Formerly this slot was named max;

nBits a value specifying the number of bits to be used in binary encoded optimizations;

names a vector of character strings providing the names of decision variables (optional);

popSize the population size;

iter the actual (or final) iteration of GA search;

run the number of consecutive generations without any improvement in the best fitness value before the GA is stopped;

maxiter the maximum number of iterations to run before the GA search is halted;

suggestions a matrix of user provided solutions and included in the initial population;

population the current (or final) population;

elitism the number of best fitness individuals to survive at each generation;

12 gaControl

```
pcrossover the crossover probability;

pmutation the mutation probability;

fitness the values of fitness function for the current (or final) population;

summary a matrix of summary statistics for fitness values at each iteration (along the rows);

bestSol if keepBest = TRUE, the best solutions at each iteration;

fitnessValue the best fitness value at the final iteration;

solution the value(s) of the decision variables giving the best fitness at the final iteration.
```

Author(s)

Luca Scrucca

See Also

For examples of usage see ga.

gaControl

A function for setting or retrieving defaults genetic operators

Description

Default settings for genetic operators used in the GA package.

Usage

```
gaControl(...)
```

Arguments

.. no arguments, a single character vector, or a named list with components.

Details

If the function is called with no arguments returns the current default settings, i.e., a list with the following default components:

```
• "binary"
```

```
- population = "gabin_Population"
```

- selection = "gabin_lrSelection"
- crossover = "gabin_spCrossover"
- mutation = "gabin_raMutation"
- "real-valued"
 - population = "gareal_Population"
 - selection = "gareal_lsSelection"
 - crossover = "gareal_laCrossover"

gaControl 13

```
- mutation = "gareal_raMutation"

• "permutation"

- population = "gaperm_Population"

- selection = "gaperm_lrSelection"

- crossover = "gaperm_oxCrossover"

- mutation = "gaperm_simMutation"

• "eps" = the tolerance value used by the package functions. By default set at sqrt(.Machine$double.eps).
```

The function may be called with a single string specifying the name of the component. In this case

the function returns the current default settings.

To change the default values, a named component must be followed by a single value (in case of "eps") or a list of component(s) specifying the name of the function for a genetic operator. See the Examples section.

Value

If the argument list is empty the function returns the current list of values. If the argument list is not empty, the returned list is invisible.

Note

The parameter values set via a call to this function will remain in effect for the rest of the session, affecting the subsequent behaviour of the functions for which the given parameters are relevant.

Author(s)

Luca Scrucca

See Also

ga

Examples

gaisl

Islands Genetic Algorithms

Description

Maximization of a fitness function using islands genetic algorithms (ISLGAs). This is a distributed multiple-population GA, where the population is partitioned into several subpopulations and assigned to separated islands. Independent GAs are executed in each island, and only occasionally sparse exchanges of individuals are performed among the islands. In principle islands can evolve sequentially, but increased computational efficiency is obtained by running GAs in parallel on each island. The latter is called island parallel GAs (ISLPGAs) and it is used by default.

Usage

```
gaisl(type = c("binary", "real-valued", "permutation"),
      fitness, ...,
      lower, upper, nBits,
      population = gaControl(type)$population,
      selection = gaControl(type)$selection,
      crossover = gaControl(type)$crossover,
      mutation = gaControl(type)$mutation,
      popSize = 100,
      numIslands = 4,
      migrationRate = 0.1,
      migrationInterval = 10,
      pcrossover = 0.8,
      pmutation = 0.1,
      elitism = base::max(1, round(popSize/numIslands*0.05)),
      updatePop = FALSE,
      postFitness = NULL,
      maxiter = 1000,
      run = maxiter,
      maxFitness = Inf,
      names = NULL,
      suggestions = NULL,
      optim = FALSE,
      optimArgs = list(method = "L-BFGS-B",
                       poptim = 0.05,
                       pressel = 0.5,
                       control = list(fnscale = -1, maxit = 100)),
      parallel = TRUE,
      monitor = if(interactive()) gaislMonitor else FALSE,
      seed = NULL)
```

Arguments

type

the type of genetic algorithm to be run depending on the nature of decision variables. Possible values are:

"binary" for binary representations of decision variables.

"real-valued" for optimization problems where the decision variables are floating-point representations of real numbers.

"permutation" for problems that involves reordering of a list.

fitness the fitness function, any allowable R function which takes as input an individual

string representing a potential solution, and returns a numerical value describ-

ing its "fitness".

... additional arguments to be passed to the fitness function. This allows to write

fitness functions that keep some variables fixed during the search.

lower a vector of length equal to the decision variables providing the lower bounds of

the search space in case of real-valued or permutation encoded optimizations. Formerly this argument was named min; its usage is allowed but deprecated.

upper a vector of length equal to the decision variables providing the upper bounds of

the search space in case of real-valued or permutation encoded optimizations. Formerly this argument was named max; its usage is allowed but deprecated.

nBits a value specifying the number of bits to be used in binary encoded optimizations.

population an R function for randomly generating an initial population. See ga_Population

for available functions.

numIslands an integer value specifying the number of islands to be used in a ring topology,

in which each island is connected unidirectionally with another island, hence

forming a single continuous pathway.

migrationRate a value in the range \$[0,1]\$ providing the proportion of individuals that should

migrate between the islands.

migrationInterval

an integer value specifying the number of iterations at which exchange of indi-

viduals takes place.

selection an R function performing selection, i.e. a function which generates a new pop-

ulation of individuals from the current population probabilistically according to

individual fitness. See ga_Selection for available functions.

crossover an R function performing crossover, i.e. a function which forms offsprings by

combining part of the genetic information from their parents. See $ga_Crossover$

for available functions.

mutation an R function performing mutation, i.e. a function which randomly alters the

values of some genes in a parent chromosome. See ga_Mutation for available

functions.

popSize the population size.

updatePop a logical defaulting to FALSE. If set at TRUE the first attribute attached to the value

returned by the user-defined fitness function is used to update the population.

Be careful though, this is an experimental feature!

postFitness a user-defined function which, if provided, receives the current ga-class object

as input, performs post fitness-evaluation steps, then returns an updated version

of the object which is used to update the GA search. *Be careful though, this is an experimental feature!*

the probability of crossover between pairs of chromosomes. Typically this is a large value and by default is set to 0.8.

pmutation the probability of mutation in a parent chromosome. Usually mutation occurs with a small probability, and by default is set to 0.1.

elitism the number of best fitness individuals to survive at each generation. By default the top 5% individuals in each island will survive at each iteration.

the maximum number of iterations to run before the GA search is halted. the number of consecutive generations without any improvement in the best fitness value before the GA is stopped.

the upper bound on the fitness function after that the GA search is interrupted. a vector of character strings providing the names of decision variables.

a matrix of solutions strings to be included in the initial population. If provided the number of columns must match the number of decision variables.

a logical defaulting to FALSE determining whether or not a local search using general-purpose optimisation algorithms should be used. See argument optimArgs for further details and finer control.

method a string specifying the general-purpose optimisation method to be used, by default is set to "L-BFGS-B". Other possible methods are those reported in optim.

a list controlling the local search algorithm with the following components:

poptim a value in the range [0,1] specifying the probability of performing a local search at each iteration of GA (default 0.1).

pressel a value in the range [0,1] specifying the pressure selection (default 0.5). The local search is started from a random solution selected with probability proportional to fitness. High values of pressel tend to select the solutions with the largest fitness, whereas low values of pressel assign quasi-uniform probabilities to any solution.

control a list of control parameters. See 'Details' section in optim.

An optional argument which allows to specify if the Islands Genetic Algorithm should be run sequentially or in parallel.

For a single machine with multiple cores, possible values are:

- a logical value specifying if parallel computing should be used (TRUE) or not (FALSE, default) for running GAs on each island;
- a numerical value which gives the number of cores to employ. By default, this is obtained from the function detectCores;
- a character string specifying the type of parallelisation to use. This depends on system OS: on Windows OS only "snow" type functionality is available, while on Unix/Linux/Mac OSX both "snow" and "multicore" (default) functionalities are available.

In all the cases described above, at the end of the search the cluster is automatically stopped by shutting down the workers.

If a cluster of multiple machines is available, evolution of GAs on each island can be executed in parallel using all, or a subset of, the cores available to the

optim

maxiter run

maxFitness

suggestions

names

optimArgs

parallel

machines belonging to the cluster. However, this option requires more work from the user, who needs to set up and register a parallel back end. In this case the cluster must be explicitly stopped with stopCluster.

monitor

a logical or an R function which takes as input the current state of the gaisl-class object and show the evolution of the search in different epochs. By default, for interactive sessions, the function gaislMonitor prints the average and best fitness values at each epoch for each island. In non interactive sessions, by default monitor = FALSE so any output is suppressed.

seed

an integer value containing the random number generator state. This argument can be used to replicate the results of a ISLGA search. Note that if parallel computing is required, the **doRNG** package must be installed.

Details

Genetic algorithms (GAs) are stochastic search algorithms inspired by the basic principles of biological evolution and natural selection. GAs simulate the evolution of living organisms, where the fittest individuals dominate over the weaker ones, by mimicking the biological mechanisms of evolution, such as selection, crossover and mutation.

The gaisl function implements the islands GAs approach, where the population is partitioned into several subpopulations and assigned to separated islands. Independent GAs are executed in each island, and only occasionally sparse exchanges of individuals are performed among the islands. The algorithm can be run in parallel or sequentially. For more information on GAs see ga.

Value

Returns an object of class gaisl-class. See gaisl-class for a description of available slots information.

Author(s)

Luca Scrucca < luca.scrucca@unipg.it>

References

Luque G., Alba E. (2011) Parallel Genetic Algorithms: Theory and Real World Applications. Springer.

Luke S. (2013) *Essentials of Metaheuristics*, 2nd edition. Lulu. Freely available at http://cs.gmu.edu/~sean/book/metaheuristics/.

Scrucca, L. (2017) On some extensions to GA package: hybrid optimisation, parallelisation and islands evolution. *The R Journal*, 9/1, 187-206. https://journal.r-project.org/archive/2017/RJ-2017-008

See Also

summary,gaisl-method,plot,gaisl-method,gaisl-class,ga

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Examples

```
## Not run:
# two-dimensional Rastrigin function
Rastrigin <- function(x1, x2)</pre>
  20 + x1^2 + x2^2 - 10*(cos(2*pi*x1) + cos(2*pi*x2))
x1 <- x2 <- seq(-5.12, 5.12, by = 0.1)
f <- outer(x1, x2, Rastrigin)
persp3D(x1, x2, f, theta = 50, phi = 20)
filled.contour(x1, x2, f, color.palette = jet.colors)
GA <- gaisl(type = "real-valued",
            fitness = function(x) -Rastrigin(x[1], x[2]),
            lower = c(-5.12, -5.12), upper = c(5.12, 5.12),
            popSize = 80, maxiter = 500,
            numIslands = 4, migrationInterval = 50)
summary(GA)
plot(GA)
## End(Not run)
```

gaisl-class

Class "gaisl"

Description

An S4 class for islands genetic algorithms (ISLGAs)

Objects from the Class

Objects can be created by calls to the gaisl function.

Slots

```
call an object of class "call" representing the matched call;
```

type a character string specifying the type of genetic algorithm used;

lower a vector providing for each decision variable the lower bounds of the search space in case of real-valued or permutation encoded optimisations. Formerly this slot was named min;

upper a vector providing for each decision variable the upper bounds of the search space in case of real-valued or permutation encoded optimizations. Formerly this slot was named max;

nBits a value specifying the number of bits to be used in binary encoded optimizations;

names a vector of character strings providing the names of decision variables (optional);

popSize the population size;

numIslands the number of islands;

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```
migrationRate the migration rate;
```

migrationInterval the migration interval;

maxiter the maximum number of ISLGA iterations before the search is halted;

run the number of consecutive generations without any improvement in the best fitness value before the ISLGA is stopped;

maxiter the maximum number of iterations to run before the GA search is halted;

suggestions a matrix of user provided solutions and included in the initial population;

elitism the number of best fitness individuals to survive at each generation;

pcrossover the crossover probability;

pmutation the mutation probability;

islands a list containing the "ga" objects corresponding to each island GA evolution;

summary a list of matrices of summary statistics for fitness values at each iteration (along the rows). Each element of the list corresponds to the evolution of an island;

fitnessValues a list of best fitness values found in each island at the final iteration;

solutions a list of matrices, one for each island, containing the values of the decision variables giving the best fitness at the final iteration;

fitnessValue the best fitness value at the final iteration;

solution a matrix containing the values of the decision variables giving the best fitness at the final iteration

Author(s)

Luca Scrucca

See Also

For examples of usage see gaisl.

gaMonitor

Monitor genetic algorithm evolution

Description

Functions to print summary statistics of fitness values at each iteration of a GA search.

Usage

```
gaMonitor(object, digits = getOption("digits"), ...)
gaislMonitor(object, digits = getOption("digits"), ...)
```

20 gaSummary

Arguments

object	an object of class ga-class or gaisl-class, usually resulting from a call to
	function ga or gaisl, respectively.
digits	minimal number of significant digits.
	further arguments passed to or from other methods.

Value

These functions print a summary of current GA step on the console.

By default, gaMonitor is called in interactive sessions by ga. The old monitoring function, used as the default until version 2.2 of **GA** package, is provided in gaMonitor2.

By default, gaislMonitor is called in interactive sessions by gaisl.

Author(s)

Luca Scrucca

gaSummary

Summarize genetic algorithm evolution

Description

A function which returns fitness summary statistics at each iteration of GA search.

Usage

```
gaSummary(x, ...)
```

Arguments

x a vector of fitness values for which summary statistics should be computed.

... further arguments passed to or from other methods.

Details

This function computes summary statistics for a vector of fitness values at current iteration of GA search.

Value

A vector with the following values: (max, mean, median, min)

Author(s)

Luca Scrucca

See Also

ga

ga_Crossover 21

ga_Crossover	Crossover operators in genetic algorithms
--------------	---

Description

Functions implementing crossover genetic operator.

Usage

```
ga_spCrossover(object, parents, ...)
gabin_spCrossover(object, parents, ...)
gabin_uCrossover(object, parents, ...)
gareal_spCrossover(object, parents, ...)
gareal_waCrossover(object, parents, ...)
gareal_laCrossover(object, parents, ...)
gareal_blxCrossover(object, parents, a = 0.5, ...)
gareal_laplaceCrossover(object, parents, a = 0, b = 0.15, ...)
gaperm_cxCrossover(object, parents, ...)
gaperm_pmxCrossover(object, parents, ...)
gaperm_oxCrossover(object, parents, ...)
gaperm_pbxCrossover(object, parents, ...)
```

Arguments

object	An object of class "ga", usually resulting from a call to function ga.
parents	A two-rows matrix of values indexing the parents from the current population.
	Further arguments passed to or from other methods.
a, b	Parameters of genetic operators.

Value

Return a list with two elements:

children	a matrix of dimension 2 times the number of decision variables containing the generated offsprings;
fitness	a vector of length 2 containing the fitness values for the offsprings. A value NA is returned if an offspring is different (which is usually the case) from the two parents.

Author(s)

Luca Scrucca

22 ga_Mutation

See Also

ga

ga_Mutation

Mutation operators in genetic algorithms

Description

Functions implementing mutation genetic operator.

Usage

```
gabin_raMutation(object, parent, ...)
gareal_raMutation(object, parent, ...)
gareal_nraMutation(object, parent, ...)
gareal_rsMutation(object, parent, ...)
gareal_powMutation(object, parent, pow = 10, ...)
gaperm_simMutation(object, parent, ...)
gaperm_ismMutation(object, parent, ...)
gaperm_swMutation(object, parent, ...)
gaperm_dmMutation(object, parent, ...)
gaperm_scrMutation(object, parent, ...)
```

Arguments

object	An object of class "ga", usually resulting from a call to function ga.
parent	A vector of values for the parent from the current population where mutation should occur.
	Further arguments passed to or from other methods.
pow	Parameters of genetic operators.

Value

Return a vector of values containing the mutated string.

Author(s)

Luca Scrucca

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ga_pmutation

Variable mutation probability in genetic algorithms

Description

A function which calculates the mutation probability for the current iteration. This enables to use GAs with variable mutation rate (see examples).

Usage

```
ga_pmutation(object, p0 = 0.5, p = 0.01, T = round(object@maxiter/2), ...)
```

Arguments

```
object An object of class "ga", usually resulting from a call to function ga.

p0 initial probability of mutation.

p limiting probability of mutation.

T maximum iteration after which it should converges to p.

... Further arguments passed to or from other methods.
```

Value

Return a numeric value in the range (0,1).

Author(s)

Luca Scrucca

See Also

```
ga, ga_Mutation
```

Examples

24 ga_Population

ga_Population

Population initialization in genetic algorithms

Description

Functions for creating a random initial population to be used in genetic algorithms.

Usage

```
gabin_Population(object, ...)
gareal_Population(object, ...)
gaperm_Population(object, ...)
```

Arguments

object An object of class "ga", usually resulting from a call to function ga.

... Further arguments passed to or from other methods.

Details

gabin_Population generates a random population of object@nBits binary values; gareal_Population generates a random (uniform) population of real values in the range [object@min, object@max]; gaperm_Population generates a random (uniform) population of integer values in the range [object@min, object@max].

Value

Return a matrix of dimension object@popSize times the number of decision variables.

Author(s)

Luca Scrucca

See Also

ga

ga_Selection 25

ga_Selection

Selection operators in genetic algorithms

Description

Functions implementing selection genetic operator.

Usage

```
ga_lrSelection(object, r = 2/(object@popSize * (object@popSize - 1)),
                       q = 2/object@popSize, ...)
ga_nlrSelection(object, q = 0.25, ...)
ga_rwSelection(object, ...)
ga_tourSelection(object, k = 3, ...)
gabin_lrSelection(object, r = 2/(object@popSize * (object@popSize - 1)),
                          q = 2/object@popSize, ...)
gabin_nlrSelection(object, q = 0.25, ...)
gabin_rwSelection(object, ...)
gabin_tourSelection(object, k = 3, ...)
gareal_lrSelection(object, r = 2/(object@popSize * (object@popSize - 1)),
                           q = 2/object@popSize, ...)
gareal_nlrSelection(object, q = 0.25, ...)
gareal_rwSelection(object, ...)
gareal_tourSelection(object, k = 3, ...)
gareal_lsSelection(object, ...)
gareal_sigmaSelection(object, ...)
gaperm_lrSelection(object, r = 2/(object@popSize * (object@popSize - 1)),
                           q = 2/object@popSize, ...)
gaperm_nlrSelection(object, q = 0.25, ...)
gaperm_rwSelection(object, ...)
gaperm_tourSelection(object, k = 3, ...)
```

Arguments

object	An object of class "ga", usually resulting from a call to function ga.
r	A tuning parameter for the specific selection operator.
q	A tuning parameter for the specific selection operator.
k	A tuning parameter for the specific selection operator.
	Further arguments passed to or from other methods.

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Value

Return a list with two elements:

population a matrix of dimension object@popSize times the number of decision variables

containing the selected individuals or strings;

fitness a vector of length object@popSize containing the fitness values for the selected

individuals.

Author(s)

Luca Scrucca

See Also

ga

numericOrNA-class Virtual Class "numericOrNA" - Simple Class for subassignment Val-

Description

The class "numericOrNA" is a simple class union (setClassUnion) of "numeric" and "logical".

Objects from the Class

Since it is a virtual Class, no objects may be created from it.

Examples

```
showClass("numericOrNA")
```

palettes

Colors palettes

Description

Functions for creating a vector of colors from pre-speficied palettes.

Usage

```
jet.colors(n)
spectral.colors(n)
bl2gr.colors(n)
```

parNames-methods 27

Arguments

n

a numerical value specifying the number of colors in the palette.

Details

jet.colors() creates a palette of colors which tend to have high brightness and not uniform luminance. Furthermore, the brightest colors, yellow and cyan, are used for intermediate data values, and this has the effect of emphasizing uninteresting (and arbitrary) values while demphasizing the extremes. For these reasons this popular palette is not recommended.

spectral.colors() creates a palette based on ColorBrewer http://colorbrewer2.org, so the resulting colors have a much uniform luminance.

The bl2gr.colors() palette returns a palette of colors from blue to green.

Value

Returns a character vector of colors encoded in hexadecimal values.

See Also

```
colors, rgb.
```

Examples

parNames-methods

Parameters or decision variables names from an object of class ga-class.

Description

A method for obtaining the names of parameters or decision variables from an object of class ga-class.

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Usage

```
parNames(object, ...)
## S4 method for signature 'ga'
parNames(object, ...)
```

Arguments

object An object of class "ga", usually resulting from a call to function ga.
... Further arguments, currently not used.

Value

A list of character values providing the names of parameters or decision variables.

Author(s)

Luca Scrucca

See Also

ga

persp3D

Perspective plot with colour levels

Description

This function draws a perspective plot of a surface with different levels in different colors.

Usage

Arguments

х, у	locations of grid lines at which the values in z are measured. These must be in ascending order. By default, equally spaced values from 0 to 1 are used. If x is a list, its components x x and x xy are used for x and y, respectively.
z	a matrix containing the values to be plotted (NAs are allowed).
theta, phi	angles defining the viewing direction. theta gives the azimuthal direction and phi the colatitude.

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d a value which can be used to vary the strength of the perspective transformation. a expansion factor applied to the z coordinates. expand xlim, ylim, zlim x-, y- and z-limits for the axes. levels a vector of values specifying the levels to be used for plotting the surface with different colors. a value specifying the numbe of levels to be used for plotting. This value is used nlevels if levels argument is not specified. the color palette used for plotting. color.palette the color of the line drawn around the surface facets. By default is set to NA so border no borders are drawn. ticktype a character specifying the type of axes tickmarks. By default "detailed" ticks are drawn. xlab, ylab, zlab character strings specifying the titles for the axes.

Details

This function enhances the default perspective plot for drawing 3-dimensional surfaces.

Further arguments passed to the function persp.

Value

Return a list with the following elements:

persp the viewing transformation matrix (see persp);

levels a vector of values giving the levels used for plotting the surface; colors a vector of strings giving the color used for plotting the surface.

Author(s)

Luca Scrucca

See Also

persp

Examples

30 plot.ga-method

plot.ga-method	Plot of Genetic Algorithm search path
----------------	---------------------------------------

Description

The plot method for ga-class objects gives a plot of best and average fitness values found during the iterations of the GA search.

Usage

Arguments

x	An object of class "ga".
У	Not used.
ylim	A vector of two values specifying the limits on the y-axis.
cex.points	The magnification to be used for points.
col	The colors to be used for best and average fitness values.
pch	The type of points to be used for best and average fitness values.
lty	The type of lines to be used for best and average fitness values.
legend	A logical specifying if a legend should be included.
grid	A function for grid drawing of NULL to avoid drawing one.
	Further arguments, currently not used.

Details

Plot best and average fitness values at each iteration of GA search.

Value

The method invisibly return a data. frame with the iterations and summary statistics for the fitness function evaluated at each iteration.

Author(s)

Luca Scrucca

See Also

```
ga, ga-class.
```

plot.gaisl-method 31

Examples

```
# See examples in help(ga)
# The following code shows how to obtain graphs using the
# ggplot2 plotting system
## Not run:
GA <- ga(...)
out <- plot(GA)
library(reshape2)
df <- melt(out[,c(1:3,5)], id.var = "iter")</pre>
library(ggplot2)
ggplot(df, aes(x = iter, y = value, group = variable, colour = variable)) +
 xlab("Generation") + ylab("Fitness values") +
 geom_point(aes(shape = variable)) +
 geom_line(aes(lty = variable)) +
 scale_colour_brewer(palette = "Set1") +
 theme_bw() +
 theme(legend.title = element_blank())
## End(Not run)
```

plot.gaisl-method

Plot of Islands Genetic Algorithm search path

Description

The plot method for gaisl-class objects gives a plot of best fitness values found in each island during the GA iterations.

Usage

```
## S4 method for signature 'gaisl'
plot(x, y, ...)
```

Arguments

```
x An object of class "gaisl".
y Not used.
... Further arguments passed to plot.default, such as ylim, ylab, etc., or to matplot, such as col, lty, and lwd.
```

Details

Plot best fitness values found in each island during the GA iterations.

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Value

The method invisibly return a list with the following components:

```
iter a vector of values specifying the interation.summary a matrix of best fitness values for each island along the columns.
```

Author(s)

Luca Scrucca

See Also

```
gaisl, gaisl-class.
```

Examples

```
# See examples in help(gaisl)
# The following code shows how to obtain graphs using the
# ggplot2 plotting system
## Not run:
GA <- gaisl(...)
out <- plot(GA)</pre>
library(reshape2)
df <- melt(out, id.var = "iter")</pre>
library(ggplot2)
ggplot(df, aes(x = iter, y = value, group = variable, colour = variable)) +
  xlab("Generation") + ylab("Fitness values") +
  geom\_line(size = 0.8) +
  scale_colour_brewer(palette = "Paired") +
  theme_bw() +
  theme(legend.title = element_blank())
## End(Not run)
```

summary.ga-method

Summary for Genetic Algorithms

Description

Summary method for class ga-class.

Usage

```
## S4 method for signature 'ga'
summary(object, ...)

## S3 method for class 'summary.ga'
print(x, digits = getOption("digits"), ...)
```

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Arguments

```
object an object of class ga-class.

x an object of class summary.ga.

digits number of significant digits.

... further arguments passed to or from other methods.
```

Value

The summary function returns an object of class summary.ga which can be printed by the corresponding print method. The function also returns invisibly a list with the information from the genetic algorithm search.

Author(s)

Luca Scrucca

See Also

ga

Examples

 $summary. \verb|gaisl-method| Summary for Islands Genetic Algorithms|$

Description

Summary method for class gaisl-class.

Usage

```
## S4 method for signature 'gaisl'
summary(object, ...)
## S3 method for class 'summary.gaisl'
print(x, digits = getOption("digits"), ...)
```

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Arguments

```
object an object of class gaisl-class.

x an object of class summary.gaisl.

digits number of significant digits.

further arguments passed to or from other methods.
```

Value

The summary function returns an object of class summary.gaisl which can be printed by the corresponding print method. The function also returns invisibly a list with the information from the islands genetic algorithm search.

Author(s)

Luca Scrucca

See Also

gaisl

Examples

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