

# Supplementary materials



## 1 MODEL SETTING

In our scATAC-seq framework, the encoder consists of a four-layer feedforward network with layer sizes of 3200, 1600, 800 and 400 neurons, yielding a 32-dimensional latent representation. The decoder and classifiers take this 32-dimensional embedding as input directly, without any intervening hidden layers. Training is performed with mini-batches of 64 samples over 3000 epochs, using the AdamW optimizer (learning rate = 0.0002, weight decay =  $5 \times 10^{-4}$ ).

## 2 METRIC DEFINITIONS

*Kappa* is a minor-class sensitive method to provide a thorough evaluation on classification performance. *F1\_SCORE*, computed by averaging precision rate over recall rate for every type, applies to multi-classification scenarios and is equivalent to accuracy for binary classification. Finally, *ACC* measures the overall proportion of correctly classified samples. These metrics are mathematically formulated in Equations (13)-(16) below.

$$\text{Jaccard} = \frac{1}{N} \sum_{i=1}^N \frac{|Y_i \cap \hat{Y}_i|}{|Y_i \cup \hat{Y}_i|} \quad (1)$$

$$\text{Kappa} = \frac{p_o - p_e}{1 - p_e} \quad (2)$$

$$\text{F1\_SCORE} = \frac{1}{K} \sum_{k=1}^K \frac{2 \cdot TP_k}{2 \cdot TP_k + FP_k + FN_k} \quad (3)$$

$$\text{ACC} = \frac{\sum_{k=1}^K TP_k}{N} \quad (4)$$

Specifically:

- $N$ : Total samples
- $Y_i$ : Ground truth set for sample  $i$
- $\hat{Y}_i$ : Predicted set for sample  $i$
- $|\cdot|$ : Set cardinality
- $\cap/\cup$ : Set intersection/union
- $p_o$ : Observed agreement (accuracy)
- $p_e$ : Expected chance agreement
- $K$ : Total classes
- $TP_k$ : True positives for class  $k$
- $FP_k$ : False positives for class  $k$
- $FN_k$ : False negatives for class  $k$

where detailed calculations can be found in [1], [2], [3].

## REFERENCES

- [1] Jaccard, P. (1902). Distribution de la flore alpine. *Bulletin de la Société Vaudoise des Sciences Naturelles*, 38, 69-130. 2

- [2] Van Rijsbergen, C. J. (2004). *The geometry of information retrieval*. Cambridge University Press. 2
- [3] Cohen, J. (1960). A coefficient of agreement for nominal scales. *Educational and Psychological Measurement*, 20(1), 37-46.