

9. Prove that the following two Lie algebras over the field \mathbb{C} are isomorphic:

(i) the 3-dimensional Lie algebra with the basis vectors E, F, G and relations

$$[E, F] = 0, \quad [E, G] = 0, \quad [F, G] = E;$$

(ii) the Lie subalgebra of the general linear Lie algebra $\mathfrak{gl}_3\mathbb{C}$, consisting of the *strictly upper triangular* 3×3 -matrices $[X_{ij}]$: here $X_{ij} = 0$ unless $j - i > 0$.

Do *not* use the classification of 3-dimensional Lie algebras.

10. For a Lie algebra \mathfrak{g} over the field \mathbb{C} consider the Lie algebra $\text{Der}(\mathfrak{g})$ of all derivations of \mathfrak{g} . Prove that the set of all *inner* derivations $\text{ad } X$ where X is ranging over \mathfrak{g} , is an ideal of $\text{Der}(\mathfrak{g})$.