

I am a theoretical computer scientist who studies algorithms for social good. The rapid integration of computing into society has led to algorithms shaping crucial decisions in areas like healthcare, education, and criminal justice. While these algorithmic solutions promise unprecedented societal advancements, they also carry the risk of amplifying biases and creating unintended negative impacts on vulnerable populations. My research focuses on algorithms for social good that are not only effective but also trustworthy and explainable. To this end, my work focuses on the following interconnected goals:

1. **Explainable AI:** Developing rigorous mathematical frameworks to interpret complex models, enabling users to understand the rationale behind algorithmic decisions.
2. **Responsible Use of AI:** Formulating safeguards to prevent AI misuse and ensure accountability. This includes watermarking AI-generated content to ensure authenticity and traceability.
3. **Effective Algorithms:** Designing and analyzing algorithms that address societal challenges while maintaining provable guarantees on fairness, efficiency, and robustness. A key social good application is creating tools for nonprofits to rigorously evaluate and optimize the impact of their initiatives.

Many algorithms proposed for social good are heuristic in nature. My work aims to illuminate their theoretical foundations, providing (A) **rigorous guarantees on algorithmic performance and behavior**, and (B) **theoretical insights for the design of more effective and trustworthy algorithms**. By bridging the gap between theory and practice, I strive to enhance the reliability and impact of algorithms designed for social good.

I have studied algorithms for social good in the context of explainable AI [MW24, LWK⁺24], evaluation of nonprofit efficacy [WM24], fairness in machine learning [RW23, RW24], resource allocation [HLW22, WR24, WH24], and societal polarization [MRUW22]. I leverage a broad theoretical toolkit including techniques in randomized linear algebra, linear programming, and discrete optimization. Research in my area also requires interdisciplinary engagement with practitioners and stakeholders. To this end, I have worked closely with an early childhood literacy nonprofit and collaborated with researchers across nine institutions, publishing in top machine learning and theoretical computer science venues such as NeurIPS, ESA, and AAI.

I am excited about the opportunity to learn from and collaborate with researchers at Amherst College. In the remainder of this document, I outline my research plans in relation to explainable AI, the responsible use of AI, and effective algorithms for social good. Informed by my prior work, I discuss concrete ideas for future research and opportunities for collaboration.

Provably Accurate Algorithms for Explainable AI

Game theory provides a valuable axiomatic framework for explaining AI predictions. While most AI applications of game-theoretic concepts use heuristic methods, I developed theoretically grounded algorithms for computing Shapley and Banzhaf values. These algorithms offer strong non-asymptotic guarantees, and superior empirical performance. My future research aims to build similarly efficient algorithms for computing other game-theoretic quantities.

Motivation

As AI predictions are increasingly incorporated into high-stakes domains like finance, law, and healthcare, users and auditors of AI systems should understand why a prediction was made. For example, a credit card

applicant should know why their application was rejected, and a defendant should be aware of how their bail was set. Further, explaining AI predictions can help identify biases and the patterns learned by models, supporting the improvement and refinement of future algorithms.

The standard method of explaining predictions is to use game-theoretic attribution techniques, quantifying how changes to the input features affect the model output. Shapley values are a particularly popular choice because they satisfy four desirable properties: null player, symmetry, additivity, and efficiency. However, Shapley values are defined over exponentially many terms and are therefore computationally infeasible to compute exactly in general. In practice, Shapley values are estimated using heuristic approaches. Arguably the most popular and effective estimator for Shapley values is Kernel SHAP. Kernel SHAP exploits an elegant connection to linear regression, sampling from an exponentially large linear system to estimate the Shapley values. While effective in practice, Kernel SHAP samples heuristically, and lacks theoretical guarantees.

My Prior Work

I developed a theoretically motivated algorithm for estimating Shapley values that outperforms Kernel SHAP in practice and offers strong non-asymptotic guarantees [MW24]. The starting point of my work was an insight from randomized linear algebra: regression problems can be effectively subsampled using statistical leverage scores. The benefit of leverage scores is that they quantify the importance of each data point in the regression problem. Instead of sampling from the exponentially large linear system via a heuristic weighting as in Kernel SHAP, the Leverage SHAP algorithm, as its name suggests, samples according to leverage scores. Modifying the standard leverage score analysis to the specific optimizations in the algorithm, I showed that Leverage SHAP can provably recover accurate Shapley values with almost a linear number of samples. Not only does leverage score sampling offer theoretical guarantees, Leverage SHAP empirically outperforms even a highly optimized version of Kernel SHAP.

While Shapley values are popular, they are not the only game-theoretic quantity that can be used to explain AI predictions. Instead of the efficiency property, we may want another application-dependent property. For example, in the context of a personal finance application, the 2-efficiency property ensures that the attribution of a composite feature like net worth is the sum of the attributions of the sub-features like assets and liabilities. If we replace the efficiency property of Shapley values with the 2-efficiency property, we arrive at Banzhaf values. Banzhaf values are simpler than Shapley values and have been found to be more accurately computed in practice. While Shapley values are known to be the solution to a linear regression problem, a regression formulation was only known for Banzhaf values in a restricted setting. In order to apply the leverage score sampling technique to Banzhaf values, I designed a linear regression problem for which the Banzhaf values are the solution [LWK⁺24]. With this formulation and leverage score sampling, I developed a new algorithm for computing Banzhaf values: Kernel Banzhaf substantially outperforms the existing Banzhaf value estimation methods. Further, because of the structure of the Banzhaf linear regression problem, Kernel Banzhaf offers even stronger non-asymptotic guarantees than Leverage SHAP.

Future Directions

My prior work establishes more efficient and theoretically motivated methods for explaining AI predictions with Shapley and Banzhaf values. Building on this foundation, I plan to explore a broader spectrum of game-theoretic concepts applicable to various social good domains. My goal is to leverage my theoretical expertise to design novel, computationally efficient algorithms for these game-theoretic quantities, thereby enhancing the interpretability and transparency of AI systems across diverse applications.

One under-studied social good setting is graph learning tasks, such as predicting the spread of disease or identifying collusion rings. Graph neural networks have emerged as a powerful tool for learning on graph

data, processing the features of adjacent nodes to identify local patterns. Because of the high stakes of social good applications, it is important to explain how graph neural networks make predictions. Unfortunately, standard game-theoretic attribution quantities like Shapley and Banzhaf values do not take into account the graph structure, and so lose the ability to explain how the graph neural network reasons. An alternative game-theoretic quantity designed specifically for graph structures is the Hameiri-Navarro (HN) value, which naturally generalizes Shapley values to graph settings. Mathematically, the HN value is the limit of a series of associated games, which can be represented as repeated matrix multiplication. This connection suggests the HN value may be computable via gradient descent. I plan to investigate the structure of the HN value to recover the underlying problem that gives rise to the gradient descent algorithm. If the problem is a linear regression problem as I suspect, I can apply leverage score sampling to design provably accurate algorithms for computing the HN value.

There is a rich game theory literature to describe attribution techniques from an axiomatic perspective. As trustworthy AI becomes increasingly important, this literature is a powerful resource for explaining AI predictions in an axiomatic way. The majority of prior work that adapts game-theoretic quantities to AI applications develops heuristic algorithms. However, as evidenced by my work on Shapley and Banzhaf values, theoretically motivated algorithms can outperform heuristic methods, while simultaneously offering strong non-asymptotic guarantees. I plan to apply my theoretical toolkit to design provably efficient algorithms for computing game-theoretic quantities relevant to social good applications.

Collaboration Opportunities

The problems in explainable AI present a rich landscape of research opportunities, spanning game theory, graph algorithms, and randomized linear algebra. I am excited to collaborate with researchers at Amherst College, building theoretically motivated approximation algorithms with performance guarantees.

Distortion-free Watermarking for the Responsible Use of AI

I previously developed distortion-free watermarking techniques to ensure the responsible use of AI-generated images, but with storage that scales with use. By using cryptographic hash functions and locality-sensitive hashing, I plan to design secure and robust watermarks that can be detected without degrading content quality or requiring costly storage. My research plans apply to both text and vision tasks, allowing for distortion-free efficient watermarking that leverages existing information in the generated content.

Motivation

As AI models become more advanced, powerful tools like Large Language Models (LLMs) for text generation and diffusion models for prompt-guided image generation are ubiquitous. While these technologies have numerous applications, they also bring new risks, such as malicious actors claiming AI-generated text as their own or fabricating realistic images of fake events, potentially causing confusion or harm. To mitigate these risks, model owners use watermarking techniques to track the content generated by their models.

However, most current watermarking methods are distortion-based, meaning they modify the output to embed identifiable markers. For text, the distribution of words is often altered while, for images, the distribution of an associated latent image is often modified. Despite their widespread use, distortion-based watermarks remain vulnerable: they can be detected and even forged by malicious actors if enough examples are available.

My Related Work

I am interested in distortion-free watermarking techniques that generate content without modifying it. In

this approach, verification of the watermark requires access to a private, correlated variable, ensuring the watermark's security and robustness against forgery. However, a significant limitation of current distortion-free methods is the need for the model owner to store the correlated variable, which can be both costly and inefficient.

In my work, I developed a distortion-free watermarking method for diffusion models [AFW⁺24]. The key idea is to generate initial noise using a finite set of seeds, where each seed is linked to a cryptographic hash function. Even if an adversary can reconstruct the noise, it remains indistinguishable from random noise and provides no information about other seeds. However, the drawback of this approach is the need to store and search through all previously generated noise vectors.

Future Directions

My goal is to develop distortion-free watermarks that scale without the need for additional storage. The key idea is to leverage context to robustly and securely generate a seed using locality-sensitive hashing (LSH). This would allow us to generate a correlated random variable from the seed in a secure and efficient manner, without distorting the distribution of the generated content.

In the LLM setting, text is generated in an auto-regressive way by predicting the next token based on the previous context. Current watermarking approaches modify the next-token distribution, either globally or contextually, making the watermarks detectable, removable, and sometimes even noticeably degrading text quality. I plan to use SimHash to convert the embedding of the prompt into seeds and then generate a random variable using cryptographic hash functions. This random variable is reproducible if we have access to the seed, and distributed identically to a sample from the true probability distribution over next tokens. To detect the watermark, we compute the correlated random variable for each seed and check its alignment with the generated text. By using SimHash, we can guarantee that nearby embedded contexts produce the same seed with high probability, making the watermark detectable without degrading text quality.

For vision tasks, a similar approach can be applied by embedding the prompt and using SimHash to derive multiple seeds. Each seed generates randomness for different portions of the image. During detection, we caption the image to obtain a vector aligning with the original prompt, apply SimHash to retrieve seeds, and check for alignment with the latent noise. This method allows for flexible tuning of hyperparameters to achieve the desired level of detection accuracy, while the cryptographic hash function ensures security.

Combining distortion-free and searchable watermarking with streaming and randomized algorithms promises security and efficiency. I plan to leverage information already present in the image or text to robustly store the correlated variable in the generated content, enabling efficient distortion-free watermarking and ultimately supporting the responsible use of AI.

Collaboration Opportunities

The problems in watermarking present fascinating algorithmic questions. I am excited to collaborate with researchers at Amherst College, leveraging shared expertise in cryptography, randomized algorithms, and hashing to develop distortion-free watermarking techniques that are both secure and scalable.

Simple and Trustworthy Algorithms for Treatment Effect Estimation

I previously designed simple and trustworthy algorithms for treatment effect estimation, motivated by the need for transparent and reliable evaluations of social programs. My work addresses challenges in natural experiment settings by developing interpretable, theoretically grounded algorithms, as demonstrated

in collaboration with a nonprofit organization. I aim to build on this research to design understandable algorithms with user-friendly performance guarantees.

Motivation

In broader societal applications, such as government spending or nonprofit resource allocation, interpretability is even more critical. It's not enough to explain individual predictions; stakeholders should have confidence in the entire model's transparency and reasoning. This need for transparency extends to the realm of treatment effect estimation, an important problem in evaluating the impact of social programs. While randomized control trials often allow us to estimate the effect of a treatment, they're not always possible or ethical to implement. In some cases, certain individuals may have a greater need for the treatment, or the treatment may have already been assigned, leaving us only to observe the outcome. These scenarios, known as natural experiments, are common in social good applications and require sophisticated analytical approaches because the treatment assignment can be confounded by other factors.

One such application is evaluating the impact of nonprofit programs. For instance, Reach Out and Read Colorado (RORCO), an early childhood literacy nonprofit, provides books to children during their pediatrician visits. RORCO has been operating for more than 20 years, distributing books to the least-served students in Colorado. Because of their extensive history, RORCO has a wealth of data but lacks a robust method for evaluating their effect in the natural experiment setting. In collaborating with RORCO, I applied more than 20 existing treatment effect estimation methods. However, each method yielded different results on their data and none offered theoretical guarantees.

My Related Work

Building on the challenges identified in evaluating nonprofit programs like RORCO's, I built a benchmark for treatment effect estimation: I curated a comprehensive dataset and constructed a benchmark for evaluating treatment effect estimators. This empirical investigation yielded valuable insights, notably that doubly robust algorithms generally provide the best performance in estimating treatment effects. However, these algorithms often suffer from two significant drawbacks: they tend to be uninterpretable, and their known theoretical guarantees are primarily asymptotic, limiting their practical applicability in finite sample scenarios. Leveraging these findings, I designed a simple, theoretically motivated algorithm and exactly analyzed its variance in the non-asymptotic setting. This new approach not only offers performance comparable to the more complex doubly robust algorithms but does so with a simpler, more interpretable estimator. The algorithm's effectiveness is not just theoretical; RORCO has already implemented it to inform their future program development, demonstrating its practical value.

Future Directions

While treatment effect estimation is well-studied, there are practically no algorithms with non-asymptotic, user-friendly guarantees. My goal is to develop simple algorithms with understandable theoretical guarantees for treatment effect estimation. Like the guarantees I developed for Shapley and Banzhaf estimators, the guarantees would be of the form: with $\text{poly}(m, 1/\epsilon, 1/\delta)$ samples, we can guarantee ϵ -approximate estimates with probability $1 - \delta$. This approach not only enhances the reliability of the estimates but also allows stakeholders to easily comprehend the impact of their programs.

Collaboration Opportunities

The problems in treatment effect estimation pose many interesting statistical questions across estimator design, causal inference, and algorithmic analysis. I am excited to collaborate with researchers at Amherst College to develop simple and provably accurate algorithms for treatment effect estimation.

Going Forward

While my primary focus is on algorithms for social good, I approach this field with the breadth of a generalist. This diverse background allows me to bring novel perspectives to socially impactful problems. For instance, my work on efficient Boolean function evaluation in classical [HKLW22] and quantum settings [CKW23, KW21, DKW19] has honed my skills in algorithmic optimization. Even my explorations into the computational complexity of board games [WL20, Wit21] have yielded insights applicable to real-world decision-making processes. These varied experiences continually enrich my approach to core problems in algorithms for social good.

The increasing prevalence of AI and algorithmic decision-making in crucial societal domains underscores the need for methods that are both effective and trustworthy. My research aims to bridge the gap between theoretical computer science and practical, socially relevant applications. I focus on developing algorithms that are not only efficient but also explainable, secure, and interpretable. Through my work on explainable AI, watermarking, and treatment effect estimation, I address some of the most pressing challenges posed by modern algorithmic systems. At Amherst College, I look forward to collaborating with fellow researchers to expand the reach of these ideas and create tangible benefits for society.

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In the tradition of theoretical computer science, an asterisk () indicates that authors are listed in alphabetical order.*

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