# Data Analysis Week 8 Further Tasks Solutions

## Further Tasks

You are encouraged to complete the following tasks by using RMarkdown to produce a single document which summarises all your work, i.e. the original questions, your R code, your comments and reflections, etc.

- 1. Data was collected on the characteristics of homes in the American city of Los Angeles (LA) in 2010 and can be found in the file LAhomes.csv on the Moodle page. The data contain the following variables:
- city the district of LA where the house was located
- type either SFR (Single Family Residences) or Condo/Twh (Condominium/Town House)
- bed the number of bedrooms
- bath the number of bathrooms
- garage the number of car spaces in the garage
- sqft the floor area of the house (in square feet)
- pool Y if the house has a pool
- spa TRUE if the house has a spa
- price the most recent sales price (\$US)

We are interested in exploring the relationships betwen price and the other variables.

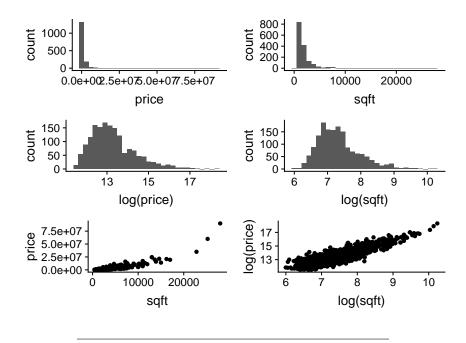
Read the data into an object called LAhomes and answer the following questions.

a. By looking at the univariate and bivariate distributions on the price and sqft variables below, what would be a sensible way to proceed if we wanted to model this data? What care must be taken if you were to proceed this way?

```
library(gridExtra) #Package to display plots side by side (like par(mfrow=c(2,2)) in base R)
hist1 <- ggplot(LAhomes,aes(x=price))+
    geom_histogram()
hist2 <- ggplot(LAhomes,aes(x=sqft))+
    geom_histogram()
hist1log <- ggplot(LAhomes,aes(x=log(price)))+
    geom_histogram()
hist2log <- ggplot(LAhomes,aes(x=log(sqft)))+
    geom_histogram()

plot1 <- ggplot(LAhomes,aes(x=sqft,y=price))+
    geom_point()

plot2 <- ggplot(LAhomes,aes(x=log(sqft),y=log(price)))+
    geom_point()
grid.arrange(hist1, hist2, hist1log, hist2log, plot1, plot2, ncol=2, nrow=3)</pre>
```



Solution Given the highly skewed nature of both price and sqft (as seen in both their histograms and their scatterplot) the use of the log tranformation significantly reduces the skewness in the data and makes the scatterplot look more linear. Hence we should model the tranformed variables log(price) and log(sqft) instead of the original variables.

If these transformations are employed, special care must be taken when interpretting the meaning of estimated model parameters since the data are no longer on the original units and the linear models of the logged variables will have a multiplacitive effect, rather than an additive effect, in the original units.

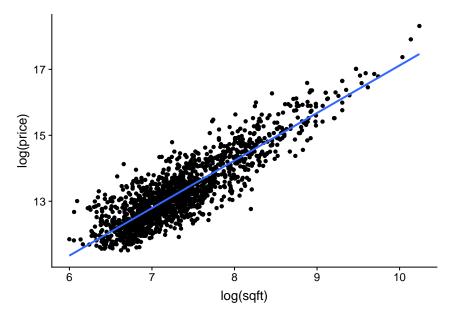
b. Fit the simple linear model with log(price) as the response and log(sqft) as the predictor. Display the fitted model on a scatterplot of the data and construct a bootstrap confidence interval (using the percentiles of the bootstrap distribution) for the slope parameter in the model and interpret its point and interval estimates.

Hint: Although you can supply the lm() function with terms like log(price) when you use the infer package to generate bootstrap intervals you the transformed variable needs to already exist. Use the mutate() function in the dplyr package to create new transformed variables.

```
LAhomes <- mutate(LAhomes,log.price = log(price),log.sqft=log(sqft))

slr.model1 <- lm(log(price) ~ log(sqft), data = LAhomes)

ggplot(LAhomes,aes(x=log(sqft),y=log(price)))+
   geom_point()+
   geom_smooth(method=lm, se = FALSE)
```



```
coeff <- slr.model1 %>% coef()

percentile_beta_ci <- LAhomes %>%
    specify(log.price ~ log.sqft) %>%
    generate(reps = 1000, type = "bootstrap") %>%
    calculate(stat = "slope") %>%
    get_ci(level = 0.95, type = "percentile")
```

The above plot shows the fitted line log(price)=2.7 + 1.44 log(sqft). The point estimate of the slope parameter estimates that for every unit increase in log(sqft) the average log(price) of houses will increase by 1.44 US dollars. Another way of saying this is that each additional 1% of square footage produces an estimate of the average price which is 1.44% higher (i.e. there is a multiplicative effect in the original units).

Note: you must be careful to avoid causative interpretations. Additional square footage does not necessarily cause the price of a specific house to go up.

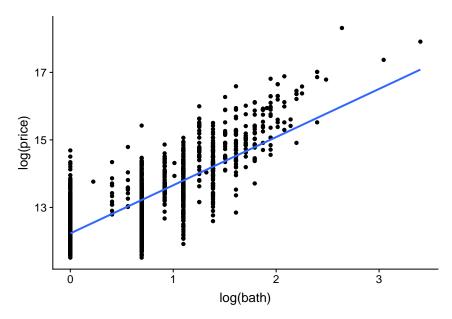
Furthermore, based on the bootstrap confidence interval, we are 95% confident that the interval from 1.4 up to 1.48 contains the true rate of increase in the average of the logged prices as log(sqft) increase. Because this interval does not contain zero we conclude that the relationship between log(price) and log(sqft) is statistically significant.

c. Repeat the analysis in part b. but with the log of the number of bathrooms (bath) as the single explanatory variable.

```
LAhomes <- mutate(LAhomes,log.bath=log(bath))

slr.model2 <- lm(log(price) ~ log(bath), data = LAhomes)

ggplot(LAhomes,aes(x=log(bath),y=log(price)))+
    geom_point()+
    geom_smooth(method=lm, se = FALSE)
```



```
coeff2 <- slr.model2 %>% coef()

percentile_beta_ci2 <- LAhomes %>%
   specify(log.price ~ log.bath) %>%
   generate(reps = 1000, type = "bootstrap") %>%
   calculate(stat = "slope") %>%
   get_ci(level = 0.95, type = "percentile")
```

The above plot shows the fitted line log(price)=12.23 + 1.43 log(bath). The point estimate of the slope parameter estimates that for every unit increase in the log of the number of bathrooms in a house the average log of the prices of houses will increase by 1.43 US dollars. Another way of saying this is that each doubling of bathroom produces an estimate of the average price which is 143% higher (i.e. there is a multiplicative effect in the original units).

Furthermore, based on the bootstrap confidence interval, we are 95% confident that the interval from 1.36 up to 1.49 contains the true rate of increase in the average of the logged prices as the log of the number of bathrooms increases. Because this interval does not contain zero we conclude that the relationship between log(price) and log(bath) is statistically significant.

d. Fit the multiple linear regression model using the **log transform of all the variables price** (as the response) and both **sqft** and **bath** (as the explanatory variables). Calculate the point and interval estimates of the coefficients of the two predictors separately. Compare their point and interval estimates to those you calculated in parts b. and c. Can you account for the differences?

*Hint:* Remember that we didn't use bootstrapping to construct the confidence intervals for parameters in multiple linear regression models, but rather used the theoretical results based on assumptions. You can access these estimates using the get\_regression\_table() function in the moderndive package.

```
mlr.model <- lm(log(price) ~ log(sqft)+log(bath), data = LAhomes)
coeff3 <- mlr.model %>% coef()
```

```
mlr.model.est <- get_regression_table(mlr.model)</pre>
glimpse(mlr.model.est)
Observations: 3
Variables: 7
$ term
            <chr> "intercept", "log(sqft)", "log(bath)"
$ estimate <dbl> 2.514, 1.471, -0.039
$ std_error <dbl> 0.262, 0.040, 0.045
$ statistic <dbl> 9.601, 37.221, -0.862
            <dbl> 0.000, 0.000, 0.389
$ p value
$ lower_ci <dbl> 2.000, 1.394, -0.128
$ upper_ci <dbl> 3.028, 1.549, 0.050
percentile beta1 ci <- c(mlr.model.est$lower ci[2],mlr.model.est$upper ci[2])
percentile_beta2_ci <- c(mlr.model.est$lower_ci[3],mlr.model.est$upper_ci[3])</pre>
percentile_beta1_ci
```

```
[1] 1.394 1.549
percentile_beta2_ci
```

```
[1] -0.128 0.050
```

The fitted model is log(price) = 2.51 + 1.47 log(sqft) - 0.04 log(bath). The first thing we notice is that the parameter associated with (the log of) the number of bathrooms has changed from 1.43 to -0.04. That it, its gone from having a positive relationship with the (log of) house prices in the single explanatory variable model to having a negative relationship when the size of the house was also included in the model. One reason for the switch in sign of the parameter estimate could be that for a house with a given size in (log) square feet, more (log) bathrooms means that less of the (log) square footage is used for bedrooms and other desirable space, thus reflecting a lower average home price. This illustrates the importance of **taking all other variables in the model into account and holding them constant** when we interpret individual parameter estimates in a multiple linear regression model. (See the "Formal Analysis" section here from Week 6's lab).

Turning to the confidence intervals, the model still predicts that the (log) square footage of the home significantly positively affects the average (log) price, since the 95% confidence interval for the log(sqft) parameter is from from 1.39 up to 1.55 which doesn't contain zero. However, now the number of bathrooms no longer significantly affects the price since the 95% confidence interval for the log(bath) parameter is from from -0.13 up to 0.05 which does contain zero. This suggests that we drop the log(bath) term from the model and return to the simple linear regression model we used in part b.

e. Using the objective measures for model comparisons, which of the models in parts b., c. and d. would you favour? Is this consistent with your conclusions in part d.?

```
kable(
   digits = 2,
   caption = "Model comparison values for different models",
)
```

Table 1: Model comparison values for different models

Model	adj.r.squared	AIC	BIC
$\frac{\operatorname{SLR}(\log(\operatorname{sqft}))}{\operatorname{SLR}(\log(\operatorname{bath}))}$ $\operatorname{MLR}$	$0.77 \\ 0.58 \\ 0.77$	2292.16 3289.80 2293.41	2308.28 3305.92 2314.91

The table lists  $R_{adj}^2$ , AIC and BIC which can be used to compare the three models. Both the criteria of minimizing AIC and BIC and maximizing  $R_{adj}^2$  leads us to prefer the model

```
\log(\text{price}) = 2.7 + 1.44 \log(\text{sqft})
```

which we first saw in part b. This agrees with our conclusions in part d.

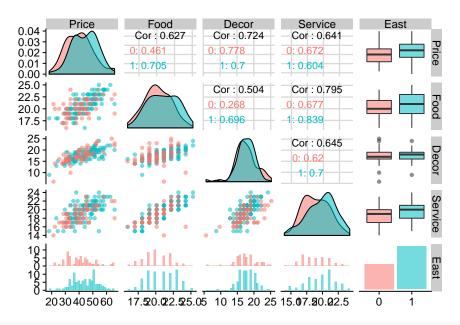
2. You have been asked to determine the pricing of a New York City (NYC) Italian restaurant's dinner menu such that it is competitively positioned with other high-end Italian restaurants by analyzing pricing data that have been collected in order to produce a regression model to predict the price of dinner.

Data from surveys of customers of 168 Italian restaurants in the target area are available. The data can be found in the file restNYC.csv on the Moodle page. Each row represents one customer survey from Italian restaurants in NYC and includes the key variables:

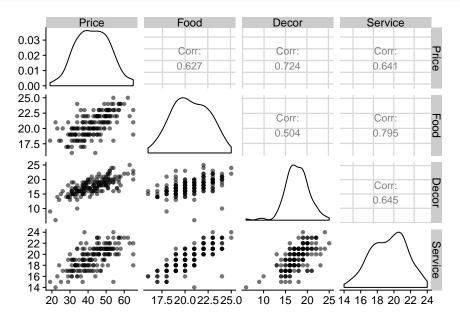
- Price price (in \$US) of dinner (including a tip and one drink)
- Food customer rating of the food (from 1 to 30)
- Decor customer rating fo the decor (from 1 to 30)
- Service customer rating of the service (from 1 to 30)
- East dummy variable with the value 1 if the restaurant is east of Fifth Avenue, 0 otherwise
- a. Use the ggpairs function in the GGally package (see the following code) to generate an informative set of graphical and numberical summaries which illuminate the relationships bewteen pairs of variables. Where do you see the strongest evidence of relationships between price and the potential explanatory variables? Is there evidence of multicollineatity in the data?

```
library(GGally)
#glimpse(restNYC)
restNYC$East <- as.factor(restNYC$East) # East needs to be a factor
ggpairs(restNYC[,4:8], aes(colour = East, alpha = 0.4)) # Including the `East` factor
ggpairs(restNYC[,4:7], aes(alpha = 0.4)) # Without the `East` factor</pre>
```

```
library(GGally)
#glimpse(restNYC)
restNYC$East <- as.factor(restNYC$East) # East needs to be a factor
ggpairs(restNYC[,4:8], aes(colour = East, alpha = 0.4)) # Including the `East` factor</pre>
```



ggpairs(restNYC[,4:7], aes(alpha = 0.4)) # Without the `East` factor



- price shows a moderate to strong correlation with 'Food, ServiceandDecor'.
- The correlation between Service and Food (0.795) is the strongest evidence of multicollinearity in the data, followed by the correlation between Service and Decor (0.645)

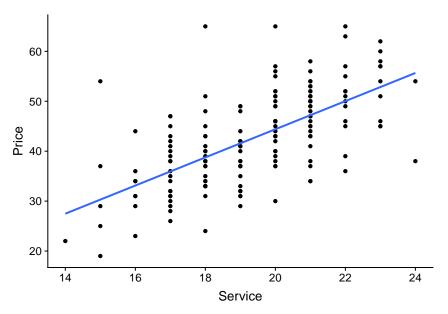
Now fit a multiple regressing model of Price on Service, Food, and Decor. What happens to the significance of Service when additional variables were added to the model?

b. Fit the simple linear model with Price as the response and Service as the predictor and display the fitted model on a scatterplot of the data. Construct a bootstrap confidence interval (using the standard error from the bootstrap distribution) for the slope parameter in the model.

#### Solution

```
slr.Service <- lm(Price ~ Service, data=restNYC)

ggplot(restNYC,aes(x=Service,y=Price))+
  geom_point()+
  geom_smooth(method=lm, se = FALSE)</pre>
```



```
coeff.Service <- slr.Service %>% coef()

percentile_beta_Service_ci <- restNYC %>%
    specify(Price ~ Service) %>%
    generate(reps = 1000, type = "bootstrap") %>%
    calculate(stat = "slope") %>%
    get_ci(level = 0.95, type = "se", point_estimate=coeff.Service[2])

mlr.Service.Food.Decor <- lm(Price ~ Service + Food + Decor, data=restNYC)

get_regression_table(mlr.Service.Food.Decor) %>%
    kable(
        digits = 2,
        caption = "Parameter estimates for MLR model of Price on Service, Food, and Decor",
    )
```

Table 2: Parameter estimates for MLR model of Price on Service, Food, and Decor

term	estimate	std_error	statistic	p_value	lower_ci	upper_ci
intercept	-24.64	4.75	-5.18	0.00	-34.03	-15.26
Service	0.14	0.40	0.34	0.73	-0.65	0.92
Food	1.56	0.37	4.17	0.00	0.82	2.29
Decor	1.85	0.22	8.49	0.00	1.42	2.28

When only Service is included in the model, it appears significant (confidence interval using the standard

error from the bootstrap: 2.25 up to 3.38, which doesn't contain zero). However, once Food and Decor are
added into the model, that is no longer the case as can be seen in the confidence interval table above, which
does contain zero.

c.	What is the correct interpretation of the coefficient on Service in the linear model which regres	ses
	Price on Service, Food, and Decor?	

## Solution

When Food and Decor are in the model, Service is not statistically significant, therefore we cannot know whether it has a significant effect on modeling Price.