

ANSWERS TO END-OF-CHAPTER PROBLEMS

CHAPTER - 2

Q 2.1) $\vec{v}(t) = \left(\frac{4}{15} t^3 \hat{i} - \frac{3}{10} t^2 \hat{j} \right) \text{ m/s} ; \quad \vec{r}(t) = \left(\frac{1}{15} t^4 \hat{i} - \frac{1}{10} t^3 \hat{j} \right) \text{ m}$

Q 2.2) $x = \frac{M_2 g t^2}{2(M_1 + M_2)}$

Q 2.3) $\text{Force of contact} = 1 \text{ N} = \frac{F m_2}{m_1 + m_2}$

Q 2.5) $T = \frac{2mMg}{m+M} ; \quad a = \left(\frac{M-m}{M+m} \right) g$

Q 2.6) $\omega < \sqrt{\frac{g}{R}}$

Q 2.7) (a) $F_{\max} = (M_1 + M_2) \frac{\mu M_1 g}{M_2}$

(b) $F_{\max} = \mu g (M_1 + M_2)$

Q 2.9) $R = \frac{v_0^2 \tan \theta}{g}$

Q 2.11) $T_1 = \frac{1}{2} [\sqrt{2} mg + ml\omega^2] ; \quad T_2 = \frac{1}{2} [-\sqrt{2} mg + ml\omega^2]$

Q 2.12) $t = \sqrt{L/\mu g} ; \quad L = 6 \text{ in}, \mu = 0.5 \rightarrow t = 0.1768 \text{ secs}$

Q 2.13) $a_1 = \frac{2M_2 - M_1}{M_1 + 4M_2} g$

Q 2.14) $a_A = \frac{2M_C g}{4M_A + M_C + \frac{M_A M_C}{M_B}}$ in + ve x direction

$$a_B = \frac{M_A}{M_B} a_A \text{ in + ve x direction}$$

$$a_C = \left(1 + \frac{M_A}{M_B}\right) a_A \text{ in - ve y direction}$$

Q 2.16) *With respect to ground,*

$$a_x = \frac{(g + A)}{2} ; a_y = \frac{(A - g)}{2}$$

Q 2.17) (b) $a_{\min} = \frac{g(\sin \theta - \mu \cos \theta)}{\mu \sin \theta + \cos \theta}$

(c) $a_{\min} = \frac{g(\sin \theta + \mu \cos \theta)}{\mu \sin \theta - \cos \theta}$

Q 2.18) $a = \frac{4F}{M + m} - g$

Q 2.19) $F = \frac{M_3(M_1 + M_2 + M_3)}{M_2} g$

Q 2.20) $a_1 = -[M_2 M_3 / (M_2 M_3 + M_1 M_3 + 2M_2 M_3 + M_3 M_3)] g$

Q 2.21) $T = \frac{\left[M + \frac{m}{l}(l - x)\right]F}{M + m}$

Q 2.22) $T_{\text{end}} = \frac{W}{2 \cos \theta} , T_{\text{middle}} = \frac{W}{2} \tan \theta$

Q 2.26) $T = 2\pi \sqrt{\frac{R^3}{GM}}$

Q 2.28) $V_{\min} = \sqrt{gR \left(\frac{\sin \theta - \mu \cos \theta}{\cos \theta + \mu \sin \theta} \right)}$

$$V_{\max} = \sqrt{gR \left(\frac{\sin \theta + \mu \cos \theta}{\cos \theta - \mu \sin \theta} \right)}$$

Q 2.29) $a_r = -r\omega^2, a_\theta = 2v_o\omega$
 $t_{\text{skidding}} = \frac{1}{v_o\omega^2} \sqrt{\mu^2 g^2 - 4v_o^2\omega^2}$

Q 2.30) $\frac{d^2 r_A}{dt^2} = \omega^2 r_A + \frac{\omega^2 M_B l}{M_A - M_B}$

$$\text{Q 2.33)} \quad \gamma = \varpi, \mathbf{A} = \frac{1}{2} \left(r_0 - \frac{v_0}{\varpi} \right), \mathbf{B} = \frac{1}{2} \left(r_0 + \frac{v_0}{\varpi} \right)$$

$$\text{Q 2.34)} \quad \varpi = \frac{\varpi_0 r_0^2}{(r_0 - vt)^2}$$

$$F_r = - \frac{m \varpi_0^2 r_0^4}{(r_0 - vt)^3}$$

$$\text{Q 2.35)} \quad \theta = \frac{1}{\mu} \ln \frac{l + \mu v_0 t}{l}$$

$$\text{Q 2.37)} \quad y = \frac{4\pi^2}{gT^2} x^2$$