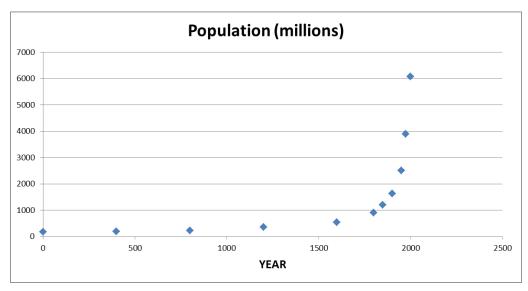
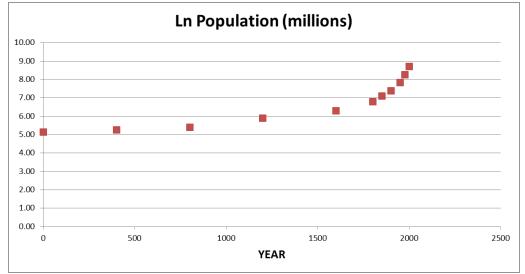
What Is Log?

What Is Log?

| Year | Population (millions) | Ln (population) |
|------|-----------------------|-----------------|
| 1 | 170 | 5.14 |
| 400 | 190 | 5.25 |
| 800 | 220 | 5.39 |
| 1200 | 360 | 5.89 |
| 1600 | 545 | 6.30 |
| 1800 | 900 | 6.80 |
| 1850 | 1200 | 7.09 |
| 1900 | 1625 | 7.39 |
| 1950 | 2500 | 7.82 |
| 1975 | 3900 | 8.27 |
| 2000 | 6080 | 8.71 |

What Is Log?

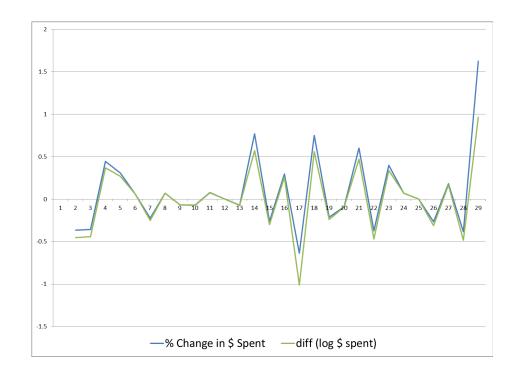




Log and Percentage Change

First difference of natural LOG = percentage change:

- Logging converts
 absolute differences into
 relative (i.e., percentage)
 differences.
- The series
 DIFF(LOG(Y))
 represents the
 percentage change in Y
 from period to period.



Elasticity: Log/Log Models

Dependent Variable : In (\$ Spent)

| | Coefficients | Standard Error | t Stat | P-value |
|--------------------|--------------|----------------|--------|---------|
| Intercept | 2.24 | 0.07 | 32.06 | 0.00 |
| log(num promo + 1) | 0.32 | 0.05 | 6.44 | 0.00 |

0.317 = change in log (\$ spent) when log(num promo) increases by 1 unit

log(
$$\$$$
 spent) when log(num promo) is 0 = 2.236 (1) log($\$$ spent) when log(num promo) is 1 = 2.553 (2) (1) - (2) = 0.317