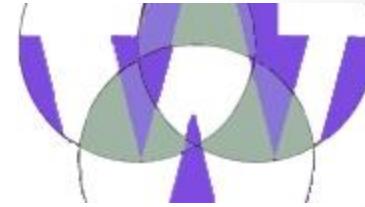


# Introduction to Data Science

Lecture 10; December 14<sup>th</sup>, 2016

Ernst Henle  
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Skype: ernst-henle

# Agenda



- Announcements
  - Social Interactions on LinkedIn: Continue to discuss statistics, job prospects, etc.
- Review: Hadoop MapReduce Lab
- Break
- Introduction to Graph Data
- Quiz Graph Data (Measures)
- Graph Data Popularity
- Quiz Graph Data (Popularity)
- Graph Data Google Matrix
- Break
- SPARQL Intro
- Quiz SPARQL intro
- SPARQL Examples
- Time Permitting:
  - Nested Tables and Associations
  - Quiz Nested Tables
  - Connectivity of the Web
- Assignment. See assignment slides at the end of the deck. Complete all assignments items from all assignment slides. Complete by this Saturday at 11:57 PM.

# MapReduce Review

( 3 )

# MapReduce Review

- Changes
  - Package name: \_\_\_\_\_
  - WordMapper.java
    - *extends Mapper<LongWritable, Text, \_\_\_\_\_, \_\_\_\_\_>*
    - *context.write(new \_\_\_\_\_, new \_\_\_\_\_);*
  - SumReducer.java
    - *extends Reducer<\_\_\_\_\_, \_\_\_\_\_, \_\_\_\_, \_\_\_\_\_>*
    - *public void reduce(\_\_\_\_ key, Iterable<\_\_\_\_\_> values, Context context)*
    - *context.write(key, new \_\_\_\_\_);*
  - WordCount.java
    - *job.setOutputKeyClass(\_\_\_\_\_);*
    - *job.setOutputValueClass(\_\_\_\_\_);*

# MapReduce Review

Map input key-value types are typically given

- Changes

- Package name: \_\_\_\_\_

Map input key type

Map input value type

- WordMapper.java

- *extends Mapper<LongWritable, Text, \_\_\_\_\_, \_\_\_\_\_>*
- *context.write(new \_\_\_\_\_, new \_\_\_\_\_);*

- SumReducer.java

- *extends Reducer<\_\_\_\_\_, \_\_\_\_\_, \_\_\_\_, \_\_\_\_\_>*
- *public void reduce(\_\_\_\_ key, Iterable<\_\_\_\_\_> values, Context context)*
- *context.write(key, new \_\_\_\_\_);*

- WordCount.java

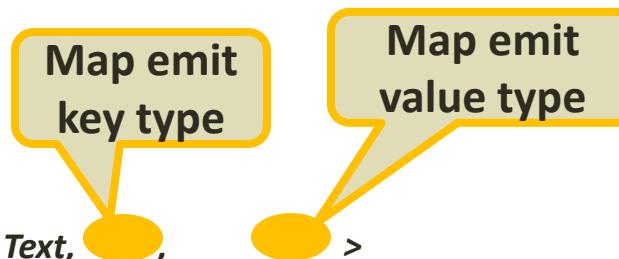
- *job.setOutputKeyClass(\_\_\_\_\_);*
- *job.setOutputValueClass(\_\_\_\_\_);*

# MapReduce Review

Map emit key-value types are chosen

- Changes

- Package name: \_\_\_\_\_



- WordMapper.java

- *extends Mapper<LongWritable, Text, \_\_\_\_\_, \_\_\_\_\_>*
  - *context.write(new \_\_\_\_\_, new \_\_\_\_\_);*

- SumReducer.java

- *extends Reducer<\_\_\_\_\_, \_\_\_\_\_, \_\_\_\_, \_\_\_\_>*
  - *public void reduce(\_\_\_\_ key, Iterable<\_\_\_\_\_> values, Context context)*
  - *context.write(key, new \_\_\_\_\_);*

- WordCount.java

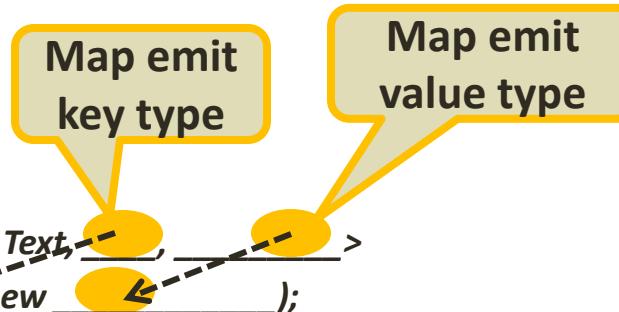
- *job.setOutputKeyClass(\_\_\_\_\_);*
  - *job.setOutputValueClass(\_\_\_\_\_);*

# MapReduce Review

Map emit key-value types need to be consistent

- Changes

- Package name: \_\_\_\_\_



- WordMapper.java

- *extends Mapper<LongWritable, Text, \_\_\_\_\_, \_\_\_\_\_>*
- *context.write(new \_\_\_\_\_, new \_\_\_\_\_);*

- SumReducer.java

- *extends Reducer<\_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_>*
- *public void reduce(\_\_\_\_ key, Iterable<\_\_\_\_\_> values, Context context)*
- *context.write(key, new \_\_\_\_\_);*

- WordCount.java

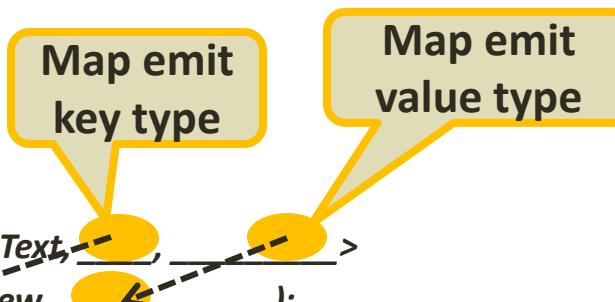
- *job.setOutputKeyClass(\_\_\_\_\_);*
- *job.setOutputValueClass(\_\_\_\_\_);*

# MapReduce Review

Map emit key-value types are the same as Reduce input key-value types

- Changes

- Package name: \_\_\_\_\_



- WordMapper.java

- *extends Mapper<LongWritable, Text, \_\_\_\_\_, \_\_\_\_\_>*
- *context.write(new \_\_\_\_\_, new \_\_\_\_\_);*

Reduce input key type

Reduce input value type

- SumReducer.java

- *extends Reducer<\_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_>*
- *public void reduce(\_\_\_\_\_, Iterable<\_\_\_\_\_, \_\_\_\_\_> values, Context context)*
- *context.write(key, new \_\_\_\_\_);*

- WordCount.java

- *job.setOutputKeyClass(\_\_\_\_\_);*
- *job.setOutputValueClass(\_\_\_\_\_);*

# MapReduce Review

Reduce emit key-value types need to be consistent

- Changes

- Package name: \_\_\_\_\_

- WordMapper.java

- *extends Mapper<LongWritable, Text, \_\_\_\_\_, \_\_\_\_\_>*
  - *context.write(new \_\_\_\_\_, new \_\_\_\_\_);*

Reduce emit key type

Reduce emit value type

- SumReducer.java

- *extends Reducer<\_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_>*
  - *public void reduce(\_\_\_\_\_, Iterable<\_\_\_\_\_, \_\_\_\_\_> values, Context context)*
  - *context.write(key, new \_\_\_\_\_);*

- WordCount.java

- *job.setOutputKeyClass(\_\_\_\_\_);*
  - *job.setOutputValueClass(\_\_\_\_\_);*

# MapReduce Review

Reduce emit key-value types are the same as Output key-value types

- Changes

- Package name: \_\_\_\_\_

- WordMapper.java

- *extends Mapper<LongWritable, Text, \_\_\_\_\_, \_\_\_\_\_>*
- *context.write(new \_\_\_\_\_, new \_\_\_\_\_);*

- SumReducer.java

- *extends Reducer<\_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_>*
- *public void reduce(\_\_\_\_\_, Iterable<\_\_\_\_\_, \_\_\_\_\_> values, Context context)*
- *context.write(key, new \_\_\_\_\_);*

Output key type

- WordCount.java

- *job.setOutputKeyClass(\_\_\_\_\_.class);*
- *job.setOutputValueClass(\_\_\_\_\_.class);*

Output value type

# MapReduce Review

## Original WordCount

- Changes
  - Package name: solution
  - WordMapper.java
    - *extends Mapper<LongWritable, Text, Text, IntWritable >*
    - *context.write(new Text(word), new IntWritable(1));*
  - SumReducer.java
    - *extends Reducer<Text, IntWritable, Text, IntWritable>*
    - *public void reduce(Text key, Iterable<IntWritable> values, Context context)*
    - *context.write(key, new IntWritable(wordCount));*
  - WordCount.java
    - *job.setOutputKeyClass(Text.class);*
    - *job.setOutputValueClass(IntWritable.class);*

# MapReduce Review

## Original WordCount

- Changes

- Package name: solution

Map emit key  
type is Text

Map emit value  
type is IntWritable

- WordMapper.java

- extends Mapper<LongWritable, Text, Text, IntWritable >*
    - context.write(new Text(word), new IntWritable(1));*

- SumReducer.java

- extends Reducer<Text, IntWritable, Text, IntWritable >*
    - public void reduce(Text key, Iterable<IntWritable> values, Context context)*
    - context.write(key, new IntWritable(wordCount));*

- WordCount.java

- job.setOutputKeyClass(Text.class);*
    - job.setOutputValueClass(IntWritable.class);*

# MapReduce Review

## Original WordCount

- Changes
  - Package name: solution
  - WordMapper.java
    - *extends Mapper<LongWritable, Text, Text, IntWritable >*
    - *context.write(new Text(word), new IntWritable(1));*
  - SumReducer.java
    - *extends Reducer<Text, IntWritable, Text, IntWritable>*
    - *public void reduce(Text key, Iterable<IntWritable> values, Context context)*
    - *context.write(key, new IntWritable(wordCount));*
  - WordCount.java
    - *job.setOutputKeyClass(Text.class);*
    - *job.setOutputValueClass(IntWritable.class);*

# MapReduce Review

## Original WordCount

- Changes
    - Package name: solution
    - WordMapper.java
      - *extends Mapper<LongWritable, Text, Text, IntWritable >*
      - *context.write(new Text(word), new IntWritable(1));*
    - SumReducer.java
      - *extends Reducer<Text, IntWritable, Text, IntWritable>*
      - *public void reduce(Text key, Iterable<IntWritable> values, Context context)*
      - *context.write(key, new IntWritable(wordCount));*
    - WordCount.java
      - *job.setOutputKeyClass(Text.class);*
      - *job.setOutputValueClass(IntWritable.class);*
- 
- The diagram illustrates the data flow in a MapReduce job:
- Mapper Stage:** An annotation "Reduce emit key type is Text" points to the key type in the Mapper's `context.write` call.
  - Reducer Stage:** Two annotations point to the reducer's `reduce` method:
    - "Reduce emit value type is IntWritable" points to the value type being emitted.
    - "Output key type is Text" points to the key type being emitted, which is the same as the mapper's key type.
  - Final Stage:** An annotation "Output value type is IntWritable" points to the `setOutputValueClass` call in the `WordCount.java` code.

# MapReduce Review

## Original WordCount

- Changes
  - Package name: solution
  - WordMapper.java
    - *extends Mapper<LongWritable, Text, Text, IntWritable >*
    - *context.write(new Text(word), new IntWritable(1));*
  - SumReducer.java
    - *extends Reducer<Text, IntWritable, Text, IntWritable>*
    - *public void reduce(Text key, Iterable<IntWritable> values, Context context)*
    - *context.write(key, new IntWritable(wordCount));*

Output key type is Text

- WordCount.java

- *job.setOutputKeyClass(Text.class);*
  - *job.setOutputValueClass(IntWritable.class);*

Output value type is  
IntWritable

Output key type  
is Text

Output value type is  
IntWritable

| Word  | Count |
|-------|-------|
| 1     | 49    |
| 10    | 1     |
| 11th  | 1     |
| 12th  | 1     |
| 1s    | 1     |
| 2     | 48    |
| 2d    | 1     |
| 2s    | 3     |
| 3     | 29    |
| 4     | 1     |
| 4d    | 1     |
| 5     | 1     |
| 5s    | 1     |
| 6     | 1     |
| 6d    | 2     |
| 6s    | 1     |
| 7     | 1     |
| 8     | 1     |
| 8d    | 2     |
| 9     | 1     |
| A     | 2027  |
| AARON | 72    |

# MapReduce Review

## Assignment: Length Count 1

- Changes
  - Package name: lengthcounts1
  - WordMapper.java
    - *extends Mapper<LongWritable, Text, Text, IntWritable >*
    - *context.write(new Text(String.valueOf(word.length()))), new IntWritable(1));*
  - SumReducer.java
    - *extends Reducer<Text, IntWritable, Text, IntWritable>*
    - *public void reduce(Text key, Iterable<IntWritable> values, Context context)*
    - *context.write(key, new IntWritable(wordCount));*
  - WordCount.java
    - *job.setOutputKeyClass(Text.class);*
    - *job.setOutputValueClass(IntWritable.class);*

The only change to WordCount does  
not require any changes to types

# MapReduce Review

## Assignment: Length Count 1

- Changes
  - Package name: lengthcounts1

Output key type  
is Text

- WordMapper.java
  - *extends Mapper<LongWritable, Text, Text, IntWritable >*
  - *context.write(new Text(String.valueOf(word.length()))), new IntWritable(1));*
- SumReducer.java
  - *extends Reducer<Text, IntWritable, Text, IntWritable>*
  - *public void reduce(Text key, Iterable<IntWritable> values, Context context)*
  - *context.write(key, new IntWritable(wordCount));*

Output key type is Text

- WordCount.java
  - *job.setOutputKeyClass(Text.class);*
  - *job.setOutputValueClass(IntWritable.class);*

| File  | Edit   | View | Se |
|-------|--------|------|----|
| 1     | 58839  |      |    |
| 10    | 10342  |      |    |
| 11    | 3830   |      |    |
| 12    | 1366   |      |    |
| 13    | 475    |      |    |
| 14    | 261    |      |    |
| 15    | 74     |      |    |
| 16    | 2      |      |    |
| 17    | 5      |      |    |
| 2     | 163405 |      |    |
| 27    | 1      |      |    |
| 3     | 199082 |      |    |
| 4     | 219685 |      |    |
| 5     | 120151 |      |    |
| 6     | 79584  |      |    |
| 7     | 59398  |      |    |
| 8     | 36863  |      |    |
| 9     | 20715  |      |    |
| (END) |        |      |    |

# MapReduce Review

## Assignment: Length Count 2

- Changes
  - Package name: lengthcounts2
  - WordMapper.java
    - *extends Mapper<LongWritable, Text, ?, IntWritable >*
    - *context.write(new IntWritable(word.length()), new IntWritable(1));*
  - SumReducer.java
    - *extends Reducer<?, IntWritable, ?, IntWritable >*
    - *public void reduce(?, key, Iterable<IntWritable> values, Context context)*
    - *context.write(key, new IntWritable(wordCount));*
  - WordCount.java
    - *job.setOutputKeyClass(?.class);*
    - *job.setOutputValueClass(IntWritable.class);*

The first change to WordCount changes  
the Map emit type to IntWritable

# MapReduce Review

## Assignment: Length Count 2

- Changes
  - Package name: lengthcounts2
  - WordMapper.java
    - *extends Mapper<LongWritable, Text, IntWritable, IntWritable >*
    - *context.write(new IntWritable(word.length()), new IntWritable(1));*
  - SumReducer.java
    - *extends Reducer<?, IntWritable, ?, IntWritable >*
    - *public void reduce(?, key, Iterable<IntWritable> values, Context context)*
    - *context.write(key, new IntWritable(wordCount));*
  - WordCount.java
    - *job.setOutputKeyClass(?.class);*
    - *job.setOutputValueClass(IntWritable.class);*

# MapReduce Review

## Assignment: Length Count 2

- Changes
  - Package name: lengthcounts2
  - WordMapper.java
    - *extends Mapper<LongWritable, Text, IntWritable, IntWritable >*
    - *context.write(new IntWritable(word.length()), new IntWritable(1));*
  - SumReducer.java
    - *extends Reducer< IntWritable, IntWritable, , IntWritable >*
    - *public void reduce(IntWritable key, Iterable<IntWritable> values, Context context)*
    - *context.write(key, new IntWritable(wordCount));*
  - WordCount.java
    - *job.setOutputKeyClass( class);*
    - *job.setOutputValueClass(IntWritable.class);*

Reduce input key type  
needs to be IntWritable

# MapReduce Review

## Assignment: Length Count 2

- Changes
  - Package name: lengthcounts2
  - WordMapper.java
    - *extends Mapper<LongWritable, Text, IntWritable, IntWritable >*
    - *context.write(new IntWritable(word.length()), new IntWritable(1));*
  - SumReducer.java
    - *extends Reducer< IntWritable, IntWritable, IntWritable, IntWritable >*
    - *public void reduce(IntWritable key, Iterable<IntWritable> values, Context context)*
    - *context.write(key, new IntWritable(wordCount));*
  - WordCount.java
    - *job.setOutputKeyClass(( ).class);*
    - *job.setOutputValueClass(IntWritable.class);*

Reduce emit key type  
needs to be IntWritable

# MapReduce Review

## Assignment: Length Count 2

- Changes
  - Package name: lengthcounts2
  - WordMapper.java
    - *extends Mapper<LongWritable, Text, IntWritable, IntWritable >*
    - *context.write(new IntWritable(word.length()), new IntWritable(1));*
  - SumReducer.java
    - *extends Reducer< IntWritable, IntWritable, IntWritable, IntWritable >*
    - *public void reduce(IntWritable key, Iterable<IntWritable> values, Context context)*
    - *context.write(key, new IntWritable(wordCount));*
  - WordCount.java
    - *job.setOutputKeyClass(IntWritable.class);*
    - *job.setOutputValueClass(IntWritable.class);*

Output key type is  
IntWritable

# MapReduce Review

## Assignment: Length Count 2

- Changes
  - Package name: lengthcounts2
  - WordMapper.java
    - *extends Mapper<LongWritable, Text, IntWritable, IntWritable >*
    - *context.write(new IntWritable(word.length()), new IntWritable(1));*
  - SumReducer.java
    - *extends Reducer< IntWritable, IntWritable, IntWritable, IntWritable >*
    - *public void reduce(IntWritable key, Iterable<IntWritable> values, Context context)*
    - *context.write(key, new IntWritable(wordCount));*
  - WordCount.java
    - *job.setOutputKeyClass(IntWritable.class);*
    - *job.setOutputValueClass(IntWritable.class);*

Output key type  
is IntWritable

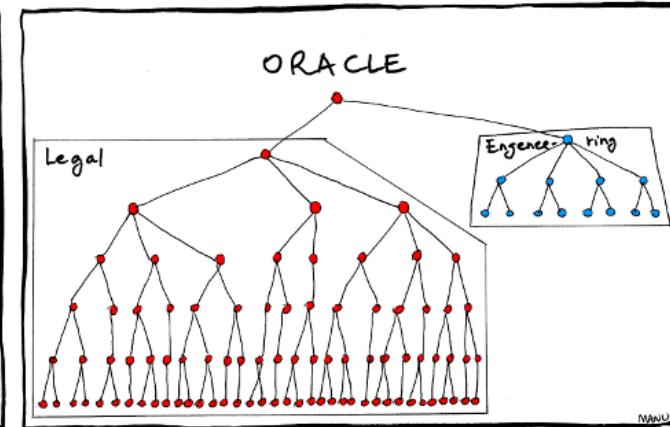
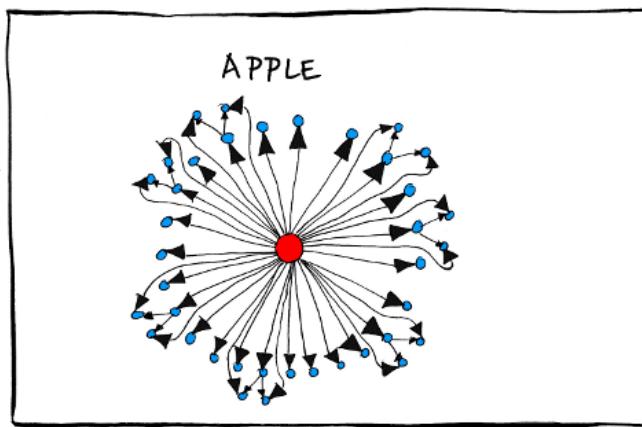
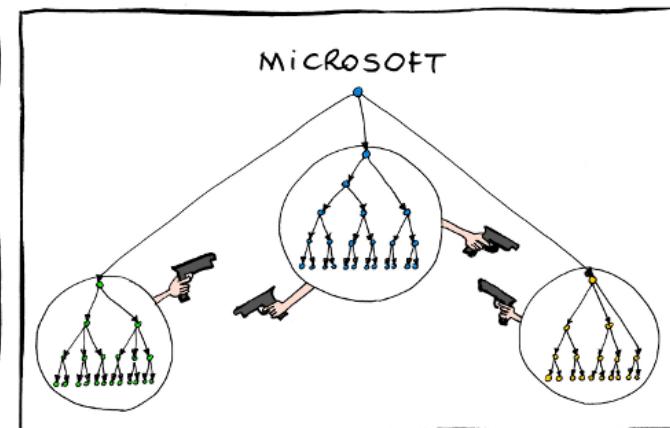
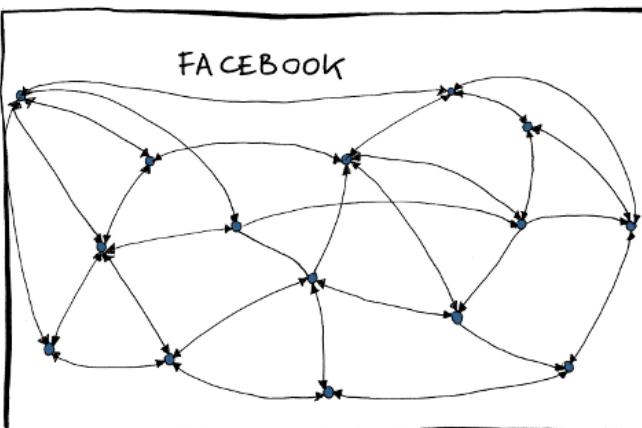
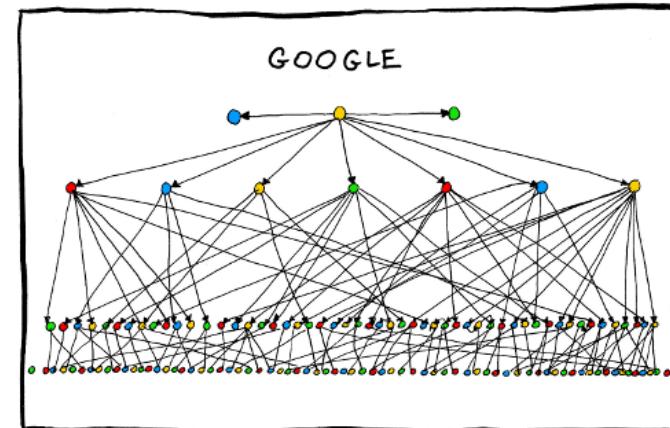
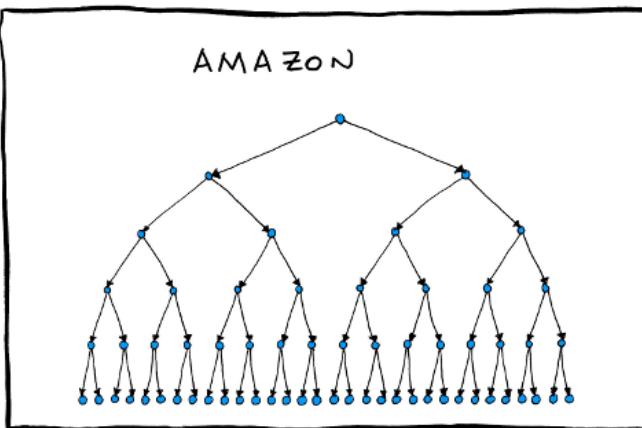
|       | File   | Edit | View | Se |
|-------|--------|------|------|----|
| 1     | 58839  |      |      |    |
| 2     | 163405 |      |      |    |
| 3     | 199082 |      |      |    |
| 4     | 219685 |      |      |    |
| 5     | 120151 |      |      |    |
| 6     | 79584  |      |      |    |
| 7     | 59398  |      |      |    |
| 8     | 36863  |      |      |    |
| 9     | 20715  |      |      |    |
| 10    | 10342  |      |      |    |
| 11    | 3830   |      |      |    |
| 12    | 1366   |      |      |    |
| 13    | 475    |      |      |    |
| 14    | 261    |      |      |    |
| 15    | 74     |      |      |    |
| 16    | 2      |      |      |    |
| 17    | 5      |      |      |    |
| 27    | 1      |      |      |    |
| (END) |        |      |      |    |

Output key type is  
IntWritable

# MapReduce Review

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# Break



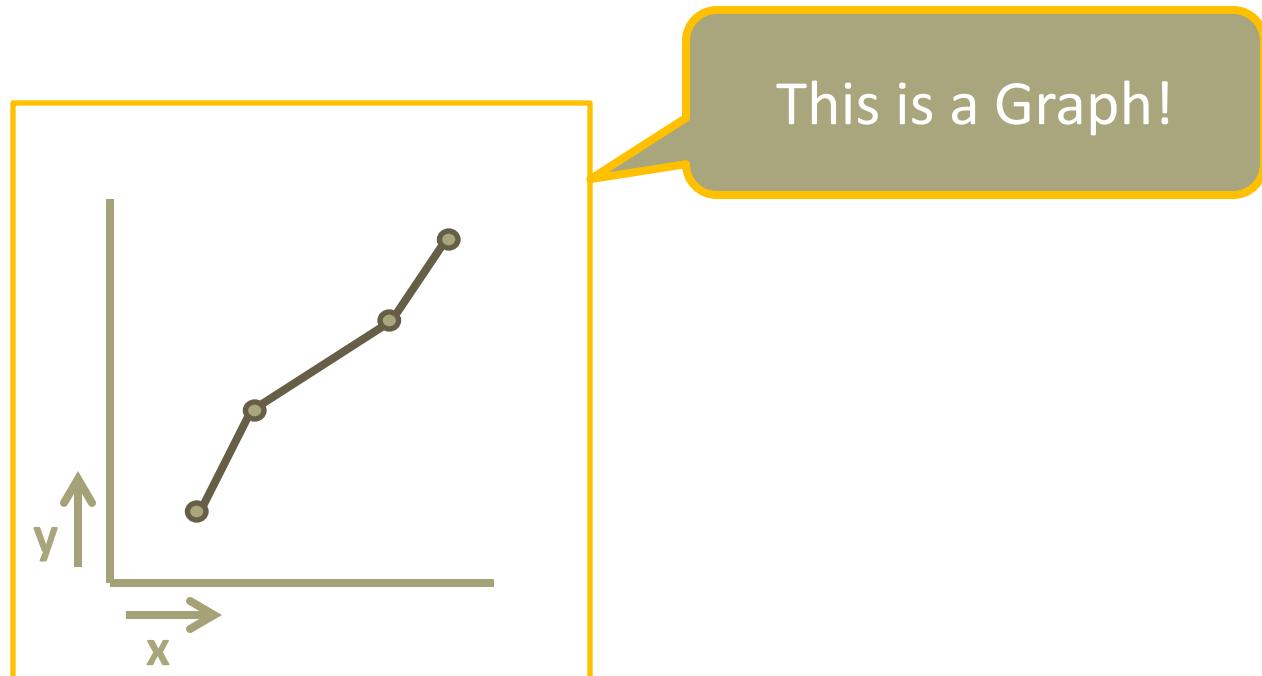
# Introduction to Graph Data

( 26 )

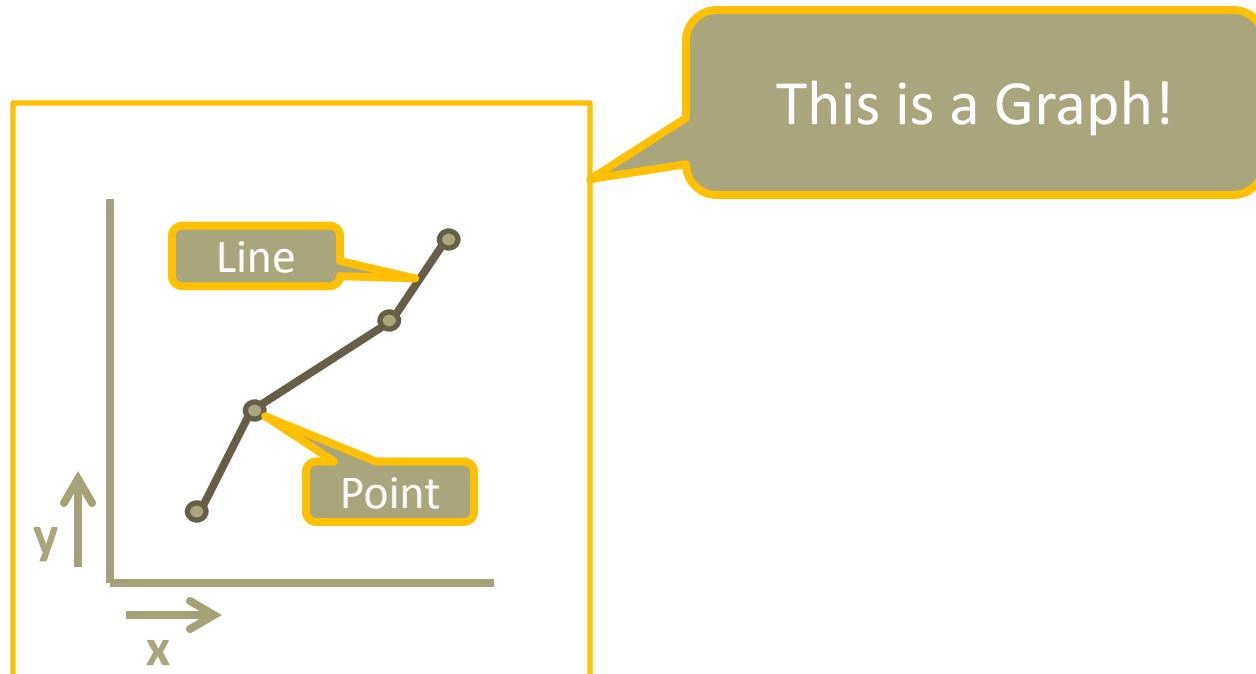
# Graph Data: What is it? (0)

What is a Graph?

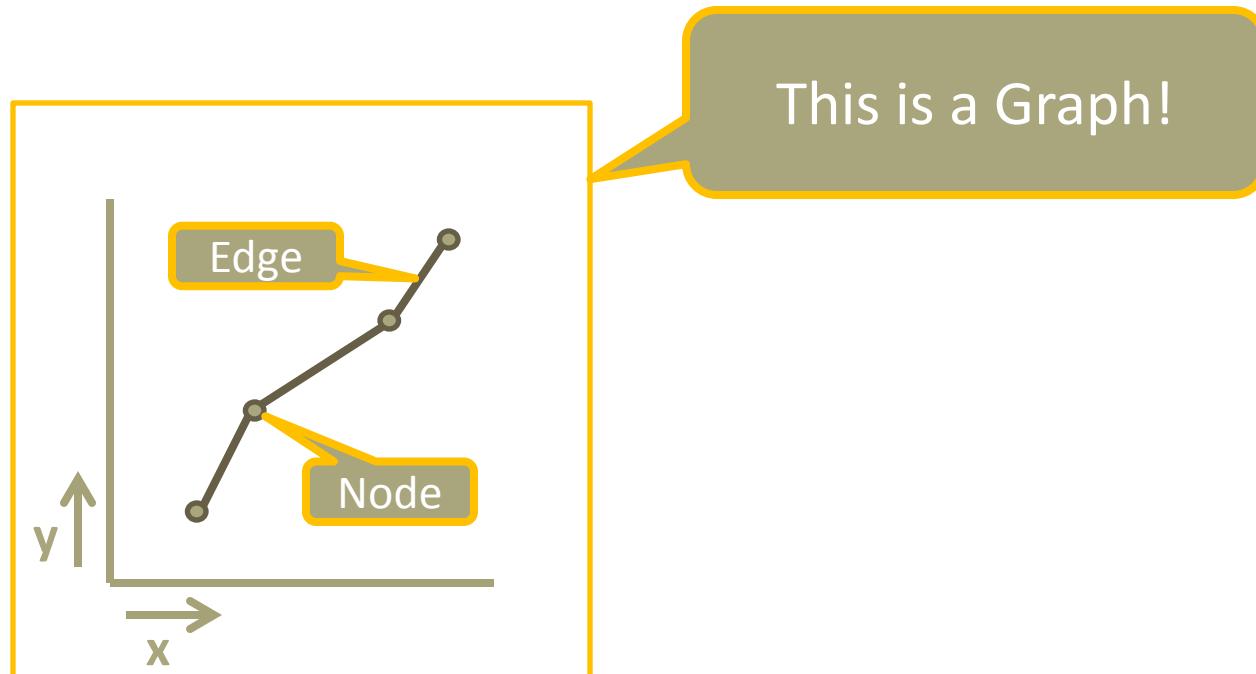
# Graph Data: What is it? (1)



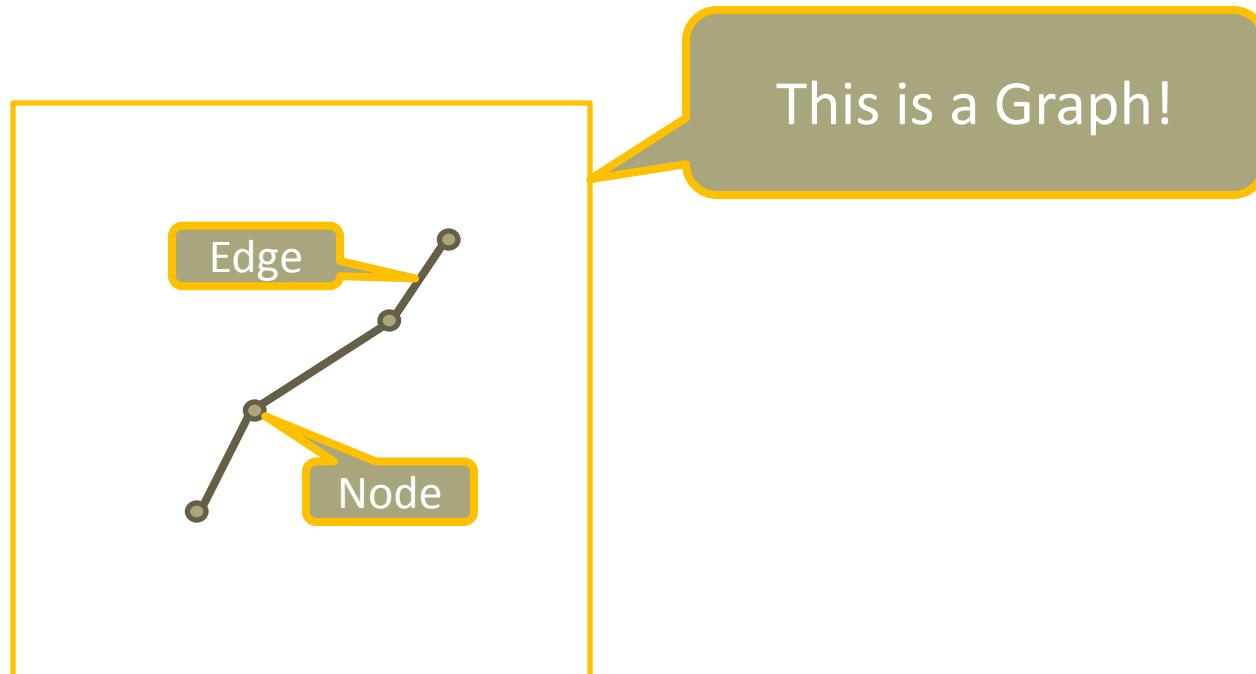
# Graph Data: What is it? (2)



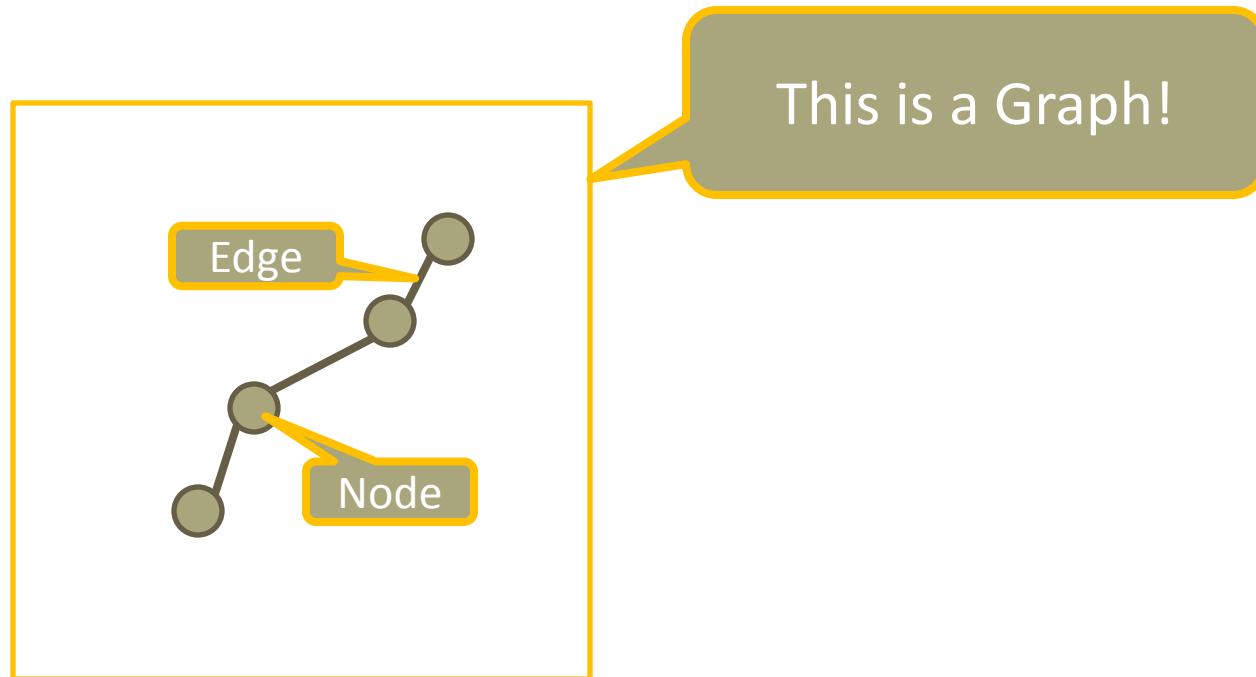
# Graph Data: What is it? (3)



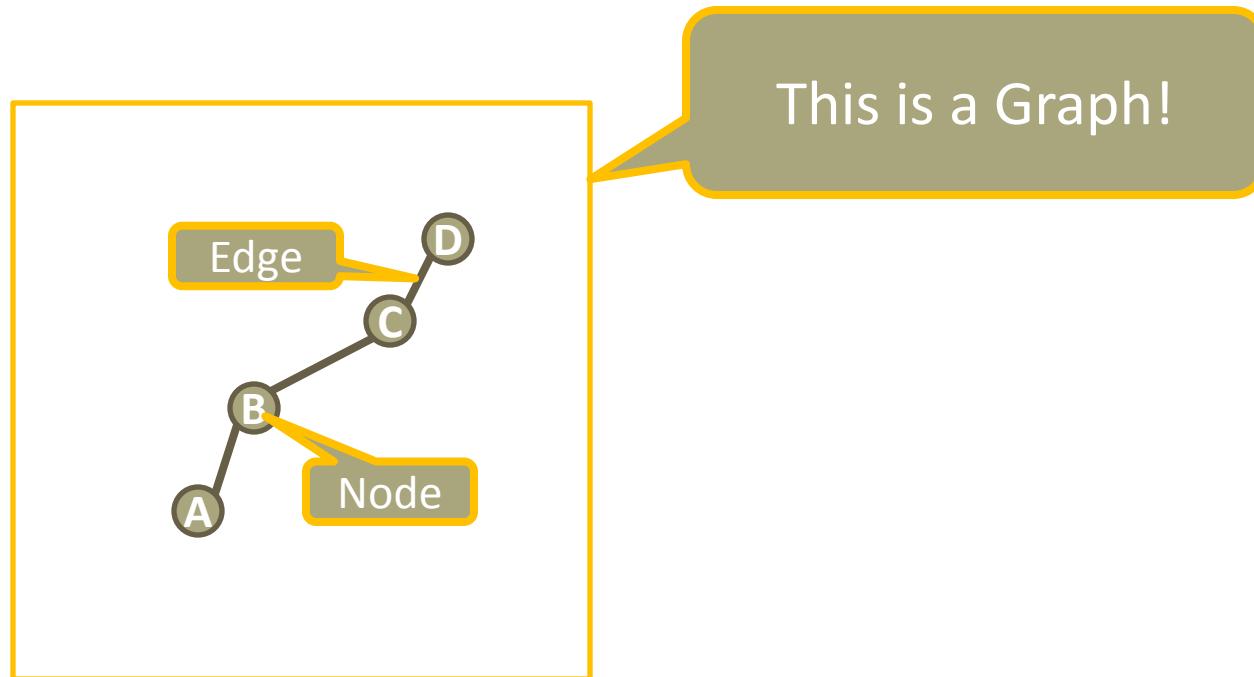
# Graph Data: What is it? (4)



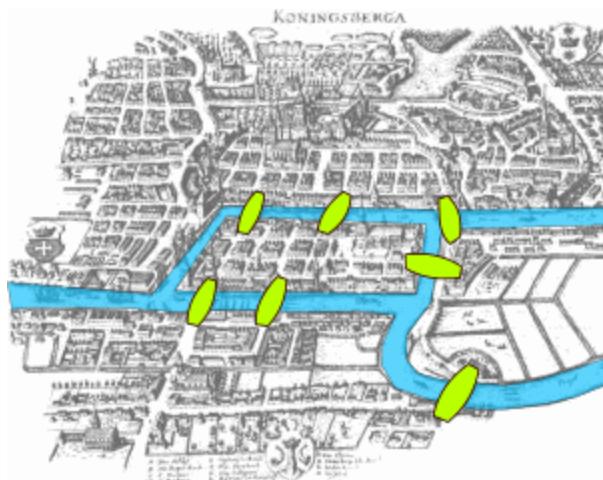
# Graph Data: What is it? (5)



# Graph Data: What is it? (6)



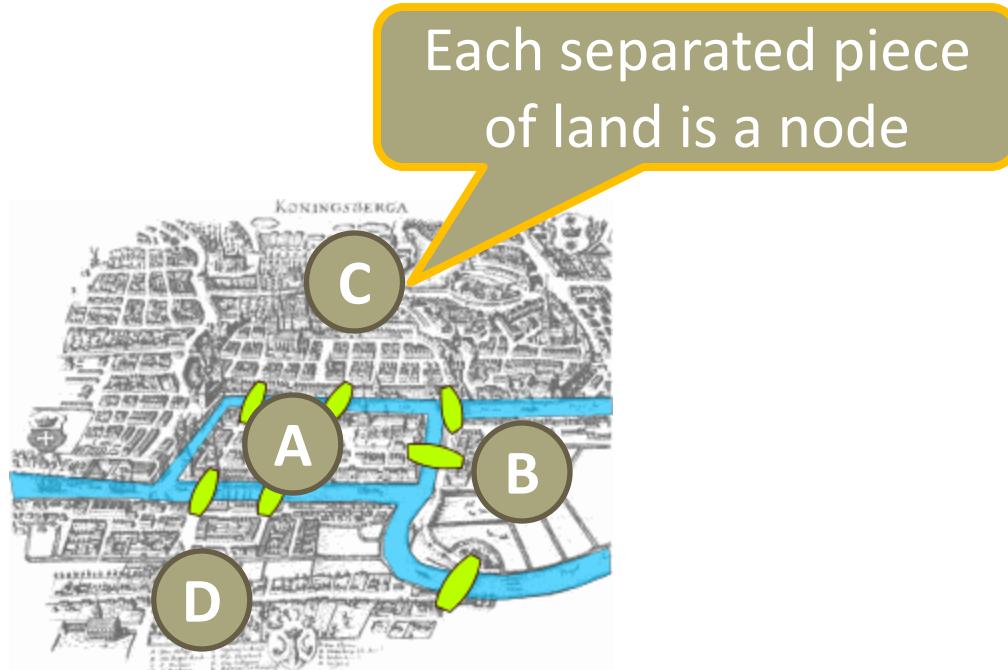
# Graph Data: Euler's Seven Bridges of Königsberg (0)



“find a walk through the city that would cross each bridge once and only once”

[http://en.wikipedia.org/wiki/Seven\\_Bridges\\_of\\_K%C3%B6nigsberg](http://en.wikipedia.org/wiki/Seven_Bridges_of_K%C3%B6nigsberg)

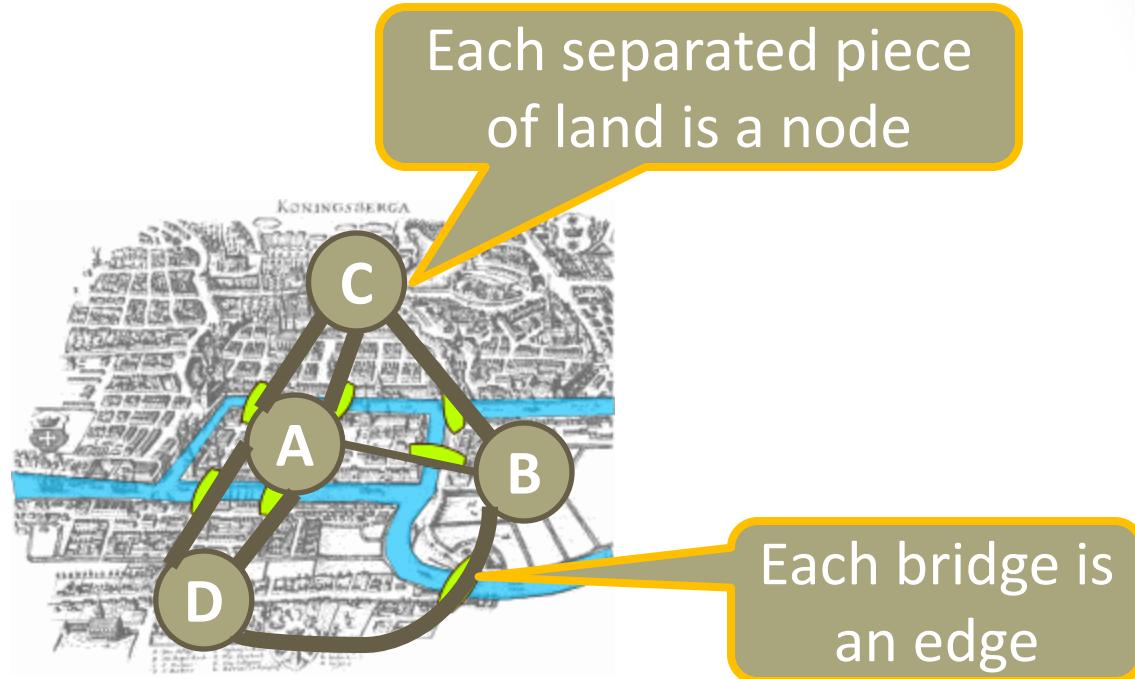
# Graph Data: Euler's Seven Bridges of Königsberg (1)



“find a walk through the city that would cross each bridge once and only once”

[http://en.wikipedia.org/wiki/Seven\\_Bridges\\_of\\_K%C3%B6nigsberg](http://en.wikipedia.org/wiki/Seven_Bridges_of_K%C3%B6nigsberg)

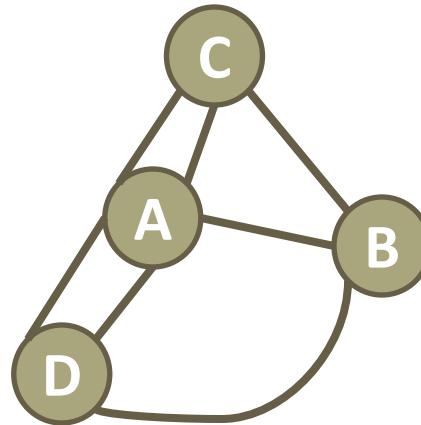
# Graph Data: Euler's Seven Bridges of Königsberg (2)



“find a walk through the city that would cross each bridge once and only once”

[http://en.wikipedia.org/wiki/Seven\\_Bridges\\_of\\_K%C3%B6nigsberg](http://en.wikipedia.org/wiki/Seven_Bridges_of_K%C3%B6nigsberg)

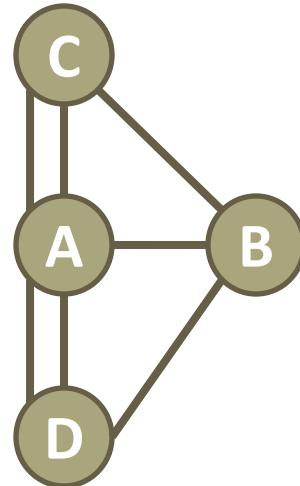
# Graph Data: Euler's Seven Bridges of Königsberg (3)



“find a walk through the city that would cross each bridge once and only once”

[http://en.wikipedia.org/wiki/Seven\\_Bridges\\_of\\_K%C3%B6nigsberg](http://en.wikipedia.org/wiki/Seven_Bridges_of_K%C3%B6nigsberg)

# Graph Data: Euler's Seven Bridges of Königsberg (4)

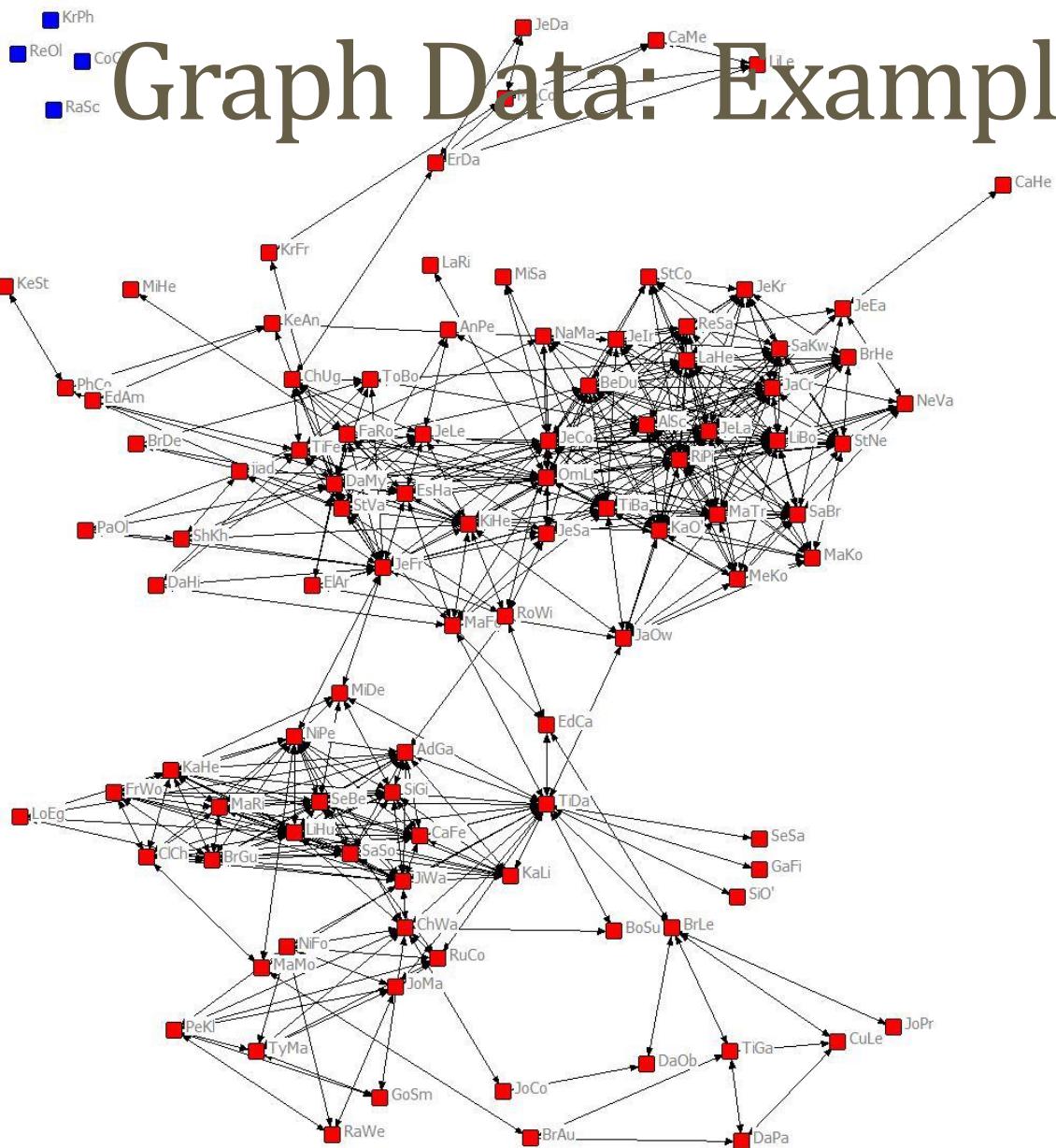


“find a walk through the city that would cross each bridge once and only once”

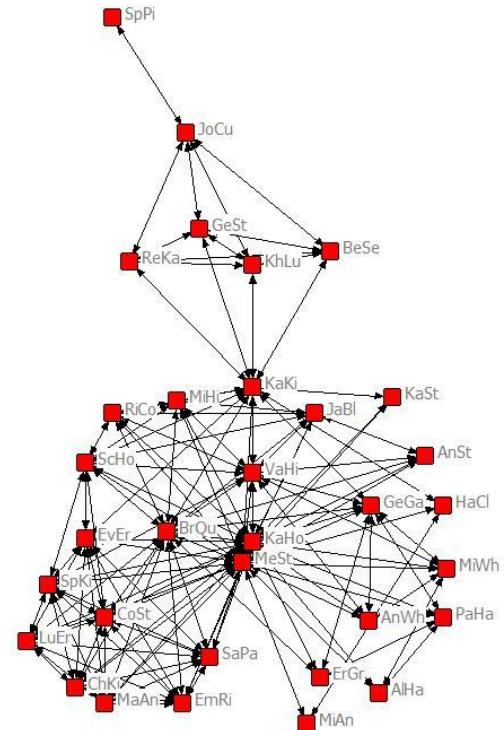
[http://en.wikipedia.org/wiki/Seven\\_Bridges\\_of\\_K%C3%B6nigsberg](http://en.wikipedia.org/wiki/Seven_Bridges_of_K%C3%B6nigsberg)

# Graph Data: Examples (0)

- Graphs represent many things like Associations and Networks.
- Graphs represent the world wide web
- Graphs represent Facebook networks
- Graphs represent metabolic pathways

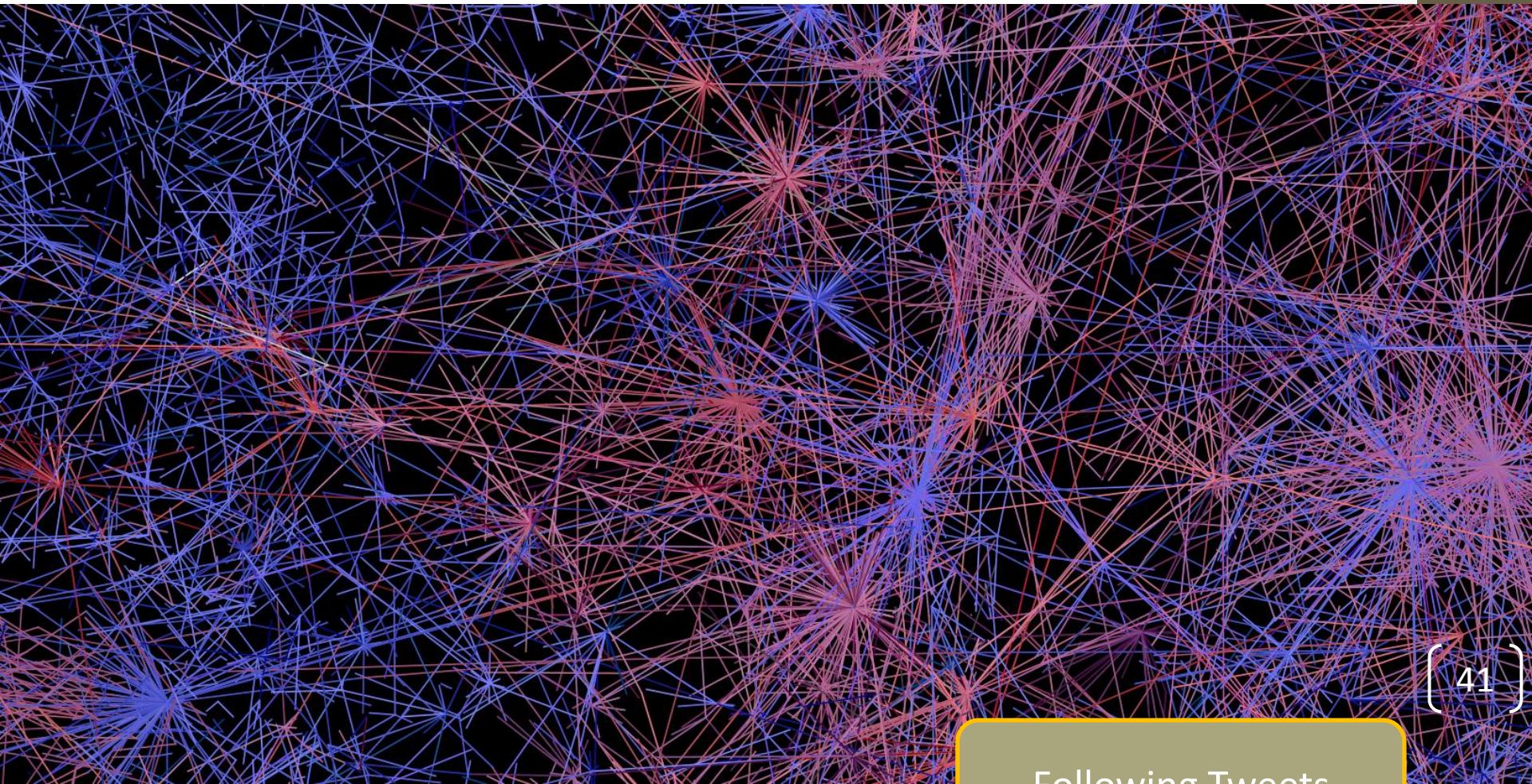


# Graph Data: Examples (1)



Facebook Connections

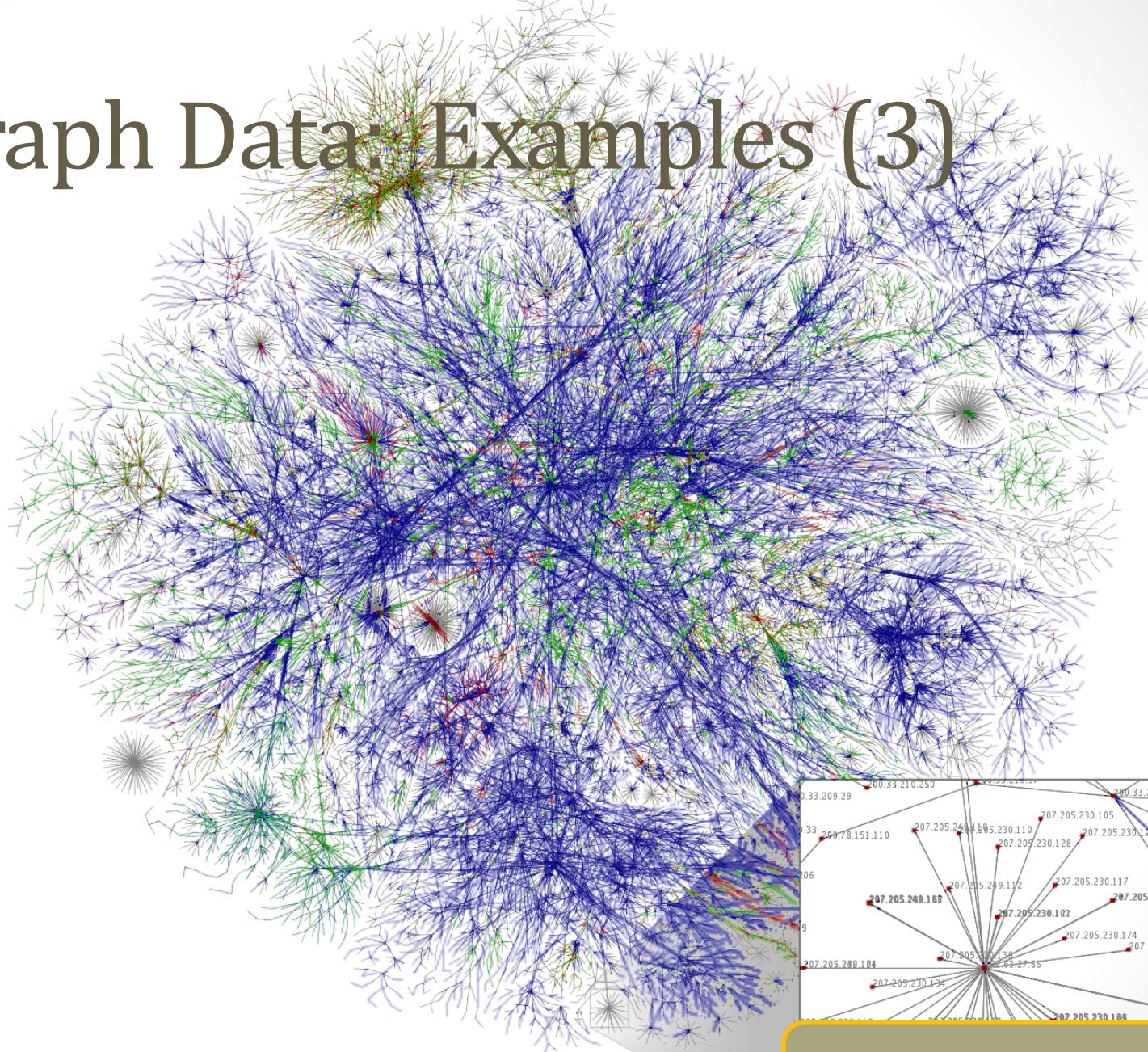
# Graph Data: Examples (2)



[ 41 ]

Following Tweets

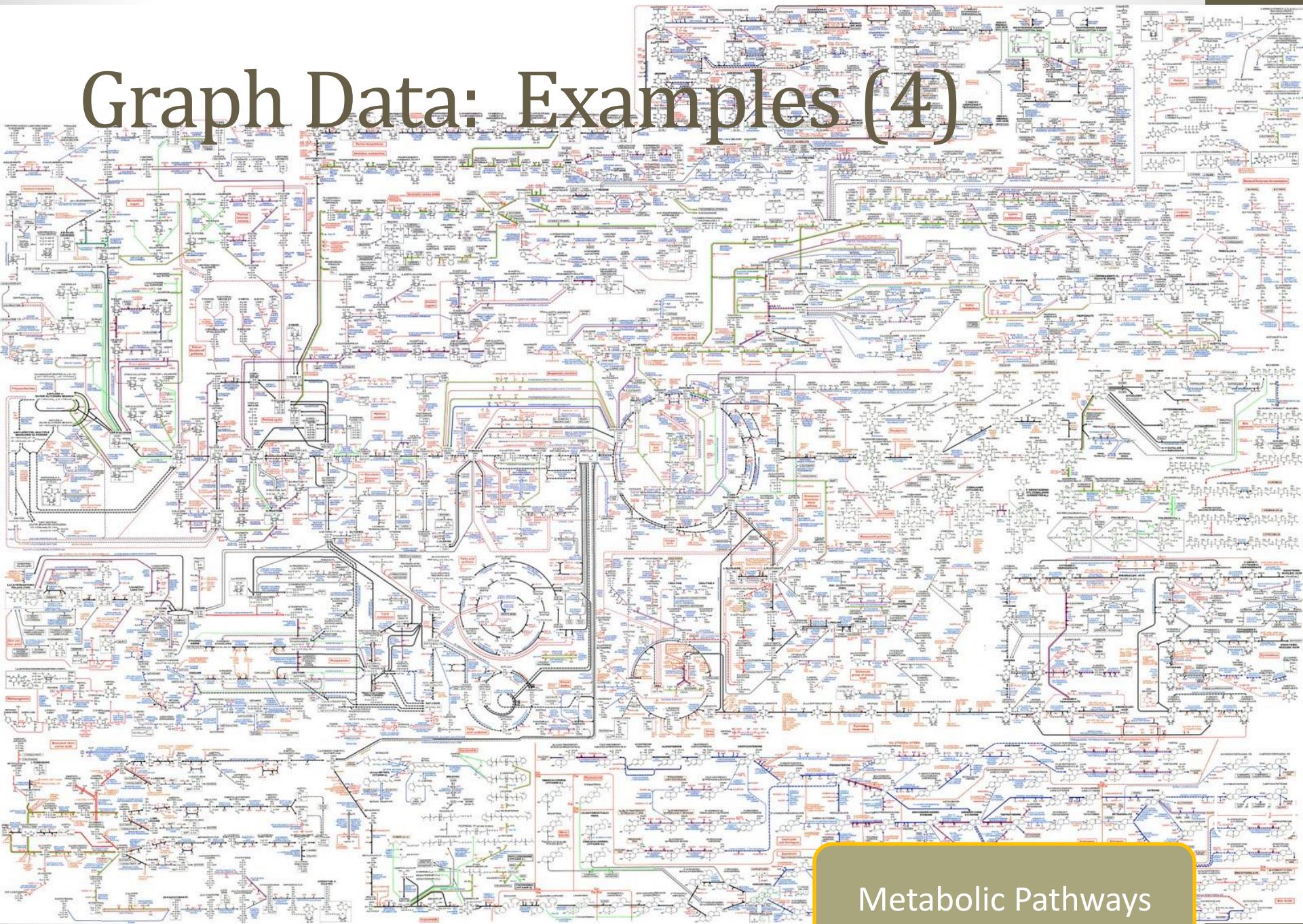
# Graph Data: Examples (3)



[ 42 ]

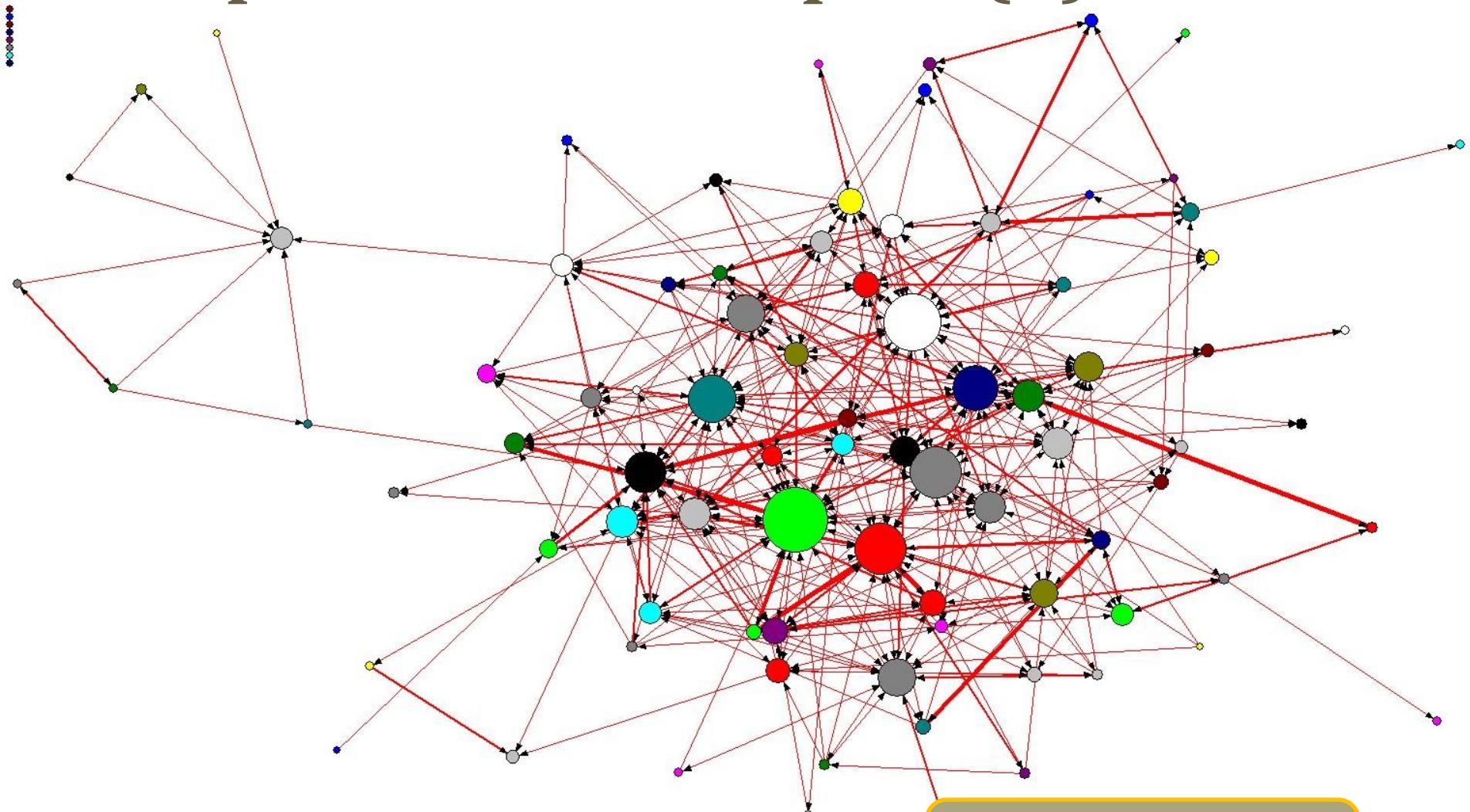
Section of the Internet

# Graph Data: Examples (4)



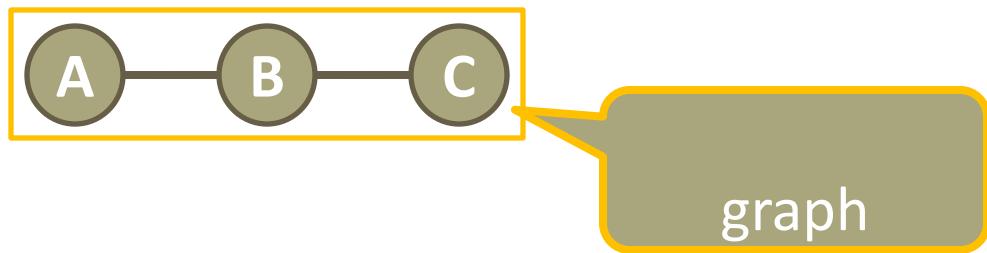
Metabolic Pathways

# Graph Data: Examples (5)

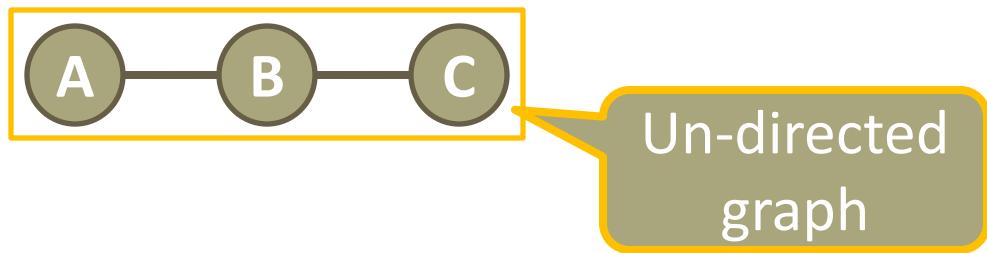


Ranked Web Pages

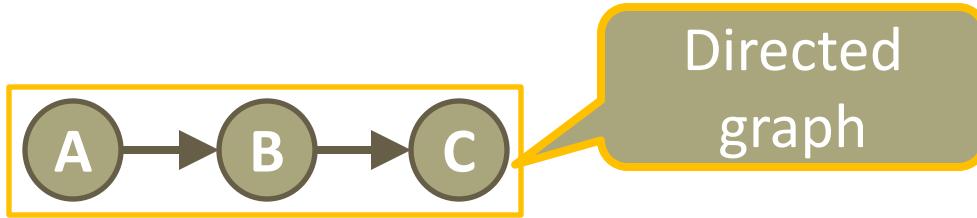
# Graph Data: Directed and Un-directed Graphs (0)



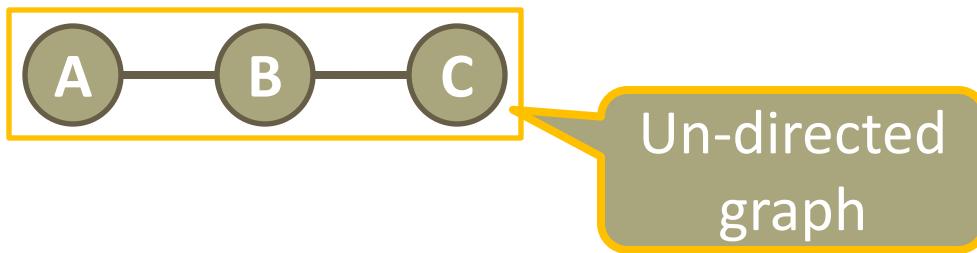
# Graph Data: Directed and Un-directed Graphs (1)



# Graph Data: Directed and Un-directed Graphs (2)

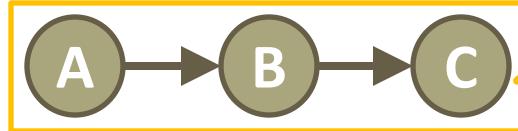


Directed  
graph



Un-directed  
graph

# Graph Data: Directed and Un-directed Graphs (3)



Directed  
graph

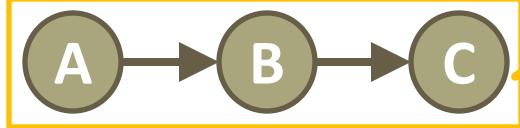
“The link goes from  
A to B”



Un-directed  
graph

“The link is  
between A and B”

# Graph Data: Directed and Un-directed Graphs (4)



Directed graph

"The link goes from A to B"

Example of directed graphs:  
World Wide Web

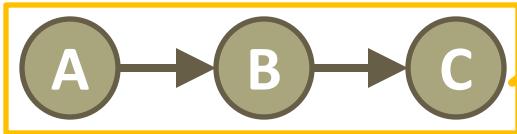


Un-directed graph

"The link is between A and B"

Examples of un-directed graphs:  
Facebook, LinkedIn

# Graph Data: Directed and Undirected Graphs (5)



Directed graph

"The link goes from A to B"

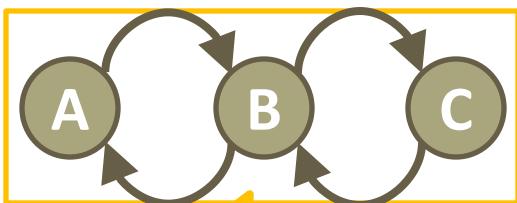
Example of directed graphs:  
World Wide Web



Un-directed graph

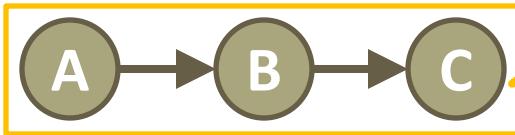
"The link is between A and B"

Examples of un-directed graphs:  
Facebook, LinkedIn



graph with bi-directional links

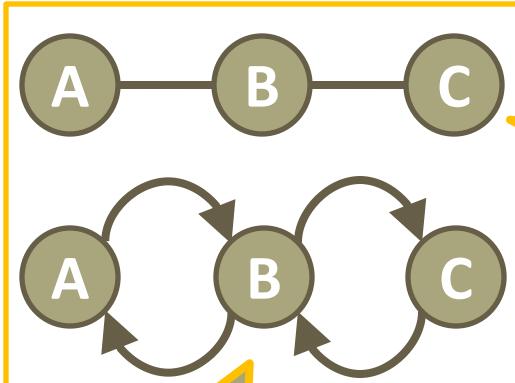
# Graph Data: Directed and Undirected Graphs (6)



Directed graph

"The link goes from A to B"

Example of directed graphs:  
World Wide Web



Un-directed graph

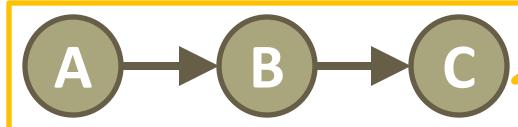
"The link is between A and B"

Examples of un-directed graphs:  
Facebook, LinkedIn

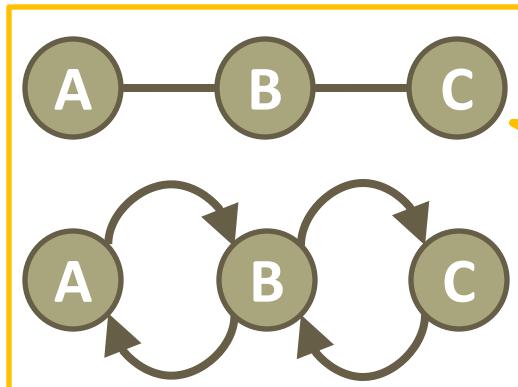
graph with bi-directional links

A graph with bi-directional links is like an undirected graph

# Graph Data: Formalize as Rectangular Data (0)



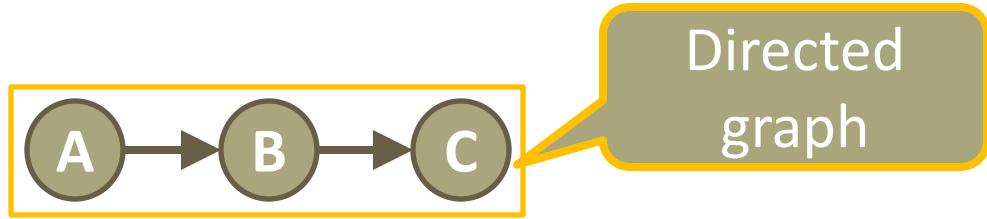
Directed  
graph



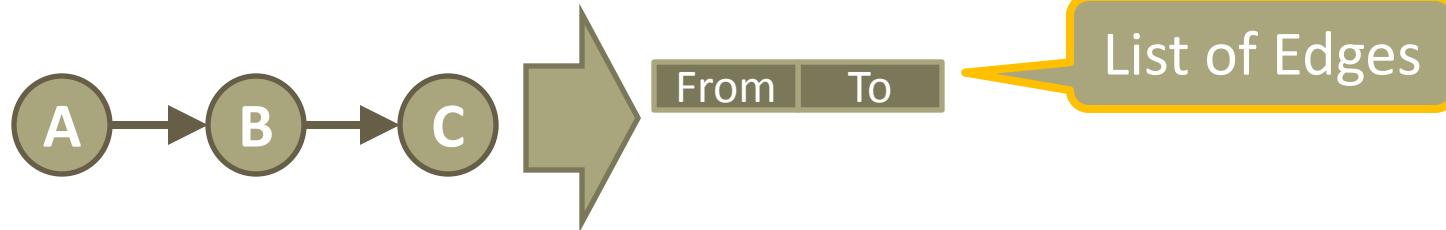
Un-directed  
graph

- How can we perform operations on graphs?
- How can we formalize graphs as rectangular data?

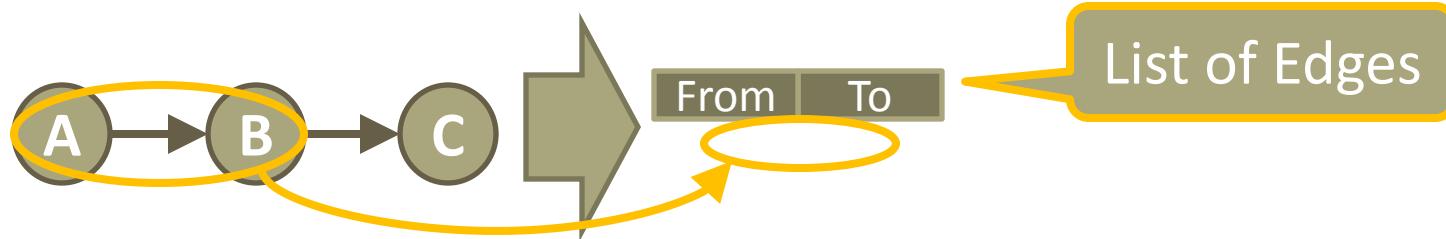
# Graph Data: Formalize as Rectangular Data (1)



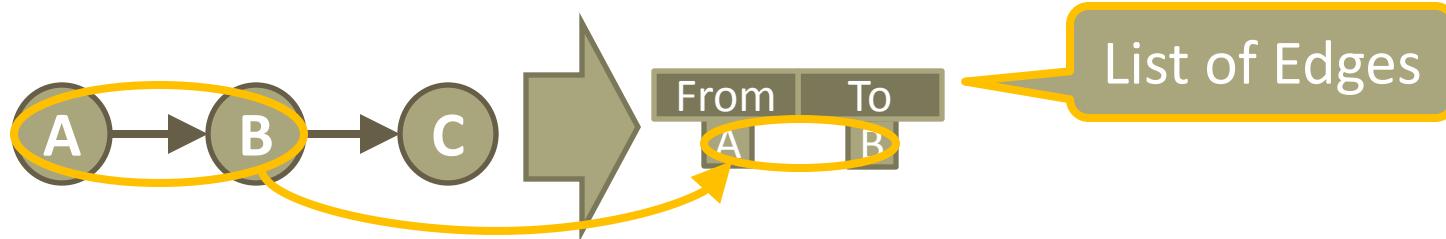
# Graph Data: Formalize as Rectangular Data (2)



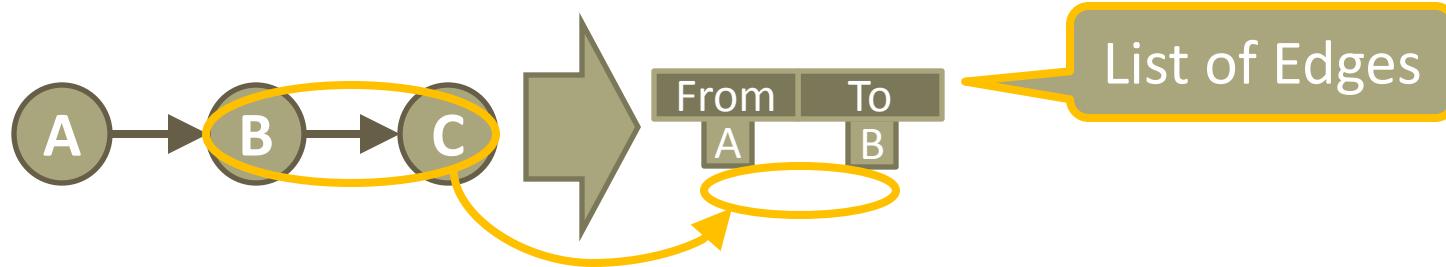
# Graph Data: Formalize as Rectangular Data (3)



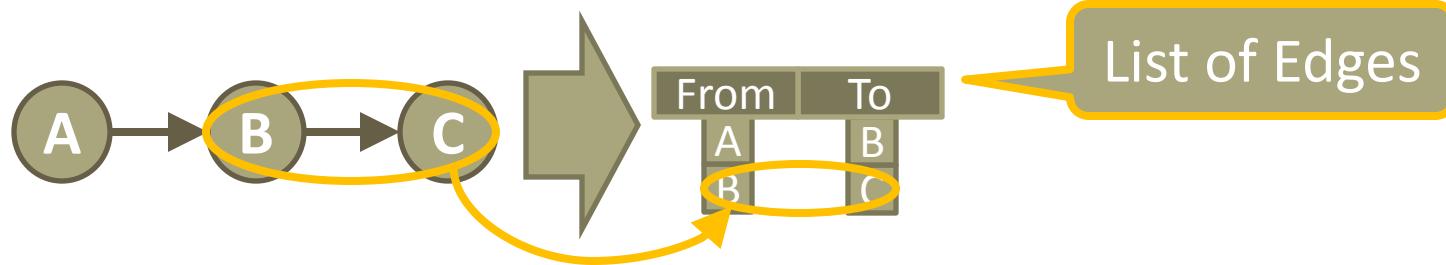
# Graph Data: Formalize as Rectangular Data (4)



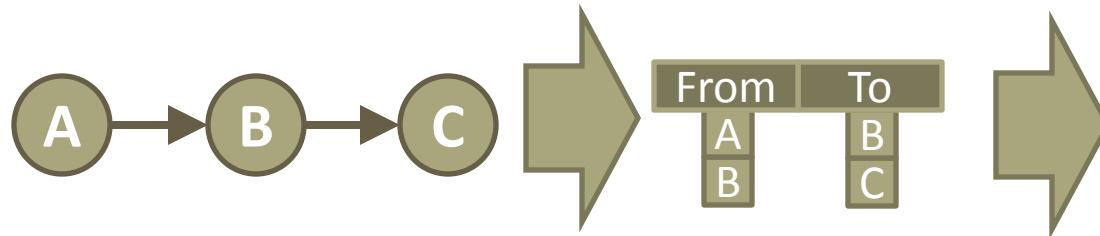
# Graph Data: Formalize as Rectangular Data (5)



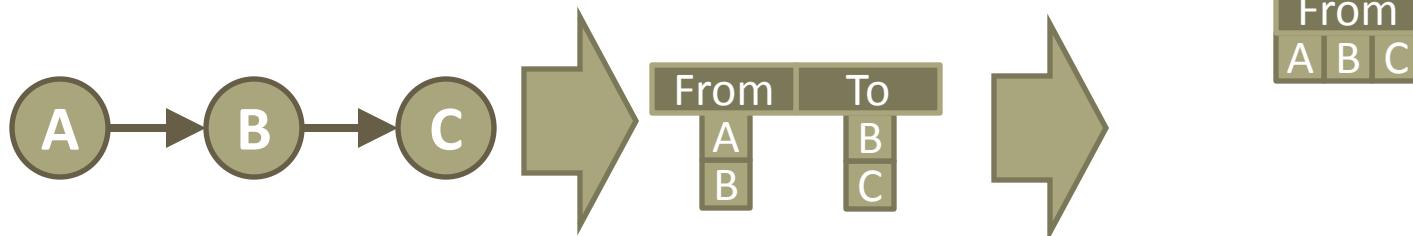
# Graph Data: Formalize as Rectangular Data (6)



# Graph Data: Formalize as Rectangular Data (7)



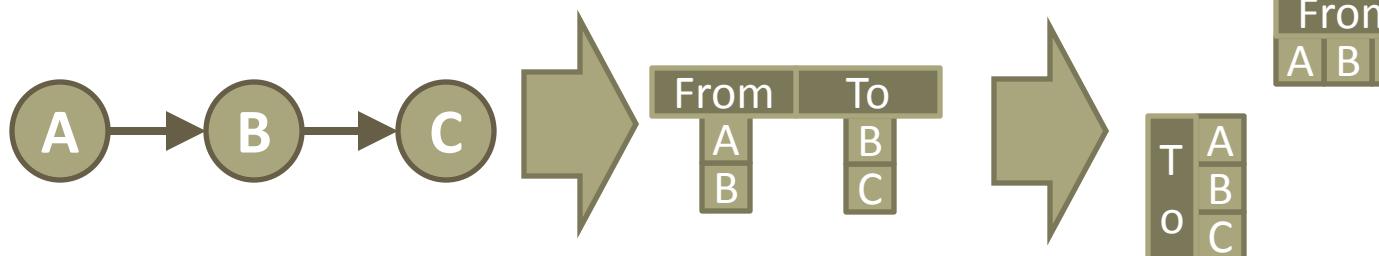
# Graph Data: Formalize as Rectangular Data (8)



Edges start from  
these nodes

From  
A B C

# Graph Data: Formalize as Rectangular Data (9)



Edges start from  
these nodes

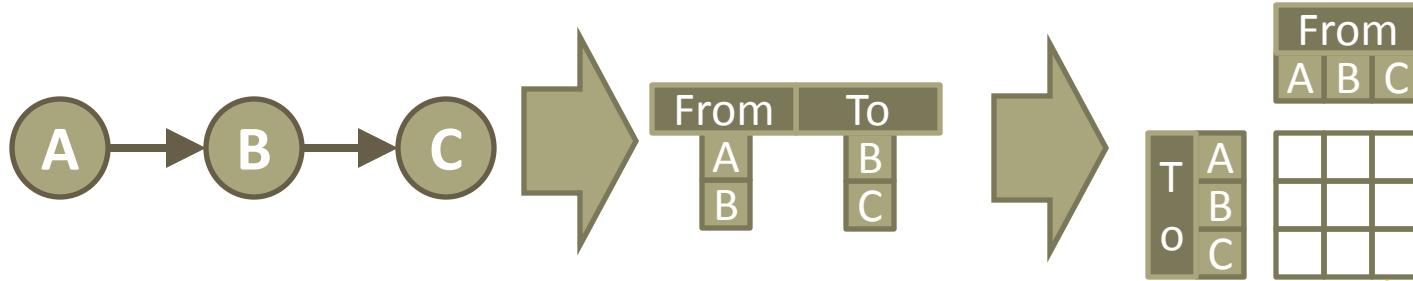
From  
A B C

Edges go to these  
nodes

T  
o  
A  
B  
C

Every node could emanate and receive  
links.

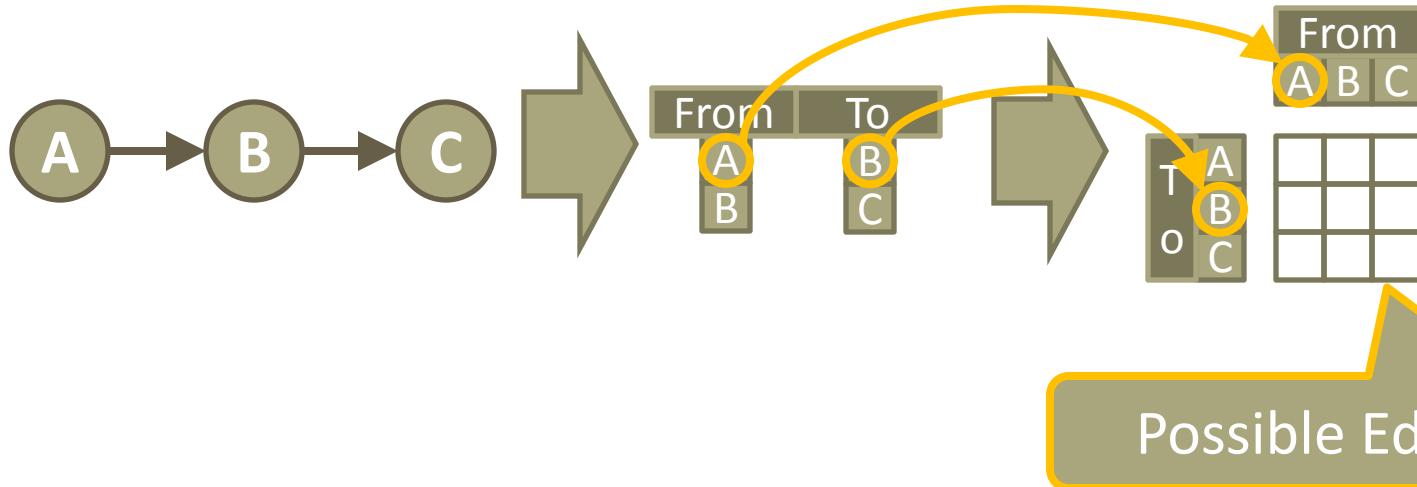
# Graph Data: Formalize as Rectangular Data (10)



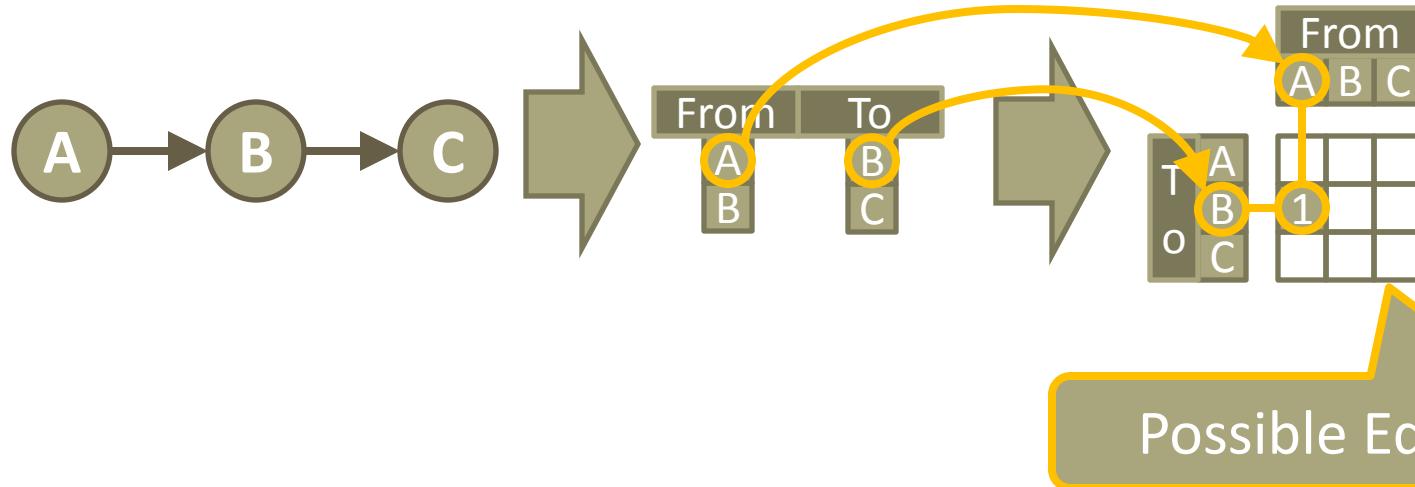
Possible Edges

Every node could emanate and receive links. Therefore the matrix is square.

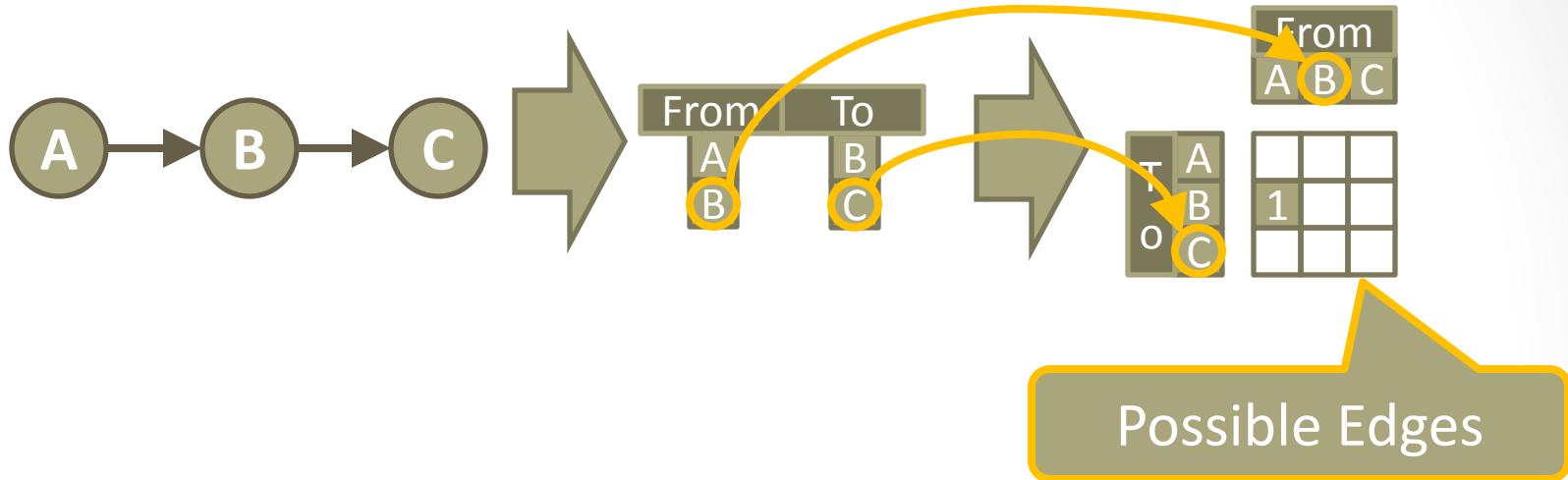
# Graph Data: Formalize as Rectangular Data (11)



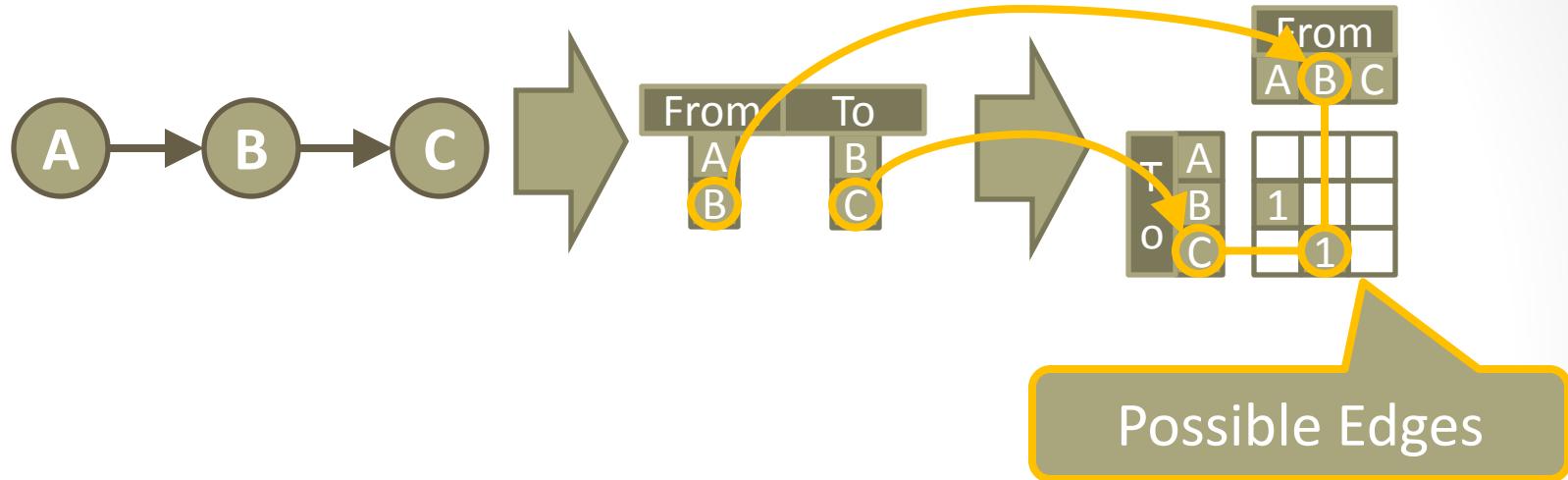
# Graph Data: Formalize as Rectangular Data (12)



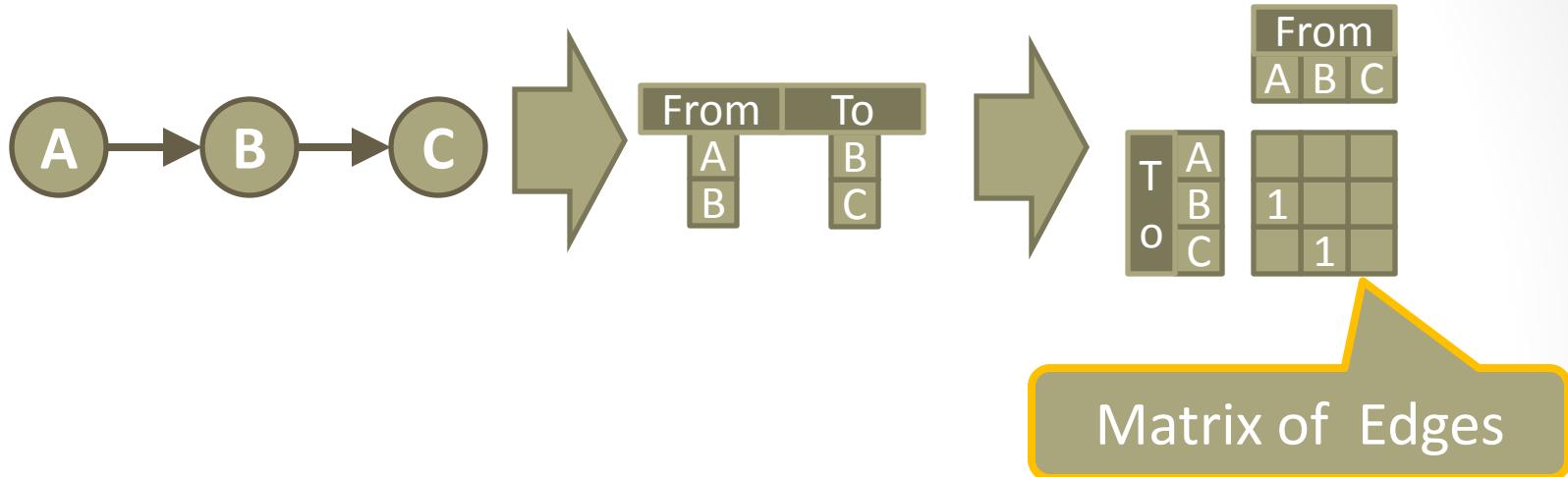
# Graph Data: Formalize as Rectangular Data (13)



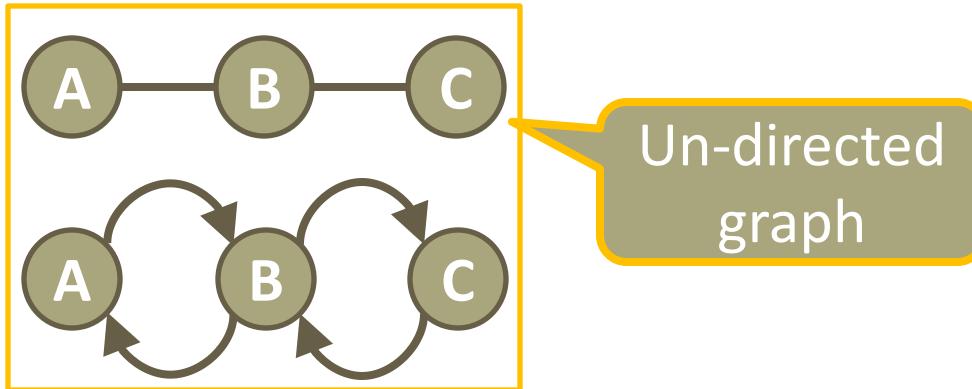
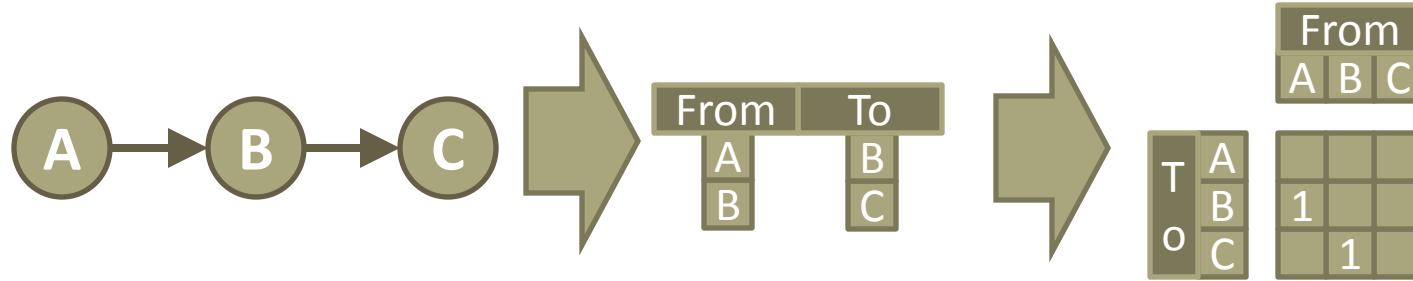
# Graph Data: Formalize as Rectangular Data (14)



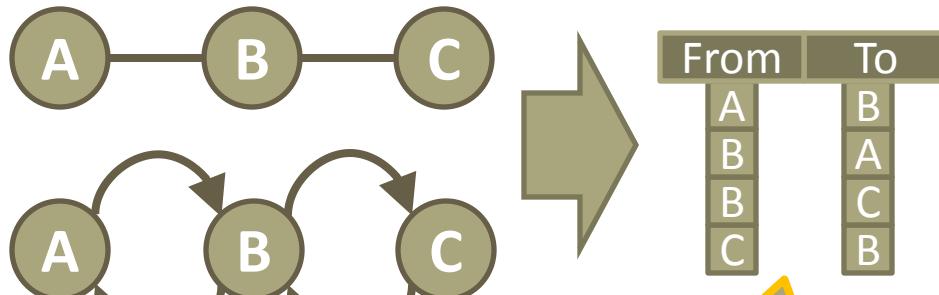
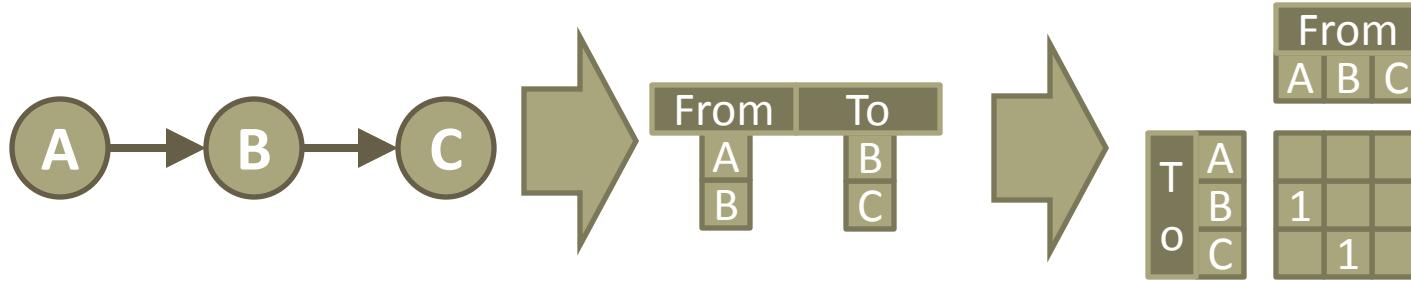
# Graph Data: Formalize as Rectangular Data (15)



# Graph Data: Formalize as Rectangular Data (16)

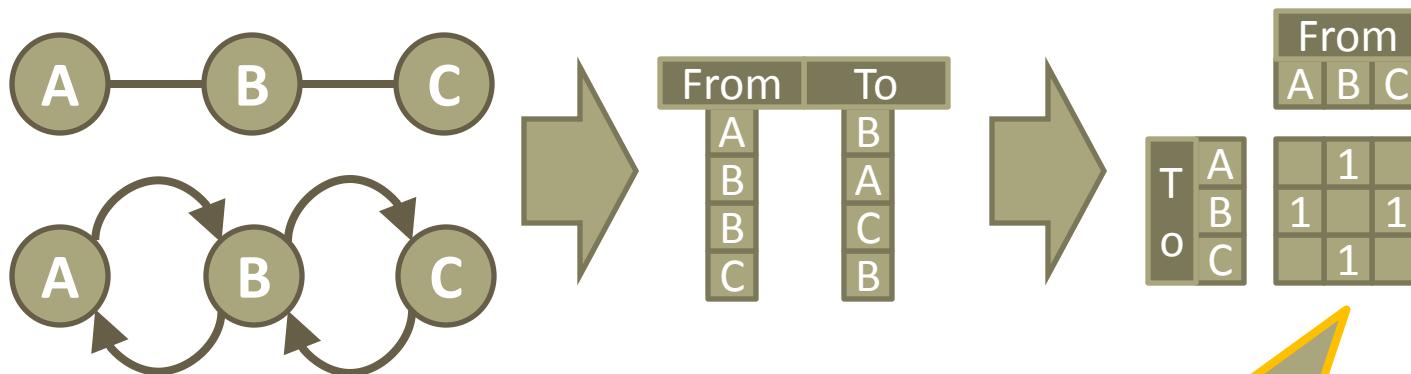
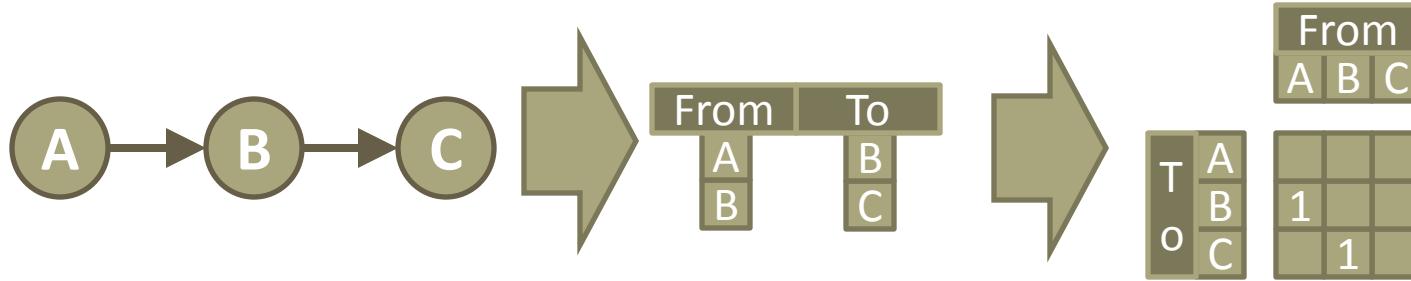


# Graph Data: Formalize as Rectangular Data (17)



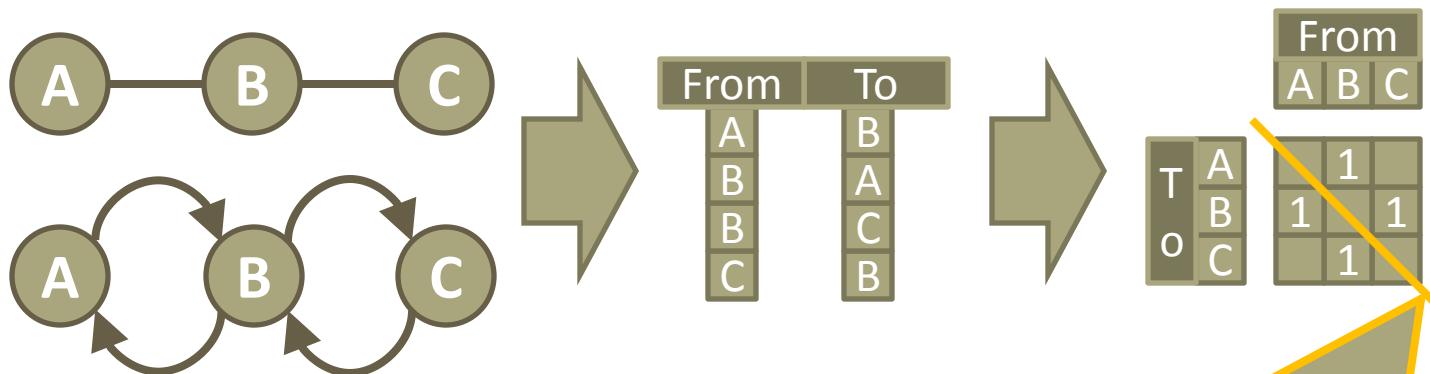
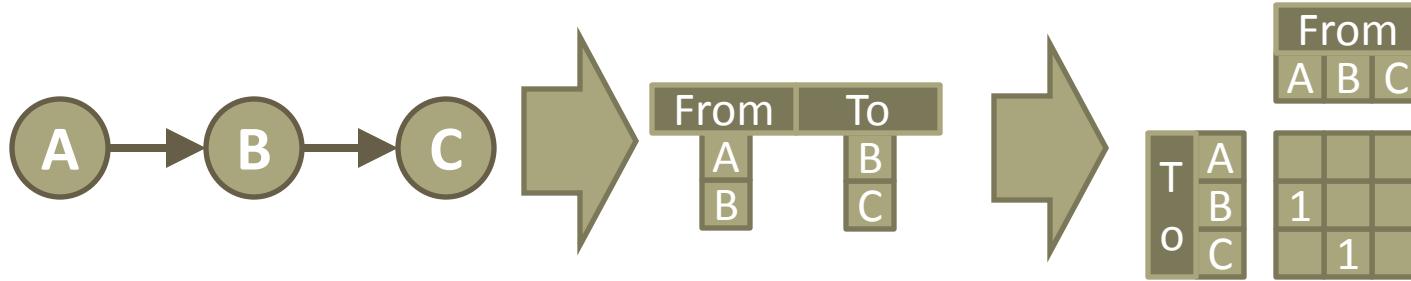
List of Edges

# Graph Data: Formalize as Rectangular Data (18)



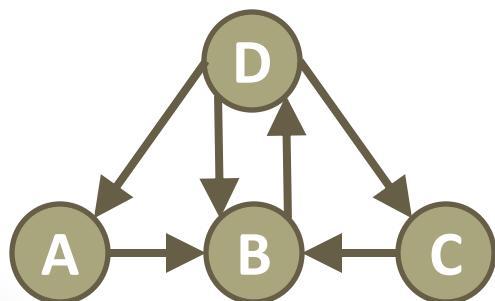
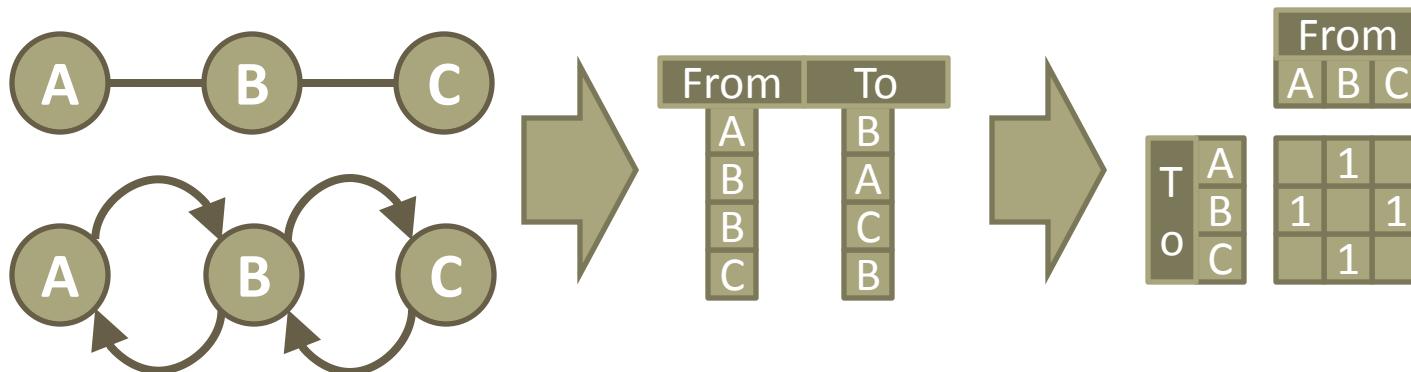
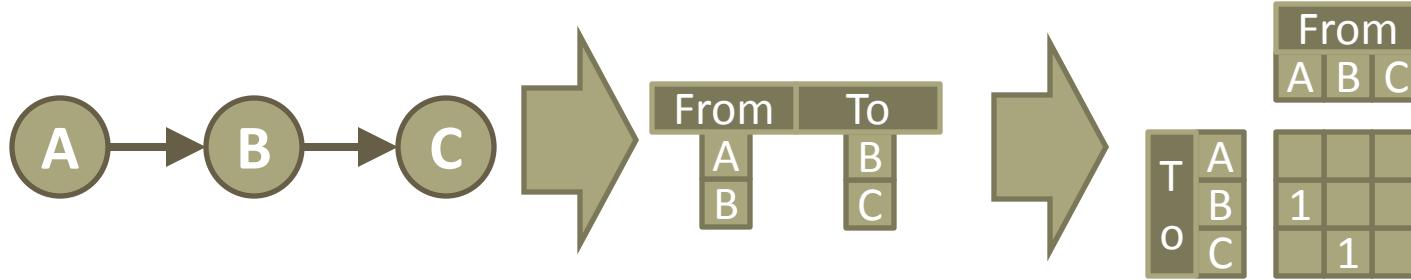
Matrix of Edges

# Graph Data: Formalize as Rectangular Data (19)

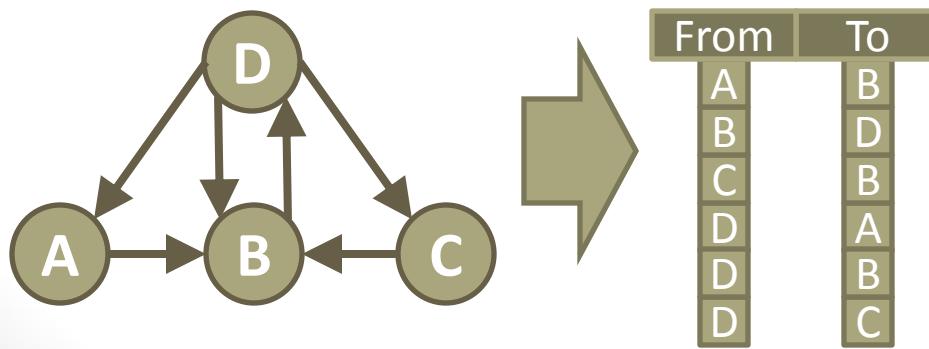
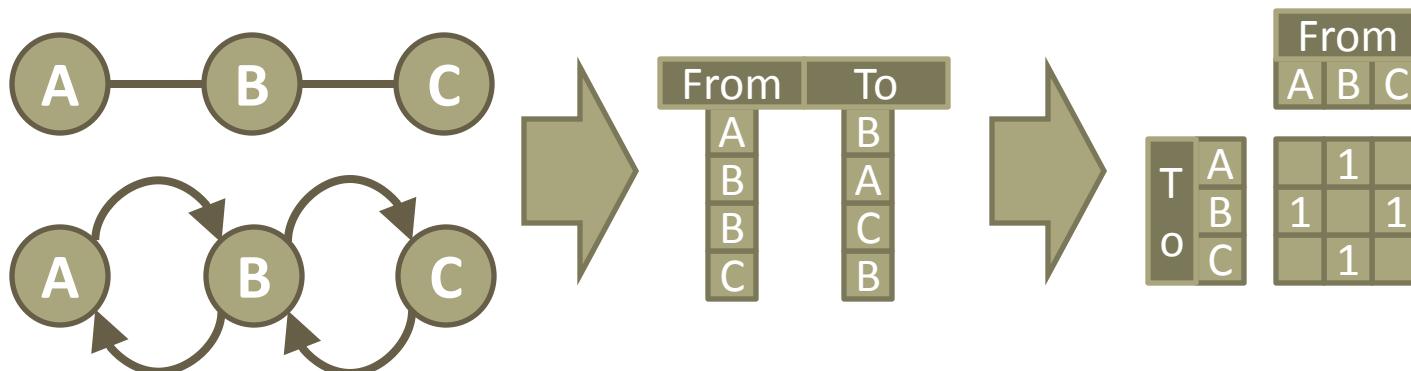
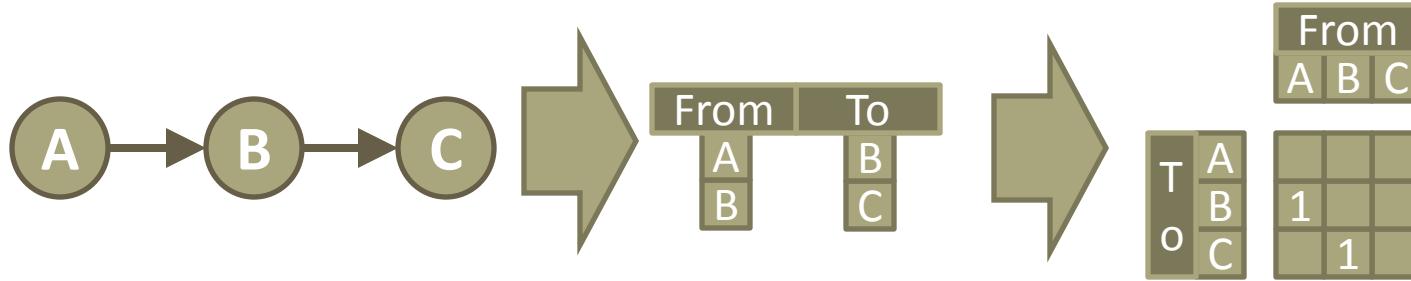


Note: undirected or bi-directional graphs Have symmetric matrices

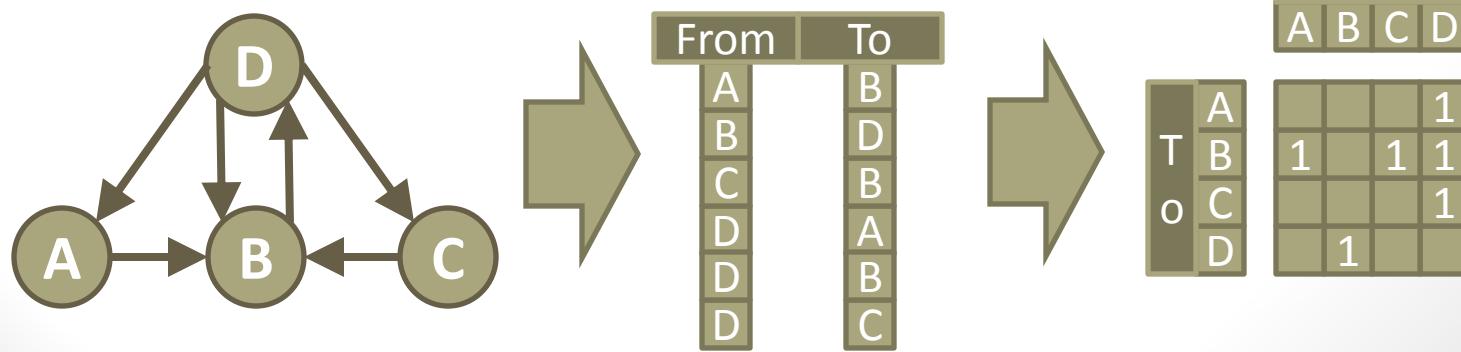
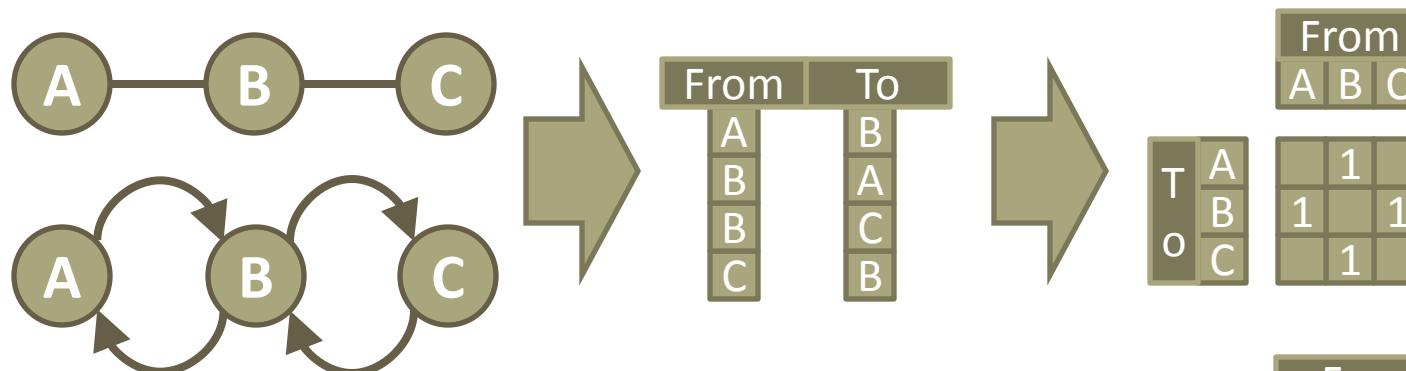
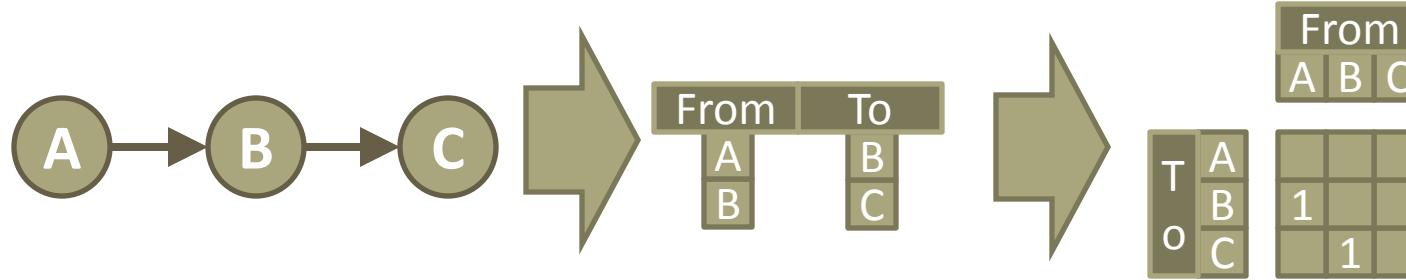
# Graph Data: Formalize as Rectangular Data (20)



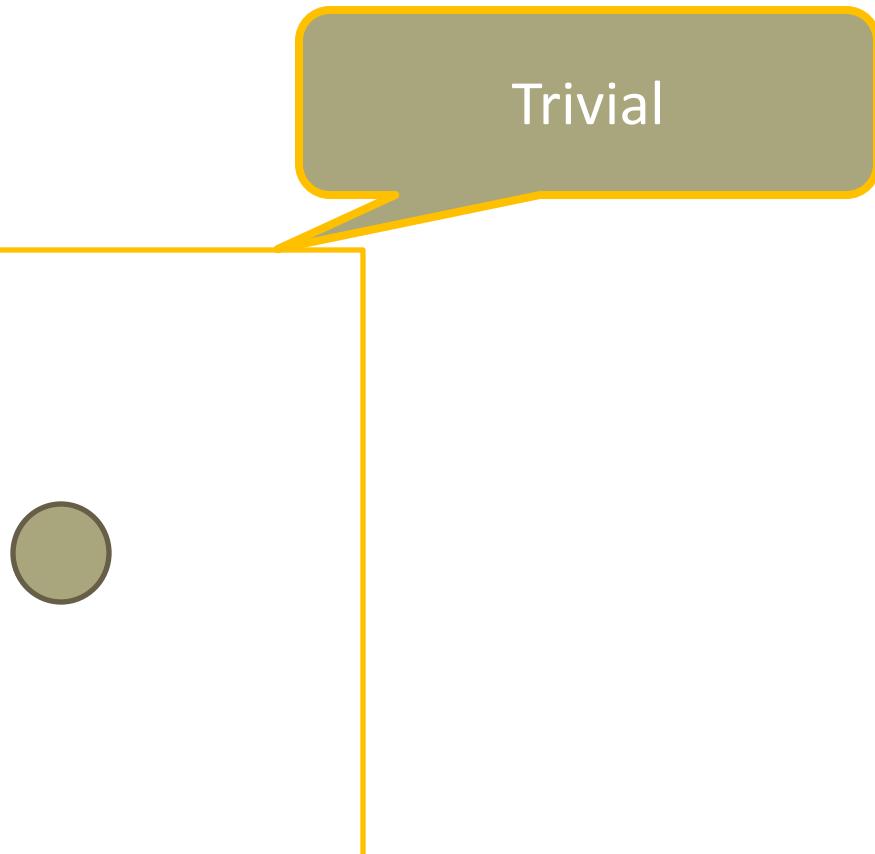
# Graph Data: Formalize as Rectangular Data (21)



# Graph Data: Formalize as Rectangular Data (22)

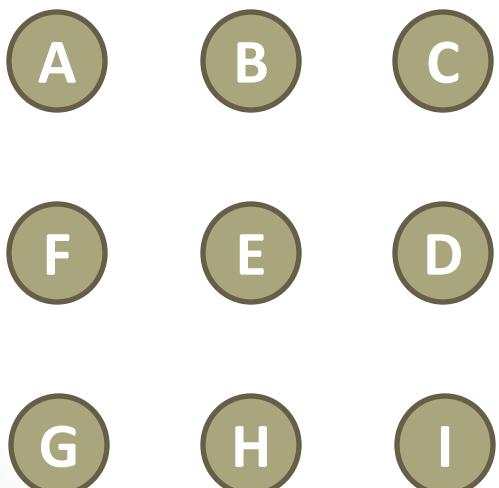


# Graph Data: Connectedness and Density (0)

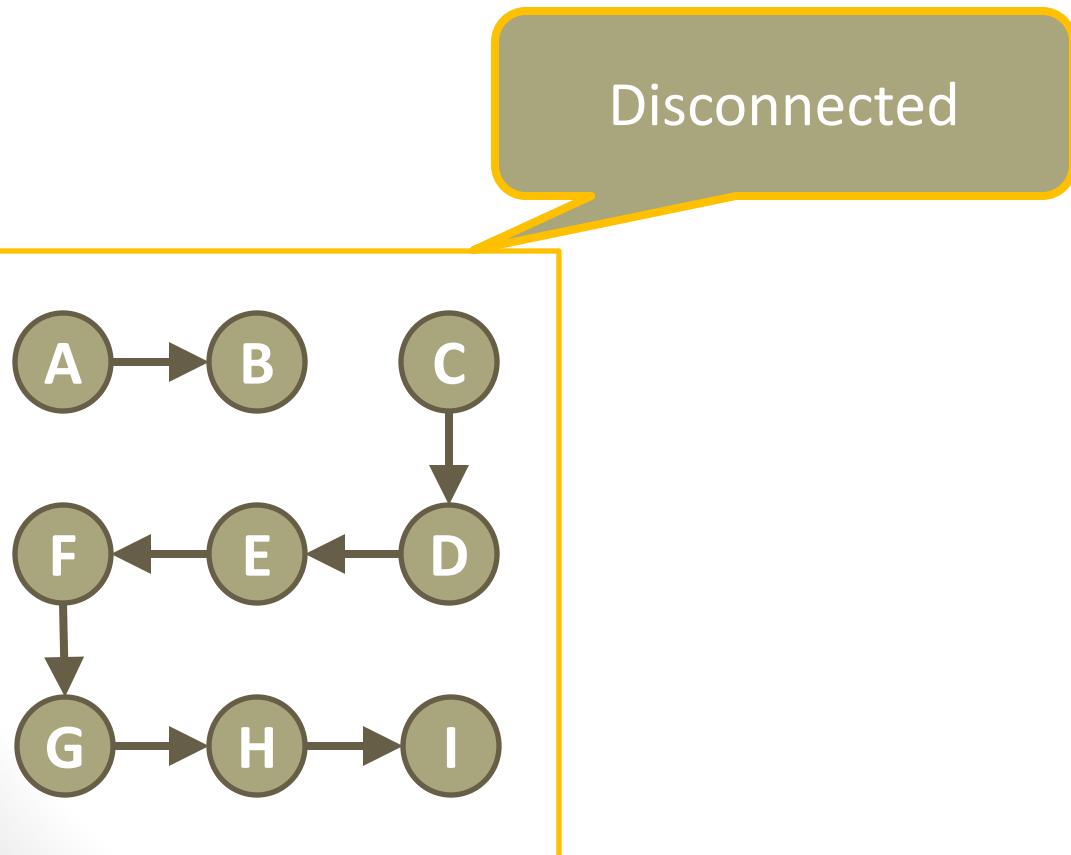


# Graph Data: Connectedness and Density (1)

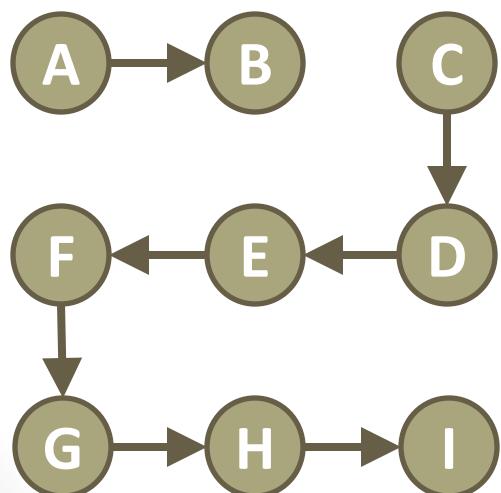
Edgeless



# Graph Data: Connectedness and Density (2)

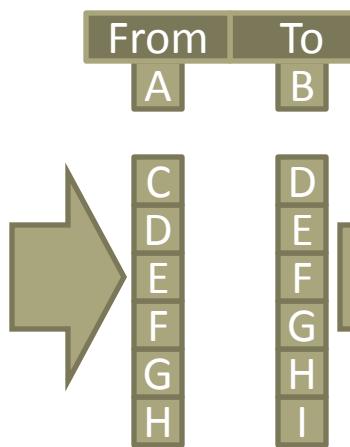
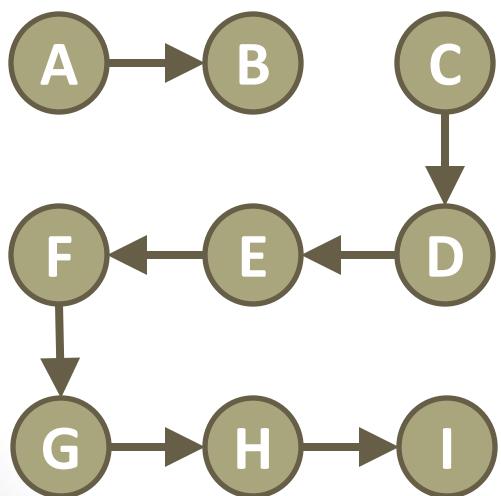


# Graph Data: Connectedness and Density (3)



| From | To |
|------|----|
| A    | B  |
| C    | D  |
| D    | E  |
| D    | F  |
| E    | G  |
| F    | G  |
| G    | H  |
| H    | I  |

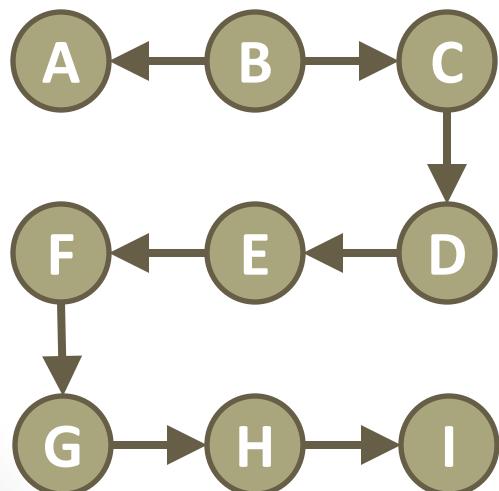
# Graph Data: Connectedness and Density (4)



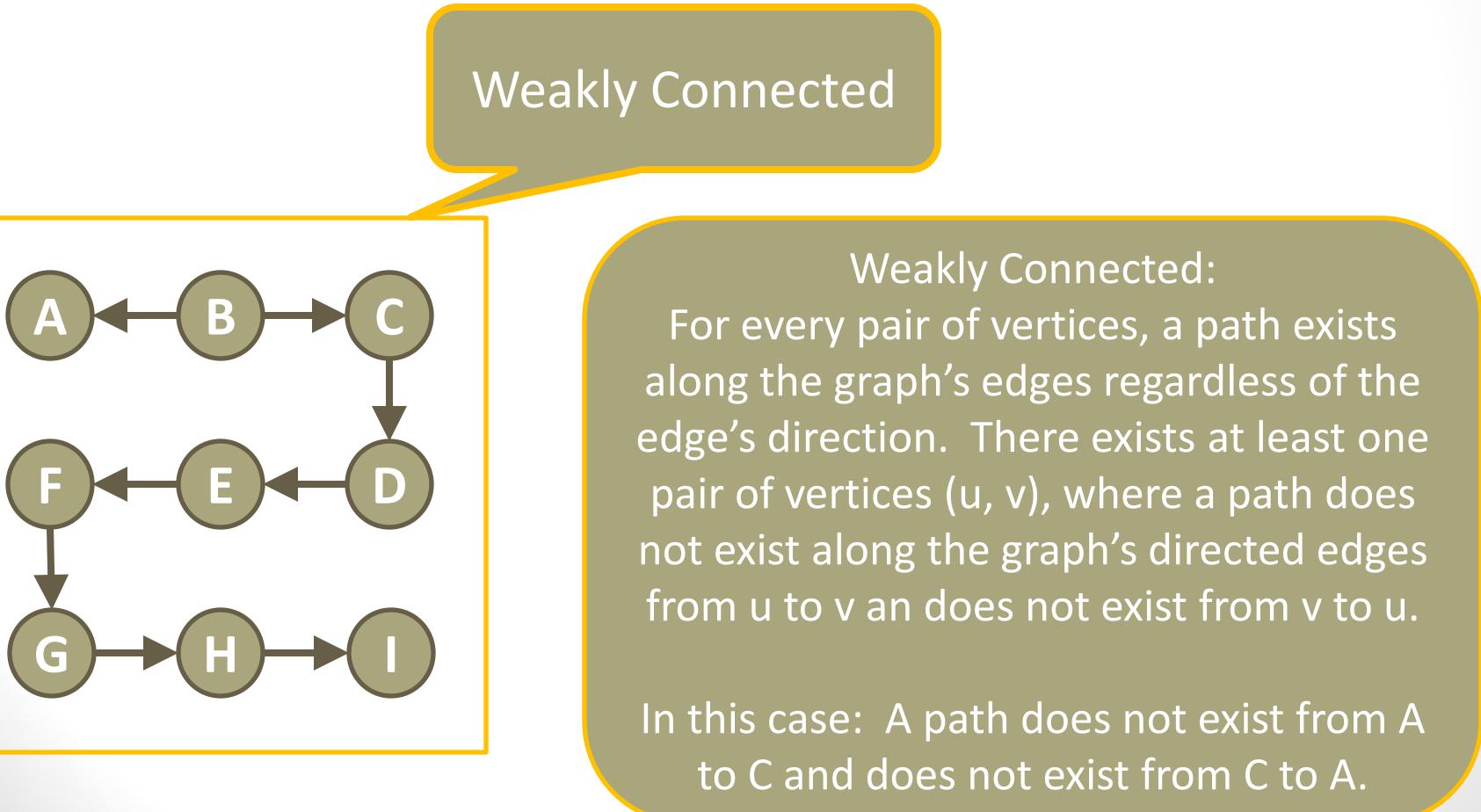
| From | A | B | C | D | E | F | G | H | I |
|------|---|---|---|---|---|---|---|---|---|
| To   | A |   |   |   |   |   |   |   |   |
| A    | 1 |   |   |   |   |   |   |   |   |
| B    |   | 1 |   |   |   |   |   |   |   |
| C    |   |   | 1 |   |   |   |   |   |   |
| D    |   |   |   | 1 |   |   |   |   |   |
| E    |   |   |   |   | 1 |   |   |   |   |
| F    |   |   |   |   |   | 1 |   |   |   |
| G    |   |   |   |   |   |   | 1 |   |   |
| H    |   |   |   |   |   |   |   | 1 |   |
| I    |   |   |   |   |   |   |   |   | 1 |

# Graph Data: Connectedness and Density (5)

Weakly Connected

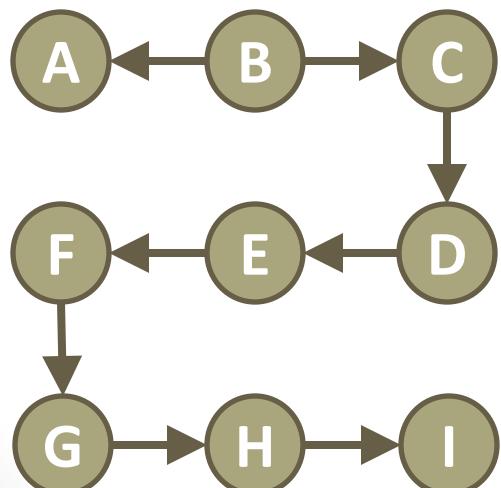


# Graph Data: Connectedness and Density (6)



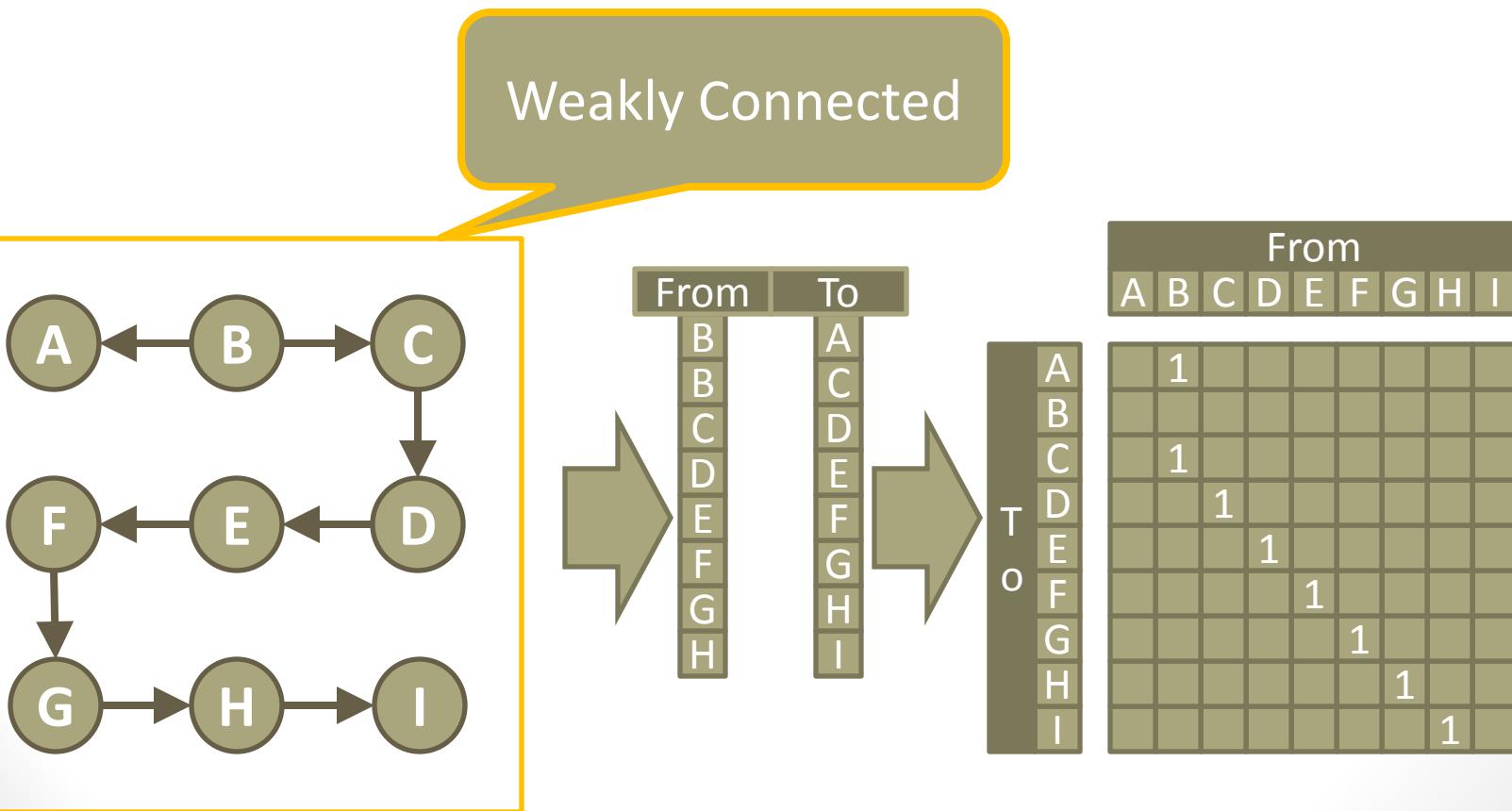
# Graph Data: Connectedness and Density (7)

Weakly Connected

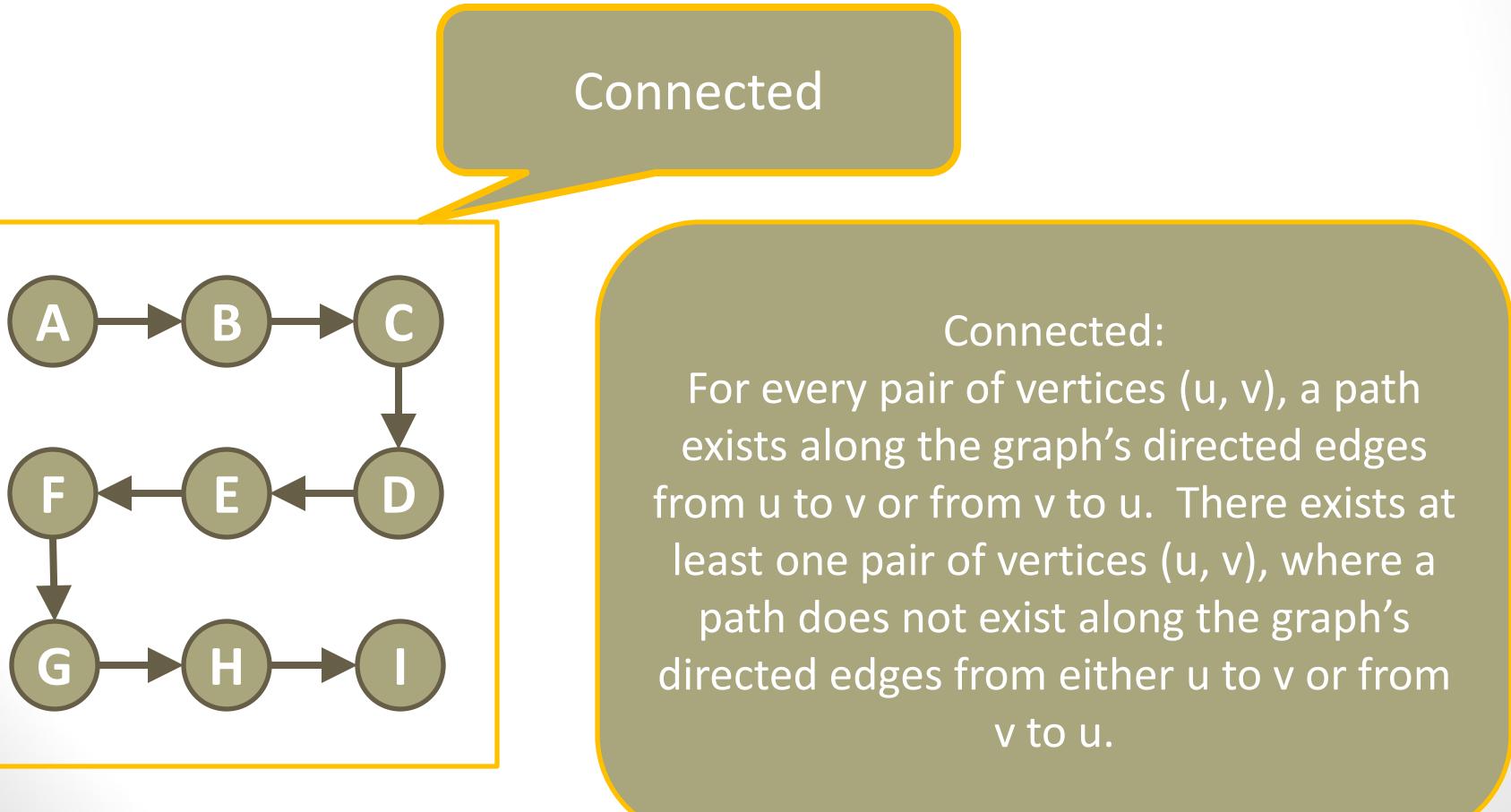


| From | To |
|------|----|
| B    | A  |
| B    | C  |
| C    | D  |
| D    | E  |
| E    | F  |
| F    | G  |
| G    | H  |
| H    | I  |

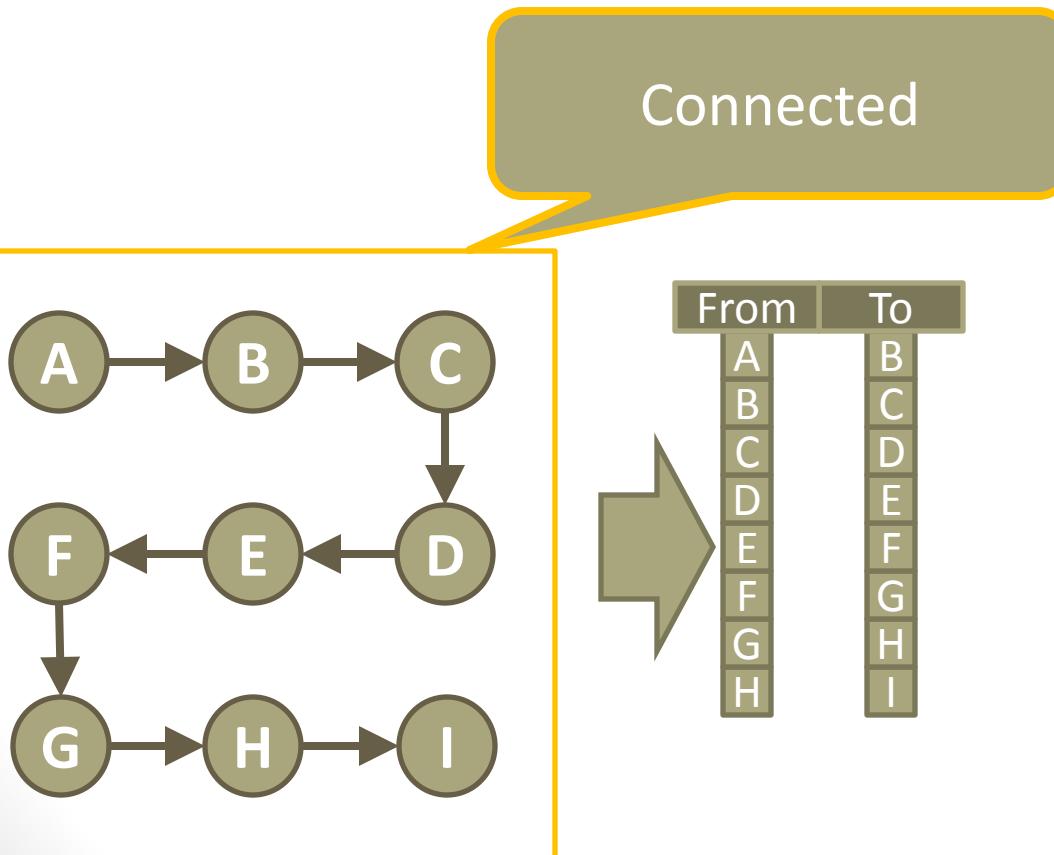
# Graph Data: Connectedness and Density (8)



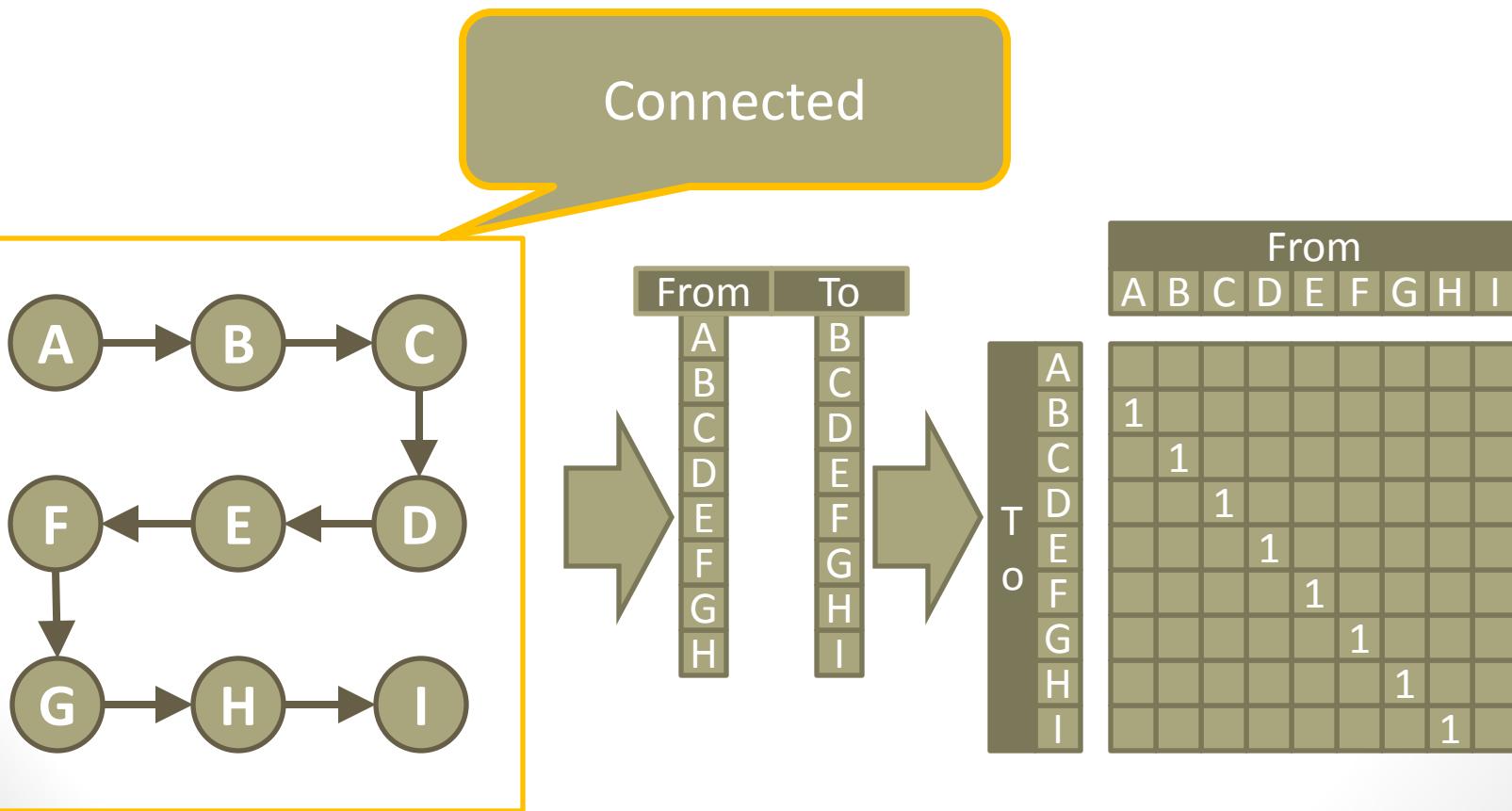
# Graph Data: Connectedness and Density (9)



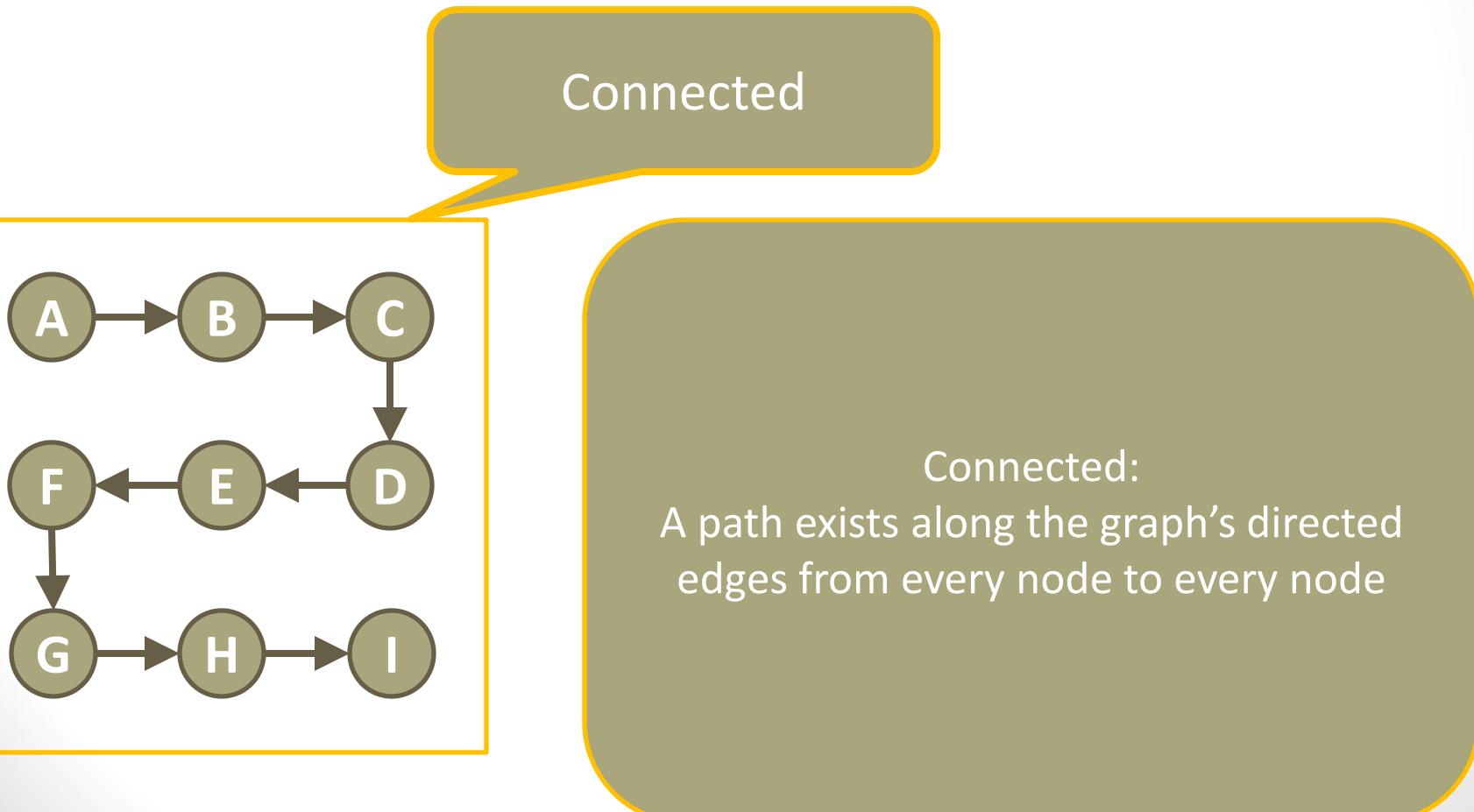
# Graph Data: Connectedness and Density (10)



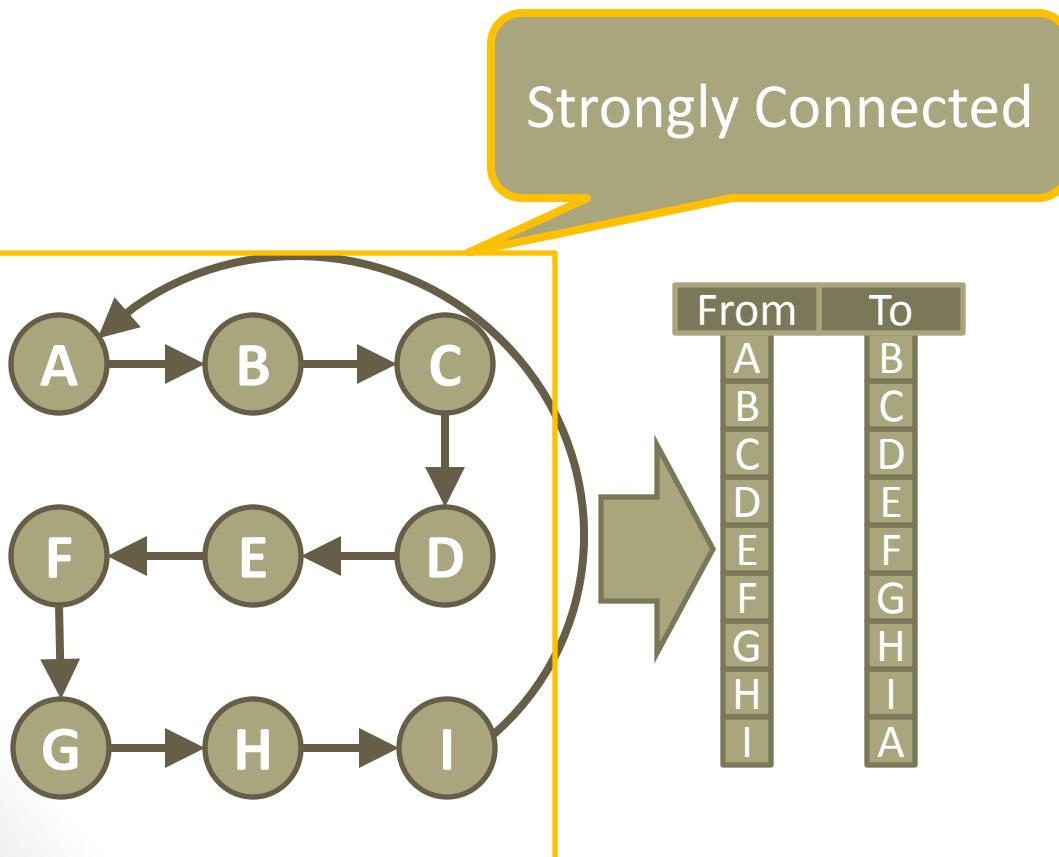
# Graph Data: Connectedness and Density (11)



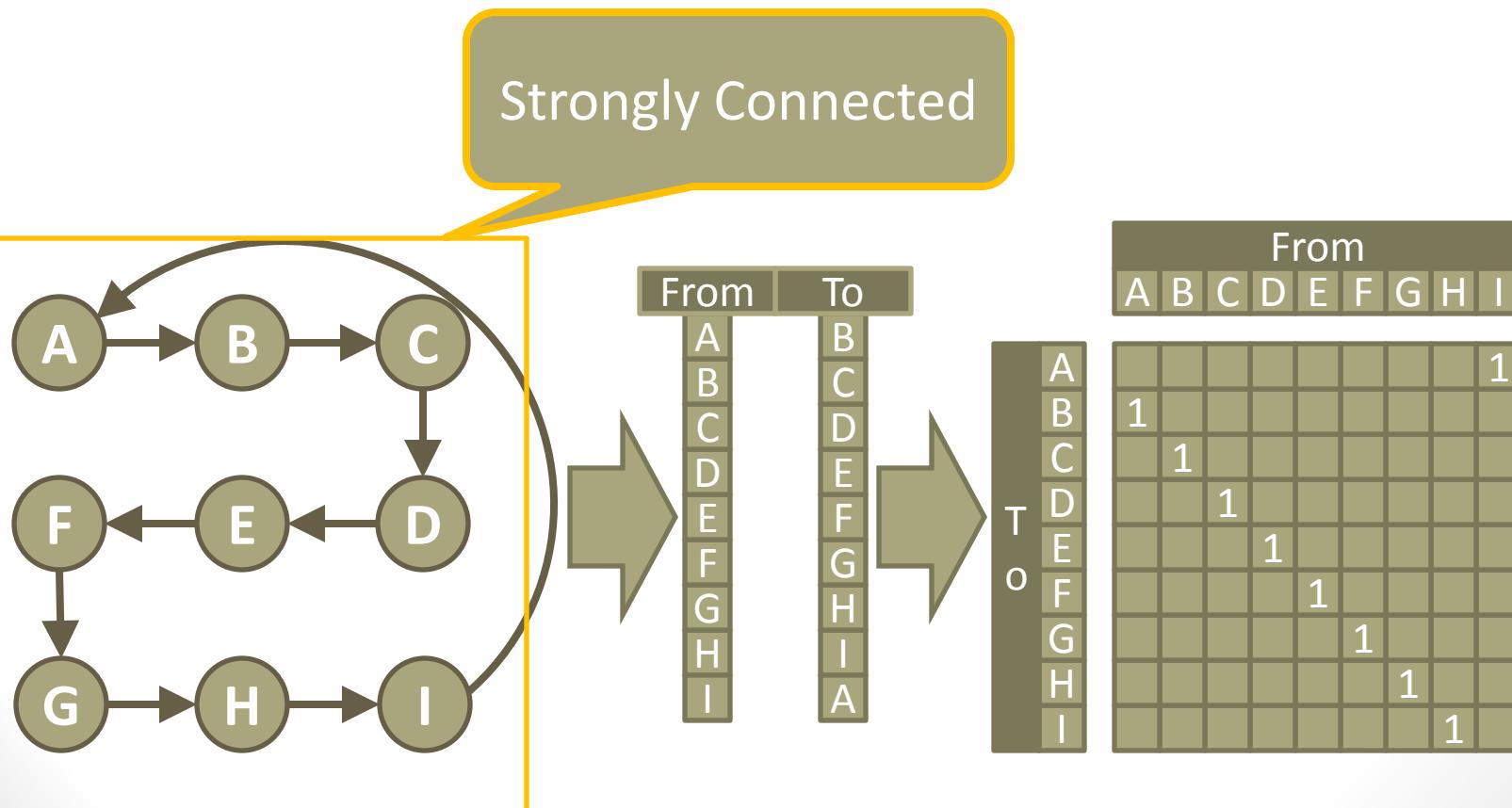
# Graph Data: Connectedness and Density (12)



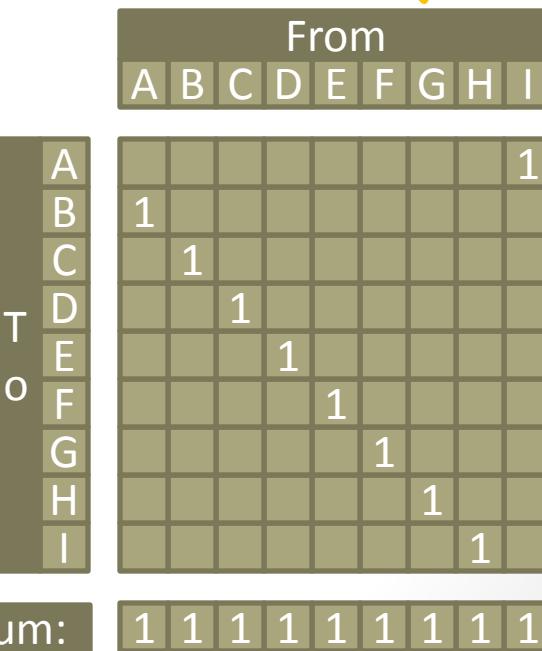
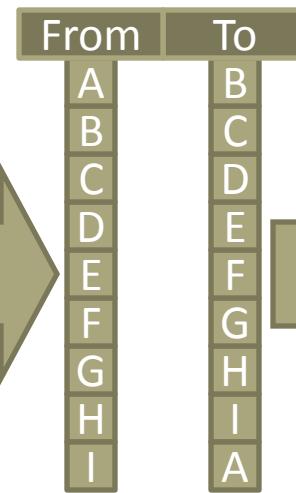
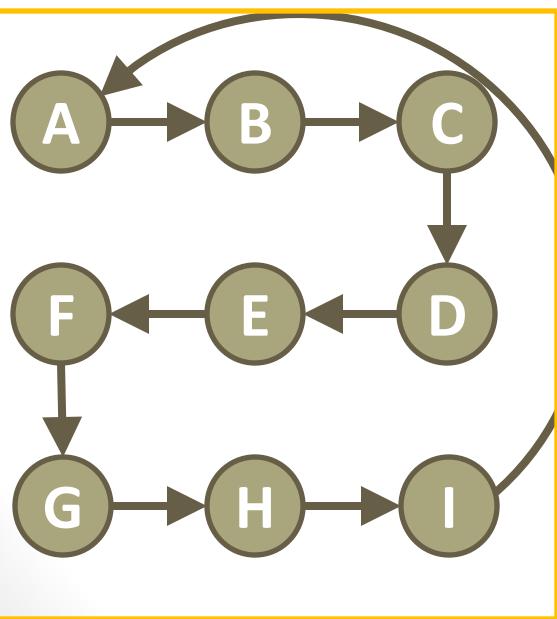
# Graph Data: Connectedness and Density (13)



# Graph Data: Connectedness and Density (14)



# Graph Data: Connectedness and Density (15)

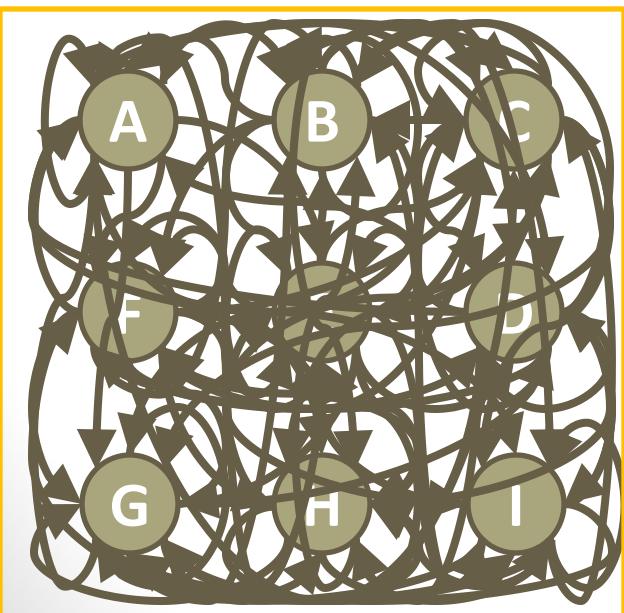


Sparse: Mean row or column sum is close to 1

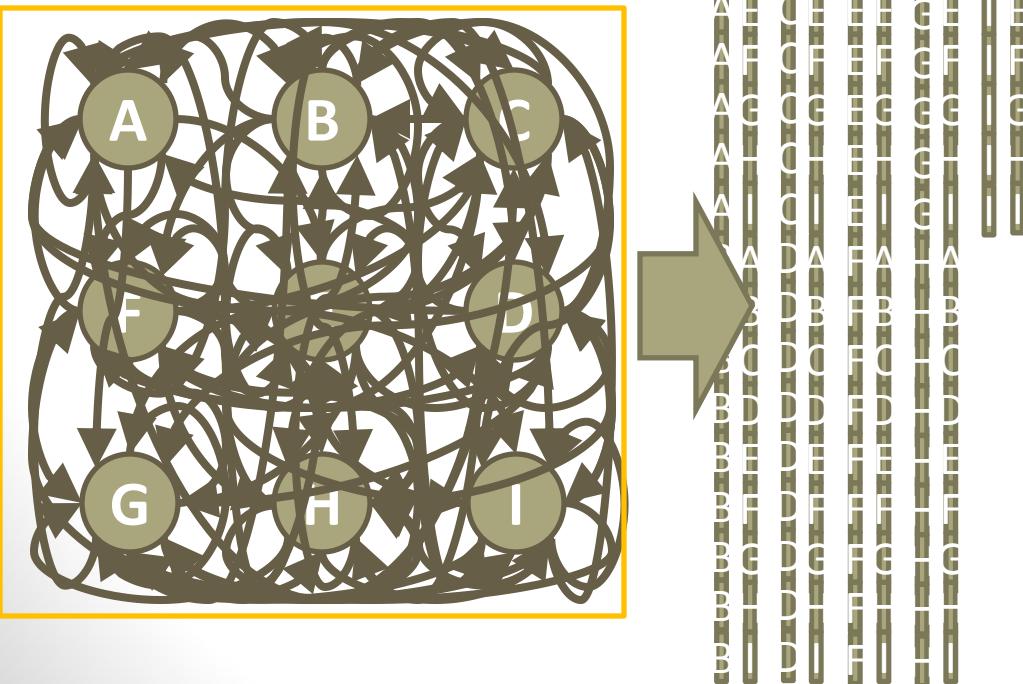
sum:

1  
1  
1  
1  
1  
1  
1  
1  
1

# Graph Data: Connectedness and Density (16)



# Graph Data: Connectedness and Density (17)



# Graph Data: Connectedness and Density (18)

| From | To |
|------|----|
| A    | A  |
| A    | B  |
| A    | C  |
| A    | D  |
| A    | E  |
| A    | F  |
| A    | G  |
| A    | H  |
| A    | I  |
| B    | A  |
| B    | B  |
| B    | C  |
| B    | D  |
| B    | E  |
| B    | F  |
| B    | G  |
| B    | H  |
| B    | I  |

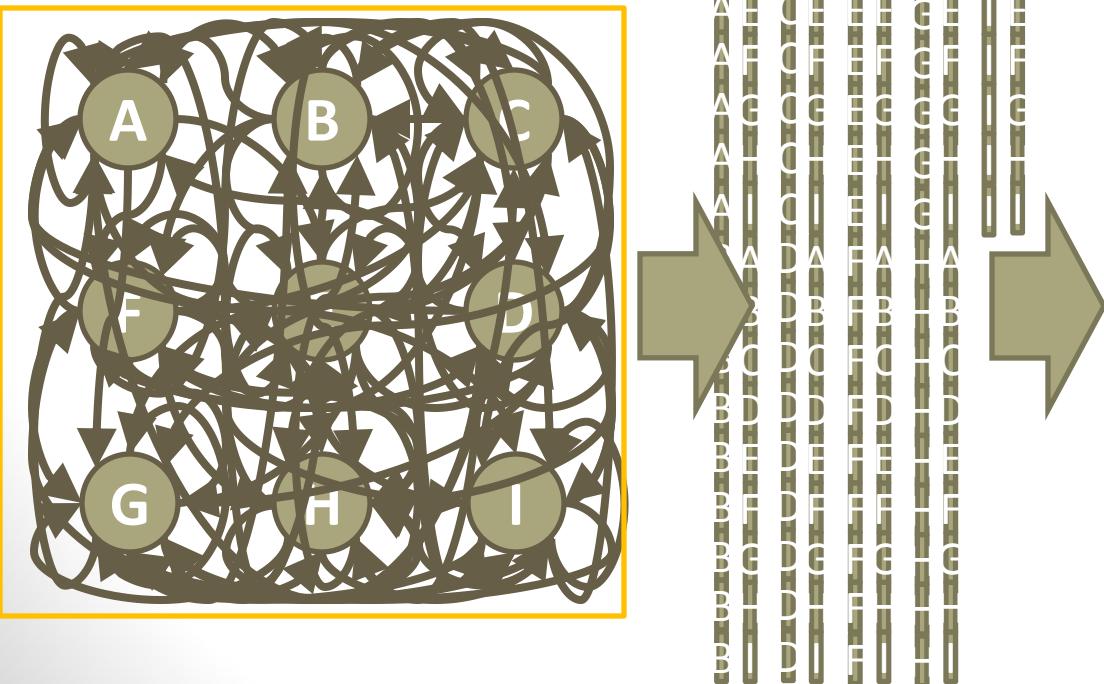
| From | To |
|------|----|
| C    | C  |
| C    | C  |
| C    | C  |
| C    | C  |
| C    | C  |
| C    | C  |
| C    | C  |
| C    | C  |
| C    | C  |
| D    | D  |
| D    | D  |
| D    | D  |
| D    | D  |
| D    | D  |
| D    | D  |
| D    | D  |
| D    | D  |
| D    | D  |
| E    | E  |
| E    | E  |
| E    | E  |
| E    | E  |
| E    | E  |
| E    | E  |
| E    | E  |
| E    | E  |
| E    | E  |
| F    | F  |
| F    | F  |
| F    | F  |
| F    | F  |
| F    | F  |
| F    | F  |
| F    | F  |
| F    | F  |
| F    | F  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |

| From | To |
|------|----|
| E    | E  |
| E    | E  |
| E    | E  |
| E    | E  |
| E    | E  |
| E    | E  |
| E    | E  |
| E    | E  |
| E    | E  |
| F    | F  |
| F    | F  |
| F    | F  |
| F    | F  |
| F    | F  |
| F    | F  |
| F    | F  |
| F    | F  |
| F    | F  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |

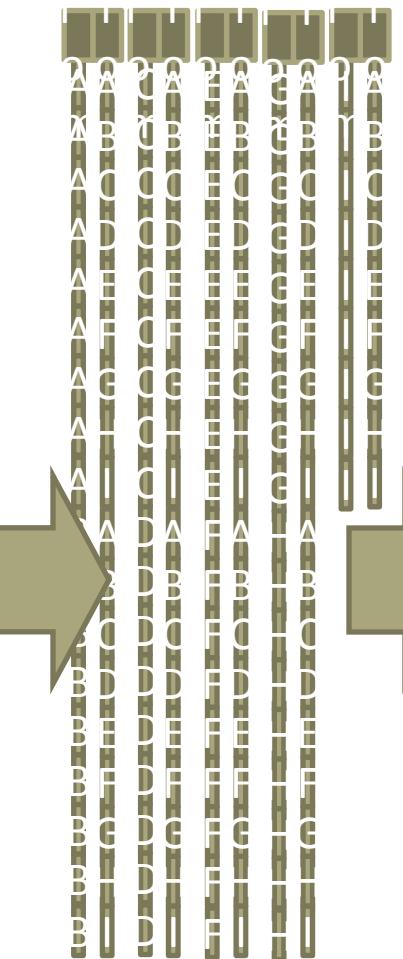
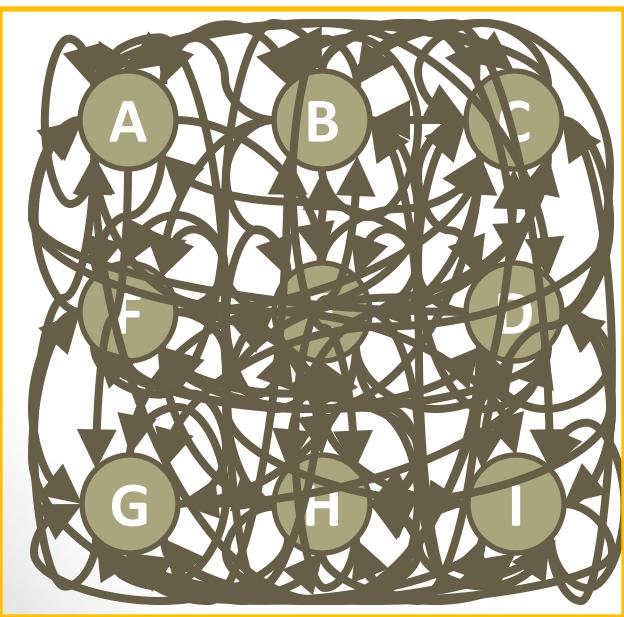
| From | To |
|------|----|
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| G    | G  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| H    | H  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |

| From | To |
|------|----|
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| I    | I  |
| A    | B  |
| A    | C  |
| A    | D  |
| A    | E  |
| A    | F  |
| A    | G  |
| A    | H  |
| A    | I  |
| B    | C  |
| B    | D  |
| B    | E  |
| B    | F  |
| B    | G  |
| B    | H  |
| B    | I  |
| C    | D  |
| C    | E  |
| C    | F  |
| C    | G  |
| C    | H  |
| C    | I  |
| D    | E  |
| D    | F  |
| D    | G  |
| D    | H  |
| D    | I  |
| E    | F  |
| E    | G  |
| E    | H  |
| E    | I  |
| F    | G  |
| F    | H  |
| F    | I  |
| G    | H  |
| G    | I  |
| H    | I  |

# Graph Data: Connectedness and Density (19)

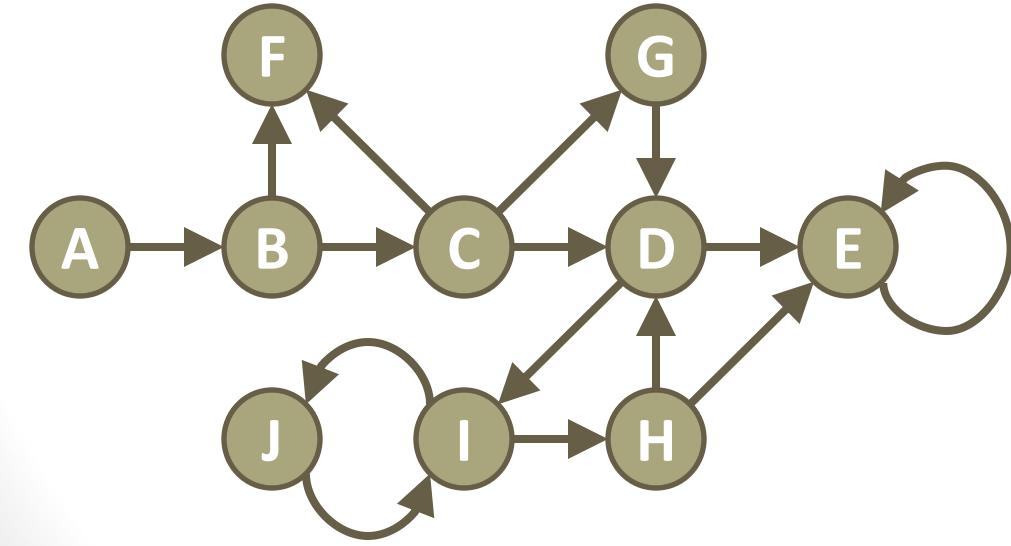


# Graph Data: Connectedness and Density (20)

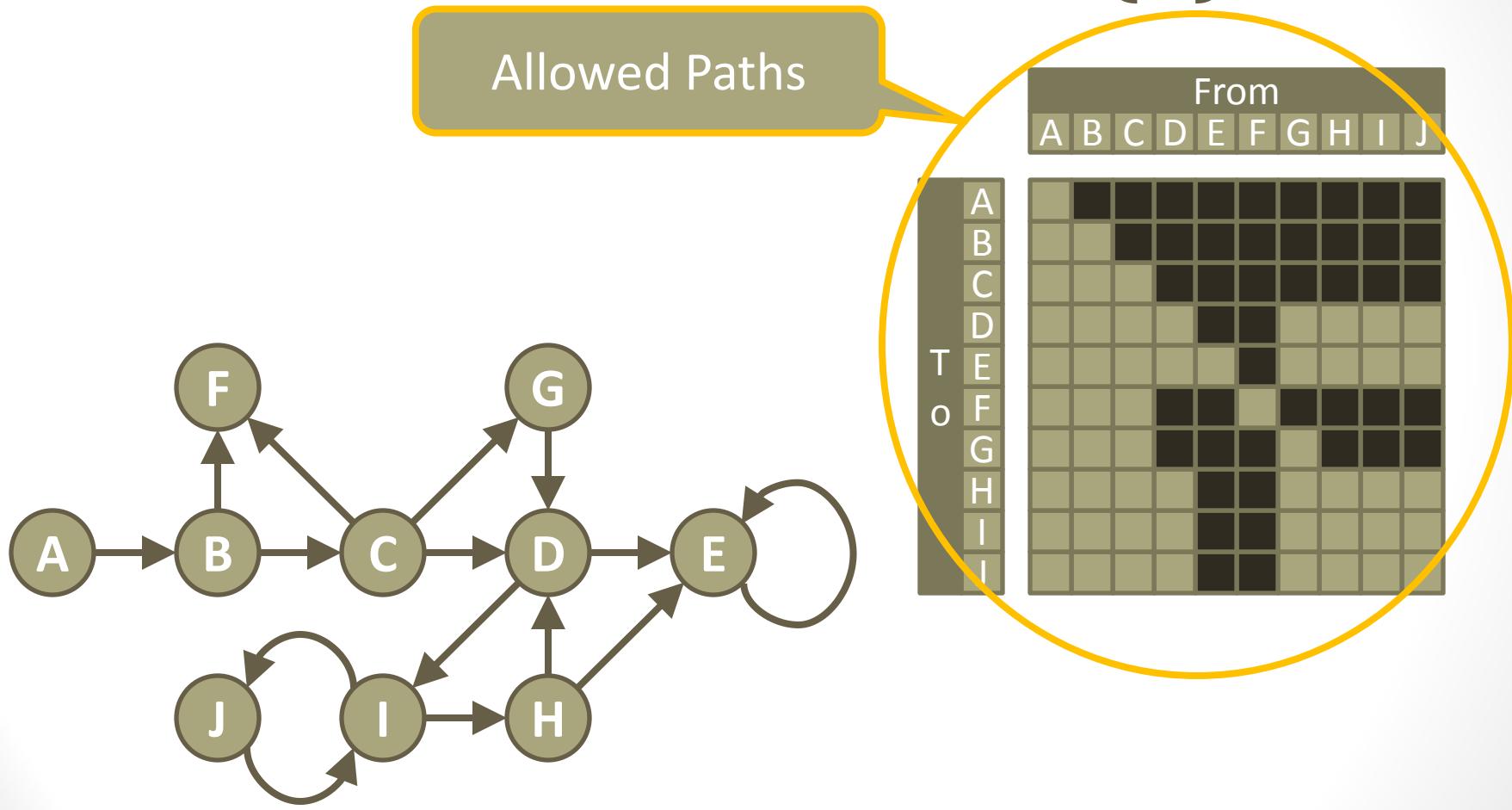


Dense: Mean row or column sum is close to number of nodes

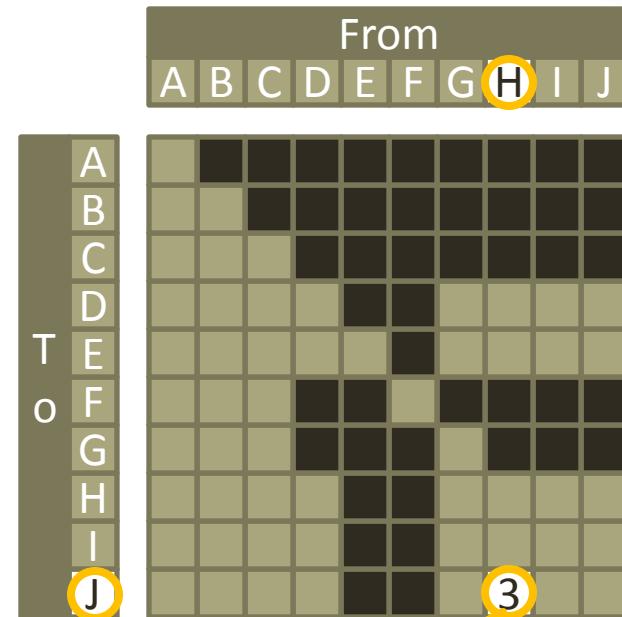
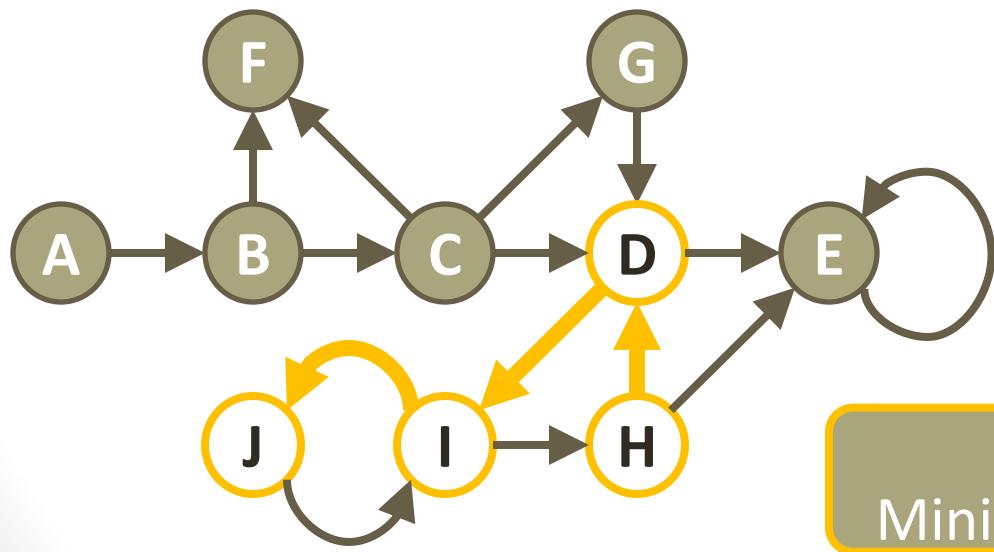
# Graph Data: Allowed Paths, Distance, and Diameter (0)



# Graph Data: Allowed Paths, Distance, and Diameter (1)



# Graph Data: Allowed Paths, Distance, and Diameter (2)

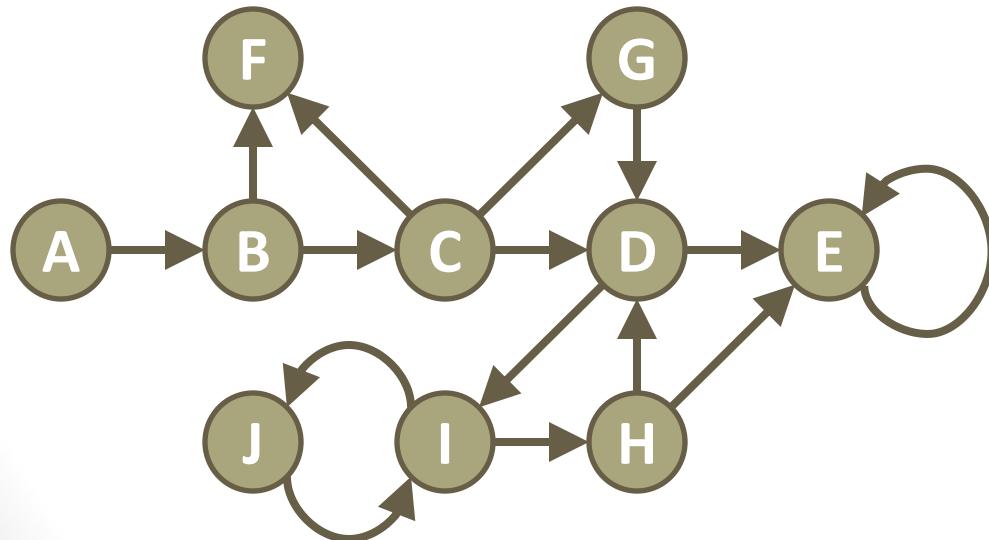


Path Distance:  
Minimum Distance from H to J

# Graph Data: Allowed Paths, Distance, and Diameter (3)

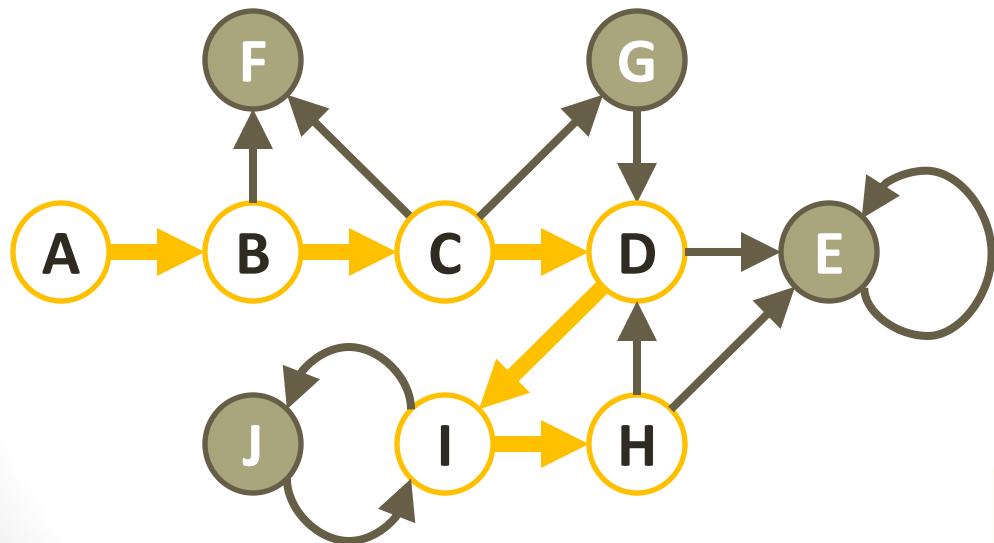
Distance Matrix:

Minimum distance between any two vertices along a directed edge



|    |   | From |   |   |   |   |   |   |   |   |   |
|----|---|------|---|---|---|---|---|---|---|---|---|
|    |   | A    | B | C | D | E | F | G | H | I | J |
| To | A | 0    |   |   |   |   |   |   |   |   |   |
|    | B | 1    | 0 |   |   |   |   |   |   |   |   |
|    | C | 2    | 1 | 0 |   |   |   |   |   |   |   |
|    | D | 3    | 2 | 1 | 0 |   |   |   | 1 | 1 | 2 |
|    | E | 4    | 3 | 2 | 1 | 0 |   |   | 2 | 1 | 2 |
|    | F | 2    | 1 | 1 |   |   | 0 |   |   |   |   |
|    | G | 4    | 2 | 1 |   |   |   | 0 |   |   |   |
|    | H | 5    | 4 | 3 | 2 |   |   |   | 3 | 0 | 1 |
|    | I | 4    | 3 | 2 | 1 |   |   |   | 2 | 2 | 0 |
|    | J | 5    | 4 | 3 | 2 |   |   |   | 3 | 3 | 1 |

# Graph Data: Allowed Paths, Distance, and Diameter (4)

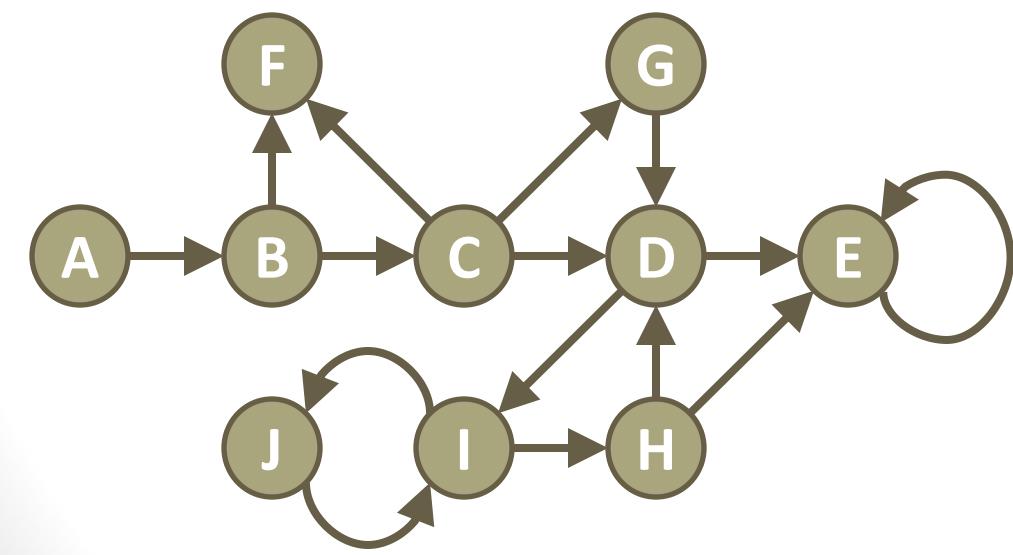


| From |   |   |   |   |   |   |   |   |   |
|------|---|---|---|---|---|---|---|---|---|
| A    | B | C | D | E | F | G | H | I | J |
| A    | 0 |   |   |   |   |   |   |   |   |
| B    | 1 | 0 |   |   |   |   |   |   |   |
| C    | 2 | 1 | 0 |   |   |   |   |   |   |
| D    | 3 | 2 | 1 | 0 |   |   |   | 1 | 1 |
| E    | 4 | 3 | 2 | 1 | 0 |   |   | 2 | 1 |
| F    | 2 | 1 | 1 |   | 0 |   |   | 2 | 3 |
| G    | 4 | 2 | 1 |   |   | 0 |   |   |   |
| H    | 4 | 3 | 2 | 2 |   | 3 | 0 | 1 | 2 |
| I    | 4 | 3 | 2 | 1 |   | 2 | 2 | 0 | 1 |
| J    | 4 | 3 | 2 | 2 |   | 3 | 3 | 1 | 0 |

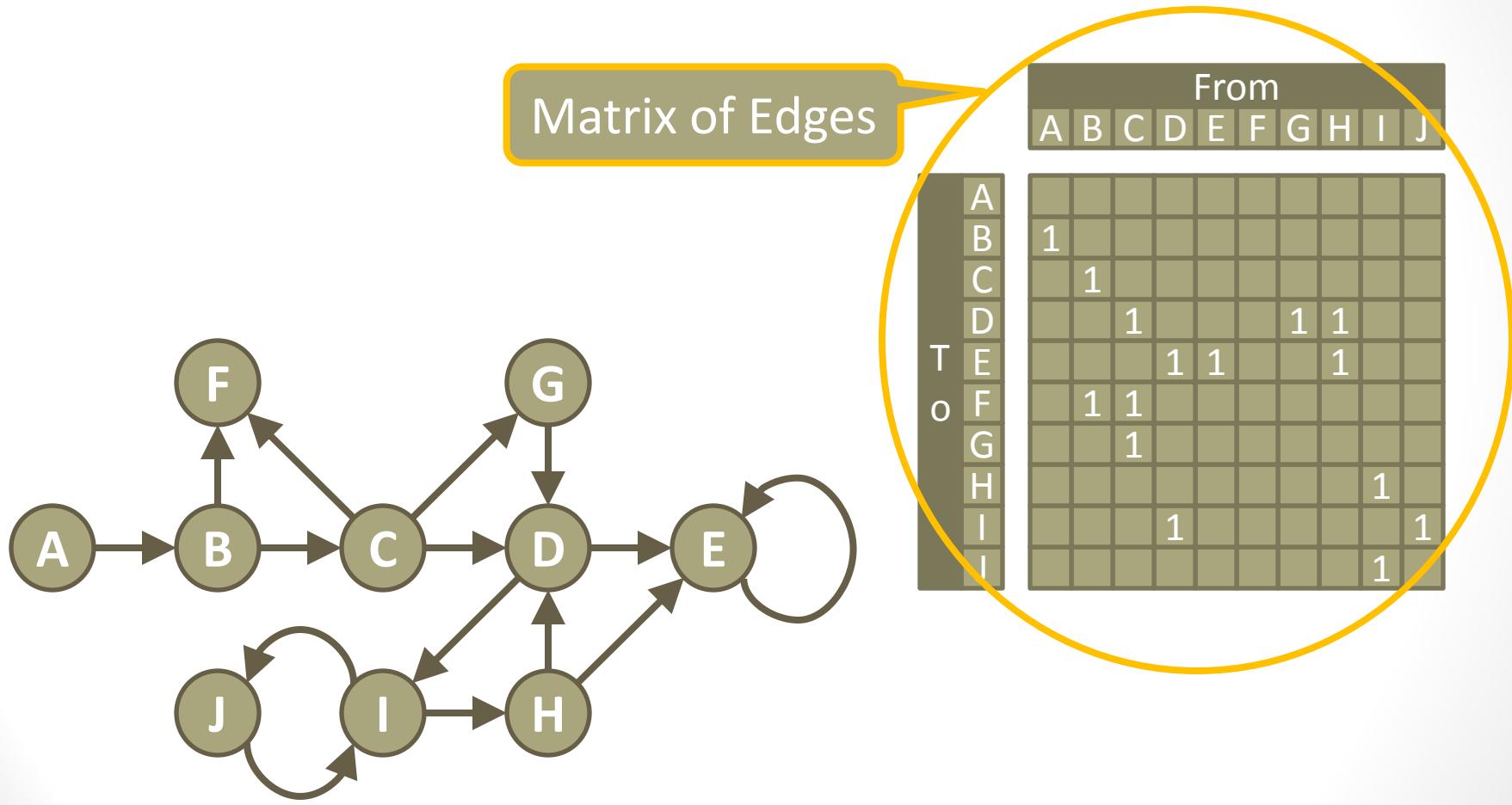
Diameter:  
Max Path Distance

(100)

# Graph Data: Order and Size (0)

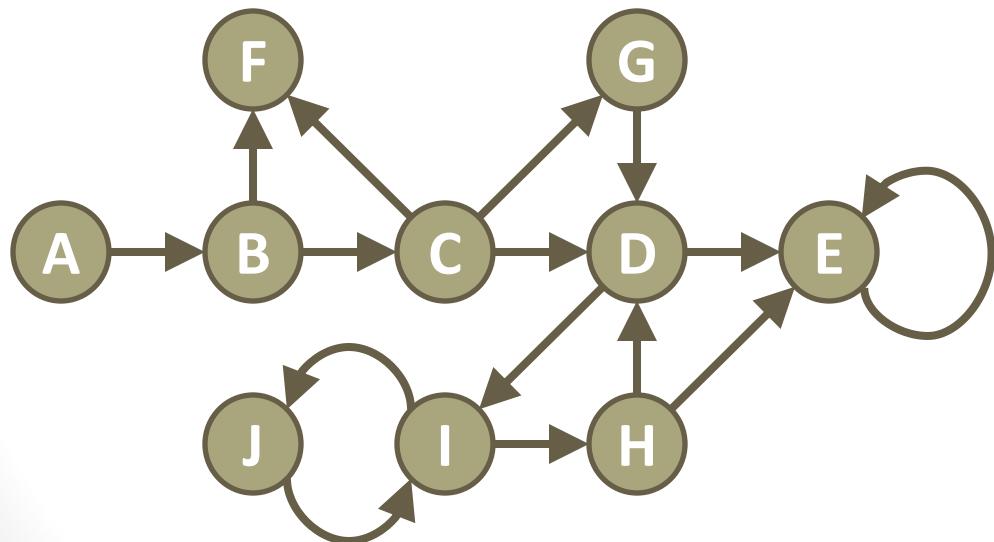


# Graph Data: Order and Size (1)



# Graph Data: Order and Size (2)

Order of Graph: 10

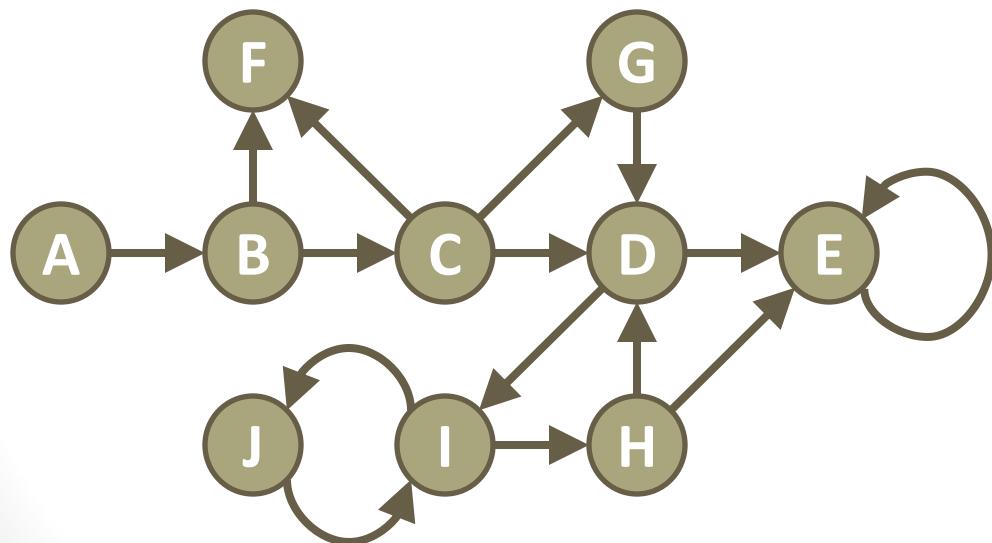


| From |   |   |   |   |   |   |   |   |   |
|------|---|---|---|---|---|---|---|---|---|
| A    | B | C | D | E | F | G | H | I | J |
| T    | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| C    |   | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| O    |   |   | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| R    |   |   |   | 1 | 1 | 1 | 1 | 1 | 1 |
| E    |   |   |   |   | 1 | 1 | 1 | 1 | 1 |
| N    |   |   |   |   |   | 1 | 1 | 1 | 1 |
| S    |   |   |   |   |   |   | 1 | 1 | 1 |
| P    |   |   |   |   |   |   |   | 1 | 1 |
| L    |   |   |   |   |   |   |   |   | 1 |

Order of Graph:  
Number of Nodes

# Graph Data: Order and Size (3)

Order of Graph: 10  
Size of Graph: 15



| From |   |   |   |   |   |   |   |   |   |
|------|---|---|---|---|---|---|---|---|---|
| A    | B | C | D | E | F | G | H | I | J |
| T    | O |   |   |   |   |   |   |   |   |
| 1    |   |   |   |   |   |   |   |   |   |
|      | 1 |   |   |   |   |   |   |   |   |
|      |   | 1 |   |   |   |   |   |   |   |
|      |   |   | 1 |   |   |   |   |   |   |
|      |   |   |   | 1 |   |   |   |   |   |
|      |   |   |   |   | 1 |   |   |   |   |
|      |   |   |   |   |   | 1 |   |   |   |
|      |   |   |   |   |   |   | 1 |   |   |
|      |   |   |   |   |   |   |   | 1 |   |
|      |   |   |   |   |   |   |   |   | 1 |

Size of Graph:  
Number of Edges

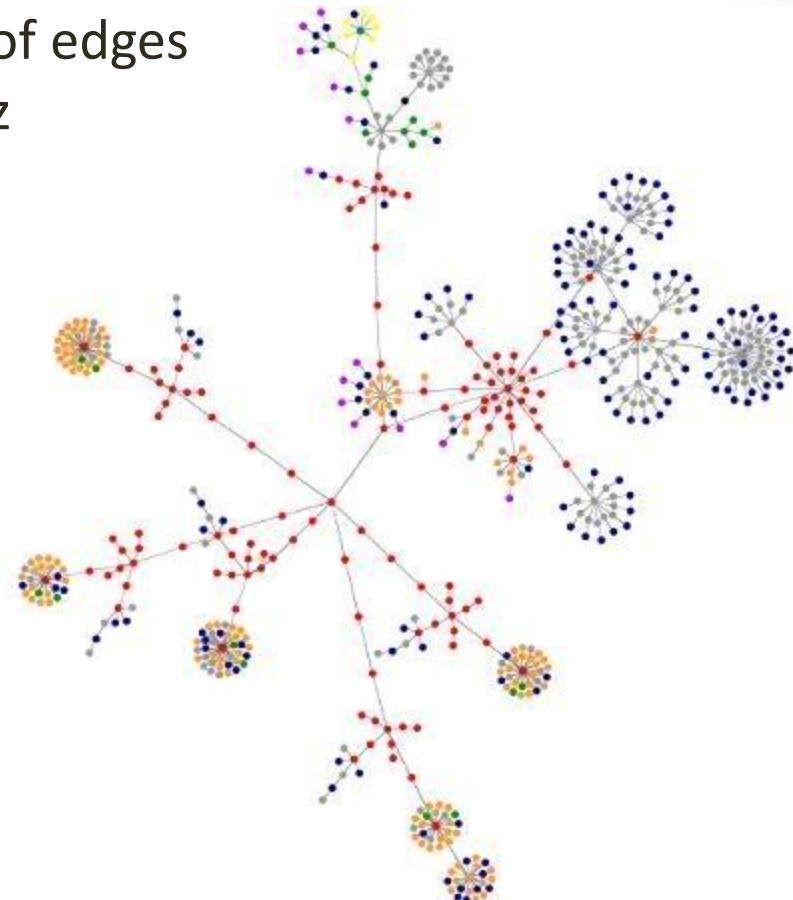
(104)

# Graph Data: Links (0)

- Graphs In General:
  - [http://en.wikipedia.org/wiki/Graph\\_theory](http://en.wikipedia.org/wiki/Graph_theory)
  - [https://en.wikipedia.org/wiki/Graph\\_\(discrete\\_mathematics\)](https://en.wikipedia.org/wiki/Graph_(discrete_mathematics))
  - [https://en.wikipedia.org/wiki/Graph\\_\(abstract\\_data\\_type\)](https://en.wikipedia.org/wiki/Graph_(abstract_data_type))
  - [https://en.wikipedia.org/wiki/List\\_of\\_graph\\_theory\\_topics](https://en.wikipedia.org/wiki/List_of_graph_theory_topics)
- Graph Diameter
  - <http://people.hofstra.edu/geotrans/eng/methods/diameter1.html>
- Distance
  - [http://en.wikipedia.org/wiki/Distance\\_\(graph\\_theory\)](http://en.wikipedia.org/wiki/Distance_(graph_theory))
- Resistance
  - [http://en.wikipedia.org/wiki/Resistance\\_distance](http://en.wikipedia.org/wiki/Resistance_distance)
- Centrality
  - [http://en.wikipedia.org/wiki/Betweenness#Betweenness\\_centrality](http://en.wikipedia.org/wiki/Betweenness#Betweenness_centrality)
- Connectivity
  - [http://en.wikipedia.org/wiki/Connectivity\\_\(graph\\_theory\)](http://en.wikipedia.org/wiki/Connectivity_(graph_theory))
- Hypergraph: One edge can connect many nodes
  - <http://en.wikipedia.org/wiki/Hypergraph>
- Degree Distribution: Histogram of in-degrees, out-degrees, in-degrees normalized by out-degrees
- Popularity (Google Matrix)
- Density: #edges/(#nodes<sup>2</sup>-#nodes)
- Clustering Coefficient
  - [http://en.wikipedia.org/wiki/Clustering\\_coefficient](http://en.wikipedia.org/wiki/Clustering_coefficient)

# Quiz Graph Data (Measures)

- The presented slide contains a list of edges that describes the graph in the quiz



# Introduction to Graph Data

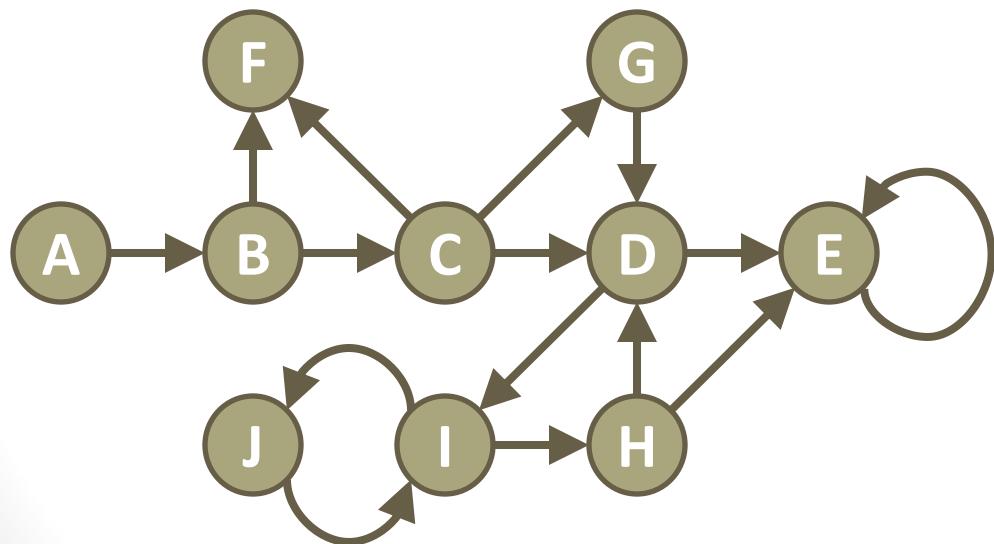
(108)

# Graph Data: Google Matrix

# Google Matrix

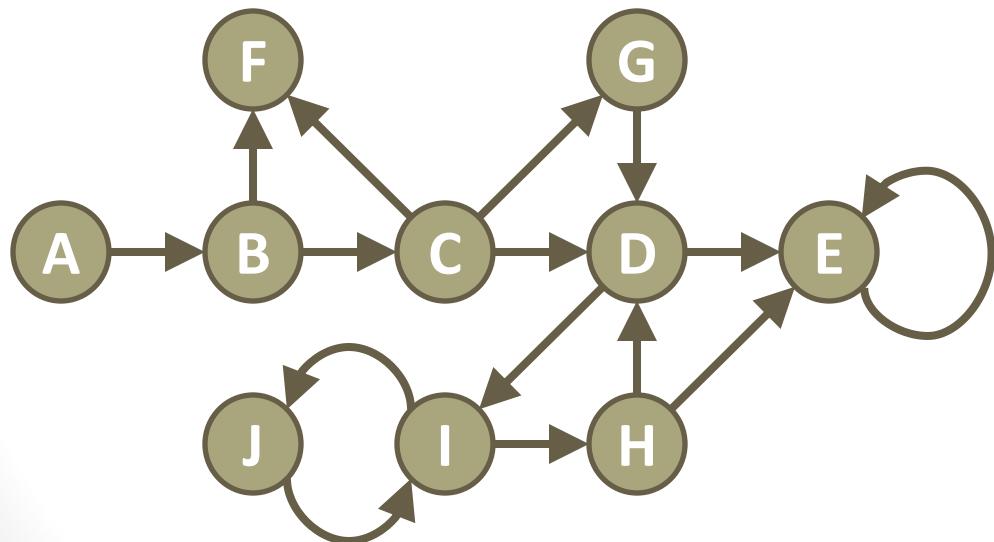
- [http://en.wikipedia.org/wiki/Google\\_matrix](http://en.wikipedia.org/wiki/Google_matrix)

# Graph Data: Popularity (0)



# Graph Data: Popularity (1)

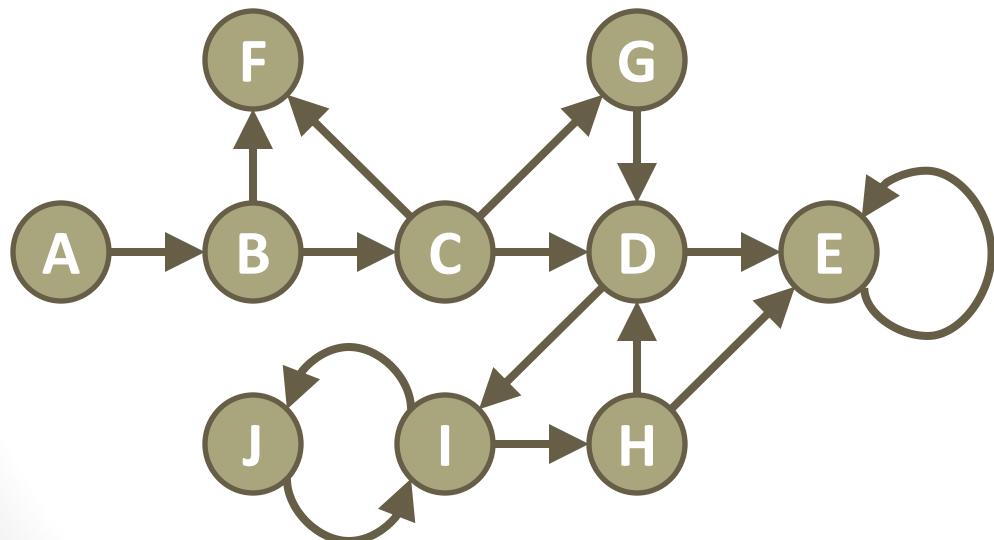
# In-degree of a node: Popularity



| From |   |   |   |   |   |   |   |   |   |   | Sum: |
|------|---|---|---|---|---|---|---|---|---|---|------|
| A    | B | C | D | E | F | G | H | I | J |   |      |
| A    |   |   |   |   |   |   |   |   |   | 0 |      |
| B    | 1 |   |   |   |   |   |   |   |   | 1 |      |
| C    |   | 1 |   |   |   |   |   |   |   | 1 |      |
| D    |   |   | 1 |   |   |   |   | 1 | 1 | 3 |      |
| E    |   |   |   | 1 | 1 |   |   |   | 1 | 3 |      |
| T    |   |   |   |   |   | 1 | 1 |   |   | 2 |      |
| O    |   |   |   | 1 | 1 |   |   |   |   | 1 |      |
| F    |   |   |   |   | 1 |   |   |   |   | 1 |      |
| G    |   |   |   |   |   |   |   |   |   | 1 |      |
| H    |   |   |   |   |   |   |   | 1 |   | 1 |      |
| I    |   |   |   |   |   |   | 1 |   |   | 2 |      |
| J    |   |   |   |   |   |   |   |   | 1 | 1 |      |

# Graph Data: Popularity (2)

In-degree of a node: Popularity



| From                |   |   |   |   |   |   |   |   |   | Sum: |  |
|---------------------|---|---|---|---|---|---|---|---|---|------|--|
| A                   | B | C | D | E | F | G | H | I | J |      |  |
| To                  | 1 |   |   |   |   |   |   |   |   | 0    |  |
|                     |   | 1 |   |   |   |   |   |   |   | 1    |  |
|                     |   |   | 1 |   |   |   |   |   |   | 1    |  |
|                     |   |   |   | 1 |   |   |   |   |   | 3    |  |
|                     |   |   |   |   | 1 |   |   |   |   | 3    |  |
|                     |   |   |   |   |   | 1 |   |   |   | 2    |  |
|                     |   |   |   |   |   |   | 1 |   |   | 1    |  |
|                     |   |   |   |   |   |   |   | 1 |   | 1    |  |
|                     |   |   |   |   |   |   |   |   | 1 | 2    |  |
|                     |   |   |   |   |   |   |   |   |   | 1    |  |
| Sum:                |   |   |   |   |   |   |   |   |   | Sum: |  |
| 1 2 3 2 1 0 1 2 2 1 |   |   |   |   |   |   |   |   |   | Sum: |  |

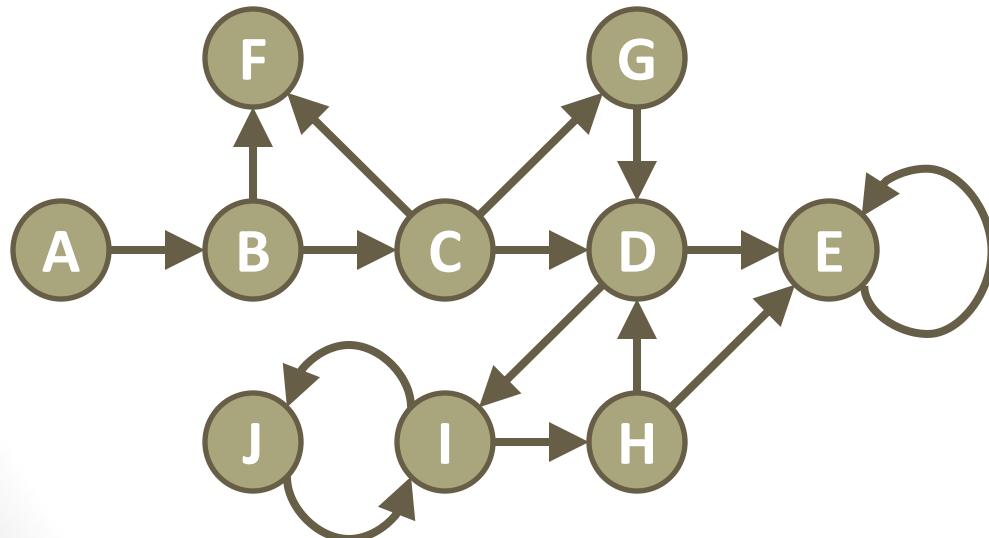
Out-degree of a node:  
Gregariousness

# Quiz Graph Data (Popularity)

- Graph Data (Popularity)
- You need to view the projected slide to answer the questions

# Graph Data: Popularity (3)

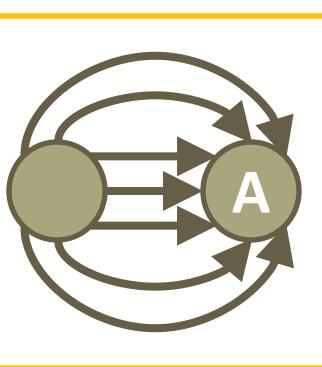
But, not every link is equally important.  
Otherwise, you could create a website with  
a thousand links that all point to your site.



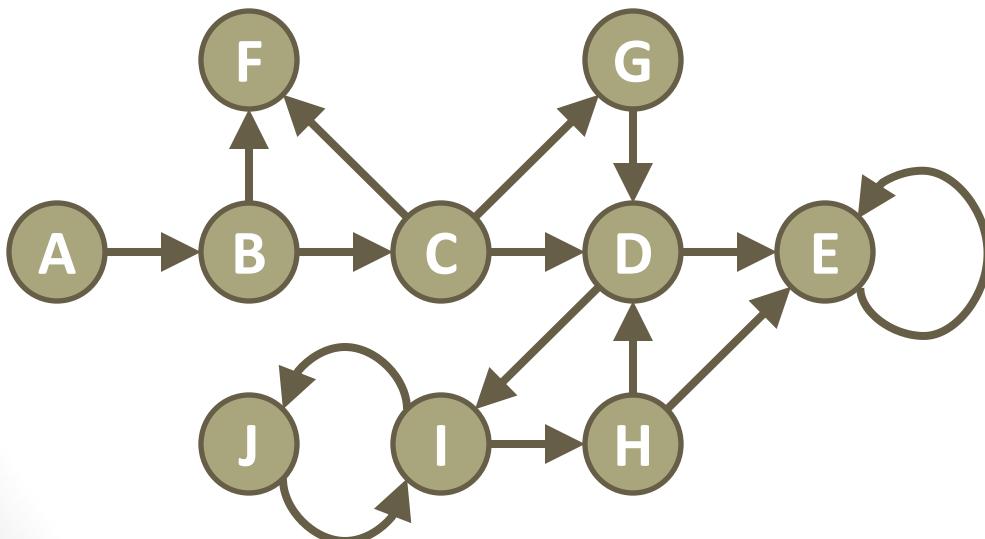
| From |   |   |   |   |   |   |   |   |   | Sum: |
|------|---|---|---|---|---|---|---|---|---|------|
| A    | B | C | D | E | F | G | H | I | J |      |
| To   | 1 |   |   |   |   |   |   |   |   | 0    |
|      |   | 1 |   |   |   |   |   |   |   | 1    |
|      |   |   | 1 |   |   |   |   |   |   | 1    |
|      |   |   |   | 1 |   |   |   |   |   | 3    |
|      |   |   |   |   | 1 |   |   |   |   | 3    |
|      |   |   |   |   |   | 1 |   |   |   | 2    |
|      |   |   |   |   |   |   | 1 |   |   | 1    |
|      |   |   |   |   |   |   |   | 1 |   | 1    |
|      |   |   |   |   |   |   |   |   | 1 | 2    |
|      |   |   |   |   |   |   |   |   |   | 1    |

Sum: 1 2 3 2 1 0 1 2 2 1

# Graph Data: Popularity (4)

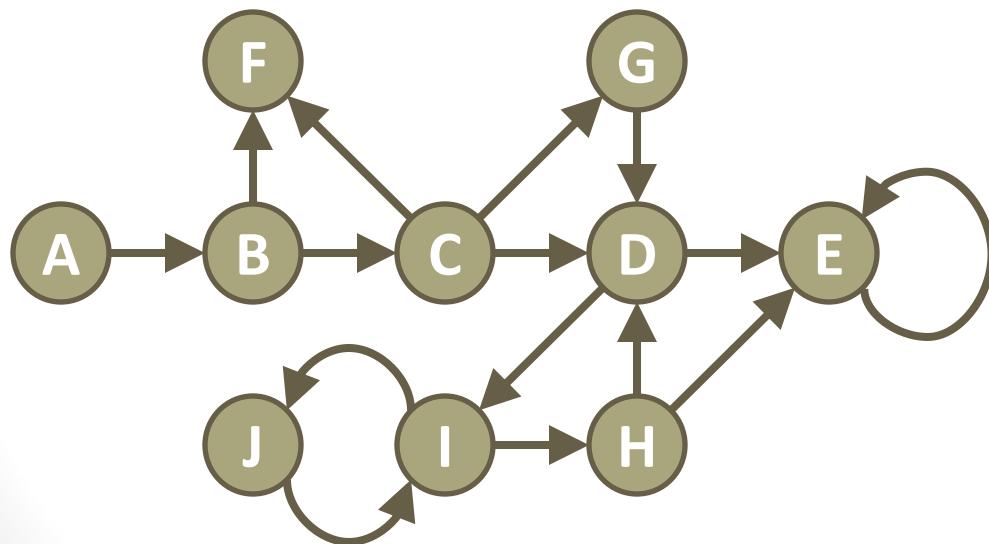


One very gregarious node  
could make another node  
very popular



|      |   | From |   |   |   |   |   |   |   |   |   | Sum: |
|------|---|------|---|---|---|---|---|---|---|---|---|------|
|      |   | A    | B | C | D | E | F | G | H | I | J |      |
| To   | A |      |   |   |   |   |   |   |   |   |   | 0    |
|      | B | 1    |   |   |   |   |   |   |   |   |   | 1    |
|      | C |      | 1 |   |   |   |   |   |   |   |   | 1    |
|      | D |      |   | 1 |   |   |   |   |   | 1 | 1 | 3    |
|      | E |      |   |   | 1 | 1 |   |   |   |   | 1 | 3    |
|      | F |      |   | 1 | 1 |   |   |   |   |   |   | 2    |
|      | G |      |   |   | 1 |   |   |   |   |   |   | 1    |
|      | H |      |   |   |   |   |   |   |   | 1 |   | 1    |
|      | I |      |   |   |   | 1 |   |   |   |   | 1 | 2    |
|      | J |      |   |   |   |   |   |   |   | 1 |   | 1    |
| Sum: |   | 1    | 2 | 3 | 2 | 1 | 0 | 1 | 2 | 2 | 1 |      |

# Graph Data: Popularity (5)



| From |   |   |   |   |   |   |   |   |   | Sum: |
|------|---|---|---|---|---|---|---|---|---|------|
| A    | B | C | D | E | F | G | H | I | J |      |
| To   | 1 |   |   |   |   |   |   |   |   | 0    |
|      |   | 1 |   |   |   |   |   |   |   | 1    |
|      |   |   | 1 |   |   |   |   |   |   | 1    |
|      |   |   |   | 1 |   |   |   |   |   | 3    |
|      |   |   |   |   | 1 |   |   |   |   | 3    |
|      |   |   |   |   |   | 1 |   |   |   | 2    |
|      |   |   |   |   |   |   | 1 |   |   | 1    |
|      |   |   |   |   |   |   |   | 1 |   | 1    |
|      |   |   |   |   |   |   |   |   | 1 | 2    |
|      |   |   |   |   |   |   |   |   |   | 1    |

Sum: 1 2 3 2 1 0 1 2 2 1

The amount of popularity that a single node can send out needs to be tempered by Gregariousness

# Graph Data: Popularity (6)

This matrix needs some  
adjustments

| From |   |   |   |   |   |   |   |   |   | Sum: |
|------|---|---|---|---|---|---|---|---|---|------|
| A    | B | C | D | E | F | G | H | I | J |      |
| To   | 1 |   |   |   |   |   |   |   |   | 0    |
|      |   | 1 |   |   |   |   |   |   |   | 1    |
|      |   |   | 1 |   |   |   |   |   |   | 1    |
|      |   |   |   | 1 |   |   |   |   |   | 3    |
|      |   |   |   |   | 1 | 1 |   |   |   | 3    |
|      |   |   |   |   |   | 1 | 1 |   |   | 2    |
|      |   |   |   |   |   |   | 1 |   |   | 1    |
|      |   |   |   |   |   |   |   | 1 |   | 2    |
|      |   |   |   |   |   |   |   |   | 1 | 1    |
|      |   |   |   |   |   |   |   |   |   | 1    |

Sum: 1 2 3 2 1 0 1 2 2 1

# Graph Data: Popularity (7)

|      | From |   |   |   |   |   |   |   |   |   |   |
|------|------|---|---|---|---|---|---|---|---|---|---|
|      | A    | B | C | D | E | F | G | H | I | J |   |
| A    |      |   |   |   |   |   |   |   |   |   | 0 |
| B    | 1    |   |   |   |   |   |   |   |   |   | 1 |
| C    |      | 1 |   |   |   |   |   |   |   |   | 1 |
| D    |      |   | 1 |   |   |   |   | 1 | 1 |   | 3 |
| E    |      |   |   | 1 | 1 |   |   |   | 1 |   | 3 |
| F    |      | 1 | 1 |   |   |   |   |   |   |   | 2 |
| G    |      |   | 1 |   |   |   |   |   |   |   | 1 |
| H    |      |   |   | 1 |   |   |   |   | 1 |   | 1 |
| I    |      |   |   |   | 1 |   |   |   |   | 1 | 2 |
| J    |      |   |   |   |   |   |   | 1 |   |   | 1 |
| sum: | 1    | 2 | 3 | 2 | 1 | 0 | 1 | 2 | 2 | 1 |   |

# Graph Data: Popularity (8)

|      | From |     |     |     |     |   |   |   |     |     |        |
|------|------|-----|-----|-----|-----|---|---|---|-----|-----|--------|
|      | A    | B   | C   | D   | E   | F | G | H | I   | J   |        |
| A    |      |     |     |     |     |   |   |   |     |     | sum: 0 |
| B    | 1    |     |     |     |     |   |   |   |     |     | 1.00   |
| C    |      | 1/2 |     |     |     |   |   |   |     |     | 0.50   |
| D    |      |     | 1/3 |     |     |   |   | 1 | 1/2 |     | 1.83   |
| E    |      |     |     | 1/2 | 1   |   |   |   | 1/2 |     | 2.00   |
| F    |      | 1/2 | 1/3 |     |     |   |   |   |     |     | 0.83   |
| G    |      |     | 1/3 |     |     |   |   |   |     |     | 0.33   |
| H    |      |     |     | 1/2 |     |   |   |   |     | 1/2 | 0.50   |
| I    |      |     |     |     | 1/2 |   |   |   |     |     | 1.50   |
| J    |      |     |     |     |     |   |   |   | 1/2 |     | 0.50   |
| sum: | 1    | 1   | 1   | 1   | 1   | 0 | 1 | 1 | 1   | 1   |        |

# Graph Data: Popularity (9)

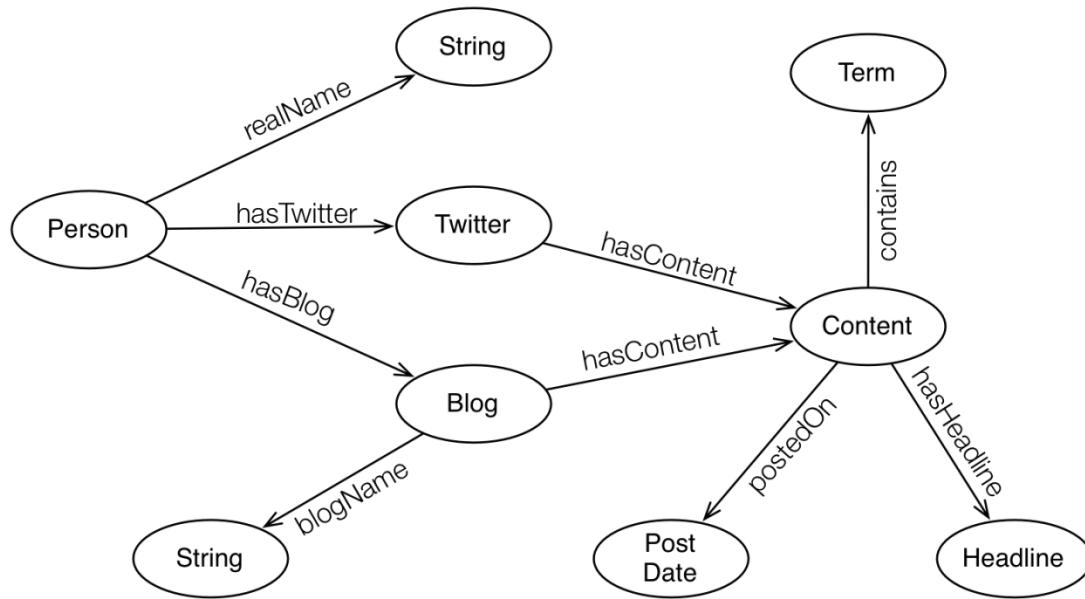
|      | From |     |     |     |   |   |   |     |     |   |      |             |
|------|------|-----|-----|-----|---|---|---|-----|-----|---|------|-------------|
|      | A    | B   | C   | D   | E | F | G | H   | I   | J | sum: | Popularity: |
| A    |      |     |     |     |   |   |   |     |     |   | 0    | 0           |
| B    | 1    |     |     |     |   |   |   |     |     |   | 1.00 | 0.111       |
| C    |      | 1/2 |     |     |   |   |   |     |     |   | 0.50 | 0.056       |
| D    |      |     | 1/3 |     |   |   | 1 | 1/2 |     |   | 1.83 | 0.204       |
| E    |      |     |     | 1/2 | 1 |   |   | 1/2 |     |   | 2.00 | 0.222       |
| F    |      | 1/2 | 1/3 |     |   |   |   |     |     |   | 0.83 | 0.092       |
| G    |      |     | 1/3 |     |   |   |   |     |     |   | 0.33 | 0.037       |
| H    |      |     |     |     |   |   |   |     | 1/2 |   | 0.50 | 0.056       |
| I    |      |     |     | 1/2 |   |   |   |     |     | 1 | 1.50 | 0.167       |
| J    |      |     |     |     |   |   |   |     | 1/2 |   | 0.50 | 0.056       |
| sum: |      |     |     |     |   |   |   |     |     |   |      |             |
|      | 1    | 1   | 1   | 1   | 1 | 0 | 1 | 1   | 1   | 1 |      |             |

# Graph Data: Popularity (10)

- Rules of a Popularity Network
  - Rule 0: Popularity transmits from one node to a downstream connected node.
  - Rule 1: Popularity transmissions from multiple nodes to a single node are additive.
  - Rule 2: A more popular node transmits more popularity.
  - Rule 3: A node splits up its popularity among its recipients.
- Continue with **EigenVectorOfGraphMatrix.R**
- Solve (or Iterate until convergence)
  - Modified Popularity is the Popularity divided by Gregariousness (Out-Degree)
  - Popularity of a website is the sum of the Modified Popularities that point to the website.

# Graph Data: Google Matrix

# Break



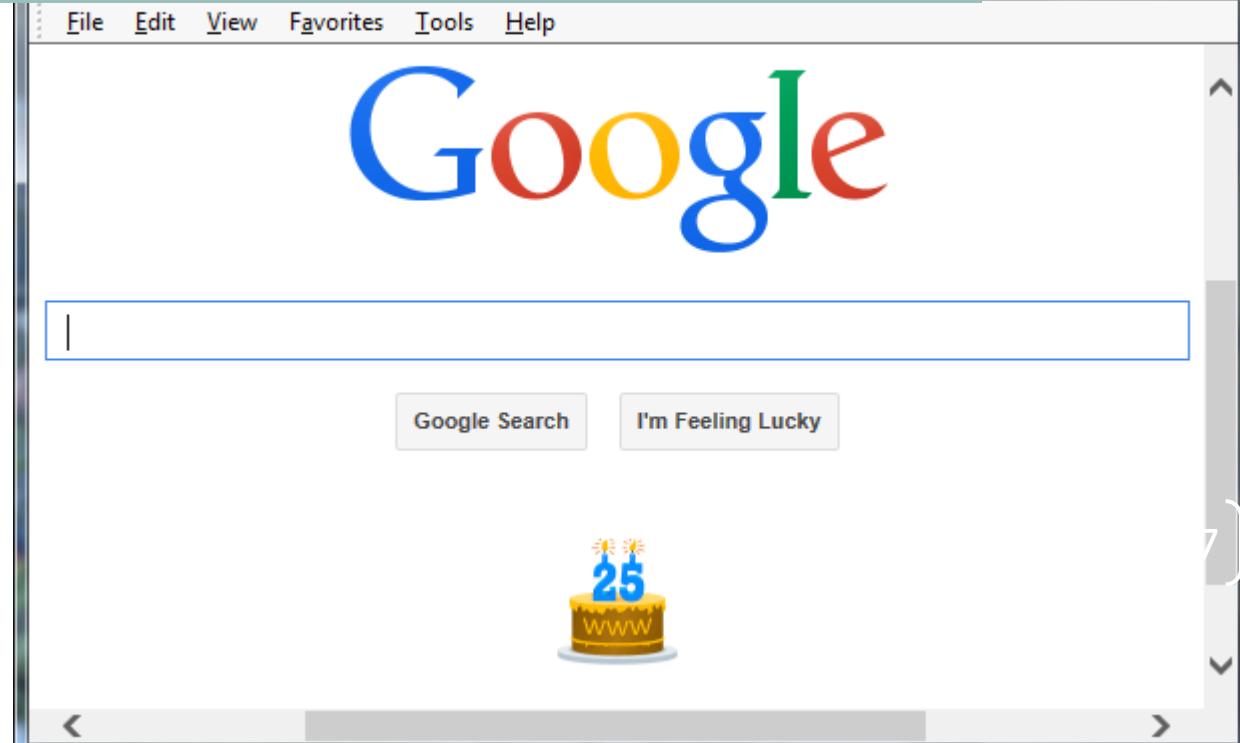
# Introduction to SPARQL

(126)

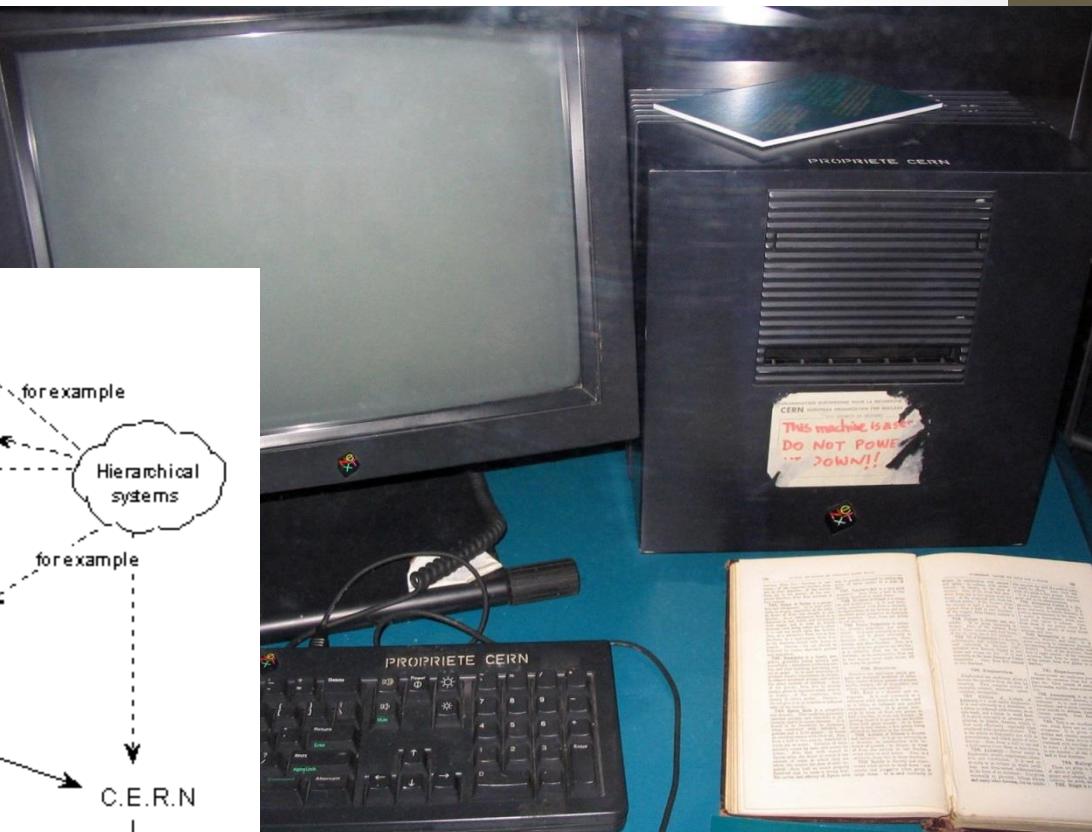
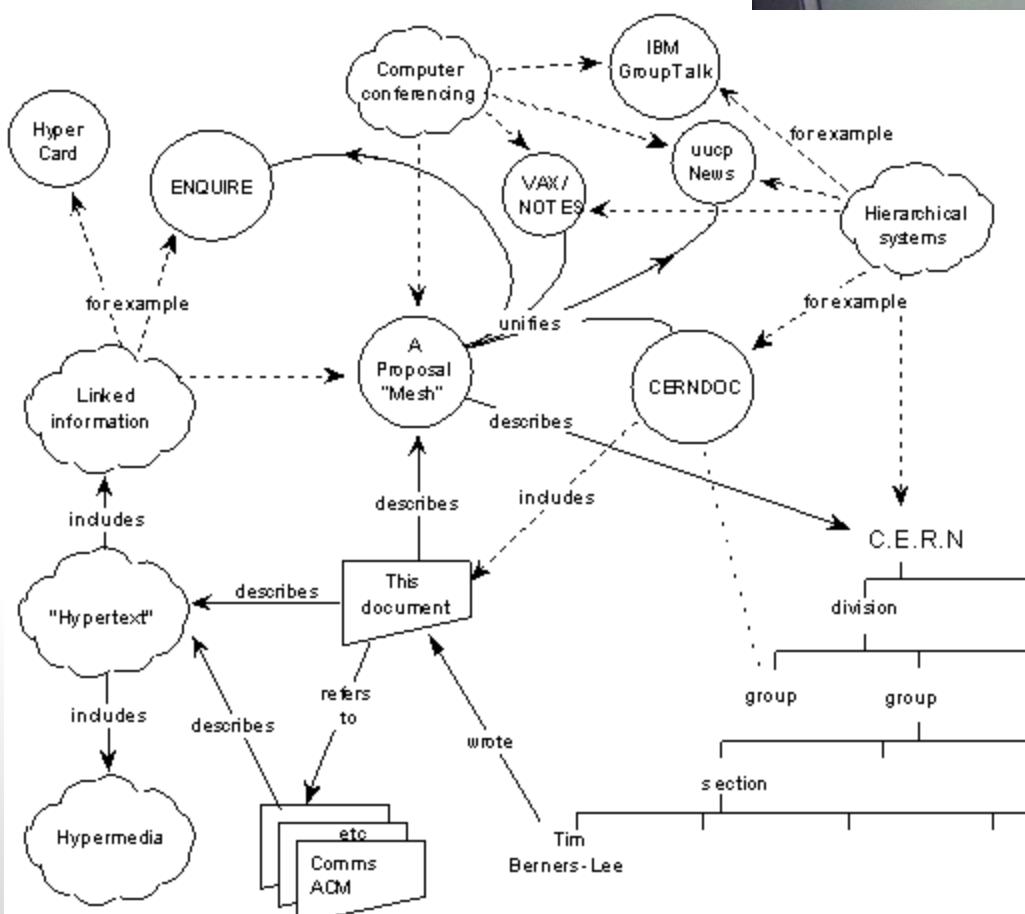
# SPARQL

- *SPARQL Protocol and RDF Query Language*
- "SPARQL will make a huge difference"

<http://blog.semantic-web.at/2009/04/22/tim-berners-lee-we-need-data-on-the-web-to-work-better-together/>



# Tim Berners-Lee's Web Server



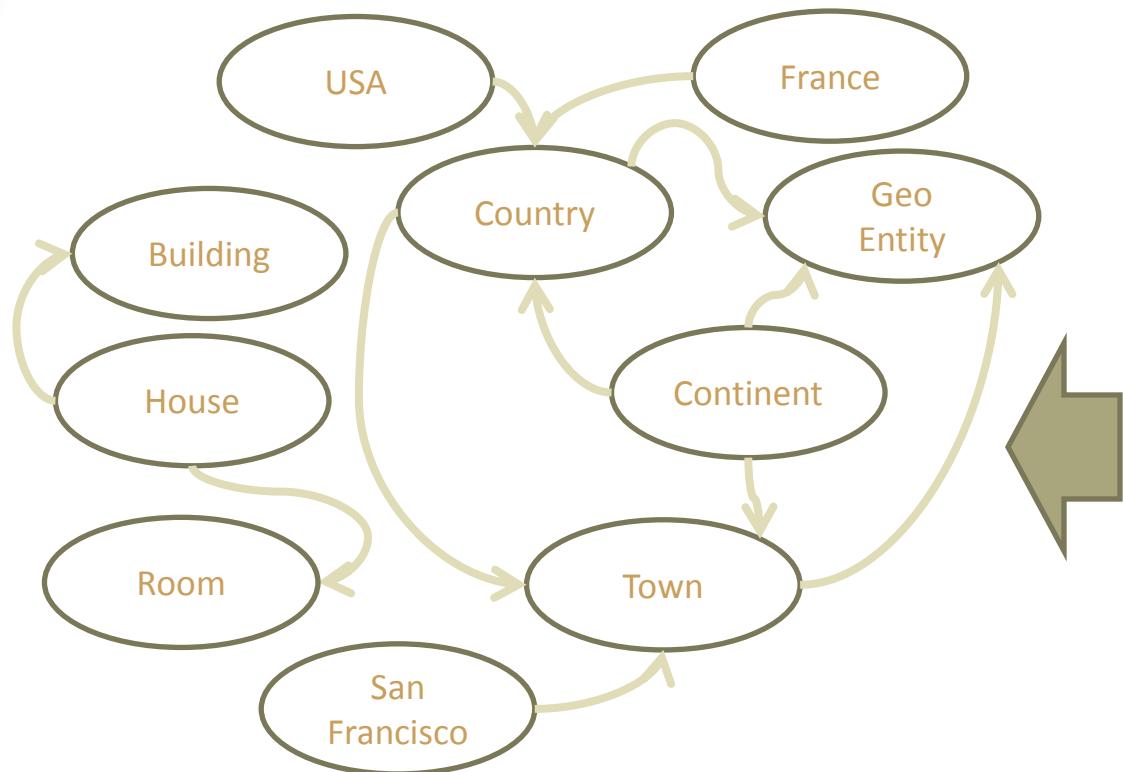
[ 128 ]

# SPARQL: Triplestore

- <http://en.wikipedia.org/wiki/Triplestore>
- <http://en.wikipedia.org/wiki/Sparql>

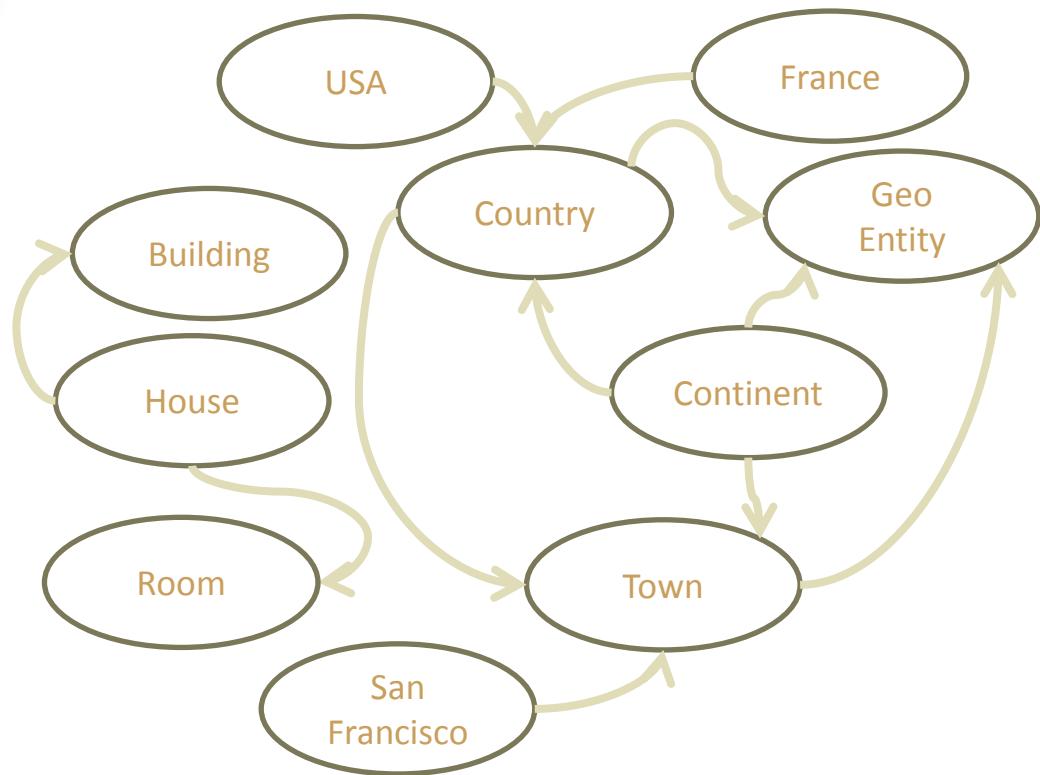
| S             | P        | O          |
|---------------|----------|------------|
| USA           | is a     | Country    |
| France        | is a     | Country    |
| Country       | is a     | Geo Entity |
| Country       | contains | Town       |
| Continent     | contains | Country    |
| Continent     | is a     | Geo Entity |
| Continent     | contains | Town       |
| Town          | is a     | Geo Entity |
| San Francisco | is a     | Town       |
| House         | contains | Room       |
| House         | is a     | Building   |

# SPARQL: Graph

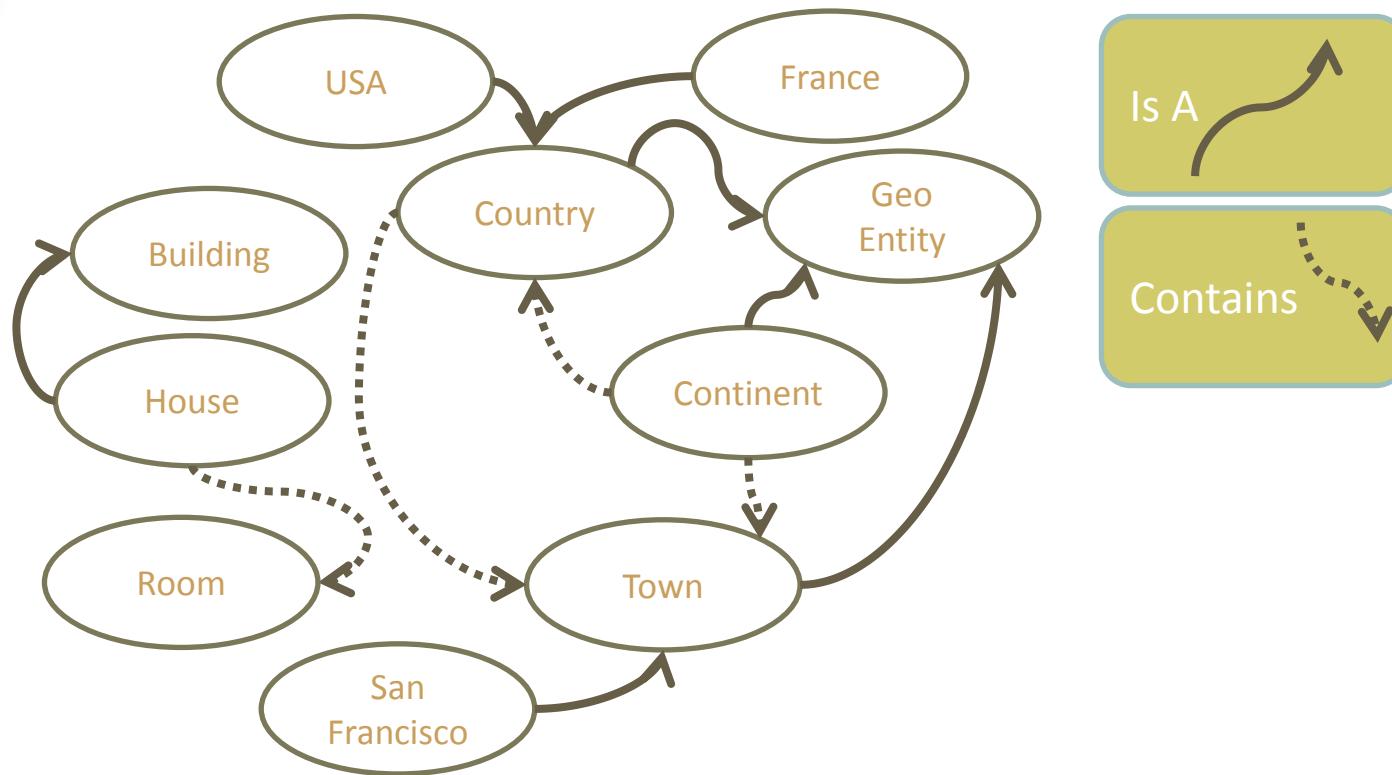


| S             | P        | O          |
|---------------|----------|------------|
| USA           | is a     | Country    |
| France        | is a     | Country    |
| Country       | is a     | Geo Entity |
| Country       | contains | Town       |
| Continent     | contains | Country    |
| Continent     | is a     | Geo Entity |
| Continent     | contains | Town       |
| Town          | is a     | Geo Entity |
| San Francisco | is a     | Town       |
| House         | contains | Room       |
| House         | is a     | Building   |

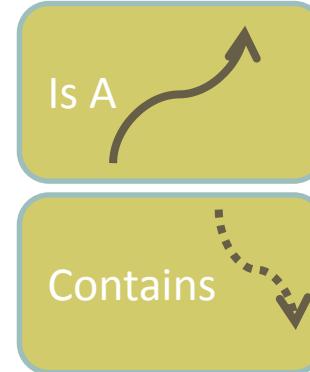
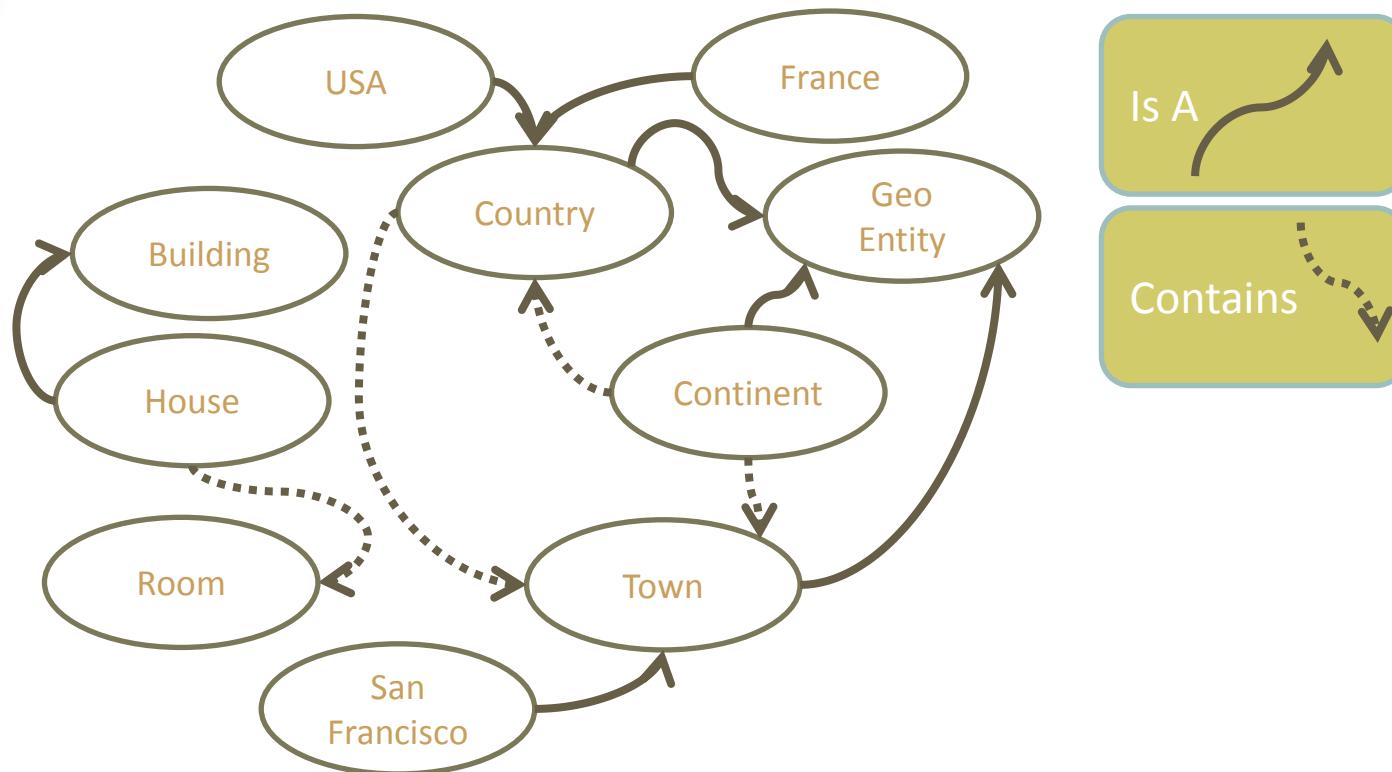
# SPARQL: Graph



# SPARQL: Graph



# SPARQL: Subjects & Objects

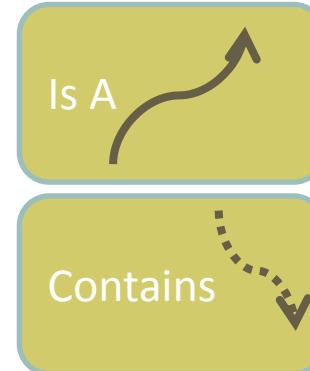
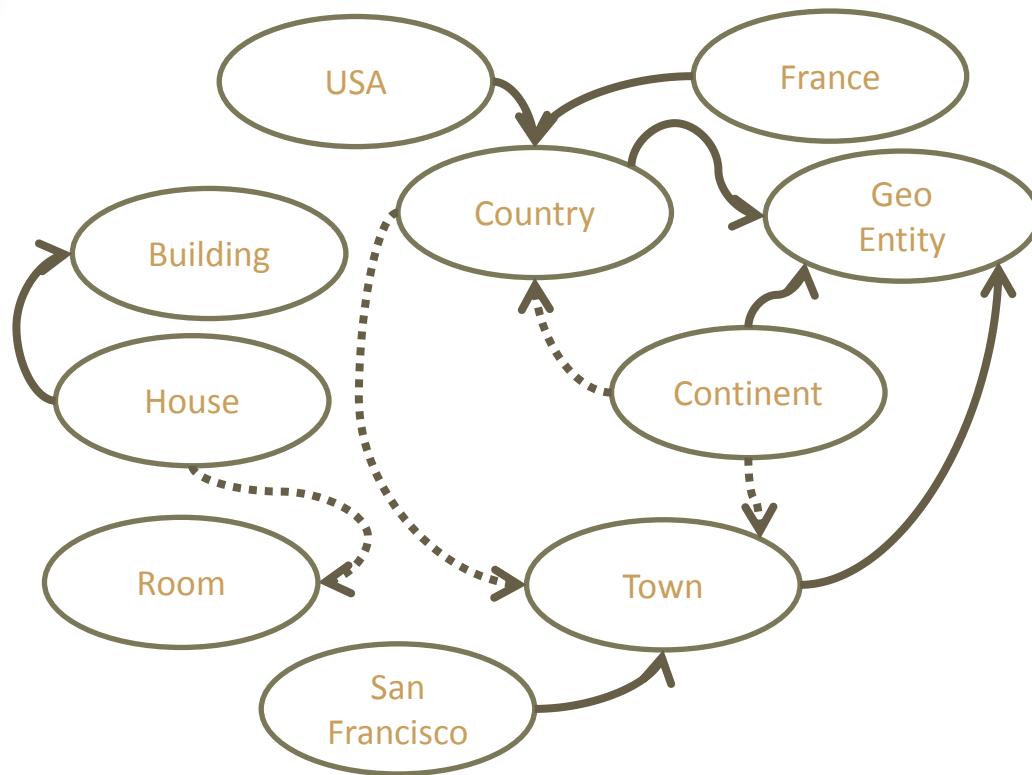


Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects



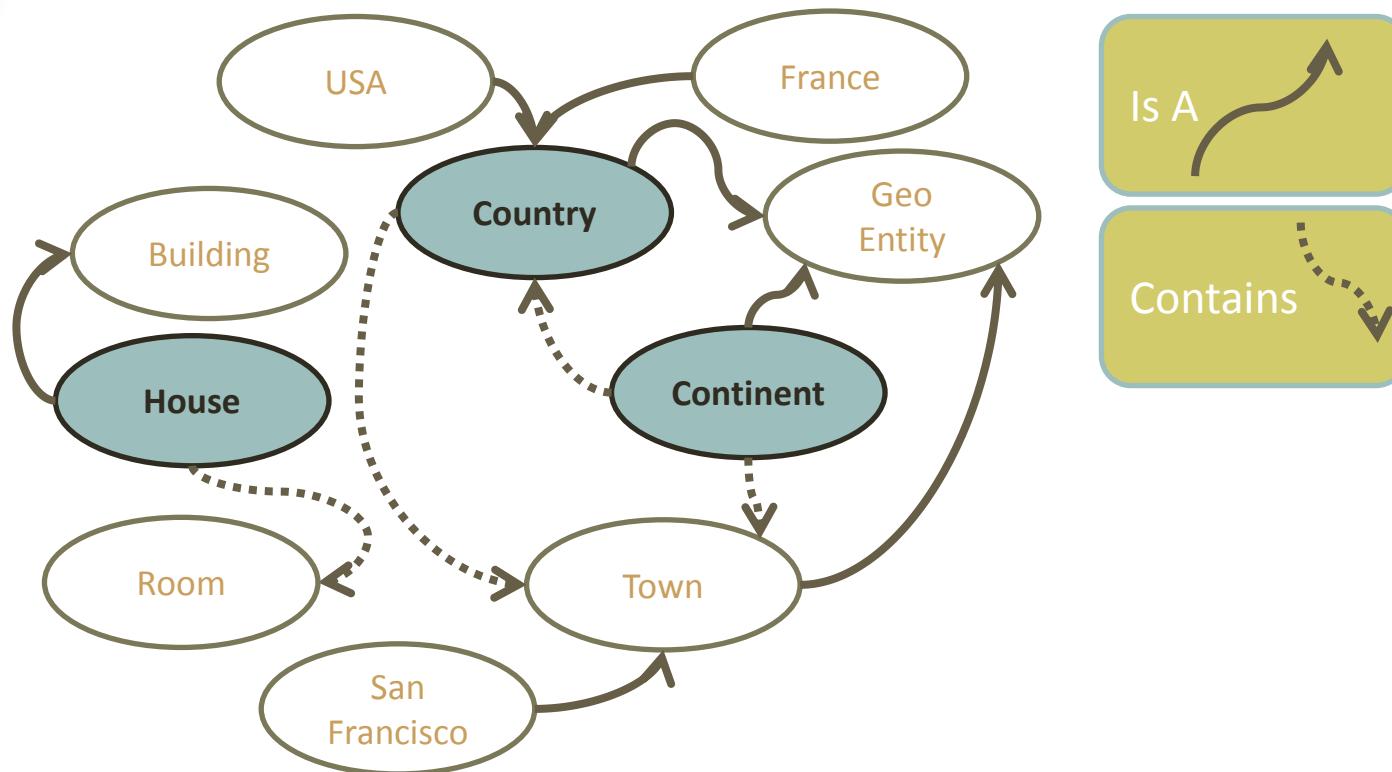
```
SELECT<return variables>  
FROM <Triplestore>  
WHERE { <condition>}
```

Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects

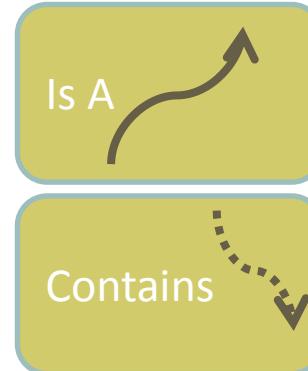
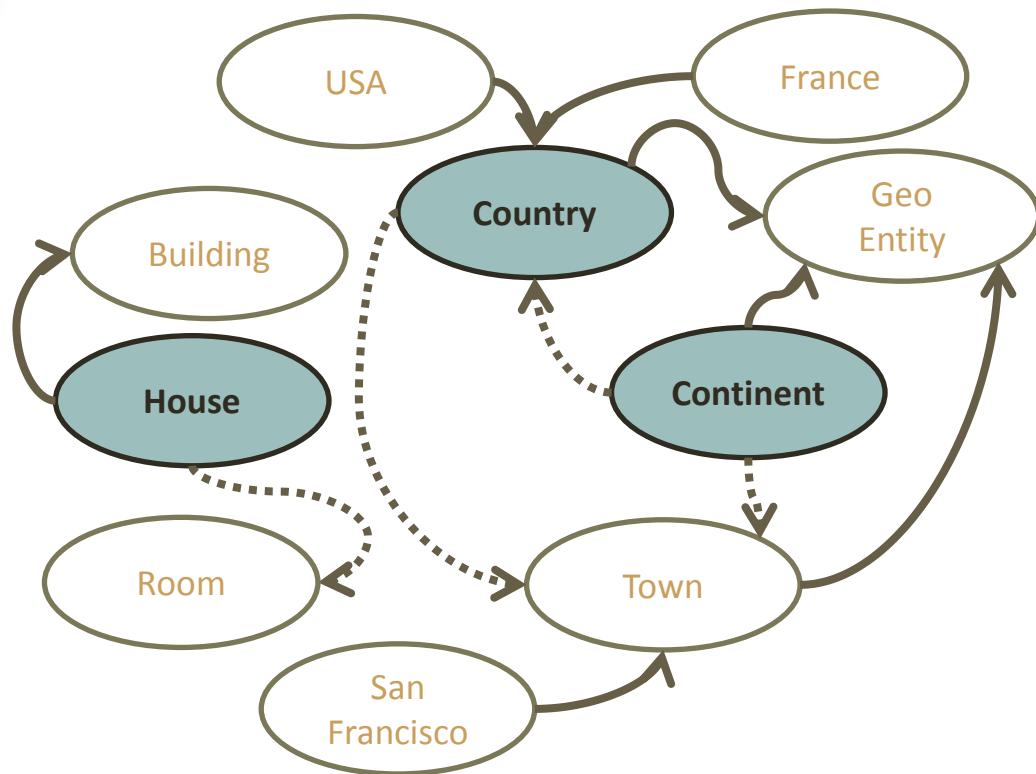


Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects



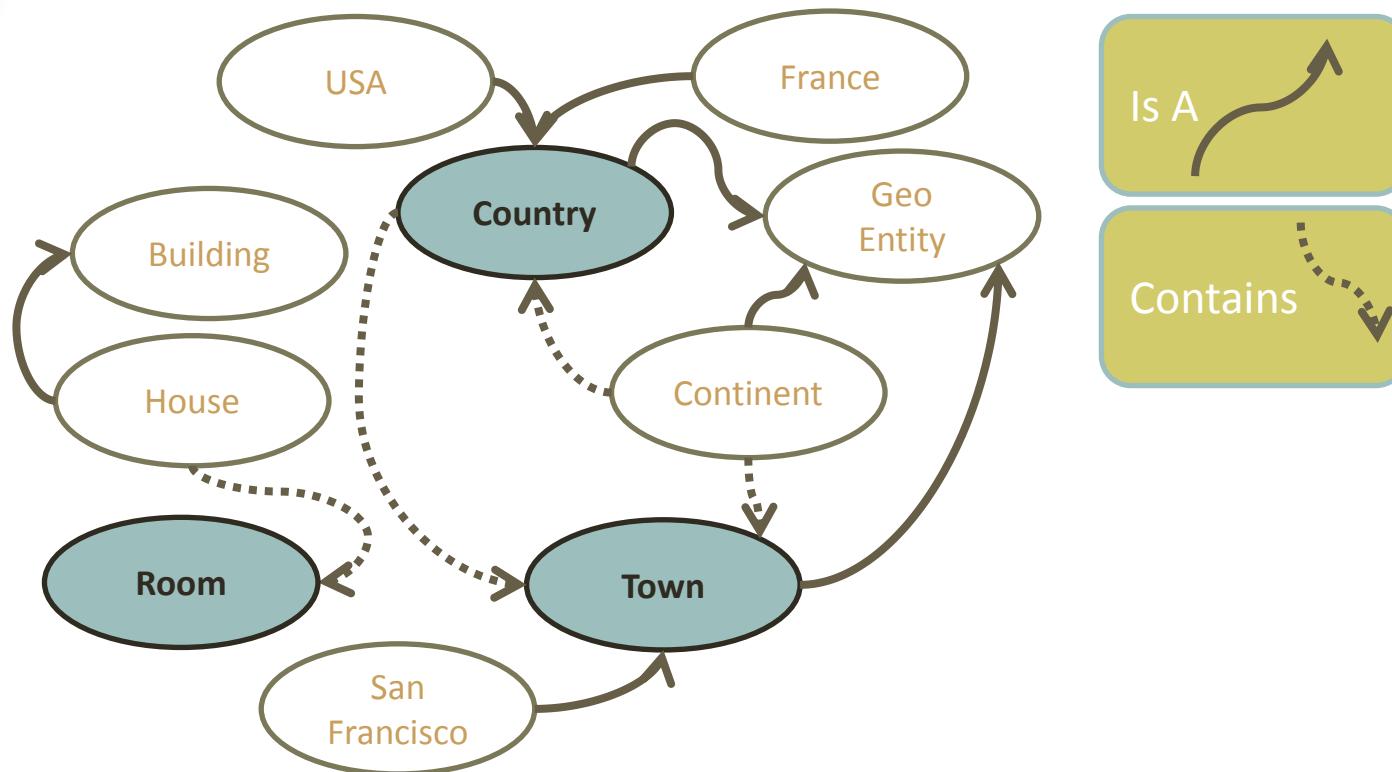
```
SELECT ?s  
FROM <myTripleStore>  
WHERE {  
?s contains ?o  
}
```

Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects

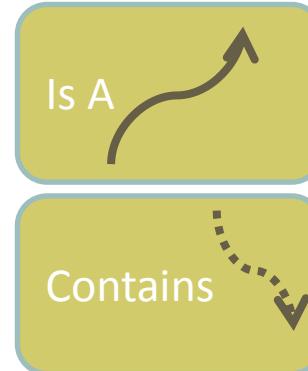
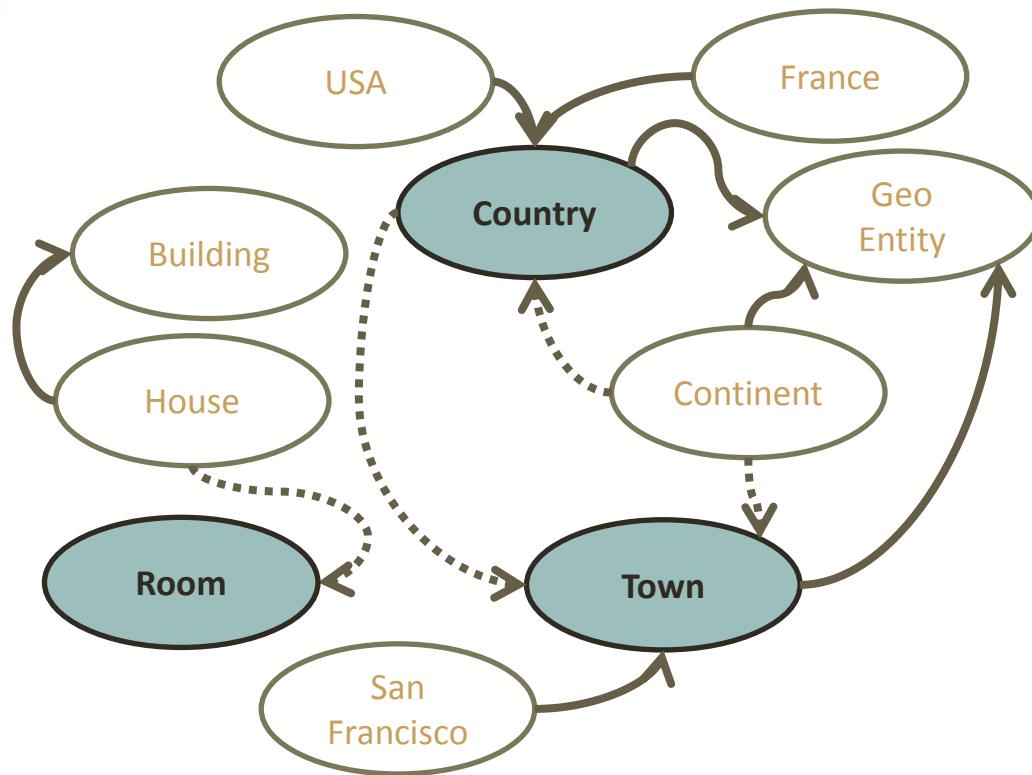


Show node (subject) that contains something

**Show node (object) that is contained by something**

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects



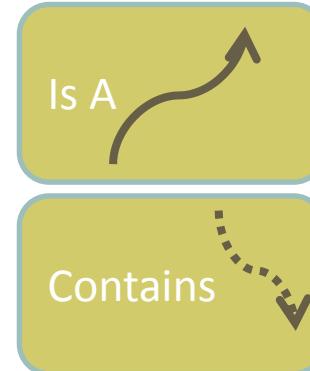
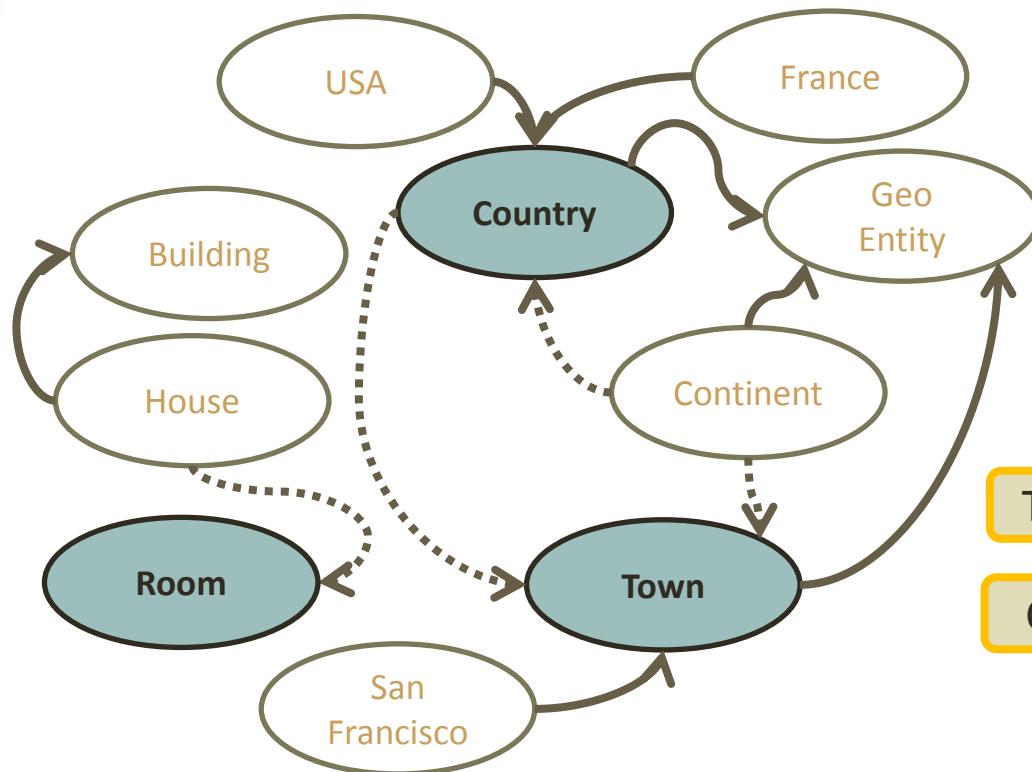
```
SELECT ?o  
FROM <myTripleStore>  
WHERE {  
?s contains ?o}
```

Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects



```
SELECT ?o  
FROM <myTripleStore>  
WHERE {  
?s contains ?o}
```

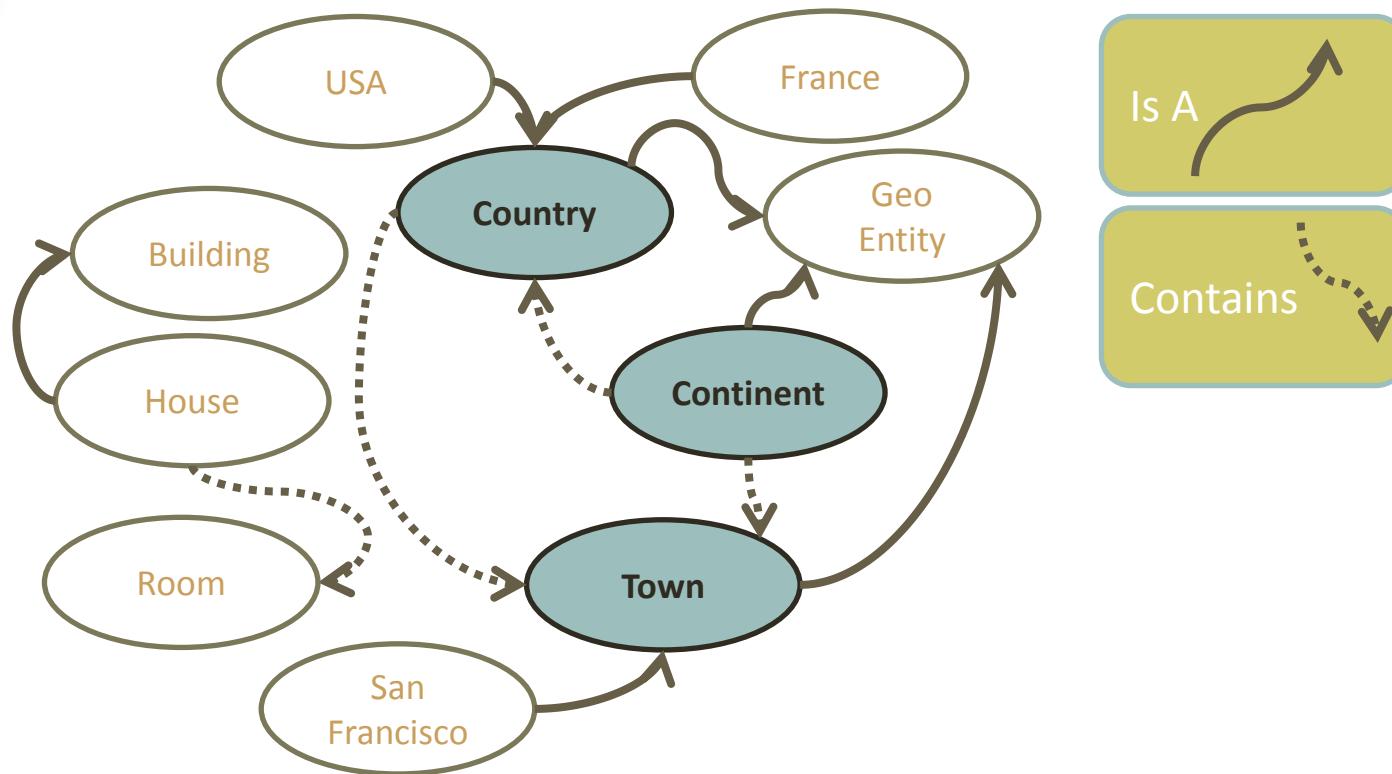
Triplestore Condition Return Variable

Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects

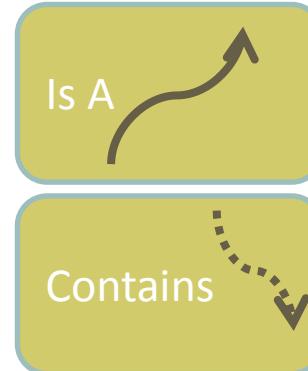
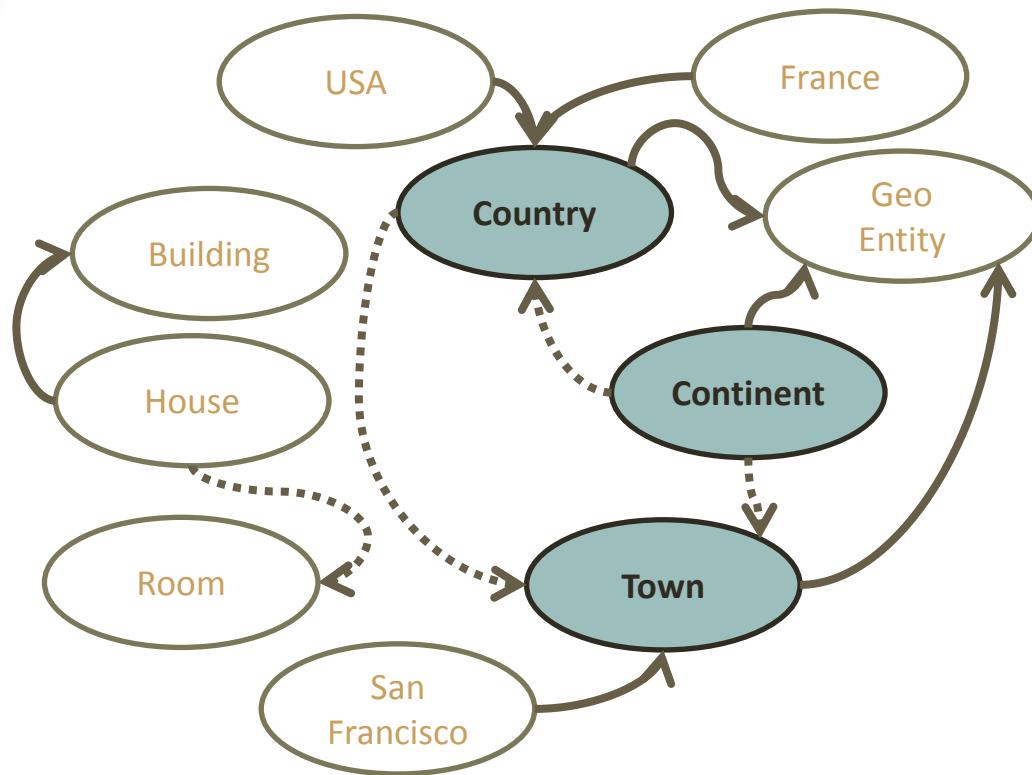


Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects



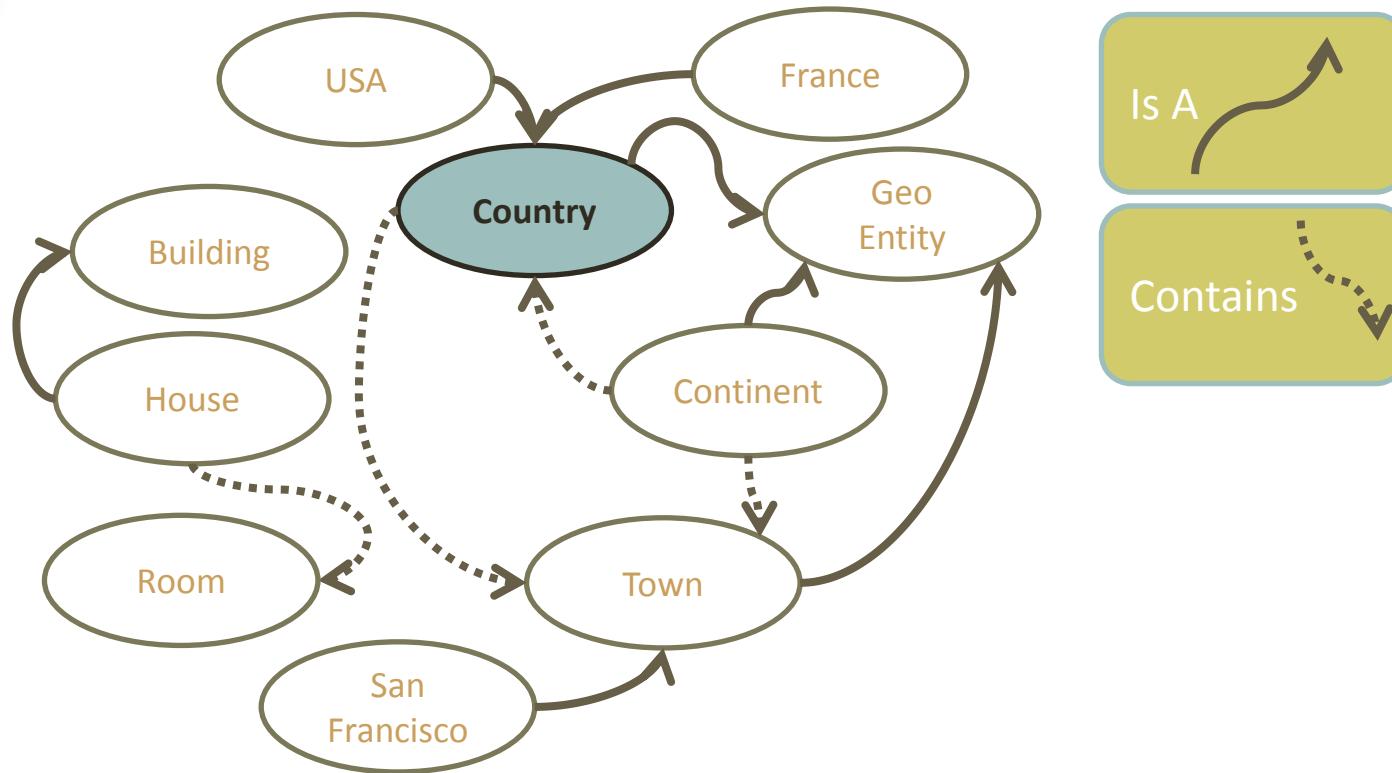
```
SELECT ?s  
FROM <myTripleStore>  
WHERE {  
?s is a Geo Entity}
```

Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects

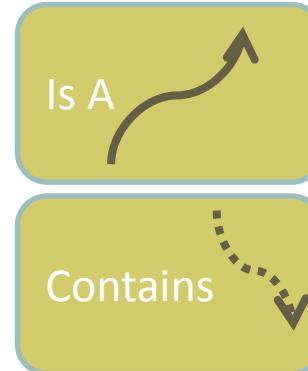
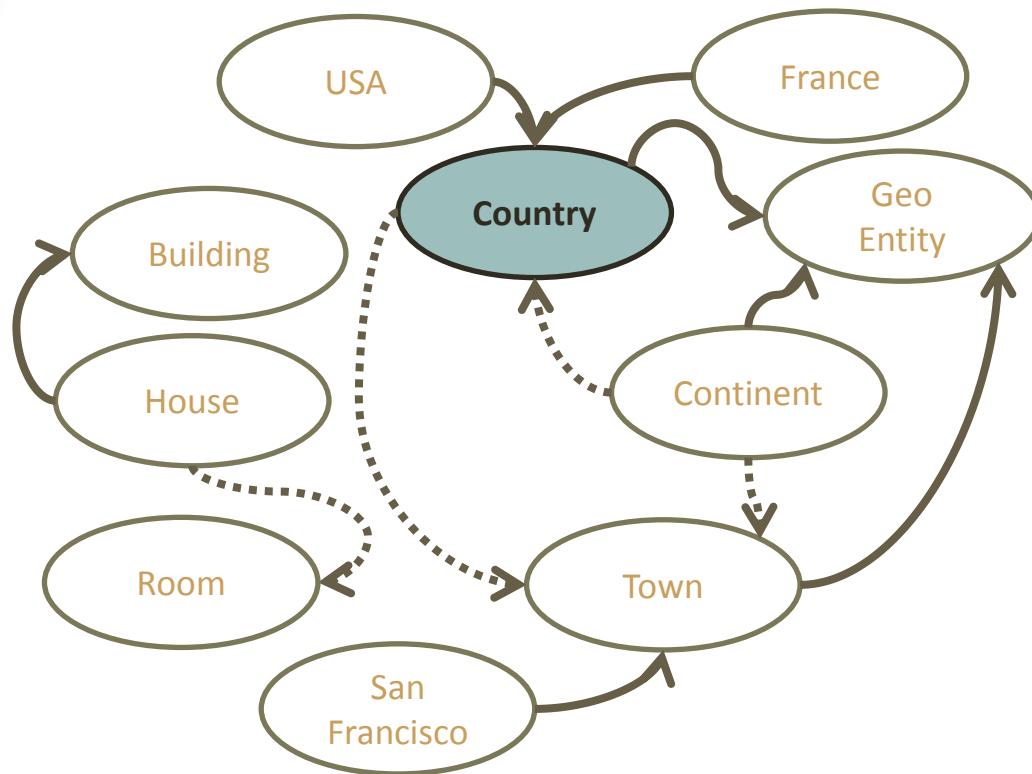


Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects



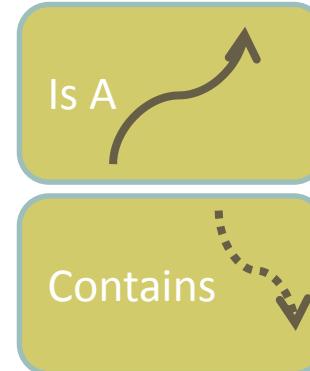
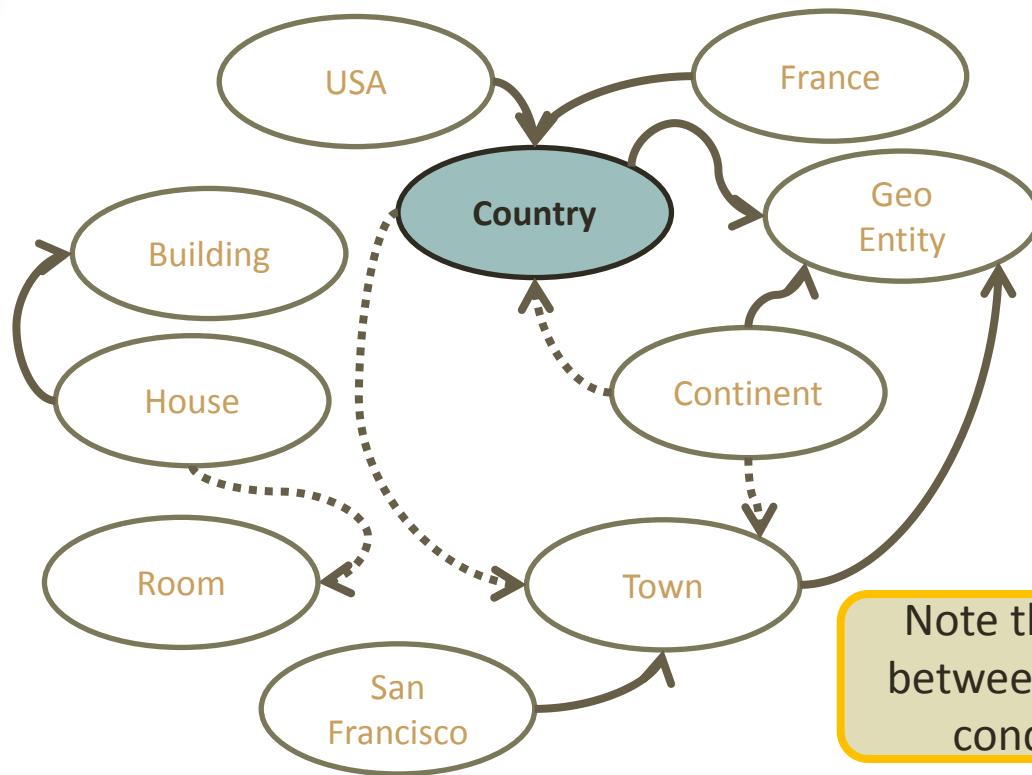
```
SELECT ?s  
FROM <myTripleStore>  
WHERE {  
?s Contains ?o .  
?x Contains ?s}
```

Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects



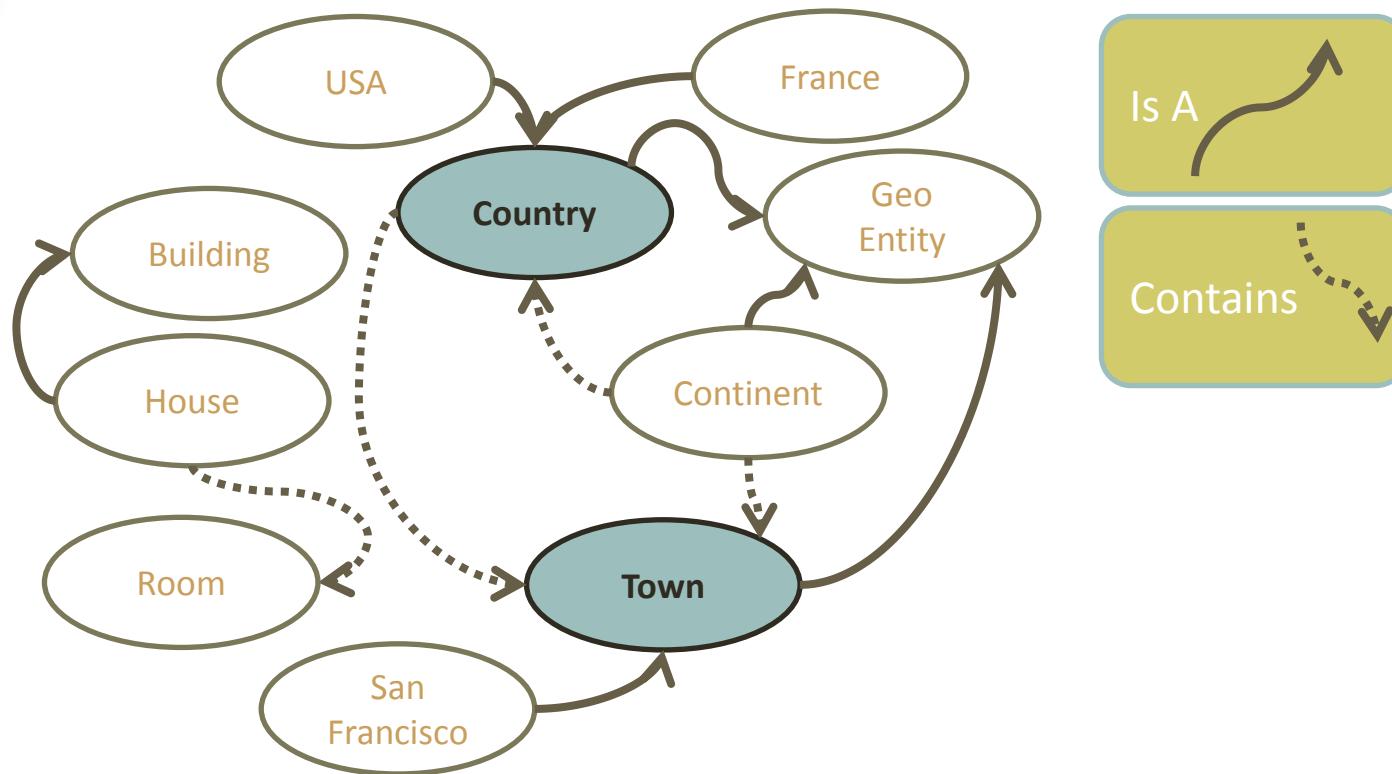
```
SELECT ?s  
FROM <myTripleStore>  
WHERE {  
?s Contains ?o.  
?x Contains ?s}
```

Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects

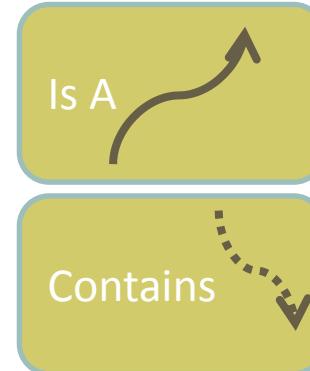
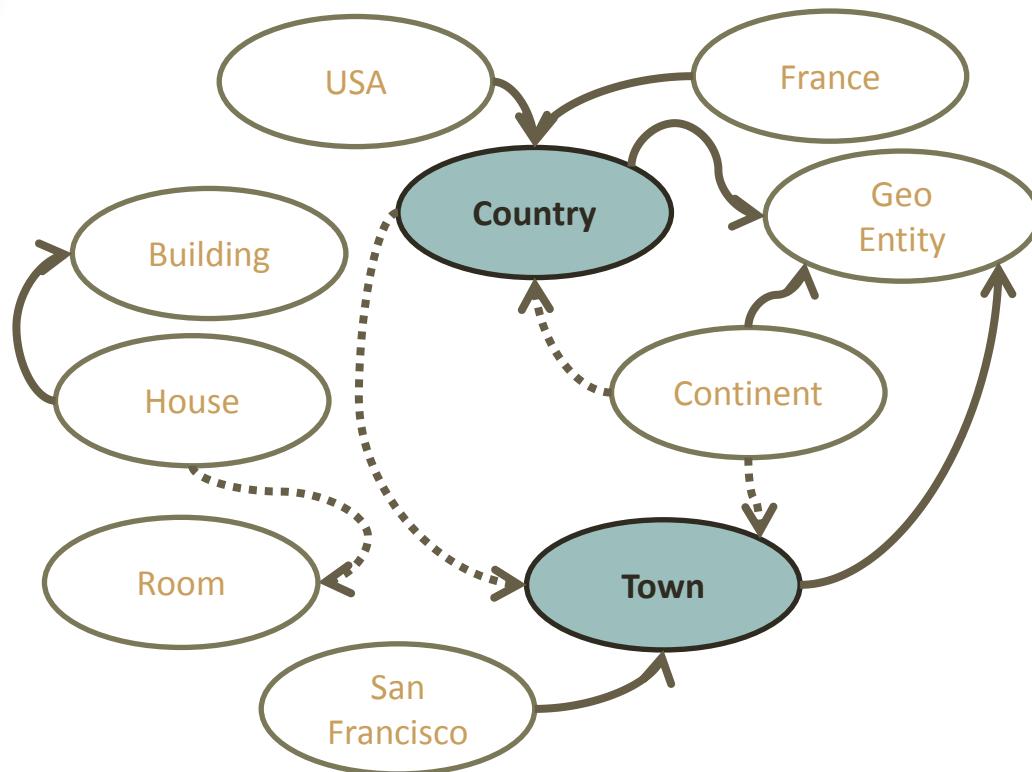


Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects



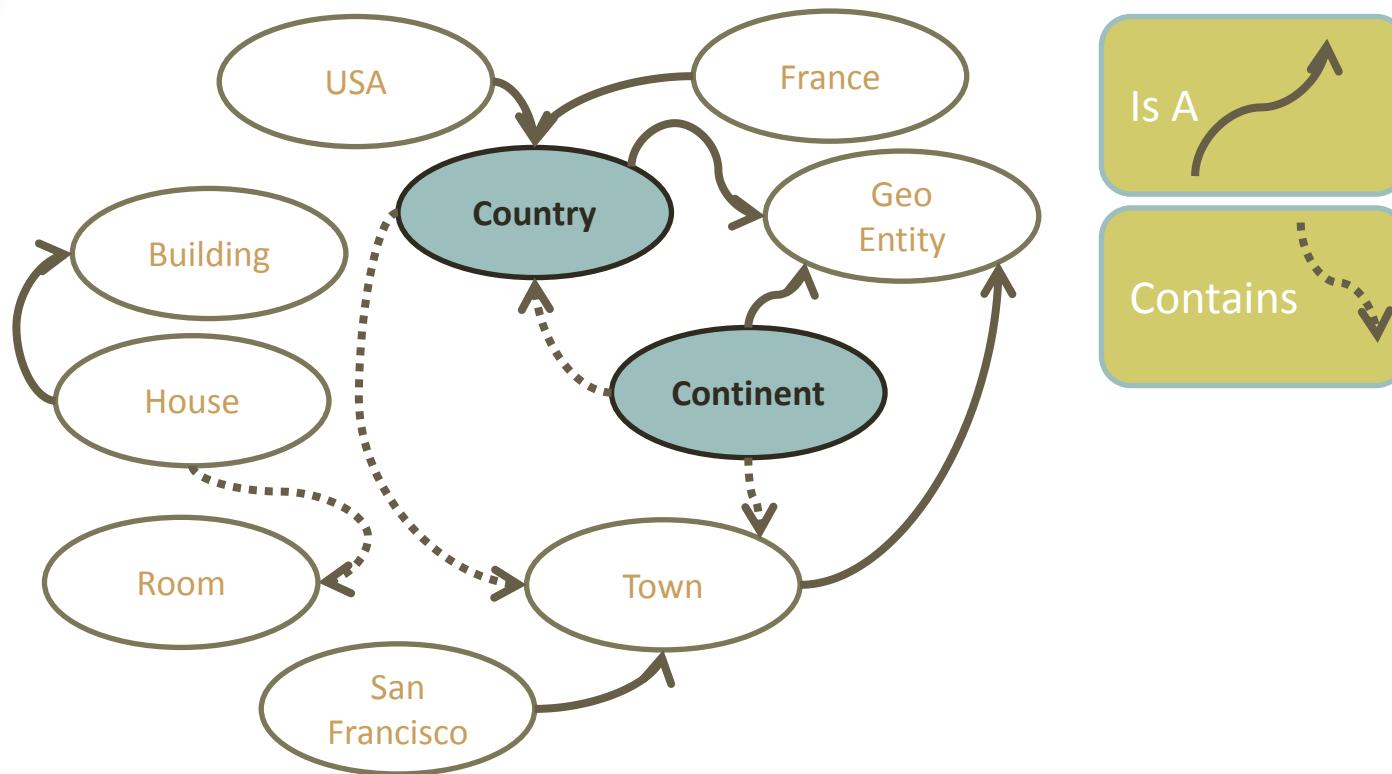
```
SELECT ?o  
FROM <myTripleStore>  
WHERE {  
?x Contains ?o .  
?o is a Geo Entity}
```

Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects

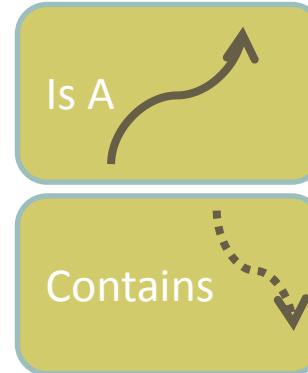
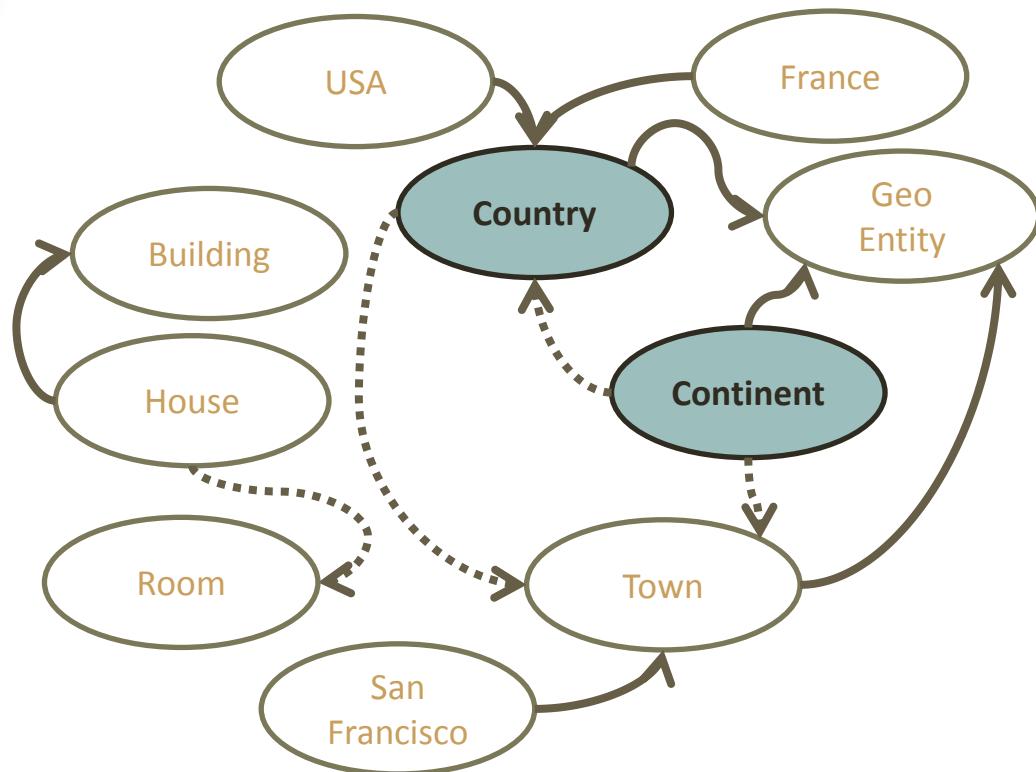


Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects



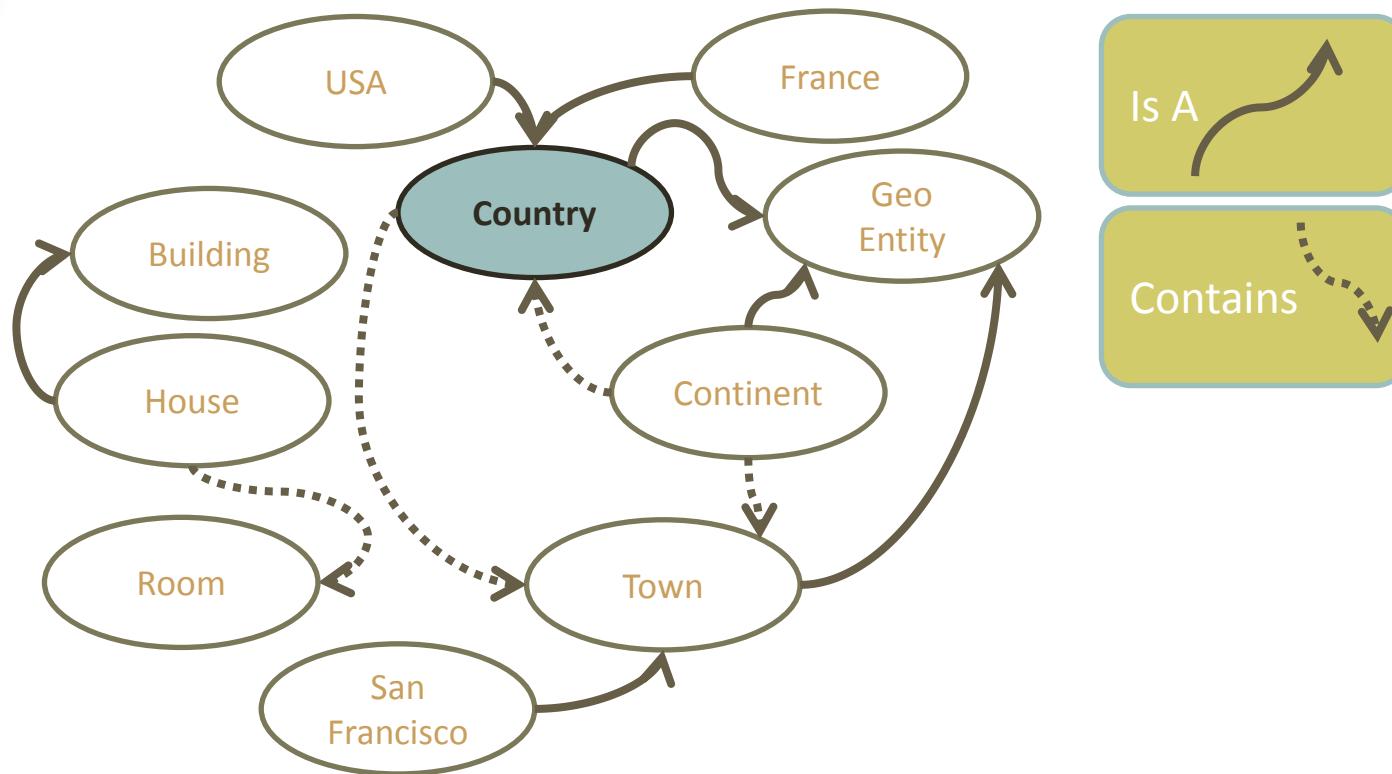
```
SELECT ?s  
FROM <myTripleStore>  
WHERE {  
?s Contains ?o .  
?s is a Geo Entity}
```

Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects

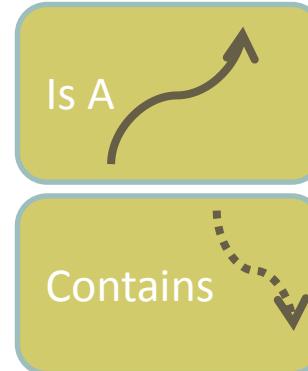
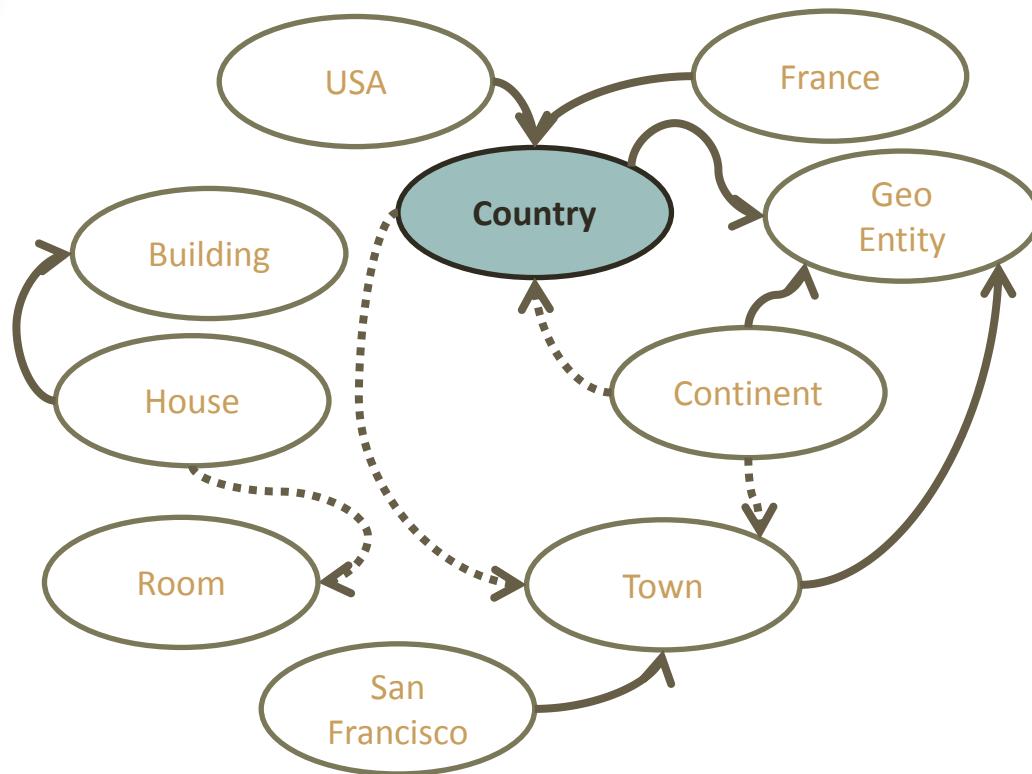


Show node (subject) that contains something

Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Subjects & Objects



```
SELECT ?s  
FROM <myTripleStore>  
WHERE {  
?s Contains ?o .  
?x Contains ?s .  
?s is a Geo Entity}
```

Show node (subject) that contains something

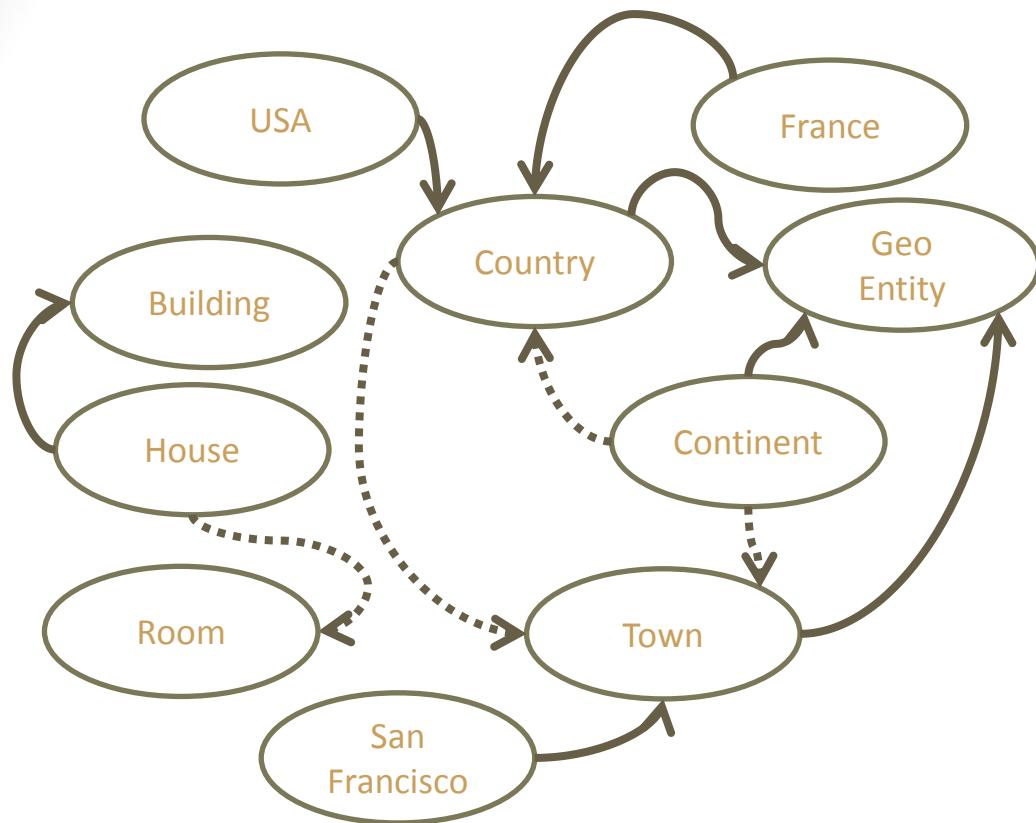
Show node (object) that is contained by something

Show node (subject) that is a Geo Entity

# SPARQL: Predicates

- Search for predicates

# SPARQL: Predicates

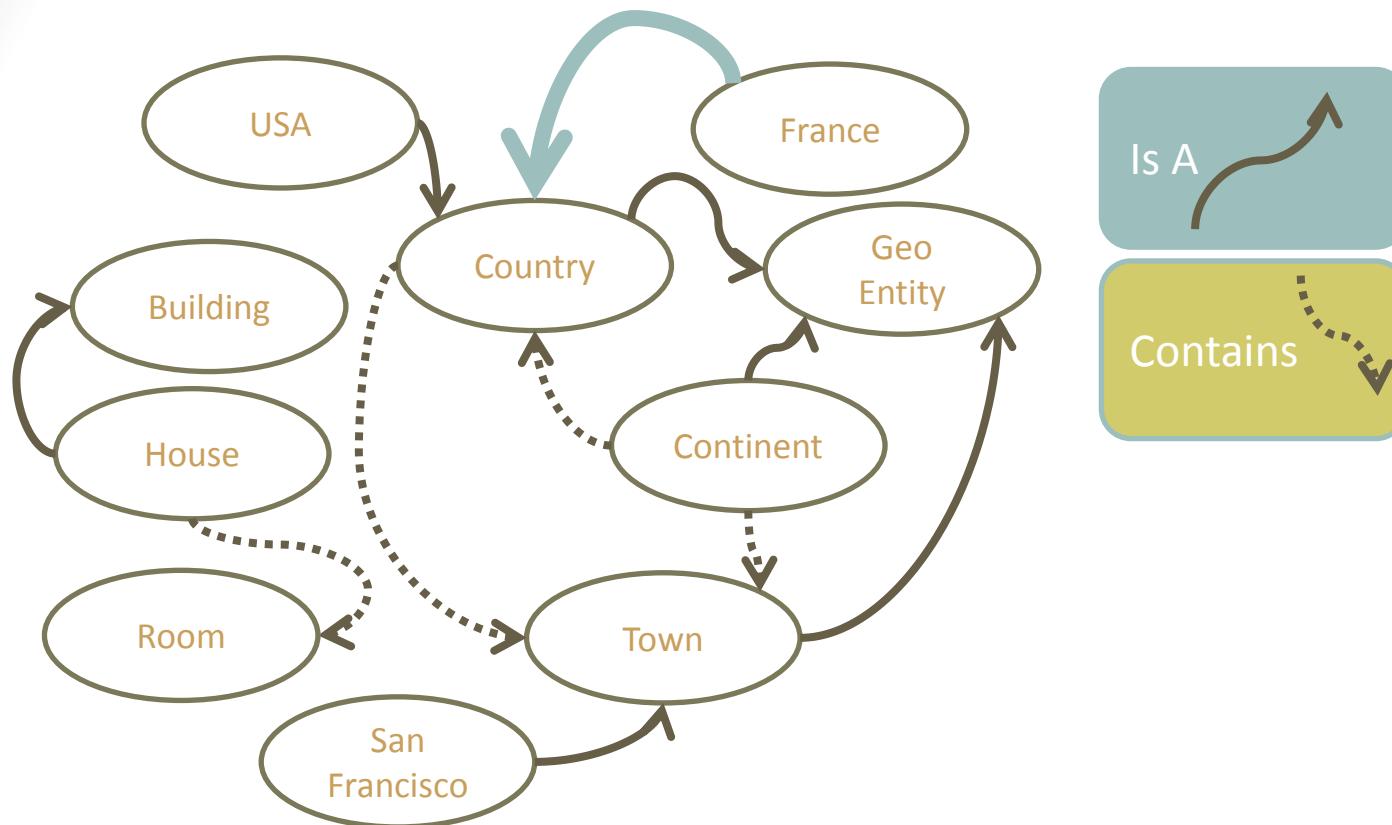


```
SELECT<return variables>  
FROM <Triplestore>  
WHERE { <condition>}
```

Show relationships (Predicate) from France to Anything

Show relationships from Country to Town

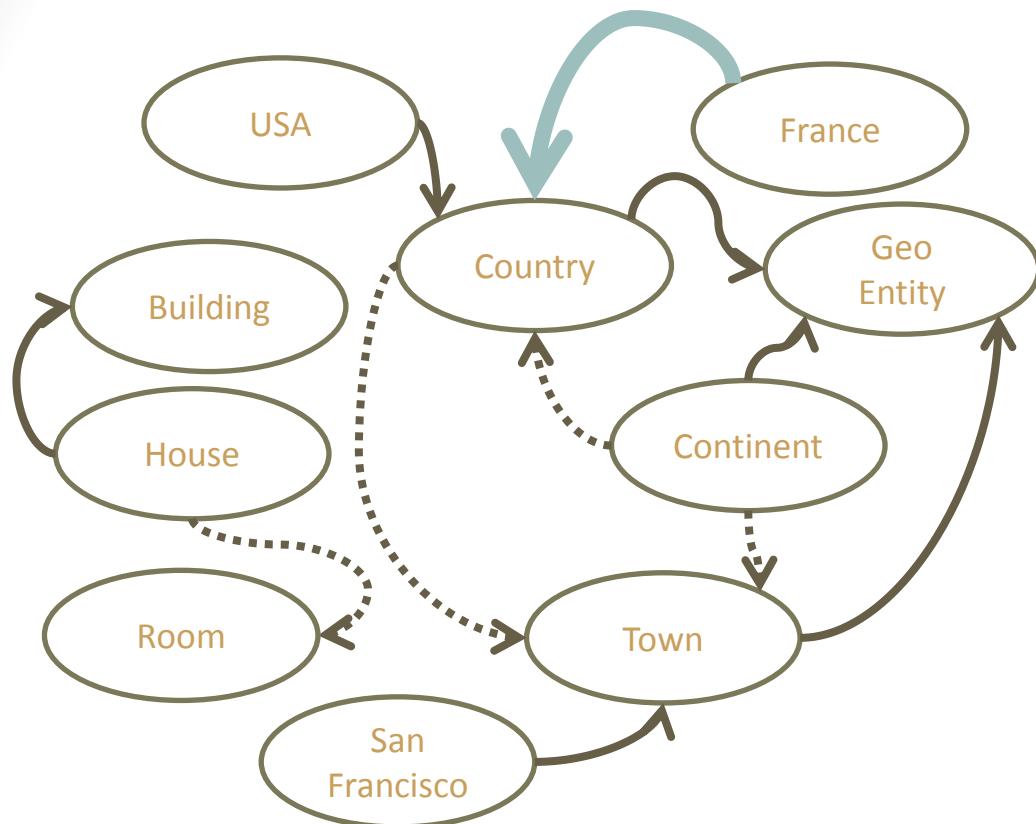
# SPARQL: Predicates



Show relationships (Predicate) from France to Anything

Show relationships from Country to Town

# SPARQL: Predicates

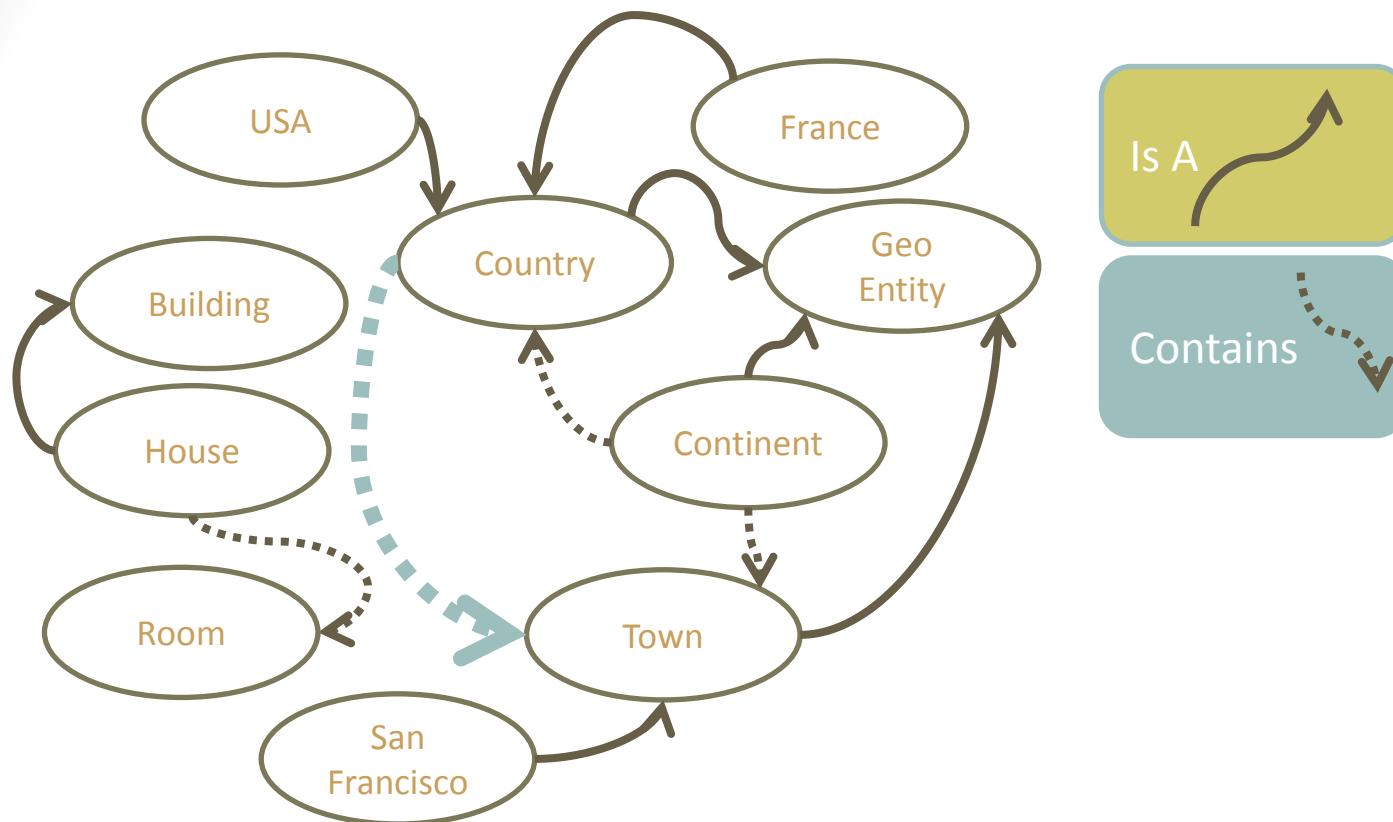


```
SELECT ?p  
FROM <myTripleStore>  
WHERE {  
  France ?p ?o}
```

Show relationships (Predicate) from France to Anything

Show relationships from Country to Town

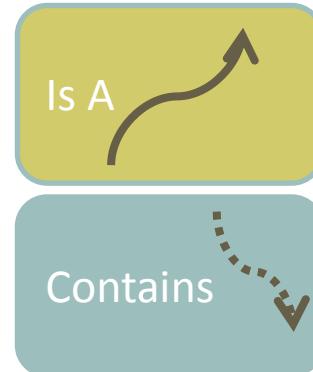
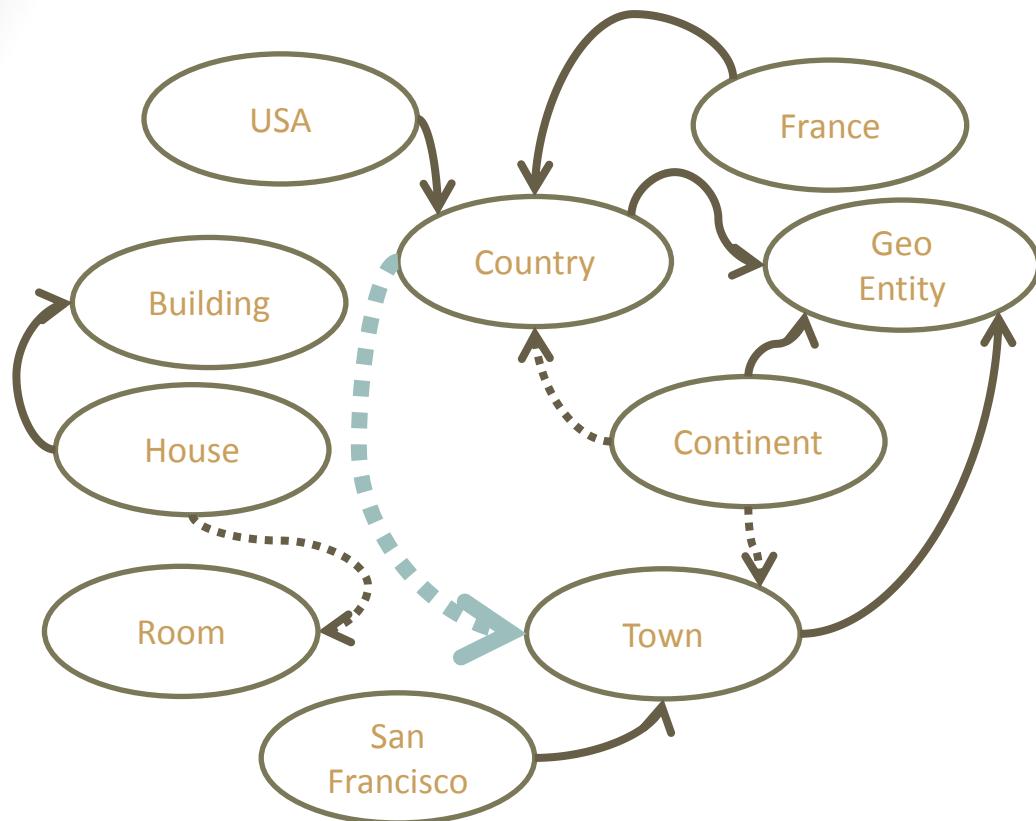
# SPARQL: Predicates



Show relationships (Predicate) from France to Anything

Show relationships from Country to Town

# SPARQL: Predicates

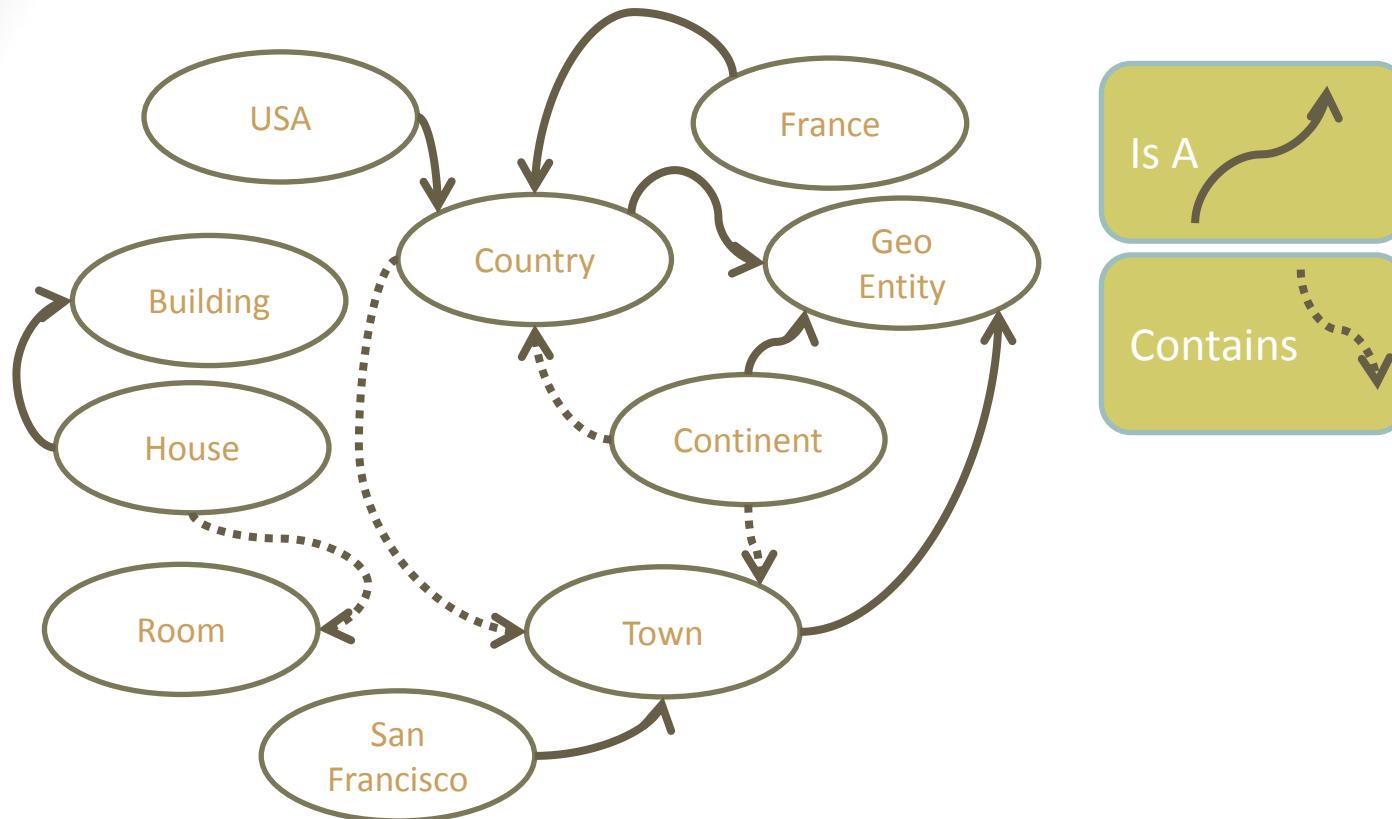


```
SELECT ?p
FROM <myTripleStore>
WHERE {
  Country ?p Town}
```

Show relationships (Predicate) from France to Anything

Show relationships from Country to Town

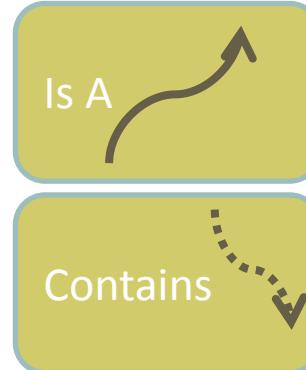
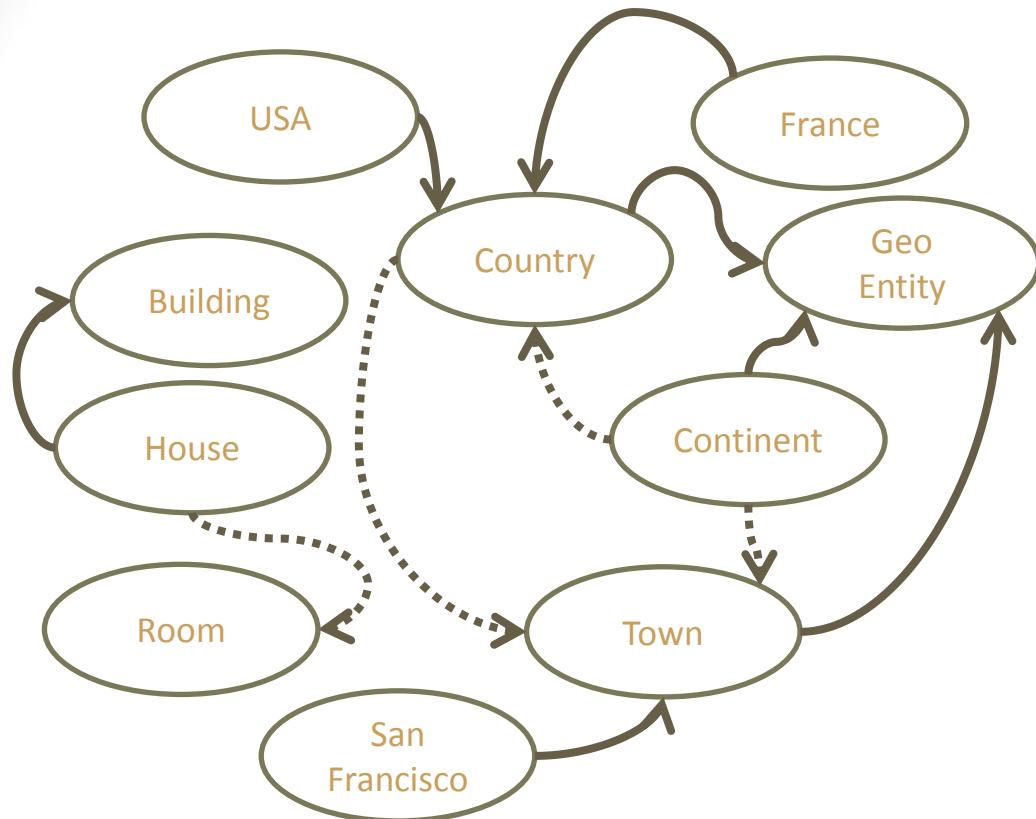
# SPARQL: Predicates



Show relationships (Predicate) from France to Anything

Show relationships from Country to Town

# SPARQL: Predicates

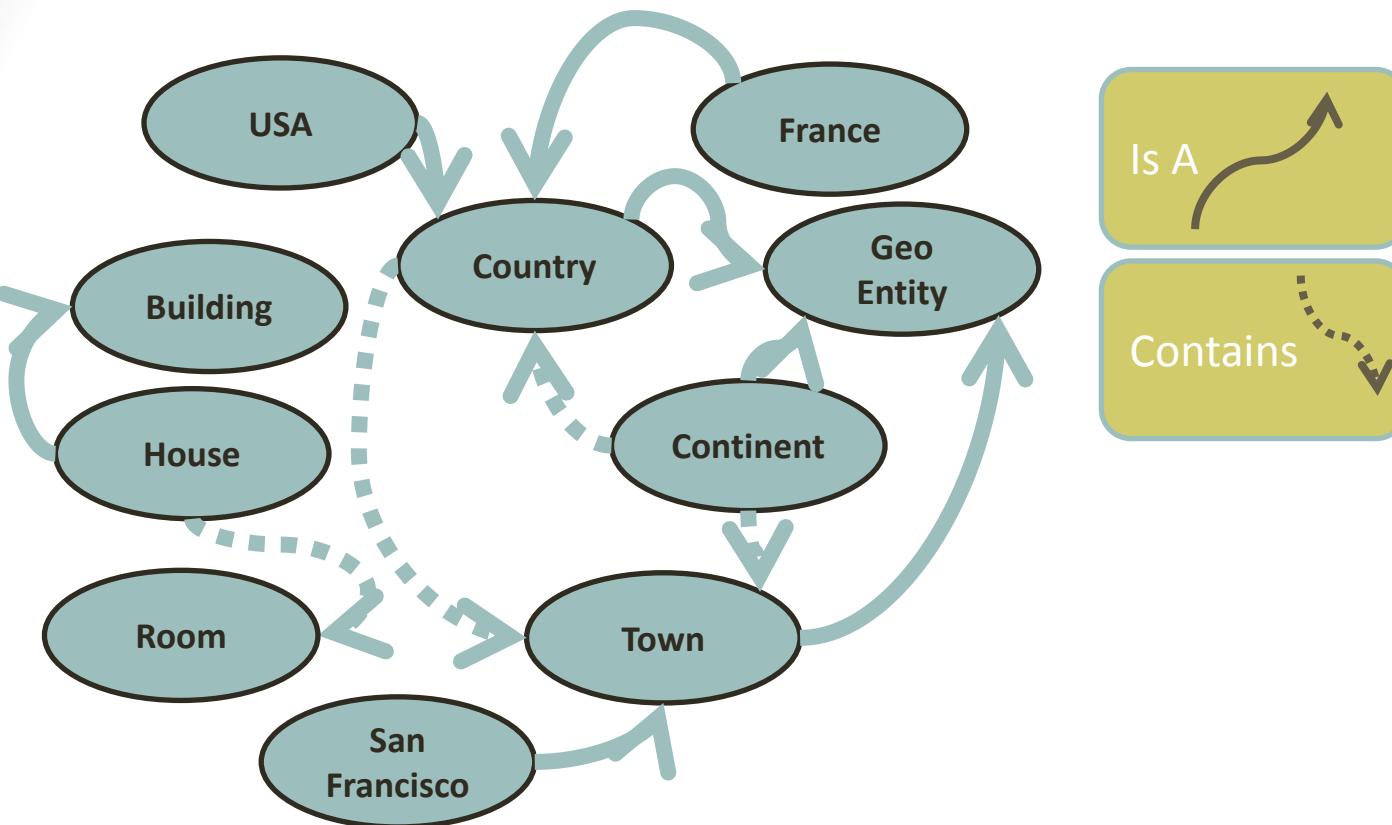


```
SELECT ?p  
FROM <myTripleStore>  
WHERE {  
  France ?p ?o .  
  Country ?p Town}
```

Show relationships (Predicate) from France to Anything

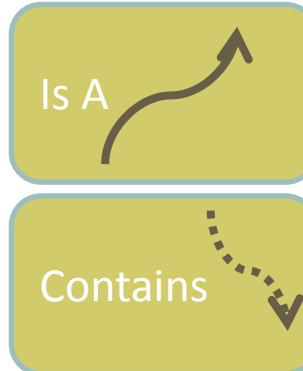
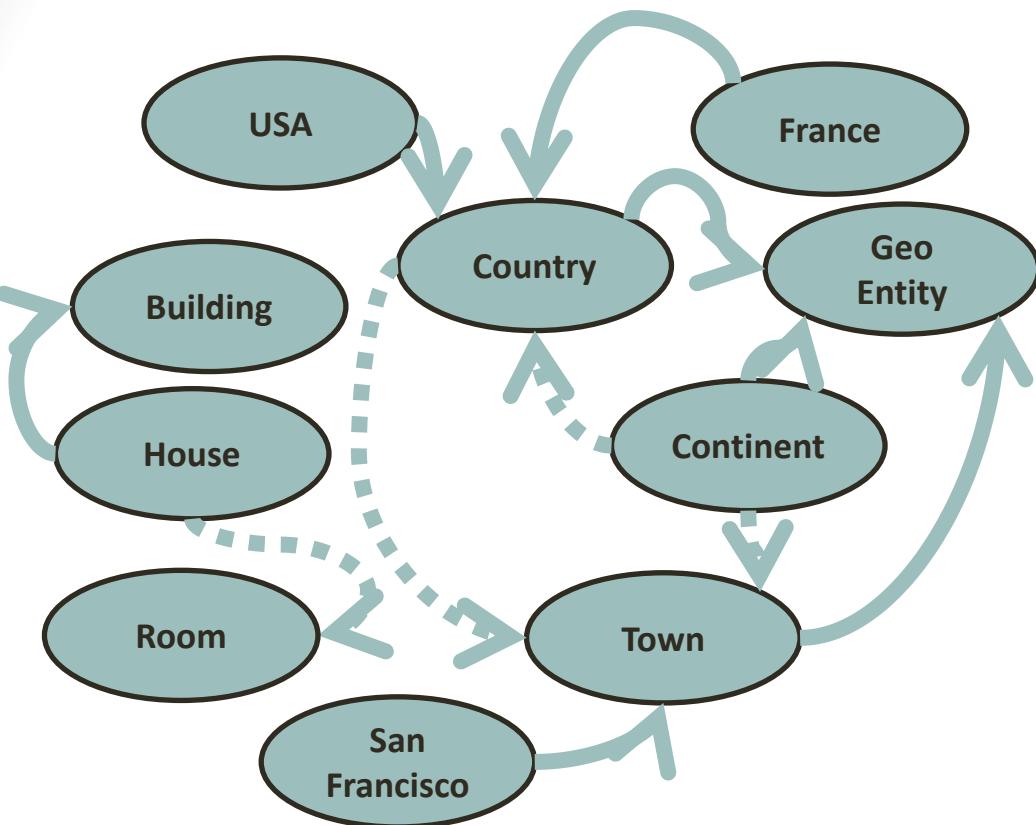
Show relationships from Country to Town

# SPARQL: Predicates



Show any node and relationship

# SPARQL: Predicates



```
SELECT ?s ?p ?o  
FROM <myTripleStore>  
WHERE {  
?s ?p ?o}
```

Show any node and relationship

# Some Links

- <http://dbpedia.org/sparql>
- <http://lod.openlinksw.com/sparql/>
- <http://librdf.org/query/>
- Online tutorial:  
<http://www.cambridgesemantics.com/semantic-university/sparql-by-example>
- 
- <http://sparql.org/sparql.html>
- <http://demo.openlinksw.com/sparql>

# Introduction to SPARQL

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# Quiz SPARQL Intro

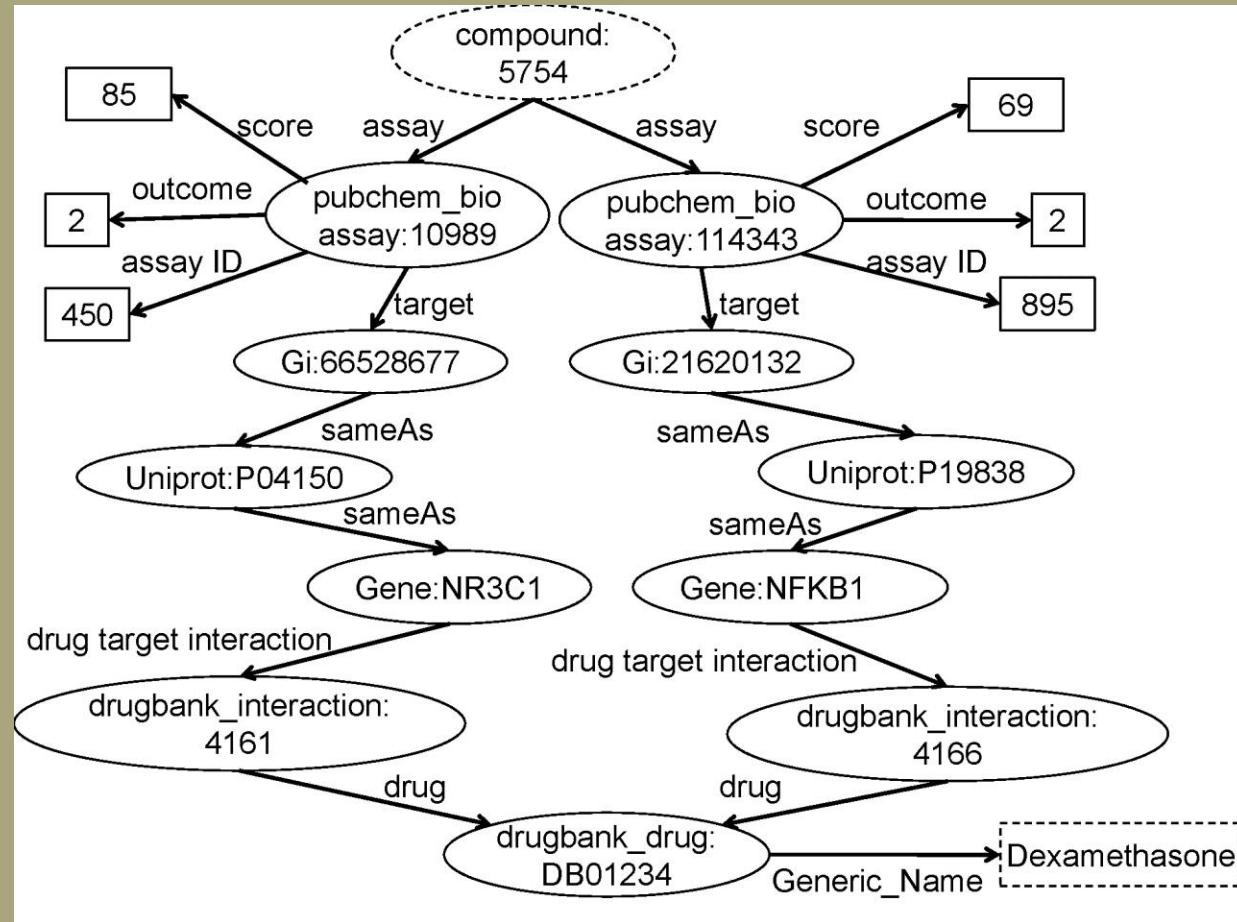
- The question and answers for the first two questions are shown during the quiz. See the projected slide.

# SPARQL Examples

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# SPARQL Examples

## Query for Adverse Drug Interactions



# SPARQL Examples

```
#Whole Database:  
SELECT ?s ?p ?o  
FROM <http://dbpedia.org>  
WHERE  
{?s ?p ?o}
```

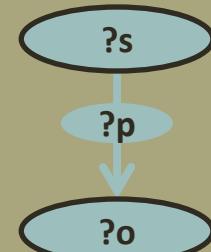
# SPARQL Examples

Return Variable

Triplestore

Condition

#Whole Database:  
SELECT ?s ?p ?o  
FROM <<http://dbpedia.org>>  
WHERE  
{?s ?p ?o}



You can get a text file with the SPARQL queries and links from Canvas.

# SPARQL Examples

- SPARQL Databases:

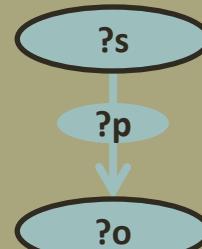
- <http://dbpedia.org/sparql>
- <http://lod.openlinksw.com/sparql/>

Return Variable

Triplestore

Condition

#Total number of triples:  
SELECT (COUNT(\*) AS ?NumberOfTriples)  
FROM <http://dbpedia.org>  
WHERE  
{?s ?p ?o}



# SPARQL Examples

- SPARQL Databases:
  - <http://dbpedia.org/sparql>

```
# Soccer players with more than 44 international goals
```

```
PREFIX property: <http://dbpedia.org/property/>
```

```
PREFIX oftype: <http://www.w3.org/1999/02/22-rdf-syntax-ns#type>
```

```
PREFIX FootballPlayer: <http://dbpedia.org/class/yago/FootballPlayer110101634>
```

```
PREFIX SoccerPlayer: <http://dbpedia.org/ontology/SoccerPlayer>
```

```
SELECT ?Player ?FootballClub (max(?NationalGoals) as ?NationalGoals)
```

Return  
Variables

```
FROM <http://dbpedia.org>
```

Triplestore

```
WHERE
```

```
{
```

```
?Player property:goals ?FootballGoals.
```

```
?Player property:nationalgoals ?NationalGoals.
```

```
?Player property:currentclub ?FootballClub.
```

```
?Player oftype: FootballPlayer:.
```

```
?Player oftype: SoccerPlayer:.
```

```
FILTER (?NationalGoals > 44 && ?NationalGoals < 1000)
```

Condition

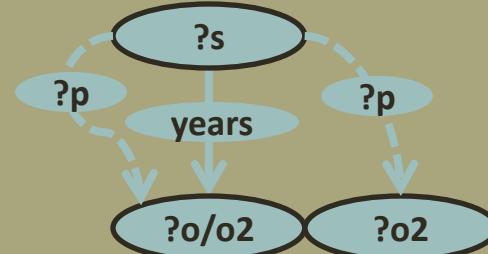
```
}ORDER BY DESC(?NationalGoals)
```

# SPARQL Examples

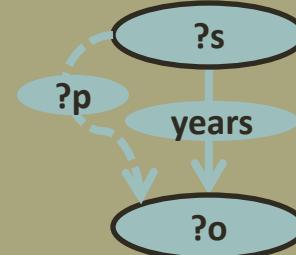
- SPARQL Databases:

- <http://dbpedia.org/sparql>
- <http://lod.openlinksw.com/sparql/>

Find all predicates that come from a node that is the subject for the predicate “years”



Find all predicates that connect nodes that are also connected by the predicate “years”



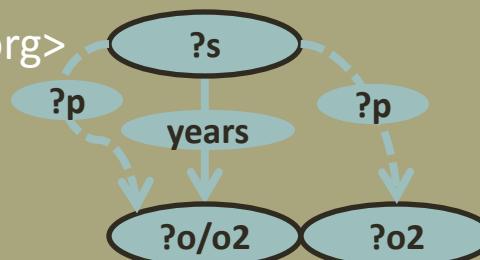
# SPARQL Examples

- SPARQL Databases:

- <http://dbpedia.org/sparql>
- <http://lod.openlinksw.com/sparql/>

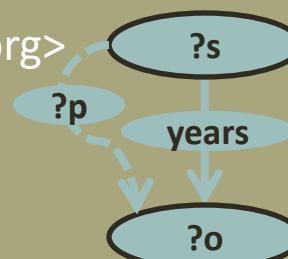
Find all predicates that come from a node that is the subject for the predicate “years”

PREFIX property: <http://dbpedia.org/property/>  
SELECT DISTINCT ?p  
FROM <http://dbpedia.org>  
WHERE {  
?s property:years ?o.  
?s ?p ?o2  
} limit 10



Find all predicates that connect nodes that are also connected by the predicate “years”

PREFIX property: <http://dbpedia.org/property/>  
SELECT DISTINCT ?p  
FROM <http://dbpedia.org>  
WHERE  
{?s property:years ?o .  
?s ?p ?o  
} limit 10



# SPARQL Examples

- SPARQL Databases:
  - <http://lod.openlinksw.com/sparql/>

```
# Get Tim Berners-Lee's email address
PREFIX foaf: <http://xmlns.com/foaf/0.1/>
SELECT DISTINCT ?name ?email
WHERE {
  ?person a foaf:Person .
  ?person foaf:name ?name .
  ?person foaf:mbox ?email .
  FILTER regex(?name, "Tim")}
```

# SPARQL Examples (6)

- SPARQL Database:
  - <http://librdf.org/query/>

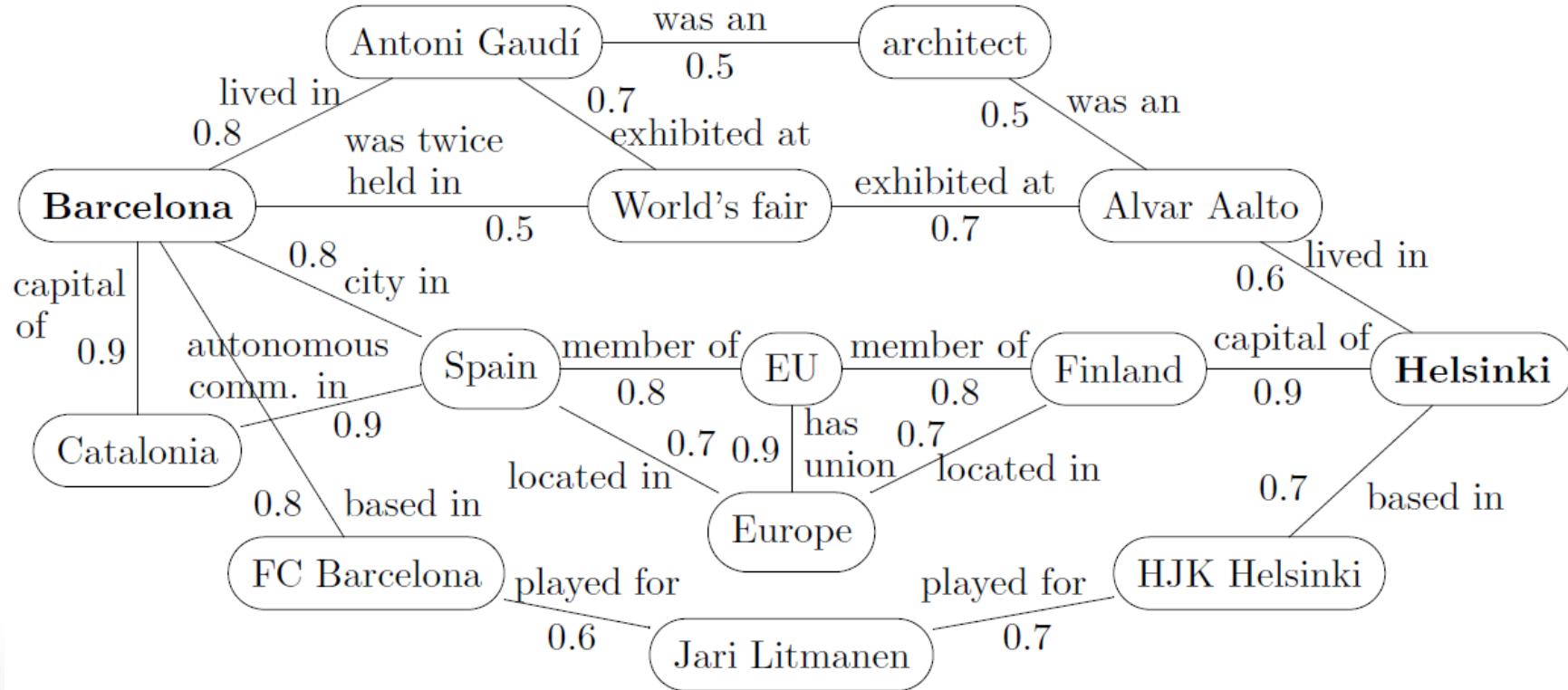
Set the RDF (database):

<http://www.daml.org/2003/01/periodictable/PeriodicTable.owl>

```
# Get data on noble gases
PREFIX table: <http://www.daml.org/2003/01/periodictable/PeriodicTable#>
PREFIX xsd: <http://www.w3.org/2001/XMLSchema#>
SELECT ?name ?symbol ?weight ?number
WHERE {
  ?element table:group ?group .
  ?group table:name "Noble gas"^^xsd:string .
  ?element table:name ?name .
  ?element table:symbol ?symbol .
  ?element table:atomicWeight ?weight .
  ?element table:atomicNumber ?number
}
ORDER BY ASC(?name)
```

No triplestore!  
The triplestore is implied.

# Future of SPARQL: Semantic Web with Weighted Edges?



# SPARQL Exercise 0

- Review the following slides for the SPARQL Quiz

# SPARQL Exercise 1

1. You have the following triple store  
<http://ImaginaryTripleStore.com>:

A X B

C X B

B X D

B Y E

F Y B

F X D

F Y E

E X D

G X E

2. You have the following SPARQL statement:

SELECT ?x

FROM

<http://ImaginaryTripleStore.com>

WHERE

{F ?p ?o .

?o ?p ?x}

## 3. Solution

3.1 List all items that fulfil “F ?p ?o”. Place them below the where clause.

F ?p ?o . ?o ?p ?x

F Y B

F X D

F Y E

3.2 List all items that fulfil “?o ?p ?x” where ?o is B, D, or E and ?p is Y. Place them below the where clause.

F ?p ?o . ?o ?p ?x

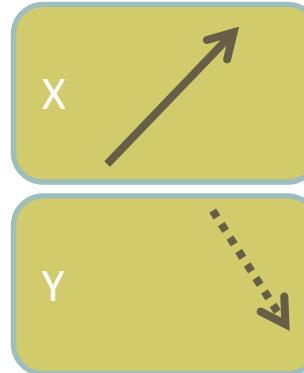
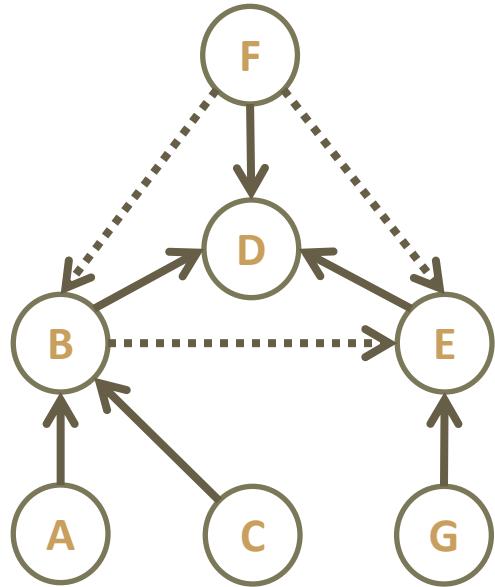
F Y B . B Y E

F X D

F Y E

3.3 List all items that were placed under “?x”

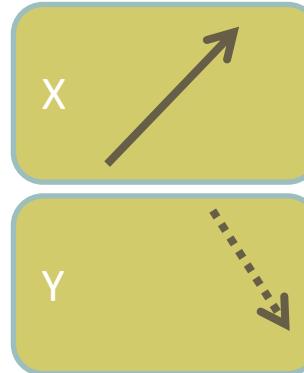
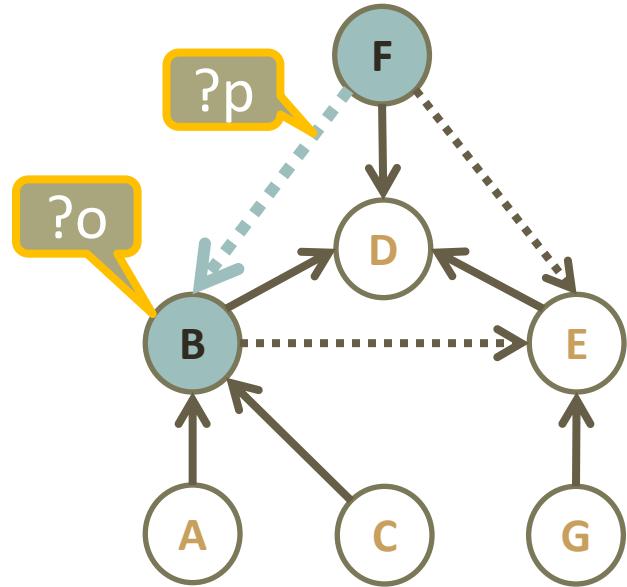
# SPARQL Exercise 1



2. You have the following SPARQL statement:

```
SELECT ?x  
FROM  
<http://ImaginaryTripleStore.com>  
WHERE  
{F ?p ?o .  
?o ?p ?x}
```

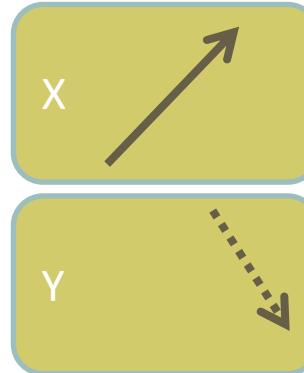
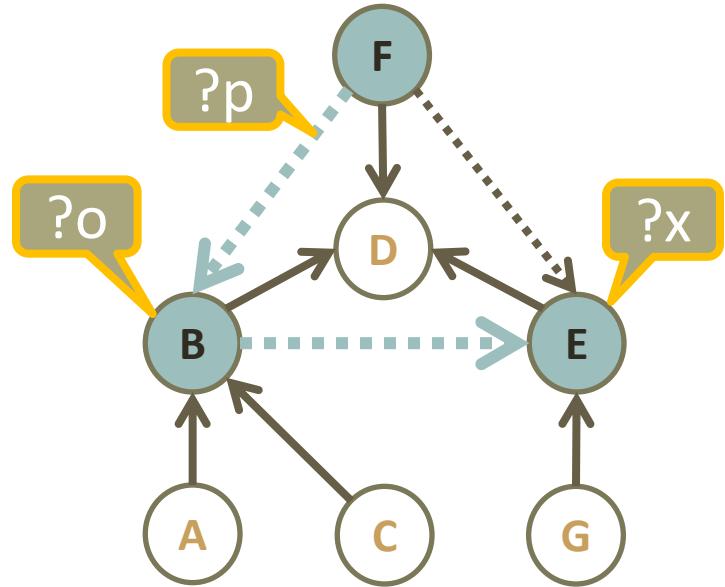
# SPARQL Exercise 1



2. You have the following SPARQL statement:

```
SELECT ?x  
FROM  
<http://ImaginaryTripleStore.com>  
WHERE  
{F ?p ?o .  
?o ?p ?x}
```

# SPARQL Exercise 1



2. You have the following SPARQL statement:

```
SELECT ?x  
FROM  
<http://ImaginaryTripleStore.com>  
WHERE  
{F ?p ?o .  
?o ?p ?x}
```

# SPARQL Exercise 2

1. You have the following triple store  
<http://ImaginaryTripleStore.com>:

A X B

C X B

B X D

B Y E

F Y B

F X D

F Y E

E X D

G X E

2. You have the following SPARQL statement:

```
SELECT ?s
FROM
<http://ImaginaryTripleStore.com>
WHERE
{?s Y ?o .
?o X D}
```

## 3. Solution

3.1 Look at the 2nd triple from the where clause first. Find all triplets that use X as a predicate where the object is D (fulfils “?o X D”). Place them below the where clause:

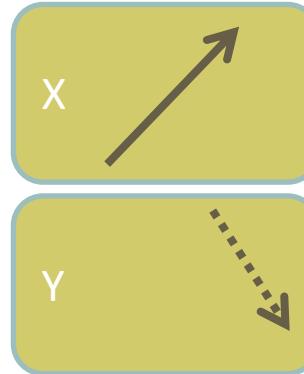
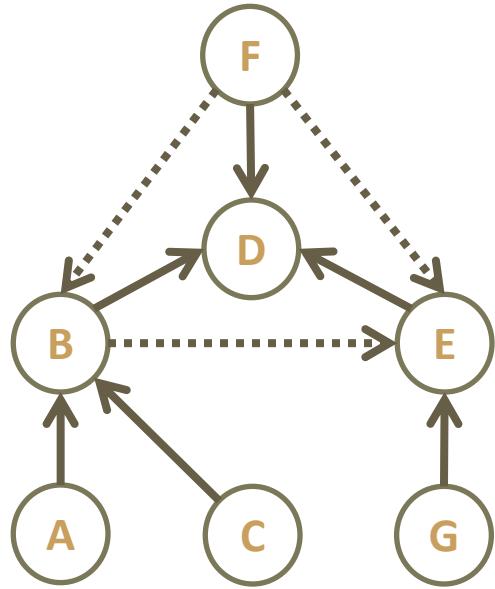
```
?s Y ?o . ?o X D
      B X D
      F X D
      E X D
```

3.2 The subject of the above triplets are: B, F, and E. Now, look at the first triplet of the where clause. Look for all triplets that have an object that is B, F, or E and that have a predicate Y (fulfils “?s Y ?o”). Place those triplets below the where clause:

```
?s Y ?o . ?o X D
      F Y B B X D
                  F X D
      F Y E E X D
      B Y E E X D
```

3.3 List all items that were placed under “?s”

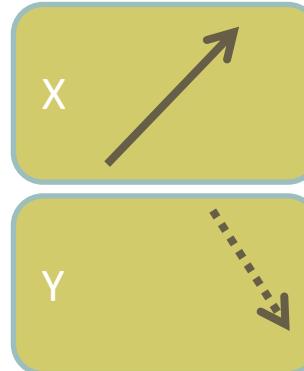
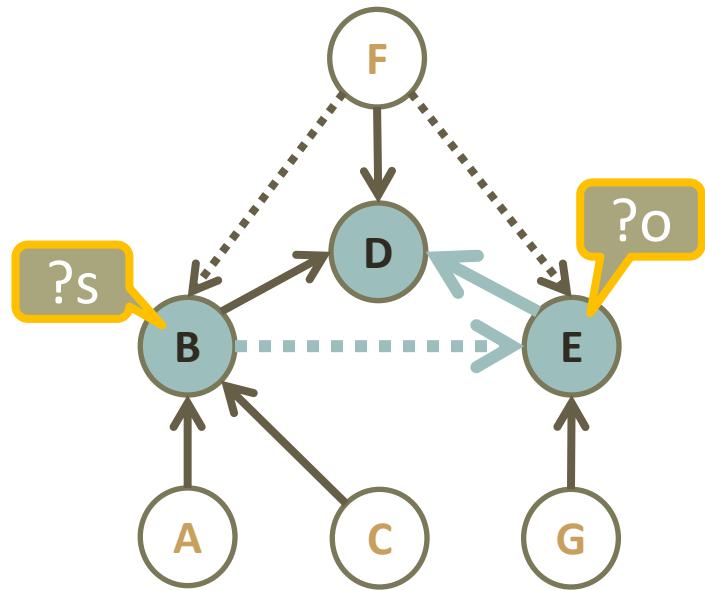
# SPARQL Exercise 2



2. You have the following SPARQL statement:

```
SELECT ?s  
FROM  
<http://ImaginaryTripleStore.com>  
WHERE  
{?s Y ?o .  
?o X D}
```

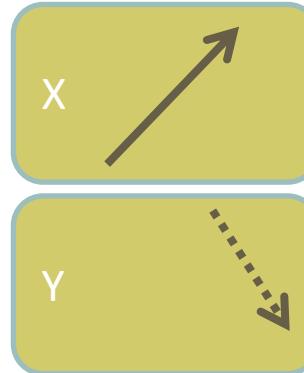
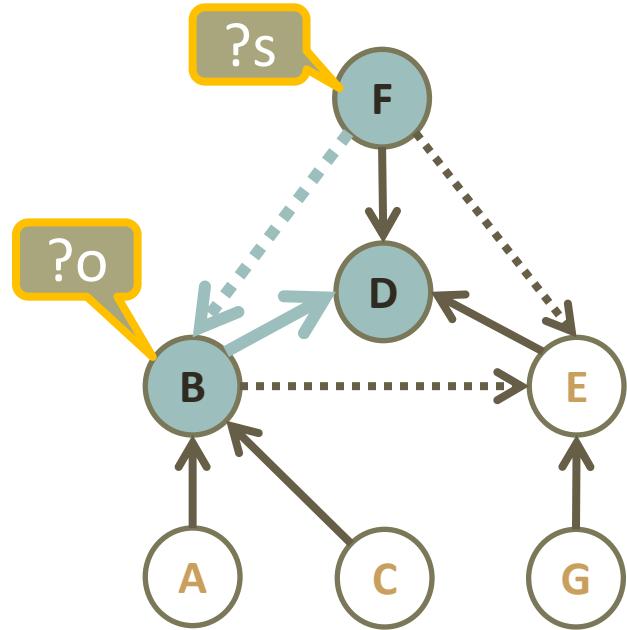
# SPARQL Exercise 2



2. You have the following SPARQL statement:

```
SELECT ?s  
FROM  
<http://ImaginaryTripleStore.com>  
WHERE  
{?s Y ?o .  
?o X D}
```

# SPARQL Exercise 2



2. You have the following SPARQL statement:

```
SELECT ?s  
FROM  
<http://ImaginaryTripleStore.com>  
WHERE  
{?s Y ?o .  
?o X D}
```

# SPARQL Examples

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# Assignment

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# Assignment

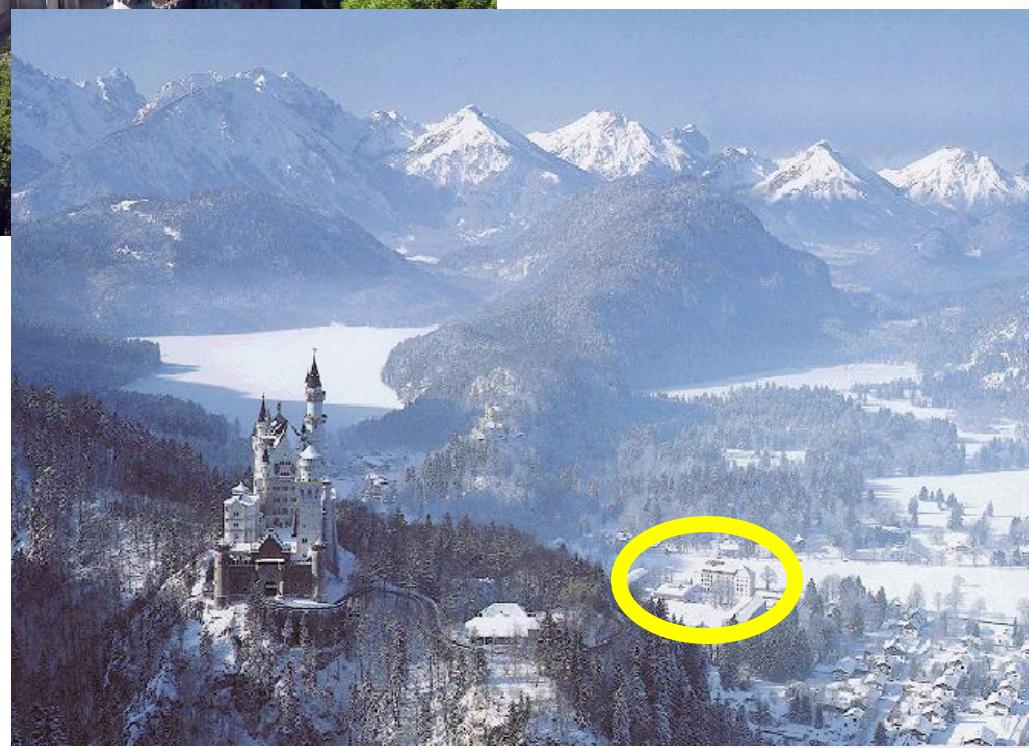
1. Comment in our LinkedIn Group on a discussion about statistics. Copy the post to a text file called post.txt. This assignment item is similar to last week's assignment.
2. Submit to Canvas by Saturday 11:57 PM post.txt.
3. Look at the SPARQL Exercises and then take the SPARQL Quiz by Saturday 11:57 PM. It is a difficult quiz you may need an hour.
4. Stats
  - a) Look at Verzani 's book: <https://cran.r-project.org/doc/contrib/Verzani-SimpleR.pdf>
  - b) Play with theses functions in R and figure out their relationships: rnorn, dnorm, pnorm, qnorm (Nothing to submit for this item)

# Assignment

(188)



Summer's  
Vacation Spot



Thank You!

# Introduction to Data Science

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