

Ryan Timbrook
Data Science 350 – Homework Assignment 6

Assignment:

Probability of texting. – You are asked to compute the probability that the driver of a car is texting at a specific intersection. –

Nationally the cumulative probability that a driver is texting is:

> $P = 0.5$, at $x = 0.1$

> $P = 0.75$ at $x = 0.3$

– You observe cars at a location three times and note the number of texting drivers:

1. 2 texting out of 20 drivers

2. 4 texting out of 20 drivers

3. 1 texting out of 20 drivers

> Given these data

– Compute the Beta prior, and report the coefficients

– Plot the prior, likelihood and posterior three times as you update your belief based on collecting more data

– Simulate the final posterior distribution and do the following:

> Plot the posterior with the 90% HDI shown

> Report the upper and lower limits of the 90% HDI

> Of the next hundred drivers what are the number of texting drivers in the 90% HDI?

> Are the drivers in this area better or worse than the national figures indicate?

Observations:

- As more observations occur and are added to the model, the posterior distribution moves closer to the likelihood as expected. This is reflected in Table 1's Bay's Triplots graphs below.
- The final posterior distribution's 90% HDI's upper and lower limits are:
 - Lower Limits: 5% 0.0589697266018973
 - Upper Limits: 95% 0.192268807963088

These observations are reflected in Table 2 below.

- There are 17 drivers of the next 100 that are texting in the 90% HDI. This is reflected in Table 3.1 below.
- The drivers in this area appear to be on par with the national average indicated above. This is reflected in Table 3.2 below.

Table 1: Plots of the prior, likelihood and posterior for each observation

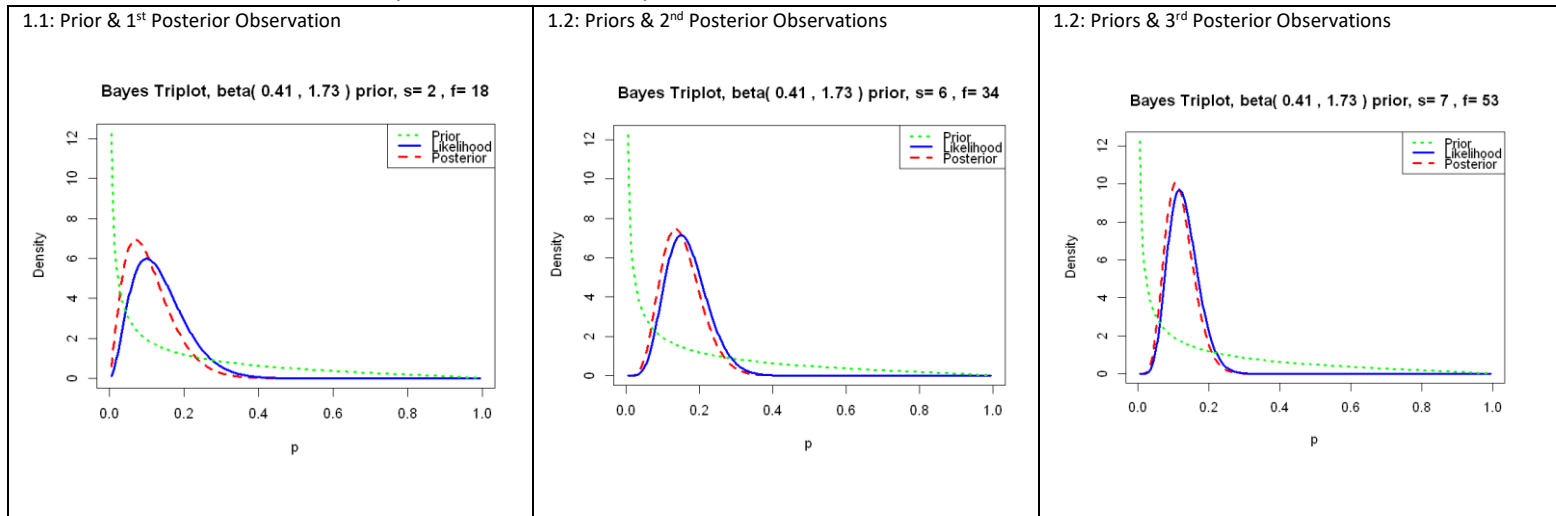


Table 2: Simulation of the final posterior distribution, plotted at 90% HDI

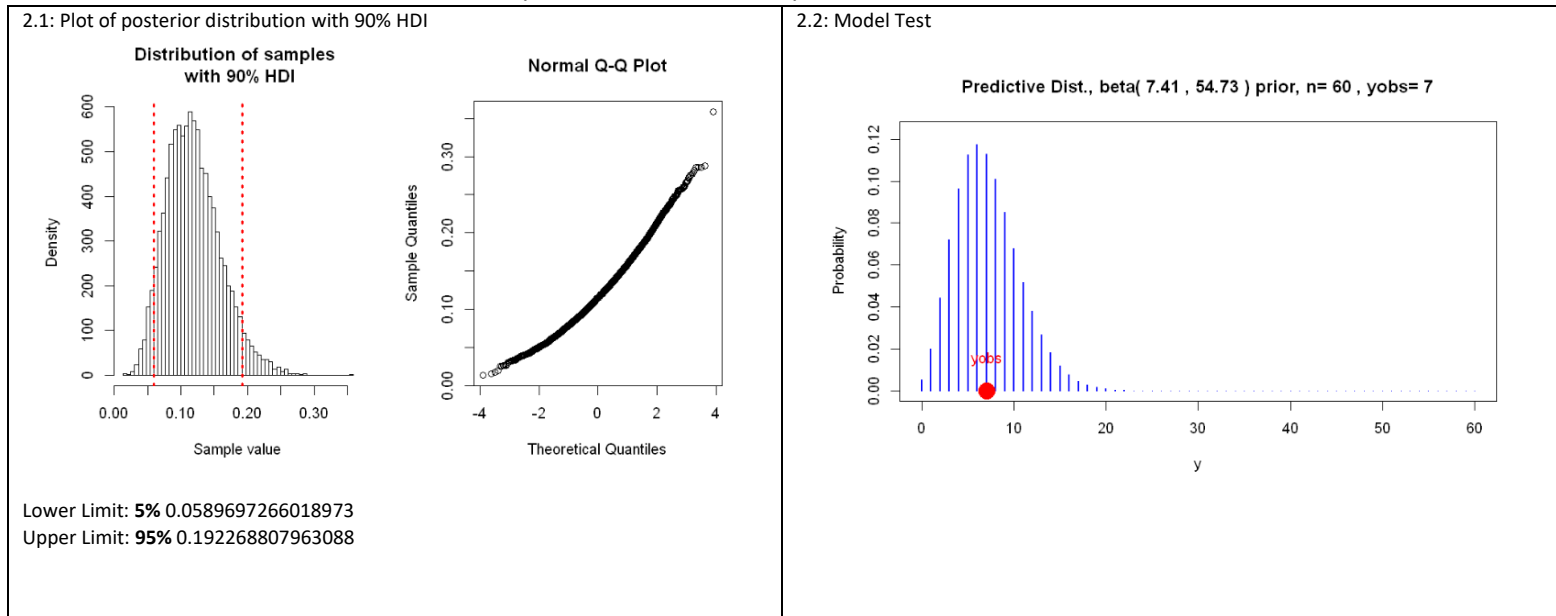
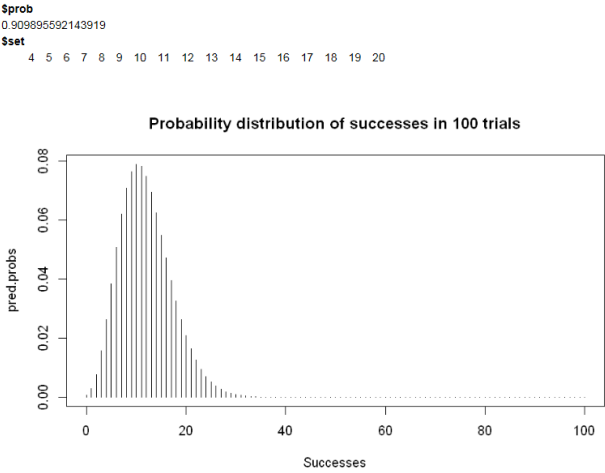


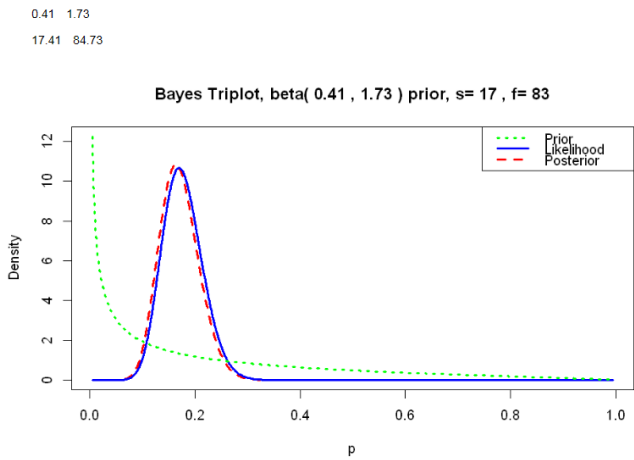
Table 3: Next hundred drivers texting in the 90% HDI

3.1: Next 100 Drivers



17 drivers are texting in the 90% HDI

3.2: National Average as prior and Next Hundred as posterior



These drivers appear to be in par with the national average