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**NPTEL** (<https://swayam.gov.in/explorer?ncCode=NPTEL>) » **Robotics and Control: Theory and Practice (course)**

 Announcements (announcements)    **About the Course** ([https://swayam.gov.in/nd1\\_noc20\\_me03/preview](https://swayam.gov.in/nd1_noc20_me03/preview))

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## Unit 3 - Week 2

### Course outline

#### How does an NPTEL online course work?

#### Week 1

#### Week 2

- Kinematic Model for Robot Manipulator (unit? unit=55&lesson=58)
- Direct Kinematics (unit? unit=55&lesson=59)
- Inverse Kinematics (unit? unit=55&lesson=60)
- Manipulator Jacobian (unit? unit=55&lesson=61)
- Manipulator Jacobian Example (unit? unit=55&lesson=62)
- **Quiz : Assignment 2 (assessment? name=83)**
- Solution For Assignment 2

## Assignment 2

The due date for submitting this assignment has passed.

Due on 2020-02-12, 23:59 IST.

### Assignment submitted on 2020-02-08, 15:16 IST

1) If a point  $p(x, y, z)$  in a coordinate frame rotates about the  $z$  -  $axis$  with angular velocity 0.01 rad. per **1 point** second, then



$$\dot{x} = 0.01y, \dot{y} = -0.01x$$



$$\dot{x} = -0.01y, \dot{y} = 0.01x$$



$$\dot{x} = -0.01x, \dot{y} = 0.01y$$



$$\dot{x} = 0.01x, \dot{y} = -0.01y$$

No, the answer is incorrect.  
Score: 0

Accepted Answers:

$$\dot{x} = -0.01y, \dot{y} = 0.01x$$

2) If the  $z_{k-1}$  and  $z_k$  axes of a robot joint coordinate frames are non intersecting then:

**1 point**

$x_k$  is the common normal to  $z_{k-1}$  and  $z_k$ .



$x_{k-1}$  is the common normal to  $z_{k-1}$  and  $z_k$ .



$y_k$  is parallel to  $z_{k-1}$ .



$y_{k-1}$  is parallel to  $z_{k-1}$ .

(unit?  
unit=55&lesson=91)

Week 3

Week 4

Week 5

Week 6

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Yes, the answer is correct.

Score: 1

Accepted Answers:

$x_k$  is the common normal to  $z_{k-1}$  and  $z_k$ .

3) If  ${}^{i-1}T_i : i = 1, 2, \dots, n$  denotes  $i^{th}$  coordinate frame with respect to  $i - 1^{th}$  coordinate frame of a  $n$  dof manipulator, then the  $k^{th}$  column of the Jacobian matrix is obtained using: **1 point**

☐

${}^0T_k$

☐

${}^kT_n$

☐

${}^{k-1}T_k$

☒

${}^{k-1}T_n$

Yes, the answer is correct.

Score: 1

Accepted Answers:

${}^{k-1}T_n$

4) The homogeneous transformation matrix representing the  $k^{th}$  joint frame with respect to  $k - 1^{th}$  joint frame of a robot manipulator is given by  ${}^{k-1}T_k =$ : **1 point**

☒

$$\begin{bmatrix} \cos\theta_k & -\cos\alpha_k \sin\theta_k & \sin\alpha_k \sin\theta_k & a_k \cos\theta_k \\ \sin\theta_k & \cos\alpha_k \cos\theta_k & -\sin\alpha_k \cos\theta_k & a_k \sin\theta_k \\ 0 & \sin\alpha_k & \cos\alpha_k & d_k \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

☐

$$\begin{bmatrix} \cos\theta_k & \cos\alpha_k \sin\theta_k & \sin\alpha_k \sin\theta_k & a_k \cos\theta_k \\ \sin\theta_k & -\cos\alpha_k \cos\theta_k & -\sin\alpha_k \cos\theta_k & a_k \sin\theta_k \\ 0 & \sin\alpha_k & \cos\alpha_k & d_k \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

☐

$$\begin{bmatrix} \cos\theta_k & -\cos\alpha_k \sin\theta_k & -\sin\alpha_k \sin\theta_k & a_k \cos\theta_k \\ \sin\theta_k & \cos\alpha_k \cos\theta_k & \sin\alpha_k \cos\theta_k & a_k \sin\theta_k \\ 0 & \sin\alpha_k & \cos\alpha_k & d_k \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

☐

$$\begin{bmatrix} \cos\theta_k & -\cos\alpha_k \sin\theta_k & \sin\alpha_k \sin\theta_k & a_k \cos\theta_k \\ \sin\theta_k & \cos\alpha_k \cos\theta_k & -\sin\alpha_k \cos\theta_k & a_k \sin\theta_k \\ 0 & \cos\alpha_k & \sin\alpha_k & d_k \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Yes, the answer is correct.

Score: 1

Accepted Answers:

$$\begin{bmatrix} \cos\theta_k & -\cos\alpha_k \sin\theta_k & \sin\alpha_k \sin\theta_k & a_k \cos\theta_k \\ \sin\theta_k & \cos\alpha_k \cos\theta_k & -\sin\alpha_k \cos\theta_k & a_k \sin\theta_k \\ 0 & \sin\alpha_k & \cos\alpha_k & d_k \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

5) Kinematic equations of a 3 axis manipulator are given as: **0 points**

$$x = [l_2 \cos\theta_2 + l_3 \cos(\theta_2 + \theta_3)] \cos\theta_1$$

$$y = [l_2 \cos \theta_2 + l_3 \cos(\theta_2 + \theta_3)] \sin \theta_1$$

$$z = l_1 + l_2 \sin \theta_2 + l_3 \sin(\theta_2 + \theta_3)$$

Then  $\cos \theta_3$  is:



$$\frac{x^2 + y^2 + (z - l_1)^2 - l_2^2 - l_3^2}{-2l_2 l_3}$$



$$\frac{x^2 + y^2 + (z - l_1)^2 - l_2^2 - l_3^2}{2l_2 l_3}$$



$$\frac{x^2 + y^2 + (z - l_1)^2 + l_2^2 - l_3^2}{-2l_2 l_3}$$



$$\frac{x^2 + y^2 + (z - l_1)^2 - l_2^2 + l_3^2}{-2l_2 l_3}$$

Yes, the answer is correct.

Score: 0

Accepted Answers:

$$\frac{x^2 + y^2 + (z - l_1)^2 - l_2^2 - l_3^2}{2l_2 l_3}$$

6) The joint co-ordinate transformations of a robot manipulator are given below:

1 point

$${}^0T_1 = \begin{bmatrix} \cos \theta_1 & 0 & -\sin \theta_1 & 0 \\ \sin \theta_1 & 0 & \cos \theta_1 & 0 \\ 0 & -1 & 0 & 10 \\ 0 & 0 & 0 & 1 \end{bmatrix}, {}^1T_2 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & -1 & 0 & q_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}, {}^2T_3 = \begin{bmatrix} \cos \theta_3 & -\sin \theta_3 & 0 & 0 \\ \sin \theta_3 & \cos \theta_3 & 0 & 0 \\ 0 & 0 & 1 & 5 \\ 0 & 0 & 0 & 1 \end{bmatrix}, 0 \leq q_2 \leq$$

The arm matrix  $T = {}^0T_3$  at  $\theta_1 = 0$ ,  $q_2 = 3$  and  $\theta_3 = \pi/2$  is given by:



$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 3 \\ 0 & -1 & 0 & -5 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



$$\begin{bmatrix} 0 & 0 & 0 & 3 \\ -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & -5 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



$$\begin{bmatrix} 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 3 \\ 0 & 0 & -1 & 5 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



$$\begin{bmatrix} 1 & 0 & 0 & 3 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & -1 & -5 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Yes, the answer is correct.

Score: 1

Accepted Answers:

$$\begin{bmatrix} 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 3 \\ 0 & 0 & -1 & 5 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

7)  $\frac{\partial T}{\partial q_2}$  in (6) for mentioned values is given by:

1 point



$$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$



$$\begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$



$$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -5 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$



$$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

No, the answer is incorrect.  
Score: 0

Accepted Answers:

$$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

8) Second column of manipulator jacobian in (6) for mentioned values is given by:

1 point



$$[0 \quad -1 \quad 0 \quad 0 \quad 0 \quad 0]^T$$



$$[-1 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0]^T$$



$$[0 \quad 1 \quad 0 \quad 0 \quad 0 \quad 0]^T$$



$$[1 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0]^T$$

Yes, the answer is correct.  
Score: 1

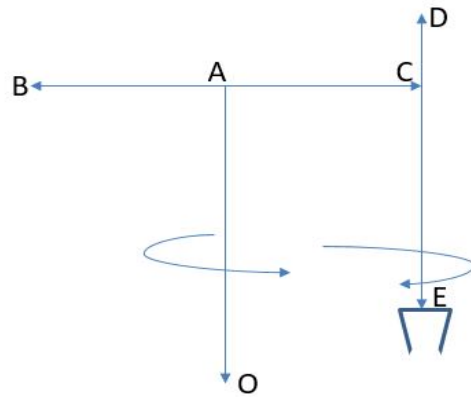
Accepted Answers:

$$[-1 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0]^T$$

9)

1 point

For the manipulator shown below,  $OA=15$ ,  $BC=10$ ,  $DE=15$ .



Joint variables are given by  $\theta_1$ ,  $d_2$ ,  $d_3$  and  $\theta_4$ . If the position and orientation of the end-effector E with respect to base O is given by:

$$\begin{bmatrix} 1/\sqrt{2} & 1/\sqrt{2} & 0 & 4 \\ 1/\sqrt{2} & -1/\sqrt{2} & 0 & 3 \\ 0 & 0 & -1 & 9 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

What is value of  $\theta_1 + \theta_4$ . Here O and E are revolute joints and A and C are prismatic?



$$\theta_1 = \pi/4$$



$$\theta_1 = \pi/2$$



$$\theta_1 = -\pi/4$$



$$\theta_1 = -\pi/2$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$\theta_1 = -\pi/4$$

10) In previous question (9), distance variables  $d_2$  and  $d_3$  are:

**1 point**



5 & 6 respectively.



5 & 9 respectively.



4 & 6 respectively.



4 & 9 respectively.

Yes, the answer is correct.

Score: 1

Accepted Answers:

5 & 6 respectively.

