

PS2 Questions

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Add your answers to this file in plain text after each question. Leave a blank line between the text of the question and the text of your answer and at least two lines between your answer and the next question.

```
.. role:: cpp(code)
```

```
:language: c++
```

Inner Product

1. How would you use `:cpp:`dot`` to implement `:cpp:`two_norm``?

To implement `two_norm` using `dot`, we take the dot product of the vector with itself. After this, we take the square root of the result. The `two_norm_d` function in `amath583.cpp` implements this logic.

Tensors

2. What is the formula that we would use for indexing if we wanted "slab-major" ordering? Hint: What is the size of a slab? It might be helpful to draw a picture of the data in 3D and see what the size is of a slab.

We want to do slab-major ordering. We assume the dimensions of Tensor are $[L, M, N]$.

$L = \text{num_slabs_}$, $M = \text{num_rows_}$, $N = \text{num_cols_}$.

For a 2d row-major matrix with dimensions $[\text{num_rows_}, \text{num_cols_}]$, we know element at $[i, j] = j + i * \text{num_cols_}$. j is used to index within a row and i is used to jump rows. We can see that index j changes the fastest. We can build on this to find the location of element $[i, j, k]$ in the Tensor in slab-major order.

k will be used to index within a slab, now we think of each slab as a matrix. In this case, index k will change the fastest and index i will change the slowest.

$j * \text{num_cols_}$ will be used to jump rows and $i * \text{num_rows_} * \text{num_cols_}$ will be used to jump the matrix within each slab.

So indexing strategy is $k + j * \text{num_cols_} + i * \text{num_rows_} * \text{num_cols_}$

This is how we will implement the indexing methods in Tensor class:

```
double& operator()(size_t i, size_t j, size_t k) {  
    return storage_[k + num_cols_*j + i*num_rows_* num_cols_];  
}  
  
const double& operator()(size_t i, size_t j, size_t k) const {  
    return storage_[ k + num_cols_*j + i*num_rows_* num_cols_];  
}
```

3. (Extra credit.) I claim that there are six distinct indexing formulas. Show that this claim is correct or that it is incorrect.

Tensor has 3 dimensions, and each element is uniquely identified by specifying a value for each of the 3 dimensions. The order of specifying these could be anything thereby leading us to $3!$ combinations, which is 6 in total.

The claim is correct.