

2 What is a Wave?

Fundamental Concepts

1. A wave requires a disturbance, and a medium that can transfer energy
2. Waves are categorized as longitudinal or transverse (or a combination of the two).

What is a Wave?

Spring Demo

Waves are organized motions in a medium.

Criteria for being a wave

Question 223.2.1

Question 223.2.2

Another way to think about waves is a transfer of energy through space without transfer of matter.

Spring Demo-
marked part

Waves require:

1. some source of disturbance
2. a medium that can be disturbed
3. some physical mechanism by which the elements of the medium can influence each other

In the limit that the string mass is negligible we represent a one-dimensional wave mathematically as a function of two variables, position and time, $y(x, t)$. There are two ways to look at waves, we call them “snapshot” and “history” (or video) views.

Longitudinal vs. transverse

Question 223.2.3

We divide the various kinds of waves that occur into two basic types:

Question 223.2.4

Question 223.2.5

Definition 2.1 *transverse wave: a traveling wave or pulse that causes the elements of the disturbed medium to move perpendicular to the direction of propagation*

Definition 2.2 *Longitudinal wave: a traveling wave or pulse that causes the elements of the medium to move parallel to the direction of propagation*



Transverse Wave

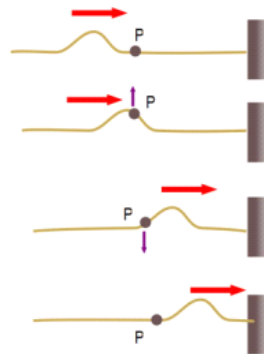


Longitudinal Wave

Long Spring Demo

Examples of waves:

A pulse on a rope:

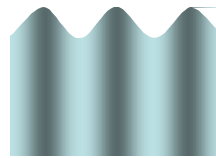


In the picture above, you see wave that has just one peak traveling to the right. We call such a wave a *pulse*. Notice how the piece of the rope marked *P* moves up and down,

but the wave is moving to the right. This pulse is a transverse wave because the parts of the medium (observe point P) move perpendicular to the direction the wave is moving.

An ocean wave:

Of course, some waves are a combination of these two basic types⁴. Water waves, for example, are transverse at the surface of the water, but are longitudinal throughout the water.



Earthquake waves:

Earthquakes produce both transverse and longitudinal waves. The two types of waves even travel at different speeds! P waves are longitudinal and travel faster, S waves are transverse and slower.

Wave speed

Question 223.2.6

Question 223.2.7

Question 223.2.8

We can perform an experiment with a rope or a long spring. Make a wave on the rope or spring. Then pull the rope or spring tighter and make another wave. We see that the wave on the tighter spring travels faster.

It is harder to do, but we can also experiment with two different ropes, one light and one heavy. We would find that the heavier the rope, the slower the wave. We can express this as

$$v = \sqrt{\frac{T_s}{\mu}}$$

where T_s is the tension in the rope, and μ is the linear mass density

$$\mu = \frac{m}{L}$$

where m is the mass of the rope, and L is the length.

⁴ You may have noticed that in Physics we tend to define basic types of things, and then use these basic types to define more complex objects.

The term μ might need an analogy to make it seem helpful. So suppose I have an iron bar that has a mass of 200 kg and is 2 m long. Further suppose I want to know how much mass there would be in a 20 cm section cut of the end of the rod. How would I find out?

This is not very hard, We could say that there are 200 kg spread out over 2 m, so each meter of rod has 100 kg of mass, that is, there is 100 kg/m of mass per unit length.

Then to find how much mass there is in a 0.20 m section of the rod I take

$$m = 100 \frac{\text{kg}}{\text{m}} \times 0.20 \text{ m} = 20.0 \text{ kg}$$

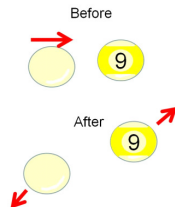
The 100 kg/m is μ . It is how much mass there is in a unit length segment of something. In this example, it is a unit length of iron bar, but for waves on string, we want the mass per unit length of string.

If you are buying stock steel bar, you might be able to buy it with a mass per unit length. If the mass per unit length is higher then the bar is more massive. The same is true with string. The larger μ , the more massive equal string segments will be.

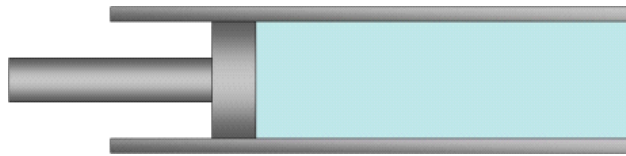
We should note that in forming this relationship, we have used our standard introductory physics assumption that the mass of the rope can be neglected. Let's consider what would happen if this were not true. Say we make a wave in a heavy cable that is suspended. The mass at the lower end of the cable pulls down on the upper part of the cable. The tension will actually change along the length of the cable, and so will the wave speed. Such a situation can't be represented by a single wave speed. But for our class, we will assume that any such changes are small enough to be ignored.

Example: Sound waves

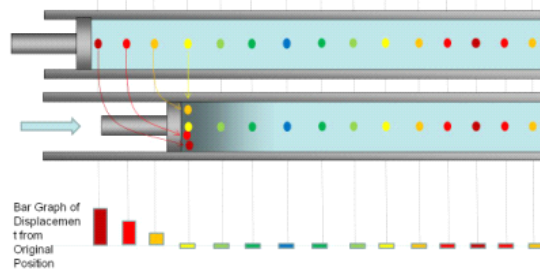
Sound is a wave. The medium is air particles. The transfer of energy is done by collision.



The wave will be a longitudinal wave. Let's see how it forms. We can take a tube with a piston in it.

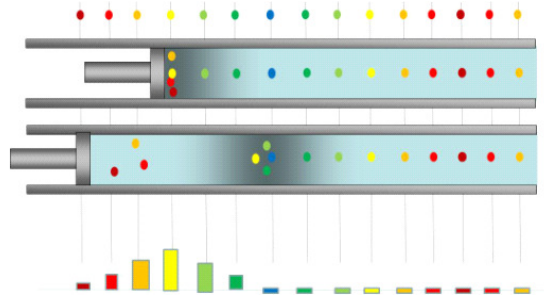


As we exert a force on the piston, the air molecules are compressed into a group. In the next figure, each dot represents a group of air molecules. In the top picture, the air molecules are not displaced. But when the piston moves, the air molecules receive energy by collision. They bunch up. We see this in the second picture.

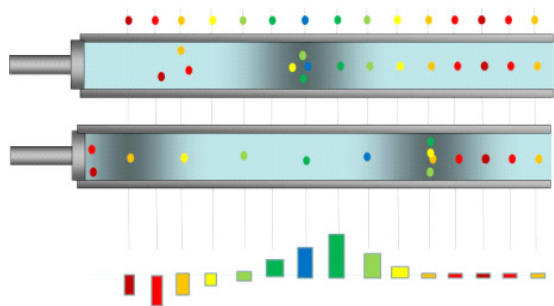


The graph below the two pictures shows how much displacement each molecule group experiences.

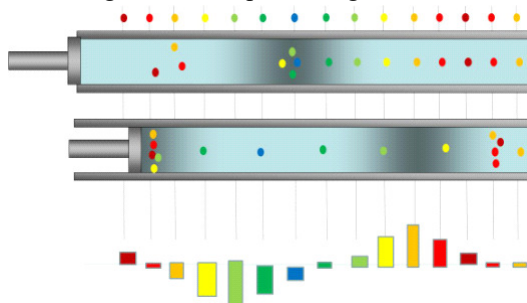
Suppose we now pull the piston back. This would allow the molecules to bounce back to the left, but the molecules that they have collided with will receive some energy and go to the right. This is shown in the next figure. Color coded dots are displayed above the before and after picture so you can see where the molecule groups started.



If we pull the piston back further, the molecules can pass their original positions.



Then we can push inward again and compress the gas.



This may seem like a senseless thing to do, but it is really what a speaker does to produce sound. In particular, a speaker is a harmonic oscillator. The simple harmonic motion of the speaker is the disturbance that makes the sound wave.



One dimensional waves

Question 223.2.9

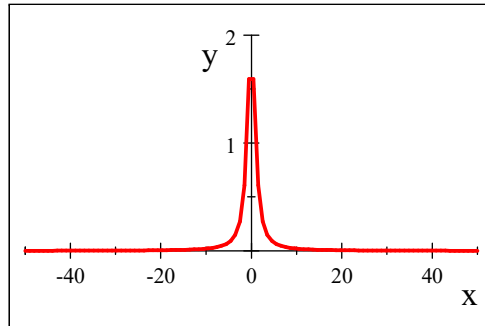
To mathematically describe a wave we will define a function of both time and position.

$$y(x, t) \quad (2.1)$$

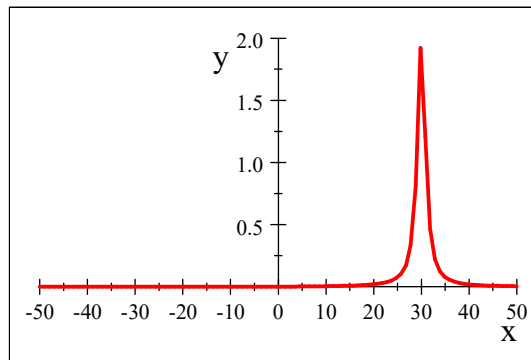
let's take a specific example⁵

$$y = \frac{2}{(x - 3.0t)^2 + 1} \quad (2.2)$$

Let's plot this for $t = 0$



what will this look like for $t = 10$?



The pulse travels along the x -axis as a function of time. We denote the speed of the pulse as v , then we can define a function

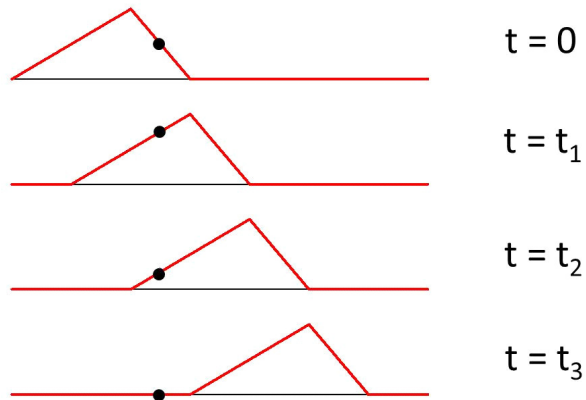
$$y(x, t) = y(x - vt, 0) \quad (2.3)$$

that describes a pulse as it travels. An element of the medium (rope, string, etc.) at position x at some time t , will have the displacement that an element had earlier at $x - vt$ when $t = 0$.

We will give $y(x - vt, 0)$ a special name, the *wave function*. It represents the y position, the transverse position in our example, of any element located at a position x at any time t .

⁵ This is not an important wave function, just one I picked because it makes a nice graphic example.

Notice that wave functions depend on two variables, x , and t . It is hard to draw a wave so that this dual dependence is clear. Often we draw two different graphs of the same wave so we can see independently the position and time dependence. So far we have used one of these graphs. A graph of our wave at a specific time, t_o . This gives $y(x, t_o)$. This representation of a wave is very like a photograph of the wave taken with a digital camera. It gives a picture of the entire wave, but only for one time, the time at which the photograph was taken. Of course we could take a series of photographs, but still each would be a picture of the wave at just one time.



Question 223.2.10

The second representation is to observe the wave at just one point in the medium, but for many times. This is very like taking a video camera and using it to record the displacement of just one part of the medium for many times. You could envision marking just one part of a rope, and then using the video recorder to make a movie of the motion of that single part of the rope. We could then go frame by frame through the video, and plot the displacement of our marked part of the rope as a function of time. Such a graph is sometimes called a history graph of the wave.

