# **NEWTON'S LAWS OF MOTION**

# From third law of motion

$$\vec{F}_{AB}\,=-\vec{F}_{BA}$$

$$\vec{F}_{AB}$$
 = Force on A due to B

$$\vec{F}_{BA}$$
 = Force on B due to A

#### 2. From second law of motion

$$F_x = \frac{dP_x}{dt} = ma_x$$
  $F_y = \frac{dP_y}{dt} = ma_y$   $F_z = \frac{dP_z}{dt} = ma_z$ 

$$F_y = \frac{dP_y}{dt} = ma_y$$

$$F_z = \frac{dP_z}{dt} = ma_z$$

### **5**. **WEIGHING MACHINE:**

A weighing machine does not measure the weight but measures the force exerted by object on its upper surface.

$$\vec{F} = -k\vec{x}$$

x is displacement of the free end from its natural length or deformation of the spring where K = spring constant.

7. SPRING PROPERTY 
$$K \times \ell$$
 = constant

= Natural length of spring.

### 8. If spring is cut into two in the ratio m: n then spring constant is given by

$$\ell_1 = \frac{m\ell}{m+n}$$
;  $\ell_2 = \frac{n.\ell}{m+n}$ 

$$\mathbf{k}\ell = \mathbf{k_1}\ell_1 = \mathbf{k_2}\ell_2$$

For series combination of springs

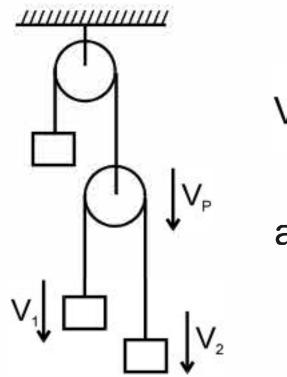
$$\frac{1}{k_{eq}} = \frac{1}{k_1} + \frac{1}{k_2} + \dots$$

For parallel combination of spring

$$k_{eq} = k_1 + k_2 + k_3 \dots$$

### 9. **SPRING BALANCE:**

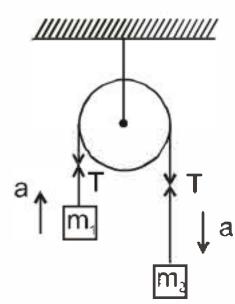
It does not measure the weight. It measures the force exerted by the object at the hook.



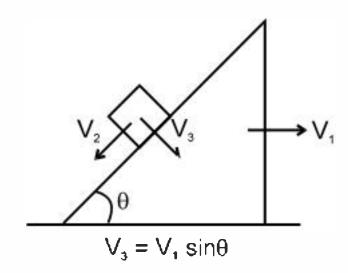
$$V_p = \frac{V_1 + V_2}{2}$$

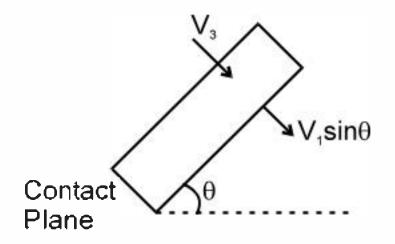
11. 
$$a = \frac{(m_2 - m_1)g}{m_1 + m_2}$$

$$T=\frac{2m_1m_2g}{m_1+m_2}$$



## 12. WEDGE CONSTRAINT:





Components of velocity along perpendicular direction to the contact plane of the two objects is always equal if there is no deformations and they remain in contact.

# 13. NEWTON'S LAW FOR A SYSTEM

$$\vec{F}_{ext} = m_1 \vec{a}_1 + m_2 \vec{a}_2 + m_3 \vec{a}_3 + \dots$$

 $\vec{F}_{ext}$  = Net external force on the system.

 $m_1$ ,  $m_2$ ,  $m_3$  are the masses of the objects of the system and  $\bar{a}_1$ ,  $\bar{a}_2$ ,  $\bar{a}_3$  are the acceleration of the objects respectively.

# 14. NEWTON'S LAW FOR NON INERTIAL FRAME:

$$\vec{F}_{Real} + \vec{F}_{Pseudo} = m\vec{a}$$

Net sum of real and pseudo force is taken in the resultant force.

 $\vec{a}$  = Acceleration of the particle in the non inertial frame

$$\vec{F}_{Pseudo} = - m \vec{a}_{Frame}$$

- (a) Inertial reference frame: Frame of reference moving with constant velocity.
- (b) Non-inertial reference frame: A frame of reference moving with non-zero acceleration.