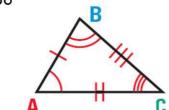
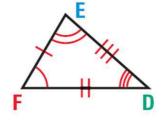
Congruence Statement

When naming two congruent triangles, order is very impo





 $\triangle ABC \cong \triangle FED$ or $\triangle BCA \cong \triangle EDF$.

Corresponding angles $\angle A \cong \angle F$

 $\angle B \cong \angle E$ $\angle C \cong \angle D$

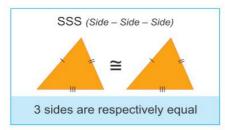
Corresponding sides

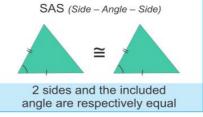
 $\overline{AB} \cong \overline{FE}$

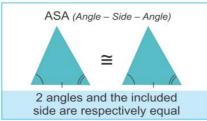
 $\overline{BC} \cong \overline{ED}$

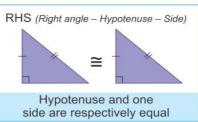
 $\overline{AC} \cong \overline{FD}$

Conditions for Congruence of Two Triangles



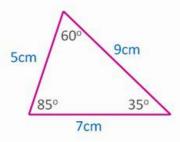


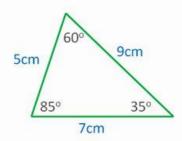




Congruent Triangles

Identical Triangles have all three Sides, and all three Angles exactly the same sizes.





If we gave several people three sticks: 5cm, 7cm and 9cm long, they would all only be able to make the exact sameTriangle.

Q1

Answer

We have to state the correspondence between the vertices, sides and angles of the following pairs of congruent triangles.

(i) $\triangle ABC \cong \triangle EFD$

Correspondence between vertices:

$$A \leftrightarrow E, \ B \leftrightarrow F, \ C \leftrightarrow D$$

Correspondence between sides:

$$AB = EF, BC = FD, CA = DE$$

Correspondence between angles:

$$\angle A = \angle E, \angle B = \angle F, \angle C = \angle D$$

(ii) $\triangle CAB \cong \triangle QRP$

Correspondence between vertices:

$$C \leftrightarrow Q, \ A \leftrightarrow R, \ B \leftrightarrow P$$

Correspondence between sides:

$$CA = QR$$
, $AB = RP$, $BC = PQ$

Correspondence between angles:

$$\angle C = \angle Q$$
, $\angle A = \angle R$, $\angle B = \angle P$

```
(iii) \triangle XZY \cong \triangle QPR
Correspondence between vertices: X \leftrightarrow Q, Z \leftrightarrow P, Y \leftrightarrow R
Correspondence between sides: XZ = QP, ZY = PR, YX = RQ
Correspondence between angles: \angle X = \angle Q, \angle Z = \angle P, \angle Y = \angle R
(iv) \triangle MPN \cong \triangle SQR
Correspondence between vertices: M \leftrightarrow S, P \leftrightarrow Q, N \leftrightarrow R
Correspondence between sides: MP = SQ, PN = QR, NM = RS
Correspondence between angles: \angle M = \angle S, \angle P = \angle Q, \angle N = \angle R
```

Q2

```
Answer:

(i) \triangle ACB \cong \triangle DEF
(SAS congruence property)
(ii) \triangle RPQ \cong \triangle LNM
(RHS congruence property)
(iii) \triangle YXZ \cong \triangle TRS
(SSS congruence property)
(iv) \triangle DEF \cong \triangle PNM
(ASA congruence property)
(v) \triangle ACB \cong \triangle ACD
(ASA congruence property)
```

Q3

```
Answer:
Given:
    PL \perp OA
   PM \perp OB
    PL = PM
To prove:
\triangle PLO \cong \triangle PMO
Proof:
In \triangle PLO \text{ and } \triangle PMO:
\angle PLO = \angle PMO (90° each)
PO = PO
                       (common)
PL = PM
                        (given)
By RHS congruence property:
\triangle PLO \cong \triangle PMO
```

Q4

```
Answer:
Given:
       AD = BC
      AD \parallel BC
We have to show that AB = DC.
Proof:
AD \parallel BC
\therefore \angle BCA = \angle DAC (alternate angles)
In \triangle ABC and \triangle CDA:
BC = DA
                         (given)
\angle BCA = \angle DAC
                      (proved above)
AC = \ AC
                        (common)
By SAS congruence property :
\triangle ABC \cong \triangle CDA
=>AB=CD
                                 (corresponding parts of the congruent triangles)
```

```
Q5
 Answer:
 Given:
  AB = AC, BD = DC
 To prove: \triangle ADB \cong \triangle ADC
 Proof:
  (i) In \triangle ADB and \triangle ADC:
  AB = AC
                     (given)
 BD = DC
                     (given)
 \mathbf{D}\mathbf{A} = \mathbf{D}\mathbf{A}
                  (common)
 By SSS congruence property :
 \triangle ADB \cong \triangle ADC
 \angle ADB = \angle ADC (corresponding parts of the congruent triangles)
                                                                                         ...(1)
 \angle ADB and \angle ADC are on the straight line.
  \therefore \angle ADB + \angle ADC = 180^{\circ}
 \angle ADB + \angle ADB = 180^{\circ}
  => 2\angle ADB = 180^{\circ}
  => \angle ADB = 90^{\circ}
 From (1):
 \angle ADB = \angle ADC = 90^{\circ}
 (ii) \angle BAD = \angle CAD (corresponding parts of the congruent triangles)
```

Q6

```
Answer:
 Given:
  AD is a bisector of \angle A.
  => \angle DAB = \angle DAC
                               ...(1)
 AD \perp BC
                              (90° each)
  => \angle BDA = \angle CDA
 To prove:
 \triangle ABC is isosceles.
  Proof:
 In \triangle DAB and \triangle DAC:
  \angle BDA = \angle CDA
                          (90° each)
 DA = DA
                          (common)
 \angle DAB = \angle DAC
                           (from 1)
 By ASA congruence property:
  \triangle DAB \cong \triangle DAC
  =>AB=AC (corresponding parts of the congruent triangles)
 Therefore, \triangle ABC is isosceles.
Q7
 Answer:
 Given:
        AB = AD
       CB = CD
 To prove:
 \triangle ABC \cong \triangle ADC
 Proof:
 In \triangle ABC and \triangle ADC:
  AB = AD
                  (given)
 BC = DC
                  (given)
 AC = AC
                  (common)
 \therefore \triangle ABC \cong \triangle ADC
                                              (by SSS congruence property)
08
 Answer:
 Given:
           PA \perp AB
          QB \perp AB
          PA = QB
  To prove: \triangle OAP \cong \triangle OBQ
  Find whether OA = OB.
  Proof:
 In \triangle OAP and \triangle OBQ:
  \angle POA = \angle QOB
                            (vertically opposite angles)
 \angle OAP = \angle OBQ
                             (90^{\circ} \text{ each})
 PA = QB
                             (given)
 By AAS congruence property:
  \triangle OAP \cong \triangle OBQ
  => OA = OB (corresponding parts of the congruent triangles)
Q9
Answer:
 Given:
 Triangles ABC and DCB are right angled at A and D, respectively.
 AC = DB
 To prove : \triangle ABC \cong \triangle DCB
 In \triangle ABC and \triangle DCB:
 \angle CAB = \angle BDC
                        (90° each)
 BC = BC
                          (common)
 AC = DB
                           (given)
\mathbf{B}y R. H. S. congruence property:
    \triangle ABC \cong \triangle DCB
Q10
```

```
Answer:
Given:
\triangle ABC is an isosceles triangle in which AB = AC.
E and F are midpoints of AC and AB, respectively.
To prove:
 BE = CF
Proof:
 E and F are midpoints of AC and AB, respectively.
 =>AF=FB,\ AE=EC
AB = AC
 =>\frac{1}{2}AB=\frac{1}{2}AC
 =>FB=EC
\angle ABC = \angle ACB
                     (angle opposite to equal sides are equal )
 => \angle FBC = \angle ECB
Consider \triangle BCF and \triangle CBE:
 BC = BC
                      (common)
 => \angle FBC = \angle ECB
Consider \triangle BCF and \triangle CBE:
 BC = BC
                      (common)
\angle FBC = \angle ECB
                     (proved above)
FB = EC
                      (proved above)
By\;SAS congruence property :
\triangle BCF \cong \triangle CBE
BE = CF
                (corresponding parts of the congruent triangles)
Q11
Answer:
Given:
AB = AC
 \triangle ABC is an isosceles triangle.
AP = AQ
To prove:
 BQ = CP
Proof:
 AB = AC (given)
AP = AQ (given)
AB - AP = AC - AQ
 =>BP=CQ
\angle ABC = \angle ACB (angle opposite to the equal sides are equal)
 => \angle PBC = \angle QCB
In \triangle PBC and \triangle QCB:
 PB = QC
               (proved above)
\angle PBC = \angle QCB (proved above)
BC = BC
               (common)
By SAS congruence property:
\triangle \ PBC \ \cong \triangle \ QCB
BQ = CP
                (corresponding parts of the congruent triangles)
```

```
Answer:
Given:
ABC is an isosceles triangle.
AB = AC
BD = CE
To prove:
BE=CD
Proof:
AB + BD = AC + CE
                      (As, AB = AC, BD = CE)
=>AD=AE
Consider \triangle ACD and \triangle ABE:
AC = AB (given)
\angle CAD = \angle BAE (common)
             (proved above)
AD = AE
By SAS congruence property:
\triangle ACD \cong \triangle ABE
=>CD=BE (corresponding parts of the congruent triangles)
```

Q13

Answer:

.Given:

 $\triangle \ ABC$ is an isosceles triangle.

AB = AC

BD = CD

To prove:

AD bisects $\angle A$ and $\angle D$.

Proof:

Consider $\triangle ABD$ and $\triangle ACD$:

AB = AC (given)

BD = CD (given)

AD = AD (common)

 $By \: SSS$ congruence property :

 $\triangle ABD \cong \triangle ACD$

 $=> \angle BAD = \angle CAD$ (by cpct)

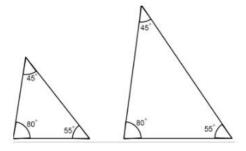
 $=> \angle BDA = \angle CDA$ (by cpct)

Q14

Answer:

No, its not necessary. If the corresponding angles of two triangles are equal, then they may or may not be congruent.

They may have proportional sides as shown in the following figure:

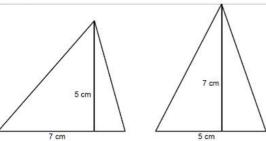


Q15

Answer:

No, two triangles are not congruent if their two corresponding sides and one angle are equal. They will be congruent only if the said angle is the included angle between the sides.

Answer:



Both triangles have equal area due to the the same product of height and base. But they are not congruent.

Q17

Answer:

- (i) the same length
- (ii) the same measure
- (iii)the same side length
- (iv) the same radius
- (v) the same length and the same breadth
- (vi) equal parts

Q18

Answer:

(i) False

This is because they can be equal only if they have equal sides.

(ii) True

This is because if squares have equal areas, then their sides must be of equal length.

(iii) False

For example, if a triangle and a square have equal area, they cannot be congruent.

(iv) False

For example, an isosceles triangle and an equilateral triangle having equal area cannot be congruent.

(v) False

They can be congruent if two sides and the included angle of a triangle are equal to the corresponding two sides and the included corresponding angle of another triangle.

(vi) True

This is because of the AAS criterion of congruency.

(vii) False

Their sides are not necessarily equal.

(viii) True

This is because of the AAS criterion of congruency.

(ix) False

This is because two right triangles are congruent if the hypotenuse and one side of the first triangle are respectively equal to the hypotenuse and the corresponding side of the second triangle.

(x) True