Exercise – 12.1

1. Find the area of a triangle whose sides are respectively 150 cm, 120 cm and 200 cm.

Sol:

The triangle whose sides are

$$a = 150 \text{ cm}$$

$$b = 120 \text{ cm}$$

$$c = 200 \text{ cm}$$

The area of a triangle =
$$\sqrt{s(s-a)(s-b)(s-c)}$$

Here 1s = semi perimeter of triangle

$$2s = a + b + c$$

$$S = \frac{a+b+c}{2} = \frac{150+200+120}{2} = 235cm$$

∴ area of triangle =
$$\sqrt{s(s-a)(s-b)(s-c)}$$

$$=\sqrt{235(235-150)(235-200)(235-120)}$$

$$=\sqrt{235(85)(35)(115)}cm^2$$

$$= 8966.56 cm^2$$

2. Find the area of a triangle whose sides are 9 cm, 12 cm and 15 cm.

Sol:

The triangle whose sides are a = 9cm, b = 12 cm and c = 15 cm

The area of a triangle =
$$\sqrt{s(s-a)(s-b)(s-c)}$$

Here 1s = semi-perimeter of a triangle

$$2s = a + b + c$$

$$S = \frac{a+b+c}{2} = \frac{9+12+15}{2} = \frac{36}{2} = 18 \text{ cm}$$

∴ area of a triangle =
$$\sqrt{s(s-a)(s-b)(s-c)}$$

$$=\sqrt{18(18-9)(18-12)(18-15)}=\sqrt{18(9)(6)(3)}$$

$$= \sqrt{18 \ cm \times 3 \ cm \times 54 \ cm^2} = 54 \ cm^2.$$

3. Find the area of a triangle two sides of which are 18 cm and 10 cm and the perimeter is 42cm.

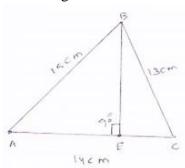
Sol:

$$21\sqrt{11}cm^2$$

4. In a \triangle ABC, AB = 15 cm, BC = 13 cm and AC = 14 cm. Find the area of \triangle ABC and hence its altitude on AC.

Sol:

The triangle sides are



Let
$$a = AB = 15$$
 cm, $BC = 13$ cm = b.
 $c = AC = 14$ cm say.

Now,

$$2s = a + b + c$$

$$\Rightarrow S = \frac{1}{2}(a+b+c)$$

$$\Rightarrow$$
 s = $\left(\frac{15+13+14}{2}\right)cm$

$$\Rightarrow$$
 s = 21 cm

$$\therefore$$
 area of a triangle = $\sqrt{s(s-a)(s-b)(s-c)}$

$$= \sqrt{21(21-15)(21-14)(21-13)} cm^2$$

$$=\sqrt{21\times6\times8\times7}$$
 cm²

$$= 84 \text{ cm}^2$$

Let BE be perpendicular (\perp^{er}) to AC

Now, area of triangle = 84 cm^2

$$\Rightarrow \frac{1}{2} \times BE \times AC = 84$$

$$\Rightarrow$$
 BE = $\frac{84 \times 2}{AC}$

$$\Rightarrow BE = \frac{168}{14} = 12cm$$

- : Length of altitude on AC is 12 cm.
- 5. The perimeter of a triangular field is 540 m and its sides are in the ratio 25 : 17 : 12. Find the area of the triangle.

Sol:

The sides of a triangle are in the ratio 25:17:12

Let the sides of a triangle are a = 25x, b = 17x and c = 12x say.

Perimeter = 25 = a + b + c = 540 cm

$$\Rightarrow 25x + 17x + 12x = 540 \text{ cm}$$

$$\Rightarrow 54x = 540cm$$

$$\Rightarrow x = \frac{540}{54}$$

$$\Rightarrow$$
 $x = 10 cm$

 \therefore The sides of a triangle are a = 250 cm, b = 170 cm and c = 120 cm

Now, Semi perimeter $s = \frac{a+b+c}{2}$

$$=\frac{540}{2}=270\ cm$$

∴ The area of the triangle =
$$\sqrt{s(s-a)(s-b)(s-c)}$$

$$=\sqrt{270(270-250)(270-170)(270-120)}$$

$$=\sqrt{270(20)(100)(150)}$$

$$=\sqrt{(9000)(9000)}$$

$$=9000 cm^{2}$$

- \therefore The area of triangle = 900 cm².
- **6.** The perimeter of a triangle is 300 m. If its sides are in the ratio 3:5:7. Find the area of the triangle.

Sol:

Given that

The perimeter of a triangle = 300 m

The sides of a triangle in the ratio 3:5:7

Let 3x, 5x, 7x be the sides of the triangle

Perimeter \Rightarrow 2s = a + b + c

$$\Rightarrow 3x + 5x + 17x = 300$$

$$\Rightarrow 15x = 300$$

$$\Rightarrow$$
 x = 20m

The triangle sides are a = 3x

$$= 3 (20) m = 60 m$$

$$b = 5x = 5(20) m = 100m$$

$$c = 7x = 140 \text{ m}$$

Semi perimeter $s = \frac{a+b+c}{2}$

$$=\frac{300}{2}m$$

$$= 150 m$$

∴ The area of the triangle = $\sqrt{s(s-a)(s-b)(s-c)}$

$$= \sqrt{150(150 - 60)(150 - 100)(150 - 140)}$$

$$= \sqrt{150 \times 10 \times 90 \times 50}$$

$$=\sqrt{1500 \times 1500 \times 3} \ cm^2$$

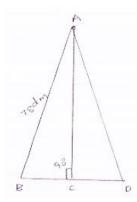
∴
$$\Delta$$
le Area = $1500\sqrt{3}$ cm^2

7. The perimeter of a triangular field is 240 dm. If two of its sides are 78 dm and 50 dm, find the length of the perpendicular on the side of length 50 dm from the opposite vertex.

Sol:

ABC be the triangle, Here
$$a = 78 \text{ dm} = AB$$
,

$$BC = b = 50 \text{ dm}$$



Now, perimeter =
$$240 \text{ dm}$$

$$\Rightarrow$$
 AB + BC + CA = 240 dm

$$\Rightarrow$$
 AC = 240 - BC - AB

$$\Rightarrow$$
 AC = 112 dm

Now,
$$2s = AB + BC + CA$$

$$\Rightarrow$$
 2s = 240

$$\Rightarrow$$
 s = 120 dm

: Area of
$$\triangle ABC = \sqrt{s(s-a)(s-b)(s-c)}$$
 by heron's formula

$$=\sqrt{120(120-78)(120-50)(120-112)}$$

$$=\sqrt{120\times42\times70\times8}$$

$$= 1680 dm^2$$

Let AD be perpendicualar on BC

Area of
$$\triangle ABC = \frac{1}{2} \times AD \times BC$$
 (area of triangle $= \frac{1}{2} \times b \times h$)

$$=\frac{1}{2} \times AD \times BC = 1680$$

$$\Rightarrow AD = \frac{2 \times 1680}{50} = 67.2 \ dm$$

8. A triangle has sides 35 cm, 54 cm and 61 cm long. Find its area. Also, find the smallest of its altitudes.

Sol:

The sides of a triangle are a = 35 cm, b = 54 cm and c = 61 cm

Now, perimeter a + b + c = 25

$$\Rightarrow$$
 S = $\frac{1}{2}$ (35 + 54 + 61)

$$\Rightarrow$$
 s = 75 cm

By using heron's formula

∴Area of triangle =
$$\sqrt{s(s-a)(s-b)(s-c)}$$

$$=\sqrt{75(75-35)(75-54)(75-61)}$$

$$=\sqrt{75(40)(21)(14)}=939.14$$
cm²

∴ The altitude will be a smallest when the side corresponding to it is longest Here, longest side is 61 cm

[: Area of
$$\triangle$$
le = $\frac{1}{2} \times b \times h$] = $\frac{1}{2} \times base \times height$

$$\therefore \frac{1}{2} \times h \times 61 = 939.14$$

$$\Rightarrow h = \frac{939.14 \times 2}{61} = 30.79 \ cm$$

Hence the length of the smallest altitude is 30.79 cm

9. The lengths of the sides of a triangle are in the ratio 3 : 4 : 5 and its perimeter is 144 cm. Find the area of the triangle and the height corresponding to the longest side.

Sol:

Let the sides of a triangle are 3x, 4x and 5x.

Now,
$$a = 3x$$
, $b = 4x$ and $c = 5x$

The perimeter 2s = 144

$$\Rightarrow 3x + 4x + 5x = 144 \ [\because a + b + c = 2s]$$

$$\Rightarrow 12x = 144$$

$$\Rightarrow$$
 x = 12

 \therefore sides of triangle are a = 3(x) = 36cm

$$b = 4(x) = 48 \text{ cm}$$

$$c = 5(x) = 60 \text{ cm}$$

Now semi perimeter $s = \frac{1}{2}(a + b + c) = \frac{1}{2}(144) = 72cm$

By heron's formulas : Area of $\Delta le = \sqrt{s(s-a)(s-b)(s-c)}$

$$=\sqrt{72(72-36)(72-48)(72-60)}$$

$$=864cm^{2}$$

Let *l* be the altitude corresponding to longest side, $\therefore \frac{1}{2} \times 60 \times l = 864$

$$\Rightarrow l = \frac{864 \times 2}{60}$$
$$\Rightarrow l = 28.8cm$$

Hence the altitude one corresponding long side = 28.8 cm

10. The perimeter of an isosceles triangle is 42 cm and its base is $\left(\frac{3}{2}\right)$ times each of the equal sides. Find the length of each side of the triangle, area of the triangle and the height of the triangle.

Sol:

Let 'x' be the measure of each equal sides

∴ Base =
$$\frac{3}{2}x$$

∴ $x + x + \frac{3}{2}x = 42$ [∴ Perimeter = $a + b + c = 42$ cm]
⇒ $\frac{7}{2}x = 42$
⇒ $x = 12$ cm

$$\therefore$$
 Sides are $a = x = 12$ cm

$$b = x = 12 \text{ cm}$$

 $c = x = \frac{3}{2} (12) \text{ cm} = 18 \text{ cm}$

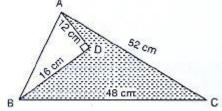
By heron's formulae

∴ Area of triangle =
$$\sqrt{s(s-a)(s-b)(s-c)}cm^2$$

= $\sqrt{21(9)(9)(21-18)}cm^2$
= $\sqrt{(21)(9)(9)(3)}cm^2$
= 71.42 cm^2

$$\therefore$$
 Area of triangle = 71.42 cm²

11. Find the area of the shaded region in Fig. Below.



Sol

Area of shaded region = Area of $\triangle ABC$ – Area of $\triangle ADB$

Now in $\triangle ADB$

$$\Rightarrow AB^2 = AD^2 + BD^2$$
 --(i)

$$\Rightarrow$$
 Given that AD = 12 cm BD = 16 cm

Substituting the values of AD and BD in the equation (i), we get

$$AB^2 = 12^2 + 16^2$$

$$AB^2 = 144 + 256$$

$$AB = \sqrt{400}$$

$$AB = 20 \text{ cm}$$

∴ Area of triangle =
$$\frac{1}{2} \times AD \times BD$$

$$=\frac{1}{2} \times 12 \times 16$$

$$= 96 cm^2$$

Now

In
$$\triangle ABC$$
, $S = \frac{1}{2}(AB + BC + CA)$

$$=\frac{1}{2}\times(52+48+20)$$

$$=\frac{1}{2}(120)$$

$$= 60 \text{ cm}$$

By using heron's formula

We know that, Area of \triangle le ABC = $\sqrt{s(s-a)(s-b)(s-c)}$

$$=\sqrt{60(60-20)(60-48)(60-52)}$$

$$=\sqrt{60(40)(12)(8)}$$

 $= 480 \text{ cm}^2$

= Area of shaded region = Area of \triangle ABC - Area of \triangle ADB

$$=(480-96)cm^2$$

 $= 384 \ cm^2$

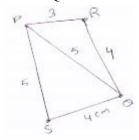
∴ Area of shaded region = 384 cm²

Exercise - 12.2

1. Find the area of a quadrilateral ABCD is which AB = 3 cm, BC = 4 cm, CD = 4 cm, DA = 5 cm and AC = 5 cm.

Sol:

For ΔPQR



$$PQ^2 = QR^2 + RP^2$$

$$(5^2) = (3)^2 + (4)^2$$
 [: $PR = 3 QR = 4$ and $PQ = 5$]

So, $\triangle PQR$ is a right angled triangle. Right angle at point R.

Area of
$$\triangle ABC = \frac{1}{2} \times QR \times RP$$

$$=\frac{1}{2}\times3\times4$$

$$=6 \text{cm}^2$$

For $\triangle QPS$

Perimeter =
$$2s = AC + CD + DA = (5 + 4 + 5)cm = 14 cm$$

$$S = 7 \text{ cm}$$

By Heron's formulae

Area of
$$\Delta le \sqrt{s(s-a)(s-b)(s-c)} cm^2$$

Area of
$$\triangle$$
le PQS = $\sqrt{7(7-5)(7-4)(7-3)}cm^2$
= $\sqrt{7 \times 2 \times 2 \times 3} cm^2$

$$=2\sqrt{21}cm^2$$

$$=(2\times 4.583)cm^2$$

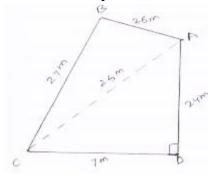
$$= 9.166 \text{ cm}^2$$

Area of PQRS = Area of PQR + Area of
$$\triangle PQS = (6 + 9.166)cm^2 = 15.166cm^2$$

2. The sides of a quadrangular field, taken in order are 26 m, 27 m, 7m are 24 m respectively. The angle contained by the last two sides is a right angle. Find its area.

Sol:

The sides of a quadrilateral field taken order as AB = 26m



$$BC = 27 \text{ m}$$

$$CD = 7m$$
 and $DA = 24 m$

Diagonal AC is joined

Now ΔADC

By applying Pythagoras theorem

$$\Rightarrow AC^2 = AD^2 + CD^2$$

$$\Rightarrow$$
 AC = $\sqrt{AD^2 + CD^2}$

$$\Rightarrow$$
 AC = $\sqrt{24^2 + 7^2}$

$$\Rightarrow$$
 AC = $\sqrt{625}$ = 25 m

Now area of ΔABC

$$S = \frac{1}{2}(AB + BC + CA) = \frac{1}{2}(26 + 27 + 25) =$$
$$= \frac{78}{2} = 39m.$$

By using heron's formula

Area (
$$\triangle$$
ABC) = $\sqrt{S(S - AD)(S_BC)(S - CA)}$
= $\sqrt{39(39 - 26)(39 - 21)(39 - 25)}$
= $\sqrt{39 \times 14 \times 13 \times 12 \times 1}$
= 291.849 cm²

Now for area of $\triangle ADC$

$$S = \frac{1}{2}(AD + CD + AC)$$
$$= \frac{1}{2}(25 + 24 + 7) = 28m$$

By using heron's formula

: Area of
$$\triangle ADC = \sqrt{S(S - AD)(S - DC)(S - CA)}$$

= $\sqrt{28(28 - 24)(28 - 7)(28 - 25)}$
= 84m^2

∴ Area of rectangular field ABCD = area of \triangle ABC + area of \triangle ADC

$$= 291.849 + 84$$

 $= 375.8 \text{m}^2$

3. The sides of a quadrilateral, taken in order are 5, 12, 14 and 15 meters respectively, and the angle contained by the first two sides is a right angle. Find its area.

Sol:

Given that sides of quadrilateral are AB = 5 m, BC = 12 m, CD = 14 m and DA = 15 m AB = 5m, BC = 12m, CD = 14 m and DA = 15 m

Join AC

Area of
$$\triangle ABC = \frac{1}{2} \times AB \times BC$$
 [: Area of $\triangle le = \frac{1}{2}(3x + 1)$]
= $\frac{1}{2} \times 5 \times 12$
= 30 cm^2

In ΔABC By applying Pythagoras theorem.

$$AC^{2} = AB^{2} + BC^{2}$$

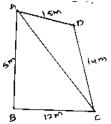
$$\Rightarrow AC = \sqrt{5^{2} + 12^{2}}$$

$$= \sqrt{25 + 144}$$

$$= \sqrt{169} = 13 \text{ m}$$

Now in $\triangle ADC$

Let 2s be the perimeter



$$\therefore 2s = (AD + DC + AC)$$

$$\Rightarrow S = \frac{1}{2}(15 + 14 + 13) = \frac{1}{2} \times 42 = 21m$$

By using Heron's formula

$$\therefore \text{ Area of } \Delta ADC = \sqrt{S(S - AD)(S - DC)(S - AC)}$$

$$= \sqrt{21(21-15)(21-14)(21-13)}$$

$$=\sqrt{21\times6\times7\times8}$$

 $= 84m^2$

: Area of quadrilateral ABCD = area of (ΔABC) + Area of (ΔADC) = $30 + 84 = 114 \text{ m}^2$

4. A park, in the shape of a quadrilateral ABCD, has $\angle C = 900$, AB = 9 m, BC = 12 m, CD = 5 m and AD = 8 m How much area does it occupy?

Sol:

Given sides of a quadrilaterals are AB = 9, BC = 12, CD = 05, DA = 08

Let us joint BD

In ΔBCD applying Pythagoras theorem.

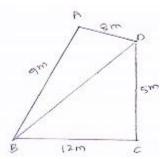
$$BD^2 = BC^2 + CD^2$$

$$=(12)^2+(5)^2$$

$$= 144 + 25$$

$$= 169$$

$$BD = 13m$$



Area of
$$\triangle BCD = \frac{1}{2} \times BC \times CD = \left[\frac{1}{2} \times 12 \times 5\right] m^2 = 30 m^2$$

For ∆ABD

$$S = \frac{perimeter}{2} = \frac{(9+8+13)}{2} = 15cm$$

By heron's formula =
$$\sqrt{s(s-a)(s-b)(s-c)}$$

Area of the triangle =
$$\sqrt{15(15-9)(15-8)(15-13)}m^2$$

$$=\sqrt{15(6)(7)(2)}m^2=6\sqrt{35}\,m^2=35.496m^2$$

Area of park = Area of
$$\triangle ABD + \triangle ABD + Area of BCD$$

$$= 35.496 + 30 \text{ m}^2$$

$$= 65.5 \text{ m}^2 \text{ (approximately)}$$

Two parallel side of a trapezium are 60 cm and 77 cm and other sides are 25 cm and 26 cm. Find the area of the trapezium.

Sol:

Given that two parallel sides of trapezium are AB = 77 and CD = 60 cm

Other sides are BC = 26 m and AD = 25 cm.

Join AE and CF

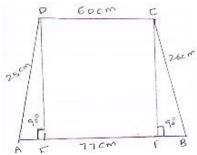
Now, DE \perp AB and CF \perp AB

$$\therefore$$
 DC = EF = 60 cm

Let
$$AE = x$$

$$\Rightarrow$$
 BF = 77 - 60 - x = 17 - x

In
$$\triangle ADE$$
, $DE^2 = AD^2 - AE^2 = 25^2 - x^2$ [: Pythagoras theorem]



And in
$$\triangle BCF$$
, $CF^2 = BC^2 - BF^2$

[: By Pythagoras theorem]

$$\Rightarrow CF = \sqrt{26^2 - (17 - x)^2}$$

But
$$DE = CF \Rightarrow DE^2 = CF^2$$

$$\Rightarrow 25^2 - x^2 = 26^2 - (17 - x)^2$$

$$\Rightarrow 25^2x^2 = 25^2 - (289 + x^2 - 34x) \quad [\because (a - b)^2 = a^2 - 2ab + b^2]$$

$$\Rightarrow 625 - x^2 = 676 - 289 - x^2 + 34x$$

$$\Rightarrow$$
 34x = 238

$$\Rightarrow$$
 x = 7

$$\therefore DE = \sqrt{25^2 - x^2} = \sqrt{625 - 7^2} = \sqrt{516} = 24cm$$

∴ Area of trapezium =
$$\frac{1}{2}$$
 (sum of parallel sides) × height = $\frac{1}{2}$ (60 × 77) × 24 =

 $1644cm^{2}$

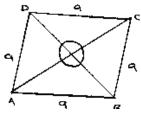
6. Find the area of a rhombus whose perimeter is 80 m and one of whose diagonal is 24 m.

Sol:

Given that,

Perimeter of rhombus = 80m

Perimeter of rhombus = $4 \times \text{side}$



$$\Rightarrow 4a = 80$$

$$\Rightarrow$$
 a = 20m

Let
$$AC = 24 \text{ m}$$

$$\therefore OA = \frac{1}{2}AC = \frac{1}{2} \times 24 = 12m$$

In ΔAOB

$$OB^2 = AB^2 - OA^2$$
 [By using Pythagoras theorem]

$$\Rightarrow OB = \sqrt{20^2 - 12^2}$$

$$=\sqrt{400-144}$$

$$=\sqrt{256} = 16 m$$

Also
$$BO = OD$$

[Diagonal of rhombus bisect each other at 90°]

$$\therefore$$
 BD = 20B = 2 ×16 = 32 m

∴ Area of rhombus =
$$\frac{1}{2} \times 32 \times 24 = 384m^2$$
 [: Area of rhombus = $\frac{1}{2} \times BD \times AC$]

7. A rhombus sheet, whose perimeter is 32 m and whose one diagonal is 10 m long, is painted on both sides at the rate of Rs 5 per m². Find the cost of painting.

Sol:

Given that,

Perimeter of a rhombus = 32 m

We know that.

Perimeter of rhombus = $4 \times \text{side}$

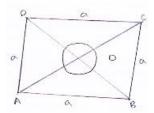
$$\Rightarrow$$
 49 = 32m

$$\Rightarrow$$
 a = 8 m

Let AC =
$$10 = OA = \frac{1}{2}AC$$

$$=\frac{1}{2} \times 10$$

$$=5m$$



By using Pythagoras theorem:

$$\therefore OB^2 = AB^2 - OA^2$$

$$\Rightarrow$$
 OB = $\sqrt{AB^2 - 0A^2}$

$$\Rightarrow$$
 OB = $\sqrt{8^2 - 5^2}$

$$\Rightarrow$$
 OB = $\sqrt{64 - 25}$

$$\Rightarrow$$
 OB = $\sqrt{39} m$

Now, BD = $2OB = 2\sqrt{39}m$

$$\therefore \text{ Area of sheet} = \frac{1}{2} \times BD \times AC = \frac{1}{2} \times 2\sqrt{39} \times 10 = 10\sqrt{39}m^2$$

- ∴ Cost of printing on both sides at the rate of Rs 5 per $m^2 = Rs \ 2 \times 10\sqrt{39} \times 5$ = Rs. 625.00
- 8. Find the area of a quadrilateral ABCD in which AD = 24 cm, \angle BAD = 90° and BCD forms an equilateral triangle whose each side is equal to 26 cm. (Take $\sqrt{3}$ = 1.73)

Sol:

Given that, a quadrilateral ABCD in which AD = 24 cm, $\angle BAD = 90^{\circ}$

BCD is equilateral triangle and sides BC = CD = BD = 26 cm

In ΔBAD By using Pythagoras theorem

$$BA^2 = BD^2 - AD^2$$

$$\Rightarrow BA = \sqrt{BD^2 - AD^2}$$

$$=\sqrt{676-576}$$

$$=\sqrt{100}=10~cm$$

Area of
$$\triangle BAD = \frac{1}{2} \times BA \times AD$$

$$=\frac{1}{2}\times10\times24$$

$$=120cm^2$$

Area of
$$\triangle BCD = \frac{\sqrt{3}}{4} \times (26)^2 = 292.37 cm^2$$

∴ Area of quadrilateral

ABCD = Area of \triangle BAD + area of \triangle BCD

$$= 120 + 292.37$$

$$=412.37 \text{ cm}^2$$

9. Find the area of a quadrilateral ABCD in which AB = 42 cm, BC = 21 cm, CD = 29 cm, DA = 34 cm and diagonal BD = 20 cm.

Sol:

Given that

Sides of a quadrilateral are AB = 42 cm, BC = 21 cm, CD = 29 cm

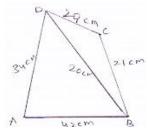
DA = 34 cm and diagonal BD = 20 cm

Area of quadrilateral = area of $\triangle ADB$ + area of $\triangle BCD$.

Now, area of ΔABD

Perimeter of ΔABD

We know that



$$2s = AB + BD + DA$$

$$\Rightarrow S = \frac{1}{2}(AB + BD + DA)$$

$$=\frac{1}{2}(34+42+20)=96$$

$$=\frac{96}{2}$$

$$= 48 cm$$

Area of
$$\triangle ABD = \sqrt{S(S - AB)(S - BD)(S - DA)}$$

$$=\sqrt{48(48-42)(48-20)(48-34)}$$

$$=\sqrt{48(14)(6)(28)}$$

$$= 336 cm^2$$

Also for area of $\triangle BCD$,

Perimeter of ΔBCD

$$2s = BC + CD + BD$$

$$\Rightarrow S = \frac{1}{2}(29 + 21 + 20) = 35 \text{ cm}$$

By using heron's formulae

Area of
$$\triangle BCD = \sqrt{s(s - bc)(s - cd)(s - db)}$$

$$= \sqrt{35(35-21)(35-29)(35-20)}$$

$$= \sqrt{210 \times 210} cm^2$$

$$= 210 cm^2$$

$$\therefore$$
 Area of quadrilateral ABCD = 336 + 210 = 546 cm²

10. Find the perimeter and area of the quadrilateral ABCD in which AB = 17 cm, AD = 9 cm, CD = 12cm, \angle ACB = 90° and AC=15cm.

Sol:

The sides of a quadrilateral ABCD in which AB = 17 cm, AD = 9 cm, CD = 12 cm, $\angle ACB = 90^{\circ}$ and AC = 15 cm

Here, By using Pythagoras theorem

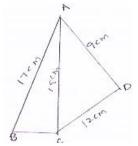
BC =
$$\sqrt{17^2 - 15^2} = \sqrt{289 - 225} = \sqrt{64} = 8cm$$

Now, area of
$$\triangle ABC = \frac{1}{2} \times 8 \times 15 = 60 \text{ cm}^2$$

For area of Δ le ACD,

Let
$$a = 15$$
 cm, $b = 12$ cm and $c = 9$ cm

Therefore,
$$S = \frac{15+12+9}{2} = \frac{36}{2} = 18 \text{ cm}$$



Area of ACD =
$$\sqrt{s(s-a)(s-b)(s-c)}$$

$$=\sqrt{18(18-15)(18-12)(18-9)}$$

$$= \sqrt{18 \times 18 \times 3 \times 3}$$

$$=\sqrt{(18\times 3)^2}$$

$$= 54 cm^2$$

 \therefore Thus, the area of quadrilateral ABCD = $60 + 54 = 114 \text{ cm}^2$

11. The adjacent sides of a parallelogram ABCD measure 34 cm and 20 cm, and the diagonal AC measures 42 cm. Find the area of the parallelogram.

Sol:

Given that adjacent sides of a parallelogram ABCD measure 34 cm and 20 cm, and the diagonal AC measures 42 cm.

Area of parallelogram = Area of $\triangle ADC$ + area of $\triangle ABC$

[: Diagonal of a parallelogram divides into two congruent triangles]

$$= 2 \times [Area\ of\ \Delta ABC]$$

Now for Area of ΔABC

Let
$$2s = AB + BC + CA$$
 [: Perimeter of $\triangle ABC$]

$$\Rightarrow$$
 S = $\frac{1}{2}$ (AB + BC + CA)

$$\Rightarrow$$
 S = $\frac{1}{2}$ (34 + 20 + 42)

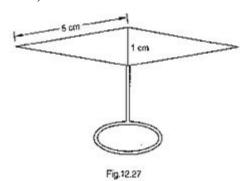
$$= \frac{1}{2}(96) = 48 cm$$

$$\therefore \text{ Area of } \Delta ABC = \sqrt{s(s-ab)(s-bc)(s-ca)} \qquad [heron's formula]$$

$$= \sqrt{48(48-34)(48-20)(48-42)}$$

$$= \sqrt{48(14)(28)(6)} = 336cm^{2}$$

- ∴ Area of parallelogram ABCD = $2[Area \ of \ \Delta ABC] = 2 \times 336 = 672 \ cm^2$
- 12. Find the area of the blades of the magnetic compass shown in Fig. 12.27. (Take $\sqrt{11}$ = 3.32).



Sol:

Area of the blades of magnetic compass = Area of $\triangle ADB + Area$ of $\triangle CDB$

Now, for area of $\triangle ADB$

Let,
$$2s = AD + DB + BA$$
 (Perimeter of $\triangle ADB$)

Semi perimeter (S) =
$$\frac{1}{2}(5 + 1 + 5) = \frac{11}{2}cm$$

By using heron's formulae

Now, area of
$$\triangle ADB = \sqrt{s(s-ad)(s-bd)(s-ba)}$$

$$= \sqrt{\frac{11}{2} \left(\frac{11}{2} - 5 \right) \left(\frac{11}{2} - 1 \right) \left(\frac{11}{2} - 5 \right)}$$

- $= 2.49 \text{ cm}^2$
- = Also, area of triangle ADB = Area of Δle CDB
- ∴ Area of the blades of magnetic compass
- $= 2 \times (area\ of\ \Delta ADB)$
- $= 2 \times 2.49$
- $= 4.98 \text{ m}^2$
- **13.** A hand fan is made by stitching lo equal size triangular strips of two different types of paper as shown in Fig. 12.28. The dimensions of equal strips are 25 cm, 25 cm and 14 cm. Find the area of each type of paper needed to make the hand fan.

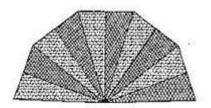


Fig. 12.28

Sol:

Given that the sides of $\triangle AOB$ are

AO = 24 cm

OB = 25 cm

BA = 14 cm

Area of each equal strips = Area of \triangle le AOB

Now, for area of $\triangle AOB$

Perimeter of ΔAOB

Let 2s = AO + OB + BA

$$\Rightarrow s = \frac{1}{2}(AO + OB + BA)$$

$$=\frac{1}{2}(25+25+14)=32$$
 cm

∴ By using Heron's formulae

Area of
$$(\Delta AOB) = \sqrt{s(s-ao)(s-ob)(s-ba)}$$

$$=\sqrt{32(32-25)(32-25)(32-14)}$$

$$=\sqrt{32(7)(4)(18)}$$

 $= 168 \text{ cm}^2$

 \therefore Area of each type of paper needed to make the hand fan = 5 × (area of $\triangle AOB$)

 $= 5 \times 168$

 $= 840 \text{ cm}^2$

14. A triangle and a parallelogram have the same base and the same area. If the sides of the triangle are 13 cm, 14 cm and 15 cm and the parallelogram stands on the base 14 cm, find the height of the parallelogram.

Sol:

The sides of a triangle DCE are

DC = 15 cm, CE = 13 cm, ED = 14 cm

Let h be the height of parallelogram ABCD

Given,

Perimeter of ΔDCE

 \Rightarrow h = 6 cm

2s = DC + CE + ED
⇒ S =
$$\frac{1}{2}$$
(15 + 13 + 4)
⇒ S = $\frac{1}{2}$ (42)
⇒ S = 21 cm
Area of $\Delta DCE = \sqrt{s(s - dc)(s - ce)(s - ed)}$ [By heron's formula]
= $\sqrt{21(21 - 15)(21 - 13)(21 - 14)}$
= $\sqrt{21 \times 7 \times 8 \times 6}$
= $\sqrt{84 \times 84}$
= 84cm²
Given that
Area of Δ^{le} DCE = area of ABCD
= Area of parallelogram ABCD = 84cm²
⇒ 24 × h = 84 [∴ Area of parallelogram = base × height]