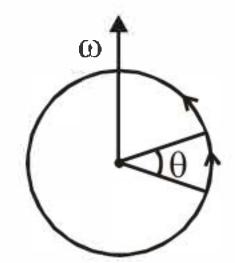
## **CIRCULAR MOTION**

$$\Rightarrow \qquad \omega_{\text{av}} = \frac{\theta_2 - \theta_1}{t_2 - t_1} = \frac{\Delta \theta}{\Delta t}$$

2. Instantaneous angular velocity 
$$\Rightarrow \omega = \frac{d}{d}$$



$$\Rightarrow \qquad \alpha_{av} = \frac{\omega_2 - \omega_1}{t_2 - t_1} = \frac{\Delta \omega}{\Delta t}$$

$$\alpha = \frac{d\omega}{dt} = \frac{d\omega}{d\theta}$$

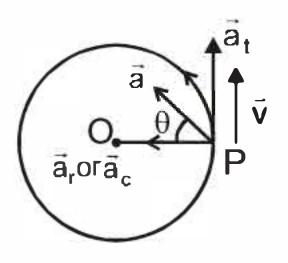
- **5**. Relation between speed and angular velocity  $\Rightarrow v = r\omega$  and  $\vec{v} = \vec{\omega} \times \vec{r}$
- **7**. Tangential acceleration (rate of change of speed)

$$\Rightarrow a_{t} = \frac{dV}{dt} = r \frac{d\omega}{dt} = \omega \frac{dr}{dt}$$

- Radial or normal or centripetal acceleration  $\Rightarrow$   $a_r = \frac{v^2}{r} = \omega^2 r$ 8.
- 9. Total acceleration

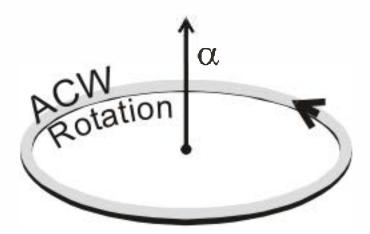
$$\Rightarrow \qquad \vec{a} = \vec{a}_t + \vec{a}_r \Rightarrow a = (a_t^2 + a_r^2)^{1/2}$$

Where 
$$\vec{a}_t = \vec{\alpha} \times \vec{r}$$
 and  $\vec{a}_r = \vec{\omega} \times \vec{v}$ 



10. Angular acceleration

$$\Rightarrow \quad \bar{\alpha} = \frac{d\bar{\omega}}{dt} \text{ (Non-uniform circular motion)}$$



12. Radius of curvature 
$$R = \frac{v^2}{a_{\perp}} = \frac{mv^2}{F_{\perp}}$$

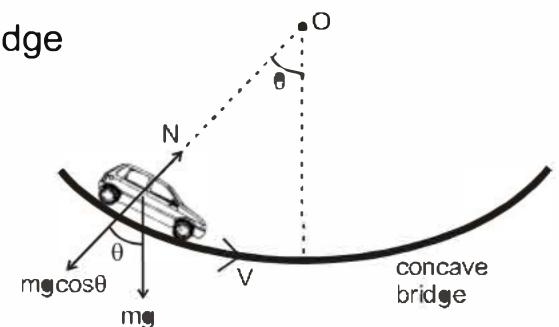
If y is a function of x. i.e.  $y = f(x)$ 

$$\Rightarrow R = \frac{\left[1 + \left(\frac{dy}{dx}\right)^2\right]^{3/2}}{\frac{d^2y}{dx^2}}$$

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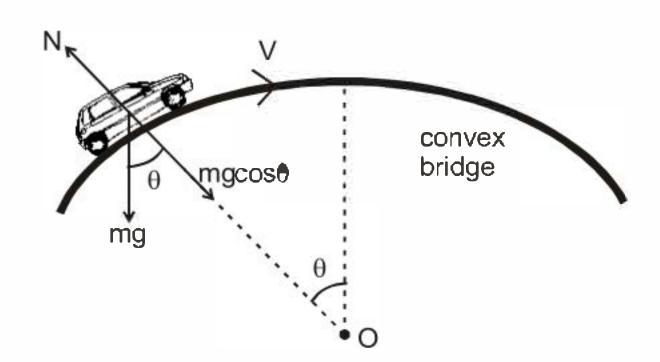
13. Normal reaction of road on a concave bridge

$$\Rightarrow N = mg \cos \theta + \frac{mv^2}{r}$$



14. Normal reaction on a convex bridge

$$\Rightarrow N = \text{mg cos } \theta - \frac{\text{mv}^2}{r}$$



15. Skidding of vehicle on a level road

$$\Rightarrow$$
  $v_{safe} \leq \sqrt{\mu gr}$ 

16. Skidding of an object on a rotating platform

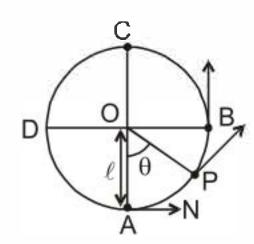
$$\Rightarrow \omega_{\text{max}} = \sqrt{\mu g/r}$$

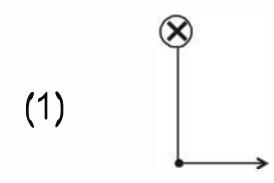
- 17. Bending of cyclist  $\Rightarrow \tan \theta = \frac{v^2}{r_0^2}$
- 18. Banking of road without friction  $\Rightarrow \tan \theta = \frac{v^2}{rg}$
- 19. Banking of road with friction  $\Rightarrow \frac{v^2}{rg} = \frac{\mu + \tan \theta}{1 \mu \tan \theta}$
- 20. Maximum also minimum safe speed on a banked frictional road

$$V_{\text{max}} = \left[ \frac{\text{rg}(\mu + \tan \theta)}{(1 - \mu \tan \theta)} \right]^{1/2} \qquad V_{\text{min}} = \left[ \frac{\text{rg}(\tan \theta - \mu)}{(1 + \mu \tan \theta)} \right]^{1/2}$$

- **21.** Centrifugal force (pseudo force)  $\Rightarrow$  f =  $m\omega^2$  r, acts outwards when the particle itself is taken as a frame.
- 22. Effect of earths rotation on apparent weight  $\Rightarrow$  N = mg mR $\omega^2$  cos $^2\theta$ ; where  $\theta$   $\Rightarrow$  latitude at a place

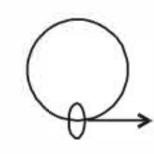
## 23. Various quantities for a critical condition in a vertical loop at different positions





$$V_{min} = \sqrt{4gL}$$

(2)



$$V_{min} = \sqrt{4gL}$$

(3)

$$V_{min} = \sqrt{4gL}$$

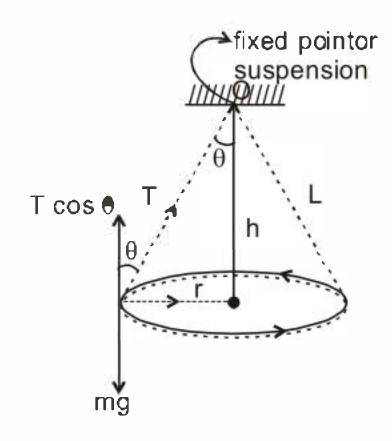
(for completing the circle) (for completing the

(for completing the circle) (for completing the circle)

## 24. Conical pendulum:

T cos θ = mg  
T sin θ = 
$$mω^2$$
 r

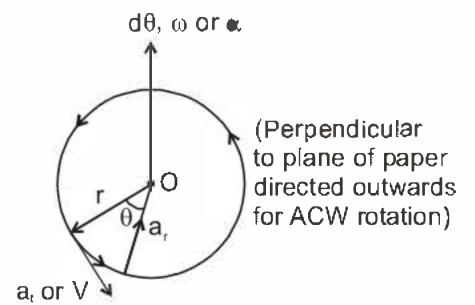
 $2\pi\sqrt{\frac{L\cos\theta}{g}}$ 



## 25. Relations amoung angular variables :

 $\omega_0 \Rightarrow$  Initial ang. velocity

$$\omega = \omega_0 + \alpha t$$



 $\omega \Rightarrow$  Find angular velocity

 $\omega \Rightarrow$  Const. angular acceleration  $\theta \Rightarrow$  Angular displacement

$$\theta = \omega_0 t + \frac{1}{2} \alpha t^2$$

$$\omega^2 = \omega_0^2 + 2\alpha \theta$$