NENG 685 HW 3 Fall 2017 Due Nov. 1, 2017

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On homework:

- If you work with anyone else, document what you worked on together.
- · Show your work.
- Always clearly label plots (axis labels, a title, and a legend if applicable).
- Homework should be done "by hand" (i.e. not with a numerical program such as MATLAB, Python, or Wolfram Alpha) unless otherwise specified. You may use a numerical program to check your work.
- If you use a numerical program to solve a problem, submit the associated code, input, and output (email submission is fine).

Do not write in the table to the right.

Problem	Points	Score	
1	10	6	
2	10	10	
3	10	10	
4	5	5	
5	5	3	
6	10	10	
Total:	50	44	
Iotal:	50	44	

1. (10 points) Determine the macroscopic scattering cross section of UO₂ as a function of a generic enrichment factor $\gamma = N_{U-235}/N_{U-238}$ where N is the atom density. Find its value assuming a density of $10\,\mathrm{g/cm^3}$, $\sigma_s^U \simeq 8.9\,\mathrm{b}$ and $\sigma_s^O \simeq 3.75\,\mathrm{b}$, and 5% weight enrichment.

$$M(U) = M(U^{235}) M(U^{236})$$

$$M(UO_2) = M(U) + M(O_2)$$

$$= \mathcal{E} + (1-\mathcal{E})\mathcal{F}$$

$$\mathcal{M}(U^{238})$$

$$M(U) = M(U^{258})$$
 to incorporate given T

Ouo2 = Ou + 2 Os (Assuming Homogeneous

So
$$\xi_{u \circ z} = \frac{\xi_{u \circ z} \xi_{u \circ$$

term in denom; wrong ans follows

7= N235 - SNA N236 - MU235 - M(U236) PNA M(U238)

6 Nen

$$N_A = 6.022 \times 10^{23}$$
 $M(0) = 15.999$ $M(U^{255}) = 235.643924$

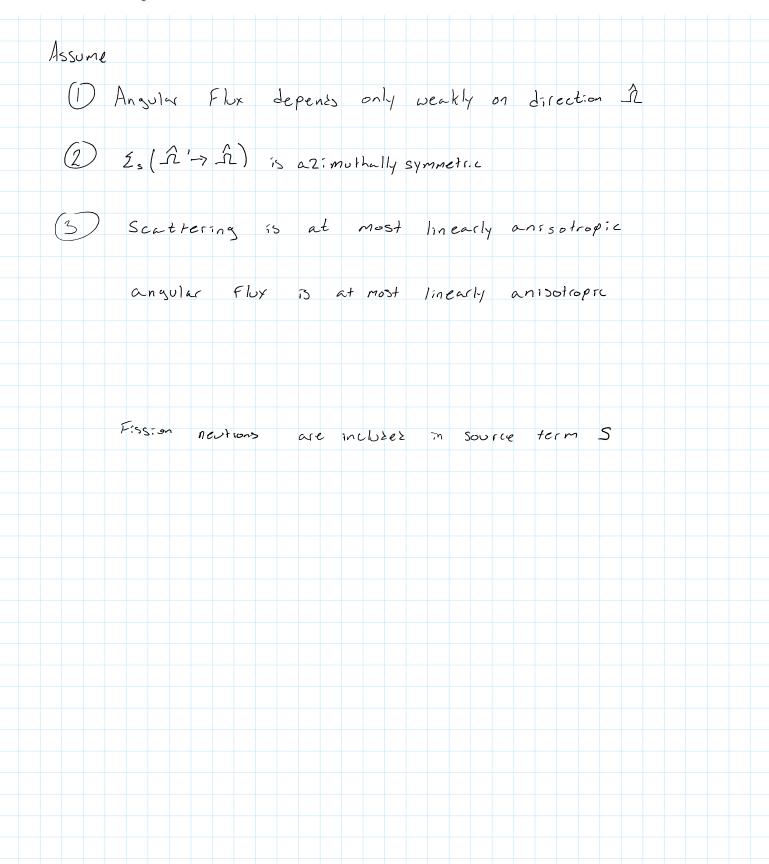
E = 5 %	M(138 U) = 238 .050 941
Juo, = 8.9 1 2 (3.75)	
$\sum_{lb2} = 16.4 $	924
X 10 24 cm	cm3 mu 3
Euon = 2.25093 x 10 [cm]	
2002 = .225 093 [cm-']	

2. (10 points) Briefly describe what each term in the Transport Equation [Eqn. (2)] physically represents.

$$\underbrace{\left[\hat{\Omega} \cdot \nabla \psi(\vec{r}, \hat{\Omega}, E)\right]}_{A} + \underbrace{\Sigma(\vec{r}, E)\psi(\vec{r}, \hat{\Omega}, E)}_{B} = \underbrace{\int_{0}^{\infty} dE' \int_{4\pi} d\hat{\Omega}' \, \Sigma_{s}(\vec{r}, E' \to E, \hat{\Omega}' \cdot \hat{\Omega})\psi(\vec{r}, \hat{\Omega}', E')}_{C} + \underbrace{\frac{\chi(E)}{k} \int_{0}^{\infty} dE' \, \nu \Sigma_{f}(\vec{r}, E') \int_{4\pi} d\hat{\Omega}' \, \psi(\vec{r}, \hat{\Omega}', E')}_{D} \tag{2}$$

Assuming Time independent

3. (10 points) List three assumptions needed to get from the Transport Equation to the Diffusion Equation.



4. (5 points) List four locations where the Diffusion Equation is not valid because the underlying assumptions do not hold; for each explain why the assumptions do not hold

Void (Vaccoum)

The basic premise For why these invalidate
the diffusion equation is the same for
all of them

Bountary

Source

At large differences the DE is no longer linear or in the case or a vacuum non continuous so the problems boundaies are extrapolites.

the

strong Absorber

of the requirements

5. (a) (2 points) Write the **steady state**, 2D diffusion equation and explain how we typically characterize it from the viewpoint of labeling second order linear PDEs. Assume D is not a function of x or y for this part.

$$\frac{1}{V} \frac{\partial}{\partial t} \phi(\vec{r}, t) - \nabla \cdot D \nabla \phi(\vec{r}, t) = V \mathcal{E}_{\vec{r}} \phi(\vec{r}, t) + S(\vec{r}, t)$$

$$-2pts: \text{ steady state implies no dependence on time; it is eliptical}$$

$$\mathcal{U}_{\mathcal{E}} = \mathcal{E}_{\mathcal{E}} \phi(\vec{r}, t) + \mathcal{E}_{\mathcal{E}} \phi(\vec{r}, t) + \mathcal{E}_{\mathcal{E}} \phi(\vec{r}, t)$$

$$\mathcal{U}_{\mathcal{E}} = \mathcal{E}_{\mathcal{E}} \phi(\vec{r}, t) + \mathcal{E}_{\mathcal{E}} \phi(\vec{r}, t) + \mathcal{E}_{\mathcal{E}} \phi(\vec{r}, t) + \mathcal{E}_{\mathcal{E}} \phi(\vec{r}, t)$$

$$\mathcal{U}_{\mathcal{E}} = \mathcal{E}_{\mathcal{E}} \phi(\vec{r}, t) + \mathcal{E}_{\mathcal{E}}$$

(b) (3 points) Can you think of any physical cases in which this characterization would change?

6. (10 points) At what energy is the lowest isolated resonance of 235 U, 238 U, 239 Pu, and 240 Pu? Why do we care about that?

We care	Since it)	ells us	Where L	re Should	aim to	collect energy
from th	le reactor	To a de	estyn para	aneter since	higher r	esonances have
	1 chance o					
	:2e for en					
$^{235}U = 2.$	8351 × 10-1	eV	23	9PU = 2.	9139 X 10	-1 eV
238 U = 6.	6791 eV		240	Po = 1.0	>451 e	\mathcal{V}