

2. Long Answer

$$\begin{aligned} \text{net}_{h_1} &= w_1 \cdot i_1 + w_3 \cdot i_2 + b_1 \cdot 1 \\ &= 0.24(0.8) + 0.43(0.3) + 1 \\ &= 0.192 + 0.129 + 1 \\ &= 1.321 \end{aligned}$$

$$\begin{aligned} \text{net}_{h_2} &= w_2 \cdot i_1 + w_4 \cdot i_2 + b_2 \cdot 1 \\ &= 0.67(0.8) + 0.14(0.3) + 1 \\ &= 0.536 + 0.042 + 1 \\ &= 1.578 \end{aligned}$$

$$\begin{aligned} \text{out}_{h_1} &= \max(0, 1.321) \rightarrow \text{ReLU} \\ &= 1.321 \end{aligned}$$

$$\begin{aligned} \text{out}_{h_2} &= \max(0, 1.578) \rightarrow \text{ReLU} \\ &= 1.578 \end{aligned}$$

$$\begin{aligned} \text{net}_{o_1} &= h_1 \cdot w_{2-1} + h_2 \cdot w_{2-3} + b_2 \cdot 1 \\ &= 1.321(0.34) + 1.578(0.81) + 1(1) \\ &= 0.44914 + 1.27818 + 1 \rightarrow = 2.72732 \end{aligned}$$

$$\begin{aligned} \text{net}_{o_2} &= h_1(w_{2-2}) + h_2(w_{2-4}) + b_2 \cdot 1 \\ &= 1.321(0.63) + 1.578(0.72) + 1(1) \\ &= 0.83223 + 1.13616 + 1 \\ &= 2.96839 \end{aligned}$$

$$\begin{aligned} \text{out}_{o_1} &= \max(0, 2.72732) \rightarrow \text{ReLU} \\ &= 2.72732 \end{aligned}$$

$$\begin{aligned} \text{out}_{o_2} &= \max(0, 2.96839) \rightarrow \text{ReLU} \\ &= 2.96839 \end{aligned}$$

$$E_{\text{total}} = \sum \frac{1}{2} (\text{target} - \text{output})^2$$

$$E_{o_1} = \frac{1}{2} (\text{target}_{o_1} - \text{out}_{o_1})^2$$

$$= \frac{1}{2} (0 - 2.72732)^2$$

$$= 3.7191371912$$

$$E_{o_2} = \frac{1}{2} (\text{target}_{o_2} - \text{out}_{o_2})^2$$

$$= \frac{1}{2} (1 - 2.96839)^2$$

$$= 1.93727959605$$

$$E_{\text{total}} = E_{o_1} + E_{o_2}$$

$$= 3.7191371912 + 1.93727959605$$

$$= 5.65641678725$$

$$\frac{\partial E_{\text{total}}}{\partial \text{out}_{o_1}} = -(\text{target}_{o_1} - \text{out}_{o_1})$$

$$= -(0 - 2.72732) \cdot (-1)(0)$$

$$= 2.72732$$

$$\frac{\partial \text{out}_{o_1}}{\partial \text{net}_{o_1}} = \text{out}_{o_1} (1 - \text{out}_{o_1})$$

$$\text{net}_{o_1} = 2.72732 (1 - 2.72732)$$

$$\text{net}_{o_1} = -4.7109543824$$

$$\frac{\partial w_s}{\partial \text{out}_{h_1}} = \text{out}_{h_1} = 1.321$$

$$\frac{\partial E_{\text{total}}}{\partial w_s} = \frac{\partial E_{\text{total}}}{\partial \text{out}_{o_1}} \cdot \frac{\partial \text{out}_{o_1}}{\partial \text{net}_{o_1}} \cdot \frac{\partial \text{net}_{o_1}}{\partial w_s}$$

$$= 2.72732 (-4.7109543824) (1.321)$$

$$= -16.9726$$

$$w_{2-1}^+ = w_{2-1} - \eta \frac{\partial E_{\text{total}}}{\partial w} = 0.34 - 0.1 (-16.9726) = 2.03726$$

$$w_{2-1} = 0.2037$$

$$w_{2-2}^+ = w_{2-2} - \eta \frac{\partial E_{total}}{\partial w} \quad \frac{\partial E_{total}}{\partial w} = -(target_{o_2} - out_{o_2})$$

$$= 0.63 - 0.1(-18.1489)$$

$$= 2.44489 \rightarrow w_{2-2} = 0.2449$$

$$\frac{\partial out_{n_2}}{\partial net_{o_2}} = -(1 - 2.96839)$$

$$= 1.96839$$

$$w_{2-3}^+ = w_{2-3} - \eta \frac{\partial E_{total}}{\partial w}$$

$$= 0.81 - 0.1(-16.9726)$$

$$= 2.50726 \rightarrow w_{2-3} = 0.2507$$

$$\frac{\partial out_{o_2}}{\partial net_{o_2}} = out_{o_2} (1 - out_{o_2})$$

$$= 2.96839(1 - 2.96839)$$

$$= -5.8429$$

$$w_{2-4}^+ = w_{2-4} - \eta \frac{\partial E_{total}}{\partial w}$$

$$= 0.72 - 0.1(-18.1489)$$

$$= 2.53489$$

$$\frac{\partial net_{o_2}}{\partial w_{2-2}} = out_{n_2}$$

$$= 1.578$$

$$w_{2-4} = 0.2535$$

$$\frac{\partial E_{o_1}}{\partial net_{o_1}} = \frac{\partial E_{o_1}}{\partial out_{n_1}} \cdot \frac{\partial out_{o_1}}{\partial net_{n_1}}$$

$$= -4.7110(2.72732)$$

$$= -12.8484$$

$$\frac{\partial E_{total}}{\partial w_{2-2}} = 1.96839(-5.8429)(1.578)$$

$$= -18.1488979557$$

$$\frac{\partial net_{o_1}}{\partial out_{n_1}} = w_{2-1} = 0.34$$

$$\frac{\partial E_{o_1}}{\partial out_{n_1}} = -12.8484(0.34)$$

$$= -4.3685$$

$$\frac{\partial E_{o_2}}{\partial net_{o_2}} = -5.8429(1.96839)$$

$$= -11.5011$$

$$\frac{\partial net_{o_2}}{\partial out_{n_2}} = w_{2-2} = 0.63$$

$$\frac{\partial E_{o2}}{\partial n_2} = -11.5011(0.63)$$

$$\frac{\partial E_{o2}}{\partial \text{net} n_2} = -7.245693$$

$$\frac{\partial E_{o1}}{\partial n_1} = -12.8484(0.81)$$

$$\frac{\partial E_{o1}}{\partial \text{net} n_1} = -10.407264$$

$$\frac{\partial E_{o2}}{\partial n_2} = -11.5011(0.72)$$

$$\frac{\partial E_{o2}}{\partial \text{net} n_2} = -8.820792$$

$$\frac{\partial E_{o1}}{\partial n_1} = -10.4073 + (-4.36) = -14.7758$$

$$\frac{\partial E_{o2}}{\partial n_2} = -7.2457 + (-8.8208) = -15.526492$$

$$\frac{\partial E_{o2}}{\partial \text{net} n_2} = -15.526492$$

$$\frac{\partial E_{\text{total}}}{\partial \text{net} n_1} = \frac{\partial E_{o1}}{\partial \text{net} n_1} + \frac{\partial E_{o2}}{\partial \text{net} n_2} = -14.7758 + 15.526492 = 0.7507$$

$$\frac{\partial \text{net} n_1}{\partial \text{net} n_1} = \text{net} n_1 (1 - \text{net} n_1) = 0.8(1 - 0.8) = 0.16$$

$$\frac{\partial \text{net} n_1}{\partial w_{1-1}} = i_1 = 0.8$$

$$\frac{\partial E_{\text{total}}}{\partial w_{1-1}} = 0.7507(0.16)(0.8) = 0.096$$

$$\frac{\partial E_{\text{total}}}{\partial w_{1-2}} = 0.7507(0.0819)(0.8) = 0.0492$$

$$\frac{\partial E_{\text{total}}}{\partial w_{1-3}} = 0.7507(0.2491)(0.3) = 0.0561$$

$$\frac{\partial E_{\text{total}}}{\partial w_{1-4}} = 0.7507(0.0819)(0.3) = 0.0184$$

$$\frac{\partial E_{\text{total}}}{\partial w_{1-5}} = 0.7507(0.0819)(0.3) = 0.0184$$

$$\frac{\partial \text{net} n_2}{\partial \text{net} n_2} = 1.09(1 - 1.09) = 0.0819$$

$$w_{1-1} = 0.1496$$

$$w_{1-2} = 0.492$$

$$w_{1-3} = 0.561$$

$$w_{1-4} = 0.184$$