¹ Non-parabolicity and band gap re-normalisation in Si doped ZnO

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Abstract

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7 INTRODUCTION

8 EXPERIMENTAL METHODS

- Films were deposited via RF magnetron sputtering using an AJA Phase II-J Orion system. The system was configured with a 'sputter-up' geometry with the substrate being suspended above two separate ceramic targets of ZnO and SiO₂ that were arranged off-centre and tilted at 5° towards the middle of the substrate. Soda-lime glass substrates (OptiWhiteTM, NSG) of size $100 \times 100 \times 4$ mm³ were used throughout. They were cleaned by scrubbing with a nylon brush and a series of de-ionized water and isopropanol alcohol rinses followed by blow drying with a nitrogen gas jet. During deposition the ZnO and SiO₂ targets were sputtered from simultaneously using powers of 150 W and 50 W respectively. A growth pressure of 2mTorr Ar was used during deposition. The substrate temperature was maintained at 350 \pm 5°C during growth and the substrate was kept static (i.e was not rotated). Deliberate gradients of both thickness and composition were subsequently achieved across the resultant film to generate a 'combinatorial' sample. A second film of pure SiO₂ was deposited under identical conditions (but without ZnO) to generate a reference film for calculating the % wt. 2 profile of SiO₂ in the co-sputtered film.
- A Shimadzu UV-Vis-IR 3700 spectrophotometer with mapping capability was used to measure the transmittance of the co-sputtered film over the range 250 2500 nm. 289 spectra were taken in total at 5 mm increments over the full sample surface. At each of these 289 points the sheet resistance was also measured using a CMT-SR2000 4-point probe mapping system. Following transmittance and sheet resistance measurements the sample was cut into one hundred $10 \times 10 \text{ mm}^2$ pieces. A selection of these pieces, 10 in total, were further scribed into four $5 \times 5 \text{ mm}^2$ sections and Hall measurement were performed on each of these sections. The Hall measurement was performed with custom built equipment, provided by Semimetrics Ltd., using a field strength of 0.8 T. Ellipsometry was performed on the same sections using a Woollam M2000-UI system. Ellipsometry was also used to map the thickness profile of the pure SiO₂ reference film.

34 RESULTS

35 Fitting of optical spectra

Figure 1 shows a typical transmittance spectra taken from a single point on the combinatorial ZnO:Si sample. The full details of the model of the dielectric permittivity, $\varepsilon(\omega)$, used to fit the data are given in [1]. The key components of the model include: 1) a Lorentzian oscillator to account for the behaviour of the system's bound electrons and to provide a smoothly varying dielectric background over the range of interest (250 – 2500 nm), 2) an extended Drude model [2], to characterise the system's free electron response, and 3) an inter-band transition model to account for the steep increase in the material's absorption coefficient ($\alpha \propto (E - E_G)^{1/2}$) in the vicinity of its direct band gap (3.3 – 3.4 eV). The two key parameters extractable from the dielectric model are the film's thickness, d, and plasma frequency, ω_p , which is related directly to the carrier concentration according to

$$\omega_p = \sqrt{\frac{n_e e^2}{m_e \varepsilon_0}} \tag{1}$$

where m_e is the effective electrons (expressed in units of the free electron mass, m_0) and ε_0 47 is the permittivity of free space.

Fitting was achieved by using a Nelder-Mead downhill simplex algorithm [3], implemented via python script, to minimize the quantity

$$\chi^2 = \sum_{i}^{N} \sqrt{\frac{y_i - O_i}{N^2}} \tag{2}$$

where N is the total number of data points in the spectra, O_i the observed transmittance at each wavelength over the range of interest, and y_i the theoretical transmittance calculated using the transfer matrix method [4] for a single thin-film on a finite, transparent substrate. The fitting algorithm was iterated until the relative fractional change in consecutive χ^2 values was less than 1×10^{-6} . The fitting of all 289 transmittance spectra taken over the combinatorial sample was fully automated, the only user input required being an initial estimate of film thickness at the point of the first spectrum. This automation ensured that the fitting of consecutive spectra was highly consistent. For all spectra, χ^2 values of < 1 were achieved indicating that all fits were as successful as that shown in figure 1.

It was not possible to extract accurate values for the optical band-gap E_G from the inter-60 band transition component of the model. All values were typically ~ 0.2 eV lower than expected (even once non-parabolicity and re-normalisation effects had been accounted for, see sections and). This is due to the presence of a population of impurity states located in energy just below the bottom of the conduction band. The presence of these states generate a broadening, commonly referred to as an 'Urbach tail' [5], in the onset of the absorption coefficient. It is very difficult to determine the extent of this broadening by fitting the dielectric model to a single transmittance spectra. The use of variable angle spectroscopic ellipsometry (VASE) was therefore necessary to determine the true band gap of the material. For each point over the combinatorial sample surface a set of three ellipsometric spectra, taken at angles of 60, 65 and 70° with respect to a plane normal to the sample surface, was measured and fitted using a parameterized semi-conductor (PSEMI-M0) model [6] over the range 350 - 1000 nm. The use of multiple spectra allowed the effect of the tail states to be extricated from the direct band to band transitions. Figure 2 shows the difference in the α^2 versus E behaviour extracted from transmittance and ellipsometry data respectively. This disparity between band gaps extracted from the two techniques has been reported previously by Srikant [7].

Conduction band non-parabolicity

For highly doped metal-oxides it has been shown that the conduction band, E_c , is 'nonparabolic' and that the origin of this non-parabolicity may be attributed to a carrier dependent effective mass, $m_e(n_e)$. The functional form of this dependence, first suggested by Pisarkiewicz *et. al* [8], is given by

$$m_e(n_e) = m_{e0} \sqrt{1 + \frac{2C\hbar^2 k}{m_{e0}}}$$
 (3)

where m_{e0} is the value of the effective mass at the conduction band minimum and C is the non-parabolicity factor, expressed in ${\rm eV}^{-1}$. The carrier wave-number can be expressed in terms of the carrier concentration according to $k=(3\pi^2n_e)^{1/3}$. By re-examining equation 1 it is clear that the relationship between ω_p^2 and n_e is becomes non-linear if the effective mass is not a constant. Figure 3 shows a plot of ω_p , extracted from the spectrophotometry measurements, versus the carrier concentration, n_e^H , determined via Hall measurements, for the sample subset cut from the original combinatorial sample. A similar χ^2 minimization procedure to that described in section, in which the fitting parameters were m_{e0} and C,

89 was applied to the data set using

$$\chi^2 = \sum_{i=1}^n \frac{(n_{e_i}^S - n_{e_i}^H)^2}{n^2} \tag{4}$$

where the superscript S corresponds to carrier concentrations calculated, using a carrier dependent effective mass $m_e(n_e)$ (equations (1) a 3), from the spectroscopically determined plasma frequencies. The superscript H denotes values of n_e determined directly via Hall measurements. To determine the uncertainty associated with the fitted m_{e0} and C values a Monte-Carlo style error treatment [9] was implemented within which the χ^2 minimization procedure was performed 1000 times. The inset plot in figure 3 shows the mean $m_e(n_e)$ relationship (solid line) and the corresponding spread (yellow line). An average extracted value of $m_{e0} = 0.35 \pm 0.02 m_0$ is higher than previous published values of $0.24 - 0.28 m_0$ for the effective mass in undoped ZnO. An average extracted value of $C = 0.30 \pm 0.01$ eV agrees very well with previously reported values of ~ 0.29 ev⁻¹ [10, 11] for Al doped ZnO films.

100 Band-gap renormalization

The optical band gap of a degenerately doped metal-oxide system increases as a function of carrier concentration (Burstein-Moss shift [12, 13] according to

$$E_G = E_{G0} + \frac{\hbar^2 (3\pi^2 n_e)^{2/3}}{2m_{eff}} \tag{5}$$

where E_{G0} is the band-gap at the conduction band minimum and the joint density of states effective mass, m_{eff} is given as

$$\frac{1}{m_{eff}} = \frac{1}{m_h} + \frac{1}{m_e(n_e)} \tag{6}$$

A constant hole effective mass value of $m_h = 0.7m_0$ [] is assumed throughout this work. Note that the non-parabolicity of the conduction band is accounted for when estimating the band gap by using the carrier dependent effective mass $m_e(n_e)$ determined in section . The data points in figure 4 show the band-gap values, determined via ellipsometry, plotted against the Hall carrier concentrations. The points lie some distance from the relationship predicted by equation 5. The apparent reduction in the real band-gap values is due the re-normalization effects of many body electron-electron, electron-ion and hole-hole interactions. Lu et. al

112 [14] have shown that the total energy shift due to re-normalization can be estimated by parameterising the detailed model described by *Jain et. al* according to

$$E_R = An_e^{1/3} + Bn_e^{1/4} + Cn_e^{1/2} (7)$$

where E_R is negative with respect to E_G . The $n_e^{1/3}$, $n_e^{1/4}$ and $n_e^{1/2}$ dependencies correspond to the exchange energy of free electrons, their correlation energy and the electron-ion interaction energy respectively. The coefficients A, B, and C, quantify the strength of each of these three dependencies. The coefficient values for the data shown in figure 4, and a value for E_{G0} , was extracted using the established minimisation procedure. Table I show the extracted values and comparative values for n-type ZnO thin-films. The strength of the $n_e^{1/3}$ dependence is roughly three times than that reported for Al doped ZnO.

121 MAPPING OF COMPOSITIONAL DEPENDENCE

Film thickness profiles were determined for the combinatorial ZnO:Si and SiO₂ samples. The % wt. SiO₂ content at each point over the combinatorial sample was estimated according to

$$x = \frac{\Gamma_B d_B}{\Gamma_A d_A + \Gamma_B d_B} \times 100\% \tag{8}$$

where Γ_A and Γ_B are the bulk densities of ZnO and SiO₂ respectively and d_A and d_B are the corresponding thicknesses, d, of the ZnO and SiO₂ films. The carrier concentration profile for the combinatorial sample was calculated from extracted ω_p^S values according to equation 128 1 and using the non-parabolic effective mass relationship, $m_e(n_e)$, determined in section . 129 The corresponding mobility profile was calculated according to

$$\mu_e = \frac{1}{n_e^S R_S de} \tag{9}$$

where R_S are the sheet resistance values obtained directly from 4 point probe measurements. Figure 3 shows the three dimensional contour profiles of n_e and μ_e accross the surface of the combinatorial sample. In both cases, a maximal ridge, corresponding to $n_e \sim 4.5 \text{ cm}^{-3}$ an $\mu_e \sim 16 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$, runs diagonally across the sample. By superimposing the contour distribution of % wt. SiO₂ content (dotted black contour lines) a very strong correlation between carrier concentration and composition becomes apparent, the maximum n_e and μ_e values corresponding to a value of x = 0.65% wt. SiO₂ content.

By plotting the distributions of n_e and μ_e with respect to x the compositional dependence can be observed directly, see figure 4. Here the strength of the combinatorial analysis is fully appreciated by its ability to generate continuous, non-ambiguous distributions of the material's electrical behaviour and shows that it is highly sensitive to the composition—the resistivity spanning over three orders of magnitude within the compositional range x = 0-0.65% wt. SiO₂. Furthermore, the uncertainty in the optimum value of x, that minimises the resistivity, is significantly reduced when compared to the multi-sample analyses that are commonly reported.

The solid straight line in the n_e vs x plot indicates the relationship predicted for 100% doping efficiency, i.e. where every Si atom incorporated into film substitutionally replace a I47 Zn atom and contributes two free electrons to the system. For low values of x, i.e. in the I48 range 0-0.5% wt. SiO₂, this relationship is adhered to. However as x increases further the I49 doping efficiency decreases rapidly and the carrier concentration is limited to $3-4\times10$ cm⁻³ for compositions up to 10% wt. SiO₂. After the optimum value of x is reached the mobility I51 drops off steeply and approaches a value of zero for values of x beyond 6%. This suggests that as x is increased beyond the optimum composition, Si is no longer incorporated into I53 the film as a substitutional dopant and substitutionally acts to increase the scattering of the I54 free carriers existing as an interstitial impunities or forming segregated Si-O phases at the I55 grain boundaries of the material.

156 CONCLUSIONS

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FIG. 2.

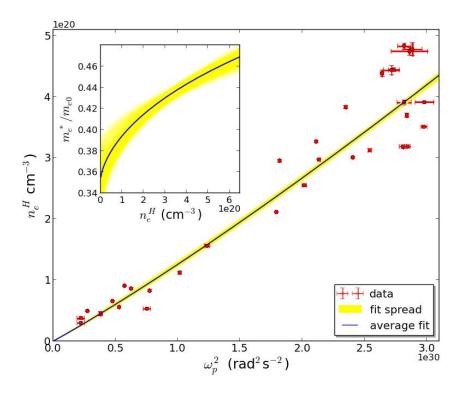


FIG. 3.

Parameter 1	Extracted Value	Copmparison [14]
$A (\times 10^{-8} \text{ eV.cm})$	2.1 ± 0.8	0.69
$B~(\times 10^{-7}~\mathrm{eV.cm^{3/2}})$	3.0 ± 2.6	1.6
$C~(\times 10^{-7}~\mathrm{eV.cm^{3/4}})$	8.7 ± 1.5	7.76
E_{G0} (eV)	3.41 ± 0.01	-

TABLE I. This is the caption

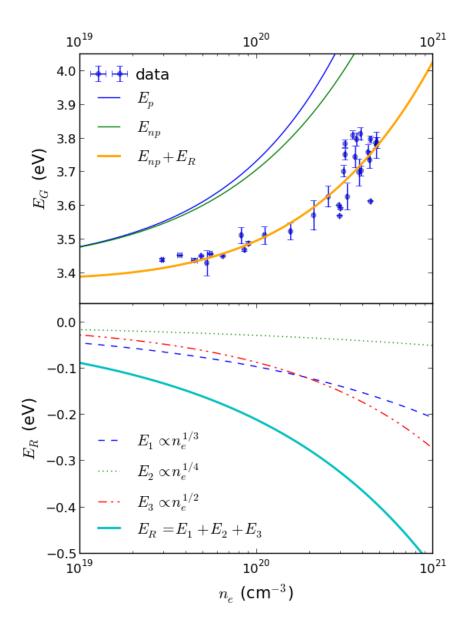


FIG. 4.

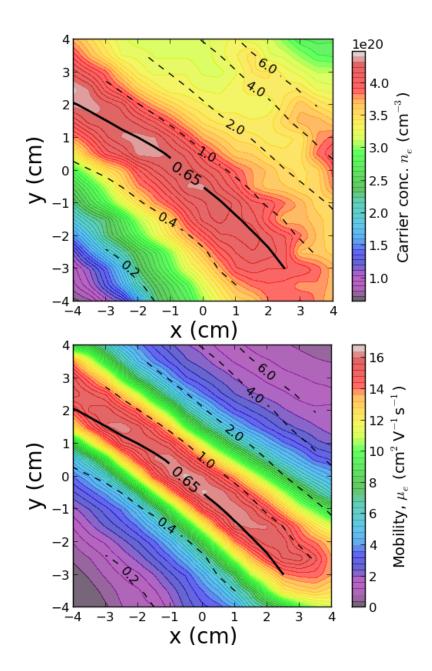


FIG. 5. Contour maps of carrier concentration and mobility over the combinatorial sample. The (-) contour lines show an overlay of the % wt. SiO₂ composition.

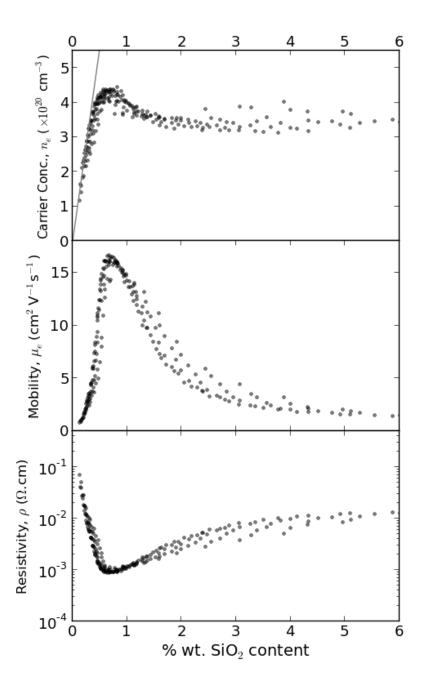


FIG. 6. Distributions of carrier concentration, mobility and resistivity with respect to % wt. SiO₂ content. The maximum values for n_e (4.4 × 10²⁰ cm⁻³) and μ_e (16.5 cm²V⁻¹s⁻¹) coincide with a composition of 0.65% wt. SiO₂. The solid straight line in the top plot shows the maximum theoretical carrier concentration with respect to SiO₂ content should every incorporated Si atom be substituted at a Zinc site and donate 2 carriers.

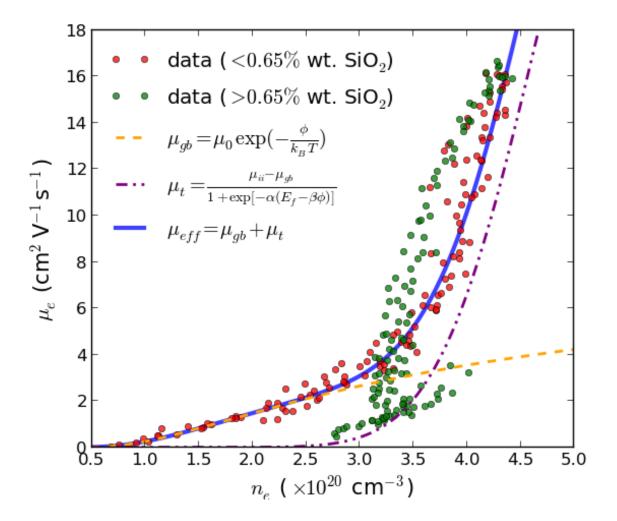


FIG. 7.