

## Optical Constants of ZnO

Hisashi YOSHIKAWA and Sadao ADACHI

Department of Electronic Engineering, Faculty of Engineering, Gunma University, Kiryu, Gunma 376, Japan

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The complex dielectric functions,  $\varepsilon(E) = \varepsilon_1(E) + i\varepsilon_2(E)$ , of ZnO have been measured by spectroscopic ellipsometry (SE) in the photon-energy range between 1.5 and 5.0 eV at room temperature. The SE measurements are carried out on the surface parallel to the optic axis  $c$ , which allows the determination of the optical constants for light polarized perpendicular ( $E \perp c$ ) and parallel to the  $c$ -axis ( $E \parallel c$ ). The measured SE spectra show the exciton peaks at  $\sim 3.4$  eV ( $E_0$  edge). These  $\varepsilon(E)$  spectra are analyzed on the basis of a simplified model of the interband transitions. Excellent agreement is achieved between the calculated and experimental results over the entire range of photon energies. Dielectric-function-related optical constants, such as the complex refractive index  $n^*(E) = n(E) + ik(E)$ , absorption coefficient  $\alpha(E)$  and normal-incidence reflectivity  $R(E)$ , of ZnO have also been reported.

KEYWORDS: ZnO, optical constant, dielectric function, refractive index, optical absorption, spectroscopic ellipsometry

### 1. Introduction

Zinc oxide (ZnO) is a member of the II–VI semiconducting compounds and has a wide band gap,  $\sim 3.4$  eV at 300 K.<sup>1)</sup> It has been used extensively as a photoconducting and fluorescent material, being effective in the visible-to-ultraviolet spectral region. The excellent optical, piezoelectric and acousto-optic properties of ZnO film also make it possible to fabricate solar cell windows,<sup>2)</sup> gas sensors,<sup>3)</sup> surface acoustic wave devices<sup>4)</sup> and integrated acousto-optic devices.<sup>5)</sup>

Accurate knowledge of the refractive index and the absorption coefficient of semiconductors is indispensable for the design and analysis of various optical and optoelectronic devices. Note that ZnO crystallizes in the wurtzite structure [space group =  $P6_3mc$  ( $C_{6v}^4$ )]. The material is thus optically anisotropic (uniaxial). Although there have been many reports on the optical constants of ZnO,<sup>6–18)</sup> currently available data in the visible-to-ultraviolet region is less than adequate.

Spectroscopic ellipsometry (SE) is an advantageous technique to investigate the optical constants of semiconductors, in particular, for determining the complex dielectric function  $\varepsilon(E) = \varepsilon_1(E) + i\varepsilon_2(E)$ . On-line digitization of the data permits the fast and efficient analysis of the structure observed in the  $\varepsilon(E)$  spectra in terms of theoretical line shapes for interband critical points (CPs).<sup>19)</sup> While most of the SE works have been confined to optically isotropic materials,<sup>20)</sup> the usefulness of this technique in the study of anisotropic systems has also been demonstrated (e.g., GaSe,<sup>21)</sup> GeSe<sub>2</sub>,<sup>22)</sup> GeS,<sup>23,24)</sup> CdSe,<sup>25,26)</sup> SnSe,<sup>27)</sup>  $\alpha$ -Al<sub>2</sub>O<sub>3</sub>,<sup>28)</sup> and CdS<sup>29)</sup>).

In this paper we present the dielectric-function spectra ( $\varepsilon = \varepsilon_1 + i\varepsilon_2$ ) of ZnO for light polarized perpendicular ( $E \perp c$ ) and parallel to the  $c$ -axis ( $E \parallel c$ ) measured by SE in the infrared-near-ultraviolet region (1.5–5.0 eV) at room temperature. It is of both technical and scientific interest to obtain the analytical expression for the optical constants of semiconductors. Therefore, we model our measured  $\varepsilon(E)$  spectra using a simplified model of the interband transitions. The model includes the lowest-direct gap  $E_0$  as the main dispersion mechanism. Dielectric-function-related optical constants, such

as the complex refractive index,  $n^*(E) = n(E) + ik(E)$ , absorption coefficient  $\alpha(E)$  and normal-incidence reflectivity  $R(E)$ , are also presented.

### 2. Theoretical Model

The fundamental absorption edge of ZnO corresponds to the direct transition from the highest valence band to the lowest conduction band at the  $\Gamma$  point ( $k = 0$ ). Figure 1 shows a schematic of the conduction and valence band structures at the  $\Gamma$  point of the zinc-blende (cubic) and wurtzite (hexagonal) crystals. In the hexagonal lattice, the conduction band is  $s$ -like, having  $\Gamma_7$  symmetry. The valence band is  $p$ -like, splitting into three doubly degenerate bands with quantum numbers  $J_z = 1/2$  ( $\Gamma_7$ ),  $3/2$  ( $\Gamma_9$ ) and  $1/2$  ( $\Gamma_7$ ) due to the spin-orbit and crystal field interactions. For convenience, the denotations  $A$ ,  $B$  and  $C$  are used for these three valence bands. Note that in CdSe and CdS the  $A$  valence band has  $\Gamma_9$  symmetry with  $J_z = 3/2$ , while  $B$  and  $C$  have  $\Gamma_7$  symmetry with  $J_z = 1/2$ .<sup>26,29)</sup> In the cubic lattice, the  $p$ -like valence band is split due to the spin-orbit interaction into a fourfold degenerate  $\Gamma_8$  state and a twofold degenerate  $\Gamma_7$  state (see Fig. 1).

The polarization vectors  $E \perp c$  and  $E \parallel c$  in the hexagonal lattice ( $C_{6v}^4$ ) belong to the  $\Gamma_5$  and  $\Gamma_1$  symmetries, respectively.<sup>30)</sup> The direct products between the conduc-

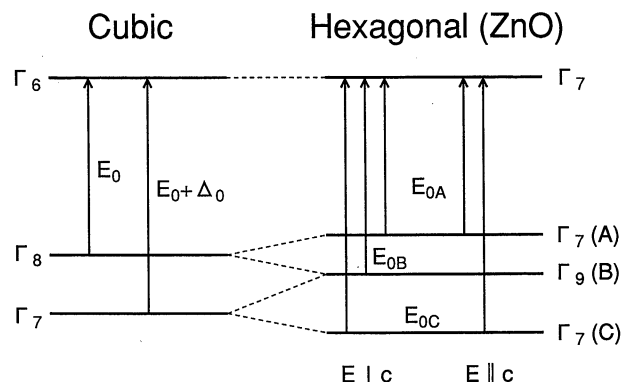


Fig. 1. Energy gaps at the  $\Gamma$  point of the zinc-blende (cubic) and wurtzite (hexagonal) lattices. Note that the  $E_{0B}$  transitions are forbidden for  $E \parallel c$ .

tion and valence band states can be given by

$$\Gamma_7^v(A) \rightarrow \Gamma_7^c : \Gamma_7 \times \Gamma_7 = \Gamma_1 + \Gamma_2 + \Gamma_5, \quad (1.a)$$

$$\Gamma_9^v(B) \rightarrow \Gamma_7^c : \Gamma_9 \times \Gamma_7 = \Gamma_5 + \Gamma_6, \quad (1.b)$$

$$\Gamma_7^v(C) \rightarrow \Gamma_7^c : \Gamma_7 \times \Gamma_7 = \Gamma_1 + \Gamma_2 + \Gamma_5. \quad (1.c)$$

The direct product  $\Gamma_7 \times \Gamma_7$  thus contains the representations for both  $E \perp c$  ( $\Gamma_5$ ) and  $E \parallel c$  ( $\Gamma_1$ ), but  $\Gamma_9 \times \Gamma_7$  contains only the representation for  $E \perp c$  ( $\Gamma_5$ ). This means that for  $E \parallel c$  the optical transitions between the  $B$  valence and conduction bands are forbidden while all the optical transitions are possible for  $E \perp c$  (see Fig. 1).

The optical constants in the interband transition region of the crystalline materials depend fundamentally on the electronic energy-band structure of the materials. The  $E_0$  gaps in the hexagonal crystals are of the three-dimensional (3D)  $M_0$  CP. Assuming the conduction and valence bands are parabolic and using the Kramers–Kronig (KK) transformation, we obtain the contribution of these gaps to  $\varepsilon(E)$ :<sup>31)</sup>

$$\varepsilon(E) = \sum_{\alpha=A,B,C} A_{0\alpha} E_{0\alpha}^{-1.5} f(\chi_{0\alpha}), \quad (2)$$

with

$$A_{0\alpha} = \frac{4}{3} \left( \frac{3}{2} \mu_{0\alpha} \right)^{1.5} P_{0\alpha}^2, \quad (3)$$

$$f(\chi_{0\alpha}) = \chi_{0\alpha}^{-2} [2 - (1 + \chi_{0\alpha})^{1/2} - (1 - \chi_{0\alpha})^{1/2}], \quad (4)$$

$$\chi_{0\alpha} = (E + i\Gamma)/E_{0\alpha}. \quad (5)$$

In eqs. (2)–(5),  $\mu_{0\alpha}$  is the combined density-of-states mass,  $P_{0\alpha}^2$  is the squared momentum-matrix element,  $\Gamma$  is the broadening energy of the  $E_{0\alpha}$  gap and  $\alpha$  ( $= A, B, C$ ) denotes the  $\Gamma_7(A) \rightarrow \Gamma_7$ ,  $\Gamma_9(B) \rightarrow \Gamma_7$  and  $\Gamma_7(C) \rightarrow \Gamma_7$  transitions, respectively.

It is well known that the excitonic interaction in the neighborhood of the lowest-direct band edge of semiconductors dramatically changes the optical spectra.<sup>32)</sup> The excitonic transitions play an important role in the fundamental optical process, since the Coulomb interaction is always present between the electrons and the holes. The hydrogenic effective-mass equation provides the solutions of the discrete and the continuum parts of the exciton states.<sup>32)</sup> The discrete series of the exciton states at the  $E_{0\alpha}$  gap can be simply written, with the Lorentzian line shape, as<sup>31)</sup>

$$\varepsilon(E) = \sum_{\alpha=A,B,C} \sum_{n=1}^{\infty} \frac{A_{0\alpha}^{n\alpha}}{E_{x0}^{n\alpha} - E - i\Gamma}, \quad (6)$$

where  $A_{0\alpha}^{n\alpha}$  is the discrete-exciton strength parameter and  $E_{x0}^{n\alpha}$  is the discrete-exciton energy given by

$$E_{x0}^{n\alpha} = E_{0\alpha} - \frac{G_{0\alpha}^{3D}}{n^2}. \quad (7)$$

In eq. (7)  $G_{0\alpha}^{3D}$  is the 3D-exciton Rydberg energy. The 3D-exciton strength parameter  $A_{0\alpha}^{n\alpha}$  is proportional to the envelope function ( $|\phi_{n\alpha}^{3D}|^2$ ) of the  $n$ th exciton,

$$|\phi_{n\alpha}^{3D}|^2 = \frac{V_0}{\pi(a_{B\alpha}^{3D})^3} n^3, \quad (8)$$

where  $a_{B\alpha}^{3D}$  is the 3D-exciton Bohr radius and  $V_0$  is the

volume of the unit cell.

The contribution of the continuum excitons to  $\varepsilon(E)$  is given by

$$\varepsilon(E) = \sum_{\alpha=A,B,C} \frac{A_{0\alpha}^{C\alpha} E_{0\alpha}^{C1}}{4G_{0\alpha}^{3D}(E + i\Gamma)^2} \ln \frac{(E_{0\alpha})^2}{(E_{0\alpha})^2 - (E + i\Gamma)^2}, \quad (9)$$

where  $A_{0\alpha}^{C\alpha}$  is the continuum-exciton strength parameter and  $E_{0\alpha}^{C1}$  is the ground-state exciton energy ( $\sim E_{0\alpha}$ ). The strength parameter  $A_{0\alpha}^{C\alpha}$  is proportional to the envelope function ( $|\phi_k(0)|^2$ ) of the continuum-exciton state ( $|k\rangle$ ),

$$|\phi_k(0)|^2 = \frac{\pi\alpha_k e^{\pi\alpha_k}}{N \sinh(\pi\alpha_k)} = \frac{2\pi\alpha_k}{N(1 - e^{\pi\alpha_k})}, \quad (10)$$

with

$$\alpha_k = \left| \frac{G_{0\alpha}^{3D}}{E - E_{0\alpha}} \right|^{1/2} = \left| \frac{G_{0\alpha}^{3D}}{(\hbar^2 k^2 / 2\mu)} \right|^{1/2}. \quad (11)$$

In eqs. (10) and (11),  $N$  is the number of the unit cell in the crystal,  $\mu$  is the exciton reduced mass, and  $k$  is the wave vector of the continuum exciton.

The fundamental reflectivity spectra of ZnO reveal the CPs at energies higher than 7 eV.<sup>12–14)</sup> These CPs may correspond to transitions at several points ( $U$ ,  $M$ , etc.) in the Brillouin zone and/or core exciton transitions. Since these transitions occur at energies well above our experimental range ( $\leq 5$  eV), we will not discuss these contributions to  $\varepsilon(E)$ .

### 3. Experimental

The ZnO single crystals used were purchased from the Fujitoku Corporation, Japan. They were grown by a vapor-phase method, not intentionally doped, and their surfaces were oriented parallel to the  $c$  axis. The crystals were mechanically polished with a diamond paste and degreased in organic solvents.

The automatic ellipsometer used was of the polarizer-sample-rotating-analyzer type (DVA-36VW-A, Mizojiri Optical, Co., Ltd., Japan). A 150 W xenon lamp was used as the light source. The SE data were obtained over the photon-energy range of 1.5–5.0 eV at room temperature. The angle of incidence and the polarizer azimuth were set at 70° and 20°, respectively.

Ellipsometry yields the complex ratio  $\rho$  between Fresnel's reflection coefficients  $r_p$  and  $r_s$ ,<sup>33)</sup>

$$\rho = \frac{r_s}{r_p} = \tan \psi e^{i\Delta}, \quad (12)$$

where  $\Delta$  and  $\psi$  are the ellipsometric variables. At each photon energy  $E = \hbar\omega$ , the four optical parameters ( $\varepsilon_{1\perp}$ ,  $\varepsilon_{2\perp}$ ,  $\varepsilon_{1\parallel}$ ,  $\varepsilon_{2\parallel}$ ) can be determined from two pairs of SE measurements [ $\rho^{\text{meas}}$  ( $\delta = 0^\circ$  and  $\delta = 90^\circ$ )] by minimizing the error function  $G(\varepsilon_{1\perp}, \varepsilon_{2\perp}, \varepsilon_{1\parallel}, \varepsilon_{2\parallel})$ ,<sup>25, 26, 29)</sup>

$$G(\varepsilon_{1\perp}, \varepsilon_{2\perp}, \varepsilon_{1\parallel}, \varepsilon_{2\parallel}) = \sum_{\delta=0^\circ, 90^\circ} \{ |\text{Re}(\rho_\delta^{\text{meas}}) - \text{Re}(\rho_\delta^{\text{cal}})|^2 + \{ \text{Im}(\rho_\delta^{\text{meas}}) - \text{Im}(\rho_\delta^{\text{cal}}) \}^2 \}, \quad (13)$$

where  $\rho^{\text{meas}}$  ( $\delta = 0^\circ$  and  $\delta = 90^\circ$ ) are the reflection coefficients measured with that the  $c$  axis is parallel to both the interface and plane of incidence ( $\delta = 0^\circ$ ) or is parallel to the interface and perpendicular to the plane of incidence ( $\delta = 90^\circ$ ).  $\rho^{\text{cal}}$  is the calculated reflection co-

efficient ratio.

#### 4. Results and Discussion

##### 4.1 SE spectra

In Fig. 2 we show the pseudodielectric-function spectra of ZnO for both  $E \perp c$  and  $E \parallel c$  measured by SE at room temperature (solid lines). Note that the pseudodielectric function is a quantity obtained from SE by means of the two-phase (ambient/substrate) model.<sup>33)</sup> It is, thus, exactly equal to the true bulk dielectric function of a given sample if its surface is perfectly smooth and is film-free. Such an ideal condition can never be achieved in practice. Because neither the thickness nor the dielectric properties of the residual surface overlayer (oxide) are known, we did not attempt any correction for them. The SE data were also taken without correction for any surface roughness.

For comparison, the data obtained from the fundamental reflectivity by Freeouf<sup>14)</sup> and those obtained from SE by Matz and Lüth<sup>17)</sup> are plotted in Fig. 2 by the dashed and dotted lines, respectively. Klucker *et al.*<sup>13)</sup> also obtained the dielectric-function spectra of ZnO from the reflectivity data by means of KK analysis. However, the  $\epsilon_2$  peak values obtained for both polarizations ( $\sim 5$ ) are much larger than those plotted in Fig. 2.

In Figs. 3 and 4 the pseudodielectric-function spectra of ZnO measured by us are shown by the solid circles. The main peaks in  $\epsilon_2$  (Fig. 4) at  $\sim 3.4$  eV for both  $E \perp c$  and  $E \parallel c$  correspond to transitions at the fundamental absorption edge ( $E_0$ ) of ZnO. The theoretical model given in Sec. II can be used to fit the experimen-

tal dispersion of  $\epsilon(E)$  over most of the spectral range. The parameters, such as  $E_{0\alpha}$  and  $A_{0\alpha}$  ( $\alpha = A, B$  and  $C$ ), are commonly used as adjustable constants for the

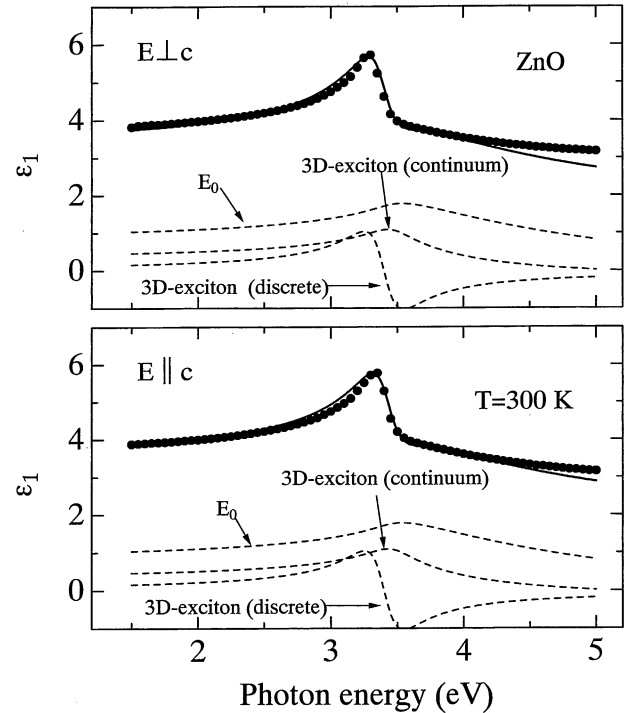


Fig. 3.  $\epsilon_1(E)$  spectrum for ZnO measured by SE at room temperature (solid circles). The solid lines represent the best-fitted results of our model to the experimental data. Individual contributions to  $\epsilon_1(E)$  of the various types of transitions are also shown by the dashed lines. They are obtained from eq. (2) for the one-electron contribution ( $E_0$ ), from eq. (6) for the discrete-exciton contribution and from eq. (9) for the continuum-exciton contribution. The fit-determined CP parameters are listed in Table I.

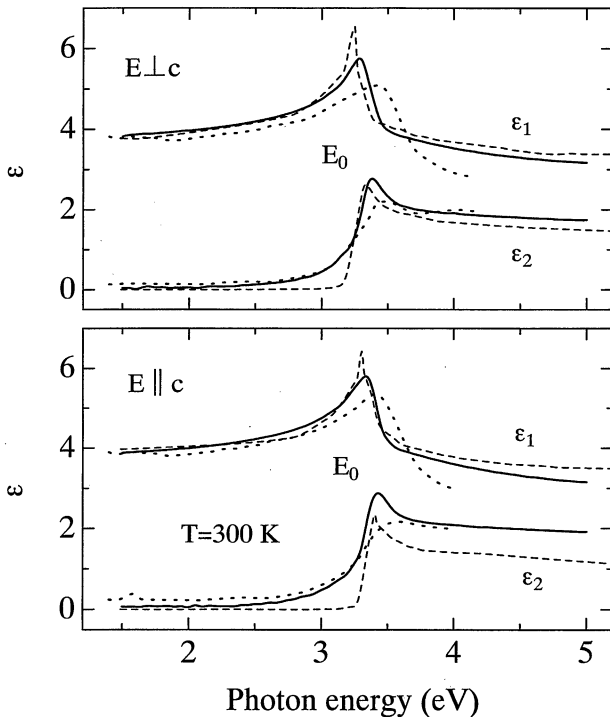


Fig. 2. Pseudodielectric-function spectra for ZnO measured by SE at room temperature (solid lines). For comparison, the fundamental-reflectivity data by Freeouf (ref. 14) and the SE data by Matz and Lüth (ref. 17) are also shown by the dashed and dotted lines, respectively.

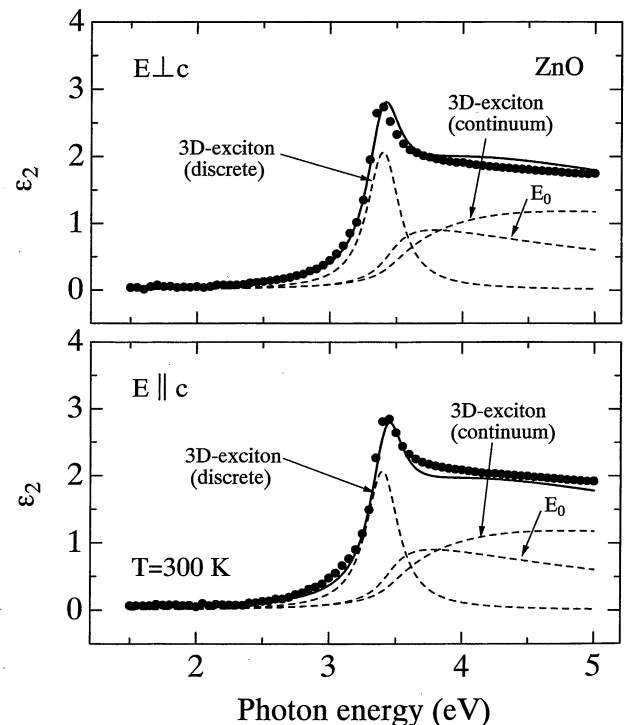


Fig. 4. As for Fig. 3, but for  $\epsilon_2(E)$ .

Table I. Parameters used in the calculation of optical constants for ZnO.

Parameter	Polarization	
	$E \perp c$	$E \parallel c$
$E_{0A}$ (eV)	3.450	3.450
$E_{0B}$ (eV)	3.453	
$E_{0C}$ (eV)	3.484	3.484
$G_{0\alpha}^{3D}$ (meV)	59	59
$A_{0A}$ (eV <sup>1.5</sup> )	12.45	0.10
$A_{0B}$ (eV <sup>1.5</sup> )	12.50	
$A_{0C}$ (eV <sup>1.5</sup> )	0.05	24.90
$A_{0x}^{1A}$ (eV)	0.13	0.001
$A_{0x}^{1B}$ (eV)	0.13	
$A_{0x}^{1C}$ (eV)	0.001	0.259
$A_{0x}^{CA}$ (eV <sup>2</sup> )	0.165	0.001
$A_{0x}^{CB}$ (eV <sup>2</sup> )	0.164	
$A_{0x}^{CC}$ (eV <sup>2</sup> )	0.006	0.329
$\Gamma(E_{0A})$ (eV)	0.145	0.145
$\Gamma(E_{0B})$ (eV)	0.145	
$\Gamma(E_{0C})$ (eV)	0.145	0.145
$\varepsilon_{1\infty}$	2.09	2.18

calculations of both  $\varepsilon_1$  ( $=\text{Re}\varepsilon$ ) and  $\varepsilon_2$  ( $=\text{Im}\varepsilon$ ). The experimental  $\varepsilon_1(E)$  values are, however, usually somewhat larger than those obtained from our theoretical model. In order to improve the fit, therefore, we consider an additional term,  $\varepsilon_{1\infty}$ , to  $\varepsilon_1$ . This term is assumed to be constant and may arise from other higher-lying gaps and core exciton transitions.

The solid lines in Figs. 3 and 4 are obtained from the sum of eqs. (2), (6), (9) and  $\varepsilon_{1\infty} = 2.09$  (2.18) for  $E \perp c$  ( $E \parallel c$ ). The best-fit parameters are listed in Table I. Individual contributions to  $\varepsilon_1$  and  $\varepsilon_2$  of the various types of transitions are also shown in these figures by the dashed lines. They are obtained from eq. (2) for the one-electron contribution, from eq. (6) for the discrete-exciton contribution and from eq. (9) for the continuum-exciton contribution.

The  $E_0$  CP is of the 3D  $M_0$  type. Hence, the line shape of the corresponding one-electron  $\varepsilon_2(E)$  spectrum [eq. (2)] is characterized by a continuous absorption obeying the well-known 1/2-power law,  $\varepsilon_2 \propto (E - E_0)^{1/2}$ . The excitonic states should, in principle, exist at each type of CP, since the Coulomb interaction is always present between the electrons and the holes. The 3D-exciton absorption spectrum consists of a series of sharp discrete lines with a rapidly decreasing oscillator strength  $\propto n^{-3}$  [eq. (6)] and a continuum absorption due to the continuum (ionized) states [eq. (9)]. Recently, Mang *et al.*<sup>34)</sup> determined the exciton Rydberg energies of  $G_{0\alpha}^{3D}$  of ZnO using two-photon absorption spectroscopy to be  $G_{0A}^{3D} = 63.1$  meV,  $G_{0B}^{3D} = 50.4$  meV and  $G_{0C}^{3D} = 48.9$  meV. For simplicity, however, we have assumed in the present analysis that  $G_{0\alpha}^{3D} = 59$  meV ( $\alpha = A, B, C$ ).<sup>35)</sup>

It is understood from Fig. 4 that the continuum-exciton transitions at the  $E_0$  edge [eq. (9)] behave like the one-electron characteristics [eq. (2)]. The deviations of the continuum-exciton spectrum from the one-electron spectrum are usually described by the so-called Sommer-

feld or Coulomb enhancement factor.<sup>36)</sup>

The lowest-direct band gap  $E_0$  of the wurtzite crystals can be obtained from that of zinc-blende by the action of a small hexagonal crystal field.<sup>37,38)</sup> Under the spin-orbit interaction, represented by the matrix element  $\Delta_{so}$ , and that of the crystal field, represented by  $\Delta_{cr}$ , the energy differences of the split-off valence bands are given by

$$E_{AB} = E_{0A} - E_{0B} = \frac{\Delta_{so} + \Delta_{cr}}{2} - \left[ \left( \frac{\Delta_{so} + \Delta_{cr}}{2} \right)^2 - \frac{2}{3} \Delta_{so} \Delta_{cr} \right]^{1/2}, \quad (14.a)$$

$$E_{CB} = E_{0C} - E_{0B} = \frac{\Delta_{so} + \Delta_{cr}}{2} + \left[ \left( \frac{\Delta_{so} + \Delta_{cr}}{2} \right)^2 - \frac{2}{3} \Delta_{so} \Delta_{cr} \right]^{1/2}. \quad (14.b)$$

The corresponding wave functions of the three valence bands are

$$|A\rangle : \alpha_A S_- \uparrow + \alpha_C S_0 \downarrow, \quad (15.a)$$

$$|B\rangle : S_+ \uparrow, \quad (15.b)$$

$$|C\rangle : \alpha_C S_- \uparrow + \alpha_A S_0 \downarrow, \quad (15.c)$$

where  $\uparrow$  and  $\downarrow$  represent spin-up and spin-down, respectively, and  $S_+$ ,  $S_-$  and  $S_0$  are functions defined by the  $p$ -like basis functions. The admixture coefficients  $\alpha_A$  and  $\alpha_C$  are written as

$$\alpha_A = \left[ 1 + \frac{1}{2} \left( 2 - \frac{3}{\Delta_{so}} E_{AB} \right)^2 \right]^{-1/2}, \quad (16.a)$$

$$\alpha_C = \left[ 1 + \frac{1}{2} \left( 2 - \frac{3}{\Delta_{so}} E_{CB} \right)^2 \right]^{-1/2}, \quad (16.b)$$

where  $\alpha_A^2 + \alpha_C^2 = 1$ . Using the values listed in Table I, we obtain  $\Delta_{so} = -15.0$  meV,  $\Delta_{cr} = 35.5$  meV,  $\alpha_A = 0.998$  and  $\alpha_C = 0.063$ . The energy parameters  $\Delta_{so}$  and  $\Delta_{cr}$  are comparable to those obtained by Mang *et al.* ( $\Delta_{so} = -3.5$  meV and  $\Delta_{cr} = 39.4$  meV at 6 K).<sup>34)</sup>

The corresponding squared  $p$ -matrix elements  $|\langle c|p|\nu\rangle|^2$  between the  $p$ -like valence and the  $s$ -like conduction band are

$$P_{0A\perp}^2 = \alpha_A^2 (P^2/2), \quad P_{0B\perp}^2 = P^2/2, \quad P_{0A\parallel}^2 = \alpha_C^2 (P^2/2), \quad (17.a)$$

for  $E \perp c$ , and

$$P_{0A\parallel}^2 = \alpha_C^2 P^2, \quad P_{0B\parallel}^2 = 0, \quad P_{0C\parallel}^2 = \alpha_A^2 P^2, \quad (17.b)$$

for  $E \parallel c$ . Then, we obtain the strength ratio

$$P_{0A\perp}^2 : P_{0B\perp}^2 : P_{0C\perp}^2 : P_{0A\parallel}^2 : P_{0B\parallel}^2 : P_{0C\parallel}^2 = 1.000 : 1.004 : 0.004 : 0.008 : 0 : 2.000. \quad (18)$$

The strength parameters,  $A_{0\alpha}$  [eq. (3)],  $A_{0x}^{n\alpha}$  [eq. (7)] and  $A_{0x}^{C\alpha}$  [eq. (10)], are constrained to satisfy the above strength ratio of eq. (18) in the present analysis (see Table I). It is found that these parameters are in agreement with the experimental data (Figs. 3 and 4).

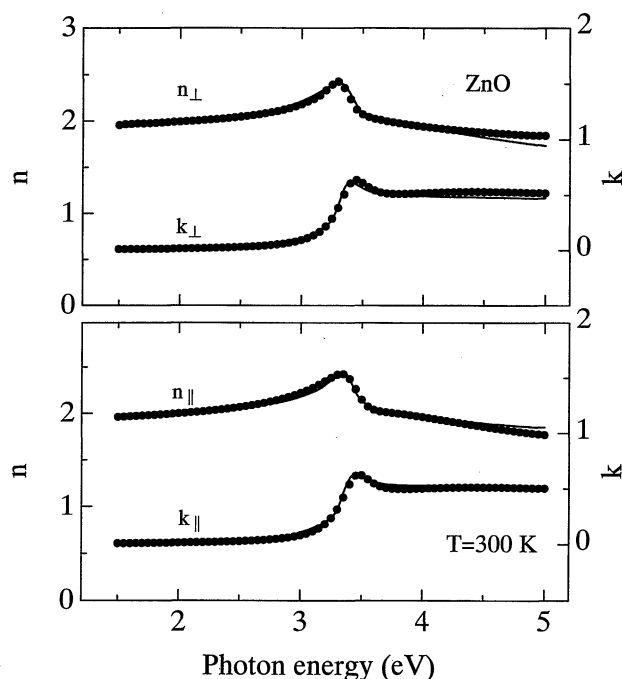


Fig. 5. Numerically calculated spectral dependence of the complex refractive index,  $n^*(E) = n(E) + ik(E)$ , for ZnO (solid lines). The solid circles represent the experimental data.

#### 4.2 Dielectric-function-related optical constants

Optical constants, such as the complex refractive index  $n^*(E) = n(E) + ik(E)$ , absorption coefficient  $\alpha(E)$  and normal-incidence reflectivity  $R(E)$ , can be easily obtained from the present study in the form of practical functions, since they are strongly related to the complex dielectric function,  $\epsilon(E)$ .

The real refractive index  $n(E)$  and extinction coefficient  $k(E)$  can be written as

$$n(E) = \left( \frac{[\epsilon_1(E)^2 + \epsilon_2(E)^2]^{1/2} + \epsilon_1(E)}{2} \right)^{1/2}, \quad (19)$$

$$k(E) = \left( \frac{[\epsilon_1(E)^2 + \epsilon_2(E)^2]^{1/2} - \epsilon_1(E)}{2} \right)^{1/2}. \quad (20)$$

In Fig. 5 we show the numerically calculated spectral dependence of the complex refractive index,  $n^*_\perp = n_\perp + ik_\perp$  ( $E \perp c$ ) and  $n^*_\parallel = n_\parallel + ik_\parallel$  ( $E \parallel c$ ), for ZnO (solid lines). They are obtained from eq. (19) for  $n$  and from eq. (20) for  $k$ . The solid circles represent the experimental data obtained by SE. The strong peaks in  $n$  and  $k$  at  $\sim 3.4$  eV are mainly due to the discrete-exciton transitions.

The absorption coefficient  $\alpha(E)$  and normal-incidence reflectivity  $R(E)$  can be given by

$$\alpha(E) = \frac{4\pi}{\lambda} k(E), \quad (21)$$

$$R(E) = \frac{[n(E) - 1]^2 + k(E)^2}{[n(E) + 1]^2 + k(E)^2}, \quad (22)$$

where  $\lambda$  is the wavelength of light in vacuum.

The numerically calculated spectral dependence of  $\alpha$  and  $R$  for ZnO are shown in Figs. 6 ( $E \perp c$ ) and 7 ( $E \parallel c$ ) by the solid lines. The open and solid circles represent the SE data of  $\alpha$  and  $R$ , respectively. It is seen in Figs. 6

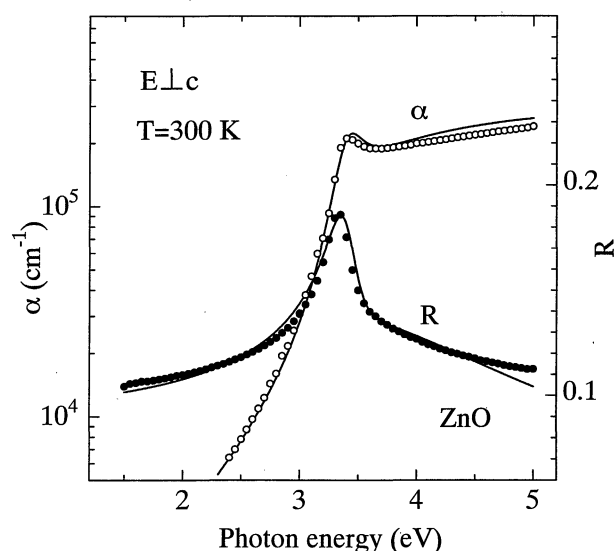


Fig. 6. Numerically calculated spectral dependence of the absorption coefficient  $\alpha(E)$  and normal-incidence reflectivity  $R(E)$  of ZnO for  $E \perp c$  (solid lines). The open and solid circles represent the experimental  $\alpha(E)$  and  $R(E)$ , respectively.

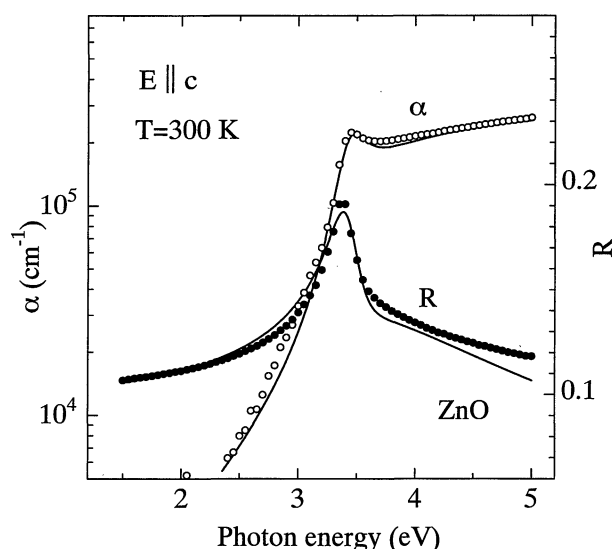


Fig. 7. As for Fig. 6, but for  $E \parallel c$ .

and 7 that the reflectivity  $R$  shows the strong discrete-exciton peaks in the spectra. The absorption coefficients at these discrete-exciton peaks are  $\sim 2 \times 10^5 \text{ cm}^{-1}$  for both polarizations. Our calculated  $\alpha$  and  $R$  spectra agree reasonably well with the experimental spectra.

#### 4.3 Refractive-index dispersion in the transparent region

It is important to know the refractive-index dispersion in the region below or near the fundamental absorption edge of semiconductors. Figures 8 and 9 show the experimental  $n(E)$  dispersion of ZnO for  $E \perp c$  (Fig. 8) and  $E \parallel c$  (Fig. 9) as measured using SE in the region near the discrete-exciton peaks. The open circles and open triangles represent the experimental data taken from the literature. They were obtained using the prism method

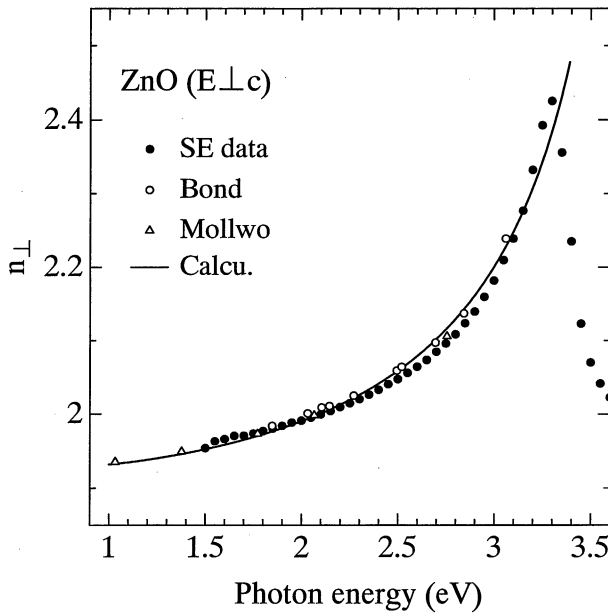


Fig. 8. Refractive-index dispersion of ZnO for  $E \perp c$  below the fundamental absorption edge. The solid circles represent our SE data. The open circles and open triangles represent the experimental data obtained by Bond (open circles, ref. 7) and Mollwo (open triangles, ref. 6), respectively.

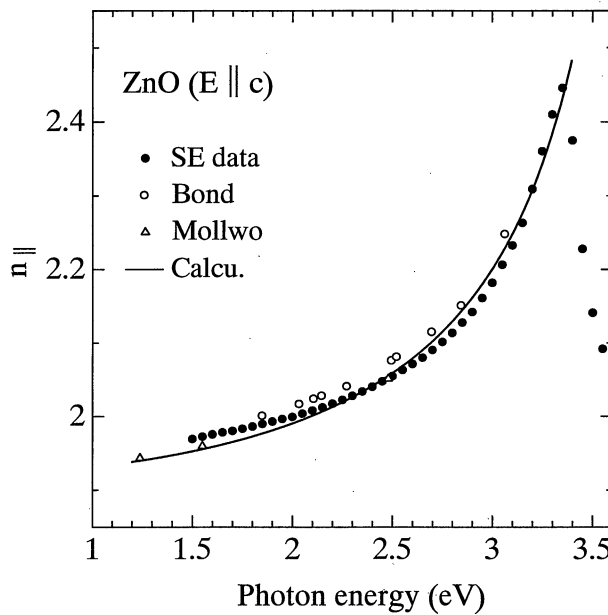


Fig. 9. As for Fig. 8, but for  $E \parallel c$ .

by Bond (open circles)<sup>7)</sup> and Mollwo (open triangles).<sup>6)</sup>

The experimental  $n(E)$  data in Figs. 8 and 9 are analyzed using the first-order Sellmeier equation:

$$n(\lambda)^2 = A + \frac{B\lambda^2}{\lambda^2 - C}, \quad (23)$$

where  $A$ ,  $B$  and  $C$  are the fitting parameters and  $\lambda$  is in  $\mu\text{m}$ . The solid lines in Figs. 8 and 9 indicate the results of eq. (23) fitted to the experimental data. The values of the fitting parameters determined here are:  $A = 2.84$ ,  $B = 0.84$  and  $C = 0.101 \mu\text{m}^2$  ( $E \perp c$ );  $A = 2.85$ ,  $B = 0.87$  and  $C = 0.096 \mu\text{m}^2$  ( $E \parallel c$ ).

As  $\lambda \rightarrow \infty$ , the electronic contribution to  $\epsilon_1$  approaches a limiting value  $\epsilon_\infty$ , the high-frequency dielectric constant. The  $\epsilon_\infty$  value, which can be obtained from eq. (23) by  $\epsilon_\infty = n^2(\lambda \rightarrow \infty) = A + B$ , are 3.68 for  $E \perp c$  and 3.72 for  $E \parallel c$ . These values are in good agreement with those estimated by Heltemes and Swinney [ $\epsilon_\infty(\perp) = 3.70$  and  $\epsilon_\infty(\parallel) = 3.75$ ],<sup>8)</sup> but are considerably smaller than those reported more recently by Venger *et al.* [ $\epsilon_\infty(\perp) = 3.95$  and  $\epsilon_\infty(\parallel) = 4.05$ ].<sup>18)</sup>

Below the reststrahlen region, the real part of the dielectric function  $\epsilon_1$  approaches a limiting value, the static dielectric constant  $\epsilon_s$ .  $\epsilon_\infty$  and  $\epsilon_s$  are related to the long-wavelength optical phonon frequencies,  $\omega_{\text{LO}}$  and  $\omega_{\text{TO}}$ , by the generalized Lyddane-Sachs-Teller relationship

$$\frac{\epsilon_s}{\epsilon_\infty} = \left( \frac{\omega_{\text{LO}}}{\omega_{\text{TO}}} \right)^2, \quad (24)$$

where  $\omega_{\text{LO}}$  and  $\omega_{\text{TO}}$  are the longitudinal and transverse optical phonon frequencies, respectively. Introducing  $\omega_{\text{LO}} = 583 \text{ cm}^{-1}$  ( $574 \text{ cm}^{-1}$ ),  $\omega_{\text{TO}} = 411 \text{ cm}^{-1}$  ( $380 \text{ cm}^{-1}$ )<sup>39)</sup> and  $\epsilon_\infty = 3.68$  ( $3.72$ ) for  $E \perp c$  ( $E \parallel c$ ) into eq. (24), we obtain  $\epsilon_s = 7.40$  for  $E \perp c$  and 8.49 for  $E \parallel c$ . These values are in reasonable agreement with those obtained by Heltemes and Swinney [ $\epsilon_s(\perp) = 7.8$  and  $\epsilon_s(\parallel) = 8.75$ ],<sup>8)</sup> but are slightly smaller than the recent values obtained by Venger *et al.* [ $\epsilon_s(\perp) = 8.1$  and  $\epsilon_\infty(\parallel) = 9.0$ ].<sup>18)</sup>

## 5. Conclusions

We have measured the spectral dependence of the complex dielectric function,  $\epsilon(E) = \epsilon_1(E) + i\epsilon_2(E)$ , of ZnO for light polarized perpendicular ( $E \perp c$ ) and parallel to the optic axis  $c$  ( $E \parallel c$ ) using SE in the photon-energy range between 1.5 and 5.0 eV at room temperature. The measured SE spectra reveal the distinct structures at  $\sim 3.4 \text{ eV}$  ( $E_0$  edge). These  $\epsilon(E)$  spectra are analyzed on the basis of a simplified model of the interband transitions. Since the excitonic effects may modify the CP singularity structures, the model is made to account for the excitonic effects at this band edge. Our theoretical model successfully explains the experimental spectra over the entire range of photon energies. Dielectric-function-related optical constants, such as the complex refractive index ( $n^* = n + ik$ ), absorption coefficient ( $\alpha$ ) and normal-incidence reflectivity ( $R$ ), of ZnO are also presented. The refractive-index data in the transparent region of ZnO have also been analyzed using the first-order Sellmeier equation. As a byproduct, the high-frequency and static dielectric constants are determined as  $\epsilon_\infty = 3.68$  and  $\epsilon_s = 7.40$  for  $E \perp c$  and  $\epsilon_\infty = 3.72$  and  $\epsilon_s = 8.49$  for  $E \parallel c$ .

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