

CS1MA20 Autumn Assignment 2021

Module Code: CS1MA20

Assignment report Title: Autumn Assignment 2021

Student Number: 30021591

Date: 12/11/2021

Hrs spent for the assignment: 3

Assignment evaluation:

Question 1

A

$$\begin{bmatrix} 1 & 9 & 7 \\ 9 & 5 & 9 \end{bmatrix}$$

B

$$\begin{bmatrix} 9 & 5 & 10 \\ 1 & 9 & 8 \end{bmatrix}$$

C

$$\begin{bmatrix} 8 & 7 \\ 10 & 10 \\ 1 & 9 \end{bmatrix}$$

1. Matrix Calculation : 30021591

This is to be done by hand, though you can use MatLab to check

Calculate $1A + 10B$ {2 marks}

Calculate $9A - 5C'$ {2}

Calculate $A \times C$ {3}

Calculate $C \times B$ {3}

$$A = \begin{bmatrix} 1 & 9 & 7 \\ 9 & 5 & 9 \end{bmatrix} B = \begin{bmatrix} 9 & 5 & 10 \\ 1 & 9 & 8 \end{bmatrix} C = \begin{bmatrix} 8 & 7 \\ 10 & 10 \\ 1 & 9 \end{bmatrix}$$

Calculate $1A + 10B$

$$1A = \begin{bmatrix} 1 & 9 & 7 \\ 9 & 5 & 9 \end{bmatrix} 10B = \begin{bmatrix} 90 & 50 & 100 \\ 10 & 90 & 80 \end{bmatrix}$$
$$1A + 10B = \begin{bmatrix} 1 + 90 & 9 + 50 & 7 + 100 \\ 9 + 10 & 5 + 90 & 9 + 80 \end{bmatrix} = \begin{bmatrix} 91 & 59 & 107 \\ 19 & 95 & 89 \end{bmatrix}$$

$$\therefore 1A + 10B = \begin{bmatrix} 91 & 59 & 107 \\ 19 & 95 & 89 \end{bmatrix}$$

Calculate $9A - 5C'$

$$9A = \begin{bmatrix} 9 & 81 & 63 \\ 81 & 45 & 81 \end{bmatrix} \quad 5C' = \begin{bmatrix} 40 & 50 & 5 \\ 35 & 50 & 45 \end{bmatrix}$$

$$9A - 5C' = \begin{bmatrix} 9 - 40 & 81 - 50 & 63 - 5 \\ 81 - 35 & 45 - 50 & 81 - 45 \end{bmatrix} = \begin{bmatrix} -31 & 31 & 58 \\ 46 & -5 & 36 \end{bmatrix}$$

$$\therefore 9A - 5C' = \begin{bmatrix} -31 & 31 & 58 \\ 46 & -5 & 36 \end{bmatrix}$$

Calculate $A \cdot C$

$$AC = \begin{bmatrix} (1 \cdot 8) + (9 \cdot 10) + (7 \cdot 1) & (1 \cdot 7) + (9 \cdot 10) + (7 \cdot 9) \\ (5 \cdot 10) + (9 \cdot 1) + (9 \cdot 8) & (9 \cdot 7) + (5 \cdot 10) + (9 \cdot 9) \end{bmatrix} = \begin{bmatrix} 8 + 90 + 7 & 7 + 90 + 63 \\ 50 + 9 + 72 & 63 + 50 + 81 \end{bmatrix}$$

$$\therefore AC = \begin{bmatrix} 105 & 160 \\ 131 & 194 \end{bmatrix}$$

Calculate $C \cdot B$

$$\begin{bmatrix} (8 \cdot 9) + (7 \cdot 1) & (8 \cdot 5) + (7 \cdot 9) & (8 \cdot 10) + (7 \cdot 8) \\ (10 \cdot 9) + (10 \cdot 1) & (10 \cdot 5) + (10 \cdot 9) & (10 \cdot 10) + (10 \cdot 8) \\ (1 \cdot 9) + (9 \cdot 1) & (1 \cdot 5) + (9 \cdot 9) & (1 \cdot 10) + (9 \cdot 8) \end{bmatrix} = \begin{bmatrix} 72 + 7 & 40 + 63 & 80 + 56 \\ 90 + 10 & 50 + 90 & 100 + 80 \\ 9 + 9 & 5 + 81 & 10 + 72 \end{bmatrix}$$

$$\therefore CB = \begin{bmatrix} 79 & 103 & 136 \\ 100 & 140 & 180 \\ 18 & 86 & 82 \end{bmatrix}$$

Question 2. Magic Matrix Equation Solving

$$\begin{array}{ccc}
 \mathbf{A} & \mathbf{x} & \mathbf{b} \\
 \begin{bmatrix} 5 & 9 \\ 5 & 10 \end{bmatrix} & \begin{bmatrix} x_0 \\ x_1 \end{bmatrix} & \begin{bmatrix} 117 \\ 125 \end{bmatrix}
 \end{array}$$

2. Magic Matrix Equation Solving : 30021591

This is to be done by hand

Find matrix M , such that MA is a diagonal matrix {2}

Use M to find x in the equation $Ax = b$ {2}

Show that Ax does equal b {2}

$$A = \begin{bmatrix} 5 & 9 \\ 5 & 10 \end{bmatrix} x = \begin{bmatrix} x_0 \\ x_1 \end{bmatrix} b = \begin{bmatrix} 117 \\ 125 \end{bmatrix}$$

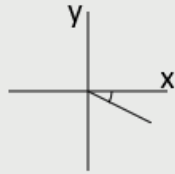
Find matrix M , such that MA is a diagonal matrix

$$MA = \begin{bmatrix} 10 & -9 \\ -5 & 5 \end{bmatrix} \cdot \begin{bmatrix} 5 & 9 \\ 5 & 10 \end{bmatrix} = \begin{bmatrix} 5 & 0 \\ 0 & 5 \end{bmatrix}$$

Use M to find x in the equation $Ax = b$ -

$$\begin{bmatrix} 10 & -9 \\ -5 & 5 \end{bmatrix} \cdot \begin{bmatrix} x_0 \\ x_1 \end{bmatrix} x = \begin{bmatrix} 5x_0 \\ 5x_1 \end{bmatrix} = \begin{bmatrix} 45 \\ 40 \end{bmatrix}$$

Question 3



3. Trigonometry : 30021591

Here $\arctan(y/x) = \arctan2(y,x)$ where x and y are as on the above

Find $\arctan(8/10)$ {2}

Find $\arctan(-8/10)$ {2}

Plot both these in graphs like that shown above {3}

Express $9\sin(x) + 9\cos(x)$ in form $K\sin(x+p)$ {3}

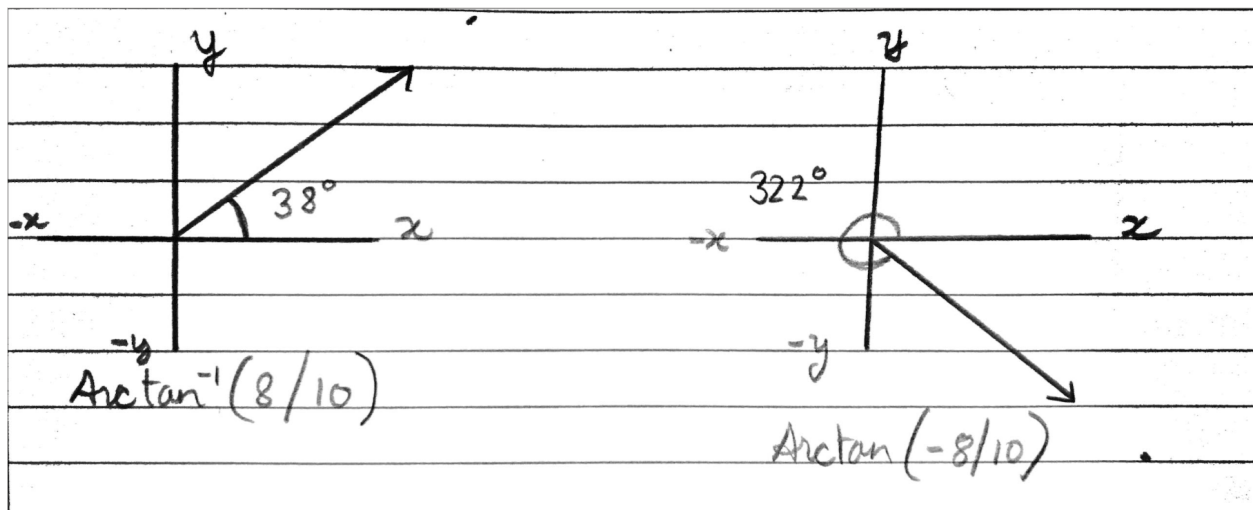
Find $\arctan(8/10)$ {2}

$$\arctan = \tan^{-1}(8/10) = 38.659 = 38^\circ$$

Find $\arctan(-8/10)$ {2}

$$\arctan = \tan^{-1}(-8/10) = 360^\circ - 38^\circ = 322^\circ$$

Plot both these in graphs like that shown above {3}



Express $9\sin(x) + 9\cos(x)$ in form $K\sin(x+p)$ {3}

$$k \cos(p) = 9$$

$$k \sin(p) = 9$$

$$\tan p = 9/9$$

$$p = \tan^{-1}(9/9) = 45^\circ$$

$$9 \sin(x + 45^\circ)$$

$$k = 9^2 + 9^2 = 162^\circ$$

Question 4

4. Exp Log Hyperbolic : 30021591

In MatLab create 2 by 2 subplots as follows: {4}

5 exp(-x/7) for x from 0 to 7

On log log scales from x = 1 to 10 a plot of x^5

sinh(3x/10) for x from -10 to +10

cosh(4x/9) for x from -9 to +9

In MatLab create 2 by 2 subplots as follows: {4}

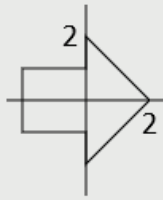
5 exp(-x/7) for x from 0 to 7

On log log scales from x = 1 to 10 a plot of x^5

sinh(3x/10) for x from -10 to +10

cosh(4x/9) for x from -9 to +9

Question 5



5. Linear Transforms : 30021591

In MatLab, define a matrix with homogenous coordinates to represent the arrow above {2}

Plot the shape in an area from -15,-15 to 15,15 {2}

Define a 3*3 matrix to rotate the shape by 10 degrees {2}

Define a 3*3 matrix to move the shape by 10,9 {2}

Plot the shape (and the area) when it has been rotated {1}

Then plot it after it has also been moved {1}

In MatLab, define a matrix with homogenous coordinates to represent the arrow above {2}

Plot the shape in an area from -15,-15 to 15,15 {2}

Define a 3*3 matrix to rotate the shape by 10 degrees {2}

Define a 3*3 matrix to move the shape by 10,9 {2}

Plot the shape (and the area) when it has been rotated {1}

Then plot it after it has also been moved {1}

Question 6

$$\begin{array}{ccc}
 \mathbf{A} & \mathbf{x} & \mathbf{b} \\
 \begin{bmatrix} 10 & 1 \\ 9 & 8 \end{bmatrix} & \begin{bmatrix} x_0 \\ x_1 \end{bmatrix} & \begin{bmatrix} 110 \\ 170 \end{bmatrix}
 \end{array}$$

6. $Ax=b$ - 2*2 by inverse : 30021591

By hand do the following:

Find the determinant of A {1}

Then find the inverse of A {2}

Hence find x in the equation $Ax = b$ {2}

Then, use MatLab to confirm your answer is correct {1}

Remember to include the MatLab commands in the report

Find the determinant of A {1}

$$\det(A) = 10 \cdot 8 - 9 \cdot 1 = 71$$

$$\text{Determinant of } A = 71$$

Then find the inverse of A {2}

$$\text{inv}(A) = \begin{bmatrix} 8 & -1 \\ -9 & 10 \end{bmatrix} \cdot \frac{1}{71} = \begin{bmatrix} \frac{8}{71} & \frac{-1}{71} \\ \frac{-9}{71} & \frac{10}{71} \end{bmatrix} = \begin{bmatrix} 0.1127 & -0.0141 \\ -0.1269 & 0.1408 \end{bmatrix}$$

$$\text{Inverse of } A = \begin{bmatrix} \mathbf{0.1127} & \mathbf{-0.0141} \\ \mathbf{-0.1269} & \mathbf{0.1408} \end{bmatrix}$$

Hence find x in the equation $Ax = b$ {2}

$$\begin{bmatrix} 0.1127 & -0.0141 \\ -0.1269 & 0.1408 \end{bmatrix} \cdot \begin{bmatrix} 10 & 1 \\ 9 & 8 \end{bmatrix} \cdot \begin{bmatrix} x_0 \\ x_1 \end{bmatrix} = \begin{bmatrix} 0.1127 & -0.0141 \\ -0.1269 & 0.1408 \end{bmatrix} \cdot \begin{bmatrix} 110 \\ 170 \end{bmatrix}$$

$$\begin{bmatrix} 0.1127 & -0.0141 \\ -0.1269 & 0.1408 \end{bmatrix} \cdot \begin{bmatrix} 110 \\ 170 \end{bmatrix} = \begin{bmatrix} 10 \\ 10 \end{bmatrix}; \mathbf{x} = \begin{bmatrix} \mathbf{10} \\ \mathbf{10} \end{bmatrix}$$

$$Ax = b = \begin{bmatrix} 10 & 1 \\ 9 & 8 \end{bmatrix} \cdot \begin{bmatrix} 10 \\ 10 \end{bmatrix} = \begin{bmatrix} 110 \\ 170 \end{bmatrix}$$

Then, use MATLAB to confirm your answer is correct {1}

$$\begin{array}{|l}
 \text{inv}(A)
 \end{array}
 \quad
 \begin{array}{|l}
 x = \text{inv}(A) * b
 \end{array}$$

ans =

```
0.1127 -0.0141  
-0.1268 0.1408
```

x =

```
10.0000  
10.0000
```

| A * x

ans =

```
110  
170
```

| b

b =

```
110  
170
```

Question 7

$$\begin{array}{c} \mathbf{A} \\ \begin{bmatrix} 1 & 9 & 8 \\ 10 & 9 & 7 \\ 5 & 10 & 9 \end{bmatrix} \end{array} \quad \begin{array}{c} \mathbf{x} \\ \begin{bmatrix} x_0 \\ x_1 \\ x_2 \end{bmatrix} \end{array} \quad \begin{array}{c} \mathbf{b} \\ \begin{bmatrix} 134 \\ 205 \\ 185 \end{bmatrix} \end{array}$$

7. $Ax=b$ - 3*3 by inverse : 30021591

By hand do the following:

Find the determinant of A {2}

Then find the inverse of A {3}

Hence find x in the equation $Ax = b$ {2}

Then, use MatLab to confirm your answer is correct {1}

Remember to include the MatLab commands in the report

Find the determinant of A {2}

$$\det(A) = 1 \cdot ((9 \cdot 9) - (10 \cdot 7)) - 9 \cdot ((10 \cdot 9) - (5 \cdot 7)) + 8 \cdot ((10 \cdot 10) - (5 \cdot 9))$$

Determinant of A = -44

Then find the inverse of A {3}

$$\begin{aligned}
inv(A) &= \begin{bmatrix} \begin{bmatrix} 9 & 7 \\ 10 & 9 \\ 9 & 8 \\ 10 & 9 \\ 9 & 8 \\ 9 & 7 \end{bmatrix} & \begin{bmatrix} 10 & 7 \\ 5 & 9 \\ 1 & 8 \\ 5 & 9 \\ 1 & 8 \\ 10 & 7 \end{bmatrix} & \begin{bmatrix} 10 & 9 \\ 5 & 10 \\ 1 & 9 \\ 5 & 10 \\ 1 & 9 \\ 10 & 9 \end{bmatrix} \end{bmatrix} \\
&= \begin{bmatrix} 81 - 70 & 90 - 35 & 100 - 45 \\ 81 - 80 & 9 - 40 & 10 - 45 \\ 63 - 72 & 7 - 18 & 9 - 90 \end{bmatrix} \\
&= \begin{bmatrix} 11 & 55 & 55 \\ 1 & -31 & -35 \\ -9 & -73 & -81 \end{bmatrix} \cdot \begin{bmatrix} + & - & + \\ - & + & - \\ + & - & + \end{bmatrix} = \begin{bmatrix} 11 & -55 & 55 \\ -1 & -31 & 3 \\ -9 & 73 & 81 \end{bmatrix} \\
inv(A)' &= \begin{bmatrix} -0.25 & 1.25 & -1.25 \\ 0.0227 & 0.7045 & -0.0681 \\ 0.2045 & -1.6590 & 1.8409 \end{bmatrix}
\end{aligned}$$

Hence find x in the equation $Ax = b$ {2}

$$\begin{aligned}
\begin{bmatrix} -0.25 & 1.25 & -1.25 \\ 0.0227 & 0.7045 & -0.0681 \\ 0.2045 & -1.6590 & 1.8409 \end{bmatrix} \cdot \begin{bmatrix} 134 \\ 205 \\ 185 \end{bmatrix} &= \begin{bmatrix} 9 \\ 5 \\ 10 \end{bmatrix}; \quad x = \begin{bmatrix} \mathbf{9} \\ \mathbf{5} \\ \mathbf{10} \end{bmatrix} \\
Ax = b &= \begin{bmatrix} 1 & 9 & 8 \\ 10 & 9 & 7 \\ 5 & 10 & 9 \end{bmatrix} \cdot \begin{bmatrix} 9 \\ 5 \\ 10 \end{bmatrix} = \begin{bmatrix} 134 \\ 205 \\ 185 \end{bmatrix}
\end{aligned}$$

Question 8

$$\begin{array}{ccc}
 \mathbf{A} & \mathbf{x} & \mathbf{b} \\
 \begin{bmatrix} 9 & 8 \\ 10 & 9 \end{bmatrix} & \begin{bmatrix} x_0 \\ x_1 \end{bmatrix} & \begin{bmatrix} 162 \\ 181 \end{bmatrix}
 \end{array}$$

8. $Ax=b$ - 2*2 Cramer : 30021591

By hand, use Cramer's Rule to find $x \{3\}$

Use MatLab to confirm your answer $\{2\}$

By hand, use Cramer's Rule to find $x \{3\}$

$$\begin{aligned}
 \det(A) &= \begin{vmatrix} 9 & 8 \\ 10 & 9 \end{vmatrix} = 9 \cdot 9 - 10 \cdot 8 \\
 &= 81 - 80 = 1
 \end{aligned}$$

$$\begin{aligned}
 \det(A) &= \begin{vmatrix} 9 & 8 \\ 10 & 9 \end{vmatrix} = 9 \cdot 9 - 10 \cdot 8 \\
 &= 81 - 80 = 1 \\
 D &= 1
 \end{aligned}$$

$$\det(x_0) = \begin{vmatrix} 162 & 8 \\ 181 & 9 \end{vmatrix} = 162 \cdot 9 - 181 \cdot 8 = 10$$

$$\det(x_1) = \begin{vmatrix} 9 & 162 \\ 10 & 181 \end{vmatrix} = 9 \cdot 181 - 10 \cdot 162 = 9$$

$$x_1 = \frac{Dx_1}{D} = \frac{9}{1} = 9$$

$$Ax = b = \begin{bmatrix} 9 & 8 \\ 10 & 9 \end{bmatrix} \cdot \begin{bmatrix} 10 \\ 9 \end{bmatrix} = \begin{bmatrix} 162 \\ 181 \end{bmatrix}$$

Use MATLAB to confirm your answer $\{2\}$

$$\left| \begin{array}{l} A = [9 \ 8; 10 \ 9] \end{array} \right.$$

A =

$$\left| \begin{array}{l} b = [162; 181] \end{array} \right.$$

b =

```
9      8
10     9
```

```
162
181
```

| $\det(A)$

ans =

```
1.0000
```

| $x_0 = [162\ 8; 181\ 9]$

$x_0 =$

```
162      8
181      9
```

| $x_1 = [9\ 162; 10\ 181]$

$x_1 =$

```
9      162
10     181
```

| $\det(x_0)$

ans =

```
10.0000
```

| $\det(x_1)$

ans =

```
9.0000
```

| $x = [\det(x_0); \det(x_1)]$

$x =$

```
10.0000
9.0000
```

| b

$b =$

```
162
181
```

| $A * x$

ans =

```
162.0000
181.0000
```

Question 9

$$\begin{matrix} A & x & b \\ \begin{bmatrix} 9 & 7 & 5 \\ 10 & 9 & 8 \\ 7 & 10 & 1 \end{bmatrix} & \begin{bmatrix} x_0 \\ x_1 \\ x_2 \end{bmatrix} & \begin{bmatrix} 151 \\ 191 \\ 144 \end{bmatrix} \end{matrix}$$

9. $Ax=b$ - 3*3 Cramer : 30021591

In MatLab, use Cramer's Rule to find x {5}
Remember to include the MatLab commands in the report

In MATLAB, use Cramer's Rule to find x {5}

```
A = [9, 7, 5; 10, 9, 8; 7, 10, 1];  
b = [151; 191; 144];
```

```
x0 = [151, 7, 5; 191, 9, 8; 144, 10, 1];  
x1 = [9, 151, 5; 10, 191, 8; 7, 144, 1];  
x2 = [9, 7, 151; 10, 9, 191; 7, 10, 144];
```

```
detA=det(A);  
detX0 = det(x0)/detA;  
detX1 = det(x1)/detA;  
detX2 = det(x2)/detA;  
x = [detX0; detX1; detX2];
```

| A

A =

```
9    7    5  
10   9    8  
7   10   1
```

| b

b =

```
151  
191  
144
```

| x0

x0 =

```
151    7    5
191    9    8
144   10    1
```

| x1

x1 =

```
 9   151    5
10   191    8
 7   144    1
```

| x2

x2 =

```
 9    7   151
10    9   191
 7   10   144
```

| detA

detA =

-132

| detX0

detX0 =

7

| detX1

detX1 =

9.0000

| detX2

detX2 =

5.0000

x =

```
7.0000
9.0000
5.0000
```

| b

b =

```
151
191
144
```

| A * x

ans =

```
151.0000
191.0000
144.0000
```

Question 10

$$\begin{matrix} P1 \\ \begin{bmatrix} -8 \\ -9 \\ 48 \end{bmatrix} \end{matrix}$$

$$\begin{matrix} P2 \\ \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix} \end{matrix}$$

$$\begin{matrix} P3 \\ \begin{bmatrix} 6 \\ -4 \\ 5 \end{bmatrix} \end{matrix}$$

10. Vectors : 30021591

Points P1..P3 are on a plane. Find vectors P1 to P2 and P2 to P3 {2}

Hence, find the vector normal to the plane {2}

Now find the equation of the plane {2}

The plane is viewed by an eye at 4,-7,4

Find the vector from P2 to the eye, and show the plane is visible {2}

In MatLab, plot the plane, the vector P2 to the eye

and the normal from P2 of length 5 {2}

Points P1..P3 are on a plane. Find vectors P1 to P2 and P2 to P3 {2}

Hence, find the vector normal to the plane {2}

Now find the equation of the plane {2}

The plane is viewed by an eye at 4,-7,4. Find the vector from P2 to the eye, and show the plane is visible {2}

In MatLab, plot the plane, the vector P2 to the eye and the normal from P2 of length 5 {2}

Question 11

$$\begin{array}{c}
 \mathbf{A} \\
 \left[\begin{array}{ccc} 10 & 10 & 1 \\ 9 & 8 & 10 \\ 9 & 7 & 5 \end{array} \right]
 \end{array}
 \quad
 \begin{array}{c}
 \mathbf{x} \\
 \left[\begin{array}{c} x_0 \\ x_1 \\ x_2 \end{array} \right]
 \end{array}
 \quad
 \begin{array}{c}
 \mathbf{b} \\
 \left[\begin{array}{c} 171 \\ 153 \\ 138 \end{array} \right]
 \end{array}$$

11. Gaussian Elimination : 30021591

By hand:

Form the Augmented Matrix {1}

Use Row Operations so this is in Row Echelon form {3}

Hence find x in the equation $Ax = b$ {2}

Go to MatLab, and first confirm your answer {2}

Then use determinants to find Augmented Matrix's Rank {2}

Show all working. Is it what you expect?

Form the Augmented Matrix {1}

$$\text{aug}(A) = \left[\begin{array}{cccc} 10 & 10 & 1 & 171 \\ 9 & 8 & 10 & 153 \\ 9 & 7 & 5 & 138 \end{array} \right]$$

Use Row Operations so this is in Row Echelon form {3}

$$\frac{1}{10} \cdot R_1 \rightarrow R_1 \quad \left[\begin{array}{cccc} 1 & 1 & \frac{1}{10} & \frac{171}{10} \\ 9 & 8 & 10 & 153 \\ 9 & 7 & 5 & 138 \end{array} \right]$$

$$\frac{1}{9} \cdot R_2 \rightarrow R_2 \quad \left[\begin{array}{cccc} 1 & 1 & \frac{1}{10} & \frac{171}{10} \\ 1 & \frac{8}{9} & \frac{10}{9} & 17 \\ 9 & 7 & 5 & 138 \end{array} \right]$$

$$\frac{1}{9} \cdot R_3 \rightarrow R_3 \quad \left[\begin{array}{cccc} 1 & 1 & \frac{1}{10} & \frac{171}{10} \\ 1 & \frac{8}{9} & \frac{10}{9} & 17 \\ 1 & \frac{7}{9} & \frac{5}{9} & \frac{46}{3} \end{array} \right]$$

$$R_2 - 1 \cdot R_1 \rightarrow R_2 \quad \left[\begin{array}{cccc} 1 & 1 & \frac{1}{10} & \frac{171}{10} \\ 1 & \frac{8}{9} & \frac{10}{9} & 17 \\ 1 & \frac{7}{9} & \frac{5}{9} & \frac{46}{3} \end{array} \right]$$

$$R_3 - 1 \cdot R_1 \rightarrow R_3$$

$$\begin{bmatrix} 1 & 1 & \frac{1}{10} & \frac{171}{10} \\ 0 & -\frac{1}{9} & \frac{91}{90} & -\frac{1}{10} \\ 0 & -\frac{2}{9} & \frac{41}{90} & -\frac{53}{30} \end{bmatrix}$$

$$-9 \cdot R2 \rightarrow R2$$

$$\begin{bmatrix} 1 & 1 & \frac{1}{10} & \frac{171}{10} \\ 0 & 1 & -\frac{91}{10} & \frac{10}{9} \\ 0 & -\frac{2}{9} & \frac{41}{90} & -\frac{53}{30} \end{bmatrix}$$

$$-\frac{9}{2} \cdot R3 \rightarrow R3$$

$$\begin{bmatrix} 1 & 1 & \frac{1}{10} & \frac{171}{10} \\ 0 & 1 & -\frac{91}{10} & \frac{10}{9} \\ 0 & 1 & \frac{41}{90} & \frac{159}{20} \end{bmatrix}$$

$$R3 - 1 \cdot R2 \rightarrow R3$$

$$\begin{bmatrix} 1 & 1 & \frac{1}{10} & \frac{171}{10} \\ 0 & 1 & -\frac{91}{10} & \frac{10}{9} \\ 0 & 0 & \frac{141}{20} & \frac{141}{20} \end{bmatrix}$$

$$\frac{20}{141} \cdot R3 \rightarrow R3$$

$$\begin{bmatrix} 1 & 1 & \frac{1}{10} & \frac{171}{10} \\ 0 & 1 & -\frac{91}{10} & \frac{10}{9} \\ 0 & 0 & 1 & 1 \end{bmatrix}$$

$$R2 + 91/10 \cdot R3 \rightarrow R2$$

$$\begin{bmatrix} 1 & 1 & \frac{1}{10} & \frac{171}{10} \\ 0 & 1 & 0 & 10 \\ 0 & 0 & 1 & 1 \end{bmatrix}$$

$$R1 - 1/10 \cdot R3 \rightarrow R1$$

$$\begin{bmatrix} 1 & 1 & 0 & 17 \\ 0 & 1 & 0 & 10 \\ 0 & 0 & 1 & 1 \end{bmatrix}$$

$$R1 - 1 \cdot R2 \rightarrow R1$$

$$\begin{bmatrix} 1 & 0 & 0 & 7 \\ 0 & 1 & 0 & 10 \\ 0 & 0 & 1 & 1 \end{bmatrix}$$

Hence find x in the equation $Ax = b$ {2}

$$Ax = b = \begin{bmatrix} 10 & 10 & 1 \\ 9 & 8 & 10 \\ 9 & 7 & 5 \end{bmatrix} \cdot \begin{bmatrix} 7 \\ 10 \\ 1 \end{bmatrix} = \begin{bmatrix} 171 \\ 153 \\ 138 \end{bmatrix}$$

Go to MATLAB, and first confirm your answer {2}

|

|


```
| A = [10 10 1; 9 8 10; 9 7 5]
```

A =

```
10    10    1
 9     8   10
 9     7    5
```

```
| b = [171 ; 153 ; 138]
```

b =

```
171
153
138
```

```
| x = mldivide(A,b)
```

x =

```
7.0000
10.0000
1.0000
```

```
| b
```

b =

```
171
153
138
```

```
| A * x
```

ans =

```
171
153
138
```

Then use determinants to find Augmented Matrix's Rank {2}

////

Question 12

$$A = \begin{bmatrix} 15 & 2 \\ -28 & 0 \end{bmatrix}$$

12. Eigenvalues and vectors - 2 : 30021591

By hand, find the characteristic equation for the matrix A {2}
 and hence find the eigenvalues of A {2}
 and then find an eigenvector for each eigenvalue {2}
 Go to MatLab, and find the eigenvalues and eigenvectors, {1}
 then show that your eigenvectors are multiples of MatLab's {1}

By hand, find the characteristic equation for the matrix A {2}

and hence find the eigenvalues of A {2}

and then find an eigenvector for each eigenvalue {2}

Go to MATLAB, and find the eigenvalues and eigenvectors, {1}

then show that your eigenvectors are multiples of MATLAB{1}

Question 3

$$A = \begin{bmatrix} 2 & 0 & 1 \\ -36 & 5 & -4 \\ 2 & 1 & 11 \end{bmatrix}$$

13. Eigenvalues and vectors - 3 : 30021591

In MatLab, find the eigenvalues and eigenvectors of A {2}

By hand, find the characteristic equation of A {2}

Show that the 3 eigenvalues are roots of this {2}

In MatLab, form matrix X from the three eigenvectors and show $\text{Inv}(X) * A * X$ is a diagonal matrix {2}

In MATLAB, find the eigenvalues and eigenvectors of A {2}

By hand, find the characteristic equation of A {2}

Show that the 3 eigenvalues are roots of this {2}

In MATLAB, form matrix X from the three eigenvectors and show $\text{Inv}(X) \cdot A \cdot X$ is a diagonal matrix {2}