## This is a testfile for vscode

Ali-loner

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## 摘要

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## Contents

## 1 This is a section

First, we present a lemma on the Lyapunov function: Let a system  $\dot{x}(t) = f(x(t), x(t-h(t)))$  with f(0,0) = 0. Assume the Lyapunov function  $F: G \to \mathbb{R}$  exists with  $x,y \in G$ , F(y) < F(x) implies

$$\left(\dot{F}\left(x\right)f\left(x,y\right)\right)\left(\ddot{F}\left(x\right)f\left(x,y\right)\right) \leq 0. \tag{1}$$

Then the solution  $x(t) \equiv 0$  is stable.

Suppose there exists a Lyapunov function  $F: \mathbb{R}^n \to \mathbb{R}$ . Then define functional  $V: \mathcal{C} \to \mathbb{R}$  as follows:

$$V(\phi) := \max_{-h \le \theta \le 0} F(\phi(\theta)), (\forall \phi \in \mathcal{C}).$$
 (2)

By definition, the following conditions hold:

$$\dot{V}(\phi) \begin{cases}
\leq 0, & \text{if } F(\phi(0)) < V(\phi), \\
= \max \left( \dot{F}(\phi(0)), f(\phi(0), \phi(-h(t))), 0 \right), & \text{if } F(\phi(0)) = V(\phi),
\end{cases}$$
(3)

where  $f(\phi(0), \phi(-h(t))) = \Psi \phi(0) + \Psi_d \phi(-h(t))$ .

Thus  $\dot{V}(\phi) > 0$  holds if and only if the following condition holds:

$$F(\phi(0)) = \max_{-h < \theta < 0} F(\phi(\theta)) \ and(\dot{F}(\phi(0)), f(\phi(0), \phi(-h(t)))) > 0. \tag{4}$$

The function F can be defined in some neighborhood  $G \subset \mathbb{R}^n$ . Moreover, the functional V is then defined for  $\phi \in \mathcal{C}$  with values in G.

Suppose Equation (??) holds for some functions  $\phi \in \mathcal{C}$ , then we can obtain the inequality  $F\left(\phi\left(-h\left(t\right)\right)\right) < F\left(\phi\left(0\right)\right)$  making  $\phi$  arbitrarily small. Thus the second condition in Equation (??) still holds but conflicts with Lemma ??. Therefore  $\dot{V}\left(\phi\right) \leq 0$  holds constantly for all  $\phi$ .



图 1: this is Ali

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