

Start 12:35 2/7 cm NAME: Gloire Rubambiza

Instructions

- Put your response to each question on a separate page and include your name and the problem number on each page.
- You do not need to attempt all of the questions. Work on the ones that you feel ready for and have time for.
- You may use scratch paper, a calculator, your texts, and your notes. Please do not use any network enabled device (smart phone, computer, tablet).
- You are welcome to discuss questions with your instructor for clarification.
- On the chart below, indicate which of the problems that you attempted should be assessed by circling the problem number.

1	2	3	4	5	6	7	8	9
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Table 1: Problems Attempted

1. MC1 I can determine whether a small number is prime, and factor an integer into its prime factorization.

MC2 I can find the greatest common divisor/greatest common factor of two positive integers and determine whether two integers are relatively prime.

For each pair of integers, find their prime factorization and use it to find the greatest common factor of the pair.

(a) 77 and 23. $7 \cdot 11 \cdot 1 \mid 1 \cdot 23$ $gcf = 1$

(b) 91 and 161. $7 \cdot 13 \cdot 1 \mid 7 \cdot 23 \cdot 1$ $gcf = 7$

(c) 126 and 135. $2 \cdot \boxed{3 \cdot 3} \cdot 7 \mid \boxed{3 \cdot 3} \cdot 3 \cdot 5$ $gcf = 9$

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Assessment 1

$$2. a) 2 \cdot 100 = 45 \div 55$$

$$45 - 0.55 = 45$$

$$100 - 4.55 = 95.45$$

$$45 \div 4.10 = 5$$

$$100 - 2.5 = 0$$

$$\text{gcd}(45, 100) = 5 \checkmark$$

$$b) 2 \cdot 19 = 10$$

$$19 - 1.10 = 9$$

$$10 - 1.9 = 1$$

$$9 - 1.9 = 0$$

$$\text{gcd}(19, 29) = 1 \checkmark$$

$$c) 64 \div 2.25 = 39 \quad 64 - 2.25 = 14$$

$$25 - 0.39 = 25$$

$$39 - 1.25 = 14$$

$$25 - 1.14 = 11$$

$$14 - 1.11 = 3$$

$$11 - 3.3 = 2$$

$$3 - 1.2 = 1$$

$$2 - 2.1 = 0$$

$$\text{gcd}(64, 25) = 1 \checkmark$$

$$3. (a) (88 + 67) \bmod 7$$

$$= 155 \bmod 7$$

$$155 = 7 \cdot 22 + 1 \checkmark$$

$$\Rightarrow (88 + 67) \bmod 7 = 1 \checkmark$$

$$3. (b) (13 - 67) \bmod 7$$

$$-54 \bmod 7$$

$$-54 = (-7 \cdot 7) - 6$$

$$-7 \cdot 7 - 6 = -55$$

$$\Rightarrow (13 - 67) \bmod 7 = 6$$

$$(13 - 67) \bmod 7 = (-54) \bmod 7$$

$$(c) (575 + 919) \bmod 2$$

$$1494 \bmod 2$$

$$1494 = (2 \cdot 747) + 0$$

$$\Rightarrow (575 + 919) \bmod 2 = 0 \text{ or}$$

$$= (-8 \cdot 7 + 2) \bmod 7$$

$$= 2$$

(Or, -54 is 2 more than a multiple of 7)

$$(d) (14 \cdot 7) \bmod 26$$

$$98 \bmod 26$$

$$98 = (3 \cdot 26) + 20$$

$$\Rightarrow (14 \cdot 7) \bmod 26 = 20$$

4. a) The additive inverse of 12 modulo 77 is 65 because $(65 \bmod 77 - 12 \bmod 77 = 0)$ $(65 + 12) \bmod 77 = 0$

b) The additive inverse of 45 modulo 8 is 3 because

$$45 \bmod 8 = 5 \bmod 8 = 0$$

$$-5 \bmod 8 = 3$$

$$\text{Also: } (45 + 3) \bmod 8 = 0$$

5. a) The multiplicative inverse of 11 mod 26 exists if the greatest common factor of 26 and 11 is 1.

In other words $1 = (m \cdot 11) \bmod 26$

$$\begin{bmatrix} 26 \\ 1 \\ 0 \end{bmatrix} = 2 \cdot \begin{bmatrix} 11 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 15 \\ 1 \\ -1 \end{bmatrix} \begin{bmatrix} 4 \\ 1 \\ -2 \end{bmatrix}$$

$$\begin{bmatrix} 11 \\ 0 \\ 1 \end{bmatrix} = 0 \cdot \begin{bmatrix} 15 \\ 1 \\ -1 \end{bmatrix} = \begin{bmatrix} 11 \\ 0 \\ 1 \end{bmatrix} \begin{bmatrix} 11 \\ 0 \\ 1 \end{bmatrix} - 2 \cdot \begin{bmatrix} 4 \\ 1 \\ -2 \end{bmatrix} = \dots$$

$$45 \bmod 8 = 5$$

Assessment 1 (cont.)

5.(a) Continued

$$\begin{bmatrix} 11 \\ 4 \\ -1 \end{bmatrix} \cdot \begin{bmatrix} 11 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 4 \\ 1 \\ -2 \end{bmatrix} \checkmark$$

$$\begin{bmatrix} 11 \\ 0 \\ 1 \end{bmatrix} \cdot \begin{bmatrix} 4 \\ 1 \\ -2 \end{bmatrix} = \begin{bmatrix} 3 \\ -2 \\ 5 \end{bmatrix} \checkmark$$

$$\begin{bmatrix} 4 \\ 1 \\ -2 \end{bmatrix} \cdot \begin{bmatrix} 3 \\ -2 \\ 5 \end{bmatrix} = \begin{bmatrix} 1 \\ 3 \\ -7 \end{bmatrix}$$

$$\Rightarrow 1 = 3 \cdot 26 + (-7) \cdot 11$$

right, equivalent 2 ways to get 1 mod 26 = 19

$$\begin{bmatrix} 3 \\ -2 \\ 5 \end{bmatrix} \cdot \begin{bmatrix} 3 \\ 3 \\ -7 \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \\ 26 \end{bmatrix}$$

Because we found the additive inverse of the original matrix operation, the multiplicative inverse does exist. The multiplicative inverse of 11 mod 26 is -7.

What about the mult. inv. of 11 modulo 22?

6.(c) $(3725)_8$ to binary \Rightarrow each octal is three binary digits
06 011 11 010 101 \checkmark

(f) $0xA3C2$ to decimal \Rightarrow each hex is 4 binary

$$\Rightarrow 10 \cdot 16^3 + 3 \cdot 16^2 + 12 \cdot 16^1 + 2 \cdot 16^0$$

$$\Rightarrow 10 \cdot 4096 + 768 + 192 + 2$$

$$\Rightarrow 5058$$

6. d) 3725 to decimal

$$\Rightarrow 3 \cdot 8^3 + 7 \cdot 8^2 + 2 \cdot 8^1 + 5 \cdot 8^0$$

$$\Rightarrow 2005 \checkmark$$

g) 0xABC2 to binary: \Rightarrow 1 hex digit = 4 binary digits

0b 1010 0011 1100 0010 \checkmark

9. a) R E S T R

S L E E P

\Rightarrow J P W X G \checkmark

b) R E S T R E S T R E

I D T O E L B F R

R E L A X A T I O N \checkmark

8a. $\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 7 & 8 & 9 & 10 & 11 & 12 \end{pmatrix}$ $\begin{pmatrix} 13 & 14 & 15 & 16 & 17 & 18 \\ 19 & 20 & 21 & 22 & 23 & 24 \end{pmatrix}$

J	U	N	G	I	E
K	P	L	N	I	R
E	C	M	D	P	O
E	A	A	E	E	H

Write across rows, transpose, then

E	G	J	L	N	O
R	N	K	I	L	P
O	D	E	P	M	C
N	C	E	E	A	A

read down columns.

Encoded message: R O N N D C K E E I P E L I M A P C A

SS algorithm for VNI then it goes to W

b)

E	G	J	L	N	O
C	A	S	I	O	M
D	E	E	E	E	
H	S	A	U	O	
S	N	I	E	R	
T	F	S	V	E	
R	O	N	R	A	
N				L	