Case study: Spanish Flu in London, Birmingham, and Liverpool

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Objectives

- 1. To explore the use of POMP models in the context of meta-populations and multiple waves.
- 2. To illustrate the use of POMP models in a more complex setting.
- 3. To demonstrate the use of diagnostic probes for model criticism.
- 4. To provide an example that can be modified to apply similar approaches to other outbreaks of emerging infectious diseases.

Emerging infectious disease pandemic I

- ▶ The 1918 Spanish flu pandemic was one of the deadliest pandemics in human history.
- ▶ The pandemic lasted from January 1918 to December 1920, spreading to nearly every part of the world.
- ▶ The pandemic was caused by the H1N1 influenza A virus.
- ▶ The pandemic was responsible for the deaths of an estimated 50 million people worldwide.

Emerging infectious disease pandemic II

Key questions included:

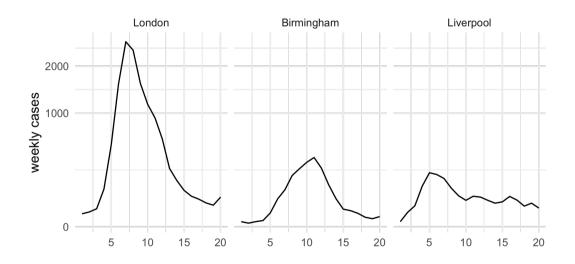
- 1. How fast will the pandemic unfold?
- 2. What are the common and differentiated characteristics of the pandemic in different cities?
- 3. How people will correspond to the pandemic?

Weekly reported data I

```
dat <- read_csv("1918flu_3cities_1wave.csv")
head(dat)</pre>
```

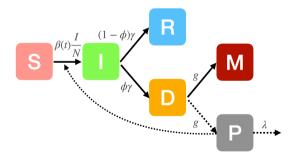
```
# A tibble: 6 \times 5
  London Birmingham Liverpool week date
   <dbl>
               <dbl>
                         <dbl> <dbl> <date>
      13
                                    1 1918-09-21
      17
                                    2 1918-09-28
                             16
3
      25
                             34
                                    3 1918-10-05
4
     110
                            127
                                    4 1918-10-12
5
     519
                  15
                           226
                                    5 1918-10-19
6
    1579
                                    6 1918-10-26
                  60
                           211
```

Weekly reported data II



SIR model with behavioral response I

- Social distancing is a common public health intervention.
- We model the effect of social distancing as a reduction in the transmission rate.
- We incorporate demographic and climatic features to model the spread of the disease.
- ▶ The SIR model with behavioral response is given by:



SIR model with behavioral response II

$$\begin{split} \frac{\mathrm{d}S}{\mathrm{d}t} &= -\beta(t)\,S\,\frac{I}{N} \\ \frac{\mathrm{d}I}{\mathrm{d}t} &= \beta(t)\,S\,\frac{I}{N} - \gamma\,I \\ \frac{\mathrm{d}R}{\mathrm{d}t} &= (1-\phi)\,\gamma\,I \\ \frac{\mathrm{d}D}{\mathrm{d}t} &= \phi\,\gamma\,I \\ \frac{\mathrm{d}M}{\mathrm{d}t} &= g\,D \\ \frac{\mathrm{d}P}{\mathrm{d}t} &= g\,D - \lambda\,P \end{split}$$

- ► S, I, R: the susceptible, infectious, and recovered populations
- ▶ D: those who have lost of infectiousness and are progressing to death due to influenza or/and pneumonia
- M: those who have died
- ▶ P: general public's risk perception based on recent influenza deaths
- N: N = S + I + R + D + M, the constant total population size

SIR model with behavioral response III

The time-dependent transmission rate $\beta(t)$ consists of two components:

$$\beta(t) = \beta_0 \cdot \left(1 - \frac{P(t)}{N}\right)^{\kappa} \tag{1}$$

- $\triangleright \beta_0$: the baseline transmission rate
- $\left(1-rac{P(t)}{N}
 ight)^{\kappa}$: represent the effect of reactive social distancing on transmission rate based on the public's risk perception P(t)

The number of reported cases C follows a Negative Binomial distribution, in London, Birmingham, and Liverpool, respectively, with ratio ρ and over-dispersion parameter k, given the cumulative number of cases H:

$$C \sim \text{NegBin}(\rho H, k)$$

SIR model with behavioral response IV

- Fixed parameters:
 - ► The total population sizes for London, Birmingham, and Liverpool are fixed at 4484523, 919444, and 802940, respectively
 - $ightharpoonup \gamma^{-1}$: the average infectious period, fixed at 4 days
 - $ightharpoonup g^{-1}$: the mean time from loss-of-infectiousness to death, fixed at 8 days
- Parameters to be estimated, initial conditions:
 - η_L, η_B, η_L : the initial fraction of susceptible individuals for London, Birmingham, and Liverpool, respectively
 - ψ_L, ψ_B, ψ_L : the initial fraction of infectious individuals for London, Birmingham, and Liverpool, respectively
- Parameters to be estimated, common features:
 - β_0 : the baseline transmission rate
 - \triangleright κ : the exponent of the social distancing effect
 - \triangleright λ : the rate at which the public's risk perception decays

The implementation in pomp: the state process for meta-populations

```
sir meta <- Csnippet("</pre>
  double *S = \&S1, *I = \&I1, *R = \&R1, *D = \&D1, *M = \&M1:
 double *P = \&P1, *H = \&H1; int N[3] = {N1, N2, N3};
 double Beta, dN SI, dN IRD, dN IR, dN ID, dN DM, dN P;
  for (int i = 0: i < 3: i++) {
   Beta = beta0*pow(1-P[i]/N[i],kappa);
    dN_SI = rbinom(S[i],1-exp(-Beta*I[i]/N[i]*dt));
    dN_IRD = rbinom(I[i],1-exp(-gamma*dt));
    dN IR = nearbyint((1-phi)*dN IRD); dN ID = nearbyint(phi*dN IRD);
    dN DM = rbinom(D[i], 1-exp(-g*dt));
    dN P = rbinom(P[i],1-exp(-lambda*dt));
    S[i] -= dN SI; I[i] += dN SI - dN IRD; R[i] += dN IR;
   D[i] += dN ID - dN DM; M[i] += dN DM; P[i] += dN DM - dN P;
   H[i] += dN IRD;}
```

The implementation in pomp: the initial conditions

```
sir meta rinit <- Csnippet("</pre>
  double *S = \&S1, *I = \&I1, *R = \&R1, *D = \&D1, *M = \&M1;
 double *P = &P1, *H = &H1; int N[3] = \{N1, N2, N3\};
  double eta[3] = {eta1, eta2, eta3};
 double psi[3] = {psi1, psi2, psi3};
 for (int i = 0; i < 3; i++) {
    S[i] = nearbyint(N[i]*eta[i]);
   I[i] = nearbvint(N[i]*psi[i]);
   R[i] = nearbyint(N[i]*(1-eta[i]-psi[i]));
    D[i] = M[i] = P[i] = H[i] = 0:
```

The implementation in pomp: the measurements

```
sir_meta_dmeas <- Csnippet("</pre>
  double lik1, lik2, lik3;
  lik1 = (ISNA(London)) ? dnbinom mu(London,rho*H1,k,1) : 0;
 lik2 = (ISNA(Birmingham)) ? dnbinom mu(Birmingham,rho*H2,k,1) : 0;
 lik3 = (ISNA(Liverpool)) ? dnbinom mu(Liverpool,rho*H3,k,1) : 0;
 lik = lik1 + lik2 + lik3:
 lik = (give log) ? lik : exp(lik);
")
sir meta rmeas <- Csnippet("
  London = rnbinom mu(k,rho*H1);
  Birmingham = rnbinom mu(k,rho*H2);
 Liverpool = rnbinom mu(k,rho*H3):
11)
```

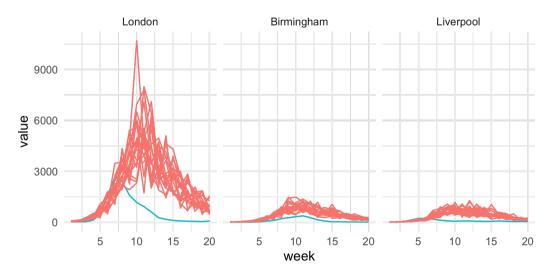
The implementation in pomp: build the model I

```
dat |> select(-date) |>
  pomp(
    times = "week". t0 = 0.
    rprocess=euler(sir_meta,delta.t=1/7),
    rinit=sir_meta_rinit, rmeasure=sir_meta_rmeas,
    dmeasure=sir_meta_dmeas, accumvars = sprintf("H%d".1:3).
    statenames=c(sprintf("S%d",1:3),sprintf("I%d",1:3),
      sprintf("R%d",1:3), sprintf("D%d",1:3), sprintf("M%d",1:3),
      sprintf("P%d",1:3), sprintf("H%d",1:3)),
    paramnames=c(
      "beta0", "kappa", "gamma", "phi", "g", "lambda", "rho", "k",
      sprintf("N%d",1:3),sprintf("eta%d",1:3),sprintf("psi%d",1:3))
  ) -> pomp meta
```

The implementation in pomp: build the model II

```
params <- c(beta0 = 5, kappa = 5, gamma = 1/4, phi = 0.0119, g = 1/8,
 lambda = 1/2, rho = 0.05, k = 10, N1 = 4484523, N2 = 919444,
 N3 = 802940, eta1 = 0.2, eta2 = 0.2, eta3 = 0.2,
 psi1 = 0.0005, psi2 = 0.0005, psi3 = 0.0005)
pomp meta |>
 simulate(
   params = params, nsim=20, format="data.frame", include.data=TRUE
 ) |>
 select(week,.id,London,Birmingham,Liverpool) |>
 reshape2::melt(id.vars = c("week",".id")) |>
 ggplot(aes(x=week, y=value, group=.id, color=.id=="data")) +
 geom_line() + facet_wrap(variable ~ .) +
 theme minimal() + guides(color="none")
```

The implementation in pomp: build the model III



License, acknowledgments, and links

- This lesson is prepared for the Simulation-based Inference for Epidemiological Dynamics module at the Summer Institute in Statistics and Modeling in Infectious Diseases, SISMID.
- ▶ The materials build on previous versions of this course and related courses.
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- ▶ Produced with R version 4.3.2 and pomp version 5.10.
- Compiled on 2024-07-24.

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R code for this lesson