

EE5301: DSP Lab/EE5801: CSP Lab

Assignment 4

Problem:

Design of digital filters such as LPF,HPF,BPF.

Technical details:

1. **LPF or Half band filter** with $f_c = 400 \text{ Hz}$, $\omega_c = \pi/2$, $N = 39$

$$h_d[n] = \begin{cases} \frac{\sin(\omega_c n)}{\pi n}, & -(N-1)/2 \leq n \leq (N-1)/2 \\ \frac{\omega_c}{\pi}, & n = 0 \end{cases}$$

2. **LPF** with $f_c = 400 \text{ Hz}$, $\omega_c = \pi/4$, $N = 39$, $h_d[n]$ is same as above.

3. **HPF** with $f_c = 1200 \text{ Hz}$, $f_s = 4800 \text{ Hz}$, $N = 39$

$$h_d[n] = \begin{cases} \frac{\sin(\pi n)}{\pi n} - \frac{\sin(\omega_c n)}{\pi n}, & -(N-1)/2 \leq n \leq (N-1)/2 \\ 1 - \frac{\omega_c}{\pi}, & n = 0 \end{cases}$$

4. **BPF** with $f_{c1} = 500 \text{ Hz}$, $f_{c2} = 1200 \text{ Hz}$, $f_s = 6000 \text{ Hz}$, $N = 39$

$$h_d[n] = \begin{cases} \frac{\sin(\omega_{c2} n)}{\pi n} - \frac{\sin(\omega_{c1} n)}{\pi n}, & -(N-1)/2 \leq n \leq (N-1)/2 \\ \frac{\omega_{c2} - \omega_{c1}}{\pi}, & n = 0 \end{cases}$$

Window functions

- Hamming window

$$W_H[n] = \begin{cases} 0.54 - 0.46 \cos\left(\frac{2\pi n}{N-1}\right), & \text{if } 0 \leq n \leq N-1 \\ 0, & \text{otherwise} \end{cases}$$

Instructions:

- In case of 1 and 2 please decide the sampling frequency f_s as discussed in lecture.

- Generate the N samples of $h_d[n]$ in time domain for the filter you want to design.
- Multiply the window function $W_H[n]$ with $h_d[n]$ to get practical impulse response $h[n]$.

Submission Details:

- Write C code to implement above system.
- Write main.c and two separate files named common_functions.c which contains 3 separate functions corresponding to LPF and HPF and BPF and header file named common_functions.h which contains function declarations. For both LPF 1 and LPF 2 you need to call same LPF function with appropriate parameter. Input to any filter functions are f_c , f_s and N . Output of any filter function is $h[n]$.
- Upload main.c, common_functions.c, common_functions.h files and a text file containing your practical impulse response $h[n]$ for all four cases.
- Also write your understanding about above filters in your own words and upload a pdf file.
- Submit all files in a single zip file with your id, Example: EE20MTECH11010_A1.zip.