

## Exercise 2.1

We did the tutorial, but are so kind to upload only the pdf without all the .jff files ;)

## Exercise 2.2

(a) This is the graphical representation of  $M = \langle \{q_0, q_1, q_2, q_3\}, \{a, b\}, \delta, q_0, \{q_2\} \rangle$ .

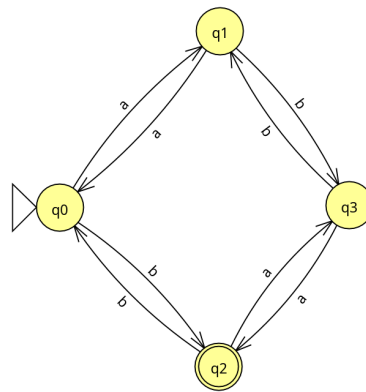


Figure 1: Graphical representation of  $M$

(b) For the sequence "abbab", we visit the following states:

$$q_0 \rightarrow q_1 \rightarrow q_3 \rightarrow q_1 \rightarrow q_0 \rightarrow q_2$$

As you can see, we end up at  $q_2$  which actually is a, and the only, final state of the DFA  $M$ .

(c)  $M$  recognizes every language that has at least a "b" in it. So the minimal length of the WORDS of the language has to be 1, since you have to reach  $q_2$  from  $q_0$ . At every NODE you have always the possibility to add an "a" or a "b", going left or right from your current position.

## Exercise 2.3

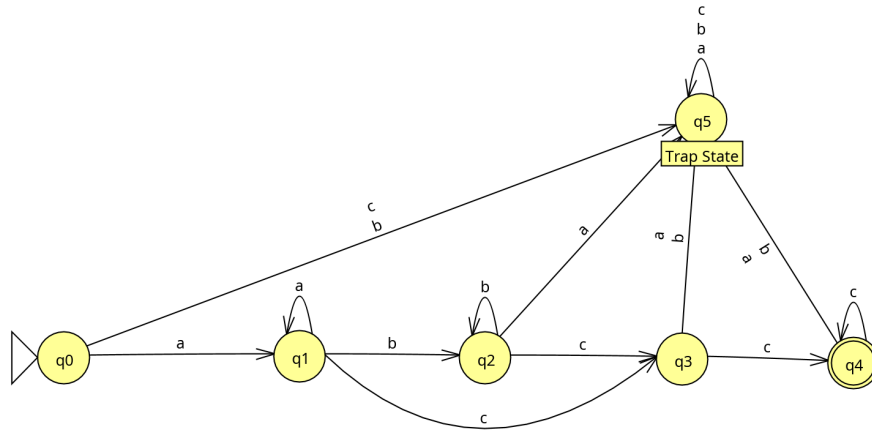


Figure 2: The DFA for the language  $L = \{a^x b^y c^z \mid x \geq 1, y \geq 0, z \geq 2\}$

## Exercise 2.4

- (a) Yes, because if we follow the states given by the word 0101010 we end up at  $q_2$ , which is a final state of the NFA.

After the first 0 we end up at  $q_2$ , from which we can go back to  $q_0$  (with  $\epsilon$ ) and then go to  $q_1$  with 1. The following SERIES 010 we do by staying on  $q_1$ ; then we go to  $q_2$  with 1 and we end on  $q_2$  with the last 0 passing by  $q_0$ .

- (b) This is the DFA equivalent to the NFA on the Exercise sheet:

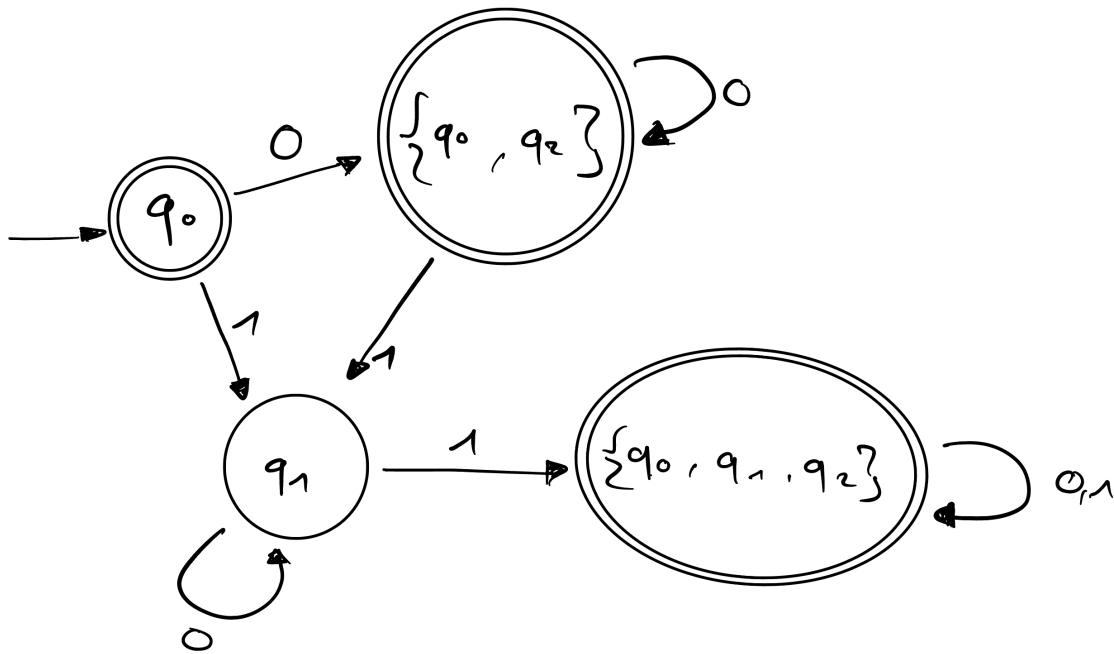


Figure 3: DFA