Exercise 2.1

We did the tutorial, but are so kind to only upload the pdf without all the .jff files;)

Exercise 2.2

(a) This is the graphical representation of the DFA $M = \langle \{q_0, q_1, q_2, q_3\}, \{a, b\}, \delta, q_0, \{q_2\} \rangle$.

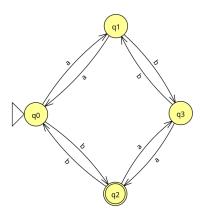


Figure 1: Graphical representation of DFA M

(b) For the sequence "abbab", we visit the following states:

$$q_0 \rightarrow q_1 \rightarrow q_3 \rightarrow q_1 \rightarrow q_0 \rightarrow q_2$$

As you can see, we end up at q_2 which is actually one, and the only, final state of the DFA M.

(c) M recognizes every language that has an odd number of "b"'s in it (at least one) and that has 0 or an even number of "a"'s. So the minimal length of the words of the language has to be 1, since you have to reach q_2 from q_0 .

Exercise 2.3

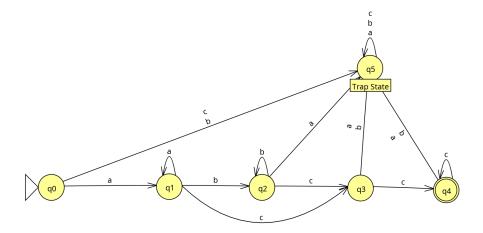


Figure 2: The DFA for the language $L=\{\,a^x\,b^y\,c^z\mid x\geq 1,\ y\geq 0,\ z\geq 2\,\}$

Exercise 2.4

- (a) Yes, because if we follow the states given by the word 0101010 we end up at q_2 , which is a final state of the NFA.
 - After the first 0 we end up at q_2 , from which we can go back to q_0 (with ϵ) and then go to q_1 with 1. The following elements 010 we do by staying on q_1 ; then we go to q_2 with 1 and we end on q_2 with the last 0 passing by q_0 .
- (b) This is the DFA equivalent to the NFA on the Exercise sheet:

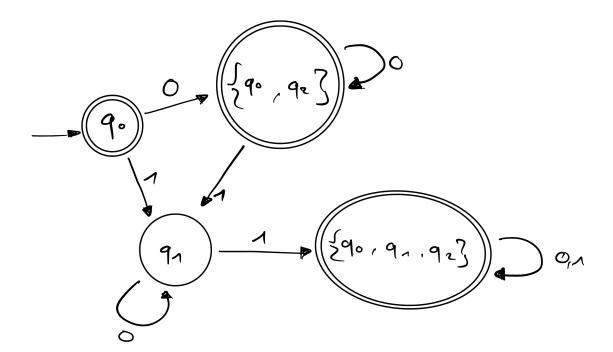


Figure 3: DFA