## Exercise 2.1

We did the tutorial, but are so kind to only upload the pdf without all the .jff files;)

## Exercise 2.2

(a) This is the graphical representation of the DFA  $M = \langle \{q_0, q_1, q_2, q_3\}, \{a, b\}, \delta, q_0, \{q_2\} \rangle$ .

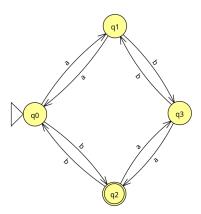


Figure 1: Graphical representation of DFA M

(b) For the sequence "abbab", we visit the following states:

$$q_0 \rightarrow q_1 \rightarrow q_3 \rightarrow q_1 \rightarrow q_0 \rightarrow q_2$$

As you can see, we end up at  $q_2$  which is actually one, and the only, final state of the DFA M.

(c) M recognizes every language that has an odd number of "b"'s in it (at least one) and that has 0 or an even number of "a"'s. So the minimal length of the words of the language has to be 1, since you have to reach  $q_2$  from  $q_0$ .

## Exercise 2.3

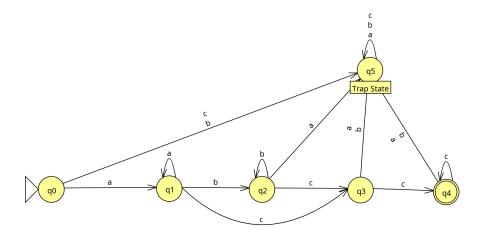


Figure 2: The DFA for the language  $L=\{\,a^x\,b^y\,c^z\mid x\geq 1,\ y\geq 0,\ z\geq 2\,\}$ 

## Exercise 2.4

- (a) Yes, because if we follow the states given by the word 0101010 we end up at  $q_2$ , which is a final state of the NFA.
  - After the first 0 we end up at  $q_2$ , from which we can go back to  $q_0$  (with  $\epsilon$ ) and then go to  $q_1$  with 1. The following elements 010 we do by staying on  $q_1$ ; then we go to  $q_2$  with 1 and we end on  $q_2$  with the last 0 passing by  $q_0$ .
- (b) This is the DFA equivalent to the NFA on the Exercise sheet:

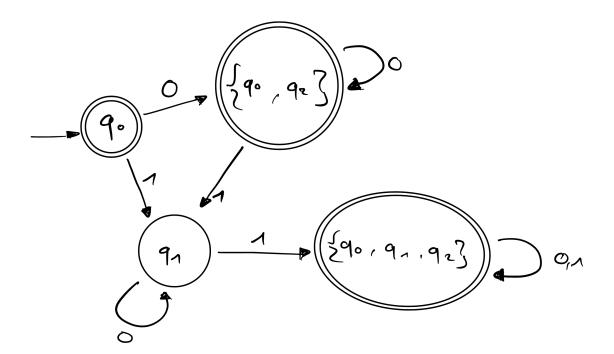


Figure 3: DFA