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Parallel Programming Models and Dependences

Concurrency and Parallelism — 2018-19

Master in Computer Science

(Mestrado Integrado em Eng. Informática)

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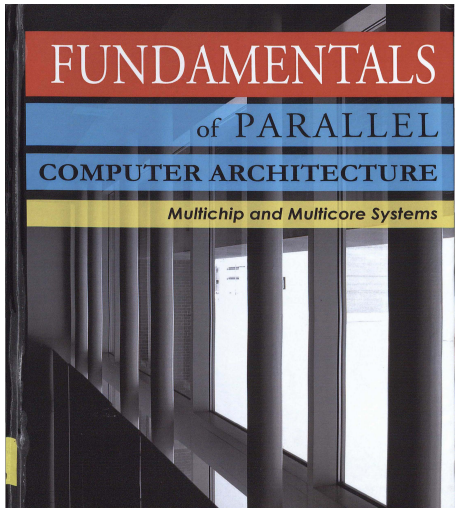
Source: Parallel Computing, CIS 410/510, Department of Computer and Information Science

Outline

- Parallel programming models
- Statement dependences
- Loop dependences

– Bibliography:

- **(Part of) Chapter 4** of book
  Yan Solihin;
  Fundamentals of Parallel Computer Architecture;
  Solihin Books (2009);
  ISBN: 978-0-98-416300-7



Parallelism

- Ability to execute different parts of a computation concurrently on different computing elements
- Why do you want parallelism?
  - Shorter running time or handling more work
- What is being parallelized?
  - *Task*: instruction, statement, procedure, …
  - *Data*: data flow, size, replication
  - Parallelism granularity
    - Coarse-grain versus fine-grained
- Evaluation
  - Was the parallelization successful?

Why is parallel programming important?

- Parallel programming has matured
  - Standard programming models
  - Common machine architectures
  - Programmer can focus on computation and use suitable programming model for implementation
- Problem
  - Performance optimization is still platform-dependent
  - Performance portability is a problem
  - Parallel programming methods are still evolving

Parallel Algorithm

- Recipe to solve a problem "in parallel" on multiple processing elements
- Standard steps for constructing a parallel algorithm
  - Identify work that can be performed concurrently
  - Partition the concurrent work on separate processors
  - Properly manage input, output, and intermediate data
  - Coordinate data accesses and work to satisfy dependences
- Which steps are hard to do?

Parallelism Views

- Where can we find parallelism?
- Program (task) view
  - Statement level
    - Between program statements
    - Which statements can be executed at the same time?
  - Block level / Loop level / Routine level / Process level
    - Larger-grained program statements
- Data view
  - How is data operated on?
  - Where does data reside?
- Resource view
  - When to access and use a shared resource?

Parallelism, Correctness, and Dependences

- Parallel execution shall always be constrained by the sequence of operations needed to be performed for a correct result
- Parallel execution must address control, data, and system dependences
- A *dependence* arises when one operation depends on an earlier operation to complete and produce a result before this later operation can be performed
  - We extend this notion of dependence to resources since some operations may depend on certain resources (e.g., due to where data is located)

Executing Two Statements in Parallel

- Want to execute two statements in parallel
- On one processor:

Processor 1:
Statement 1;
Statement 2;

- On two processors:

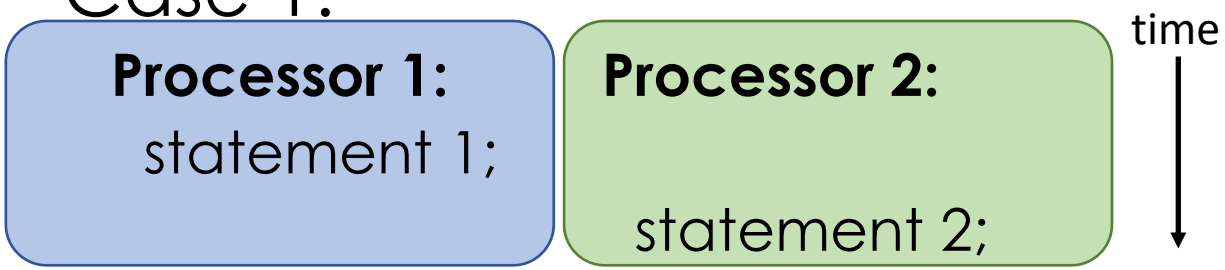
Processor 1:
Statement 1;

Processor 2:
Statement 2;

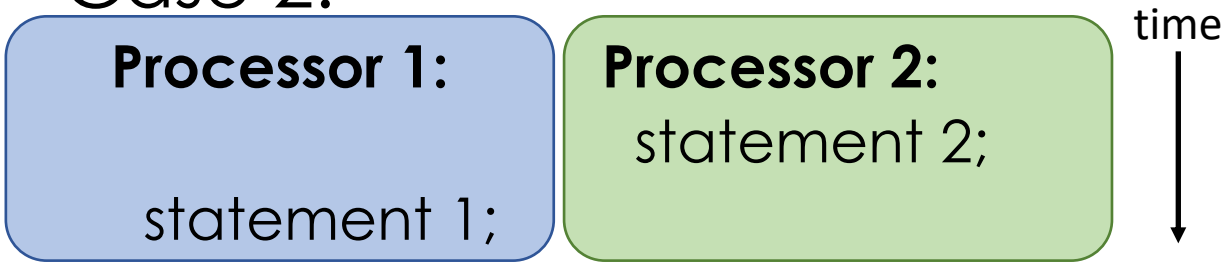
- Fundamental (*concurrent*) execution assumption
  - Processors execute independent of each other
  - No assumptions made about speed of processor execution

Sequential Consistency in Parallel Execution

- Case 1:



- Case 2:



- Sequential consistency
  - Statements execution does not interfere with each other
  - Computation results are the same (independent of order)

Independent versus Dependent

- In other words the execution of

```
statement1;
statement2;
```

must be equivalent to

```
statement2;
statement1;
```

- Their order of execution must not matter!
- If true, the statements are *independent* of each other
- Two statements are *dependent* when the order of their execution affects the computation outcome

Examples

- Example 1

```
S1: a=1;
S2: b=1;
```

  - Statements are independent

- Example 2

```
S1: a=1;
S2: b=a;
```

  - Dependent (*true (flow) dependence*)
    - Second is dependent on first
    - Can you remove dependence?

- Example 3

```
S1: a=f(x);
S2: a=b;
```

  - Dependent (*output dependence*)
    - Second is dependent on first
    - Can you remove dependence? How?

- Example 4

```
S1: a=b;
S2: b=1;
```

  - Dependent (*anti-dependence*)
    - First is dependent on second
    - Can you remove dependence? How?

True Dependence and Anti-Dependence

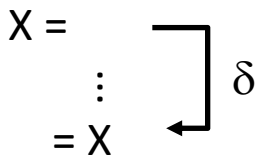
- Given statements S1 and S2,

  S1;

  S2;

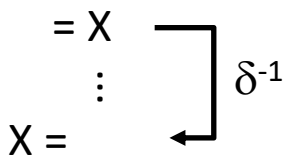
- S2 has a *true (flow) dependence* on S1

  if and only if **S2 reads a value written by S1**
  (RAW – Read After Write)



- S2 has a *anti-dependence* on S1

  if and only if **S2 writes a value read by S1**
  (WAR – Write After Read)



Output Dependence

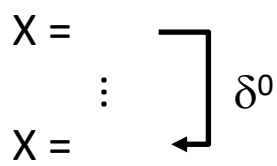
- Given statements S1 and S2,

  S1;

  S2;

- S2 has an *output dependence* on S1

  if and only if **S2 writes a variable written by S1** (WAW – Write After Write)

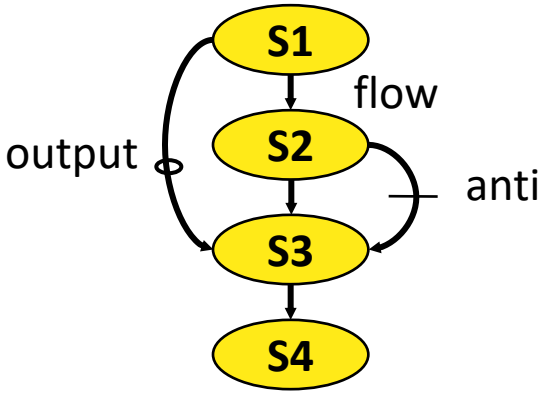


- Anti- and output dependences are "name" dependences
  - How can we get rid of anti- and output dependences?

Statement Dependence Graphs

- Can use graphs to show dependence relationships
- Example

  S1: a=1;
  S2: b=a;
  S3: a=b+1;
  S4: c=a;



- $S_1 \ \delta \ S_2$: S_2 is flow-dependent on S_1
- $S_1 \ \delta^0 \ S_3$: S_3 is output-dependent on S_1
- $S_2 \ \delta^{-1} \ S_3$: S_3 is anti-dependent on S_2

When can two statements execute in parallel?

- Statements S1 and S2 can execute in parallel if and only if there are *no dependences* between them, i.e., no
  - *True dependences*; nor
  - *Anti-dependences*; nor
  - *Output dependences.*
- Some dependences can be removed by modifying the program
  - Rearranging statements
  - Eliminating statements

How do you compute dependences?

- Data dependence relations can be found by comparing the IN and OUT sets of each node
- The IN and OUT sets of a statement S are defined as:
  - IN(S) : set of memory locations (variables) that may be used in S
  - OUT(S) : set of memory locations (variables) that may be modified by S
- Note that these sets include all memory locations that may be fetched or modified
  - As such, the sets can be conservatively large

IN / OUT Sets and Computing Dependences

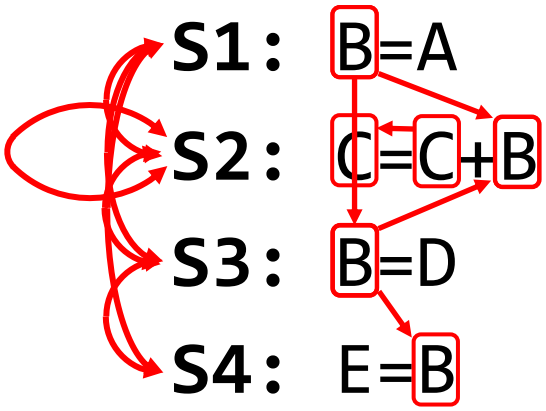
- Assuming that there is a path from S1 to S2 , the following shows how to intersect the IN and OUT sets to test for data dependence

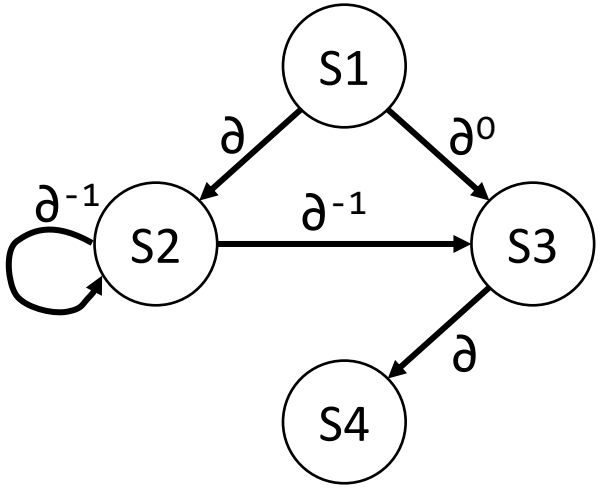
$$out(S_1) \cap in(S_2) \neq \varnothing \qquad S_1 \; \delta \; S_2 \qquad \text{flow dependence}$$

$$in(S_1) \cap out(S_2) \neq \varnothing \qquad S_1 \; \delta^{-1} \; S_2 \qquad \text{anti-dependence}$$

$$out(S_1) \cap out(S_2) \neq \varnothing \qquad S_1 \; \delta^{0} \; S_2 \qquad \text{output dependence}$$

Example





Loop-Level Parallelism

- Significant parallelism can be identified **within loops**

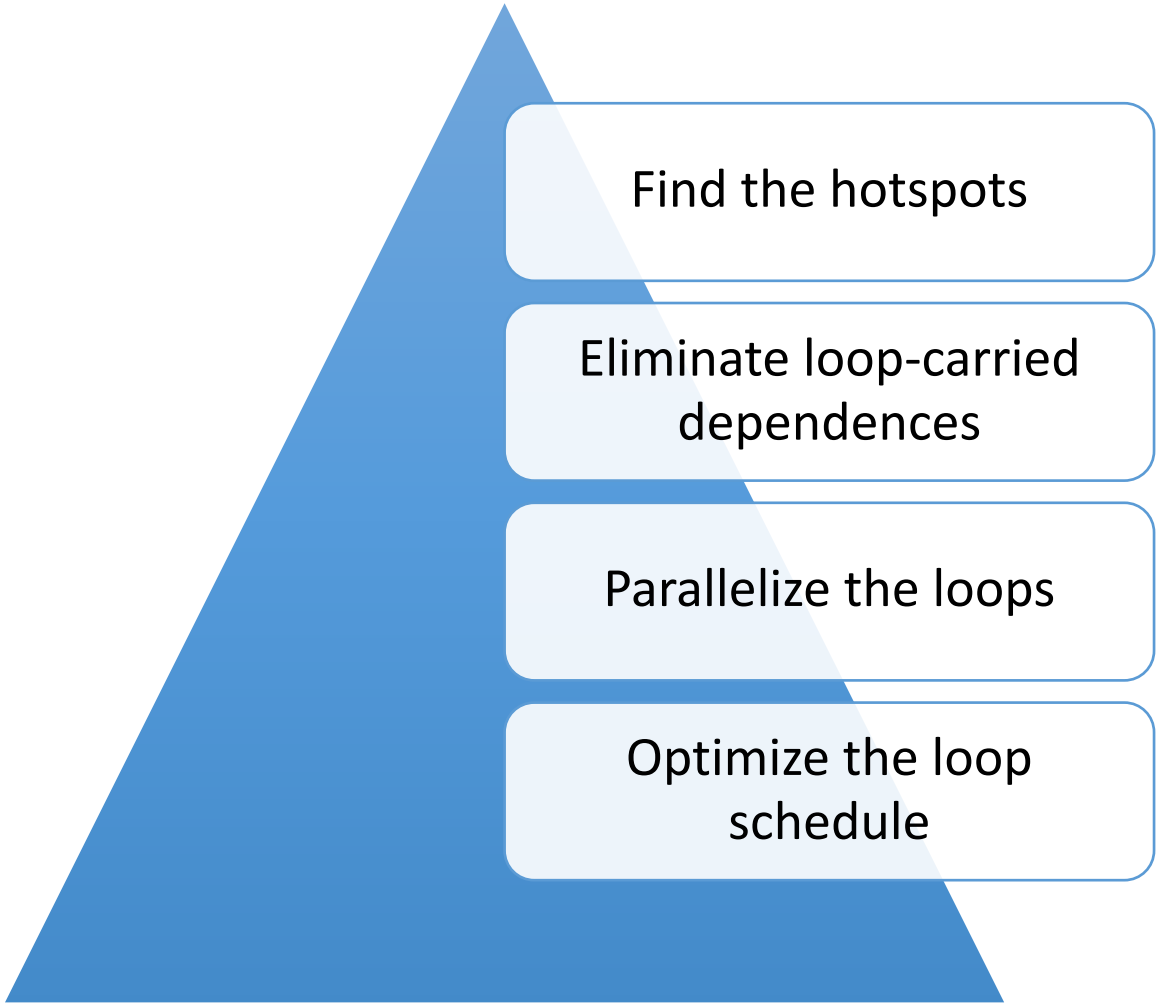
```
for (i=0; i<100; i++)
    S1: a[i] = i;
```

```
parallel_for (i=0; i<100; i++)
{
    S1: a[i] = i;
    S2: b[i] = 2*a[i];
}
```

?

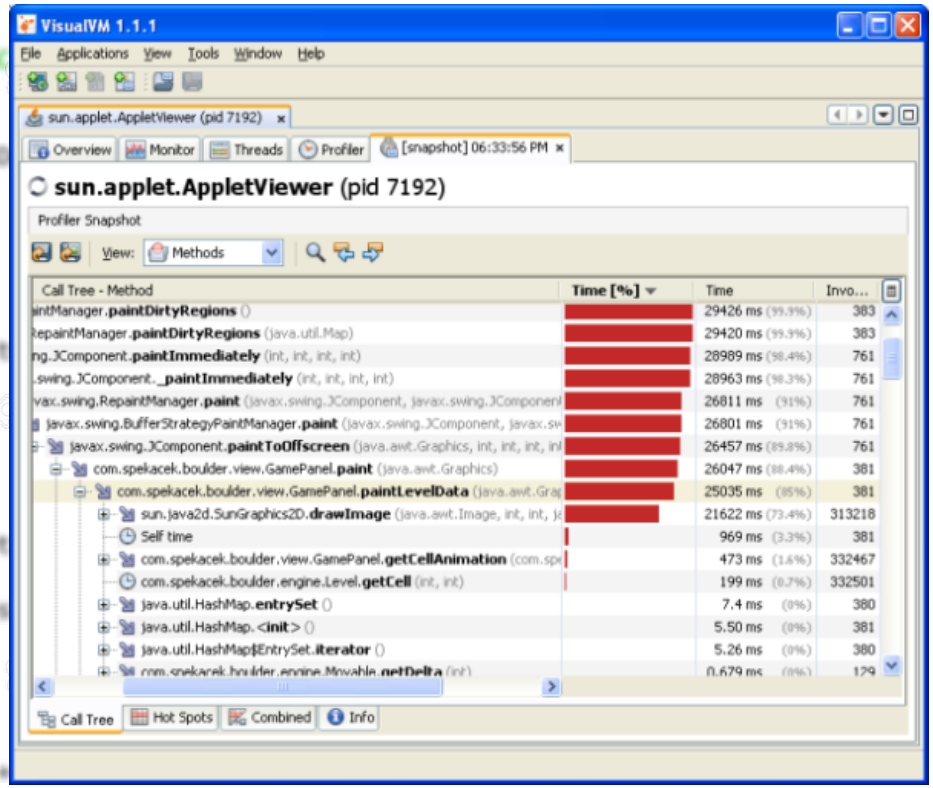
- Dependences? What about *i*, the loop index?
- *DOALL* loop (a.k.a. *foreach* loop)
  - All iterations are independent of each other
  - All statements will be executed in parallel at the same time
    - Is this really true?

General Approach for Loop Parallelism



Find the hotspots

- By code inspection
- By using performance analysis tools



Eliminate loop-carried dependences

- Statements dependences include: true dependences, anti-dependences and output dependences.
- Loop dependences also include those, carried from one execution of the loop to another.

Loop Dependences

- A *loop-carried* dependence is a dependence between two statements instances in two different iterations of a loop

```
S1: a = 5;
S2: b = a;
```

True dependence — the memory location 'a' is written (in S1) before it is read (in S2)

S1 ð S2

```
for (i=1; i<n; i++) {
    S1: a[i] = a[i-1];
}
```

True dependence — a memory location 'a[j]' is written before it is read in the next iteration of the loop

S1[j] ð S1[j+1]

Loop Dependences

- A *loop-carried* dependence is a dependence between two statements instances in two different iterations of a loop

```
S1: b = a;
S2: a = 5;
```

Anti-dependence — the memory location ‘a’ is read (in S1) before it is written (in S2)

S1 ∂^{-1} **S2**

```
for (i=0; i<n-1; i++) {
    S1: a[i] = a[i+1];
}
```

Anti-dependence — a memory location ’a[j]’ is read before it is written in the next iteration of the loop

S1[j] ∂^{-1} **S1[j+1]**

Loop Dependences

- A *loop-carried* dependence is a dependence between two statements instances in two different iterations of a loop

```
S1: c = 8;
S2: c = 15;
```

Output dependence — the same memory location ‘c’ is written (in S1) and then written once again (in S2)

S1 ∂^o S2

```
for (i=0; i<n; i++) {
    S1: c[i] = i;
    S2: c[i+1] = 5;
}
```

Output dependence — the same memory location ’a[j]’ is written (in S2) and then written again in the next iteration of the loop (in S1)

S2[j] ∂^o S1[j+1]

Loop Dependences

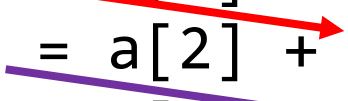
- A *loop-carried* dependence is a dependence between two statements instances in two different iterations of a loop
- Otherwise, it is *loop-independent*
- Loop-carried dependences can prevent loop iteration parallelization

Loop dependences: examples

- The following loop cannot be parallelized (without rewriting)

```
a[0] = 1;
for (i=1; i<N; i++) {
    a[i] = a[i] + a[i-1];
}
```

```
i=1: a[1] = a[1] + a[0];
i=2: a[2] = a[2] + a[1];
i=3: a[3] = a[3] + a[2];
...
```



Each iteration depends on the result of the preceding iteration

Detecting dependences

- Analyze how each variable is used within a loop iteration:
- Is the variable read and never written?
  => no dependences!
- For each written variable: can there be any accesses in other iterations than the current?
  => there are dependences!

Simple rule of thumb

- A loop that matches the following criteria has no dependences and can be parallelized:

1. All assignments to shared data are to arrays:
2. Each element is assigned by at most one iteration; and
3. No iteration reads elements assigned by any other iteration.

Example 1

- Is this loop parallelizable?

```
for (i=1; i<N; i+=2) {
    a[i] = a[i] + a[i-1];
}
```

```
i=1: a[1] = a[1] + a[0];
i=3: a[3] = a[3] + a[2];
i=5: a[5] = a[5] + a[4];
...
```

No dependences!

YES!! It is parallelizable!

Example 2

- Is this loop parallelizable?

```
for (i=0; i<N/2; i++) {
    a[i] = a[i] + a[i+N/2];
}
```

```
i=0: a[0] = a[0] + a[0+N/2];
i=1: a[1] = a[1] + a[1+N/2];
...
i=N/2-1: a[N/2-1] = a[N/2-1] + a[N-1];
```

No dependences!

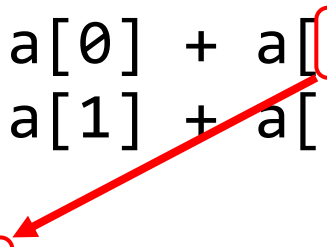
YES!! It is parallelizable!

Example 3

- Is this loop parallelizable?

```
for (i=0; i<=N/2; i++) {
    a[i] = a[i] + a[i+N/2];
}
```

```
i=0:   a[0]   = a[0]   + a[0+N/2];
i=1:   a[1]   = a[1]   + a[1+N/2];
...
i=N/2: a[N/2] = a[N/2] + a[N];
```



Loop carried true dependence

It is NOT parallelizable!

Example 4

- Is this loop parallelizable?

```
for (i=0; i<N; i++) {
    a[idx[i]] = a[idx[i]] + b[idx[i]];
}
```

```
i=0: a[?1] = a[?1] + b[?1];
i=1: a[?2] = a[?2] + b[?2];
i=3: a[?3] = a[?3] + b[?3];
...
```

Don't know which index is accessed in each iteration of the loop.

It is NOT parallelizable!

Removing dependences 1

- How to remove this dependence?

```
for (i=0; i<=N/2; i++) {
    a[i] = a[i] + a[i+N/2];
}
```

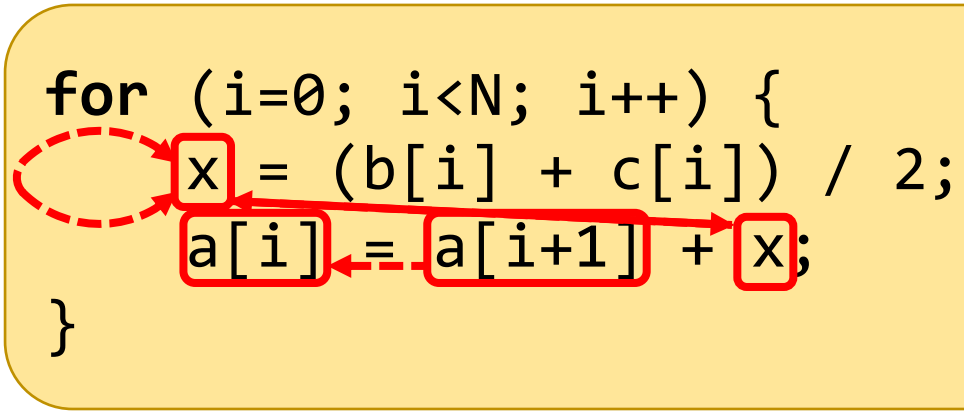
Take the dependent iteration out of the loop

```
for (i=0; i<N/2; i++) {
    a[i] = a[i] + a[i+N/2];
}
a[N/2] = a[N/2] + a[N];
```

Removing dependences 2

- How to remove this dependence?

```
for (i=0; i<N; i++) {
    x = (b[i] + c[i]) / 2;
    a[i] = a[i+1] + x;
}
```



- True dependence inside the loop (x)
- Output dependence between iterations (x)
- Anti-dependence between iterations (x)
- Anti-dependence between iterations (a[i])

- To remove the dependences on ‘x’ privatize it

Removing dependences 2

```
for (i=0; i<N; i++) {
    x = (b[i] + c[i]) / 2;
    a[i] = a[i+1] + x;
}
```

- How to remove this dependence?

```
for (i=0; i<N; i++) {
    int x = (b[i] + c[i]) / 2;
    a[i] = a[i+1] + x;
}
```

Anti-dependence between iterations (a[i])

- To remove the dependence on ‘a[i]’ make copy of ‘a’

Removing dependences 2

```
for (i=0; i<N; i++) {
    x = (b[i] + c[i]) / 2;
    a[i] = a[i+1] + x;
}
```

- How to remove this dependence?

```
for (i=0; i<N; i++) {
    a2[i] = a[i+1];
}
for (i=0; i<N; i++) {
    int x = (b[i] + c[i]) / 2;
    a[i] = a2[i] + x;
}
```

Anti-dependence between iterations (a[i])

- Both 'for' are parallelizable!! *Should we do it?*

Removing dependences 3

- How to remove this dependence?

```
for (i=1; i<N; i++) {
    b[i] += a[i-1];
    a[i] += c[i];
}
```

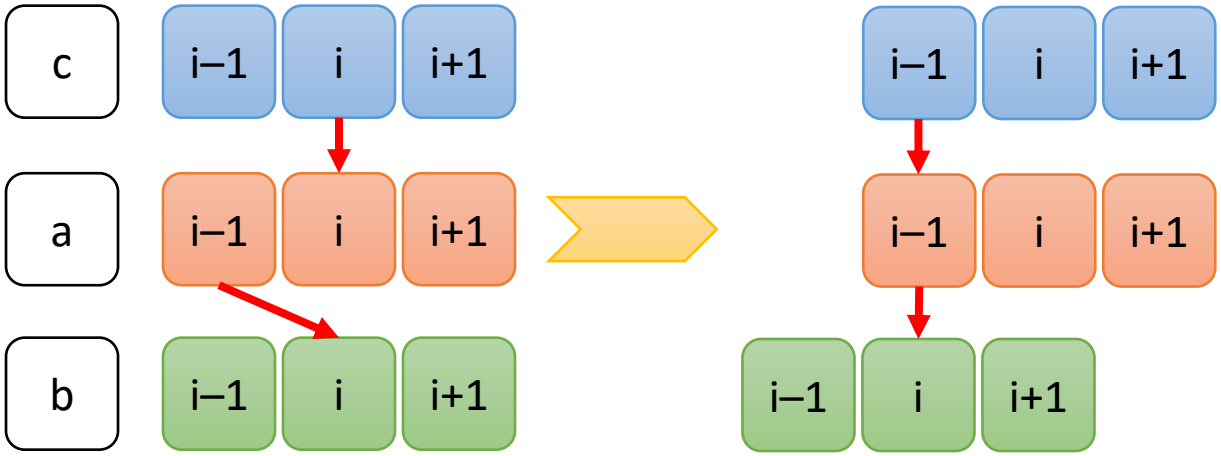
```
i=1: b[1]=b[1]+a[0]; a[1]=a[1]+c[1]
i=2: b[2]=b[2]+a[1]; a[2]=a[2]+c[2]
...
i=N-1 : b[N-1]=b[N-1]+a[N-2]; a[N-1]=a[N-1]+c[N-1]
```

Removing dependences 3

- How to remove this dependence?

```
for (i=1; i<N; i++) {
    b[i] += a[i-1];
    a[i] += c[i];
}
```

Use *software pipelining!*



Removing dependences 3

- How to remove this dependence?

```
for (i=1; i<N; i++) {
    b[i] += a[i-1];
    a[i] += c[i];
}
```

```
b[1] += a[0];
for (i=1; i<N-1; i++) {
    a[i] += c[i];
    b[i+1] += a[i];
}
a[N] += c[N];
```

Removing dependences 4

The END