

Matlab[©] Exercise II: Active Noise Control with an FIR filter

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Question 1

Question 1.1

Question 1.2

```
1 %% Initialization
2
3 close all
4 clear all
5
6 % Load uncorrupted signal d
7 % N is the number of samples (signal length)
8 load gong.mat;
9 [N,k]=size(y);
10 d = y;
11
12 % Generate zero-mean white noise sequence g with standard deviation 0.35
13 sg = 0.35;
14 g = sg*randn(N,1);
15 g = g - mean(g);
16
17 % Generate noise sequences v1 and v2
18 a1 = [1 -0.90]; b1 = [1 -.2];
19 a2 = [1 -0.95]; b2 = [1 -.3];
20 v1 = filter(b1,a1,g);
21 v2 = filter(b2,a2,g);
22
23 % Generate the corrupted signal x
24 x = d + v1;
25
26 %% Exercise 1: Determining the optimal FIR Wiener Filter
27 % Goal: reconstruct d from x and v2 by estimating v1 from v2
```

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28
29 % Let n vary between the desired filter orders
30 n = [1 2 4 6];
31 Stdd = zeros(length(n),1);
32 W_tot = zeros(max(n),length(n));
33 for k = 1:4
34 % First we determine Rv2 and Rv1v2 needed to set up the Wiener-Hopf
35
36 % Calculate the first two values of rv2 (i.e. rv2(0) and rv2(1))
37 % using eq (3.116) from Hayes
38 h = dimpulse(b2, a2, 20);
39 c(1,1) = b2(1)*conj(h(1)) + b2(2)*conj(h(2));
40 c(2,1) = b2(2)*conj(h(1));
41
42 rv2 = zeros(200,1);
43 rv2(1) = (sg^2*c(1,1) - a2(2)*sg^(2)*c(2,1))/(1-a2(2)^2);
44 rv2(2) = sg^2*c(2,1) - a2(2)*rv2(1);
45
46 % Calculate the rest of rv2 until it becomes (almost) zero
47 % We only determine one side of the auto-correlation function and then
48 % mirror, to get the double sided ACF (centered at index 200)
49 for i=3:200,
50     rv2(i) = -1*a2(2)*rv2(i-1);
51 end
52 rv2_ds = [rv2(end:-1:1); rv2(2:end)];
53
54 % Next we determine the the cross-correlation function between v1 and v2
55 bb = conv(b1,a2);
56 aa = conv(b2,a1);
57 rv1v2_ds = filter(bb,aa,rv2_ds);
58
59 % Put rv2 and rv1v2 into matrix form for the Wiener-Hopf equations
60 Rv2 = zeros(n(k),n(k));
61 for i = 1:n(k)
62     for j = 1:n(k)
63         Rv2(i,j) = rv2_ds(200+j-i);
64     end
65 end
66 Rv1v2 = zeros(n(k),1);
67 for i=1:n(k),
68     Rv1v2(i,1) = rv1v2_ds(200+i-1);
69 end
70
71 % Solve for the optimal filter
72 W = Rv2\Rv1v2;
73 v1e = filter(W,1,v2);
74 de = x - v1e;
75
76 % Save the necessary data necessary to evaluate the sound
77 W_tot(1:length(W),k) = W;
78 Stdd(k) = std(d-de);
79 end

```

Table 1: Output coefficients $w(j)$ for the optimal FIR Wiener filter

Coefficient $w(j)$	Filter order m			
	1	2	4	6
$w(0)$	0.7759	0.9209	0.9935	0.9995
$w(1)$	0	-0.1623	0.0327	0.0487
$w(2)$	0	0	-0.0765	-0.0242
$w(3)$	0	0	-0.2255	-0.0514
$w(4)$	0	0	0	-0.0859
$w(5)$	0	0	0	-0.1916

Question 2

Table 2: Standard deviation σ_W between the sound $d(n)$ and the estimated sound $x(n) - \hat{v}_1(n)$

Filter order m	σ_W
1	0.2075
2	0.1996
4	0.1674
6	0.1362

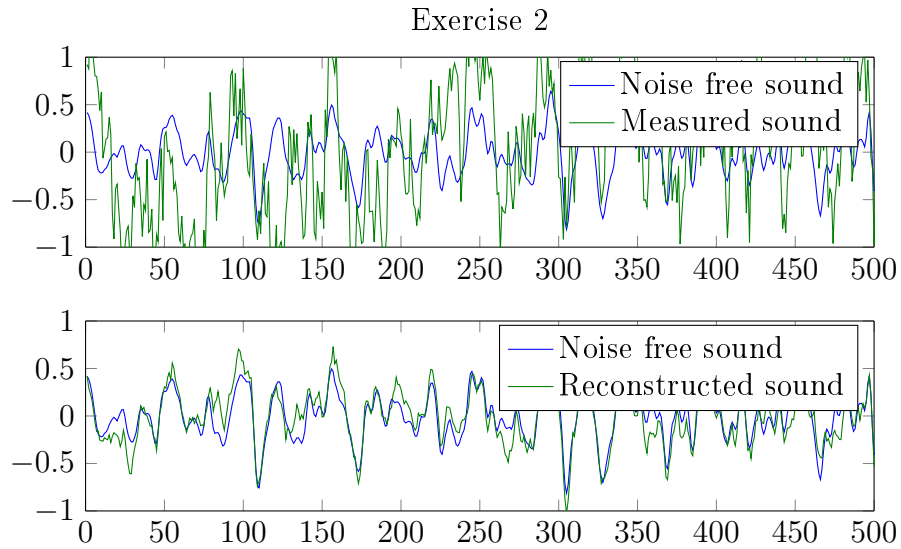


Figure 1: Subplot 1 shows the original sound and the noise corrupted signal. Subplot 2 shows the original sound and the filtered sound with optimal Wiener filter $W(z)$ of order 6

Question 3

```

1 %% Exercise 3: Filter by approximating the correlation functions
2 % Goal: Approximate the auto- and cross correlation functions used in
3 %       the Wiener-Hopf equations from the signals
4
5 %n = input('Order filter: ');
6 % Let n vary between the desired filter orders
7 n = [1 2 4 6];
8 Stdd2 = zeros(length(n),1);
9 W_tot2 = zeros(max(n),length(n));
10 for k = 1:length(n)
11 % Construct an n by (N-n+1) matrix V2 containing shifted versions of v2
12 V2 = zeros(n(k), N-n(k)+1);
13 for i=1:n(k)
14     V2(i,:) = v2(n(k)+1-i:N+1-i);
15 end
16
17 % Use V2 and v1 to estimate Rv2 and Rv1v2
18 rv2e = zeros(n(k),1);
19 for i = 1:n(k)
20     rv2e(i) = sum(V2(1,:).*V2(i,:));
21 end
22
23 % Put rv2e in a Toeplitz matrix like in Exercise 2
24 rv2e_ds = [rv2e(end:-1:1);rv2e(2:end)];
25 Rv2e = zeros(n(k),n(k));
26 for i = 1:n(k)
27     for j = 1:n(k)
28         Rv2e(i,j) = rv2e_ds(n(k)+j-i);
29     end
30 end
31
32 Rv1v2e = zeros(n(k),1);
33 for i=1:n(k),
34     Rv1v2e(i,1) = sum(x(n(k):end).*(V2(i,:).'));
35 end
36
37 % Calculate filter using Wiener-Hopf equations and reconstruct the signal
38 w = Rv2e\Rv1v2e;
39 v1e = filter(w,1,v2);
40 de = x - v1e;
41
42 % Save all the variables for the different values of n
43 std(d-de);
44 Stdd2(k) = std(d-de);
45 W_tot2(1:length(w),k) = w;
46 end

```

Table 3: Output coefficients $w(j)$ for the estimated FIR Wiener filter

Coefficient $w(j)$	Filter order m			
	1	2	4	6
$w(0)$	0.7679	0.9200	0.9960	0.9995
$w(1)$	0	-0.1689	0.0339	0.0513
$w(2)$	0	0	-0.0783	-0.0243
$w(3)$	0	0	-0.2342	-0.0548
$w(4)$	0	0	0	-0.0885
$w(5)$	0	0	0	-0.1956

Table 4: Standard deviation σ_w between the sound $d(n)$ and the estimated sound $x(n) - \hat{v}_1(n)$

Filter order m	σ_w
1	0.2177
2	0.2089
4	0.1750
6	0.1423

Exercise3

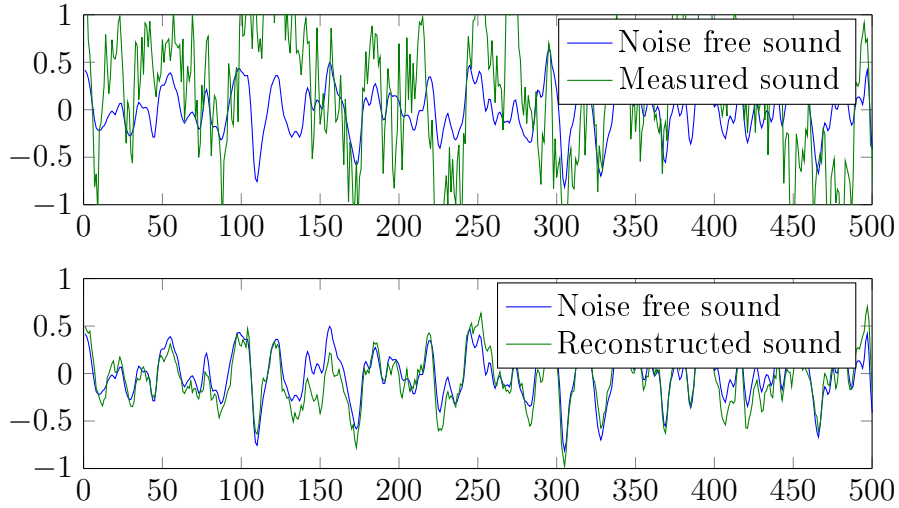


Figure 2: Subplot 1 shows the original sound and the noise corrupted signal. Subplot 2 shows the original sound and the filtered sound with estimated Wiener filter $w(z)$ of order 6