This exam has 6 problems on 2 pages. There are no calculators, phones, or other electronic devices allowed during this exam. Be sure to show all your work.

Name:

Score:

id-number:

Problem 1. Solve the following limits if posible:

- (a) $\lim_{h\to 0} \frac{\sqrt{h+1}-1}{h}$
- (b) $\lim_{x\to\infty} \frac{34000x^2+6000x+25000}{1+x+x^2+x^3}$
- (c) $\lim_{x\to 5} \frac{2x^2-7x-15}{3x^2-11x-20}$
- (d) $\lim_{x\to 0} \frac{x}{|x|}$

Problem 2. Derive w.r.t. both variables:

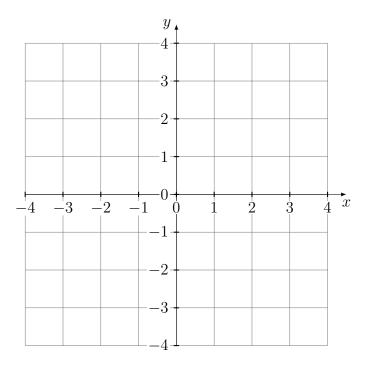
- (a) $x^{\ln 4}e^{x^2+y^2}$
- (b) $\frac{x^{\frac{1}{4}}y^{\frac{1}{3}}}{e^x}$
- (c) $\ln x^3 y^2$

Problem 3. Solve the following integrals by direct methods, substitution and parts respectively:

- (a) $\int_0^1 x^{\frac{1}{2}} dx$
- (b) $\int xe^{-x^2}dx$
- (c) $\int x \ln x dx$

Problem 4. Find the derivative of w with respect to z of the following function $\ln{(x^4y^3z^6t^2w)}$ by making use of the implicit function theorem.

Problem 5. Sketch the following function e^{-x^2} by showing analytically over what intervals the functions is increasing and decreasing, over what intervals the function is convex or concave and where are the maxima and minima of the function if at all.



Problem 6. Solve the following problem using the Khun-Tuker conditions:

$$\max_{x,y} \quad f(x,y) = -x^2 - xy - y^2$$

$$s.t. \quad x - 2y \le -1$$

$$2x + y \le 2$$