



Master's thesis

# Model independent search for Dark Matter using Machine Learning

In final states with dileptons and Missing Transverse Energy with the ATLAS  
detector at the LHC

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## Abstract

The focus of this thesis is to perform an independent search for new physics phenomena, such as evidence of a Dark Matter (DM) candidate and its possible mediator using supervised Machine Learning (ML). A Neural Network (NN) and a Boosted Decision Tree (BDT) will be trained on various Monte Carlo (MC) simulated data samples featuring well-defined predictions from a set of DM models and the SM background. The analysis uses data recorded by the ATLAS detector, from proton-proton (pp) collisions at the LHC during the Run II data taking period from 2015 to 2018 at 13 TeV. The data consists of dilepton final states with Missing Transverse Energy (MET).

The emphasis is to set up an ML algorithm to learn the features on a set of models predicting DM candidates with a dilepton + MET final state, such as simplified DM models involving or not a mediator, including those models based on effective field theory (EFT) and supersymmetry. Then optimizing relevant signal search regions, based on, among others, the invariant mass of the two leptons and the missing transverse energy, thus reaching better search sensitivities.

After preparing both a NN and a BDT ML algorithm and exploring methods to mitigate the weighting and padding of the datasets, we concluded, that a BDT approach was best suited for this search. We first tested a less model independent approach training a BDT with all the Standard Model (SM) background processes and one DM model, including all the simulated samples, for every model. The second approach consisted of a dataset containing all the DM models and all the SM backgrounds. The latter only trained three BDTs in orthogonal MET spaces. The three MET regions:  $E_T^{miss} \in [50, 100]$  GeV,  $E_T^{miss} \in [100, 150]$  GeV, and  $E_T^{miss} > 150$ .

We tested each model by computing a Bayesian mass exclusion limit. To compare the approaches, we statistically combined the mass exclusion limit of all SRs into one combined SR. Doing this for every model we observed that we were able to compute higher expected mass exclusions limits using the more model independent approach of dividing a dataset into different regions of kinematical phase space.

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# List of Acronyms

**SM** Standard Model

**DM** Dark Matter

**LHC** Large Hadron Collider

**MET** Missing Transverse Energy

**MC** Monte Carlo

**ML** Machine Learning

**NN** Neural Network

**BDT** Boosted Decision Tree

# Chapter 1

## Introduction

After the Higgs boson, the last ingredient of the Standard Model (SM), was discovered in 2012 [1], we still question its nature. Is it the long-awaited SM particle, is it the first of a series of scalar particles? With the advent of higher energies and higher collision rates, the Large Hadron Collider (LHC) continues the voyage towards new physics phenomena. The ambitious LHC physics programme may shed light on some of the greatest mysteries in physics today. The focus of this work is to perform an independent search for new physics phenomena, such as evidence of a Dark Matter (DM) candidate and its plausible mediator using supervised learning. A Neural Network (NN) and a Boosted Decision Tree (BDT) will be trained on various Monte Carlo (MC) simulated data samples featuring well-defined predictions from a set of new physics theories. The analysis uses proton-proton (pp) collisions at the LHC from Run II at 13 TeV, recorded by the ATLAS detector. The data consists of dilepton final states with Missing Transverse Energy (MET). By comparing the empirical data collected from Run II with SM simulated samples we will carefully select the features to be used in the training phase of the Machine learning (ML) networks.

One of the biggest motivations for this project is to search for Dark Matter (DM), one of the biggest mysteries in science to this day. It can be a Weakly Interacting Particle (WIMP) [2] or the Axion [3] which are both postulated by cosmological constraints. This project will focus on DM particles that are described by WIMP theories. The emphasis is to set up a NN and a BDT to be trained on a set of models predicting DM particles, such as supersymmetry, simplified DM models involving or not a mediator, including those

models based on effective field theory (EFT). This way we aim at a model independent search of a DM particle, possibly together with its mediator.

We concentrate on dilepton and Missing Transverse Energy (MET) final states,  $pp \rightarrow l^+l^-\chi\chi = l^+l^- + \text{MET}$ . Where the MET is due to DM since we cannot detect it directly in particle detectors. There are various Beyond Standard Model (BSM) models with a DM candidate  $\chi$  leading to this process final state. The standard practice in new physics searches today is to choose one model and do a thorough data analysis to test it. However, the emphasis of this project as aforementioned will be to let an ML algorithm learn the features of various DM models predicting a dilepton + MET final state, thus optimizing relevant signal search regions, based on, among others, the invariant mass of the 2 leptons and the missing transverse energy, thus reaching better search sensitivities. Utilizing the powerful tool of ML it might help recognize a pattern that is common through all the different models studied, at least within each of the signal regions defined, which might in turn get us closer to finding a real empirical signal of DM through data. The goal is to study various BSM models, such as: Mono-Z', Dark Higgs, Light Vector and inelastic

EFT [4], Mono-Z [5] and Supersymmetry [6]. These models are built upon different theoretical principles, making them phenomenologically different from each other, with some common experimental features. Thus, this approach to build a generic ML algorithm to be simultaneously trained on all of them could reduce the computational time needed to train an ML algorithm.

Should I mention that the goal was to study mono-z and susy here?

We will start this thesis by introducing the theoretical foundation behind the SM using Quantum Field Theory, thereafter we will present the theory behind the DM models we will study. After the field theory description of the background and signal that will be used on the ML algorithms, we will present how we can actually measure anything from this, both from a kinematical and experimental point of view. Afterwards, we will present the ATLAS detector and the current method of studying for new physics in CERN related high energy particle physics research. After that we will give a theoretical description of both NNs and BDTs, as well as the tools that will be used to evaluate their performances.

After that we will show the methods we will use to prepare the dataset for ML, meaning

the event selection as well as the feature selection. In this section we will discuss what problems arise using our method. After that we will present the whole dataset and how we plan to do our model independent approach. Then we will present the challenges that arise when having extreme datasets for NNs and BDTs, and what methods we use to mitigate these challenges. Lastly, we will present the results of every method studied and discuss the results.



## Part I

The theory behind modern particle  
physics / Background



## Chapter 2

# The Standard Model of Particle Physics

$$\mathcal{L}_{SM} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + i\bar{\psi}\not{D}\psi + \psi_i y_{ij}\psi_j\phi + h.c. + |D_\mu\phi|^2 - V(\phi) \quad (2.1)$$

Equation (2.1) represents the elegant equation which can explain phenomena in nature with great precision, and is the mathematical foundation of what we know as the Standard Model (SM) of particle physics. It consists of three *symmetry groups*. The gauge group explaining electromagnetism  $U(1)$ , the gauge group describing the weak force  $SU(2)_L$  and the gauge group describing the strong force  $SU(3)_C$ . In this chapter we will delve into each of these groups, the spontaneous symmetry breaking phenomena that gives mass to particles, as well as how to calculate the cross-section of processes.

As the SM is described using Quantum Field Theory, we will now give a description of what a *field* is. A quantum field is a fundamental concept in quantum physics that describes the underlying fabric of reality, where particles and their interactions are represented as excitations or vibrations of these fields.

The theory of this section is mainly based of Peskin's and Schroeder's "An Introduction to Quantum Field Theory" [7] and partly Thomson's "Modern Particle Physics" [8].

## 2.1 Quantum Electrodynamics

In the beginning there was nothing; *then God said, "Let there be light," and there was light.* This lead us to the first part of the Standard Model, Quantum Electrodynamics, or QED for short,

$$\mathcal{L}_{QED} = \bar{\psi} (iD^\mu - m) \psi - \frac{1}{4} B^{\mu\nu} B_{\mu\nu} \quad (2.2)$$

with  $\bar{\psi} = \psi^\dagger \gamma^0$ , where  $\psi$  is a bispinor field of spin-1/2<sup>1</sup>,  $m$  is the mass of  $\psi$ ,  $\gamma^\mu$  are the Dirac matrices, defined as

$$\gamma^0 = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}, \quad \gamma^1 = \begin{pmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \end{pmatrix},$$

$$\gamma^2 = \begin{pmatrix} 0 & 0 & 0 & -i \\ 0 & 0 & i & 0 \\ 0 & i & 0 & 0 \\ -i & 0 & 0 & 0 \end{pmatrix}, \quad \gamma^3 = \begin{pmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \\ -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{pmatrix}$$

Furthermore we have  $D^\mu \equiv \gamma^\mu D_\mu$  where  $iD_\mu = i\partial_\mu - eB_\mu$  is the covariant derivative, where  $e$  is the coupling constant<sup>2</sup>,  $B_{\mu\nu} = \partial_\mu B_\nu - \partial_\nu B_\mu$  is the electromagnetic field tensor<sup>3</sup>.  $B_\mu$  is the covariant four-potential<sup>4</sup> of the Lagrangian, also known as the gauge field.

The above Lagrangian is described by a  $U(1)$  symmetry group, meaning that it corresponds to the *unitary* group of one unitary matrix with determinant 1<sup>5</sup>. The consequence of QED being described by this symmetry group is, recalling Noether's theorem, that there is only one unique degree of freedom, this is the rotation of phase angle,  $\alpha$ , of

<sup>1</sup>In QED, it is the electron or positron field

<sup>2</sup>Which in QED is the electric charge of  $\psi$ .

<sup>3</sup>Taking  $\partial_\mu B^{\mu\nu} + \star \partial_\mu B^{\mu\nu} = 0$  gives all of Maxwell's equations.

<sup>4</sup>Defined as  $B_\mu = (\frac{1}{c}\phi, \mathbf{B})$  where  $\phi$  is the electric potential and  $\mathbf{B}$  is the magnetic potential we know and love from electrodynamics.

<sup>5</sup>For more information about group theory we refer the reader to Georgi's "LIE ALGEBRAS IN PARTICLE PHYSICS. FROM ISOSPIN TO UNIFIED THEORIES" [9]

the field  $\psi$ . This means that

$$\psi \rightarrow \psi' = e^{i\alpha} \psi \quad (2.3)$$

and

$$B_\mu \rightarrow B'_\mu = \frac{1}{e} D_\mu \alpha \quad (2.4)$$

Which yields  $\psi = \psi'$  and  $B_\mu = B'_\mu$ , meaning that our theory is gauge invariant.

## 2.2 Yang-Mills Theory

While QED is expressed by the Lagrangian in Eq. (2.2), which is part of a  $U(1)$  symmetry group, it can still be described by a more general Lagrangian using *Yang-Mills* theory. The Yang-Mills Lagrangian looks almost identical to the QED Lagrangian, the differences being that the gauge freedom changes from a rotation of the phase angle  $\alpha$  of the field  $\psi$ , to a more general gauge in  $\alpha^a$  in the field  $f_i$

$$f_i \rightarrow (1 + i\alpha^a t^a + \mathcal{O}(\alpha^2)) f_i$$

The covariant derivative also changes to a more general

$$iD_\mu = i\partial_\mu - eB_\mu \rightarrow iD_\mu = i\partial_\mu - gA_\mu^a t^a$$

where  $e$  is replaced for a more general scale factor  $g$ , the vector field  $B_\mu$  to a more general  $A_\mu^a$  which transforms as

$$A_\mu^a \rightarrow A_\mu^a + \frac{1}{g} \partial_\mu \alpha^a + f^{abc} A_\mu^b \alpha^c$$

where  $f^{abc}$  is a set of numbers called the *structure constants*. The important thing to note about the Yang-Mills is that the covariant derivative can be *non-Abelian*, meaning that the commutator of the operator becomes

$$[D_\mu, D_\nu] = -igF_{\mu\nu}^a t^a$$

this new  $t^a$  factor is a Lie algebra generator, which for our purposes represent a local gauge symmetry we have on the field. The structure constant has to fulfill the criteria

that

$$[t^a, t^b] = i f^{abc} t^c \quad (2.5)$$

The difference between the Yang-Mills and the QED Lagrangian is most noticeable when fully writing

$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + g f^{abc} A_\mu^b A_\nu^c$$

Where the last term takes into account the *self interaction* of bosons. Adding all of this up we get the following Lagrangian

$$\mathcal{L}_{YM} = \bar{f} (iD^\mu - m) f - \frac{1}{4} (F_{\mu\nu}^a)^2 \quad (2.6)$$

where we use the notation  $f \equiv \begin{pmatrix} f_1 & f_2 & \dots & f_n \end{pmatrix}^T$  where  $f_i$  is a field. Using the Euler-Lagrange equation with the Yang-Mills Lagrangian above yields the equation of motion

$$\partial^\mu F_{\mu\nu}^a + g f^{abc} A^{b\mu} F_{\mu\nu}^c = -g \bar{\psi} \gamma_\nu t^a \psi \quad (2.7)$$

As using Noether's theorem on the equation of motion gives us the conserved quantity of the theory, we will apply it for every symmetry group in the SM. There is also a theorem<sup>6</sup> that states that for an  $SU(n)$  symmetry group there are  $n^2 - 1$  vector fields.

If we were to choose  $U(1)$  as our local symmetry group the generator  $t^a = \mathbb{I}$  and all the structure constants are  $f^{abc} = 0$ , meaning that we get the QED back. Noether's theorem states that the conserved quantity of the Lagrangian is the electric charge  $e$ .

## 2.3 Weak theory

Using the Yang-Mills Lagrangian from Eq. (2.6) on  $SU(2)$ , choosing  $t^a = \frac{\sigma^i}{2}$ , where  $\sigma^i$  are the Pauli matrices given as

$$\sigma^1 = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, \quad \sigma^2 = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}, \quad \sigma^3 = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \quad (2.8)$$

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<sup>6</sup>See Georgi's book [9]

The structure constants are the Levi-Civita  $f^{abc} = \epsilon^{ijk}$ . Where  $i, j, k \in [1, 2, 3]$ . The Weak theory gives us the gauge freedoms of

$$f \rightarrow (1 + i\alpha^i \sigma^i + \mathcal{O}(\alpha^2)) f$$

Using the notation of  $A_\mu \rightarrow W_\mu$  we get that there are  $2^2 - 1$ , meaning three vector fields

$$W_\mu^i \rightarrow W_\mu^i + \frac{1}{g} \partial_\mu \alpha^i + \epsilon^{ijk} W_\mu^j \alpha^k$$

If one were to apply Noether's theorem on this Lagrangian we would get that two quantities are conserved, the *hypercharge* and *isospin*. In this theory we have isospin doublets, meaning

$$f = \begin{pmatrix} f_1 \\ f_2 \end{pmatrix} \rightarrow \begin{pmatrix} U \\ D \end{pmatrix}$$

For *up and down type* particles.

## 2.4 Quantum Chromodynamics

Using the Yang-Mills Lagrangian from Eq. (2.6) on an  $SU(3)$ , choosing  $t^a = \frac{\lambda^a}{2}$ , where  $\lambda^a$ , the *Gell-Mann matrices*, are the  $SU(3)$  equivalent of the  $SU(2)$  Pauli matrices:

$$\begin{aligned} \lambda^1 &= \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, & \lambda^2 &= \begin{pmatrix} 0 & -i & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, & \lambda^3 &= \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \\ \lambda^4 &= \begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix}, & \lambda^5 &= \begin{pmatrix} 0 & 0 & -i \\ 0 & 0 & 0 \\ i & 0 & 0 \end{pmatrix}, & \lambda^6 &= \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}, \\ \lambda^7 &= \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -i \\ 0 & i & 0 \end{pmatrix}, & \lambda^8 &= \frac{1}{\sqrt{3}} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix} \end{aligned} \tag{2.9}$$

The structure constant have to obey Eq. (2.5), thus we get

$$\begin{aligned} f^{123} &= 1 \\ f^{147} = -f^{156} = f^{246} = f^{257} = f^{345} = -f^{367} &= \frac{1}{2} \\ f^{458} = f^{678} &= \frac{\sqrt{3}}{2} \end{aligned}$$

Using the notation of  $A_\mu \rightarrow G_\mu$  we get that there are  $3^2 - 1$ , meaning *eight* vector fields

$$G_\mu^a \rightarrow G_\mu^a + \frac{1}{g} \partial_\mu \alpha^a + \epsilon^{abc} G_\mu^b \alpha^c$$

If one were to use Noether's theorem on the  $SU(3)$  Yang-Mills Lagrangian, we would get that there are three conserved quantities for this symmetry group. These are the colors,  $r, g$  and  $b$ . With all the information above we can fully describe Quantum Chromodynamics, which describe quark interactions. The eight vector fields are the eight different gluons that are in the theory.

In this theory we have color triplets

$$f = \begin{pmatrix} f_1 \\ f_2 \\ f_3 \end{pmatrix}$$

where  $f_i$  is the color state of the particle we are studying.

## 2.5 Electroweak unification and the BEH Mechanism

We have so far explained the three symmetry groups that form the SM, but this is not the full picture yet. To get the full SM we need to talk about the electroweak  $U(1)_Y \otimes SU(2)_L$  unification that can be explained when studying the spontaneous symmetry breaking (SSB) phenomena, which also includes the *Higgs* boson.

If we introduce a new complex scalar field  $\phi$  that transforms in the  $SU(2)$  representation,

we can write the Lagrangian

$$\mathcal{L} = -\frac{1}{2} \text{Tr} (W_{\mu\nu} W^{\mu\nu}) - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} + (D_\mu \phi)^\dagger (D^\mu \phi) - \lambda \left( \phi^\dagger \phi - \frac{v^2}{2} \right)^2 \quad (2.10)$$

with

$$D_\mu \phi = \partial_\mu \phi - ig W_\mu^a \sigma^a - i \frac{e}{2} B_\mu \phi \quad (2.11)$$

where  $W_\mu$  and  $B_\mu$  are vector fields of the  $SU(2)$  and  $U(1)$  group respectively. And where  $-\lambda \left( \phi^\dagger \phi - \frac{v^2}{2} \right)^2 = V(\phi)$  is the potential of the new complex scalar field. Writing

$$\phi = \begin{pmatrix} o \\ v + H(x) \end{pmatrix} \quad (2.12)$$

where  $H$  is real scalar field, expands the potential to be

$$V(H) = \frac{1}{2} m_H^2 H^2 + \frac{1}{2v} m_H^2 H^3 + \frac{1}{8v^2} m_H^2 H^4 \quad (2.13)$$

where we have used that  $m_H = \sqrt{2\lambda}v$ . This potential is the so-called *Sombrero potential*, and we can reveal that this scalar field  $H$  is the Higgs boson. The consequences of writing our complex scalar field using Eq. (2.12) comes when from the shape of the potential, this gives rise to the mass of particles. The SSB comes from the fact that the fields have two minima on the potential but can move around in a higher dimensional space (around the sombrero edge) to get to the other minima.

Another thing that follows from Eq. (2.12) is that expanding on Eq. (2.11) gives rise (after a lot of math) to the following relations

$$W_\mu^\pm = \frac{W_\mu^1 \mp i W_\mu^2}{\sqrt{2}} \quad (2.14)$$

$$Z_\mu = \frac{g W_\mu^3 - e B_\mu}{\sqrt{g^2 + e^2}} \quad (2.15)$$

$$A_\mu = \frac{g B_\mu - e W_\mu^3}{\sqrt{g^2 + e^2}} \quad (2.16)$$

These are the  $W$  and  $Z$  boson as well as the photon, respectively. To explicitly show how the SSB phenomena gives mass to every other particle, one can compute the unitary gauge transformation of the scalar field, this adds an extra term on the Lagrangian called the *Yukawa* Lagrangian

$$\mathcal{L}_{YU} = \psi_i y_{ij} \psi_j \phi = \overline{U}_L G_u U_R \phi^0 + \overline{D}_L G_u U_R \phi^- \overline{U}_L G_D D_R \phi^+ \overline{D}_L G_u D_R \phi^0$$

where  $G_{u,d}$  are the Yukawa couplings. As we are looking at a complex scalar field in the  $SU(2)$  representation we have from the Yang-Mills theory that we can write

$$f = \begin{pmatrix} U \\ D \end{pmatrix}$$

where  $U, D$  is the field *up and down type* spinor. For example this can be the first generation quark two component spinor  $Q = \begin{pmatrix} u \\ d \end{pmatrix}$  consisting of the *up* and *down* quark.

The standard for weak interactions is to define *right* and *left* handed helicity using the operators

$$L = \frac{1}{2}(\mathbb{I} - \gamma_5), \quad \text{and} \quad R = \frac{1}{2}(\mathbb{I} + \gamma_5)$$

where  $\gamma_5 = i\gamma^0\gamma^1\gamma^2\gamma^3$ . Such that we can write

$$U_L = L \begin{pmatrix} U \\ D \end{pmatrix} = \begin{pmatrix} U \\ 0 \end{pmatrix}, \quad \text{and} \quad D_R = R \begin{pmatrix} U \\ D \end{pmatrix} = \begin{pmatrix} 0 \\ D \end{pmatrix}$$

as well as their hermitian conjugates.

## 2.6 S-matrix expansion

But how do we calculate processes? To explain this generally, we can conduct an S-matrix expansion. To be more precise and use terms from quantum field theory rather than quantum mechanics, we can use the scattering operator  $\mathcal{S}$  on the interaction term

of the SM Lagrangian  $\mathcal{L}_{int}$ . Starting by defining the general operator

$$\begin{aligned} \mathcal{S} &= \sum_{i=vertices} \mathcal{S}^{(i)}, \quad \text{where } \mathcal{S}^{(0)} = \mathbb{I} \quad \text{and} \\ \mathcal{S}^{(n)} &= (-i)^n \mathcal{T} \int_{-\infty}^{\infty} d^4 \mathbf{x}_1 \cdots \int_{-\infty}^{\infty} d^4 \mathbf{x}_n [\mathcal{H}_{int}(x_1) \cdots \mathcal{H}_{int}(x_n)] \end{aligned} \quad (2.17)$$

where  $\mathcal{T}$  is the *time operator* ordering the terms such that we calculate our desired process,  $\mathcal{H}_{int} = -\mathcal{L}_{int}$  is the interaction Lagrangian, and  $\mathbf{x}_i$  are coordinates in spacetime. The  $\mathcal{S}$  operator sums over all *vertices* of a *Feynman diagram*. To calculate the probability amplitude we can start with an easy example using QED, the Bhabha scattering process  $e^- e^+ \rightarrow e^- e^+$ . The interaction Lagrangian in that gives us this scattering process is  $\mathcal{L}_{int} = e \bar{\psi}(x) \gamma^\mu \psi(x) A_\mu$ . To calculate the probability amplitude we use the scattering operator in the following way

$$\begin{aligned} \langle f | \mathcal{S}^{(n)} | i \rangle &\rightarrow \langle e^- e^+ | S^{(2)} | e^- e^+ \rangle \\ &= \langle e^- e^+ | \left( -e^2 \mathcal{T} \int_{-\infty}^{\infty} d^4 \mathbf{x} \int_{-\infty}^{\infty} d^4 \mathbf{y} \bar{\psi}(x) \gamma^\mu \psi(x) A_\mu(x) \bar{\psi}(y) \gamma^\nu \psi(y) A_\nu(y) \right) | e^- e^+ \rangle \end{aligned}$$

Starting by using the time operator  $\mathcal{T}$  on the integrals, which gives us the *normal order* of the operations, we can start by using *Wicks theorem* to "connect" the two points in spacetime  $\mathbf{x}$  and  $\mathbf{y}$ . As we know there are no photons on the initial or final state, we can connect the photons as *propagators*, meaning

$$S^{(2)} = -\frac{e^2}{2} \int_{-\infty}^{\infty} d^4 \mathbf{x} \int_{-\infty}^{\infty} d^4 \mathbf{y} \mathcal{N} \left( \overline{\psi}(x) \gamma^\mu \overline{A_\mu(x) \psi(x)} \overline{\psi}(y) \gamma^\nu A_\nu(y) \psi(y) \right)$$

where

$$\overline{A_\mu(x) A_\nu(y)} = \langle 0 | \mathcal{T}(A_\mu(x) A_\nu(y)) | 0 \rangle = \cdots = D_{\mu\nu}^F(x - y) = \int_{-\infty}^{\infty} \frac{d^4 q}{(2\pi)^4} D_{\mu\nu}^F(q) e^{-iq(x-y)}$$

with

$$D_{\mu\nu}^F(k) = \frac{-g_{\mu\nu} + r_{\mu\nu}}{(q^2 + i\epsilon)} \quad (2.18)$$

Here we have omitted the mathematical details, but to summarize it with words. We calculated the photon propagator which connects two spacetime points  $\mathbf{x}$  and  $\mathbf{y}$  by calculating the Greens function of the Minkowski space using among other the residue theorem

from complex analysis. If we were now to define  $|e^- e^+\rangle, \langle e^- e^+|, \bar{\psi}$  and  $\psi$  we could directly calculate the scattering amplitude by setting in the values, as this usually involves solving integrals that use Dirac delta function<sup>7</sup>. To complete our example we define

$$|e^- e^+\rangle = (\sqrt{2E_p} a_p^\dagger)(\sqrt{2E_k} b_k) |0\rangle, \quad \text{and} \quad \langle e^- e^+| = (2\sqrt{E_p E_k}) \langle 0| a_p b_k^\dagger$$

where  $E_i$  is the energy of the particle and  $a_i, b_i$  and  $a_i^\dagger, b_i^\dagger$  are creation and annihilation operators, respectively. In general fermion fields have

$$\psi \equiv \int \frac{d^3 p}{(2\pi)^3} \frac{1}{\sqrt{2E_p}} \left( \sum_s a_{\mathbf{p}}^s u^s(p) e^{-ip \cdot x} + b_{\mathbf{p}}^{s\dagger} v^s(p) e^{ip \cdot x} \right) = \psi_p^+ + \psi_p^-$$

Where, depending on  $\psi^+$  (for  $u(p)$ ) and  $\psi^-$  (for  $v(p)$ ) are the particle and antiparticle fields **Is this the real name**, respectively. It is standard convention to say that ingoing particles and anti-particles on an interaction are written as  $\psi^+$  and  $\bar{\psi}^-$ , respectively, and their hermitian conjugate when they are outgoing. With this information we can connect the initial and final particles to their fields, solving the bra we have

$$\langle e^- e^+| \bar{\psi}(x) \psi(x) = (2\sqrt{E_p E_k}) \langle 0| a_p b_k^\dagger \bar{\psi}_{k'}^- \psi_{p'}^+,$$

Giving

$$\langle e^- e^+| \bar{\psi}(x) \psi(x) = \langle 0| \int \frac{d^3 p'}{(2\pi)^3} \int \frac{d^3 k'}{(2\pi)^3} \sqrt{\frac{E_p E_k}{E_{p'} E_{k'}}} \left( \sum_{s,t} a_{\mathbf{p}'}^{\dagger,s} u^s(p') e^{-ip' \cdot x} + b_{\mathbf{k}'}^t \bar{v}^t(k') e^{-ik' \cdot x} \right) a_p b_k^\dagger$$

using the relation  $a_{p's} a_{pt}^\dagger = (2\pi)^2 \delta^{(3)}(p' - p) - a_{p's}^\dagger a_{pt}$  where the latter part kills vacuum, we get

$$\langle e^- e^+| \bar{\psi}(x) \psi(x) = u(x) \bar{v}(x) \langle 0|$$

Doing the same for the ket, and setting all of this into the initial equation we get

$$\langle f| \mathcal{S}^{(n)} |i\rangle = -\frac{e^2}{2} \langle 0| \int_{-\infty}^{\infty} d^4 \mathbf{x} \int_{-\infty}^{\infty} d^4 \mathbf{y} u(x) \gamma^\mu \bar{v}(x) D_{\mu\nu}^F(x - y) \bar{u}(y) \gamma^\nu v(y) |0\rangle$$

Giving us

$$(2\pi)^4 \delta^{(4)}(p_1 + p_2 - p'_1 - p'_2) \bar{v}(p_1) \gamma^\mu u(p_2) \frac{g_{\mu\nu}}{q^2} \bar{u}(p'_1) \gamma^\nu v(p'_2)$$

---

<sup>7</sup>At least while omitting loops, which we will do in this thesis

we can relate the scattering amplitude to a variable called the *transition amplitude*,  $\mathcal{M}_{fi}$  by using

$$\langle f | \mathcal{S} | i \rangle = i(2\pi)^4 \delta^{(4)} \left( \sum_i p_i - \sum_f p_f \right) \mathcal{M}_{fi}$$

Meaning that we have

$$\mathcal{M}_{bhabha} = \bar{v}(p_1) \gamma^\mu u(p_2) \frac{g_{\mu\nu}}{q^2} \bar{u}(p'_1) \gamma^\nu v(p'_2)$$

The reason we did all this is to calculate the *differential cross-section* (in the center of mass frame) from this, using

$$\frac{d\sigma}{d\Omega} = \frac{1}{64\pi^2 s} \frac{p_f^*}{p_i^*} |\mathcal{M}_{fi}|^2 \quad (2.19)$$

where  $p_f^*$  and  $p_i^*$  are the magnitudes of the final- and initial-state momenta, respectively. From the differential cross-section we can also calculate the cross-section by integrating over  $d\Omega$ .

$$\sigma = \int_0^{2\pi} \int_0^\pi \frac{1}{64\pi^2 s} \frac{p_f^*}{p_i^*} |\mathcal{M}_{fi}|^2 \sin \theta d\theta d\phi \quad (2.20)$$

This method is a general way to calculate the cross-section of an event we want to study, but usually one just constructs the matrix element  $\mathcal{M}_{fi}$  from *Feynman diagrams*. In this calculation we already introduced the photon propagator in Eq. (2.18), and we implicitly simplified it to be  $\frac{g_{\mu\nu}}{q^2}$ , which is valid for our purposes, and can be used in any event where the photon is the propagator. Feynman realized this and made Feynman rules to construct diagrams. The rules are shown in Figure 2.1.

Meaning that following these rules we just constructed the Feynman diagram for Bhabha scattering shown in Figure 2.2

### Lowest-order Feynman rules

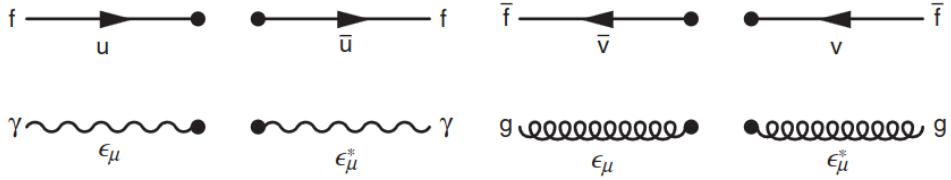
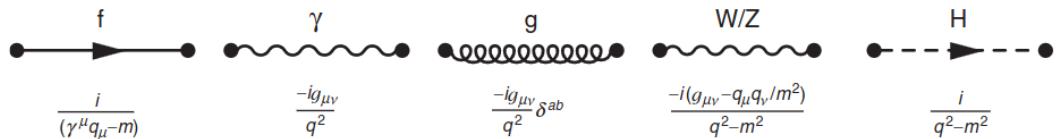
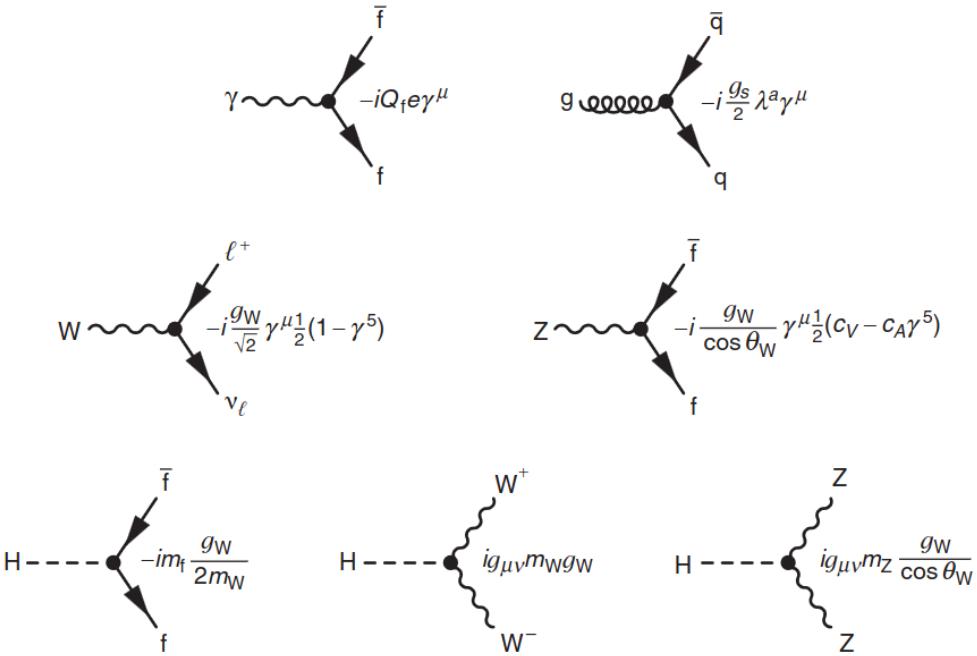
**External particles:**

**Propagators:**

**Three-point vertices:**


Figure 2.1: The Standard Model Feynman rules. Image taken from Thomson's "Modern Particle Physics" [8]

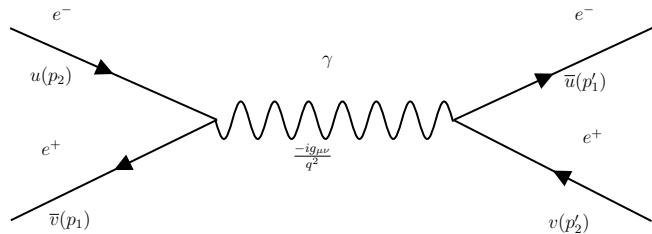


Figure 2.2: Bhabha scattering Feynman diagram

## 2.7 Adding it all up

Combining the three groups  $U(1)_Y \otimes SU(2)_L \otimes SU(3)_C$  as well as introducing the Higgs field from Eq. (2.12) gives us the SM Lagrangian

$$\mathcal{L}_{SM} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + i\bar{\psi}\not{D}\psi + \psi_i y_{ij}\psi_j\phi + h.c. + |D_\mu\phi|^2 - V(\phi)$$

All of this is great at explaining what we know so far, which is depicted in Figure 2.3

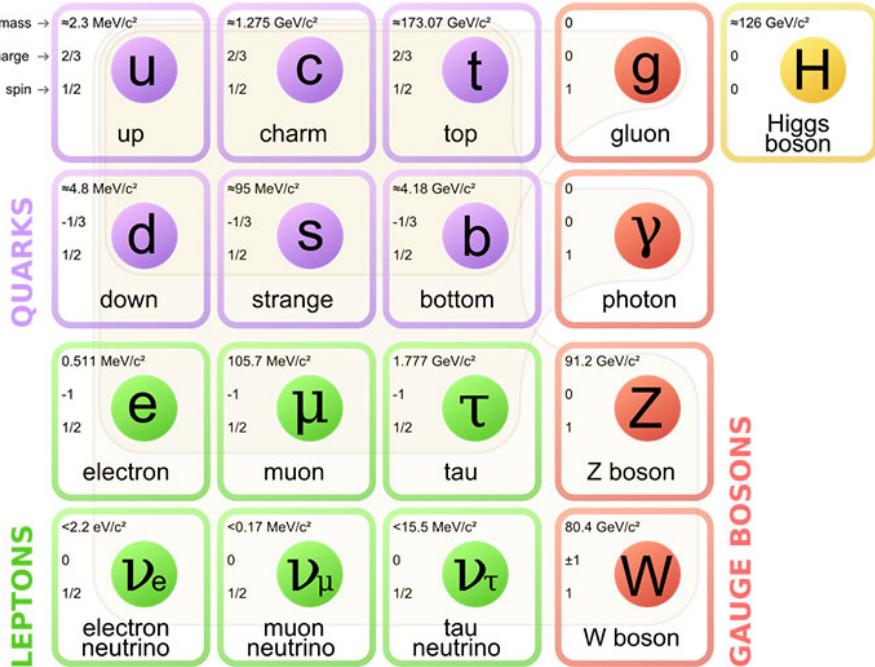


Figure 2.3: The Standard Model of particle physics. Image taken from Wikipedia [[how to cite](#)]

From Figure 2.3 we can see all the particles of the standard model. These include the quarks  $u, d, c, s, t$  and  $b$ , the leptons  $e, \mu$  and  $\tau$  as well as their neutrino partners, the carrier of the strong force  $g$ , the carriers of the weak force  $W^\pm$  and  $Z$ , the carrier of the electromagnetic force  $\gamma$  and the Higgs boson  $H$ . From the figure we can also see which particles can interact with each of the bosons.

These are the building blocks of nature, as mesons, subatomic particles consisting of two quarks, and baryons, meaning subatomic particles consisting of three quarks (such as the proton and neutron) can further build atoms with electrons to furthermore create chemistry via quantum mechanical processes.



# Chapter 3

## Beyond Standard Model Dark Matter

While the standard model of particle physics has been incredibly successful in describing the behavior of subatomic particles, it is not a complete description of the universe. For example, the standard model cannot explain the mysterious gravitational forces that hold galaxies together, and it fails to account for the abundance of matter that we observe in the universe.

These mysteries have led scientists to propose the existence of Dark Matter (DM), a mysterious substance that makes up a significant fraction of the matter in the universe. The name DM comes from the fact that we cannot observe the particles as they do not interact with matter via any of the forces described by the SM. This makes it extremely difficult to detect directly. However, its presence can be inferred through its gravitational effects on visible matter, such as stars and galaxies, which is why we know it is there [10, 11]. In this thesis we will look at so-called Weakly Interacting Massive Particles (WIMP) DM candidates. There is no formal definition of a WIMP, but broadly it is a new elementary particle which interacts via gravity and other forces, potentially outside the SM.

There are several extensions of the SM that include DM candidate particles interacting via a so-called Beyond Standard Model (BSM) Lagrangian. Such as Supersymmetry [6], Universal Extra Dimensions [12] and little Higgs models [13]. In this chapter we will present the BSM models we will be studying that have a dilepton and Missing Transverse Energy final state.

### 3.1 Mono-Z' candidates

Six of the models that will be studied in this thesis come from a new theoretical gauge boson that behaves like the  $Z$  boson. The theory is based on the papers by Bauer et al. [4] which have previously been studied by ATLAS [14] and CMS collaborations [15].

The models we will study assume a  $U(1)'$  symmetry for a new  $Z'$  gauge boson, from this we can extend the SM Lagrangian from Eq. (2.1), to include the  $Z'$  coupling to the SM particles by

$$\mathcal{L} \supset - \sum_q g_q \bar{q} \gamma^\mu q Z'_\mu \quad (3.1)$$

where the couplings are the same as for gauged baryon number  $U(1)_B$  with  $g_q = \frac{g_B}{6}$ . The six models we will study are based on three interactions of this new  $Z'$  (decaying into two leptons) and DM candidates  $\chi$ , which again are divided into a Heavy Dark Sector (HDS) and Light Dark Sector (LDS) based on the mass of the DM candidate, for more information on this and the selection of parameters see Chapter 6.2.

#### 3.1.1 Z' Dark Higgs

A model with a new  $Z'$  naturally comes with a set of scalars responsible for SSB. Because of this, we will look at a new scalar particle that couples to the  $Z'$ , which we will call the Dark Higgs (DH),  $h_D$ . Analogous to the SM process of Higgs-boson radiation from a  $W$  or  $Z$ , the DH is radiated from the  $Z'$  in a dark-Higgsstrahlung process. In addition, we will assume that this DH boson couples with invisible states, such as DM. A minimal model for this process, with the  $U(1)'$  symmetry as well as a  $\Phi_D$  scalar field with an invisible singlet scalar  $\phi_\chi$  can be seen below

$$\mathcal{L} \supset |D_\mu \Phi_D|^2 + \mu_D^2 |\Phi_D|^2 - \lambda_D |\Phi_D|^2 - \frac{1}{4} (F'_{\mu\nu})^2 + \frac{1}{2} (\partial_\mu \phi_\chi) - \lambda_\chi |\Phi_D|^2 \phi_\chi^2 - V(\phi_\chi) \quad (3.2)$$

with the DH field  $\Phi_D = \frac{1}{\sqrt{2}}(v_D + h_D)$  obtaining a vacuum expectation value giving mass to the  $Z'$ ,  $m_{Z'}$ . The coupling of the DH with  $Z'$  is

$$Q_h g_Z m_{Z'} h_D Z'_\mu Z'^\mu \equiv g_{h_D} m_{Z'} h_D Z'_\mu Z'^\mu \quad (3.3)$$

where  $Q_h$  is the charge of the  $\Phi_D$  which is a free parameter. The Feynman diagram for this model can be seen in Figure 3.1

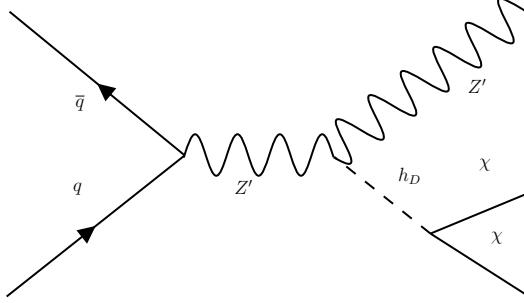


Figure 3.1:  $Z'$  Dark Higgs Model

### 3.1.2 $Z'$ Light Vector

The second mono- $Z'$  model we will look at, is when the  $Z'$  is relatively light such that it can be produced in the decay of a DM state. As an example we can consider a  $Z'$  coupled to a new fermion which has both Dirac and Majorana masses,  $M_d$  and  $M_m$  respectively. Where the Majorana mass can be generated from the  $U(1)' h_D$  through a  $y_\chi \Phi_\chi \bar{\chi} \chi^c$ , such that

$$\mathcal{L} \supset \bar{\chi}(i\cancel{D} - M_d)\chi - \frac{M_m}{2}(\bar{\chi}\chi + h.c)$$

This leads to two Majorana states  $\chi_{1,2}$  with masses  $M_{1,2} = |M_m \pm M_d|$ . We will study the process  $Z' \rightarrow \chi_1 \chi_2$ , where  $\chi_2 \rightarrow Z' \chi_1$ . This model can be seen in Figure 3.2

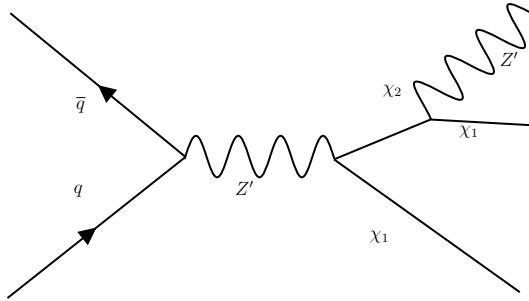


Figure 3.2:  $Z'$  Light Vector Model

Where it is assumed the mass splitting of the two states,  $\chi_{1,2}$ , is larger than  $m_{Z'}$ , such that the heavier state,  $\chi_2$  can decay into an on-shell  $Z'$  and a stable DM candidate  $\chi_1$ . The  $\chi_{1,2}$  interaction with the  $Z'$  is off-diagonal, and taking  $M_m > M_d$  we can write the interaction

$$\frac{g_\chi}{2} Z'_\mu (\bar{\chi}_2 \gamma^\mu \gamma^5 \chi_1 + \bar{\chi}_1 \gamma^\mu \gamma^5 \chi_2) \quad (3.4)$$

### 3.1.3 $Z'$ Effective Field Theory

The aforementioned models rely on the  $Z'$  coupling to the quarks as seen in Eq. (3.1). In the third model we do not assume anything about the couplings, and rather than producing the DM candidates through the new  $Z'$ , we consider the possibility that the DM states are produced through a new constant interaction:

$$\frac{1}{2\Lambda^2} \bar{q}\gamma_\mu q (\bar{\chi}_2 \gamma^\mu \gamma^5 \chi_1 + \bar{\chi}_1 \gamma^\mu \gamma^5 \chi_2) \quad (3.5)$$

Similarly to the Light Vector model we assume two DM states  $\chi_{1,2}$  with an off-diagonal coupling to the  $Z'$ , however, the intermediate  $s$ -channel of the  $Z'$  has effectively been replaced with a heavy  $Z'_H$ . Where  $Z'_H$  has been integrated to give the operator from Eq. (3.5). The process can be seen in Figure 3.3.

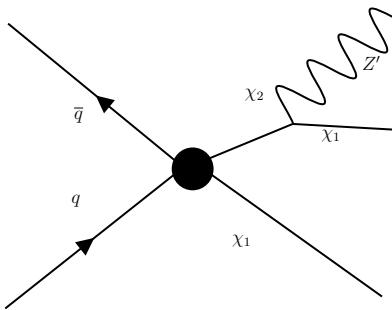


Figure 3.3:  $Z'$  Effective Field Theory Model

## 3.2 Supersimmetree

This section might be removed if we do not test any SUSY samples.

# Chapter 4

## Production, Detection and Analysis

Now that we have established the necessary theoretical groundwork of particle physics in Chapter 2 and explored our DM candidates in 3, it is time to explore how this knowledge can be applied. This leads us to ask important questions such as, how can we measure what we have learned? How do we put it into practice? Most importantly, how can we use this knowledge to uncover new physics phenomena?

To answer these questions, we have divided this chapter into three sections, each of which will focus on a different aspect of experimental particle physics. The first section will delve into particle production, followed by an examination of particle detection with the ATLAS detector at the LHC, and finally, we will explore the intricacies of data analysis in particle physics.

## 4.1 Particle production

Having already been introduced to the SM we are now ready to dive into the subject of how we can produce the particles that we wish to detect. In this chapter we will start from the basic kinematics of particles and then move to more complex variables that will be of use when analyzing data from detectors. The material for the first section is based on Thomson's book Modern Particle Physics [8], Jacksons' "Kinematics" [16] and Vadla's PhD. thesis [17].

### 4.1.1 Particle kinematics

When working on a relativistic setting, such as we do in high energy particle physics, four vectors are the natural object to consider to generally describe our particles. As we are mainly interested in the motion of the particles, we will look at the four-momentum. Instead of using general variables, we will describe the particles using the four-momentum in terms of the geometry of the detectors (See Chapter 4.2), that means we will use the polar angle,  $\theta$ , and the azimuthal angle,  $\phi$ , such that we have

$$p^\mu = (E, p_x, p_y, p_z) \xrightarrow{Lab} (E, p_T \cos \phi, p_T \sin \phi, |\mathbf{p}| \cos \theta) \quad (4.1)$$

where  $p_T$  is the *transverse momentum* expressed as

$$p_T \equiv \sqrt{p_x^2 + p_y^2} = |\mathbf{p}| \sin \theta \quad (4.2)$$

Where the relativistic energy and momentum are given as,  $E = \gamma\beta$  and  $\mathbf{p} = \gamma m\beta$ , with  $\gamma = 1/\sqrt{1 - \beta^2}$  and  $\beta = \mathbf{v}/c$ <sup>1</sup> where  $m$  is the mass of the particle and  $c$  is the speed of light in vacuum. By contracting<sup>2</sup> two four-momenta we get the important Lorentz invariant square of the *invariant mass*

$$m^2 = p_\mu p^\mu = E^2 - |\mathbf{p}|^2$$

---

<sup>1</sup>As this is a particle physics thesis I will convert to Natural Units where we set  $c = 1$

<sup>2</sup>Using the particle physicists convention of the Minkowski metric tensor  $\eta_{\mu\nu}, (+, -, -, -)$

which can be generalized for a system containing  $n$  particles as

$$m^2 = p_\mu p^\mu = \left( \sum_{i=1}^n E_i \right)^2 - \left( \sum_{i=1}^n \mathbf{p}_i \right)^2 \quad (4.3)$$

As this thesis will focus on a dilepton (and missing transverse energy) final state, which is of the type  $2 \rightarrow 2$  (+MET) then the invariant mass of the two leptons in the final state will be of interest, we will denote this as  $m_{ll}$ . From this we can also get another interesting variable, the *transverse energy*. This follows directly from Eq. (4.3)

$$E_T = \sqrt{m^2 + p_T^2} \quad (4.4)$$

The invariant mass is what we measure in the final state only. As we analyze data<sup>3</sup> from Run II on LHC, which operated at  $\sqrt{s} = 13$  TeV, it is important to consider the determination of the center-of-mass energy, which characterizes the initial state of the colliding protons. While the LHC controls the initial state, it is crucial to understand that the 13 TeV energy value associated with the incoming protons does not directly define the center-of-mass energy of the initial state. Instead, it is the partons, primarily gluons but also including quarks, that contribute to the center-of-mass energy. These partons have the ability to possess any collision energy below 13 TeV. The momentum fractions of the partons are determined by the product of the invariant mass and the pseudorapidity ( $m/\eta$ ) of the final state particles, for more info on partons see Chapter 4.1.2.

The aim of this thesis is to search for DM, which we know interacts weakly with matter in the same way as neutrinos, meaning it leaves no signal in detectors. So how can we detect its presence? As we know that the transverse momenta before a particle collision is zero<sup>4</sup>, then we know that the sum of transverse momenta must be zero after the collision as well, to conserve momentum. From this we often can infer the presence of the non-interacting particles from the presence of *missing transverse energy*<sup>5</sup> (MET), which

<sup>3</sup>And mostly simulations mimicking the ATLAS detector

<sup>4</sup>Because protons travel along the beam axis on our coordinates

<sup>5</sup>Also called *missing momentum*. While energy is a scalar quantity without direction, we use the term "missing transverse energy" to emphasize the magnitude of the missing transverse momentum vector. This convention is adopted due to the nature of our energy measurements in calorimeters, which actually gives us directions

is defined by

$$E_T^{miss} = \mathbf{p}_{miss} \equiv - \sum_i \mathbf{p}_{T,i} \quad (4.5)$$

where the sum extends over the measured momenta of all the observed particles in an event, as well as all the tracks which are reconstructed, but not associated with any particle<sup>6</sup>. From this formula, if all particles produced in the collision have been detected, then this sum should be zero. Meaning that significant MET is an indicative of the presence of undetected particles.

Another useful kinematic variable is the *hadronic activity* which is the scalar sum of the transverse momentum of all jets in an event, defined as

$$H_T = \sum_{i \in \{jets\}} ||\mathbf{p}_{T,i}|| \quad (4.6)$$

This gives a measurement of the hadronic energy scale of an event. Another handy trick comes from the realization that the centre-of-mass frame is between the hadrons, where the total momentum is given as a function of the energy of the hadron. This means that the final state particles are boosted along the beam axis. With this realization we can now introduce a Lorentz invariant<sup>7</sup> kinematic property known as the *rapidity*,  $y$  used to express the lepton angles

$$y \equiv \frac{1}{2} \ln \left( \frac{E + p_z}{E - p_z} \right) \quad (4.7)$$

We can use that  $p_Z = E \cos \theta$  in the high-energy limit as the mass is negligible. In this limit we can use the *pseudorapidity*,  $\eta$ , defined by

$$\eta \equiv -\ln \left( \tan \frac{\theta}{2} \right) \quad (4.8)$$

The pseudorapidity is an interesting variable as, in the same was as  $\theta$ , it can tell us how close to the beam the final state particles are<sup>8</sup>, but this time independently of the boost as it does not include the mass of the particle. The pseudorapidity also gives us that for a single particle the phase space is uniformly distributed on  $(\eta, \phi)$ -space. This variable can also be negative, meaning it is boosted along the other beam direction. From this

<sup>6</sup>Referred to as *soft terms*

<sup>7</sup>Under boosts along the beam axis

<sup>8</sup>Where the higher  $|\eta|$  means closer to the beam

we can define a new variable which will come handy with particle identification, which is called the *R-cone*, that defines a circle in  $(\eta, \phi)$ -space surrounding the object of interest. It is defined as

$$\Delta R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2} \quad (4.9)$$

Another interesting variable is the *transverse mass*, defined as

$$m_T^2 = m^2 + p_T^2 \quad (4.10)$$

where  $m^2$  is the invariant mass defined in Eq. (4.3). What is interesting about this variable is that it is a generalization of the invariant mass in the transverse plane and can thus accommodate the MET coming from invisible particles. We can take this further by looking at a variable which calculates a transverse mass for two leptons by distributing the total  $p_T^{miss}$  among the two systems, and minimizing the maximum of the two transverse masses by varying the distribution of the  $p_T^{miss}$ -vector in terms of the size of  $p_T$ . This is called the *stransverse mass* and is defined by

$$m_{T2}^2(\chi) = \min_{\mathbf{q}_T^{(1)} + \mathbf{q}_T^{(2)} = \mathbf{p}_T} \left[ \max \left\{ m_T^2 \left( \mathbf{p}_T^{\ell_1}, \mathbf{q}_T^{(1)}; \chi \right), m_T^2 \left( \mathbf{p}_T^{\ell_2}, \mathbf{q}_T^{(2)}; \chi \right) \right\} \right] \quad (4.11)$$

where  $\mathbf{q}_T$  are "dummy 2-vectors",  $\chi$  is a free parameter used to "guess" the mass of the invisible particle, and  $m_T^2(\mathbf{p}_T, \mathbf{q}_T)$  is an application of Eq. (4.10) using two particles:

$$m_T^2(\mathbf{p}_T, \mathbf{q}_T) = 2(p_T q_T - \mathbf{p}_T \cdot \mathbf{q}_T)$$

For a more detailed explanation and interpretation of the stransverse mass we refer the reader to the paper by Barr et al. [18]. Even though the stransverse mass was made with neutralinos in mind, it can still be used to calculate SM processes. For example, if we want to reduce  $WW$  background events, we can first recall that each boson can decay as  $W \rightarrow l + \nu_l$  with the  $W$  mass as an endpoint. Meaning that we can use  $m_{T2}$  to reduce the  $WW$  events in a dilepton final state by requiring that  $m_{T2} > m_W$ .

### 4.1.2 Proton-proton collisions

With all the kinematics out of the way the question of how the particles are produced still remains. The answer could be an electron positron collider, as they did in LEP, a proton anti-proton collider, like the SppS. As this thesis uses LHC data we will look at proton-proton collisions. The reason as to why this works is that protons are also made of elementary particles, two *up* and one *down* to be specific. Because of this it is not hard to realize that the Feynman rules acquired from the SM (Chapter 2) also apply here. In this subsection we will study how different effects of  $pp$ -collisions affect the cross-section, and therefore the expected number of events to occur, from a kinematical point of view.

### Parton Distribution Functions

Although the proton is made up for two up quarks and one down quark, called the *valence quarks*. The proton also consists of gluons and other quarks, called partons. These partons become important in deep inelastic scatterings, where the proton breaks apart due the high energies in the collisions. As we accelerate the protons before colliding them, we also accelerate the quarks and gluons inside it, each of the quarks carry a momentum fraction  $x$ , called the Bjorken  $x$ . We can then calculate the invariant mass of two colliding partons  $q_1$  and  $q_2$ , with the momentum fraction  $x_1$  and  $x_2$ , from the proton's momentum  $p_1$  and  $p_2$  respectively as

$$m^2 = x_1 x_2 s$$

where  $s$  is the centre-of-mass energy squared of the  $pp$ -system. The valence quarks in the proton do not only interact with the other valence quarks in the other proton, but they might also emit gluons which decay into quark anti-quarks pairs, making a “sea” of gluons and quarks around the valence quarks. The momentum of the partons inside the proton are dependent on the momentum transfer  $Q^2$  and is represented by an experimentally determined momentum distribution, known as the *parton distribution function* (PDF) [19]  $f(x, Q^2)$ . **Question: Should I say more about PDFs than this? I feel like it is not relevant for my thesis, but is still good to know.** In other words, the PDFs give the probability of a parton to collide with the momentum fraction  $x$ . The shape and form the PDFs play an important role of estimating the processes that occur after the proton collisions, and therefore are crucial when simulating events using Monte Carlo

[20]. If we take as an example the process  $pp \rightarrow l^+l^- + X$  where  $X$  denotes any hadrons formed by the remaining quarks. Figure 4.1 showcases the process.

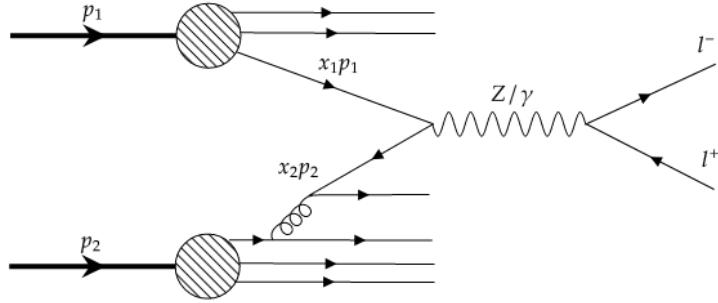


Figure 4.1: Feynman diagram depicting the  $pp \rightarrow l^+l^- + X$  process where  $X$  denotes any hadrons formed by the remaining quarks not taking part in the  $q\bar{q}$ -collision carrying  $x_1$  and  $x_2$  momentum from the protons  $p_1$  and  $p_2$  respectively

The cross-section for the process is

$$\sigma(p(p_1)p(p_2) \rightarrow l^+l^- + X) = \int_0^1 \int_0^1 \sum_f f_f(x_1) \bar{f}_f(x_2) \cdot \sigma(q_f(x_1 p_1) + \bar{q}_f(x_2 p_2) \rightarrow l^+l^-) dx_2 dx_1 \quad (4.12)$$

where  $\sigma(q_f(x_1 p_1) + \bar{q}_f(x_2 p_2) \rightarrow l^+l^-)$  is calculated using the rules explained in Chapter 2, and  $f$  are the PDFs. As we can see this can drastically change the cross-section, and with that the probability, for an event we want to study.

### Breit-Wigner resonance

Another important aspect when looking at particle collisions is the *Breit-Wigner resonance*. All unstable particles have a decay rate,  $\Gamma$ , (given as inverse of the lifetime  $\tau$ ) which is present in the wave function,  $\Psi \propto e^{-i(m-i\Gamma/2)}$ . This decay rate also becomes apparent when the unstable particle is the propagator of an event we are studying

$$\sigma \propto \frac{1}{(s - m^2)^2 - m^2 \Gamma^2} \quad (4.13)$$

From this we can see that as the square of the centre-of-mass energy  $s$ , approaches the unstable particles mass  $m$ , there will be a resonance at the invariant mass of the unstable particle, this is called the Breit-Wigner resonance. It is because of resonances like this that we can identify particles such as the  $Z$  boson. This resonance will also be present

when studying some BSM DM models in this thesis.

**Question: should I cite the original paper or Z discovery?**

### Expected events

The most important value we need to know when studying  $pp$ -collisions is the number of interactions taking place, this is defined as

$$N = \sigma \int \mathcal{L}(t) dt, \quad \text{where } \mathcal{L} = f \frac{n_1 n_2}{\sigma_x \sigma_y} \quad (4.14)$$

where  $\sigma$  is the cross-section of the interaction as expressed in Eq 2.20 while also taking into account the effects from Eq. (4.12) and Eq. (4.13). The last three symbols come from accelerator kinematics where  $\sigma_{x,y}$  denotes the beam size,  $f$  is the frequency of bunch crossings, and  $n_{1,2}$  is the number of particles in bunches.

## 4.2 The ATLAS detector

We have so far on this chapter discussed how particles are produced. But we so far not yet explained how we actually detect them, arguably the most important matter in the field of high energy particle physics. This section of the chapter is just about that, and we will explain how the detection happens in A Toroidal LHC ApparatuS, or more commonly known as the ATLAS detector. Figure 4.2 showcases the detector and its size. The information of this section is largely based on the original ATLAS Collaboration introduction paper presented to CERN [21].

The ATLAS detector is a general multipurpose<sup>9</sup> detector located at the LHC and covers nearly the entire solid angle around the collision point, as described with the  $(\eta, \phi)$ -coordinates in Section 4.1.1. The ATLAS detector consists of four main subdetectors; (i) an inner tracking detector (ID), an (ii) electromagnetic calorimeter (ECAL), and a (iii) hadronic calorimeter (HCAL), and lastly (iv) a muon spectrometer (MS). Figure 4.3 visualizes the four (i) – (iv) main sub-detectors, along with how the different particle types interact with each layer. A brief description of each layer is explained in this section.

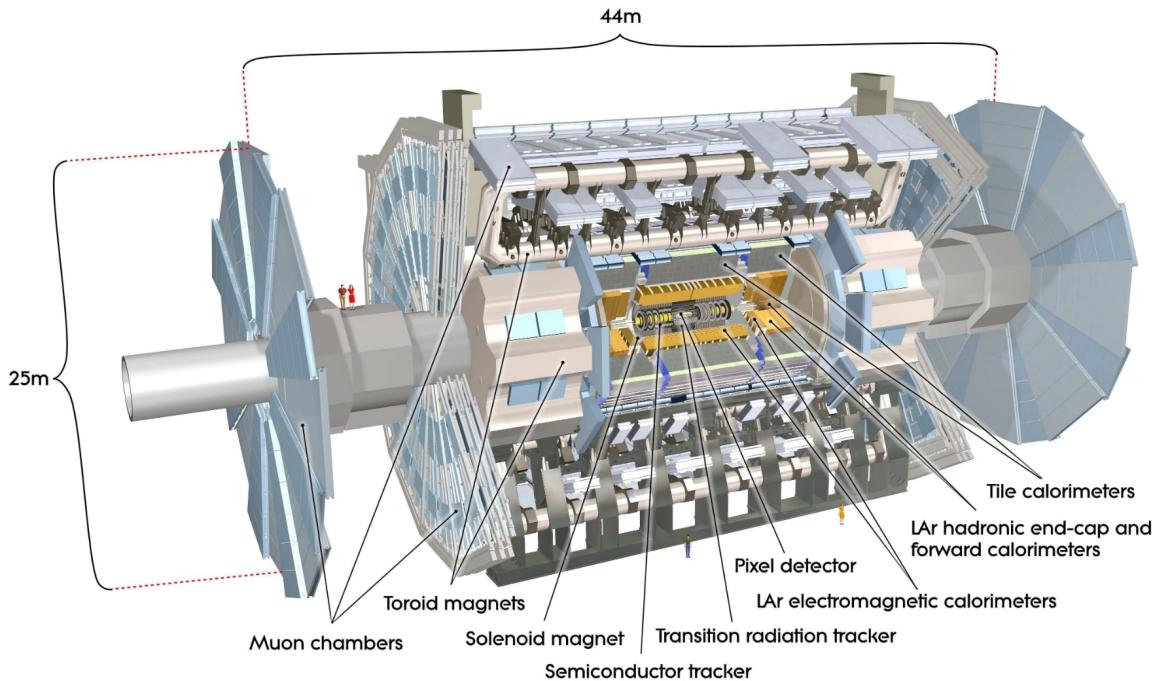


Figure 4.2: Cut-away view of the ATLAS detector, image taken from Ref. [21]

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<sup>9</sup>Probing  $pp-$  and  $AA-$  (heavy ions) collisions.

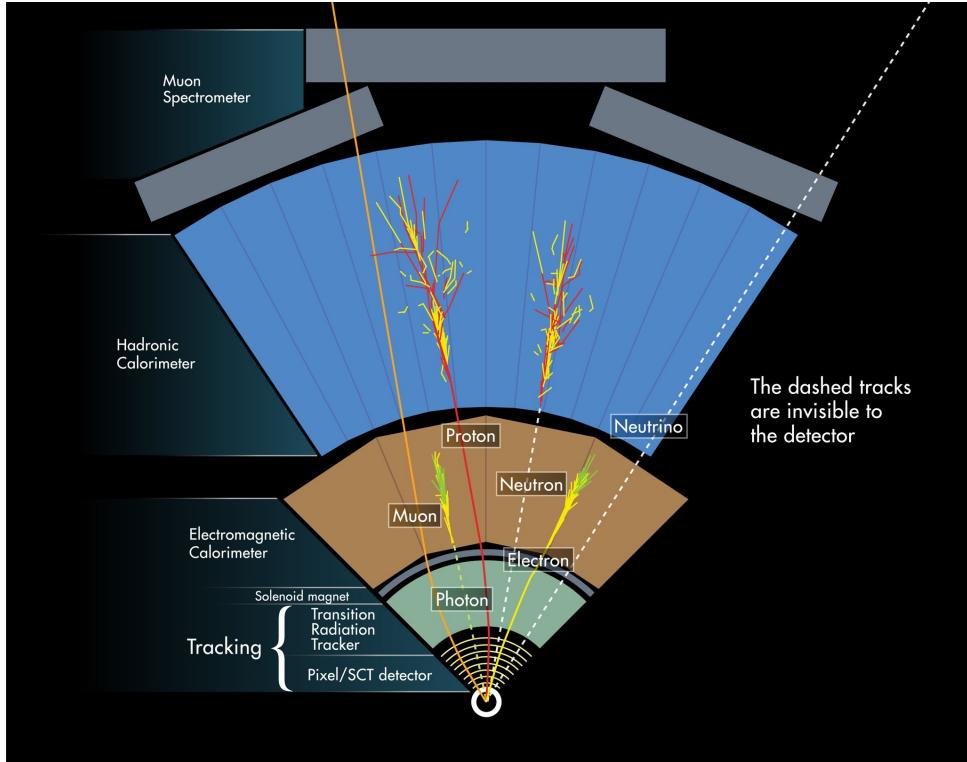


Figure 4.3: Illustration of the ATLAS detector layers, image taken from Ref. [22]

#### 4.2.1 Inner detector

The inner-detector (ID) system is immersed in a 2T axial magnetic field and provides charged-particle tracking in the range  $|\eta| < 2.5$ . The ID provides the first measurements of the momentum and identification of electrically charged particles, as these can be determined by the curvature of their reconstructed tracks. The ID is made of three independent systems; the pixel detector, the semiconductor tracker (SCT) and the transition radiation tracker (TRT).

The pixel detector is made up of 80 million silicon pixel sensors, each of size  $50 \times 400 \mu\text{m}^2$ , and spread over multiple layers. Outside the pixel layers are the SCTs, which consist of silicon microstrips trackers, also placed on multiple layers. The SCT covers the pseudo-rapidity region  $|\eta| < 2.5$ . Furthest away from the interaction point lies the TRTs, they consist of 4 mm in diameter straw tubes, which enables track-following up to  $|\eta| = 2.0$ .

### 4.2.2 The calorimeters

The ATLAS detector has two types of calorimeters, the *electromagnetic calorimeter* (ECAL) and the *hadronic calorimeter* (HCAL), both designed to fully stop certain types of particles. Both calorimeters covers a pseudorapidity range  $|\eta| < 4.9$ . The ECAL is immediately surrounding the inner detector and is divided into a barrel part ( $|\eta| < 1.475$ ) and two end-cap components ( $1.375 < |\eta| < 3.2$ ). The ECAL consists of absorbing lead plates, with liquid Argon (LAr) in between. The thickness of the calorimeter is made to fully measure the shower of photons and electron/positrons. The muons will only lose a small fraction of their energy as they have longer interaction lengths with lead.

The HCAL is immediately surrounding the ECAL on all sides and consists of two types of detectors. In the barrel ( $|\eta| < 1.0$ ) and the extended barrel regions ( $0.8 < |\eta| < 1.7$ ), the HCAL is made of steel plates with plastic scintillator tiles as active material. While on the end-cap regions ( $1.5 < |\eta| < 3.2$ ) there are hadronic LAr detectors, with absorbing copper plates as active material; in the forward region ( $3.1 < |\eta| < 4.9$ ) a combination of copper and tungsten plates are used as active material. The active materials are chosen to maximize the interaction cross-section with hadrons, such as neutrons, protons and pions. The depth of the HCALs is also designed to fully stop the particles and their showers in order to measure their total energies. Hadrons are efficiently stopped at the HCALs, meaning that only muons and invisible particles, such as neutrinos and potentially dark matter, leave the HCAL.

### 4.2.3 Muon spectrometer

The outermost layer of the ATLAS detector is the *muon spectrometer* (MS), dedicated to the measurement of the muons momenta. The MS, similar to the ID, consists of multiple layers of detector material, and is immersed in a strong magnetic field to bend the trajectories of the charged muons. The MS is made of four different types of detector component: (i) Monitored Drift Tubes (MDTs) on the barrel, (ii) Cathode Strip Chambers (CSCs) dealing with the events closer to the beam line in the end cap, (iii) Resistive Plate Chambers (RPCs) in the barrel and (iv) Thin Gap Chambers (TGCs) in the end caps. The MDTs and CSCs are used for tracking while the RPCs and TGCs are used for

triggers. The tracking is provided for pseudorapidities up to  $|\eta| < 2.7$ , and the trigger system only extends to  $|\eta| < 2.4$ .

#### 4.2.4 Summary of ATLAS

**Question: should I remove this summary or maybe combine it with the summary on Section 4.4?**

The main four parts of the ATLAS detector; *inner-detector* (ID), *electromagnetic calorimeter* (ECAL), *hadronic calorimeter* (HCAL), and the *muon spectrometer* (MS), have briefly been explained. For an easier understanding on the different parts I refer the reader to Figure 4.3 which shows visually how different particles interact with the detector. We can start by noting that there are only three types of particles that interact with the ID, muons, protons and electrons (there might also be other electrically charged hadrons that interact with the ID). From the ID pixel and SCT detectors we can get information about  $\phi, \eta, p_T$  and from the TRT we can get to know the *charge* of the particles (depending on how the magnet bends their trajectories)<sup>10</sup>. Going to the next layer we see that in the ECAL the electron is completely stopped, such that we can know its energy,  $E$ . We can also note that the photons will interact with matter here and also be completely stopped. It is worth noting that in just the two first detector parts we have all the information we need to calculate interesting kinematic variables for the electron and photons. Going further into the detector, we see that the HCAL completely stops the proton and that now the detector interacts with the neutrons, giving us information about their energies (and location for neutrons). Lastly we see that the muon flies through all of this and finally hits the MS where we can get information about its energy. **Note/Question to Farid/Eirik: Why does it not stop?**

The noteworthy particle in Figure 4.3, which was not mentioned in the summary above either, is the *neutrino*. The reason for this is that the neutrino, just like DM, is an *invisible particle*, meaning that it does not interact with matter. We can still reconstruct information about the neutrino and DM however, we do this as explained in Section 4.1.1 with variables such as the MET, Eq. (4.5), as we know the centre-of-mass energy that

---

<sup>10</sup>So as we know that the proton is positively charged, then we know that the muon and electron in Figure 4.3 have negative charge

went into the collision.

Another thing to add is that the explanation of the detector is brief in this thesis. The reality is much more complicated than this as there are, i.e. *triggers* (which might be excluding DM events) choosing which events are "important enough to record" as the *hardware and data storage* is a big problem considering the magnitude of events that happen each second. There are as well as algorithmic procedures to calculate the variables aforementioned from the detector signal which both consume energy and time. As this is not the focus of my thesis I will refer the reader to further literature explaining the real hardships when collecting data at the ATLAS detector and other LHC projects. [23]

***Question: Is it okay for me to do this and move on? Or should I write about this?***

## 4.3 Data analysis

The time has come to explore how we can search for new physics phenomena, now that it has been established how particles are produced and how we detect them. In this section we will take into account the classic way of searching for new physics which is called the *cut and count method*, but there are other methods to search for new physics, such as Machine Learning (ML) which is the method pursued in this thesis. There might be other methods, such as Quantum ML, but as of today we are still in an early stage of the technology [24] **Can I include this?**. To give a short description of the cut and count method, it makes kinematical *cuts* such that we isolate signal from background. The way the signal and background are made is by Monte Carlo (MC) simulations, such that we can more easily identify SM background from DM and then compare our results with real data. As it wouldn't be a real experimental physics discovery without making a statistical analysis of the results we will also explain how we utilize this tool. To guide us through this process I will use  $ZZ^{(*)}$  channel in the discovery of the Higgs Boson in 2012 [1] as an example of the success of this method.

### 4.3.1 Cut and count method

The cut and count method is what is currently the standard method of doing data analysis with CERN related research<sup>11</sup>. As the name implies, the cut and count method works by making cuts on kinematical variables and afterwards counting how many events are left. The goal of using this method is to make cuts such that we remove as many background events as possible while also keeping as many signal events as possible. For example, if we were to study a new physics model with a new light vector boson behaving similarly to the  $Z$  boson, but with a higher mass, then a good kinematical cut to remove many background processes would be to require that  $m_{ll} > 100$  GeV, as this would remove the majority of  $Z$ -resonance from the final state, making it easier to "find" the new physics model.

To more thoroughly explore the cut and count method we can look at the Higgs discovery, in particular the  $H \rightarrow ZZ^{(*)} \rightarrow 4l$ <sup>12</sup> channel. In section 4.1 of the original article

<sup>11</sup>This standard method is shifting towards machine learning

<sup>12</sup>Where  $l$  is for lepton, but only means  $e^\pm$  or  $\mu^\pm$ . *Question: should i explain why not  $\tau$ ?*

[1] there is something called *event selection*. The event selection are the kinematical cuts used. The kinematical cuts used in the article, aside from the *standard selection criteria* (see Chapter 6.3), were:

- Single-lepton or dilepton triggers
- Four leptons on final state with  $p_T > 20, 15, 10, 7$  GeV, in the order of most energetic to least
- Higgs-boson candidates are formed by selecting two same flavor opposite charge lepton pairs

The first "cut" is to make sure that we have leptons on both the data and simulations. The second cut is that there needs to be four leptons, with different  $p_T$  cuts to remove background while keeping as much signal as possible. And lastly we want to have two lepton pairs of the same-flavor with opposite-charge, this is to make sure that the leptons that we observe actually decay from  $Z$ -bosons. What now remains is to explore the "count" part of this method. When counting the events that pass the event selection one usually counts the background events that pass, the data points that pass, and also the signal events that pass. For the 2012 Higgs discovery, the Higgs channel with a Higgs mass of 125 GeV was used as signal. The results of the 2012 discovery is shown Figure 4.4.

Although this section made the process look simple, it was through the effort of many scientists working together that made this happen. The great computational power needed to *correctly* simulate events and reconstruct objects from detector signal was, and still is a big challenge. Not to mention the state-of-the-art technology to be able to both accelerate the protons to an energy high enough to "create" new physics, and to actually be able to detect it. But this alone was not enough to claim the discovery, as we're physicist we need to be completely sure that what we show is true. We do this with statistics which is the next section.

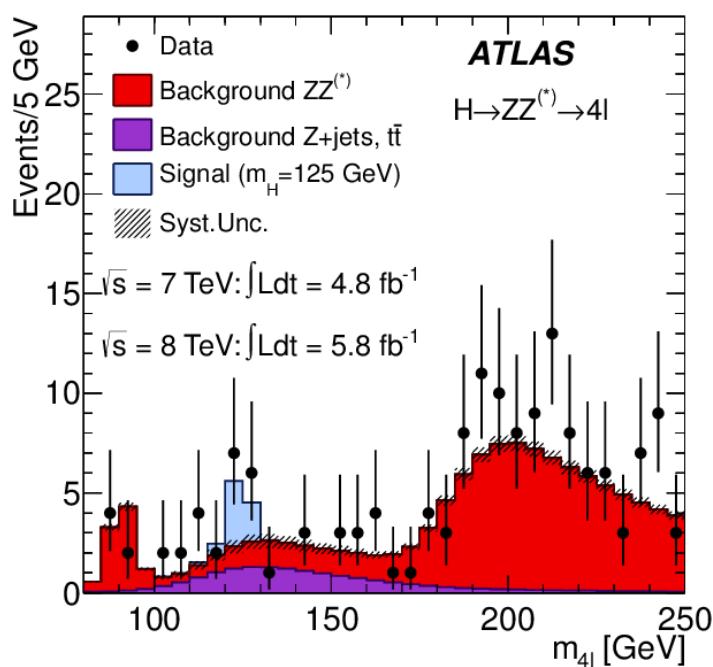


Figure 4.4: The Higgs discovery on the  $ZZ^{(*)}$  channel, image taken from Ref. [1]

### 4.3.2 Statistical tools

To make any sort of claim in modern physics we should be absolutely certain that what we are claiming is true, as just making the cuts and isolating a signal to background is not enough. To be specific we need to be *at least  $5\sigma$  sure* to claim any new discoveries. But as not everything in experimental high energy particle physics is a new discovery, but is in fact for the most part *exclusions*. Then we need to explain what an exclusion is, and how to make them.

This thesis is following Bugge's lecture notes on statistics [**Question: how do I cite his powerpoint from FYS5555**] and the example set by the ATLAS Collaboration article "Search for new particles in events with one lepton and missing transverse momentum in pp collisions at  $\sqrt{s} = 8$  TeV with the ATLAS detector" [25], where a Bayesian analysis is performed to set limits on the studied processes. Using the signal+background hypothesis, the expected number of events in each channel of a process we are studying is

$$N_{\text{exp}} = \varepsilon_{\text{sig}} L_{\text{int}} \sigma B + N_{\text{bkg}}$$

where  $L_{\text{int}}$  is the integrated luminosity,  $\varepsilon_{\text{sig}}$  is the signal selection efficiency defined as the fraction of signal events that satisfy the event selection criteria,  $N_{\text{bkg}}$  is the expected number of background events, and  $\sigma B$  is the cross-section times branching ratio of the process. Using Poisson statistics, the likelihood to observe  $N_{\text{obs}}$  events is

$$\mathcal{L}(N_{\text{obs}}|\sigma B) = \frac{(N_{\text{exp}})^{N_{\text{obs}}} e^{-N_{\text{exp}}}}{N_{\text{obs}}!} \quad (4.15)$$

We include uncertainties by introducing nuisance parameters  $\theta_i$ , each with a probability density function  $g_i(\theta_i)$ , and integrating the product of the Poisson likelihood with the probability density function. The integrated likelihood is

$$\mathcal{L}_B(N_{\text{obs}}|\sigma B) = \int \mathcal{L}(N_{\text{obs}}|\sigma B) \prod g_i(\theta_i) d\theta_i \quad (4.16)$$

where a log-normal distribution is used for the  $g_i(\theta_i)$ . The nuisance parameters are taken to be:  $L_{\text{int}}$ ,  $\varepsilon_{\text{sig}}$  and  $N_{\text{bkg}}$ , with the appropriate correlation accounted for between the first and the third parameters. The measurements of the two decay channels (muon or

electron final state for  $H \rightarrow lll'l'$ ) are combined assuming the same branching fraction for each, thus Eq. 4.16 remains valid with the Poisson likelihood replaced by the product of the Poisson likelihoods for the two channels. The integrated luminosities for the electron and muon channels are fully correlated. We can further use Bayes' theorem which gives the posterior probability that the signal has signal strength  $\sigma B$ :

$$P_{\text{post}}(\sigma B | N_{\text{obs}}) = N \mathcal{L}_B(N_{\text{obs}} | \sigma B) P_{\text{prior}}(\sigma B) \quad (4.17)$$

where  $P_{\text{prior}}(\sigma B)$  is the assumed prior probability, here chosen to be flat in  $\sigma B$ , for  $\sigma B > 0$ . The constant factor  $N$  normalizes the total probability to one. The posterior probability is evaluated for each mass and decay channel as well as for their combination, and then used to set a limit on  $\sigma B$ .

As we can see, the inputs for the evaluation of  $\mathcal{L}_B$  (and  $P_{\text{post}}$ ) are  $\varepsilon_{\text{sig}}$ ,  $L_{\text{int}}$ ,  $N_{\text{bkg}}$  and  $N_{\text{obs}}$  and the uncertainties of the first three. The uncertainties for these should account for experimental and theoretical systematic effects as well as the statistics of the simulated samples. For this thesis the systematic uncertainties will not be calculated, but will rather be assumed to be  $\pm 30\%$  of the background, as this is roughly the standard value of ATLAS papers.

To make exclusions we can use Eq. (4.17) to establish a *confidence limit* (CL). CLs are defined as the probability to observe the number of events observed in an experiment,  $N_{\text{obs}}$ , or *less* given signal+background. We usually define a signal+background hypothesis to be excluded when  $\text{CL}_{s+b} < 5\%$ . Meaning a 95% CL. Such that the probability to falsely exclude an existing signal(+background) is 5%. The standard practice in particle physics when using CL is to *set limits* on theoretical models, rather than exclude them.

On the other side, to claim any discovery in particle physics we need to know the *significance* of any statistical fluctuation. Before getting to the significance we can discuss the *p-value*, defined as the probability to observe the number of events observed in the

experiment,  $n_{\text{obs}}$ , or *more* given only background

$$p = P(N \geq N_{\text{obs}} | \lambda = N_{\text{bkg}}) = \sum_{k=N_{\text{obs}}}^{\infty} \mathcal{L}(k | N_{\text{bkg}}) \quad (4.18)$$

The smaller the  $p$ -value, the less compatible an observation is with the background only hypothesis, meaning more likely to be a discovery. From this we can find the significance  $Z$  by

$$p = \int_{-\infty}^{-Z} \frac{e^{-x^2/2}}{\sqrt{2\pi}} dx$$

As mentioned in the start of this subsection, a discovery in particle physics is defined to be at least a  $Z = 5\sigma$  deviation from the background hypothesis, meaning that we would have a  $p$ -value of  $p \leq 2.87 \times 10^{-7}$ . In other words, with a  $5\sigma$  deviation, the probability to falsely discover something is at worst one in roughly 3.5 million.

As the significance is an interesting quantity we can give it its own definition. In this thesis we will use the low statistics formula for the significance, as this is the most general one. We can either define the significance as the *observed significance* by

$$Z = \sqrt{2 \left[ N_{\text{obs}} \ln \frac{N_{\text{obs}}}{N_{\text{bkg}}} - N_{\text{obs}} + N_{\text{bkg}} \right]} \quad (4.19)$$

or as the *expected significance* by changing  $N_{\text{obs}} \rightarrow N_{\text{sig}} + N_{\text{bkg}}$ , where  $N_{\text{sig}}$  is the number of signal events

$$Z = \sqrt{2 \left[ (N_{\text{sig}} + N_{\text{bkg}}) \ln \left( 1 + \frac{N_{\text{sig}}}{N_{\text{bkg}}} \right) - N_{\text{sig}} \right]} \quad (4.20)$$

However, Eq. (4.18) did not include any nuisance parameters, it used Eq. (4.15) instead of Eq. (4.16). We want to express the significance with uncertainties. From "Discovery sensitivity for a counting experiment with background uncertainty" from Glen Cowan [26], we can use Eq. (17) on his paper that reads

$$Z = \left[ -2 \left( N_{\text{obs}} \ln \left[ \frac{N_{\text{obs}} + m}{(1 + \tau)N_{\text{obs}}} \right] + m \ln \left[ \frac{\tau(N_{\text{obs}} + m)}{(1 + \tau)m} \right] \right) \right]^{1/2}$$

where  $m = \tau N_{\text{bkg}}$  and Eq. (19) that reads

$$\tau = \frac{N_{\text{bkg}}}{\sigma_{\text{bkg}}^2}$$

where  $\sigma_{\text{bkg}}$  is the uncertainty of the background. This gives us

$$Z = \sqrt{-2 \left( N_{\text{obs}} \ln \left[ \frac{N_{\text{obs}} + \frac{N_{\text{bkg}}^2}{\sigma_{\text{bkg}}^2}}{(1 + \frac{N_{\text{bkg}}}{\sigma_{\text{bkg}}^2}) N_{\text{obs}}} \right] + \frac{N_{\text{bkg}}^2}{\sigma_{\text{bkg}}^2} \ln \left[ \frac{\frac{N_{\text{bkg}}}{\sigma_{\text{bkg}}^2} (N_{\text{obs}} + \frac{N_{\text{bkg}}^2}{\sigma_{\text{bkg}}^2})}{(1 + \frac{N_{\text{bkg}}}{\sigma_{\text{bkg}}^2}) \frac{N_{\text{bkg}}^2}{\sigma_{\text{bkg}}^2}} \right] \right)} \quad (4.21)$$

Which makes for a better estimate of the significance one has in reality. **Question:**  
**Should I add plots showing CLs and significance?**

## 4.4 Summary

In this chapter we have studied how one can calculate the number of expected events from a  $pp$ -collision can lead to the discovery of new particles. Using special relativity as a tool, we can express the four-momentum of the particles with detector-coordinates,  $p^\mu = (E, p_T \cos \phi, p_T \sin \phi, |p| \cos \theta)$ . From this four-momentum vector we can thereafter calculate interesting kinematic variables such as the invariant mass  $m_{ll}$ , missing transverse energy  $E_T^{miss}$ , stransverse momentum,  $m_{T2}$ , among others. Using the advanced ATLAS detector the four-momentum can be recorded from the accelerated protons at the LHC. With the recorded data and MC simulations taking into account the experimental features such as the PDFs and Breit-Wigner resonance, as well as the ATLAS kinematics, we can compare how the simulated events fare with the data recorded. By playing around with the kinematical variables of the particles and making cuts to isolate new physics signal we can see if there is a discrepancy between the data recorded and the SM background. After creating this signal region with the cut and count method we conduct a statistical analysis to see how the new theory/observed data deviates from our current understanding of physics.

This state-of-the-art method is what currently is being used at CERN and has lead to a great advancement in the field. However, with the rise of new technologies, such as *machine learning*, which excel at classification tasks, a door has been opened to try new methods. In this thesis we will use ML to hopefully create a better and more general signal region than what the current cut and count method does. Before describing how, we will explain what machine learning is, this is the subject of the next chapter.

**Question:** I don't know if this summary is too dense, or if the opening to ML is too superficial. Feel free to comment as harshly as you want here :-)



# Chapter 5

## Machine Learning

Machine Learning (ML) has emerged as a powerful tool for analyzing complex datasets and making accurate predictions. Its applications span across various fields, from natural language processing to image recognition, and it has been used successfully to solve a range of problems.

The main approach of this thesis will be to use ML as its popular rise has proven to be effective at binary classification tasks [27, 28] in High Energy Particle Physics. For our purposes it will be a powerful tool to attempt to classify events as SM background or as DM signal.

To give a short description of the essence of ML we can start by considering a general parameter  $\beta = \{\beta_1, \beta_2, \dots, \beta_n\}$  for an n-dimensional problem, which for our purposes can be seen as what are called *weights* and *biases* ( $\beta = \{w, b\}$ ), the goal is to choose these parameters  $\beta$  such that we minimize a cost (also called loss) function  $C(\beta)$  with respect to a set of data points given by a matrix  $\mathbf{X}$ . This matrix  $\mathbf{X}$  will be our dataset containing  $n$  *features* for each event  $m$ , and is of the following form

$$\mathbf{X} = \begin{pmatrix} x_{11} & x_{21} & x_{31} & \cdots & x_{n1} \\ x_{12} & x_{22} & x_{32} & \cdots & x_{n2} \\ x_{13} & x_{23} & x_{33} & \cdots & x_{n3} \\ \vdots & \vdots & \vdots & \cdots & \vdots \\ x_{1m} & x_{2m} & x_{3m} & \cdots & x_{nm} \end{pmatrix} \quad (5.1)$$

This project will only focus on Supervised Learning, meaning that we know what the output is a binary representation of signal and background, such that we can use target values  $\mathbf{t}$ . Then we give the network a score depending on how close the predicted output is to real values  $\mathbf{t}$ . Then we repeat the process after tweaking the parameters  $\beta$  and see if the score gets better.

To this end, we will first provide a mathematical foundation for ML, starting with a brief overview of the different types of ML algorithms we will study, such as Neural Networks (NN) and Boosted Decision Trees (BDT). Other aspects such as the importance of feature selection and feature engineering in preparing the data for ML algorithms, as well as the concept of model evaluation and optimization will be discussed in Chapter [7](#).

## 5.1 Neural Networks

The theoretical foundation for this chapter is mainly based of Hjort-Jensen's lecture notes [29, 30, 31]. Before beginning, we can briefly explain the idea behind NNs. As stated by Hjorth-Jensen in [29]:

*The idea of NN is to mimic the neural networks in the human brain, which is composed of billions of neurons that communicate with each other by sending electrical signals. Each neuron accumulates its incoming signals, which must exceed an activation threshold to yield an output. If the threshold is not overcome, the neuron remains inactive, i.e. has zero output*

That takes us to what a *neuron* is.

### 5.1.1 Artificial neurons

To describe the behavior of a neuron mathematically we can use the following model that mimics how one neuron works

$$y = f \left( \sum_{i=1}^n w_i x_i \right) = f(z) \quad (5.2)$$

Where  $y$ , the output of the neuron, is the value of its *activation function* (See section 5.1.3), which has the weighted,  $w_i$ , sum of signals  $x_1, \dots, x_n$  received by  $n$  neurons that are in a presiding layer.

The goal of NNs is to mimic the biological nervous system by letting each neuron interact with each other by sending signals, for us is in the form of a mathematical function between each layer, called the activation function. Most NNs consist of an input layer, an output layer and intermediate layers, called hidden layers. All the layers can contain an arbitrary number of neurons, and each connection between two neurons is associated with a weight variable  $w_i$ . The goal of using NNs is to teach the network the patterns of the data to then predict some target. In the context of our search for DM, by giving a NN our data set of events as its input layer, we can then train the network to classify events as signal or background.

Explained in greater detail if we were to look at a single event of the data, we start with an input with all the relevant features of the event,  $\mathbf{X}$ . Using Eq. (5.2) on every neuron on the next layer we can teach the network if there are any connections between the features, we can repeat this process for  $n$  layers. As an output we want a single neuron to see if it has predicted the event to be a signal or background, since this is binary output. After analyzing the prediction we can use the labels on the target data  $\mathbf{t}$  to tell (the network) whether it predicted correctly or wrong. We can then use a *cost function* and a specific *metric* to evaluate numerically how well the network predicted the output by giving it a score. Seeing how the results fare we can then back-propagate to shift the weights and biases and repeat the process until we are satisfied with our result. Each of these iterations is called an epoch.

To generalize our artificial neuron to a whole network we can look at a Multilayer Perceptron (MLP). An MLP is a network consisting of at least three layers of neurons, the input, one or more hidden layers, and an output. The number of neurons can vary for each layer. The above explanation is a very dense and simplified one. In reality, it is complicated to find out which cost function, activation function, metric, etc. are best suited to the given problem. But before we get into the gory details we can explore the mathematical model that illustrates what was tried to be explained above.

### 5.1.2 Optimizers

The way we "tweak the parameters  $\beta$  to see if the network prediction gets better" is by using something called an *optimizer*. We will mainly focus on the theory behind the *Stochastic Gradient Descent* (SDG) optimizer as it is more easy to digest. Before explaining the SDG we have to look at the Gradient Descent (GD).

Given a cost function  $C(\beta)$  we can get closer to the minimum by calculating the gradient  $\nabla_\beta C(\beta)$  wrt. the unknown parameters from the NN  $\beta$ . If we were to calculate the gradient at a specific point  $\beta_i$  in the parameter space, the negative gradient would correspond to the direction where a small change  $d\beta$  in this parameter space would result in the biggest decrease in the cost function. In the same way we in physics would determine where the local (or global) minima at a complex multidimensional potential numerically.

In GD, we can choose (which needs to be optimized) a step size  $\eta$  related to the size of an iteration in the parameter space; this is called the *learning rate*. The mathematical function for an iteration in parameter space to optimize the parameter  $\beta$  such that it minimizes the cost function is given as

$$\beta_{i+1} = \beta_i - \eta \nabla_\beta C(\beta_i) \quad (5.3)$$

To converge towards a minimum we should select a learning rate  $\eta$  small enough to not "step over" the minimum point of the cost-function-space, but also not too small to get stuck on a local minimum rather than the global minimum. Thus using the learning rate as a hyperparameter in a grid search is a good way to optimize a NN for a given task.

In GD one computes the cost function and its gradient globally for all data points. This quickly becomes computationally heavy when dealing with large datasets. Thus, a common approach is to compute the gradient over batches of the data. For our purposes it would be optimal to use GD, but our data size is massive, of the order of  $10^8$  events (13 GB), becoming computationally impossible. Thus instead of making an  $n \times 10^8$  matrix (see Eq. (5.1)), we could for example split it into ten smaller matrices of  $n \times 10^7$  to then perform a parameter update, making the computation possible. This is where SGD comes in, for each step, or epoch the data is divided randomly into  $N$  batches of size  $n$ . Then for each batch we use Eq. (5.3) to update the parameters, thus updating  $\beta_{i+1}$   $N$ -times for each epoch. The idea of SGD comes from the observation that the cost function can almost always be written as a sum over  $n$  data points. The main advantage of SGD is not to ease the computation however, as using more batches also reduces the risk of getting stuck in a local minimum since it introduces a randomness of which part of the parameter space we move through, but this is at the cost of reducing statistics which might not be ideal for every problem.

There are other optimization algorithms we could use, such as the popular ADAM [32]. The Adaptive Moment Estimation (ADAM) is a more advanced optimization algorithm that uses adaptive learning rates. It computes individual learning rates for each weight based on the average of past gradients and their variances. ADAM also uses momentum to accelerate the convergence of the optimization algorithm. We will test both ADAM

and SGD when optimizing our networks.

### 5.1.3 Activation functions

As seen in Section 5.1.1, an important aspect of NNs are activation functions and cost functions. As shall become apparent in Section 5.1.4, when evaluating an activation function we get the neuron output, but what are these activation functions? Mathematically speaking, activation functions are: Non-constant, Bounded, Monotonically-increasing and continuous functions. In this project we will utilize two different activation functions at different layers. The first one is a sigmoid activation function

$$f(x) = \frac{1}{1 + e^{-x}} \quad (5.4)$$

which is the most basic activation function, this will be used from the input layer to our first hidden layer as the risks of having little neuron activation is minimal here. On all other layers we will utilize a Rectified Linear Unit (ReLU)

$$f(x) = x^+ = \max(0, x) = \begin{cases} x & \text{if } x > 0, \\ 0. & \text{otherwise.} \end{cases} \quad (5.5)$$

Which has better gradient propagation, meaning that there are fewer vanishing gradient problems compared to the sigmoidal function.

### 5.1.4 Feed Forward network

To describe how the network "guesses" outputs in a mathematical model we can start by looking at Eq. (5.2) where we got an output  $y$  from an activation function  $f$  that receives  $x_i$  as input. We can expand the function as following

$$y = f \left( \sum_{i=1}^n w_i x_i + b_i \right) = f(z) \quad (5.6)$$

where  $w_i$  is still the weight, and we now use the previously introduced bias  $b_i$  which is normally needed in case of zero activation weights or inputs. The difference comes now in the interpretation; where in the activation  $z = (\sum_{i=1}^n w_i x_i + b_i)$  the inputs  $x_i$  are now the

outputs of the neurons in the preceding layer. Furthermore, an MLP is fully-connected, meaning that each neuron received a weighted sum of the output of **all** neurons in the previous layer. To expand Eq. (5.6) we can first look at the output of every neuron  $i$  in a weighted sum  $z_i^1$  for each input  $x_j$  on a layer

$$z_i^1 = \sum_{j=1}^M w_{ij}^1 x_j + b_i^1 \quad (5.7)$$

Where  $M$  stands for all possible inputs to a given neuron  $i$  in the *first* layer. Such that if we evaluate the weighted sum in an activation function  $f_i$  for each neuron  $i$ , then the output of all neurons in layer 1 is  $y_i^1$

$$y_i^1 = f(z_i^1) = f\left(\sum_{j=1}^M w_{ij}^1 x_j + b_i^1\right)$$

To generalize this for  $l$ -layers, which may have different activation functions, we write it as

$$y_i^l = f^l(z_i^l) = f^l\left(\sum_{j=1}^{N_{l-1}} w_{ij}^l y_j^{l-1} + b_i^l\right)$$

Where  $N_l$  is the number of neurons in layer  $l$ . Thus, when the output of all the nodes in the first hidden layer is computed, the values of the subsequent layer can be calculated and so forth until the output is obtained. With this we can show that we only need the inputs  $x_n$  to calculate the output with  $l$  hidden layers

$$y^{l+1} = f^{l+1}\left[\sum_{j=1}^{N_l} w_{ij}^{l+1} f^l\left(\sum_{k=1}^{N_{l-1}} w_{jk}^l \left(\cdots f^1\left(\sum_{n=1}^{N_0} w_{mn}^1 x_n + b_m^1\right) \cdots\right) + b_j^l\right) + b_i^{l+1}\right] \quad (5.8)$$

This shows that an MLP is nothing more than an analytic function, specifically a mapping of real-valued vectors  $\hat{x} \in \mathbb{R}^n \rightarrow \hat{y} \in \mathbb{R}^m$ . We can also see that the above equation is essentially a nested sum of scaled activation functions of the form

$$f(x) = c_1 f(c_2 x + c_3) + c_4$$

where the parameters  $c_i$  are the weights and biases. By adjusting these parameters we shift the activation function to better match the label we are training the data on, this is the flexibility of a NN. Something else we can note is that Eq. (5.8) can easily be

changed into matrix notation, as hinted with Eq. (5.1). However, this realization can help make computing the values a much easier task by for example utilizing TensorFlow [33] or other mathematical packages in Python. An illustration showing the main idea of how a Feed forward network is set up is shown in Figure 5.1.

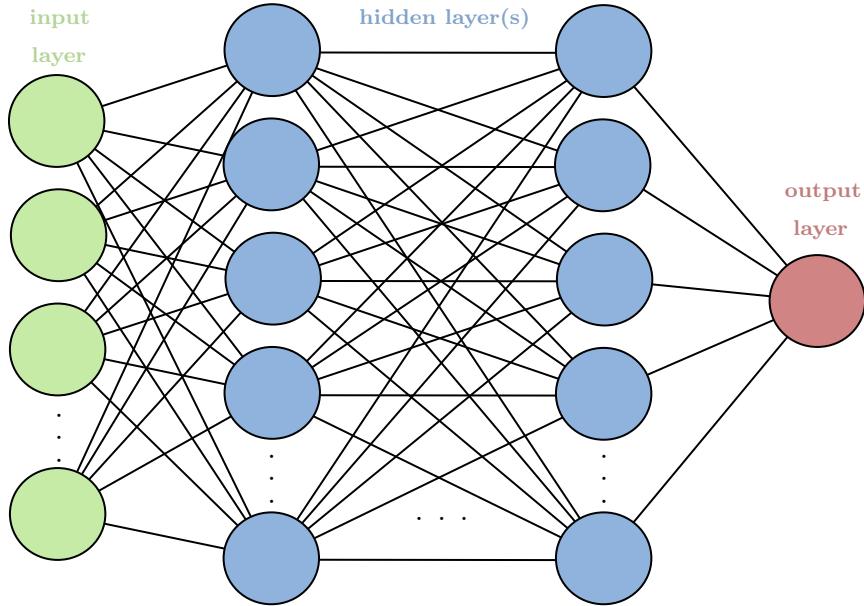


Figure 5.1: Basic illustration of a network with two hidden layers.

### 5.1.5 Back Propagation algorithm

So far we have only explained Feed Forward networks, which helps us to compute the output of the NN in terms of basic linear algebra. We mentioned the possibility to adjust the weight and biases, but never explained how. Now is the time to dive into that subject, as we will explain the back propagation algorithm. What we want to know is how the changes in the biases and weights in the network change the cost function, and how we could use the final output to modify the weights? Before we derive these equations we start by a plain regression problem, using the Mean Squared Error (MSE) as a cost function for pedagogical reasons

$$C(\hat{W}) = \frac{1}{2} \sum_{i=1}^n (y_i - t_i)^2 \quad (5.9)$$

where  $\hat{W}$  is the matrix containing all the weights and (more importantly)  $t_i$  are the targets, which are the labels of events telling whether we have a signal or background

event. To generalize this we first have to generalize to Eq. (5.7) for a layer  $l$

$$z_i^l = \sum_{j=1}^M w_{ij}^l y_j^{l-1} + b_i^l \Leftrightarrow \hat{z}^l = (\hat{W}^l)^T \hat{y}^{l-1} + \hat{b}^l$$

where the right side is written in matrix notation. From the definition of  $z_j^l$  with an activation function, Eq. (5.6), we have

$$\frac{\partial z_j^l}{\partial w_{ij}^l} = y_i^{l-1} \quad (5.10)$$

and

$$\frac{\partial z_j^l}{\partial y_i^{l-1}} = w_{ij}^l$$

which again, with the definition of the sigmoid activation function, Eq. (5.4), gives us

$$\frac{\partial y_j^l}{\partial z_j^l} = y_j^l(1 - y_j^l) = f(z_j^l)(1 - f(z_j^l)) \quad (5.11)$$

Furthermore, we need to take the derivative of Eq. (5.9) with respect to the weights, doing so for a respective layer  $l = L$  we have

$$\frac{\partial C(\hat{W}^L)}{\partial w_{jk}^L} = (y_j^L - t_j) \frac{\partial y_j^L}{\partial w_{jk}^L}$$

where the last partial derivative is easily computed using the chain rule with Eq. (5.10) and Eq. (5.11)

$$\frac{\partial y_j^L}{\partial w_{jk}^L} = \frac{\partial y_j^L}{\partial z_j^L} \frac{\partial z_j^L}{\partial w_{jk}^L} = y_j^L(1 - y_j^L)y_k^{L-1}$$

Such that

$$\frac{\partial C(\hat{W}^L)}{\partial w_{jk}^L} = (y_j^L - t_j) y_j^L(1 - y_j^L)y_k^{L-1} := \delta_j^L y_k^{L-1} \quad (5.12)$$

where we have defined the error

$$\delta_j^L := (y_j^L - t_j) y_j^L(1 - y_j^L) = f'(z_j^L) \frac{\partial C}{\partial y_j^L} \quad (5.13)$$

or in matrix form

$$\delta^L = f'(\hat{z}^L) \circ \frac{\partial C}{\partial \hat{y}^L}$$

where on the right-hand side we wrote this as a Hadamard product<sup>1</sup>. This error  $\delta^L$  is an important expression, since as we can see in the index form of this expression in Eq. (5.13), we can measure how fast the cost function is changing as a function of the  $j$ -th output activation. This means that if the cost function doesn't depend on a particular neuron  $j$ , then  $\delta_j^L$  would be small.

We also notice that everything in Eq. (5.13) is easily computed. Thus, we can also see how the weight changes the cost function using Eq. (5.12) quite easily. Another thing we can compute with Eq. (5.13) is

$$\delta_j^L = \frac{\partial C}{\partial z_j^L} = \frac{\partial C}{\partial y_j^L} \frac{\partial y_j^L}{\partial z_j^L}$$

which can be interpreted in terms of the biases  $b_j^L$  as

$$\delta_j^L = \frac{\partial C}{\partial b_j^L} \frac{\partial b_j^L}{\partial z_j^L} = \frac{\partial C}{\partial b_j^L} \quad (5.14)$$

where the error  $\delta_j^L$  is exactly equal to the rate of change of the cost function as a function of the bias.

Something interesting is that when using Eq. (5.12 - 5.14) we see that if a neuron output  $y_j^L$  is small, then the gradient term, Eq. (5.12), will also be small. We say then that the weight learns slowly, meaning that the contribution of said neuron is less important "to fix" than those that have a higher weight. Of course this example is a very simple one to wrap our heads around, but the magic comes when the algorithm is evaluating a random neuron in a layer  $n$ , after using many layers the NN becomes a **black box** for us to wrap our heads around!

It is also worth noting that when the activation function is flat at some specific values (which also varies with the chosen function!) the derivative will tend towards zero, making the gradient small, meaning the network is learning slow as well. To finish up our back propagation algorithm we still need one equation. We are now going to propagate backwards in order to determine the weights and biases. We start by representing the

---

<sup>1</sup>Also called *element-wise* product,  $(A \circ B)_{ij} = (A \odot B)_{ij} = (A)_{ij}(B)_{ij}$

error in the layer before the final one  $L - 1$  in terms of the errors of the output layer. If we try to express Eq. (5.13) in terms of the output layer  $l + 1$ , using the chain rule and summing over all  $k$  entries we get

$$\delta_j^l = \sum_k \frac{\partial C}{\partial z_k^{l+1}} \frac{\partial z_k^{l+1}}{\partial z_j^l} = \sum_k \delta_k^{l+1} \frac{\partial z_k^{l+1}}{\partial z_j^l}$$

recalling Eq. (5.7) (replacing 1 with  $l + 1$ ) we get

$$\delta_j^l = \sum_k \delta_k^{l+1} w_{kj}^{l+1} f'(z_j^l) \quad (5.15)$$

Which is the final equation we needed to start back propagating.

### 5.1.6 Summary

To summarize the whole process of the NN

- First take the input data  $\mathbf{x}$  and the activation  $\mathbf{z}_1$  of the input later, and then compute the activation function  $f(z)$  to get the next neuron outputs  $\mathbf{y}^1$ . Mathematically this is taking the first step of the feed forward algorithm, i.e. choosing  $l = 0$  in Eq. (5.8)
- Secondly we commit all the way in Eq. (5.8) and compute all  $\mathbf{z}_l$ , activation function and  $\mathbf{y}^l$ .
- After that we compute the output error  $\boldsymbol{\delta}^L$  by using Eq. (5.13) for all values  $j$ .
- Then we back propagate the error for each  $l = L - 1, L - 2, \dots, 2$  with Eq. (5.15).
- The last step is then to update the weights and biases using Eq. (5.3) for each  $l$  and updating using

$$w_{jk}^l \leftarrow w_{jk}^l - \eta \delta_j^l y_k^{l-1}$$

and

$$b_j^l \leftarrow b_j^l - \eta \delta_j^l$$

This whole procedure is usually called an epoch, which we can repeat as many times as we want to better reduce the cost function in hope of converging to the global minima.

## 5.2 Boosted Decision Trees

In the previous chapter, we explored how NNs can aid in the task of signal and background classification, such as the one in this thesis where we are looking DM signal in the SM background. In this chapter, we will delve into Boosted Decision Trees (BDTs), another powerful tool for binary classifications. BDTs, unlike neural networks, are not based on simulating biological neurons. Instead, they rely on decision trees, a simple yet powerful idea that has been around for decades. [34, 35] Decision trees are built by recursively splitting data based on the values of features until a stopping condition is met. BDTs take this idea one step further by training an ensemble of decision trees, where each tree attempts to correct the mistakes of its predecessors.

BDTs have several advantages over other machine learning algorithms, such as neural networks, for binary classification problems. They are highly interpretable, which allows us to understand how they arrived at their decisions. This is particularly important in this field, high energy particle physics, where the ability to interpret results is crucial. BDTs are also highly resilient to overfitting and can handle missing data effectively. Given their strengths, BDTs have been widely used in particle physics for binary classification tasks, such as distinguishing signal from background events. The idea of the BDTs used in high energy physics today was proposed as early as 2001 by Friedmann in the paper *Greedy Function Approximation* [36], and since then have become an indispensable tool in the field. In particular, in the ATLAS collaboration challenge *The Higgs boson machine learning challenge* [37] the creation of a BDT package called **XGBoost** [38] increased the popularity even more as they won the challenge. Today **XGBoost** has become a standard ML tool used in the field.

In this chapter, we will explore the theory behind BDTs in the context of *extreme gradient boosting*, for this we are mainly interested in two ways of making DTs, a set of Classification And Regression Trees (CART). The theory is mainly based of Hjort-Jensen's lecture notes [39, 40] and section 2 on the original **XGBoost** paper [38].

### 5.2.1 Decision trees

Starting with Decision Trees (DT) in the context of this DM search. The idea behind DTs is to find the most important features which contain the most information of signal (DM), and then split the dataset along the values of these features with the goal of creating a dataset containing pure signal. As we are going to use kinematical variables as features we will use this to both augment and automate the classical cut and count method (Chapter 4.3), which is based of making kinematical cuts on the variables. To find which kinematical features are most important in splitting the dataset we have to achieve a stopping criterion where we end up on a so-called *leaf node*.

A DT is typically divided into *root nodes*, *interior nodes* and a final *leaf nodes*, also called leaves, which are all connected by *branches*, hence the name decision tree. As mentioned in the start of this chapter, we will look at two ways of making DTs, the first one we will look at is the *regression tree*.

### 5.2.2 Regression trees

As previously mentioned the leaves contain the prediction of a trained network, and are used to make new predictions on new datasets based on the information the DT learning in the branching process. As how to construct trees, there are mainly two steps we need to follow:

1. Split the predictor space (set of possible values  $x_1, x_2, \dots, x_p$ ) into  $J$  distinct and non-overlapping regions,  $R_1, R_2, \dots, R_J$
2. For every observation that falls into the region  $R_j$ , we make the same prediction, which is the mean of the response values for the training observations in  $R_j$

Is this too similar to 9.3 in [39]?

But how do we construct the regions  $R_1, R_2, \dots, R_J$ ? In theory these regions could have any shape, but for simplicity and pedagogical reasons we will choose to divide the predictor space into high-dimensional rectangles, or boxes. This means that the goal is to find boxes  $R_1, R_2, \dots, R_J$  that minimize a *cost function*, which again, for pedagogical

reasons will be the MSE (Eq. (5.9)), defined as

$$\sum_{j=1}^J \sum_{i \in R_j} (y_i - \bar{y}_{R_j})^2$$

where  $\bar{y}_{R_j}$  is the mean response for the training observations within box  $j$ . Ideally we would consider every possible partition of the feature space into  $J$  boxes, but this is computationally infeasible. Thus, the common approach is to begin at the top of the tree, where all observations belong to a single region, and then split the predictor space; where every split is indicated via two new branches down in the tree. This is greedy (as in *Greedy Function Approximation* [36]) since the best split is made in the first step, rather than looking ahead and picking a split that might lead to a better tree in a future step.

To make any split we start by selecting the predictor  $x_j$  and a cut point  $s$  that splits the predictor space into two regions  $R_1$  and  $R_2$

$$\{X|x_j < s\} \quad \text{and} \quad \{X|x_j \geq s\}$$

so that we obtain the lowest MSE,

$$\sum_{i:x_i \in R_1} (y_i - \bar{y}_{R_1})^2 + \sum_{i:x_i \in R_2} (y_i - \bar{y}_{R_2})^2$$

where we consider all predictors  $x_1, x_2, \dots, x_p$  and each possible value  $s$  for each of them, where these values can be randomly assigned numbers. For any  $j$  and  $s$  we define the pair of half-planes where  $\bar{y}_{R_1}$  and  $\bar{y}_{R_2}$  are the mean responses for the training observations in  $R_1(j, s)$  and  $R_2(j, s)$  respectively. The goal is to find the value  $j$  and  $s$  such that we minimize the cost function, which can be done quickly depending on the number of predictors.

Then we repeat the process looking for the best predictor and best cut point, but instead of stopping with two regions, we split one of the two into another two regions creating a total of three regions. This is called the depth of a tree, and we can in principle continue to split indefinitely, however one usually sets a stopping criterion on how many events should be at a leaf.

The method explored above is straight forward, but often leads to overfitting and unnecessarily large and complicated trees. To mediate this one usually uses a so-called *Cost complexity* pruning algorithm. For regression procedures, the algorithm, rather than considering every possible subtree, considers a sequence of trees indexed by a non-negative tuning parameter  $\alpha$ . For each value of this  $\alpha$  there corresponds a subtree  $T \in T_0$  such that

$$\sum_{m=1}^{\bar{T}} \sum_{i:x_i \in R_m} (y_i - \bar{y}_{R_m})^2 + \alpha T \quad (5.16)$$

is as small possible. In the equation above  $T$  is the number of terminal nodes of the tree  $T$ ,  $R_m$  is the rectangle corresponding to the  $m$ -th terminal node. This tuning parameter  $\alpha$  controls a trade-off between the subtree's complexity and its fit to the training data. As  $\alpha$  increases, the above equation will give us a higher value, meaning that our trees would normally prioritize less complex models. This procedure is repeated until we minimize Eq. (5.16) and choose a suitable value for  $\alpha$ . This is the essence of regression trees.

### 5.2.3 Classification trees

The second DT type we will study is the *classification tree*. Classification trees are very similar to regression trees, except that they are used to predict a qualitative response rather than a quantitative one. This means that classification trees are used for predictive modeling in which the output variable is discrete, such as classifying an email as spam or not spam, or predicting whether an event in our dataset is a DM signal or SM background event.

Like regression trees, classification trees recursively split the data based on the values of input variables until a stopping condition is met. However, the splitting criteria for classification trees are different. Classification trees cannot use the MSE function used in regression trees as a criterion for making binary splits, instead they use the *classification error rate*. The classification error rate, classification trees have discrete outputs, is simply the fraction of the training observations in a region that do not belong to the most common class.

Classification trees use measures such as Gini index or the entropy to determine quality

of a split at each node. The idea behind these quality measures is to select the split that maximizes the separation between the different categories of the output variable.

If a classification tasks takes for example  $k = 1, 2, \dots, K$  values as outputs, we can define a probability distribution function  $p_{mk}$  that represents the number of observations of  $k$  in a region  $R_m$  with  $N_m$  observations. We can represent this likelihood function in terms of the proportion  $I(y_i = k)$  of observations of this output in region  $R_m$  as

$$p_{mk} = \frac{1}{N_m} \sum_{x_i \in R_m} I(y_i = k)$$

where  $p_{mk}$  represents the majority class of observations in region  $m$ . The tree most common ways of splitting a node are given by: The misclassification error

$$p_{mk} = \frac{1}{N_m} \sum_{x_i \in R_m} I(y_i \neq k) = 1 - p_{mk}$$

The Gini index  $G$

$$G = \sum_{k=1}^K p_{mk}(1 - p_{mk}) \quad (5.17)$$

and the entropy  $s$

$$s = - \sum_{k=1}^K p_{mk} \log(p_{mk})$$

### 5.2.4 The CART algorithm

As we are going to look at extreme gradient boosting, the main algorithm for this type of DT is the Classification And Regression Tree (CART). For classification, the CART algorithm splits the dataset in two subsets using a single feature  $k$  and threshold  $t_k$ . This could for example be a threshold set by a value of the invariant mass of an event we are trying to classify as background or signal. The way we optimize the pair  $(k, t_k)$  such that we get the purest subset is by for example using the Gini factor  $G$ . With this the cost function tries to minimize

$$C(k, t_k) = \frac{m_{left}}{m} G_{left} + \frac{m_{right}}{m} G_{right}$$

where  $G_{left/right}$  calculates the impurity of the left/right subset using Eq. (5.17) and  $m_{left/right}$  is the number of events in the left/right subset. Once the algorithm successfully splits the training set into two, it splits the subsets using the same algorithm, and so on, recursively. For our purposes we will make the DT stop searching for the pair  $(k, t_k)$  once we have reached the maximum depth we chose, or whenever the sum of the weights on a leaf is one. Both of these are hyperparameters that need to be optimized, for that see Chapter 7.3.2.

The CART algorithm for regression works similarly to the one for classification, but instead of trying to split the training set in a way that minimizes the Gini or entropy impurity, it tries to split the training set in a way that minimizes the (MSE). Meaning that we have

$$C(k, t_k) = \frac{m_{left}}{m} MSE_{left} + \frac{m_{right}}{m} MSE_{right}$$

with

$$MSE_{node} = \frac{1}{m_{node}} \sum_{i \in node} (\bar{y}_{node} - y_i)^2$$

and

$$\bar{y}_{node} = \frac{1}{m_{node}} \sum_{i \in node} y_i$$

### 5.2.5 Ensemble modeling and (extreme) gradient boosting

Now that we have explained how DTs work, we still need more information to get the full picture of *Boosted* DTs. For this section of the chapter we. As we are going to look at a massive dataset, a single tree is not strong enough to be used in practice. What is actually used is the *ensemble model*, which sums up the prediction of multiple trees together. What is important of these models is that the different trees we are summing together try to complement each other. For example if the first split on one tree is on the invariant mass of a dilepton pair, while on another tree it is the MET, then we know physically that these are important features that DM + dilepton models have as a signature, meaning that it should be a good combination. Mathematically, we can write

the prediction of an ensemble model in the form

$$\hat{y}_i = \sum_{k=1}^K f_k(x_i), \quad f_k \in \mathcal{F} \quad (5.18)$$

where  $K$  is the number of trees we want to sum over,  $f_k$  is a function of the functional space  $\mathcal{F}$ , where  $\mathcal{F}$  is the set of all possible CARTs. With this we want to minimize the objective function of the form

$$\mathcal{L} = \sum_i^n C(y_i, \hat{y}_i) + \sum_{k=1}^K \Omega(f_k)$$

where we sum over  $n$  leaves,  $C$  is training cost function (for example it can be the MSE), and  $\Omega(f_k)$  is the complexity of the tree  $f_k$ , which penalizes the more complex models. We can see from both functions above that we need to learn all trees at once to make predictions, this is however both computationally demanding and intractable. Instead, we can use an additive strategy, where we fix what we have learned, and add a new tree at a time. Using Eq. 5.18 with 0 trees and going up we see that we get

$$\begin{aligned}\hat{y}_i^{(0)} &= 0 \\ \hat{y}_i^{(1)} &= f_1(x_i) = \hat{y}_i^{(0)} + f_1(x_i) \\ \hat{y}_i^{(2)} &= f_1(x_i) + f_2(x_i) = \hat{y}_i^{(1)} + f_2(x_i) \\ \hat{y}_i^{(3)} &= f_1(x_i) + f_2(x_i) + f_3(x_i) = \hat{y}_i^{(2)} + f_3(x_i)\end{aligned}$$

and so on. Mathematically we see that a prediction at step  $t$  as in  $\hat{y}_i^{(t)}$  takes the form

$$\hat{y}_i^{(t)} = \sum_{k=1}^t f_k(x_i) = \hat{y}_i^{(t-1)} + f_t(x_i) \quad (5.19)$$

Such that we can now write the objective to be

$$\mathcal{L}^{(t)} = \sum_i^n C(y_i, \hat{y}_i^{(t-1)} + f_t(x_i)) + \Omega(f_t) \quad (5.20)$$

from which we can set up our choice for cost function. In general case we take the Taylor expansion of the loss function up to the second order such that we get

$$\mathcal{L}^{(t)} = \sum_i^n \left[ C(y_i, \hat{y}_i^{(t-1)}) + g_i f_t(x_i) + \frac{1}{2} h_i f_t^2(x_i) \right] + \Omega(f_t) + const$$

where

$$g_i \equiv \partial_{\hat{y}_i^{(t-1)}} C(y_i, \hat{y}_i^{(t-1)}) \quad \text{and} \quad h_i \equiv \partial_{\hat{y}_i^{(t-1)}}^2 C(y_i, \hat{y}_i^{(t-1)})$$

Such that the specific objective at step  $t$  becomes

$$\sum_{i=1}^n \left[ g_i f_t(x_i) + \frac{1}{2} h_i f_t^2(x_i) \right] + \Omega(f_t) \quad (5.21)$$

where we removed all constants. Such that Eq (5.21) becomes the optimization goal for the new tree. As we can see the above equation can take into account any cost function as it is written in a general form with a Taylor expansion. Furthermore, we can rewrite this by expanding

$$\Omega(f_t) \rightarrow \alpha T + \frac{1}{2} \lambda \sum_{j=1}^T w_j^2$$

where the first term is the same as in Eq. (5.16), and the second is called the *regularization term* (see Chapter 5.3.1). Inserting this into Eq. (5.21) we get

$$\mathcal{L}^{(t)} = \sum_{j=1}^T \left[ \left( \sum_{i=1}^n g_i \right) w_j + \frac{1}{2} \left( \sum_{i=1}^n h_i + \lambda \right) w_j^2 \right] + \alpha T$$

such that with a fixed tree structure,  $q$ , we can define the optimal weight  $w_j^*$  on a leaf  $j$  as

$$w_j^* = -\frac{\sum_{i=1}^n g_i}{\sum_{i=1}^n h_i + \lambda} \quad (5.22)$$

and correspondingly the optimal objective reduction

$$\mathcal{L}^{(t)}(q) = -\frac{1}{2} \sum_{j=1}^T \frac{(\sum_{i=1}^n g_i)^2}{\sum_{i=1}^n h_i + \lambda} + \alpha T \quad (5.23)$$

With both of these equations we have all we need to use BDTs, the extreme part of the gradient boosting is something the **XGBoost** algorithm has implemented in terms of system optimization, such as parallelizing the tree boosting task, and can be read in more

detail on section 4 of the original paper [38].

### 5.2.6 Summary

So in short BDTs split datasets based on different values of the features on the dataset, figure 5.2 shows an illustration of how DTs work.

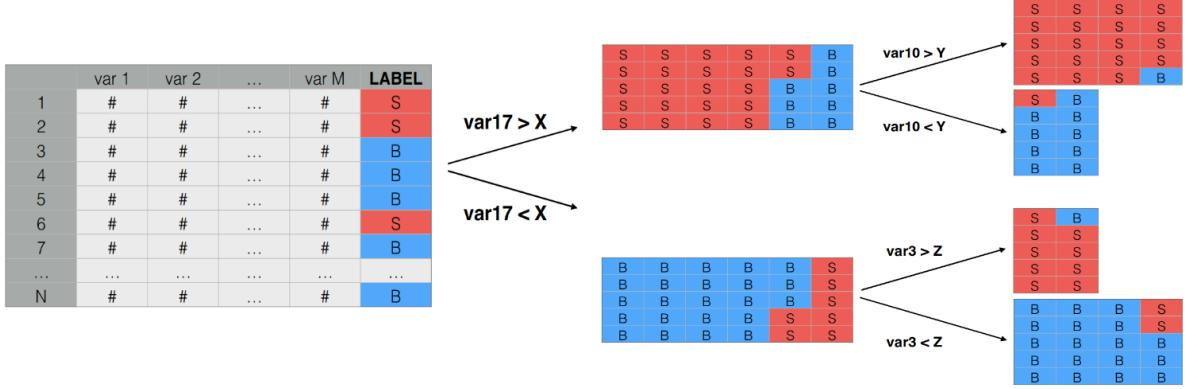


Figure 5.2: Image showcasing how decision trees work by splitting a dataset of  $N$  events with  $M$  features whenever a threshold  $X$ ,  $Y$  or  $Z$  for a feature is passed. The label  $S$  and  $B$  state whether the event is signal or background respectively.

The above illustration just shows how one tree might work, in reality we can choose to have an arbitrary number of trees and combine their results with the ensembling and boosting method. Then after combining the generated tree structures we use Eq. (5.22) and Eq. (5.23) to minimize the objective to get the most accurate predictions as possible.

## 5.3 Tools and evaluation methods used for both algorithms

Now that we have explained how both NNs and BDTs work, we will present the tools and evaluating method that we will use in this thesis.

### 5.3.1 Cost functions

Cost functions have been mentioned throughout this chapter, but what are they? Cost functions are what we will utilize to evaluate how well the output of the network fares against the target, i.e. if our network "guesses" right whether an event is signal or background, thus making this a very important part of our network! Before getting into this we first have to look at logistic regression. Since we are studying a binary classification task where the output is either  $t_i = 0$  or  $t_i = 1$ , meaning background or signal. We can introduce a polynomial model of order  $n$  as

$$\hat{y}_i = \beta_0 + \beta_1 x_i + \beta_2 x_i^2 + \cdots + \beta_n x_i^n$$

where the hat notation,  $\hat{y}$ , symbolizes a condensed matrix form of the output of a layer. We can define the probabilities of getting  $t_i = 0$  or  $1$  given our input  $x_i$  and  $\beta$  with the help of a logistic function. Using this we get the probability as

$$p(t_i = 1|x_i, \beta) = \frac{1}{1 + e^{-t_i}}$$

and

$$p(t_i = 0|x_i, \beta) = 1 - p(t_i = 1|x_i, \beta)$$

We want to then define the total likelihood for all possible outcomes from a dataset  $\mathcal{D} = \{(t_i, x_i)\}$ , with the binary labels  $t_i \in \{0, 1\}$ , applying the Maximum Likelihood Estimation (MLE) principle. This gives us

$$P(\mathcal{D}|\beta) = \prod_{i=1}^n [p(t_i = 1|x_i, \beta)]^{t_i} [1 - p(t_i = 1|x_i, \beta)]^{1-t_i}$$

from which we obtain the log-likelihood

$$C(\boldsymbol{\beta}) = \sum_{i=1}^n (t_i \log p(t_i = 1|x_i, \boldsymbol{\beta}) + (1 - t_i) \log[1 - p(t_i = 1|x_i, \boldsymbol{\beta})])$$

By taking the parameter  $\boldsymbol{\beta}$  to first order in  $x_i$  and reordering the logarithm we get

$$C(\boldsymbol{\beta}) = - \sum_{i=1}^n (y_i(\beta_0 + \beta_1 x_i) - \log(1 + \exp(\beta_0 + \beta_1 x_i))) \quad (5.24)$$

This equation we will use throughout the thesis and is known as the *cross entropy*. The two beta parameters used are the weight and biases,  $\beta_1 = w$  and  $\beta_0 = b$ . The goal is to change these parameters such that it minimizes the cost function.

## L2-regularization

Furthermore, we will add an extra term to the cost function, proportional to the size of the weights. We do this to constrain the size of the weights, so they don't grow out of control, this is to reduce *overfitting*. We will use the so-called *L2-norm* where the cost function becomes

$$C(\boldsymbol{\beta}) \rightarrow C(\boldsymbol{\beta}) + \lambda \sum_{ij} w_{ij}^2 \quad (5.25)$$

meaning that we add a term where we sum up **all** the weights squared. The factor  $\lambda$  is called the regularization parameter. The L2-norm combats overfitting by forcing the weights to be small, but not making them exactly zero. This is so that less significant features still have some influence over the final prediction, although small.

### 5.3.2 Sample weight

A "sample weights" array is an array of numbers that specify how much weight each sample in a batch should have in computing the total loss. It is commonly used in imbalanced classification problems (the idea being to give more weight to rarely-seen classes). Taken from the original documentation [41]. To mathematically illustrate how this weight works is by multiplying a constant term  $\chi$  into the cost/loss function that is used further on the error propagation. As an example we can extend the simple MSE,

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Eq. (5.9) to

$$C(\hat{W}) = \frac{1}{2} \sum_{i=1}^n \chi_i (y_i - t_i)^2 \quad (5.26)$$

This will become an important feature when discussing network optimization in Chapter 7, and especially for particle physicists as we want to re-weight Monte Carlo events to expected events to correctly showcase kinematical distributions.

### 5.3.3 Area under the ROC-curve

To evaluate how well our networks do. We will use the accuracy, which literally tells us how many events it guessed right. But also take into account a more advanced metrics, this is the Area Under the "Receiver Operating Characteristic (ROC)" Curve (AUC). Before explaining what the AUC is we first need to explore the ROC curves. The ROC curves helps us illustrate how successful a network is a *binary classification* (only). The ROC curve, as the name states is a curve, where we plot the *True Positive Rate* (TPR) against the *False Positive Rate* (FPR). The TPR is defined by dividing the *True Positive* (TP), which is when the network correctly guesses a signal event to be a signal event, by the *Positive* (P), which is the total number of signal events in the data.

$$\text{TPR} = \frac{\text{TP}}{\text{P}}$$

On the other hand, the FPR is when we divide the *False Positive* (FP), when the network guesses a background event to be signal event, divided by the *Negatives* (N), the total number of background events in the data.

$$\text{FPR} = \frac{\text{FP}}{\text{N}}$$

To get a numerical value of how well a network classifies data we thus calculate the AUC. The TP and the FP are both going to be predictions from the networks, which for this thesis will give an event a score from 0 to 1<sup>2</sup>, meaning that if we had a perfect network which guesses everything correctly we would only get TPs and thus an AUC of 1. If we were to get an area of 0.5 this would mean that the network is randomly

---

<sup>2</sup>Where 0 means that the network believes an event has 0% chance of being a signal event, and 1 means that the networks believes with 100% certainty that an event is a signal event.

guessing whether an event is a signal or background, practically making a coin toss for every event. The goal is to have a network to give an AUC score as closely to 1 as possible.

While only using the accuracy as a metric is not a bad start, it is not favorable to use as a metric if datasets are unbalanced. As an example, if we had a dataset with 100 events, where 95 were background events and 5 were signal events, if we only used accuracy as a metric we would be inclined to think that an accuracy of 95% is great. However, as the dataset is unbalanced, the network could easily take a shortcut and guess every event to be a background event. Meaning that the network learned nothing. This is where the AUC comes into play, as this metric highlights whenever a network guesses wrongly in a binary classification. Meaning that if we used the worst case scenario with 95% accuracy when guessing everything to be background, we would have a  $\text{TPR} = 0$  and an  $\text{FPR} = 0$ , if we were to plot this we would get a flat line on the FPR and TPR axis, meaning that it would give us an AUC of 0.5. Highlighting that our network is randomly guessing, and that it needs to be optimized further. In Figure 5.3 we see an example of a ROC curve.

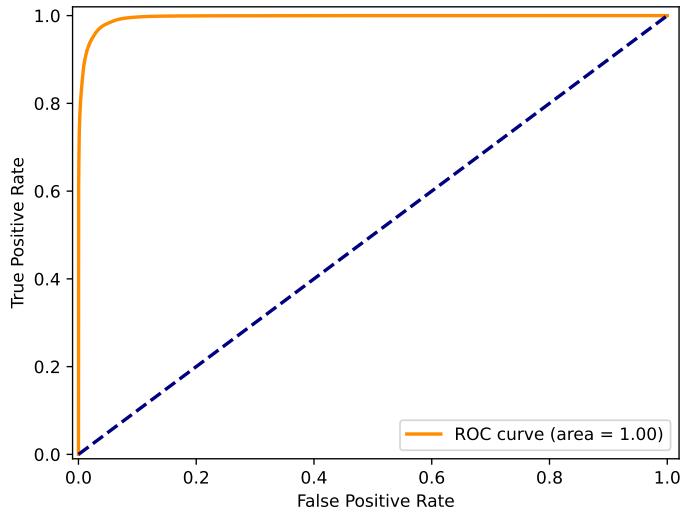


Figure 5.3: Illustration of a ROC curve. The orange line is the result of a network, while the dashed blue line is to illustrate a random guess

*Comment for farid/eirik, I used wikipedia as a source on the theory here, how do I cite that?*

### 5.3.4 Validation plots

Another tool that we will use to evaluate how well a network does is by making so-called *validation plots*. The way these plots work is by first dividing the *already predicted* data set into background and signal. Then making histograms from 0-1 with the prediction score of the network for each event. As a score closer to 1 means that the network predicts an event to be a signal event, and 0 means that the network predicts a background event. Then we would ideally have all the signal events shoved to the right and all the background events shoved to the left. Usually this is not the case in high energy particle physics, as some background events might be similar to signal events. We will therefore utilize this kind of plots to see the distribution of the network predictions.

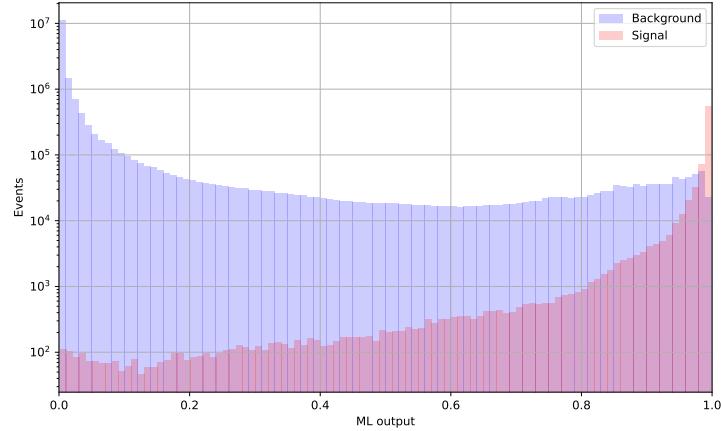
Is this  
the real  
name of  
the plots?

In addition to just sorting events by the ML score, we will also re-weight the events (which are MC events) into expected events<sup>3</sup>. The difference this makes can be seen in Figure 5.4. We can however still use the non-re-weighted plots to see how well the network has learned to sort, but these plots will not be used in this thesis, and can rather be found on the GitHub repo.

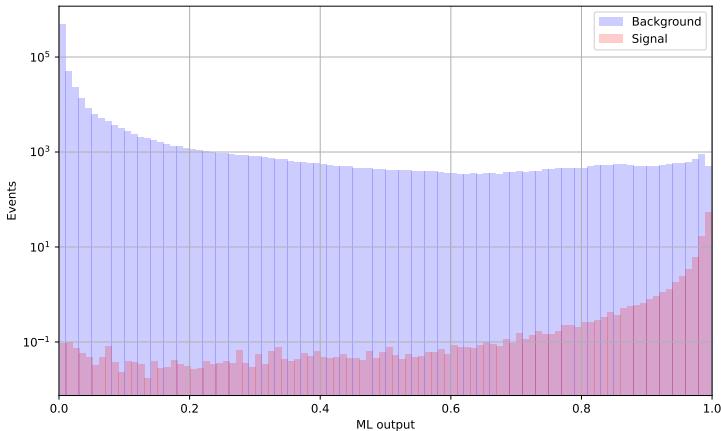
It is standard practice to make fill the histograms with semi-transparent colors, such that one can visualize the whole spectra for both background and signal. In this thesis we will use this, as well as validation plots where we divide the SM events into their respective background channels and fill them with opaque colors, while leaving the signal unfilled. We will in addition include real data points in the latter plots, to see how well SM simulations agree with the data. Ideally we want our data to not agree with the SM simulations when the network predicts a score close to one, as this discrepancy could be a hint of new physics.

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<sup>3</sup>See Chapter 7.1.1 for more information



(a) No re-weighting MC events to expected events



(b) Re-weighting MC events to expected events

Figure 5.4: Illustration of the validation plots. Plot a) shows how the network learned a dataset without re-weighting events, while b) shows how it looks re-weighted.

### 5.3.5 Significance plots

To create signal regions which will be used for statistical analysis we will also look at significance plots. The way these plots work is by using Eq. (4.20) on the number of signal and background events that are present after making a cut on the ML output on the validation plots. As an example, in Figure 5.5 we see the re-weighted validation plot from the previous section, and we can calculate the expected significance by counting the number of signal and background events that have an ML score greater than 0.5, 0.6, 0.7, 0.8, 0.9 and 0.99 respectively.

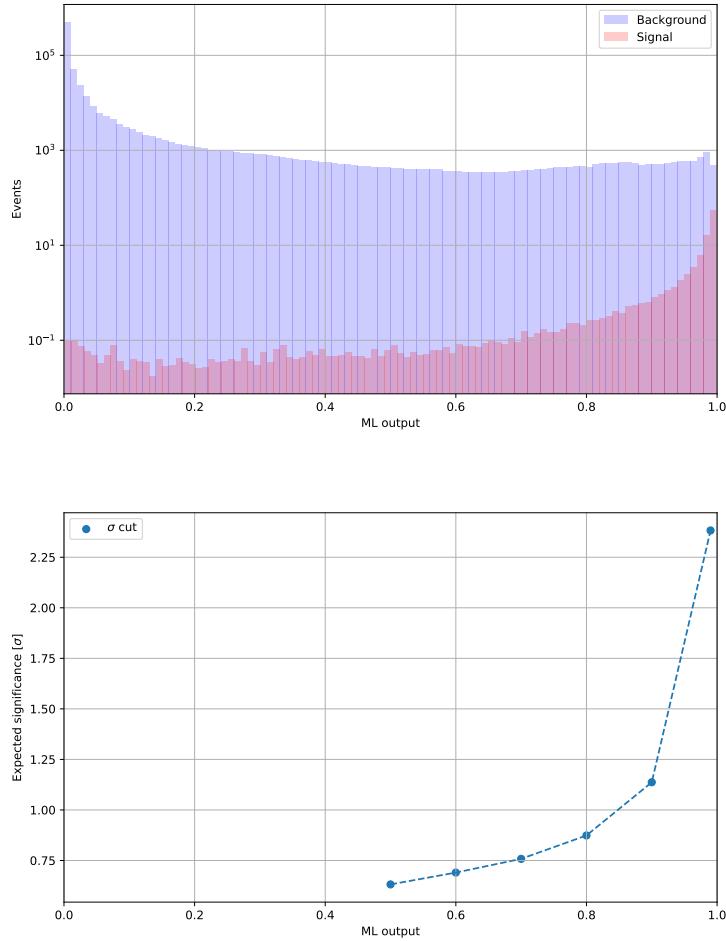


Figure 5.5: Plot showing the expected significance that is calculated from a) when making cuts on the ML output score. The dashed lines are to guide the eye.

### 5.3.6 BDT and NN exclusive plots

#### Feature importance

For BDTs, as we can calculate which features had the most impact when splitting the data, we will also include feature importance plots. As the name states these plots tell us how important the features in the dataset were in the training to separate signal from background. As we are using the `XGBoost` package when working with BDTs, we will use the inbuilt functions of the package to plot the feature importance.

When plotting the feature importance there are several metrics we can use to determine how important they are, for this thesis we will mainly look at

- Gain: which measures the relative contribution of a feature to the model's performance
- Weight: the number of times a feature appears on a tree to split the data
- Cover: the number of samples affected by the split with a feature

Where the first one is the standard used by `XGBoost`.

#### Metric and loss evolution

For NNs we can plot how the metrics (AUC and binary accuracy) as well as the loss function change over the training epochs. We will plot these changes for both the training and testing set. Where the goal is that the metric and loss converge to the same point for the training and testing set.

# Part II

## Implementation / Methods



# Chapter 6

## Data Preparation

Now is the time to focus on the critical task of preparing the data for our DM search using ML. This task is essential because accurately distinguishing between signal and background events is a key challenge in searching for any new signal event, as seen on Section 4.3. In this chapter we will define what *background* and *signal* actually are, as well as selecting appropriate kinematical cuts to define the control region for our search. In addition, we will explain the data preparing procedure such that it is in a format that is well-suited for our ML algorithms. The reason this process is of great importance is, so we can maximize the chances of our ML algorithm to accurately identify any DM signals. Moreover, by providing a detailed explanation of the data preparation process, we can ensure that our dataset is both reliable and effective, and that our analysis is robust and trustworthy. In short, this chapter represents a critical step towards achieving our goal of using ML to classify DM from SM events using ATLAS data, and it is essential to the success of our overall research goal.

## 6.1 Standard Model background estimation

As we are going to look at dilepton final states with missing transverse energy to try to teach our ML to learn DM signatures, then we need to take into account all possible SM background event that have this kind of final states. The SM backgrounds processes we will look at are explained in the next subsections. In Appendix A is the full list of dataset IDs for background process used in this thesis.

### 6.1.1 W and Drell Yan

$W + \text{jets}$  and  $Z/\gamma^* + \text{jets}$  can decay into final states that mimic the one we are searching for. The  $W$  boson can give us a lepton and neutrino  $W \rightarrow l\nu_l$ , which gives us MET, and  $Z/\gamma \rightarrow ll$ , which gives us a dilepton final state. All the production mechanism for these background processes be seen in Figure 6.1. As the  $W$  boson behaves differently than the  $Z$  and  $\gamma$ , since the  $W$  boson can decay into neutrinos giving us MET, while the  $Z$  and  $\gamma$  processes have the highest cross-section. We will divide these background processes into two,  $W$  and  $Z/\gamma^* + \text{jets}$ , also called *Drell Yan* processes. To simulate these background processes Sherpa 2.2.11 [42] was used.

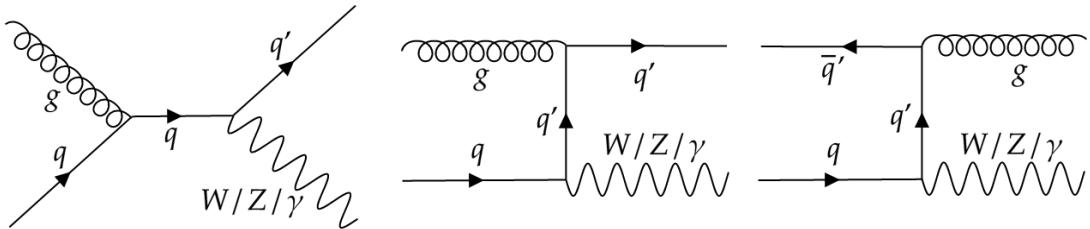


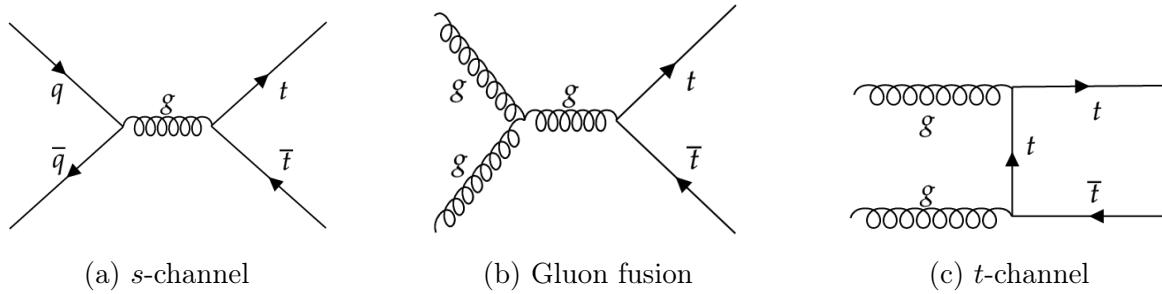
Figure 6.1: Diagrams showcasing SM  $W/Z/\gamma + \text{jets}$  production. A quark marked with a prime, indicated that the quark might be a different flavor after interacting with a boson.

### 6.1.2 Top pair

Another SM background process we will look at are processes that have a  $t\bar{t}$  in them. Since the top has a high branching ratio of decaying into a  $b$ -quark<sup>1</sup> and a  $W$  boson,  $t \rightarrow bW^+$ , where the  $W$  boson can again decay into a neutrino giving us MET. The main production mechanism for these processes can be seen in Figure 6.2. To simulate these background processes Powheg-Box v2 [43] interfaced with Pythia 8 [44] was used.

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<sup>1</sup>Making  $b$ -tagging an effective method to isolate this background channel

Figure 6.2: Diagrams showcasing SM  $t\bar{t}$  production

### 6.1.3 Single top

On the same note we have processes with a single top. Where again the top has a high branching ratio of decaying into a  $b$ -quark and a  $W$  boson,  $t \rightarrow bW^+$ , where the  $W$  boson can again decay into a neutrino giving us MET. The main production mechanism for these processes can be seen in Figure 6.3. To simulate these background processes Powheg-Box v2 [43] interfaced with Pythia 8 [44] was used.

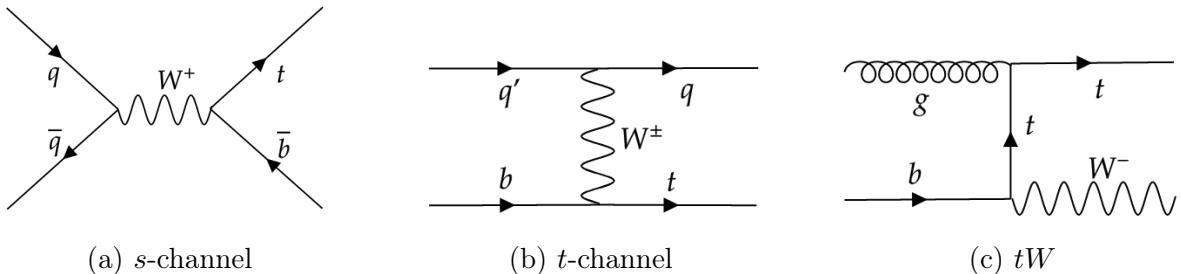


Figure 6.3: Diagrams showcasing SM single top productions. A quark marked with a prime, indicated that the quark might be a different flavor after interacting with a boson.

### 6.1.4 Diboson

The last SM background process we will look at are processes containing two bosons, called *diboson* backgrounds. The two SM bosons we will consider when looking into these final states are the  $W$  and  $Z$ , as these can decay as  $W/Z \rightarrow ll'/ll$  or  $W \rightarrow l\nu_l$ , where the prime means a different lepton flavor. The main production mechanism for these processes can be seen in Figure 6.4. To simulate these background processes Sherpa 2.2.11 [42] was used.

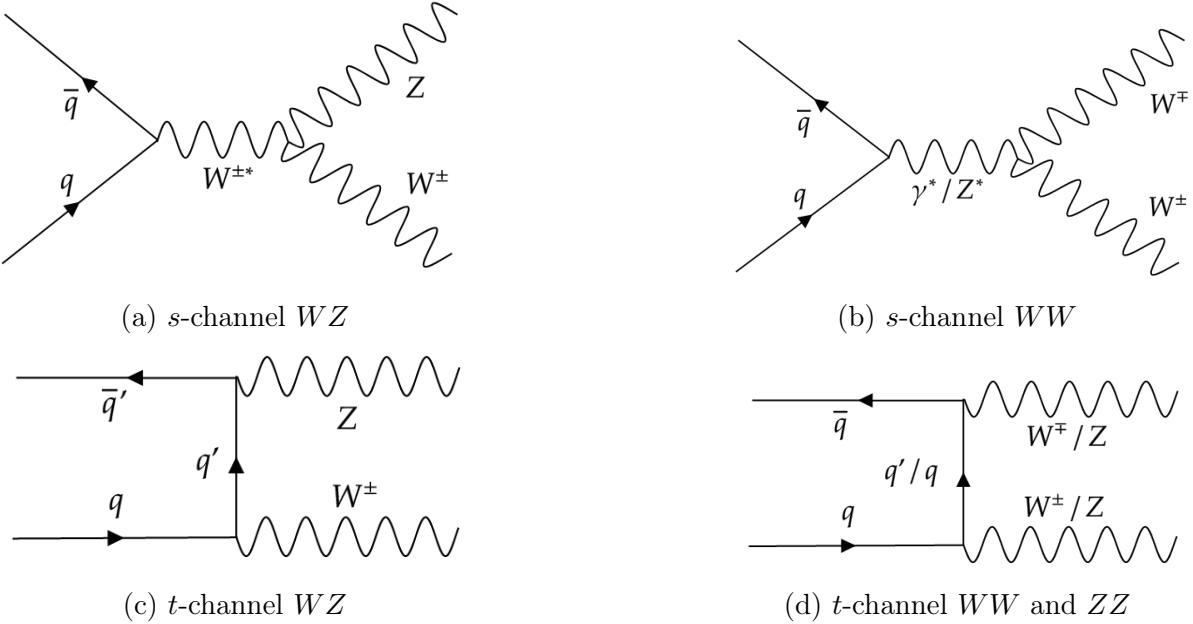


Figure 6.4: Diagrams showcasing SM diboson production. A star superscript on a boson indicates that the boson needs to be virtual and off mass shell. A quark marked with a prime, indicated that the quark might be a different flavor after interacting with a boson.

## 6.2 Dark Matter samples

The models in Chapter 3 contain three relevant couplings

- the coupling  $g_D$  between the  $Z'$  and the DM particles ( $Z'Z'h_D$  or  $Z'\chi_1\chi_2$ )
- the coupling  $g_q$  between the  $Z'$  and quarks
- and the coupling  $g_l$  between the  $Z'$  and leptons

The coupling to quarks and leptons are assumed to be the same for all generations. When simulating the couplings were set to

- $g_D = 1$ ,
- $g_q = 0.1$ ,
- and  $g_l = 0.01$ .

In addition to the couplings, as mentioned on Chapter 3, we will divide the three models, DH, LV and EFT into two more regions. The difference being the masses, Table 6.1 showcases the definition of the Light Dark Sector (LDS) and Heavy Dark Sector (HDS).

Table 6.1: Dark sector masses in light- and heavy dark sector models

	Dark Higgs	Light Vector / Inelastic EFT
Light Dark Sector	$m_\chi = 5 \text{ GeV}$ $m_{h_D} = 125 \text{ GeV}$	$m_{\chi_1} = 5 \text{ GeV}$ $m_{\chi_2} = m_{\chi_1} + m_{Z'} + 25 \text{ GeV}$
Heavy Dark Sector	$m_\chi = 5 \text{ GeV}$ $m_{h_D} = m_{Z'}$	$m_{\chi_1} = m_{Z'}/2$ $m_{\chi_2} = 2m_{Z'}$

The simulated masses of the new  $Z'$  boson for this thesis are

$$m_{Z'} = [130, 200, 400, 600, 800, 900, 1100, 1200, 1300, 1400, 1500] \text{ GeV}.$$

For the DH and LV model and

$$m_{Z'} = [130, 200, 300, 400, 500, 600, 700, 800, 900, 1000, 1100, 1200, 1300, 1400, 1500] \text{ GeV}.$$

For the EFT model. **Question: Should I add an appendix with DSIDs like I did on Appendix A?**

### 6.3 Object selection

Before getting into our DM search and regions we will study we have to define how standard objects are defined. By standard objects we mean electron, muons and jets. As this thesis is made using ATLAS data and simulations we will use the same standard criteria cuts they choose.

The electrons are selected using the criteria on Table 6.2. The muons are selected using the criteria on Table 6.3. The jets are selected using the criteria on Table 6.4. The missing transverse energy is reconstructed from jets selected and calibrated according to the information in Table 6.4. In addition to these a kinematical cut of  $m_{ll} > 10 \text{ GeV}$  will be made to exclude hadron productions.

I don't know how else to present these

Table 6.2: Electron selection criteria.

Feature	Selection criteria
Transverse momentum	$p_T > 25 \text{ GeV}$
Pseudorapidity range	$ \eta  < 1.37$ or $1.52 <  \eta  < 2.47$
$d_0$ significance cut	$ d_0(\sigma)  < 5$
$z_0$ cut	$ \Delta z_0 \sin \theta  < 0.5 \text{ mm}$

Table 6.3: Muon selection criteria.

Feature	Selection criteria
Transverse momentum	$p_T > 27(20) \text{ GeV}$ for leading (sub-leading)
Pseudorapidity cut	$ \eta  < 2.5$
$d_0$ significance cut	$ d_0(\sigma)  < 5$
$z_0$ cut	$ \Delta z_0 \sin \theta  < 0.5 \text{ mm}$

Table 6.4: Jet selection criteria.

Feature	Selection criteria
Algorithm	Anti- $k_t$
$R$ -parameter	0.4
Transverse momentum	$p_T > 20 \text{ GeV}$
Pseudorapidity cut	$ \eta  < 4.5$
Jet Vertex Tagger	$> 0.5$ for $p_T < 60 \text{ GeV}$ , $ \eta  < 2.4$
forward JVT	fJVT $< 0.4$ and $ \text{timing}  < 10 \text{ ns}$ for $p_T < 120 \text{ GeV}$ , $2.5 <  \eta  < 4.5$
b-jet tagging	DL1r score $> 0.665$ with 85% efficiency

## 6.4 Control region

Now that we have defined what our background and signal are, the next step is to create a so-called *control region*. The control region is the kinematical region we will use as a base for our search. As we are conducting a model independent search we want our kinematical cuts to be minimal and as general as possible. As we are looking at a dilepton final state, then we need to first define what we mean by that. If we were only searching for DM with the  $Z'$  model, then a sensible definition would be a Same Flavor Opposite Sign (SFOS) leptons ( $e^\pm e^\mp, \mu^\pm \mu^\mp$ ). However, to stay as general, and model independent, as possible we will also study other possible combinations as these might be important for theories such as SUSY or Lepton Flavor Violating (LFV) models. These are Different

Flavor Same Sign (DFSS), DFOS and SFSS lepton pairs.

Since we are looking for DM, which we expect to behave similarly to a neutrino, then a nice kinematical variable to set a general cut to isolate signal from background is the MET, we can see the distribution of MET on all of Run II in a dilepton final state in Figure 6.5.

As we are conducting a model independent search, we want to use minimal cuts. The MET cut made in this thesis was chosen to be of 50 GeV (violet line in plot), meaning we will *only* look at events where the MET is greater than this. As we can see from Figure 6.5 by making a kinematical cut on 50 GeV we are cutting out a massive part of the background processes while only losing a small part of the signal.

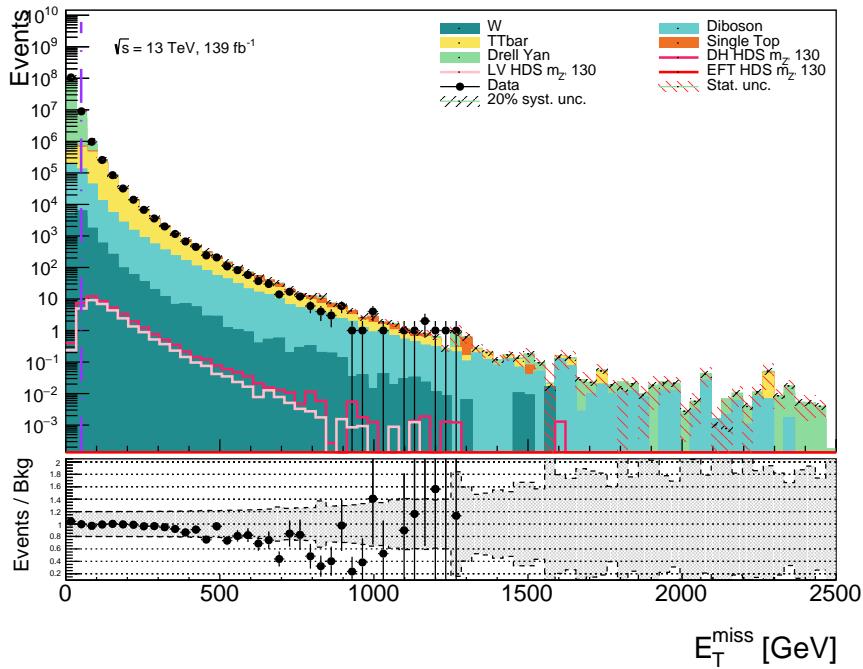


Figure 6.5: Distribution of MET when looking at a dilepton final state in all of Run II. The violet line shows where we will make our MET cut to create a control region. The DM models here have the highest cross-section making them the most visible to our purposes.

Other than the object selection criteria, these are the only cuts that will be used to define the control region. Their summary can be seen in Table 6.5

Table 6.5: Table showcasing the cuts used to define the control region for our model independent search.

Feature	Selection criteria
Dilepton final state	$\ell^\pm \ell^\mp, \ell^\pm \ell^\pm, \ell^\pm \ell'^\mp$ and $\ell^\pm \ell'^\pm$
Missing Transverse Energy	$E_T^{miss} > 50 \text{ GeV}$

## 6.5 Feature selection for ML

For this thesis there are many possible kinematic variables that can be used as features for our ML algorithms, in this section we will make use of the kinematical variables presented in Section 4.1.1 as well as introduce new variables that might help our ML algorithm to correctly learn the patterns of SM background and DM signal events.

As we are studying a final state with two leptons it is therefore natural to look at the kinematics for both of these as these will give us as general information as possible. The first thing we will look at is the transverse momentum,  $p_T$ , of each lepton as defined in Eq. (4.2). We will also look at the azimuthal angle,  $\phi$  and the pseudorapidity,  $\eta$  defined in Eq. (4.8), to know where in the detector the leptons are located. With this we have practically constructed a four-momentum from which we could learn all particle kinematics. However, we want to help our ML algorithm as much as possible in the task of learning SM background and DM signal. A powerful kinematical variable for this is therefore the invariant mass,  $m_{ll}$  defined in Eq. (4.3), which can help the ML algorithm sort out resonant models. Another variable of interest is the transverse energy,  $E_T$  defined in Eq. (4.4) for the lepton pair. The distribution of the invariant mass can be seen in Figure 6.6.

As we are studying DM, an invisible particle, the most important kinematical variable to distinguish background from signal is the missing transverse energy,  $E_T^{miss}$  defined in Eq. (4.5), as this is how we expect DM to be recorded. Another version of the MET is the so-called *Object-based  $E_T^{miss}$  significance*, or  $E_T^{miss,sig}$  for short, this variable is used to deal with artificial or fake  $E_T^{miss}$ . The way  $E_T^{miss,sig}$  works is by weighing the value of

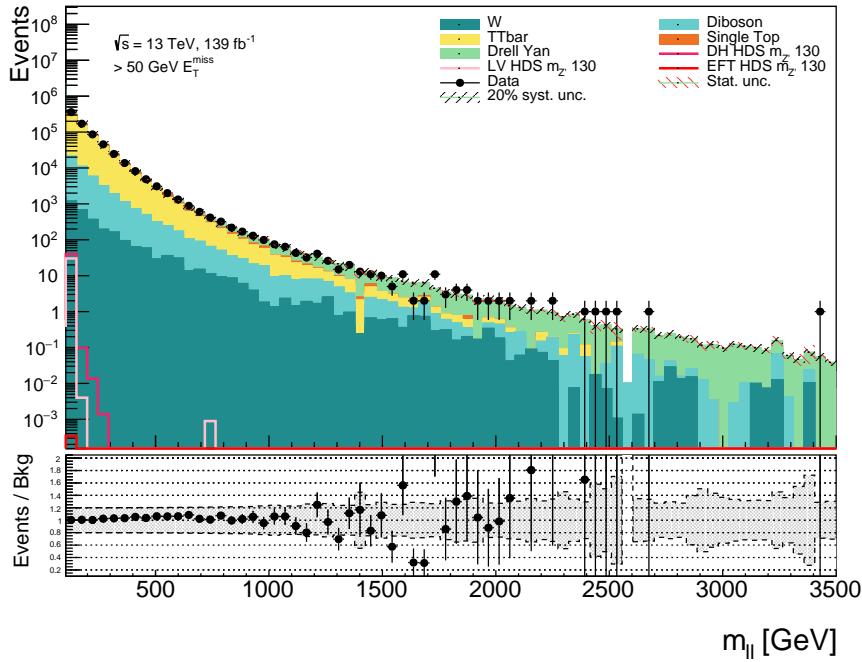


Figure 6.6: Distribution of  $m_{ll}$  in control region.

$E_T^{miss}$  by the precision of its reconstruction. It is defined as

$$E_T^{miss,sig} = \frac{E_T^{miss}}{\sigma(E_T^{miss})} \quad (6.1)$$

where  $\sigma(E_T^{miss})$  is the uncertainty of the reconstruction of the  $E_T^{miss}$ , which consider the individual uncertainties of the objects that enter the  $E_T^{miss}$  calculation. The distribution of this variable can be seen in Figure 6.7. In this thesis we will use both  $E_T^{miss}$  and  $E_T^{miss,sig}$  even though they are correlated, as the algorithm might choose in different instances<sup>2</sup> which of these is of more importance.

To keep the trend of variables for invisible particles, we will also study the transverse mass,  $m_T$  defined in Eq. (4.10), and stransverse mass,  $m_{T2}$  defined in Eq. (4.11) which might help our ML algorithm to sort i.e. W backgrounds from the signal. The distribution of the stransverse mass can be seen in Figure 6.8. Moving on to more jet related variables, we will count the number of b- and light jets with  $p_T \geq 30, 40$  GeV respectively. As the jet reconstruction is already a hard task, which becomes even harder when pushing the limits of our selection criteria with a MET cut. In Figure 6.9 we can see how the

<sup>2</sup>Meaning different *signal regions* when conducting a model independent search. See Chapter 7.1.2

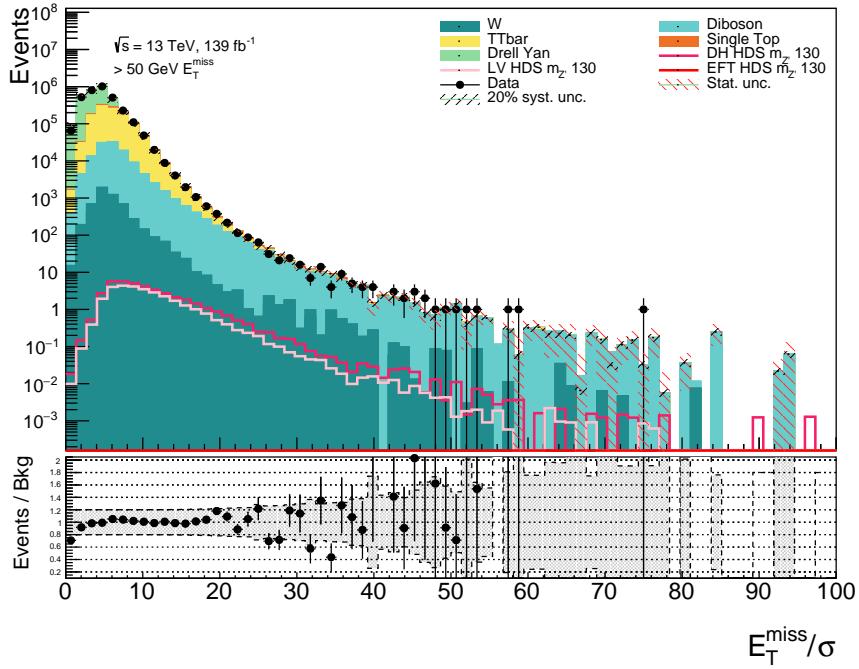
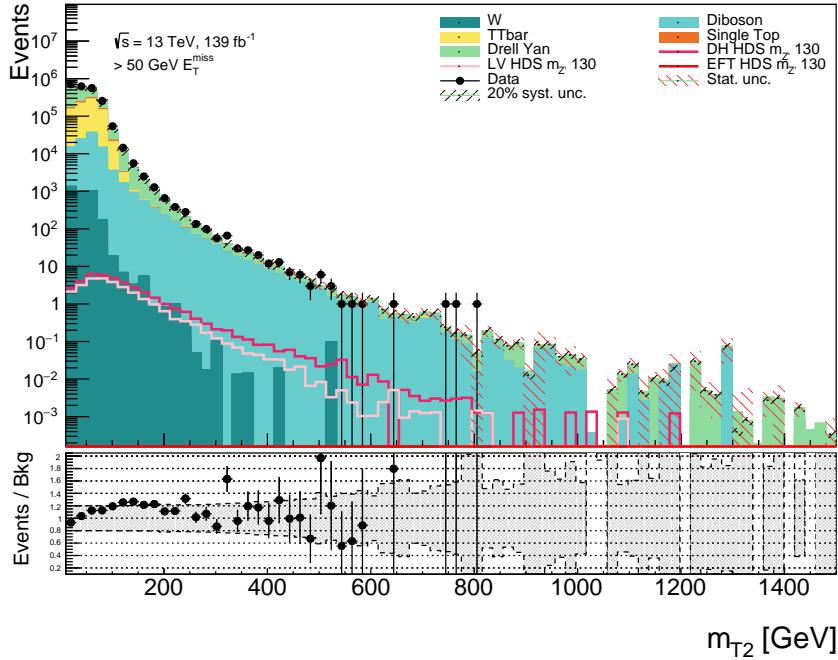
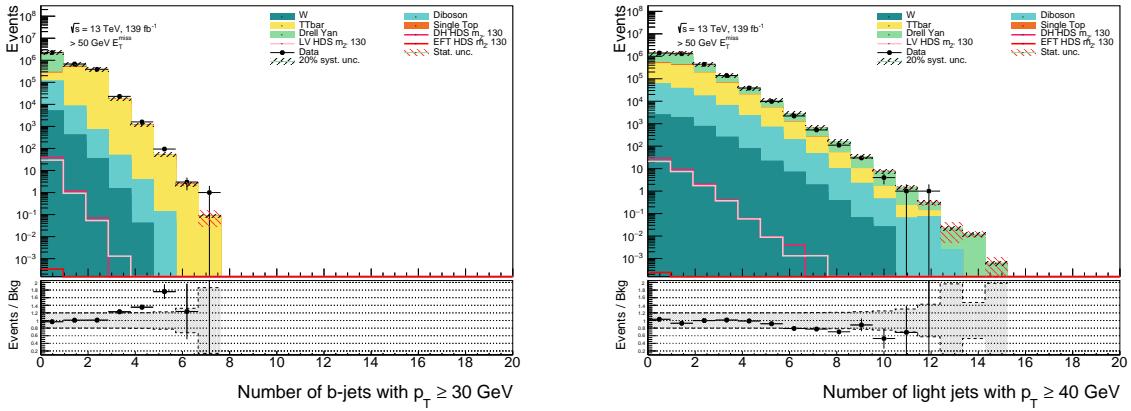


Figure 6.7: Distribution of  $E_T^{miss,sig}$  in control region.

data and MC simulations of the SM agree when counting the number of b- and light jets with a  $p_T$  cut of  $\geq 30$  GeV and  $\geq 40$  GeV respectively. The agreement with different  $p_T$  cuts can be seen in Appendix C. We will also look at the  $p_T$ ,  $\eta$  and  $\phi$  of the three most energetic jets, as these have the best MC and data agreement (see Figure 6.9), and the invariant mass of the two most energetic jets  $m_{jj}$ .

Although these jet variables might not sound like the most useful when singling out DM signal from SM background, there is always the possibility that our ML algorithm sees a pattern which is overlooked by us when conducting these kinds of searches. Another variable we will look at is the hadronic activity,  $H_T$  defined in Eq. (4.6), from which we will also look at the ratio between the MET and hadronic activity,  $E_T^{miss}/H_T$ , as this can help the ML algorithm sort out DM events from background events.

To know the distance between the "lepton-jet" and "MET-jet" we will look at the difference in azimuthal angle between: the lepton pair,  $\Delta\phi(l_1, l_2)$ , the dilepton jet and MET jet,  $\Delta\phi(l l, E_T^{miss})$ , the leading lepton and MET jet,  $\Delta\phi(l_l, E_T^{miss})$ , and the lepton closest to the MET jet and the MET jet,  $\Delta\phi(l_c, E_T^{miss})$ . In some of the models we are study-

Figure 6.8: Distribution of  $m_{T2}$  in control region.Figure 6.9: b- and light jet distributions with  $p_T \geq 30$  and  $\geq 40$  GeV, respectively.

ing it is expected for DM and the leptons pair to be back to back. The distribution of  $\Delta\phi(l l, E_T^{miss})$  can be seen in Figure 6.10.

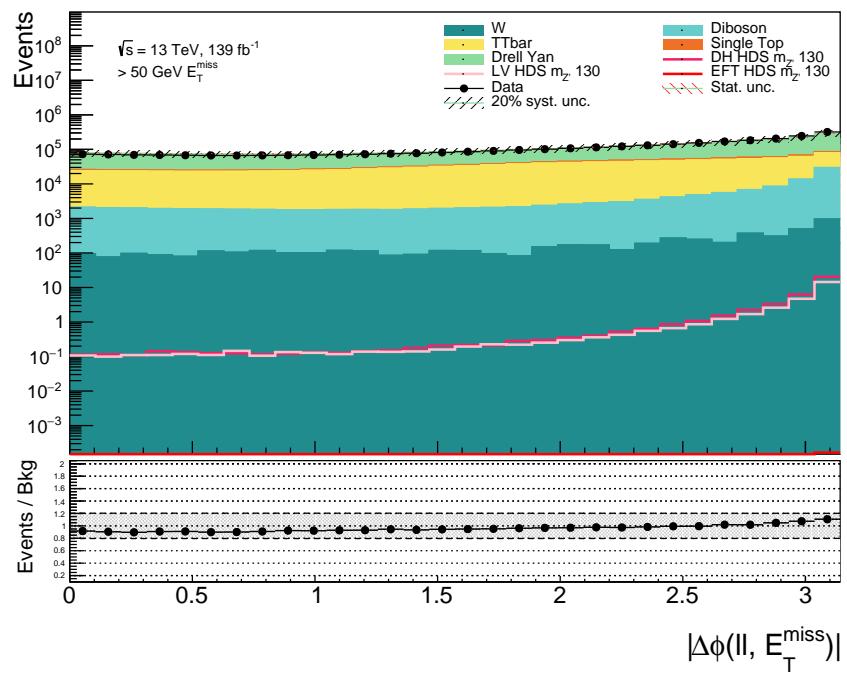


Figure 6.10: Distribution of  $\Delta\phi(l\bar{l}, E_T^{\text{miss}})$  in control region.

The kinematic variables used are summarized in Table 6.6 and the distribution of the remaining kinematical variables are shown in Appendix B.

Table 6.6: Table showcasing the kinematic variables that will be used as features on our ML algorithm.

\* These have poor MC and data agreement. † These create *jagged arrays*.

Kinematic variable	Feature name
$p_T$ of both leptons	lep1pt & lep2pt
$\phi$ of both leptons	lep1phi & lep2phi
$\eta$ of both leptons	lep1eta & lep2eta
Invariant mass of dilepton pair, $m_{ll}$	mll
Missing transverse energy in event, $E_T^{miss}$	met
Missing transverse energy significance in event, $E_T^{miss,sig}$	met_sig
Transverse mass in an event, $m_T$	mt
Stransverse mass in an event, $m_{T2}$	mt2
Transverse energy of lepton pair, $E_T$	et
$\phi$ between lepton pair, $\Delta\phi(l_1, l_2)^*$	dPhiLeps
$\phi$ between lepton pair and MET jet, $\Delta\phi(ll, E_T^{miss})$	dPhiLLMet
$\phi$ between leading lepton and MET jet, $\Delta\phi(l_l, E_T^{miss})$	dPhiLeadMet
$\phi$ between the closest lepton and MET jet, $\Delta\phi(l_c, E_T^{miss})^*$	dPhiCloseMet
Hadronic activity, $H_T$	ht
Ratio between $E_T^{miss}$ and $H_T$ , $E_T^{miss}/H_T$	rt
Number of b-jets	nbjets
Number of light jets*	nljets
$p_T$ of three jets with highest $p_T$ †	jet1pt & jet2pt & jet3pt
$\phi$ of three jets with highest $p_T$ †	jet1phi & jet2phi & jet3phi
$\eta$ of three jets with highest $p_T$ †	jet1eta & jet2eta & jet3eta
Invariant mass of two jets with highest $p_T$ , $m_{jj}$ †	mjj

## 6.6 Transfer to ML friendly syntax

We have so far explained how the data will be used and carefully selected, however the question of how the data is made, and the number of samples we will work with still remains unanswered.

As mentioned when defining what our background and signal is, we will mainly look at MC simulations. The MC simulations are made into ROOT [45] NTuples which already have passed the object selection criteria on section 6.3. What remains is to set the kinematical cuts, so we have our control region. To do this as well as saving the remaining

events into a new file which will be used for our ML algorithm I utilized the algorithms on `EventSelector`<sup>3</sup>, which also saved the event that passed the event selection criteria as `ROOT` histograms to make plotting the distributions easier. After saving the events that passed the selection criteria I used the algorithms on `DataPrep`<sup>4</sup> to plot the actual distributions of kinematical variables, and more importantly converting all the events that passed the event selection into an ML friendly syntax. For this thesis we are converting from `ROOT NTuples` to `pandas DataFrame` [46] which can furthermore be saved as `h5` files to be read more efficiently. The reason we chose `pandas DataFrame` is because of the easily readable kinematics per event, the easily applicable kinematical cuts to the whole dataset (to more effectively create signal regions), and most importantly because of the compatibility with `XGBoost` [38] and `TensorFlow` [33] which will be the ML packages we will utilize for both BDTs and NNs.

## 6.7 Problems

There are however still problems that needs to be addressed before starting our ML, the biggest are addressed here.

### 6.7.1 Missing variables

For this thesis, as shown in Table 6.6 with the  $\dagger$ , we will record events with up to three jets in the final state. However, there isn't always three jets in the recorded events that we will be studying, this creates *jagged arrays* which we can interpret as arrays with missing values. This is an unwanted feature that we need to avoid when training an ML algorithm, and is a problem that is not common in other ML tasks aside from high energy particle physics. To mediate this problem we chose to set the  $p_T$  to zero for the missing jets and  $m_{jj}$  to zero if there are less than two jets, this is something that is physically reasonable as it doesn't violate any conservation laws. More problematic however is the  $\eta$  and  $\phi$  when there aren't jets. To mediate this I've set the values to -999, which has no physical meaning and is impossible to achieve, this we did so it becomes easier for us to identify the jagged arrays that need different interventions when preparing both NNs

---

<sup>3</sup>Available here: <https://github.com/rubenguevara/Master-Thesis/tree/master/EventSelector>

<sup>4</sup>Available here: <https://github.com/rubenguevara/Master-Thesis/tree/master/DataPrep>

and BDTs. The methods we explored to mediate the jagged array problem is further explained in Chapter 7.2.1.

### 6.7.2 MC and data disagreement

There is also another problem, with the final states that are not SFOS, as the MC generated background on these tend to be lower than the recorded data. The number of events that are not SFOS are minimal though, and we think the reason it does not fit the data is because we are not including fake leptons.

something  
more to  
add?

Now that we have explained how the data has been prepared and the problems that arise with this we are ready to start playing around with ML! **Question: Anything else to add to this chapter?**



# Chapter 7

## Machine Learning

We have now presented the dataset and theory behind everything, and are thus ready to start making our ML algorithms. The first part of this chapter will be a presentation of the dataset in more details, included all the events and the difficult variable called *weights*. We will also explore how we divide our dataset into a training and testing set. Afterwards we will discuss the crucial task of optimizing the architecture and hyperparameters of the ML models for obtaining high-performance classifiers. In this field, the challenge is often to distinguish between signal events from rare physics phenomena, such as our DM interactions, and the much more common SM background events. Since these signals events are extremely rare, the classifiers need to be highly optimized in order to effectively separate them from the background. In addition, the datasets have numerous features, which can lead to overfitting or poor generalization if not properly optimized. Another hardship is how to mitigate the phenomena of jagged arrays and missing variables described in the previous chapter.

It is therefore essential to carefully choose the model architecture and hyperparameters, as well as the dataset pre-processing techniques, in order to achieve the best possible performance in the search for the rare DM physics phenomena. This can involve optimizing parameters such as the learning rate, the regularization strength, (exclusively for the NNs) the number of layers, the number of neurons per layer, (exclusively for the BDTs) the number of trees, and the tree depth. The second and third part of this chapter will be just about optimization for the NNs and BDTs respectively.

## 7.1 The datasets

The way we are making datasets in this project, to keep it as close to model independent as possible, will be of the following format

- Make a dataset with all the SM backgrounds and one DM model.
- Make a dataset with all the SM backgrounds and all the DM models, divided into different signal regions and statistically combine the results of each signal region

The idea behind the first one is to start with a model dependent approach, where we train an ML algorithm to learn just one model at a time. **Question: I do not know which of the following I should include as a reason for the first one**

- The reason for taking this approach and not just having one dataset with all the models included, which would indeed make it a model independent approach, is because of the different phenomenology and experimental signatures of the models we are studying. **Question: Should I give concrete examples on how SUSY vs Z' differs, or is this sentence enough?**
- The reason for taking this approach, is because it is still closer to being more model independent than normal ML HEP searches, as these usually train on the whole SM background dataset with just one signal model with fixed masses and parameters. While what we would be doing is combining all the different masses and parameters into one.

For the second one, even if we were to include models with different signatures it would work out in our favor. For example, if we created Signal Regions (SR) in different regions of the  $m_{ll}$  phase space, *and* trained an ML network in each respective SR, then the network would learn the DM resonance appearing in each area, instead of learning the model resonance. Indeed, achieving model independence. Furthermore, the plan is to combine the results of each respective region to get an overall view of all of Run II.

In this project we will look at real and simulated data from the ATLAS detector from all running periods of Run II. This is from period *a, d* and *e* each with an integrated luminosity of 36.4, 44.3 and 58.5  $fb^{-1}$  respectively. In Table 7.1 we can see the overall number

of MC samples and expected events for all background channels as well as DM models. In addition to using the features in Table 6.6, we will also include the EventID, dataset ID, period, dilepton final state, label telling us whether an event is signal or background and the *weight* of each event.

Table 7.1: Table showcasing the number of MC samples and expected events for every background channel and DM model that will be used in this thesis.

\* The expected number of events for any BSM model has prefixed assumptions about for example cross-section, decay width, etc. As we do not empirically know if any of these assumptions are correct, these are not set in stone.

Channel	MC samples	Expected events
W	38,684	5,436.3
Drell Yan	47,201,697	2,198,257.6
TTbar	28,126,697	978,530.8
Single top	729,624	93,898.5
Diboson	10,983,689	116,653.5
Standard model total	87,080,391	3,392,776.7
$Z'$ Dark Higgs Heavy Dark Sector	498,621	*54.92
$Z'$ Dark Higgs Light Dark Sector	892,365	*155.37
$Z'$ Light Vector Heavy Dark Sector	521,759	*39.82
$Z'$ Light Vector Light Dark Sector	470,352	*235.70
$Z'$ Effective Field Theory Heavy Dark Sector	715,409	*0.0004
$Z'$ Effective Field Theory Light Dark Sector	640,963	*0.0007

### 7.1.1 Weights

The weights are crucial for most of what is to come further in this thesis. The weights only apply to MC simulations and can be interpreted as corrections to simulate real data, which is why the MC samples and expected events on Table 7.1 differ, where the latter has applied weights. The weights on this project are defined as Eq. (7.1)

$$W = w_{mc} \times w_{pu} \times w_{xs} \times w_{lsf} \times w_{nlo,ew} \times w_{ttbar} \times w_{jet} \times w_{bjet} \times \frac{\text{lumi}_{period}}{\sum w_{mc,DSID}} \quad (7.1)$$

This equation has a lot of information in it, so every part of this will be discussed. Starting from the raw MC weight,  $w_{mc}$ , which gives the relative probability of an event within a sample [44], the pile-up weight  $w_{pu}$ , is a weight used to correct object reconstruction as it can be possible for multiple objects to cross on the identification process. [47]

The cross-section weight  $w_{xs}$ , defined as  $w_{xs} := xs \times w_{kf} \times g_{eff}$  where  $xs$  is the cross-section of the process,  $w_{kf}$  is the  $k$ -factor which tries to correct for the absence of these higher-order term, for more details we refer the reader to the study done by Catani et al. [48].  $g_{eff}$  is the filter efficiency, which is the expected fraction of MC events that pass through the generator criteria.

The Lepton and trigger Scale Factor (LSF),  $w_{lsf}$ , which are applied in order to correct for differences in reconstruction in MC with respect to data, the Next to Leading Order (NLO) electroweak correction  $w_{nlo,ew}$ , which corrects for higher order EW diagrams, for more details we refer the reader to the paper by Denner et al. [49].

The  $w_{t\bar{t}bar}$ ,  $w_{jet}$  and  $w_{bjet}$ , which are reconstruction corrections for  $t\bar{t}$  [50], jets [51] and b-jets [52], respectively. And lastly the luminosity of the period, meaning

$$\text{lumi}_{period} = \begin{cases} 36.4 \text{ fb}^{-1}, & \text{for period = a} \\ 44.3 \text{ fb}^{-1}, & \text{for period = d} \\ 58.5 \text{ fb}^{-1}, & \text{for period = e} \end{cases}$$

divided by the Sum Of Weights (SOW),  $\sum w_{mc}$  of every sample for each dataset ID.

### 7.1.2 Signal regions

As a first step towards achieving model independence we will create three Signal Regions (SR). The goal is then to train one network in each respective SR that contains all models we wish to study. The SR we will study are defined below

- SR1:  $m_{ll} > 110$  GeV and  $E_T^{miss} \in [50, 100]$  GeV
- SR2:  $m_{ll} > 110$  GeV and  $E_T^{miss} \in [100, 150]$  GeV
- SR3:  $m_{ll} > 110$  GeV and  $E_T^{miss} > 150$  GeV

where the  $m_{ll}$  cut is made such that we remove as much background as possible before training<sup>1</sup> and where the MET regions are orthogonal. The goal of having kinematically

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<sup>1</sup>As the models we are studying start with  $m_{Z'} = 130$  GeV, see Chapter 6.2

orthogonal SRs when training is for the ML network to learn *DM resonant physics* in each respective region, rather than learning the *model in the dataset*.

### 7.1.3 Train and test split

When training our networks we will use 80% of the dataset, the remaining 20% will be used to test whether the networks are learning any physical patterns or learning the dataset. When splitting the datasets however, we need to be absolutely certain that the distributions follow the same shape and have the same ratio of background channels as well as having good MC and data agreement. In this thesis we will utilize a function from `scikit learn` [53] called `train_test_split` which can easily split our dataset into a training and testing set of our size, while also sorting the label of the event. Another benefit of using this function is that it has included a random seed such that we can always split the datasets in the same shape.

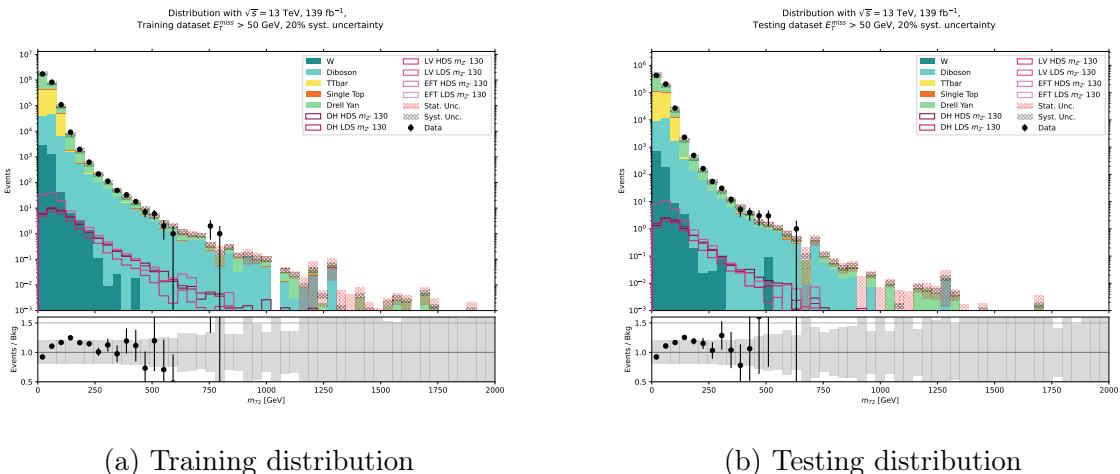


Figure 7.1: Train and test distribution of the stransverse mass when dividing SM background and DM samples into 80% and 20% datasets. The integrated luminosity for each distribution is 80% and 20% of  $139 \text{ fb}^{-1}$  respectively

In Figure 7.1 we can see that the distribution remains the same when we split the dataset into 80-20, where we also see the data and MC agree. To see the distribution of every other kinematical variable see the GitHub repo<sup>2</sup>. In addition to splitting the data, when making validation plots (See Chapter 5.3.4), when plotting MC simulations and real data, we need to make sure that the luminosity of the plot is correct. That means that if we

<sup>2</sup>Available here: [https://github.com/rubenguevara/Master-Thesis/tree/master/Plots/Data\\_Analysis/train\\_test\\_split](https://github.com/rubenguevara/Master-Thesis/tree/master/Plots/Data_Analysis/train_test_split)

are plotting the network score in the test dataset, as this is 20% of the whole dataset we need to scale everything with a factor of 5, so we get back to 100% and the full luminosity of Run II.

## 7.2 Neural Network Training

For this thesis we utilize `TensorFlow v. 2.7.1 GPU` for all NNs. After creating the dataset, the first and most important thing is to marinate the `batch_size` whenever we try anything while using the dataset. This is because of both the size of the dataset and because of the imbalance between signal and background, as explained in section 5.1.2 and as seen in Table 7.1.

The highest possible batch size that could be used for this thesis was  $2^{24}$ <sup>3</sup>, leading to roughly 17 million samples per batch. This is the best that a dedicated GPU, NVIDIA A100-PCIE-40GB, could handle. The batch size also decreases the more complex the NN becomes, as this requires greater computational power.

With this out of the way there are still a few problems to solve to optimize our NN. These are described below.

### 7.2.1 Padding of data

There are two difficulties to overcome when utilizing NNs as compared to BDTs. The hardest to solve, as a reliable solution seems not to exist yet, is the padding of jagged arrays (see Chapter 6.7.1). Padding is the process of filling missing values of a dataset entering a network. This problem doesn't usually appear in other fields than high energy particle physics. To recapitulate what was done in Chapter 6.7.1, the problem arises when the size of some features is not constant. This is the case of number of jets in an event. When creating the dataset the missing values of  $p_T$  and  $m_{jj}$  were set to zero, while the missing values of  $\eta$  and  $\phi$  were set to -999.

As mentioned before, there is no consensus of how the padding should be done, and there are many methods of doing so. The classical data scientist way of solving this problem would be to just take the mean of every feature and use that as a variable for every event with missing values. That means replacing every  $p_T, m_{jj} = 0$  and  $\eta, \phi = -999$  with

---

<sup>3</sup>It has to be a power of two because of the alignment of virtual processors (VP) onto physical processors (PP) of the GPU. As the number of PP is often a power of 2, using a number of VP different from a power of 2 leads to poor performance.

the mean of every  $p_T$ ,  $m_{jj}$ ,  $\eta$  and  $\phi$  (excluding the 0's and -999's respectively). However, this is not popular among physicists since it breaks conservation laws when we say there are jets present in an event when in reality there are none. Another approach is to use Bayesian statistics or ML to estimate the missing values, these options will not be pursued in this thesis due to time, but might be of interest for future projects. Another approach, is setting all the missing values to zero, as this might mean that there isn't anything there, but this also breaks conservation laws since  $\eta, \phi = 0$  have physical meaning, this is also highly looked down upon by data scientists since this could affect the weighting when training the network and potentially create a false pattern for the network to follow which would lead to a bias.

The jet  $p_T$  and  $m_{jj}$  being 0 is a valid form of padding the dataset, as this doesn't break any fundamental law of physics. However, setting  $\phi$  as something outside  $[-\pi, \pi]$  doesn't make much sense as this is the angle around the detector. Setting a high value of  $|\eta|$  might be physically possible (in the future) but as of today the ATLAS detector has a  $|\eta| < 4.9$  (see Chapter 4.2) as the pseudorapidity states how close to the beam line the objects recorded are. However, having a  $p_T$  of a jet equal to zero while still recording the  $\eta$  and  $\phi$  breaks the laws of physics, so this is a problem that needs to be fixed.

Another approach that will not be pursued in this thesis, would be to just remove all events that have a missing value completely getting rid of the problem, but this reduces the statistics of the dataset which is not desired when searching for new physics, and more importantly completely removes the kinematical distributions that is present in the SM, meaning the NN would learn wrong physics. One could also just remove the features with missing values to conserve statistics, albeit make it harder for the network to see any pattern that we might miss, but this is also not a desirable mitigation.

Instead, we have tried to create new kinematic variables that work around the need of padding. These features are just *counting features*, meaning that we count the number of jets that fulfill some criteria, such as the number of b-jets with  $p_T > 20$  GeV, the number of light jets with  $p_T > 40$  GeV, the number of jets recorded in the central calorimeter ( $|\eta| < 2.5$ ), and the number of jets with  $p_T > 50$  GeV recorded in the forward

calorimeter ( $|\eta| > 2.5$ ). The  $p_T$  cuts are optimized to allow a good agreement between data and simulations, the full distributions with different cuts in the control region can be seen in Appendix D. A summary of these variables is shown in Table 7.2.

To come

Table 7.2: Table showcasing plausible kinematic variables that will not need padding.

Kinematic variable	Feature name
Number of b-jets with $p_T > 20$ GeV	n_bjetPt20
Number of light-jets with $p_T > 40$ GeV	n_ljetPt40
Number of jets recorded in Central calorimeter	n_jetsetaCentral
Number of jets recorded in Forward calorimeter with $p_T > 50$ GeV	n_jetsetaForward50

When training our NN with these new variables instead of dropping features with missing variables we hope that the NN learns more physics by hopefully recognizing patterns between all high level features.

### 7.2.2 Normalization of data

Moving onto the second problem, which is not as problematic as the previous one, namely the normalization of data. Since neural networks send a lot of data into multiple neurons and multiple layers using activation functions and carrying weights and biases that change for every back propagation iteration, it is important to make sure that a neuron output doesn't die when moving around the network. Meaning that a neuron output becomes insignificant compared to others when navigating the loss-phase space. A fast way for neurons to die off is to not normalize the data and send it through the network as it is available. The reason it might die is because we send in numbers which vary significantly to each other, i.e. the  $p_T$  might be as high as thousands GeV, while  $E_T^{\text{miss}}/\sigma$  might be as low as 0.1. What might happen when sending such different numbers is that the network might think "obviously the high number is more important than the low number" thus making the activation function worse for the feature, even though this feature is of high importance when looking at MET final states. A way to fix this problem is to normalize all features. There are many ways to do this, one could do *min max scaling* which normalizes every feature from  $[0, 1]$ , completely solving the problem above. Mathematically speaking

this is done by

$$X_{norm} = \frac{X - X_{min}}{X_{max} - X_{min}} \quad (7.2)$$

Where  $X$  is the array containing all events for a given feature, while  $X_{min}$  and  $X_{max}$  are the lowest and highest values in the said array. Another way to normalize the data is to make the mean of the data 0 and the standard deviation to one, this is called *Z-score normalization*

$$X_{norm} = \frac{X - \bar{X}}{\sqrt{\sigma_X^2}} \quad (7.3)$$

where  $\bar{X}$  is the mean of said array and  $\sigma_X^2$  is the variance. One could also use pre-built functions in TensorFlow that provide a normalization, such as `Batch_normalization` which normalizes the data entering the network per batch. This is usually used in Convolutional NN's as it improves computational speed. Another one, `Normalize`, provides the same as Eq. (7.3) for the whole training set going in. This is however computationally heavy to use. The `Layer_normalization`, which normalizes the activations of the previous layer in a batch *independently*, rather than *across* a batch like `Batch_Normalization`. Both `Batch_Normalization` and `Layer_Normalization` use an optimized version of the Z-score when normalizing the data, meaning that all the features take are normalized such that the mean value becomes 0 and the fluctuations are  $\pm 1$ .

There is a big difference when normalizing data ourselves or using TensorFlow. TensorFlow remembers how the data was normalized when training such that the test data will be normalized the same way, making testing easier. While if we use Eq. (7.2) or Eq. (7.3) ourselves, we have to make sure that we use the same values for  $X_{max}$ ,  $X_{min}$ ,  $\bar{X}$  or  $\sigma_X^2$  when normalizing the test data.

### 7.2.3 Balancing of signal and background

A big problem that needs to be addressed in this thesis is what we should use as sample weights (see Section 5.3.2). If we were to not use any form of sample weights to mitigate the imbalance in our data set it could potentially lead *majority class classification* where the networks could get "lazy" and guess that everything is background.

To combat the majority class classification, we will as mentioned make use of the sample

weights. We will study three cases

1. Unweighted training, meaning that we will be setting the sample weight to one
2. Weighted training, meaning that we will be setting the sample weight to the weights used to re-weight MC events to expected events explained in Chapter 7.1.1
3. Balanced training, where we will make set the weight of all signal events to one, while weighing down the background by the ratio of signal events divided by background events,  $\frac{N_{sig}}{N_{bkg}}$

where the latter would in terms of weights mimic a 50-50 distribution of signal and background. To test the different balancing methods we will use a dataset containing only SM processes from Table 7.1, and train a network to single our the  $W$  channel from the other SM backgrounds as this has the lowest statistics. Meaning that it more accurately mimics our low statistics DM signal from Table 7.1 that gives rise to the dataset imbalance.

#### 7.2.4 Re-weighting MC to expected events

Even if the weighting method previously described might help the NN give us better results, we also want to include the weights used to re-weight MC events to expected events. This is desirable in the sense that we want to show our ML networks the true kinematical distributions of each feature. As the re-weighting weights are generated with simulation corrections as well as luminosity and cross-section in mind, it is heavily desirable to also apply these corrections when training our networks, such that it can correctly predict new events regardless of their weight. This is especially crucial when using real data on our predictions, as these have no weights.

Ideally one would take into account both the data imbalance between the signal and background as well as the re-weighting weights when training a network. To do this using TensorFlow we could make use of two parameters when training the network: `class_weight` and `sample_weight`. `class_weight` works as a dictionary that weighs events that have the same keys as the dictionary. For our purposes we could make a dictionary where we weigh signal and background events differently, this could be the

same type of scaling that was done in the previous section. `sample_weight` takes in individual weights for every single event that goes into the network, meaning that it is crucial that we know that the desired weight matches the desired event. Ideally we would use both weighting methods, `class_weight` to balance the signal to background ratio and `sample_weight` with the re-weighting weights. However, there is a bug in TensorFlow (up to version GPU 2.7.1) that makes it, so the program doesn't run when using both parameters. This is not a big problem though, as when looking at the source code [54] one can see that what TensorFlow does with both weights is multiply them together.

For this thesis we tried testing four different methods to re-weight and balance the dataset, which expands further than the idea of point 3. in the previous section. Firstly all background events were re-weighted to expected events, and in addition we expanded the balancing ratio,  $\frac{N_{sig}}{N_{bkg}}$ , to be

1.  $\frac{N_{sig,MC}}{N_{bkg,MC}}$  where we weigh down all background events wrt. the number of MC samples
2.  $\frac{N_{bkg,MC}}{N_{sig,MC}}$  where we weigh up all signal events wrt. the number of MC samples
3.  $\frac{N_{sig,MC}}{N_{bkg,exp}}$  where we weigh down all background events wrt. the number of expected events
4.  $\frac{N_{bkg,exp}}{N_{sig,MC}}$  where we weigh up all signal events wrt. the number of expected events

Where we are not re-weighting the signal events to expected signal events when training because this would in principle remove all events from the NN as there are so few events (see Table 7.1). And also because the expected events of the signal take into account assumptions that are not empirically proven, such as the couplings, masses, decay widths, etc. Taken all of these factors into account what remains is to choose a network architecture and which hyperparameters to use to best fit our task.

### 7.2.5 Architecture and hyperparameter tuning

The architecture of the NN utilized in this project is of the form shown in Figure 7.2.

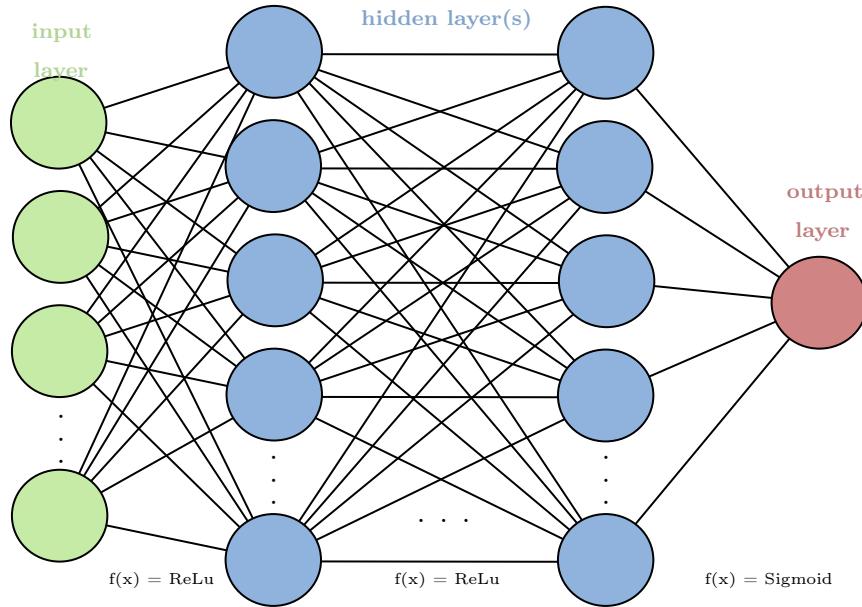


Figure 7.2: Architecture of the NN used on this thesis. The neurons on the hidden layer(s) is a hyperparameter, as well as the number of hidden layers.

Making this type of NN using `TensorFlow` is easy. An algorithm showing one of the possibilities can be seen in Algorithm 7.1.

Algorithm 7.1: Neural network definition using TensorFlow

```

1 import tensorflow as tf
2 from tensorflow.keras import layers
3
4 def Neural_Network(inputsize , n_layers , n_neuron , eta , lamda):
5
6     model=tf.keras.Sequential()
7
8     for i in range(n_layers):
9         if (i==0):
10             model.add(layers.Dense(n_neuron , activation='relu' , kernel_regularizer=
11                         tf.keras.regularizers.l2(lamda) , input_dim=inputsize))
12         else:
13             model.add(layers.Dense(n_neuron , activation='relu' , kernel_regularizer=
14                         tf.keras.regularizers.l2(lamda)))
15
16     model.add(layers.Dense(1,activation='sigmoid'))
17
18     opt=tf.optimizers.SGD(learning_rate=eta) # or Adam!
19
20     model.compile(loss=tf.losses.BinaryCrossentropy() ,
21                   optimizer=opt ,
22                   metrics = [tf.keras.metrics.BinaryAccuracy()])
23
24     return model

```

To get the best performance on our NN, we need to find which hyperparameters help the

network reach the highest significance. To do this, we need to do a grid search. For our neural network we will mainly focus on four hyperparameters explained on section 5.1:

- The learning rate  $\eta$
- The L2-regressor variable  $\lambda$
- The number of neurons on each hidden layer `n_neuron`
- Possibly the number of layers `n_layers`, excluding the output. Meaning that `n_layers = 1` means no hidden layer

The metrics that will be used to estimate the best hyperparameters are AUC, binary accuracy and most importantly the expected significance<sup>4</sup>. The expected significance for this section has been calculated using the low statistics formula Eq. (4.20) without uncertainties. The expected significance will also be calculated when making a cut on 0.85 on the network prediction score, as explained in Chapter 5.3.5. Meaning we will only look at events which the network rates as signal with 85% confidence and above. For some models where the expected events are too low (EFT models), meaning that the expected significance will be 0 or NaN, if this happens we will use the hyperparameters of the network which gives us the highest AUC on the testing set. This will procedure will be done for every single network we will explore.

---

<sup>4</sup>See Chapter 5.3 for explanation of metrics.

## 7.3 Boosted Decision Tree Training

When working with BDTs we do not run into as many problems as we do with NNs. For example the padding and normalization of data can be completely avoided, making the whole procedure a lot easier when one uses exotic data as we do in high energy particle physics. The weights are still an obstacle that needs to overcome when using BDTs. This will be discussed in the next section.

For this project we will as mentioned utilize the eXtreme Gradient Boosting, or `XGBoost` for short, package [38] made for the Higgs ML Challenge [37] whenever we mention BDTs. This project utilized version 1.5.0 without GPU adaptability. `XGBoost` also helps to avoid padding as it is integrated with a `missing_variable` variable where we can simply write the number of the variable that is missing.

### 7.3.1 Sample weights

For `XGBoost` there is a different problem when it comes to weights. `XGBoost` has a variable called `scale_pos_weight` where we can help the network deal with imbalanced data, such as the one we have. Meaning that the whole problem of combining the re-weighting weights with the balancing weights from Chapter 7.2.4 completely disappears. Albeit there is a caveat, `XGBoost` does not have the possibility to include negative weights, which this dataset has. The reason `XGBoost` does not include weights, is because when calculating the number of events in a leaf node, which is made by taking the sum of sample weights, we cannot have a negative value [55, 56]. As for the MC generators, Sherpa [42] takes into account higher order diagrams and needs to add negative weights to "counter" the over counting of diagrams [57], which are important to correctly scale the simulated events to real data. In the future this might no longer be a problem as future MC generators might only have positive weights.

A method to mitigate this problem is to use the absolute value of the weights when training. This is however not generally accepted as a solution, and some even say it should be avoided. There are other options however, one of these options is to not include events with negative weights on the training set. This is an okay thing to do, as we

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to this  
other than  
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words...

can imagine that if we were to only include events with positive weights on the training, it might be the same as putting the negative weights on the "testing dataset" (Chapter 7.1.3).

Another one that has been used on a published ATLAS (internal) article (chapter 9.3) [58] is to normalize the weights when using the absolute value with respect to the sum of weights over the sum of absolute weights. The reason behind this is that the sum of weights is obviously not the same when we take the absolute value. Mathematically speaking, if we have an array of weights  $W$ , we can update this like

$$W \rightarrow |W| \frac{\sum_i W_i}{\sum_i |W_i|} \quad (7.4)$$

such that the weights are at least in the same scale.

### 7.3.2 Architecture and hyperparameter tuning

Making a BDT for our purposes is fairly easy as well using XGBoost. One way to do it is using the code below in Algorithm 7.2

Algorithm 7.2: Boosted Decision Tree definition using XGBoost

```

1 import xgboost as xgb
2
3 Boosted_Dcision_Tree = xgb.XGBClassifier(
4     max_depth,
5     use_label_encoder=False,
6     n_estimators,
7     learning_rate,
8     reg_lambda,
9     predictor = 'cpu_predictor',
10    tree_method = 'hist',
11    scale_pos_weight = sow_bkg/sow_sig,
12    objective = 'binary:logistic',
13    eval_metric = 'auc',
14    min_child_weight = 1,
15    missing = -999,
16    random_state = 42,
17    verbosity = 1)

```

To get the best performance on our BDT we have to do a grid search here as well. The trainable hyperparameters here are different from NN's, with XGBoost we will focus on the following hyperparameters

- Tree depth: how many times we split the data
- Number of estimators: how many trees we use to do the gradient boosting

- The learning rate  $\eta$
- L2-regressor  $\lambda$ , to stop overtraining

The metrics that will be used to estimate the best hyperparameters are AUC, binary accuracy and most importantly the expected significance<sup>5</sup>. The expected significance for this section has been calculated using the low statistics formula Eq. (4.20) without uncertainties. The expected significance will also be calculated when making a cut on 0.85 on the network prediction score, as explained in Chapter 5.3.5. Meaning we will only look at events which the network rates as signal with 85% confidence and above. For some models where the expected events are too low (EFT models), meaning that the expected significance will be 0 or NaN, if this happens we will use the hyperparameters of the network which gives us the highest AUC on the testing set. This will procedure will be done for every single network we will explore.

---

<sup>5</sup>See Chapter 5.3 for explanation of metrics.



## Part III

## Results



# Chapter 8

## Model dependent approach

The results for the network optimizations can be seen in Appendix E, where it became apparent that the performance of BDTs is better at scoring a higher significance than NNs, and faster. Because of this and time constraints of this thesis we decided to compute the results of the model dependent and model independent search using BDTs only.

The time has come to test how our networks fare on learning our models. This chapter showcases the results of the method which we called the model dependent approach. This method trains one BDT for each model we have, including all the mass points and simulated samples, then we test how well the network has learned the model and create a mass exclusion limit for it.

To navigate through the process we will take a model as an example, the Dark Higgs Heavy Dark Sector model, and afterwards present the combined exclusion limits for every model. As all of our models had  $m_{Z'} = 130$  GeV as a lower limit, to reduce computational time we decided to make a cut of  $m_{ll} > 110$  GeV.

## 8.1 Walkthrough of method

We conducted a grid search to optimize the BDT and trained the network using 80% of the SM background samples and 80% of every different  $Z'$  mass sample of the model. Using this approach for this model gave the features in Figure 8.1 as the most important ones. The most important variables here are the ones which we expect to be important on a dilepton and MET final state.

To showcase how the network sorts signal from background we can see the validation plots in Figure 8.2 showing all the signal samples which can be seen down to  $2 \times 10^{-3}$  expected events. The reason for this limit is arbitrary and was chosen for aesthetics.

While the validation plot might seem like the network is not doing an impressive job at sorting signal from background, we can actually see how well the network learns the different mass points by looking at the ROC curves for each mass point, this is shown in Figure 8.3. Here we see that the network struggles a tiny bit to learn the models with lowest  $m_{Z'}$ , but the AUC score is still 0.96, meaning that it actually learned to sort the signal from SM background.

To define the region we will use to make any exclusions we can choose the validation plot bin that gives us the highest significance, this can be seen in Figure 8.4 for a few mass points (to not drown the plot). From this we see that we get at best an expected significance of approximately  $0.7\sigma$  (without uncertainties), even though the network got an AUC score of 0.96 for the mass point on the muon channel. From this we can *conclude* **Question: is this word way too harsh?** that it is the re-weighting using the cross-section that punishes the performance of our networks. This is something that will follow for every result.

As the last bin has the greatest significance, we can effectively make a cut based on the BDT score. Counting the number of events on this last bin, as well as their uncertainties we can calculate a mass exclusion for both electron and muon channel. Following the method explained in Chapter 4.3.2 using the values in Table F.1 we can create a mass exclusion for each leptonic channel. The results can be seen in Figure 8.5.

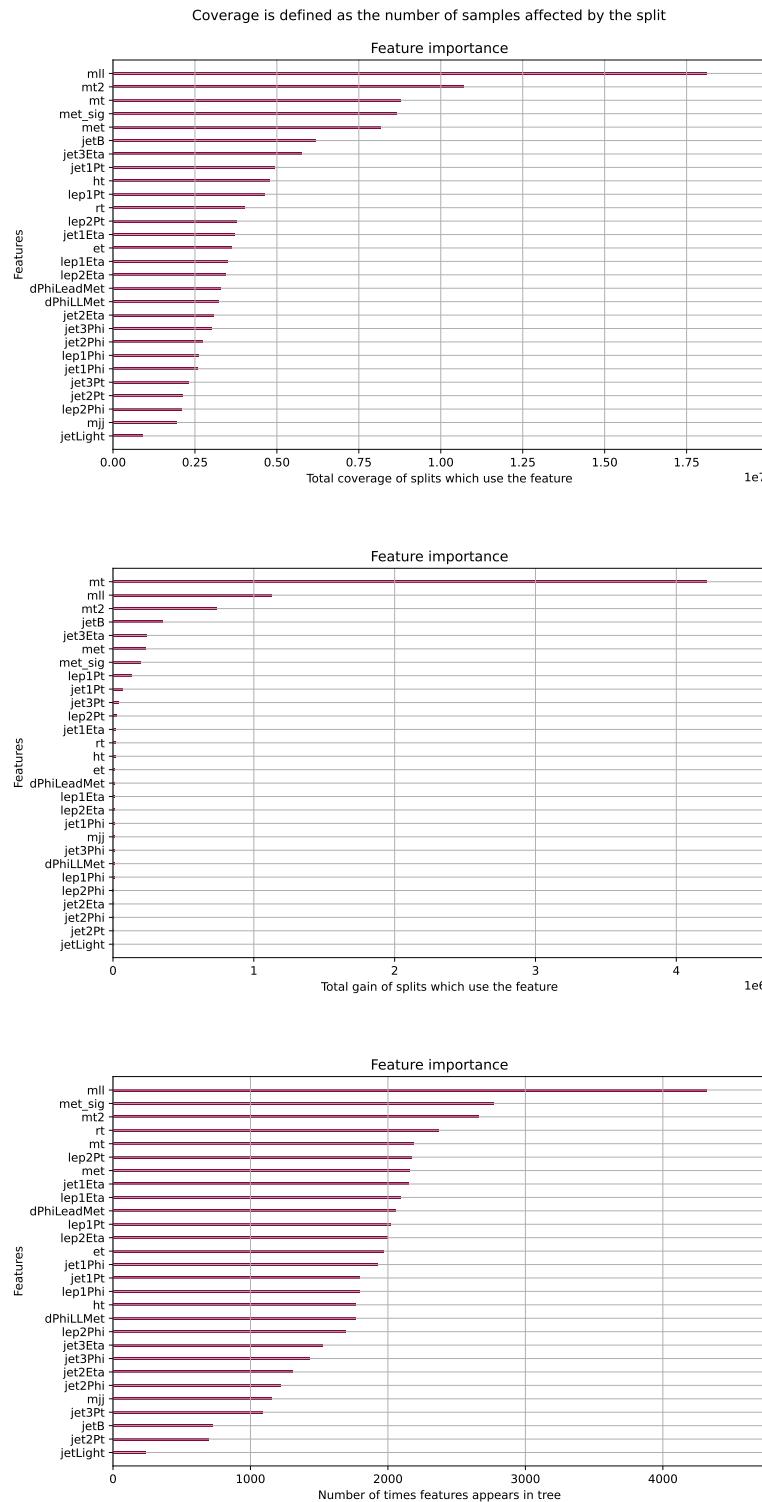
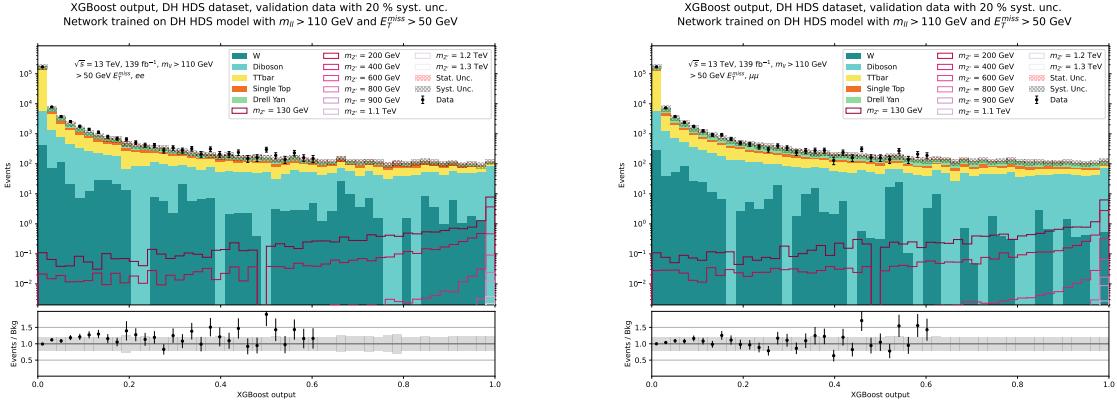
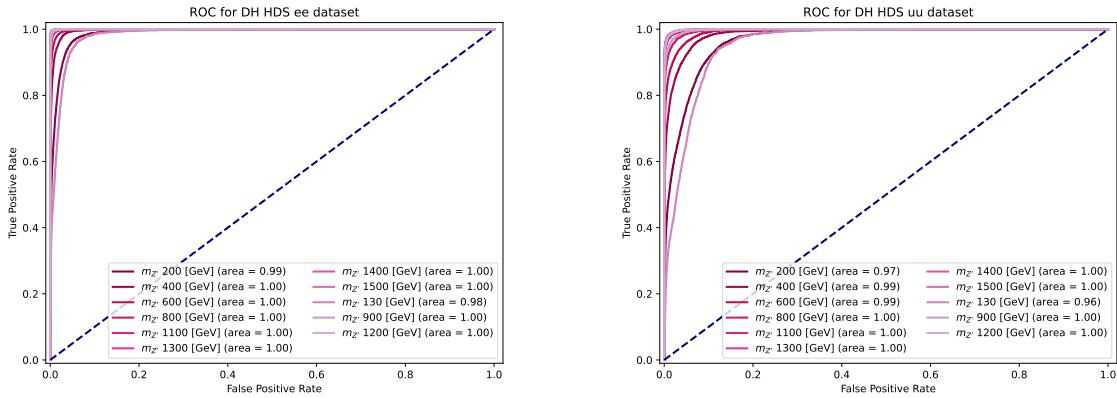
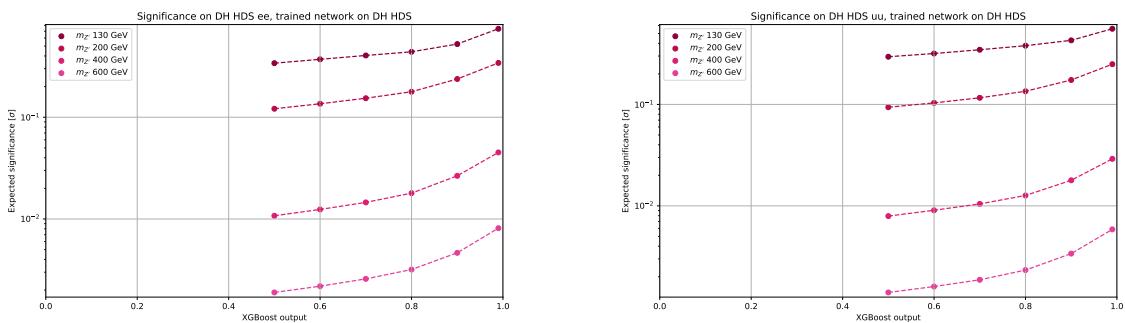


Figure 8.1: Feature importance for network trained on  $Z'$  DH HDS

Figure 8.2: Validation plots for network trained on  $Z'$  DH HDSFigure 8.3: ROC plots for every  $Z'$  mass point on network trained on  $Z'$  DH HDSFigure 8.4: Expected significance plots for  $Z'$  mass points on network trained on  $Z'$  DH HDS

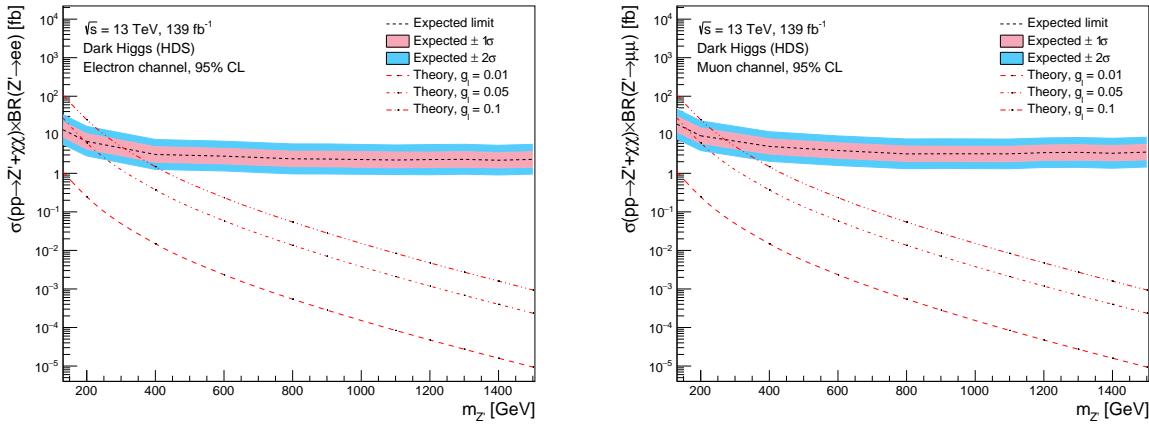


Figure 8.5: Mass exclusion limits of  $ee$  and  $\mu\mu$  channel for all  $Z'$  DH HDS model

We can furthermore statistically combine both of these results to get the exclusion on a general dilepton final state. Following this method for all other five models<sup>1</sup> we can get the results in Figure 8.6.

One thing to note about the mass exclusion limits above, is that as the lepton coupling for all models being tested was chosen to be  $g_l = 0.01$ , we decided to include how the limits would look if we increased this coupling to  $g_l = 0.05$  and  $g_l = 0.1$ . Doing so we have assumed that the efficiency of the cuts stays the same, as well as the number of background events on the last bin. This assumption is noteworthy due to the fact that if we increased the lepton coupling constant of our model, this would increase the branching ratio of the leptonic decays. Meaning that when simulating the events we would have gotten more events. As one of the greatest challenges to overcome in this thesis was the imbalanced dataset, this fact would have helped mitigate the problem. In addition, a general rule of thumb in ML is that the more statistics one has when training a network, the better the network will learn. The point of this information is that by increasing the lepton coupling constant of the signal, the network might have a greater efficiency when learning, as well as reduce the number of background events on the last bin. However, due to time constraints on this thesis we did not have the chance to explore the possibility of simulating more events.

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<sup>1</sup>For more plots look at the GitHub repo: in [https://github.com/rubenguevara/Master-Thesis/tree/master/Plots/XGBoost/DH\\_HDS](https://github.com/rubenguevara/Master-Thesis/tree/master/Plots/XGBoost/DH_HDS) changing "DH\_HDS" for the model of interest

## 8.2 Mass exclusion limits for the combined channels

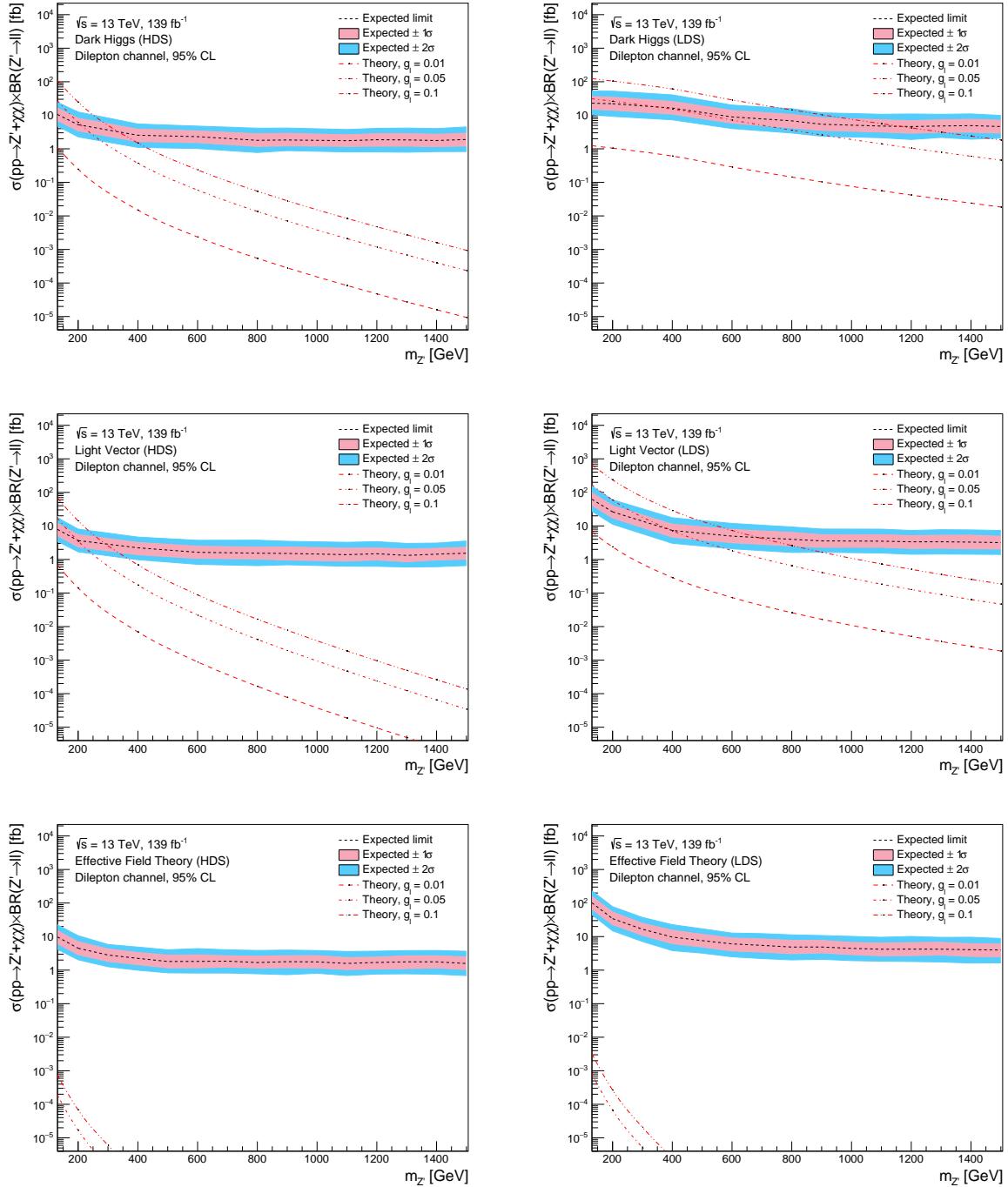


Figure 8.6: Mass exclusion limits of combined  $ee$  and  $\mu\mu$  channel for all models

# Chapter 9

## Model independent approach

The results for the network optimizations can be seen in Appendix E, where it became apparent that the performance of BDTs is better at scoring a higher significance than NNs, and faster. Because of this and time constraints of this thesis we decided to compute the results of the model dependent and model independent search using BDTs only.

In this chapter we will explore how three BDTs fare at learning the six models we have. These three BDTs were trained on a dataset containing 80% of all SM background events and 80% of all our signal events in orthogonal Signal Regions (SR). To recap the regions we have

- SR1:  $m_{ll} > 110$  GeV and  $E_T^{miss} \in [50, 100]$  GeV
- SR2:  $m_{ll} > 110$  GeV and  $E_T^{miss} \in [100, 150]$  GeV
- SR3:  $m_{ll} > 110$  GeV and  $E_T^{miss} > 150$  GeV

To compare this method to the previous method we will statistically combine the mass exclusions results for each SR for each final state in a model. To navigate through the process we will again take a model as an example, the Dark Higgs Heavy Dark Sector model, and afterwards present the combined exclusion limits for every model. All the results can be found in the GitHub repo<sup>1</sup>.

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<sup>1</sup>Available here: [https://github.com/rubenguevara/Master-Thesis/tree/master/Plots/XGBoost/Model\\_independent](https://github.com/rubenguevara/Master-Thesis/tree/master/Plots/XGBoost/Model_independent)

## 9.1 Walkthrough of method

Following the same method presented in Chapter 8.1. We start by looking at the feature importance of the network trained on SRs, this can be seen in Figure 9.1 where we show the feature importance using the *weight*<sup>2</sup> metric to not overflow the chapter. From these results we see that as hoped, **Question: can i say as hoped if I havent earlier explicitly said I hope this?** the variables that are of importance change in every region. Even though they change, they are all are the ones we expect from a dilepton and MET final state.

This time however we decided to show the validation plots, ROC curve and expected significance for every signal region of the model together. This can be seen in Figure 9.2, 9.3 and 9.4 for SR1, SR2 and SR3 respectively. Here we can again see how having different SRs changes the performance of the network.

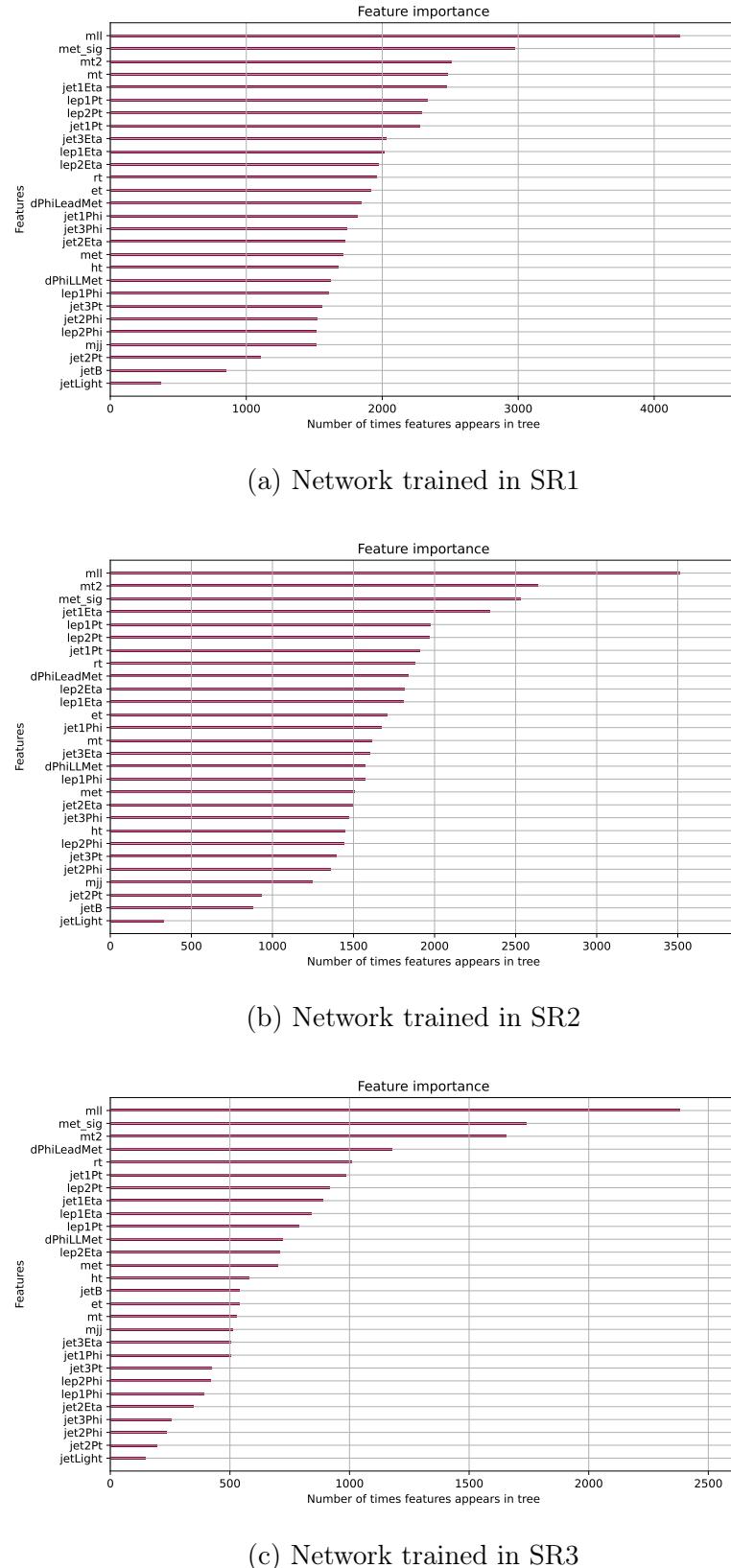
Using again the last bin of the validation set to make a cut on the dataset to make limits, we get the values seen in Table F.7, F.8 and F.9 for SR1, SR2 and SR3 respectively. Using these to compute limits for the electron and muon channel for every SR using the method explained in Chapter 4.3.2 we get the exclusion plots shown in Figure 9.5.

We can furthermore statistically combine the results for each SR such that we get the exclusion in Figure 9.6. Even further, we can statistically combine both of these results to get the exclusion on a general dilepton final state. Following this method for all other five models we can get the results in Figure 9.7.

Where again we assumed that we have the same efficiency and number of background events on the last bin when increasing the lepton coupling constant.

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<sup>2</sup>See Chapter 5.3.6 for definition

Figure 9.1: Feature importance for network trained on  $Z'$  DH HDS in all SRs

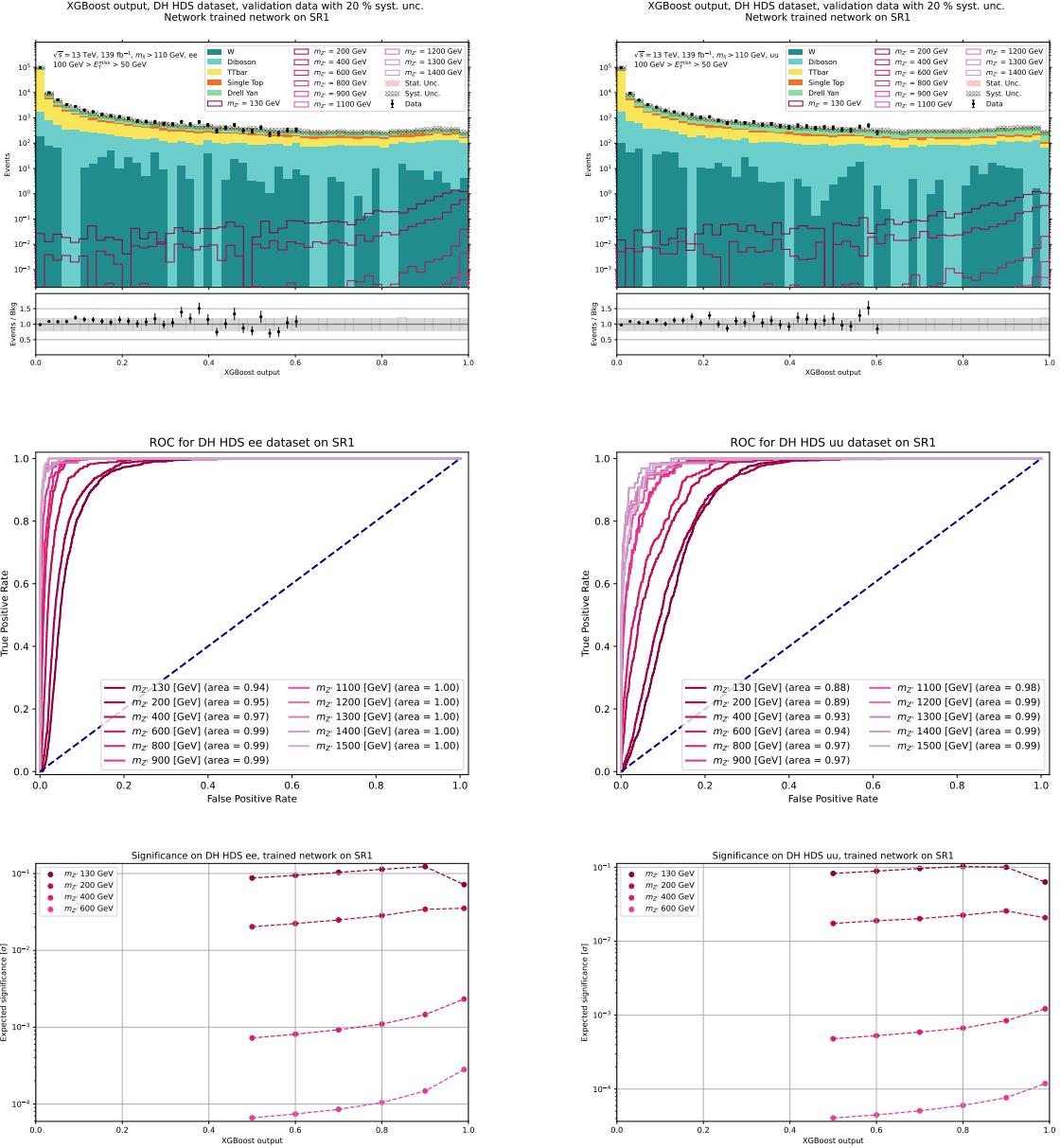
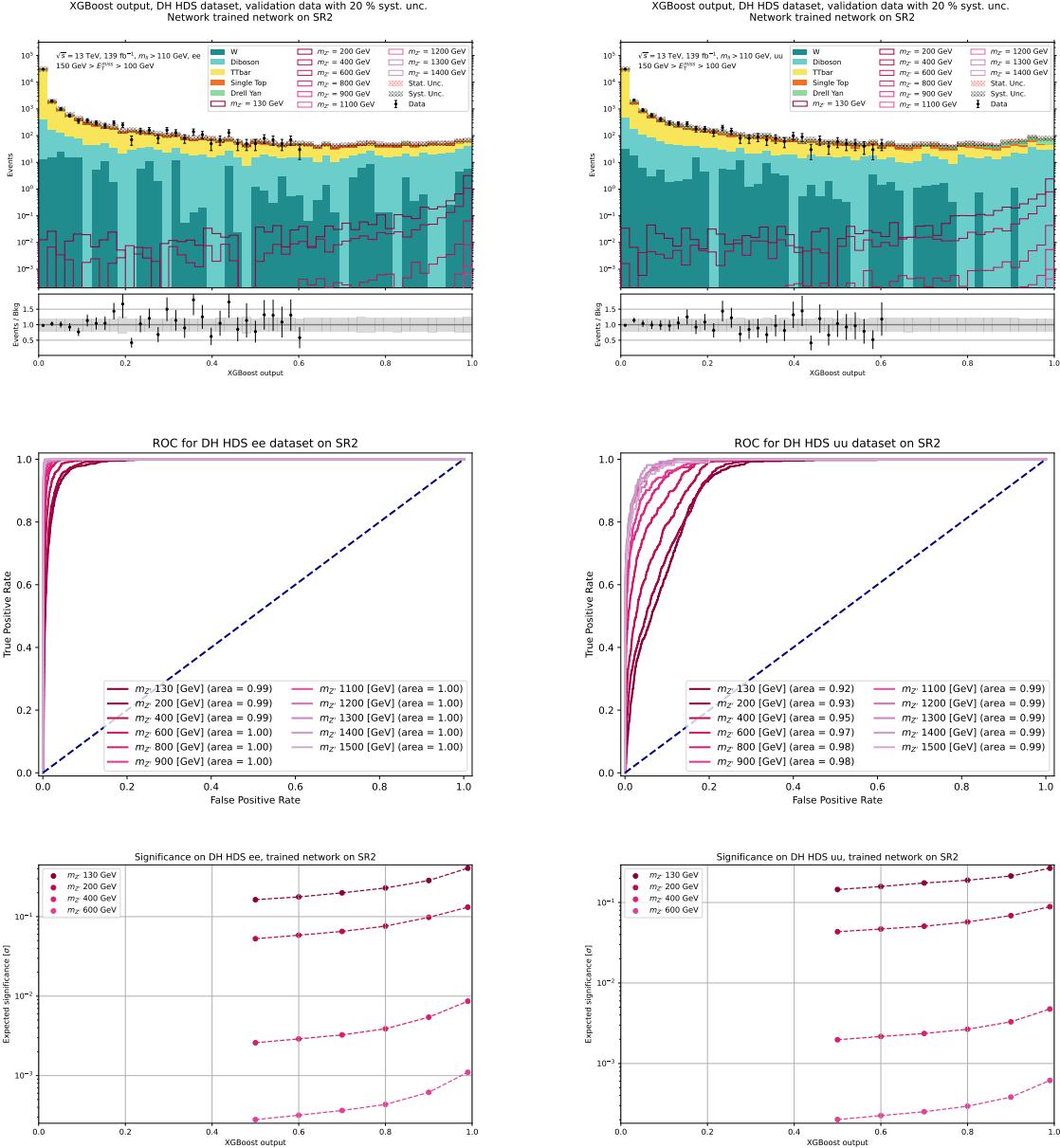
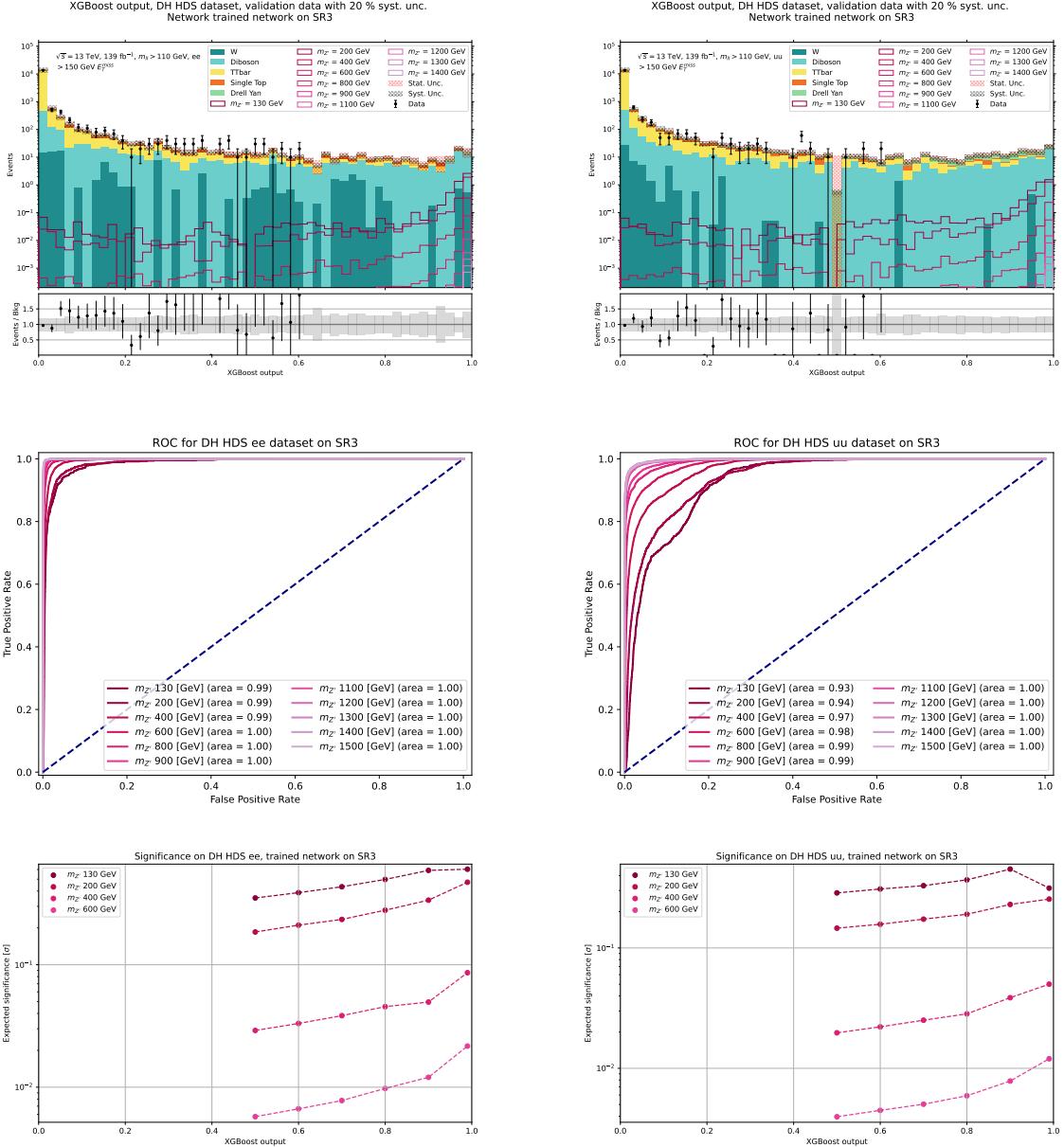


Figure 9.2: XGBoost results for DH HDS model on  $ee$  and  $\mu\mu$  channel in SR1

Figure 9.3: XGBoost results for DH HDS model on  $ee$  and  $\mu\mu$  channel in SR2

Figure 9.4: XGBoost results for DH HDS model on  $ee$  and  $\mu\mu$  channel in SR3

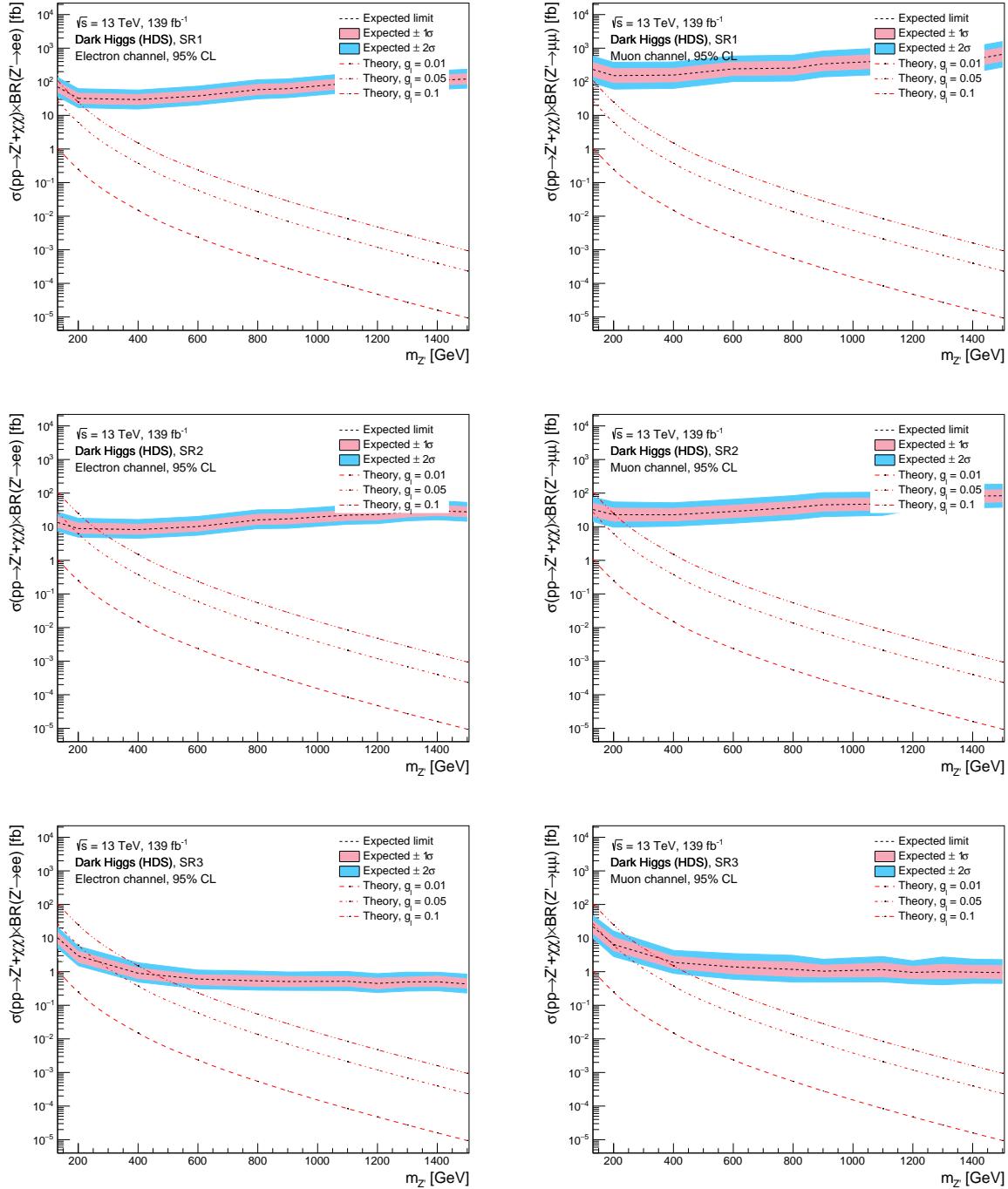


Figure 9.5: Mass exclusion limits results for DH HDS model on  $ee$  and  $\mu\mu$  channel in all SRs

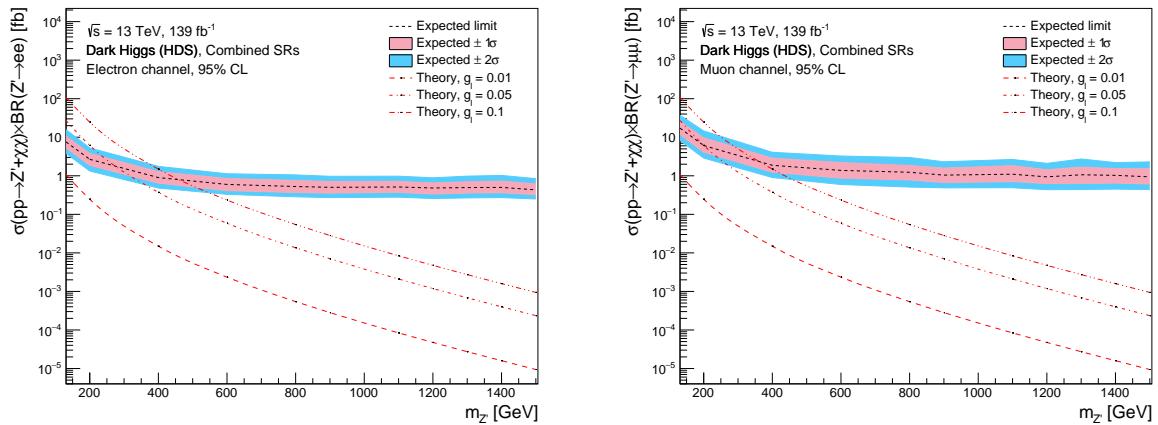


Figure 9.6: Mass exclusion limits results for DH HDS model on  $ee$  and  $\mu\mu$  channel in combined SRs

## 9.2 Mass exclusion limits for the combined channels

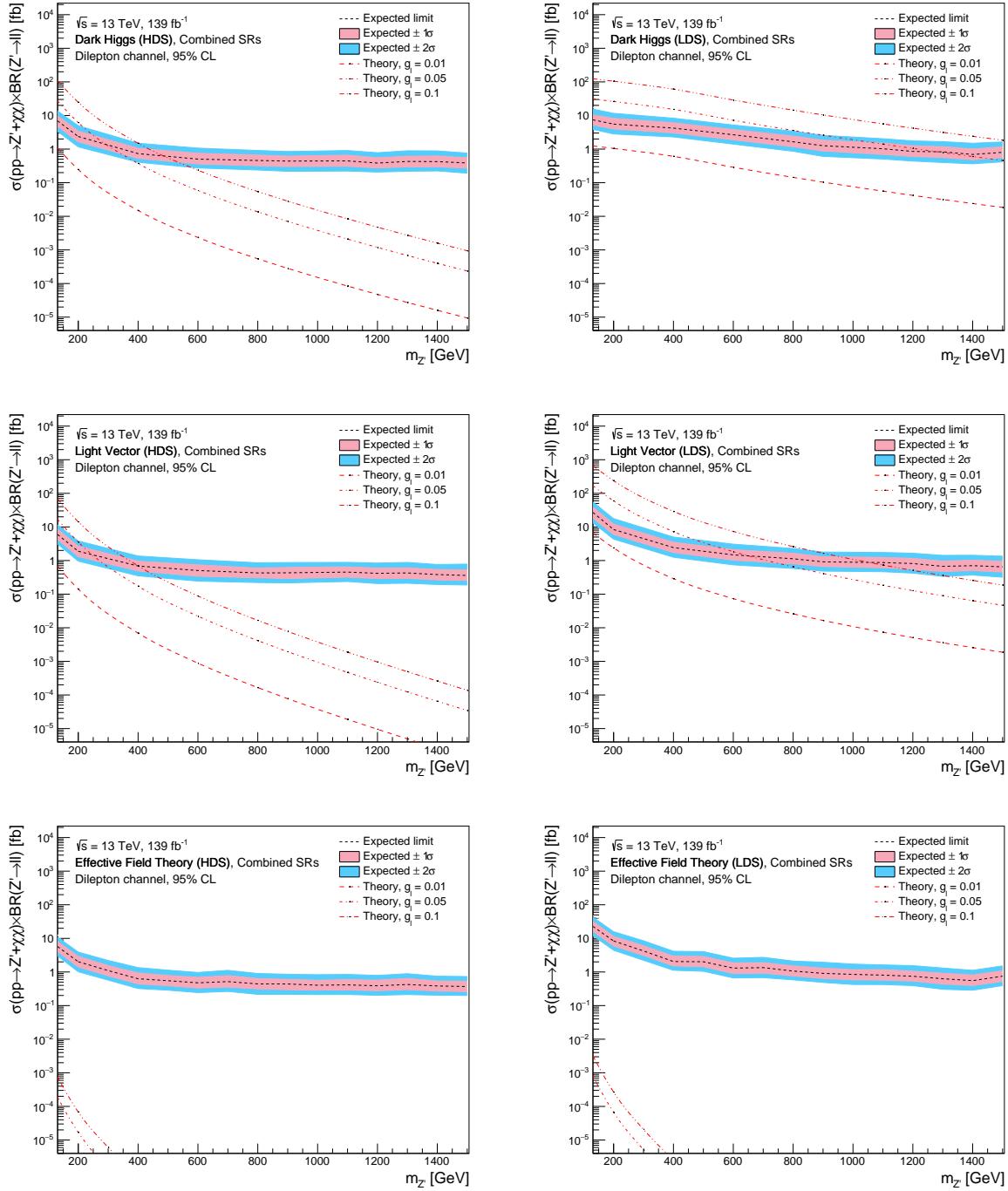


Figure 9.7: Mass exclusion limits of combined  $ee$  and  $\mu\mu$  channel for all models



# Chapter 10

## Conclusion

After exploring the intricacies of preparing both a NN and a BDT ML algorithm to learn a binary classification task of DM signal and SM background, we concluded, due to time, that a BDT ML approach was best suited for this search. The searches we conducted were made on three models all containing a new  $U(1)'$  vector boson,  $Z'$ , that can decay and couple to a DM WIMP candidate. The first one being  $Z'$  coupling to a new scalar boson  $h_D$ , which we call the Dark Higgs (DH) model. The second is an off-shell  $Z'$  decaying into two dark states  $\chi_1$  and  $\chi_2$ , where the latter decays again into a  $Z'$  and  $\chi_1$  which is the DM candidate, this we called the Light Vector (LV) model. The third model, is an inelastic Effective Field Theory model, which is similar to the LV model, with the exception being that there are no assumptions about the quark coupling to the  $Z'$ , we called this the EFT model. The three models were furthermore split into two groups, the difference being the mass of the DM candidate, we called these for the Heavy- and Light Dark Sector (HDS and LDS) for heavy and light DM respectively.

As the ultimate goal for the thesis was to test model independent approaches for new physics searches using ML, we first tested a less model dependent approach than is the standard in high energy physics today. This approach consisted of using a dataset with all the SM background processes with a dilepton and MET final state and one of the aforementioned models, including all the simulated  $Z'$  mediator masses<sup>1</sup>. To better the performance and computational time, we only looked at events with  $\text{MET} > 50 \text{ GeV}$ , and as the models tested had a lower limit of the mediator mass at  $m_{Z'} = 130 \text{ GeV}$ ,

---

<sup>1</sup>As the standard approach is to train using only one simulated mediator mass

we also only looked at events with  $m_{ll} > 110$  GeV. Then we trained one BDT for each model using this type of dataset. To test the results of this approach we computed mass exclusion limits using Bayesian statistics for every model.

The second approach consisted of a dataset containing all the DM models and all the SM background. The difference however was that we trained three BDTs in orthogonal MET spaces. All the networks only looked at events with, again  $m_{ll} > 110$  GeV, while the other three were divided into three MET regions, the first signal region (SR1) having  $E_T^{miss} \in [50, 100]$  GeV, the second signal region (SR2) having  $E_T^{miss} \in [100, 150]$  GeV, and the third signal region (SR3) having  $E_T^{miss} > 150$  GeV. After training the networks we tested each model by computing the same mass exclusion limit using Bayesian statistics in every respective SR. To compare this approach with the previous, we statistically combined the mass exclusion limit of all SRs into one combined SR.

Doing this for every model we observed that we were able to compute higher mass limits using the more model independent approach of dividing a dataset into different regions of kinematical phase space. While we had originally planned to test these methods using more DM models, such as the Mono-Z and SUSY, due to time we were not able to test if the model independent approach worked using more experimentally distinct models. For the future it would be interesting to see if this approach could be used to train less ML networks and still get good, if not better results as demonstrated by the few models in this paper, when conducting search for new physics which might get us closer to understanding more of spacetime.

# Appendix A

## Dataset IDs for MC samples

Table A.1: Drell Yan background MC samples

Dataset ID	Process
700320	Zee_maxHTpTV2_BFilter
700321	Zee_maxHTpTV2_CFilterBVeto
700322	Zee_maxHTpTV2_CVetoBVeto
700323	Zmumu_maxHTpTV2_BFilter
700324	Zmumu_maxHTpTV2_CFilterBVeto
700325	Zmumu_maxHTpTV2_CVetoBVeto
700326	Ztautau_LL_maxHTpTV2_BFilter
700327	Ztautau_LL_maxHTpTV2_CFilterBVeto
700328	Ztautau_LL_maxHTpTV2_CVetoBVeto
700452	Zee_mZ_120_ECMS_BFilter
700453	Zee_mZ_120_ECMS_CFilterBVeto
700454	Zee_mZ_120_ECMS_CVetoBVeto
700455	Zmumu_mZ_120_ECMS_BFilter
700456	Zmumu_mZ_120_ECMS_CFilterBVeto
700457	Zmumu_mZ_120_ECMS_CVetoBVeto
700458	Ztautau_mZ_120_ECMS_BFilter
700459	Ztautau_mZ_120_ECMS_CFilterBVeto
700460	Ztautau_mZ_120_ECMS_CVetoBVeto

Table A.2: Single top and TTbar background MC samples

Dataset ID	Process
410472	$t\bar{t}$ dilepton filtered
410644	Single top $s$ -channel (top)
410645	Single top $s$ -channel (anti-top)
410648	$W + t$ associated production dilepton filtered (top)
410649	$W + t$ associated production dilepton filtered (anti-top)
410658	Single top $t$ -channel (top)
410659	Single top $t$ -channel (anti-top)

Table A.3: Diboson background MC samples

Dataset ID	Process
363356	$Z \rightarrow qq + Z \rightarrow ll$
363358	$W \rightarrow qq + Z \rightarrow ll$
363359	$W^+ \rightarrow qq + W^- \rightarrow l\nu$
363360	$W^+ \rightarrow l\nu + W^- \rightarrow qq$
363489	$W \rightarrow l\nu + Z \rightarrow qq$
364250	$llll$
364253	$lll\nu$
364254	$ll\nu\nu$
364255	$l\nu\nu\nu$

Table A.4: W background MC samples

Dataset ID	Process
364156	$W \rightarrow \mu\nu$ maxHTpTV0_70_CVetoBVeto
364157	$W \rightarrow \mu\nu$ maxHTpTV0_70_CFilterBVeto
364158	$W \rightarrow \mu\nu$ maxHTpTV0_70_BFilter
364159	$W \rightarrow \mu\nu$ maxHTpTV70_140_CVetoBVeto
364160	$W \rightarrow \mu\nu$ maxHTpTV70_140_CFilterBVeto
364161	$W \rightarrow \mu\nu$ maxHTpTV70_140_BFilter
364162	$W \rightarrow \mu\nu$ maxHTpTV140_280_CVetoBVeto
364163	$W \rightarrow \mu\nu$ maxHTpTV140_280_CFilterBVeto
364164	$W \rightarrow \mu\nu$ maxHTpTV140_280_BFilter
364165	$W \rightarrow \mu\nu$ maxHTpTV280_500_CVetoBVeto
364166	$W \rightarrow \mu\nu$ maxHTpTV280_500_CFilterBVeto
364167	$W \rightarrow \mu\nu$ maxHTpTV280_500_BFilter
364168	$W \rightarrow \mu\nu$ maxHTpTV500_1000
364169	$W \rightarrow \mu\nu$ maxHTpTV1000_E_CMS
364170	$W \rightarrow e\nu$ maxHTpTV0_70_CVetoBVeto
364171	$W \rightarrow e\nu$ maxHTpTV0_70_CFilterBVeto
364172	$W \rightarrow e\nu$ maxHTpTV0_70_BFilter
364173	$W \rightarrow e\nu$ maxHTpTV70_140_CVetoBVeto
364174	$W \rightarrow e\nu$ maxHTpTV70_140_CFilterBVeto
364175	$W \rightarrow e\nu$ maxHTpTV70_140_BFilter
364176	$W \rightarrow e\nu$ maxHTpTV140_280_CVetoBVeto
364177	$W \rightarrow e\nu$ maxHTpTV140_280_CFilterBVeto
364178	$W \rightarrow e\nu$ maxHTpTV140_280_BFilter
364179	$W \rightarrow e\nu$ maxHTpTV280_500_CVetoBVeto
364180	$W \rightarrow e\nu$ maxHTpTV280_500_CFilterBVeto
364181	$W \rightarrow e\nu$ maxHTpTV280_500_BFilter
364182	$W \rightarrow e\nu$ maxHTpTV500_1000
364183	$W \rightarrow e\nu$ maxHTpTV1000_E_CMS
364184	$W \rightarrow \tau\nu$ maxHTpTV0_70_CVetoBVeto
364185	$W \rightarrow \tau\nu$ maxHTpTV0_70_CFilterBVeto
364186	$W \rightarrow \tau\nu$ maxHTpTV0_70_BFilter
364187	$W \rightarrow \tau\nu$ maxHTpTV70_140_CVetoBVeto
364188	$W \rightarrow \tau\nu$ maxHTpTV70_140_CFilterBVeto
364189	$W \rightarrow \tau\nu$ maxHTpTV70_140_BFilter
364190	$W \rightarrow \tau\nu$ maxHTpTV140_280_CVetoBVeto
364191	$W \rightarrow \tau\nu$ maxHTpTV140_280_CFilterBVeto
364192	$W \rightarrow \tau\nu$ maxHTpTV140_280_BFilter
364193	$W \rightarrow \tau\nu$ maxHTpTV280_500_CVetoBVeto
364194	$W \rightarrow \tau\nu$ maxHTpTV280_500_CFilterBVeto
364195	$W \rightarrow \tau\nu$ maxHTpTV280_500_BFilter
364196	$W \rightarrow \tau\nu$ maxHTpTV500_1000
364197	$W \rightarrow \tau\nu$ maxHTpTV1000_E_CMS



## Appendix B

# Kinematical variables' distribution in control region

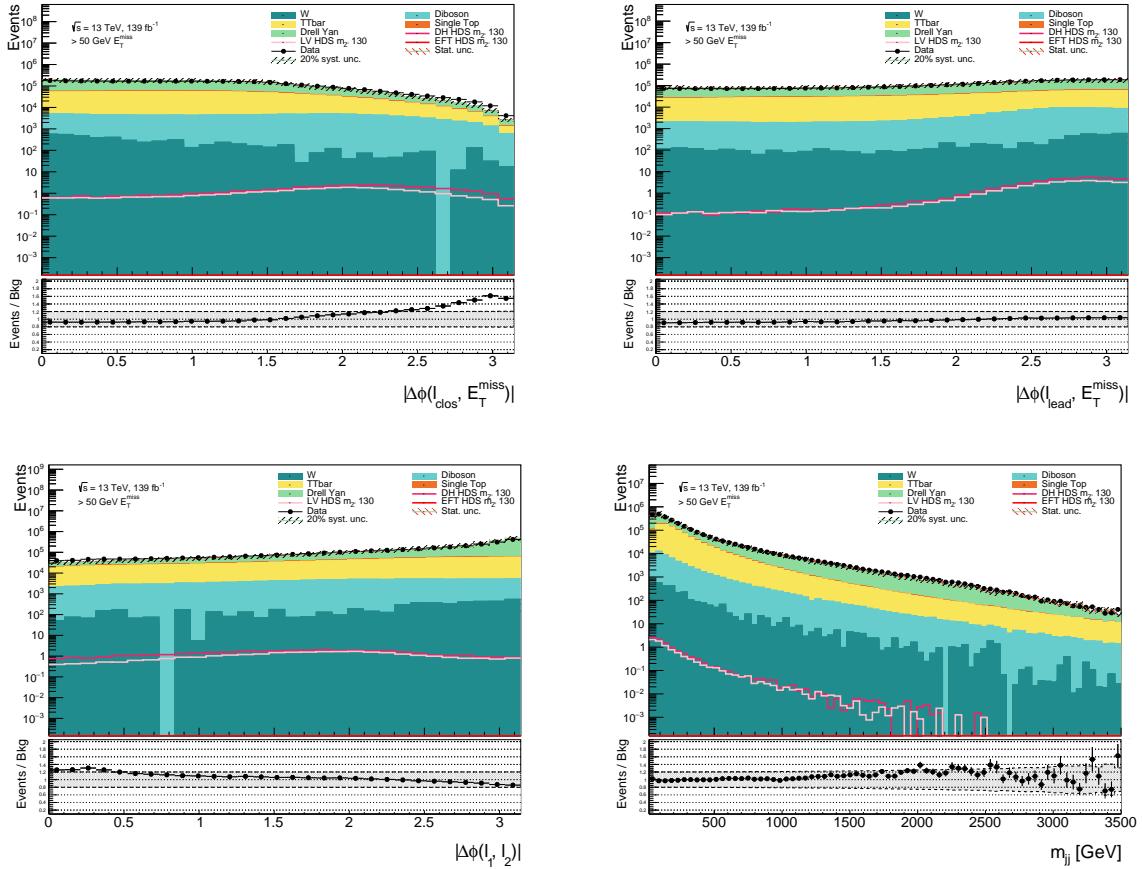
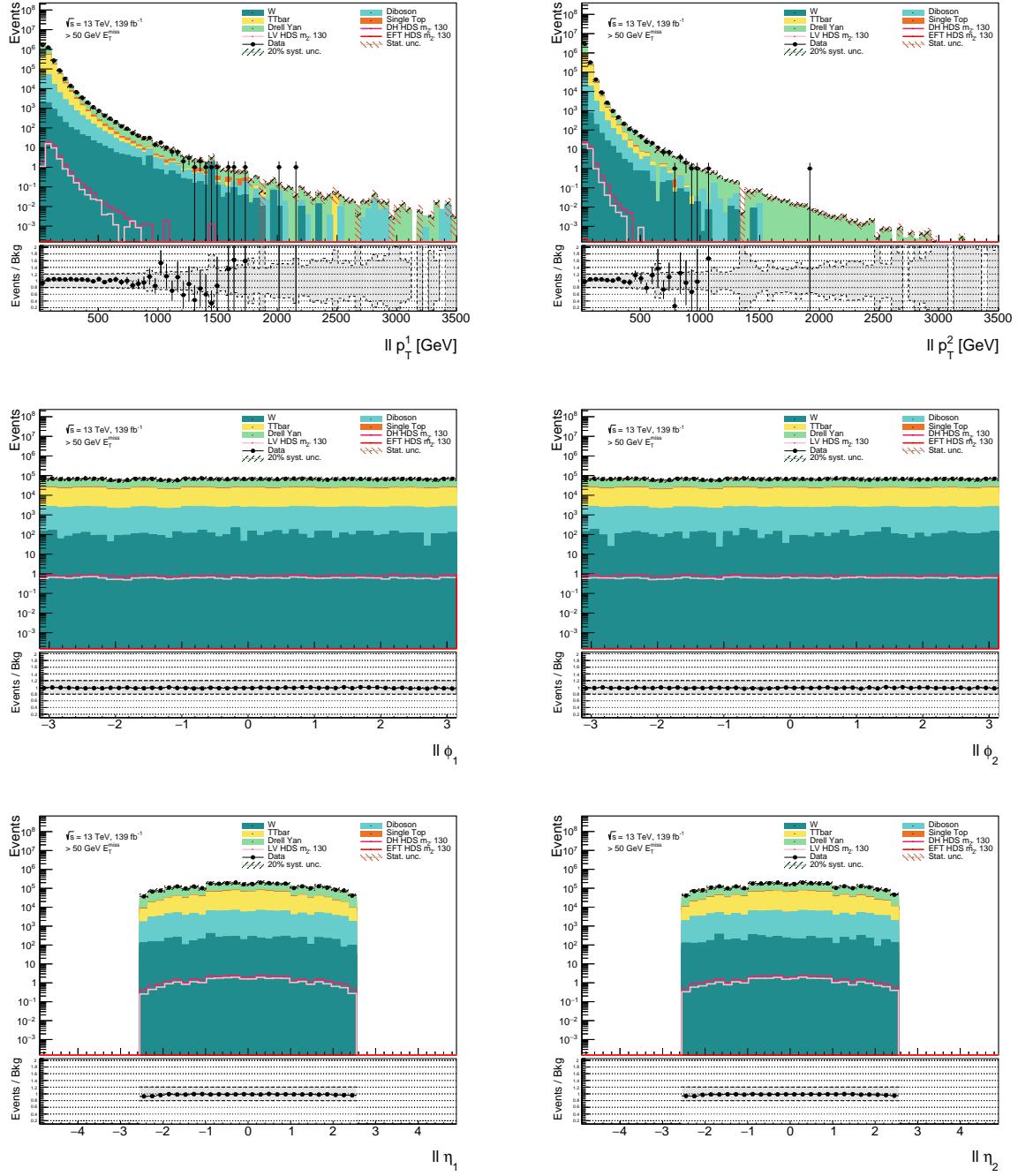


Figure B.1:  $\Delta\phi(l_c, E_T^{\text{miss}})$ ,  $\Delta\phi(l_{\text{lead}}, E_T^{\text{miss}})$ ,  $\Delta\phi(l_1, l_2)$  and  $m_{jj}$  distribution in the control region.

Figure B.2: Leptons  $p_T$ ,  $\phi$  and  $\eta$  distribution in the control region.

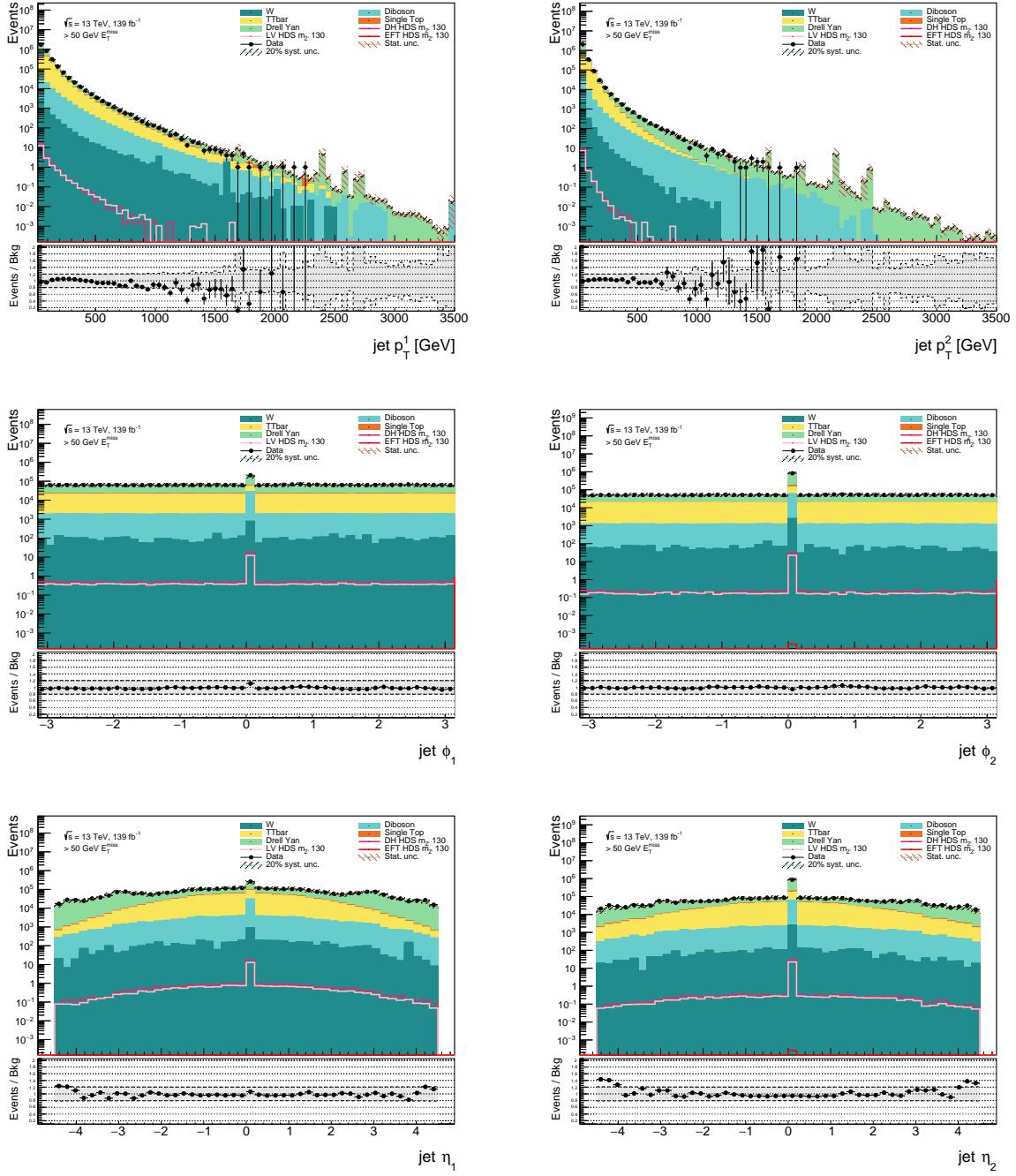


Figure B.3: Leading jets  $p_T$ ,  $\phi$  and  $\eta$  distribution in the control region.

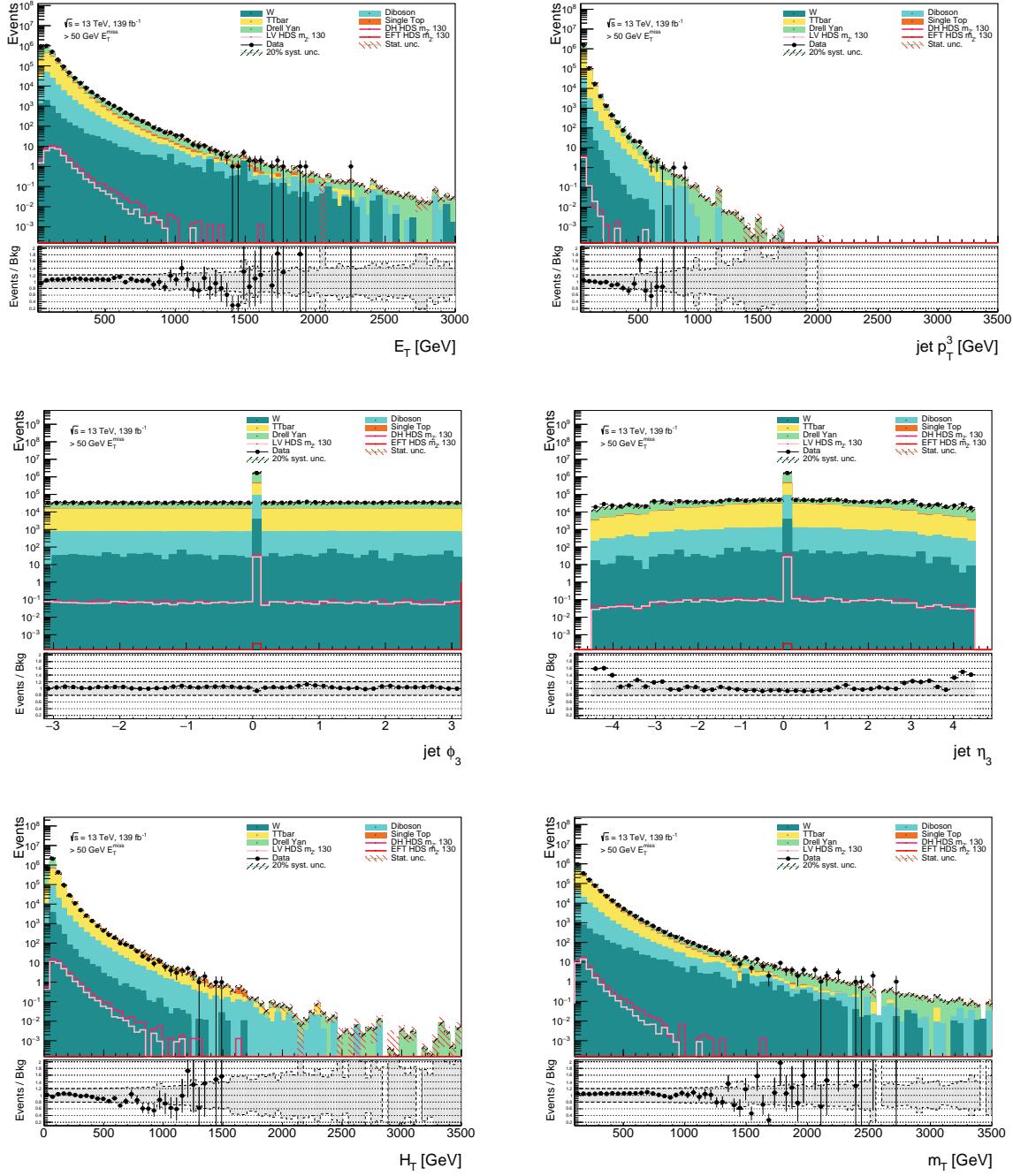


Figure B.4:  $p_T, \phi$  and  $\eta$  of third leading jet and the dilepton pairs  $E_T$ ,  $H_T$  and  $m_T$  distribution in the control region.

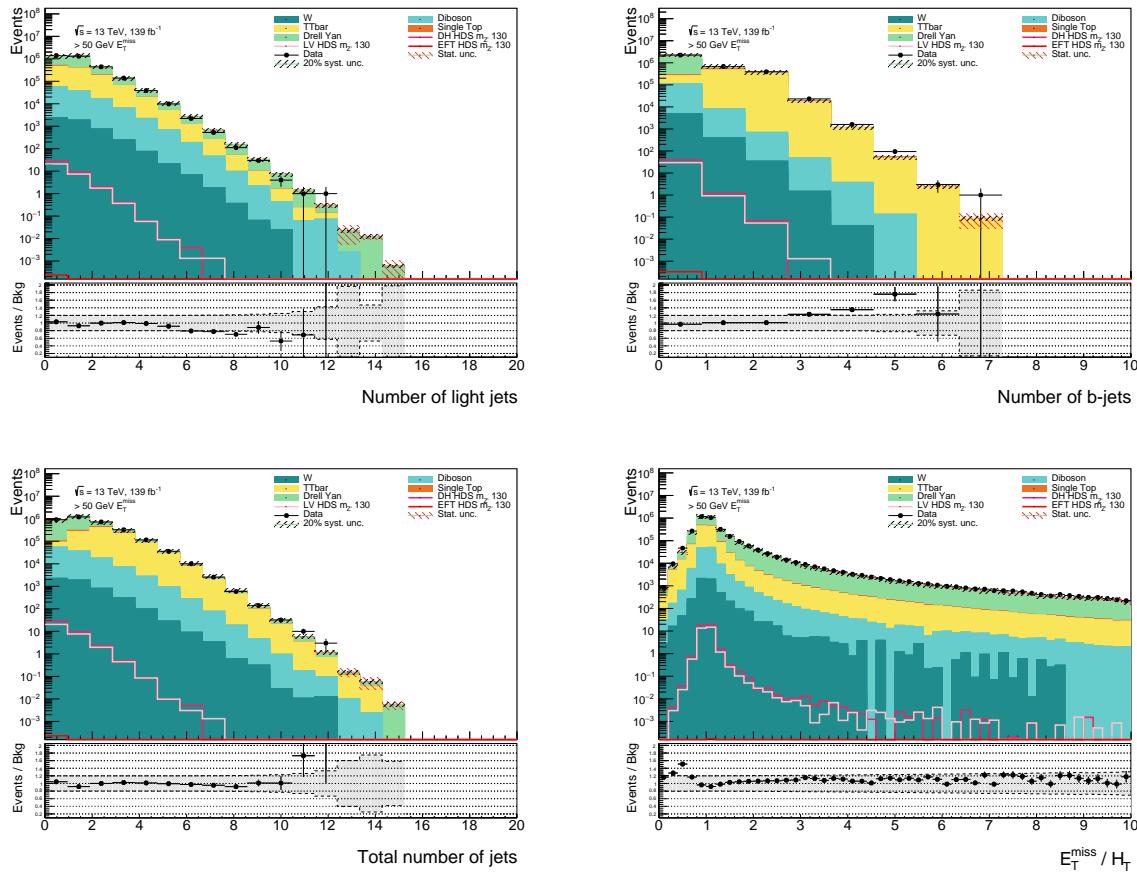


Figure B.5: Number of light, b- and total jets and  $E_T^{\text{miss}} / H_T$  distribution in the control region.



## Appendix C

### Data and MC agreement jets CR

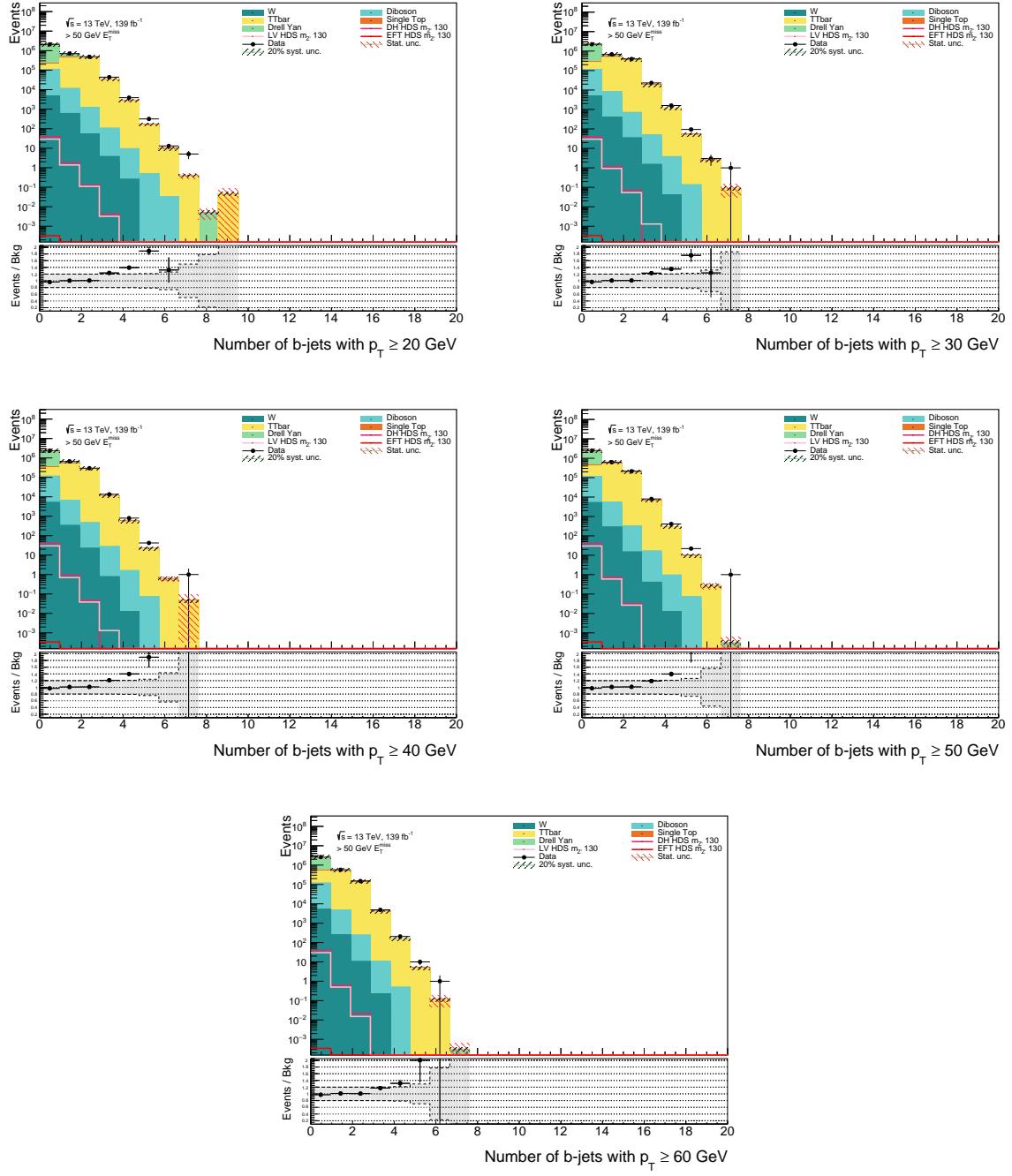


Figure C.1: Data and MC agreement on number of b- jets with different  $p_T$  cuts in CR.

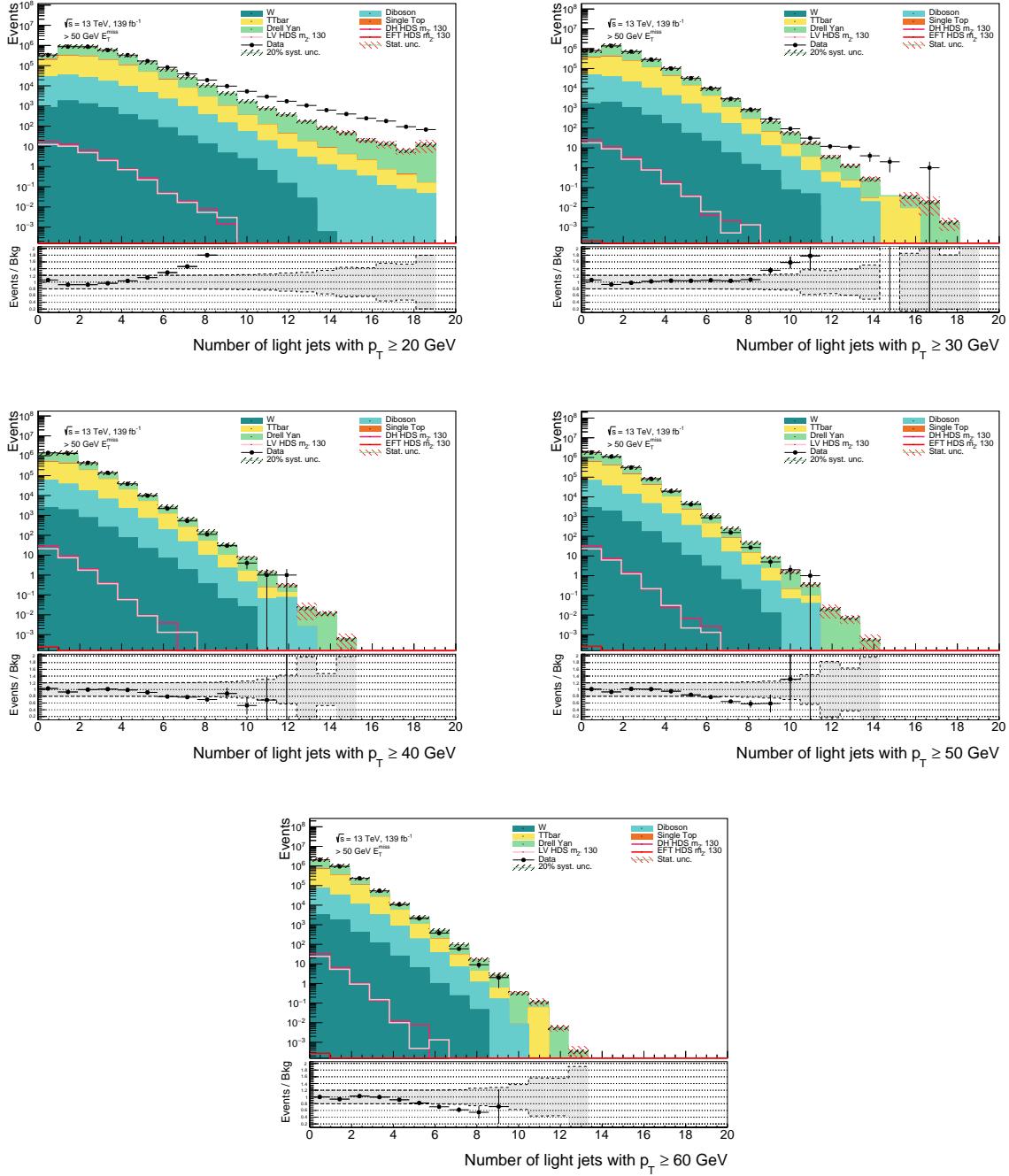


Figure C.2: Data and MC agreement on number of light jets with different  $p_T$  cuts in CR.



## Appendix D

### Data and MC agreement jets CR

Soon to come



# Appendix E

## Network optimization

### E.1 Neural Network Training

For most of the NN optimization methods we trained a NN with the following hyperparameters:

- One hidden layer
- 100 neurons in the hidden layer
- 0.1 learning rate  $\eta$
- $10^{-5}$  L2-regularization parameter  $\lambda$
- The ADAM optimizer

We will mention whenever these parameters were not used. The results for the different network optimization methods explained in Chapter 7.2 follow from here. Starting with the normalization of data.

### E.1.1 Normalization of data

We trained a network using 80% of the whole SM background events as well as 80% of all the  $Z'$  DH HDS samples. As sample weights we only balanced the signal and background using MC events. We did this by using method 3. on Chapter 7.2.3. We tested on the remaining 20% of the SM background events, as well as 20% of  $Z'$  DH HDS events where  $m_{Z'} = 130$  GeV. The different normalization methods explained in Chapter 7.2.2 have been tested and can be seen in the Figure E.1.

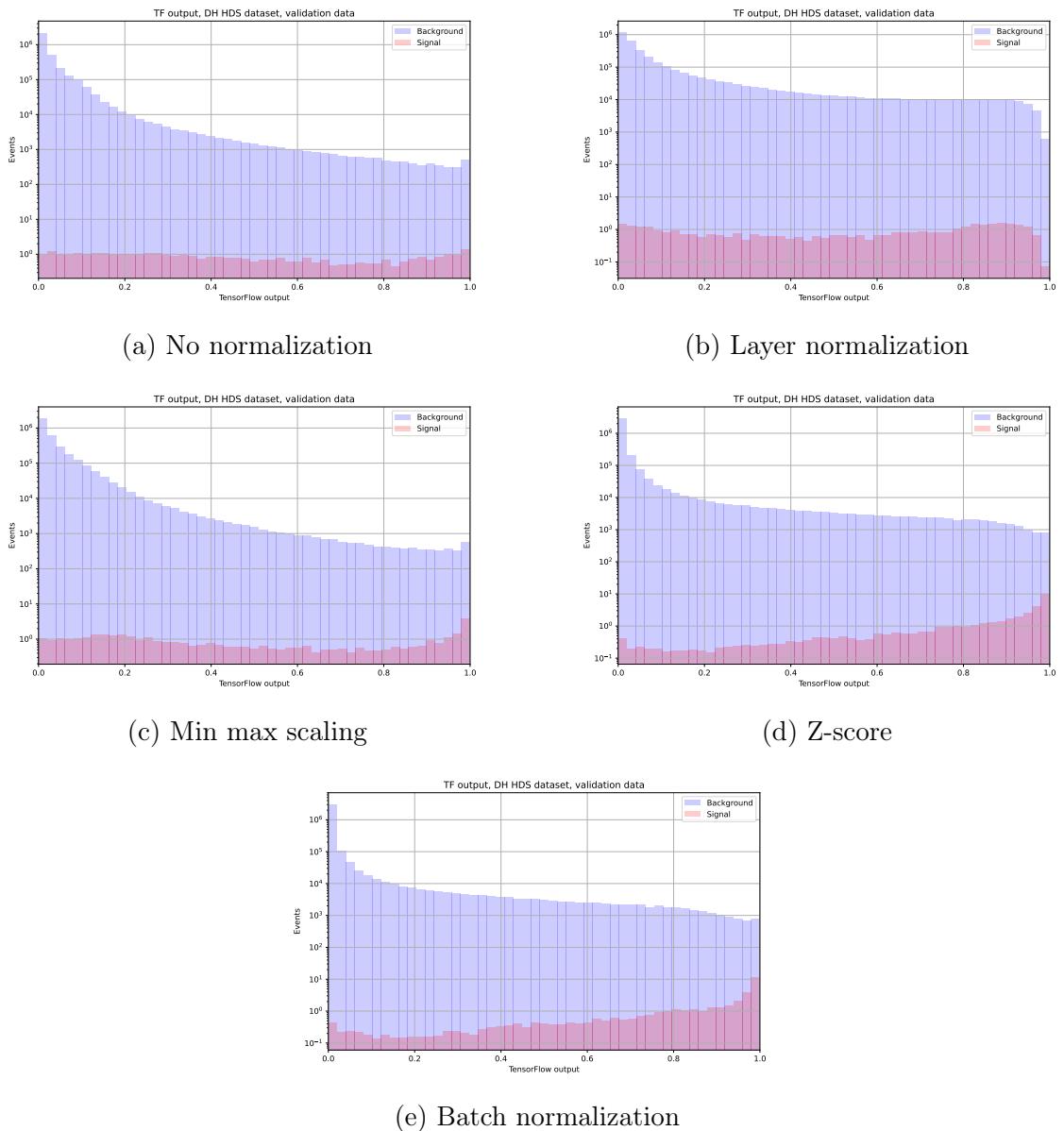


Figure E.1: NN prediction when using different normalization methods. This is testing a dataset with 20% of the  $Z'$  DH HDS  $m_{Z'} = 130$  GeV events.

Including data points as well as uncertainties on the best performing normalization methods, as well as their calculate expected significance as explained in Chapter 5.3.5, yields the plots shown in Figure E.2. For more Figures showing NN training results see the GitHub repo<sup>1</sup>.

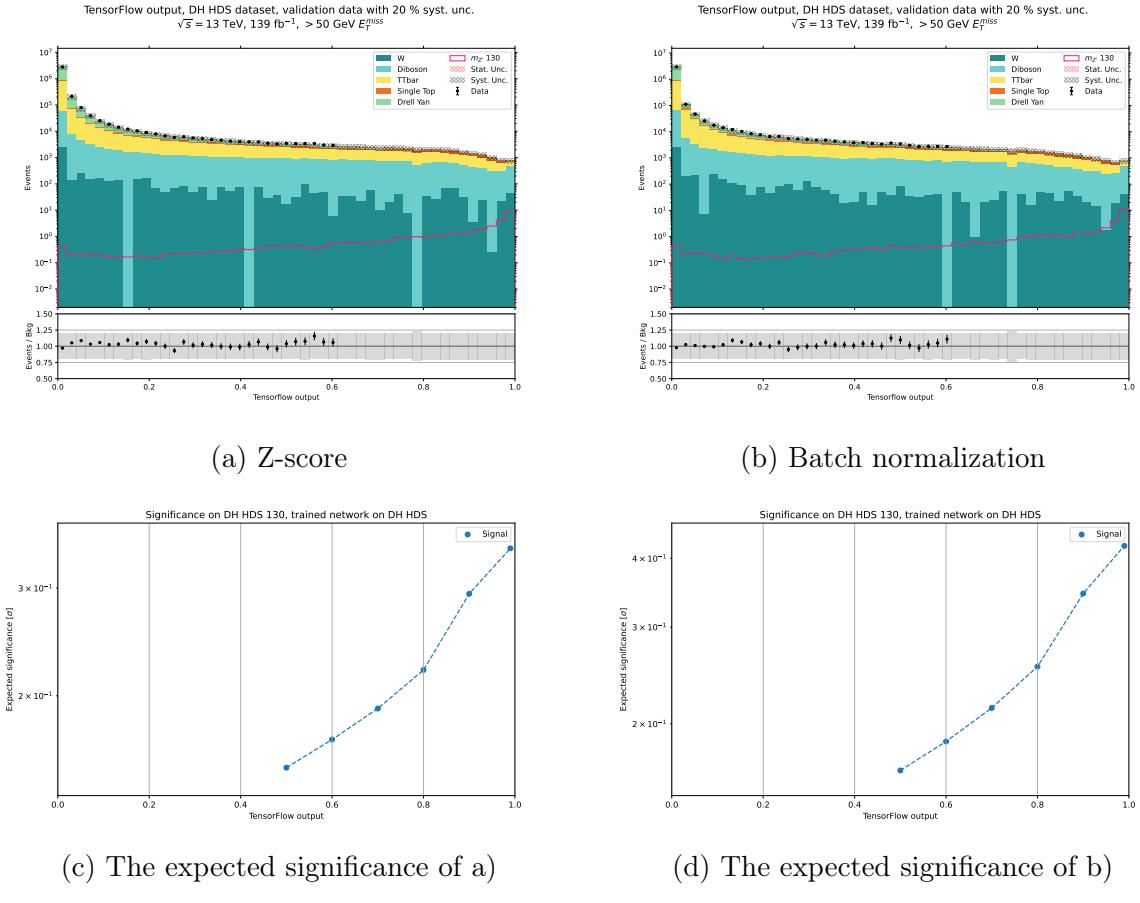


Figure E.2: Comparison of the best normalization methods. Figure a) and b) show the validation data of both cases, c) and d) show the expected significance of the validation plots when making a cut on the output.

As we can see the **Batch\_normalization** method gives us the highest signal and background but is it reasonable to use this method when one is not using a CNN? The reason batch normalization might work best for our case is because when we divide the data by batches it might unevenly represent the SM / signal and their ratio. But by using batch normalization it takes the average of all the batches creating a closer to real distribution. For the following examples in this chapter we will use batch normalization to make the optimal network.

<sup>1</sup> Available here: [https://github.com/rubenguevara/Master-Thesis/tree/master/Plots/NeuralNetwork/Normalization\\_method](https://github.com/rubenguevara/Master-Thesis/tree/master/Plots/NeuralNetwork/Normalization_method)

### E.1.2 Balancing of signal and background

To try the different sample weight methods explained in Chapter 7.2.3 we used a dataset consisting of only SM events where the goal was to treat the  $W$  channel as signal and try to isolate it from other SM processes. To train we used `Batch_normalization` and 80% of the SM background events. To test we used the remaining 20% of SM events. We also tested the difference in performance when using the SGD and ADAM optimizers. The difference in distributions when using different optimizers can be seen in Figure E.3, here the balancing method (3. on Chapter 7.2.3) is used.

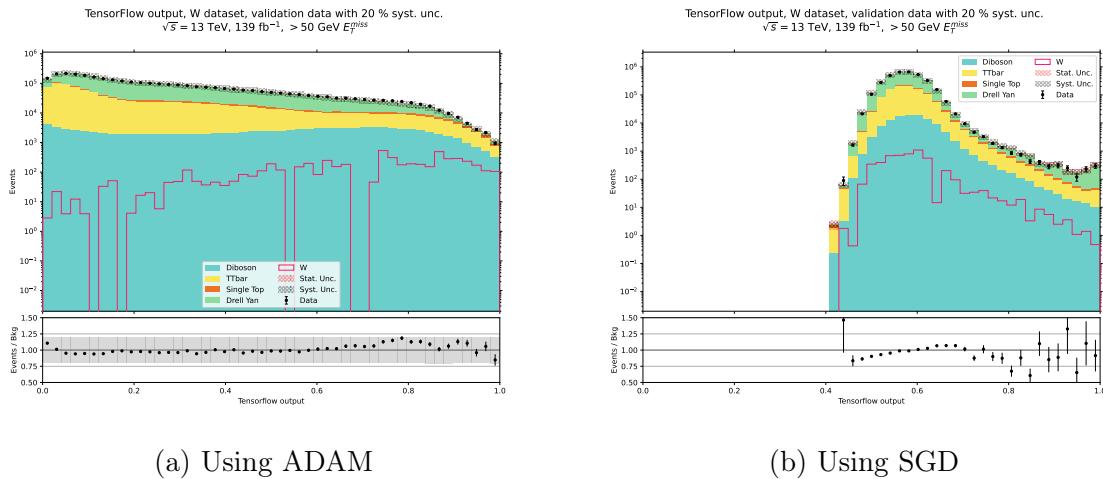


Figure E.3: Validation plots using SGD and ADAM. This was done using a dataset where the goal was to isolate the  $W$  background process from other SM background processes

As ADAM is far better at sorting signal from background we will only use this optimizer further. The results for the different weighting methods can be seen in Figure E.4, which shows the validation plots and in Figure E.5 which shows the ROC score. For more Figures showing NN training results see the GitHub repo<sup>2</sup>.

From the figures we see that the only way the network does not predict every event to be a background event<sup>3</sup> is when we introduce the balancing method. We also see that the AUC increases more as well. Meaning that we must balance our dataset. Something else to mention, as to why the network does such a poor job at classifying the  $W$  background, is that the network here was not optimized for the search. If we were to conduct a

<sup>2</sup> Available here: <https://github.com/rubenguevara/Master-Thesis/tree/master/Plots/NeuralNetwork/W>

<sup>3</sup> Since the output is the score from 0-1 our network gives every event, where 0 means that the network predicts 0% chance for an event to be signal

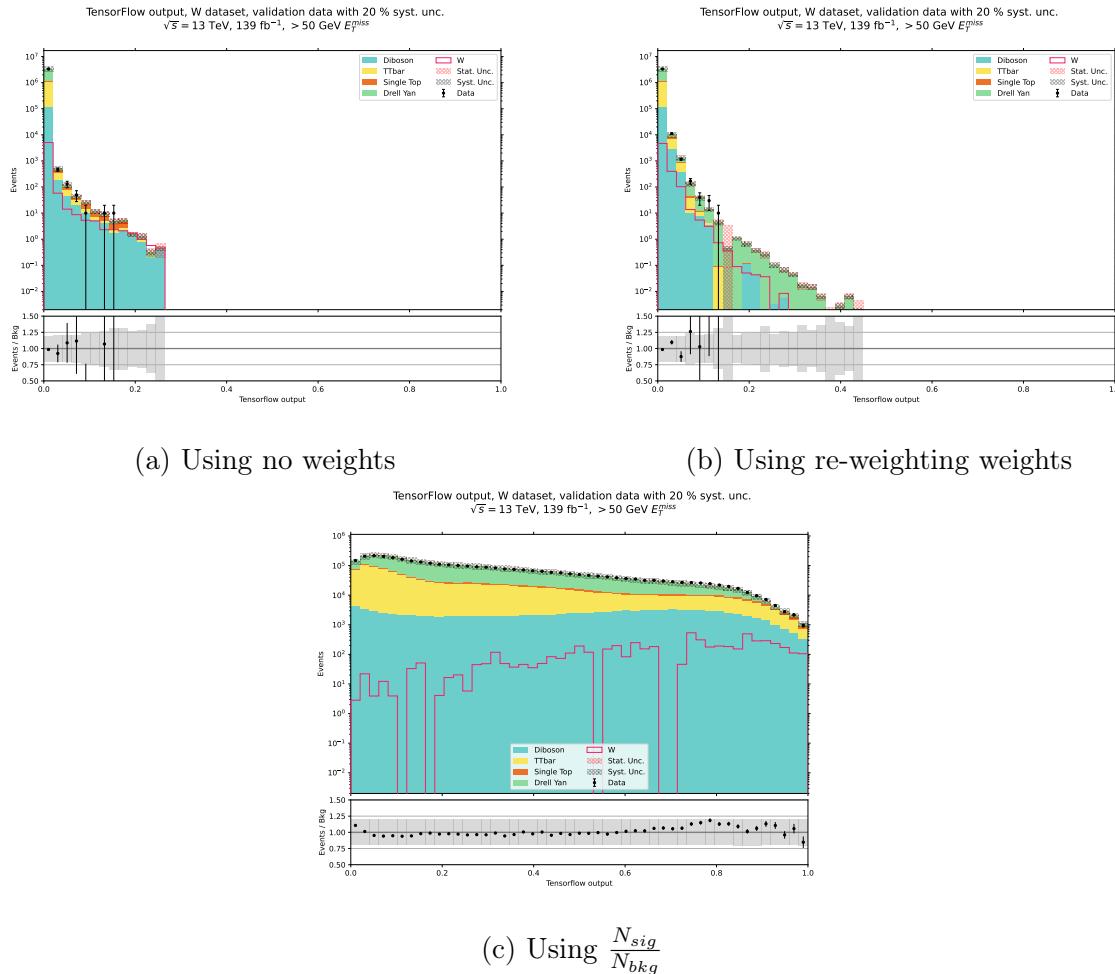


Figure E.4: Validation plots of different balancing methods. This was done using a dataset where the goal was to isolate the  $W$  background process from other SM background processes

thorough grid search of all hyperparameters it would yield greater results, but as this chapter is for testing methods rather analyzing data we will not delve further into it for now,

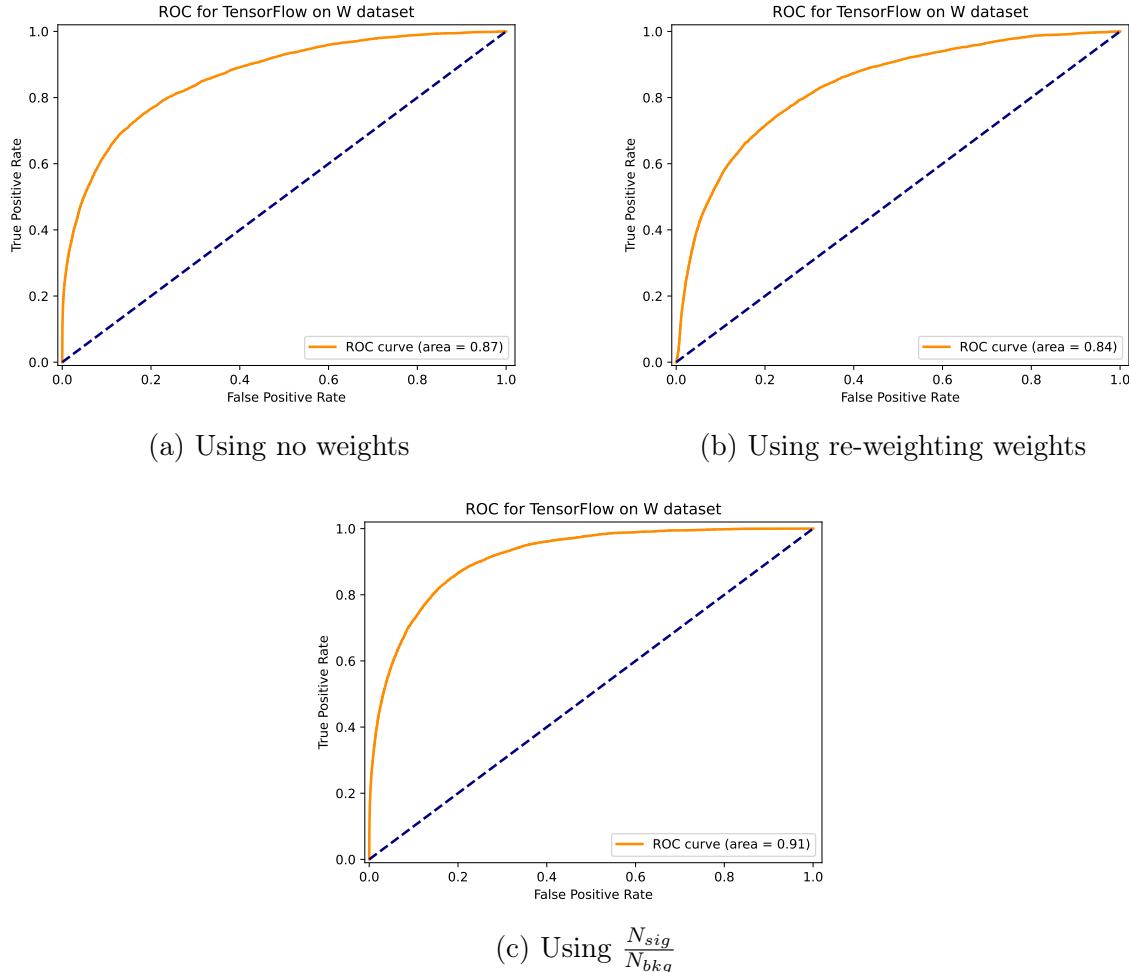


Figure E.5: ROC plots of different balancing methods. This was done using a dataset where the goal was to isolate the  $W$  background process from other SM background processes

### E.1.3 Sample weights to get expected events

To try the different sample weight methods explained in Chapter 7.2.4 which include the weights (Chapter 7.1.1), we used a dataset consisting of only SM events where the goal was to treat the  $W$  channel as signal and try to isolate it from other SM processes. To train we used `Batch_normalization` and 80% of the SM background events. To test we used the remaining 20% of SM events. The results can be seen in Figure E.6, which shows the validation plots and in Figure E.7 which shows the ROC score. For more Figures showing NN training results see the GitHub repo<sup>4</sup>.

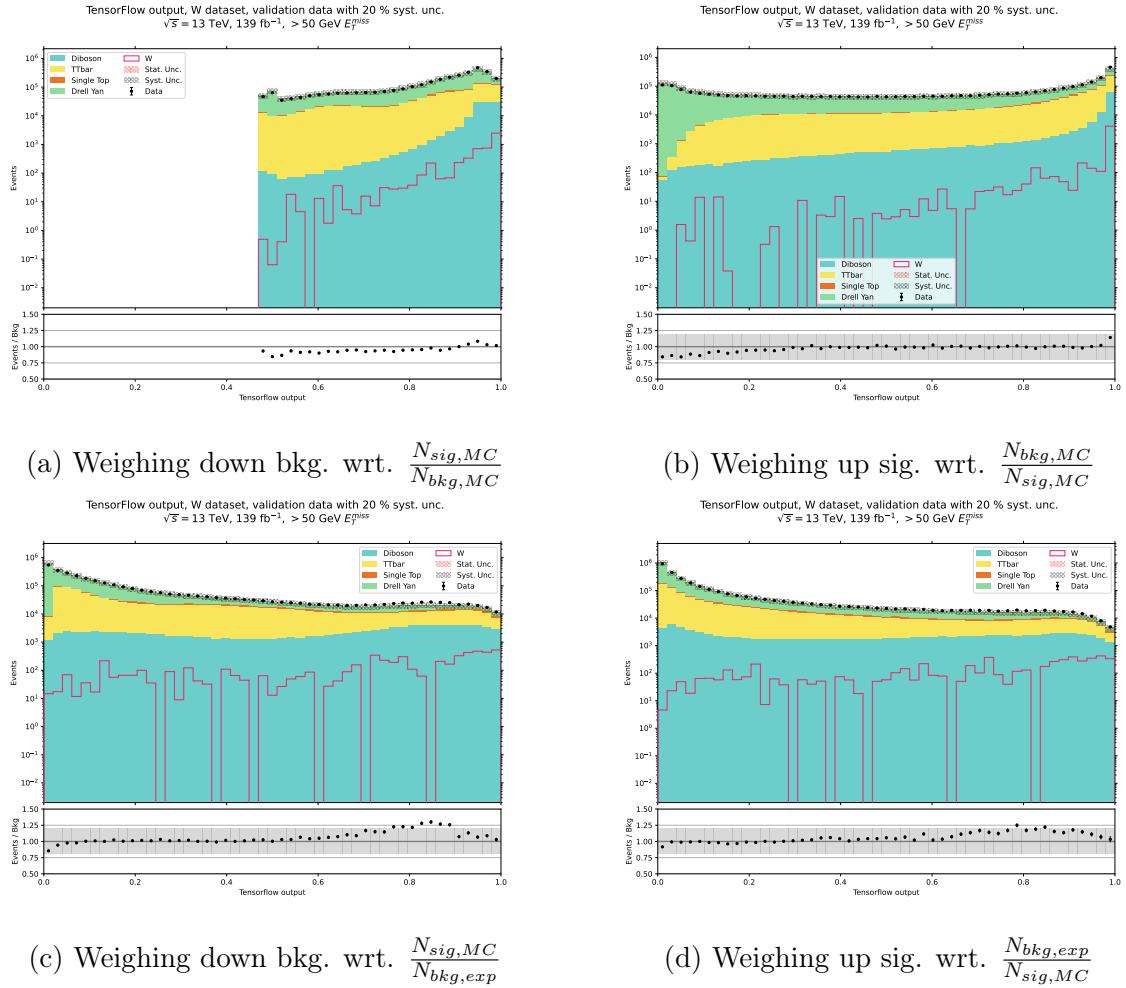


Figure E.6: Validation plots of different balancing methods when re-weighting background events to expected events. This was done using a dataset where the goal was to isolate the  $W$  background process from other SM background processes

As we are only re-weighting the background events, we can see from the figures that we get the best results when balancing with respect to the expected number of background

<sup>4</sup> Available here: <https://github.com/rubenguevara/Master-Thesis/tree/master/Plots/NeuralNetwork/W>

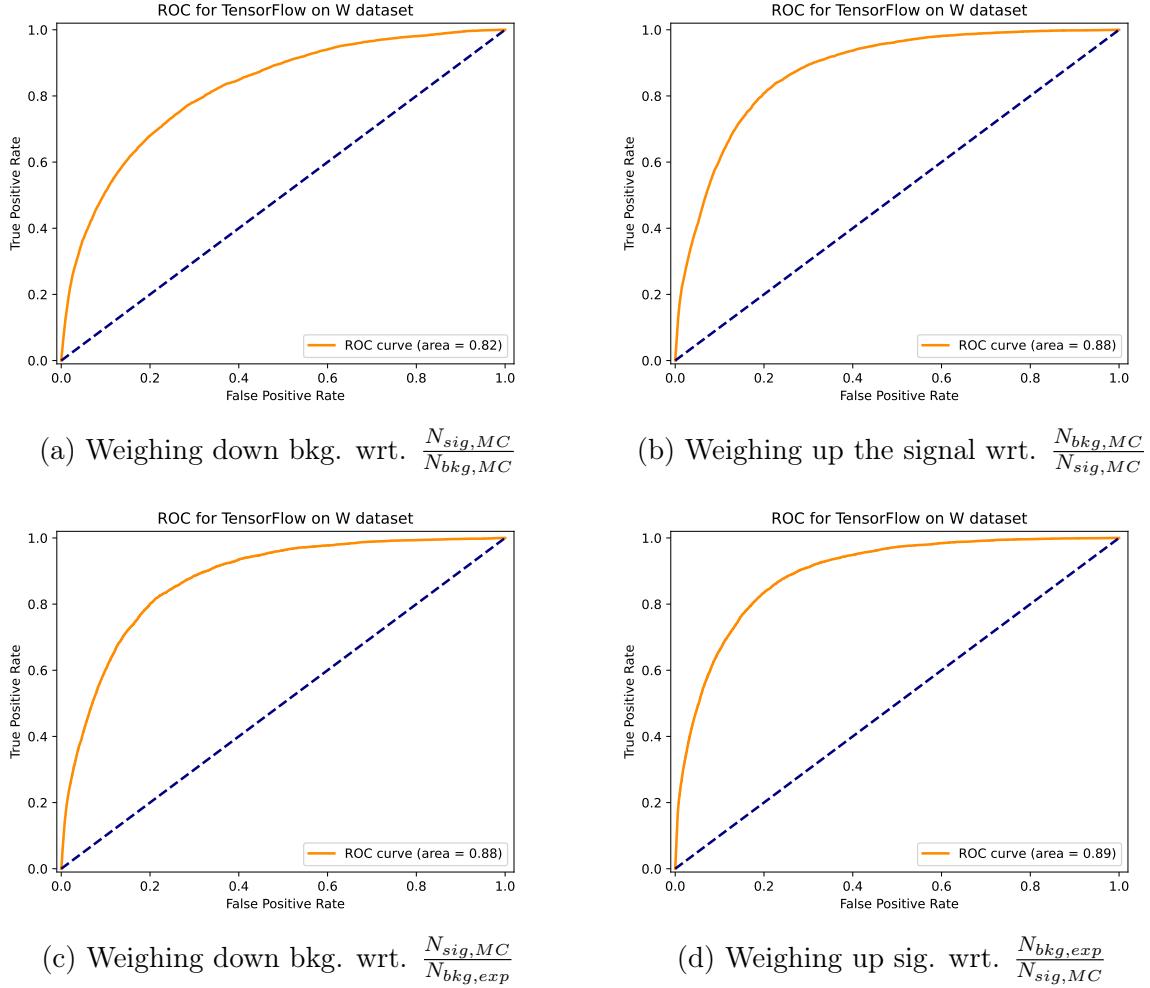


Figure E.7: ROC plots of different balancing methods when re-weighting background events to expected events. This was done using a dataset where the goal was to isolate the  $W$  background process from other SM background processes

events. Which is optimal, as this is what goes into the network. Whether it is better to weigh down the background or weight up the signal is not clear however, from the AUC of the ROC curves it is slightly better to weigh up the signal. To check which gives a higher expected significance however we can look at the expected significance, this is shown in Figure E.8. Here we see that there is a greater expected significance when weighing up the signal events.

As a last note for the testing of these methods, the networks, while still getting over  $5\sigma$  expected significance (without errors) on the  $W$  channel, do not have the best distribution on the validation plots. The reason for this might be because we did not optimize the networks we tested, but rather used the same network for test.

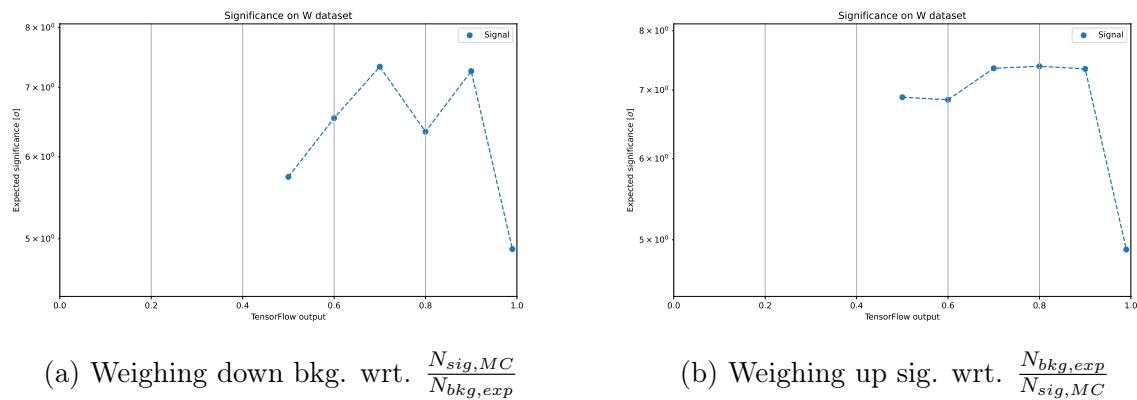


Figure E.8: Expected significance plots of the best balancing methods when re-weighting background events to expected events. This was done using a dataset where the goal was to isolate the  $W$  background process from other SM background processes

### E.1.4 Padding of data

For the padding problem. We will as explained in Chapter 7.2.1 try the new variables presented in Table 7.2. The other method we tried was to remove the features with jagged arrays, that means the  $p_T, \eta, \phi$  of the three most energetic jets, as well as the invariant mass of the two most energetic ones,  $m_{jj}$ . The trained a network using 80% of the whole SM background events as well as 80% of all the Z' DH HDS samples. As sample weights we used the best method from the previous section, which was to re-weight every background event and balance the dataset by weighing up all signal events by the ratio of expected number of background events over signal MC events,  $\frac{N_{bkg,exp}}{N_{sig,MC}}$ . As the best normalization method was `Batch_normalization`, this method was used here. We also utilized the ADAM optimizer instead of SGD.

As changing features changes the whole dataset, then to get the best results as possible we went through a full grid search following the steps in Chapter 7.2.5 for both networks. The result for the hyperparameters that gave the highest significance can be seen in Figure E.9.

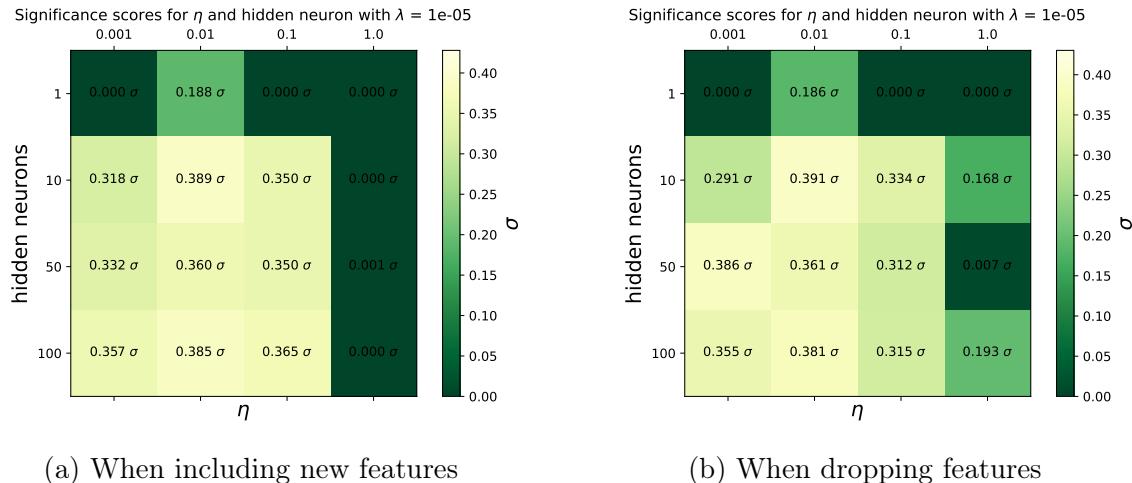


Figure E.9: Grid search result for pad testing on NN. This is training a dataset with 80% of all Z' DH HDS events.

This means that the best hyperparameters for both networks coincidentally is the same, meaning: `n_neuron = 10`, `eta = 0.01`, `lambda = 1e-5`. The loss, AUC and binary accuracy over epochs for the best networks can be seen in Figure E.10 and Figure E.11.

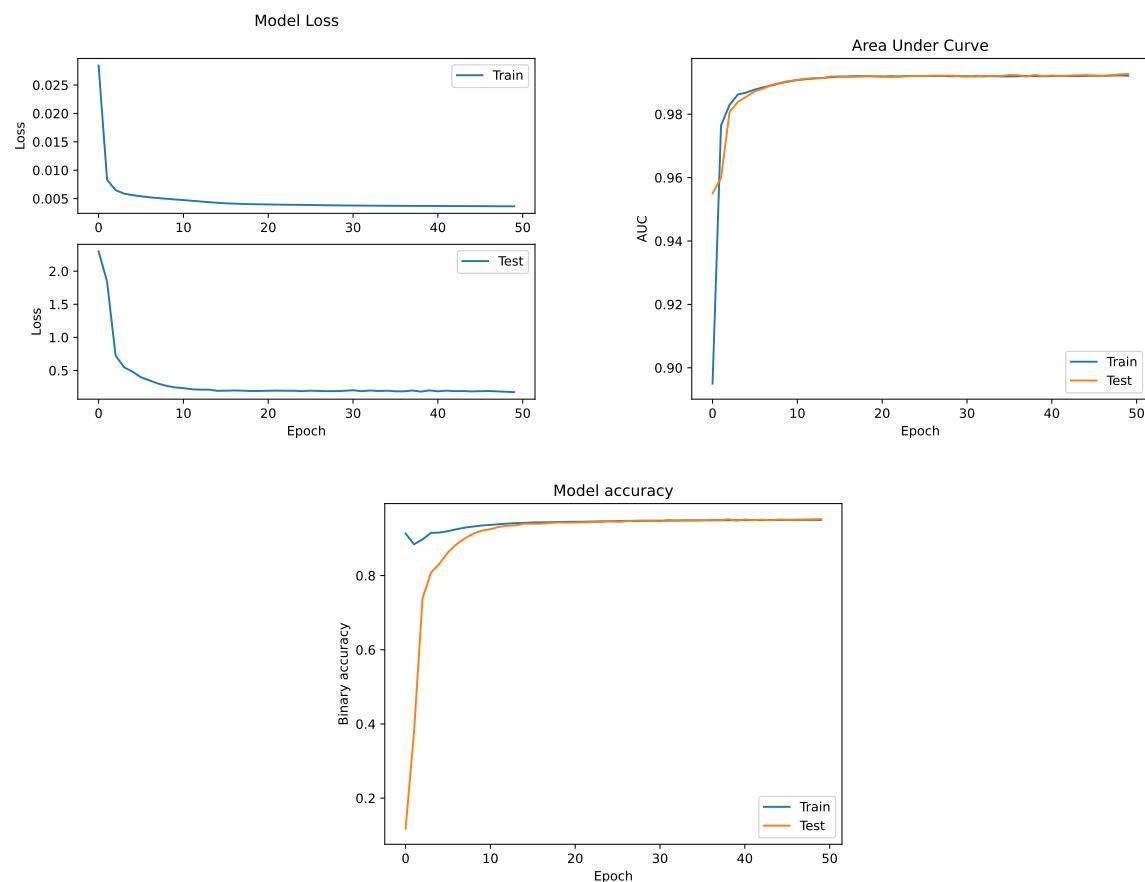


Figure E.10: NN parameters after 50 epochs with new features. This is training a dataset with 80% of all  $Z'$  DH HDS events.

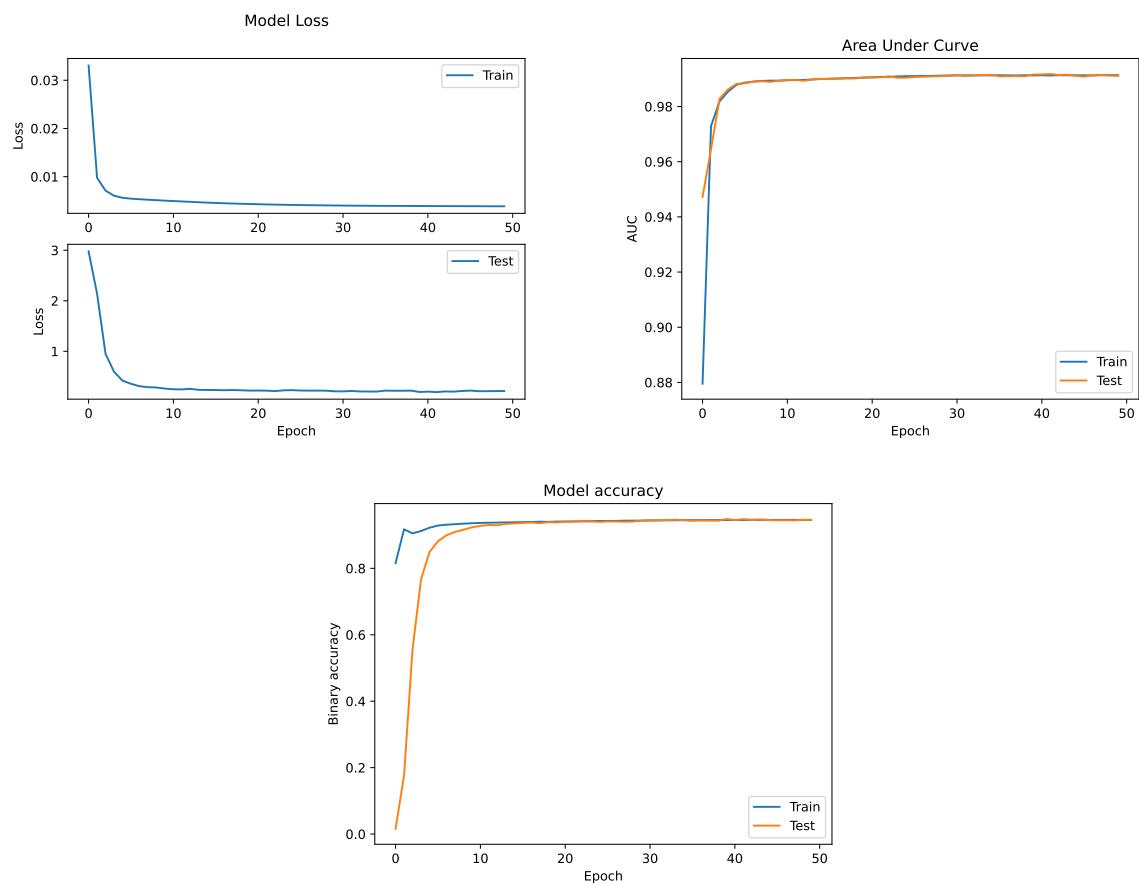


Figure E.11: NN parameters after 50 epochs when dropping features. This is training a dataset with 80% of all Z' DH HDS events.

We tested on the remaining 20% of the SM background events, as well as 20% of Z' DH HDS events where  $m_{Z'} = 130$  GeV. The ROC scores for each network can be seen in Figure E.12. The validation plots can be seen in Figure E.13

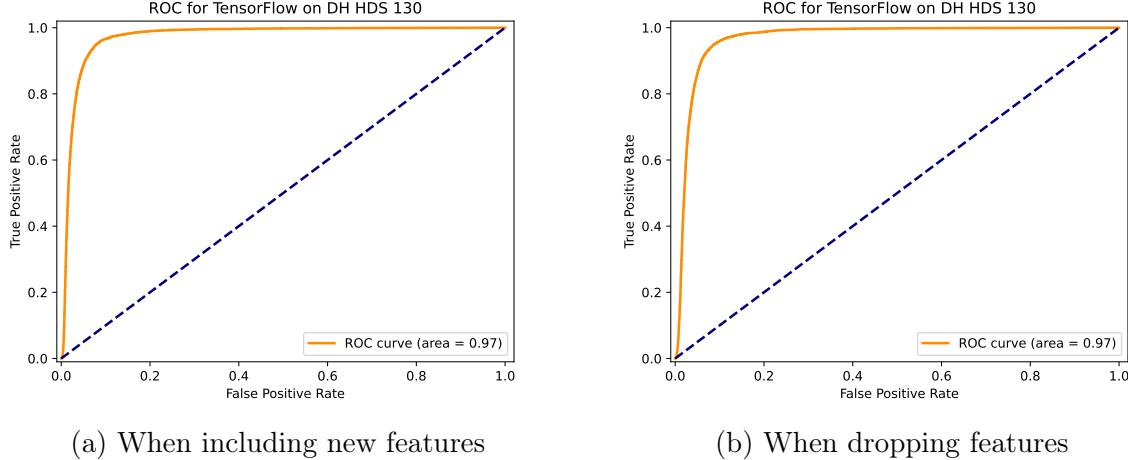


Figure E.12: ROC plots for both padding methods. This is testing a dataset with 20% of the Z' DH HDS  $m_{Z'} = 130$  GeV events.

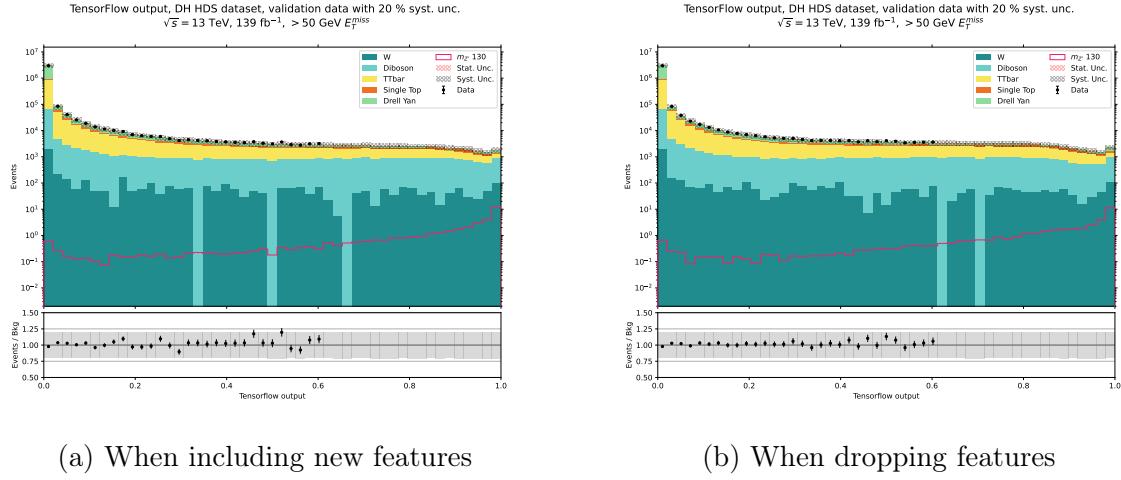


Figure E.13: Validation plots for both padding methods. This is testing a dataset with 20% of the Z' DH HDS  $m_{Z'} = 130$  GeV events.

As we can see the performance of both methods is the same, to check if the sensitivity increases more with the new padding method or not we can check the significance of each model. This can be seen in Figure E.14, which shows a slight improvement on the sensitivity of the network when using the features.

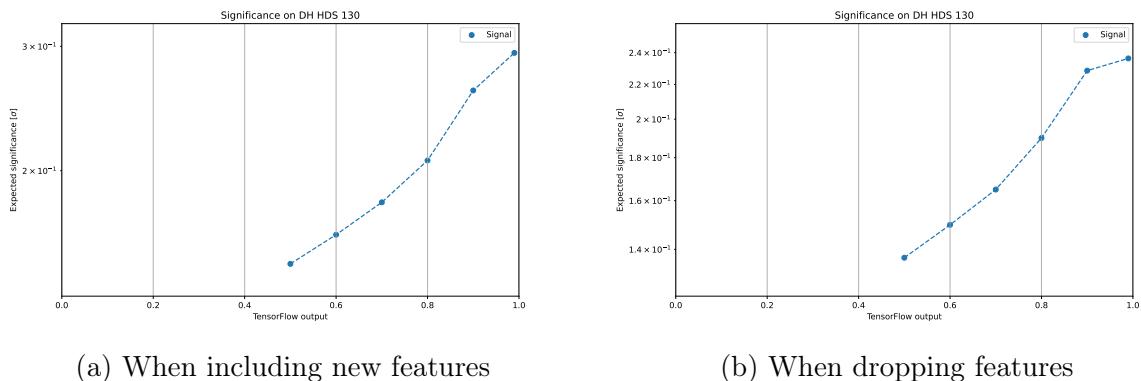


Figure E.14: Significance plots for both padding methods. This is testing a dataset with 20% of the Z' DH HDS  $m_{Z'} = 130$  GeV events.

## E.2 Boosted Decision Tree Training

As the only technique that needed to be tested for BDTs was the different weighting methods, we conducted these here. We only tested the weighting techniques where we only look at the positive weights, and where we scale the weights wrt. the sum of the weights over the sum over the absolute value of weights. To compare we also included the unweighted method (only balancing data). The hyperparameters used to train the different networks in this chapter were

- L2- $\lambda = 10^{-5}$
- Number of trees = 200
- Depth of trees = 6
- Learning rate  $\eta = 0.1$

### E.2.1 Weights

The results of the different weighting methods can be seen in Figure E.15.

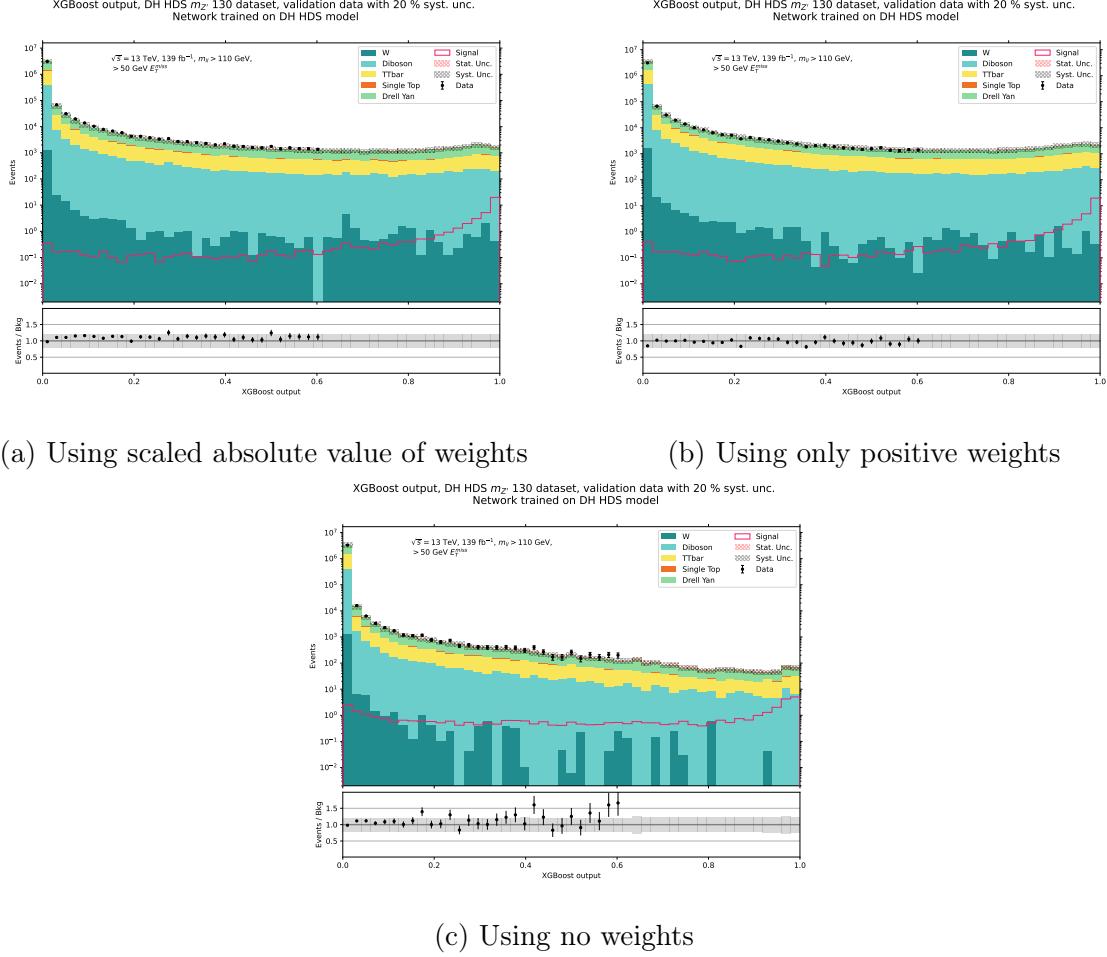


Figure E.15: Difference when using different weighting methods. All networks were trained using the balancing method explained in Section 7.3.1

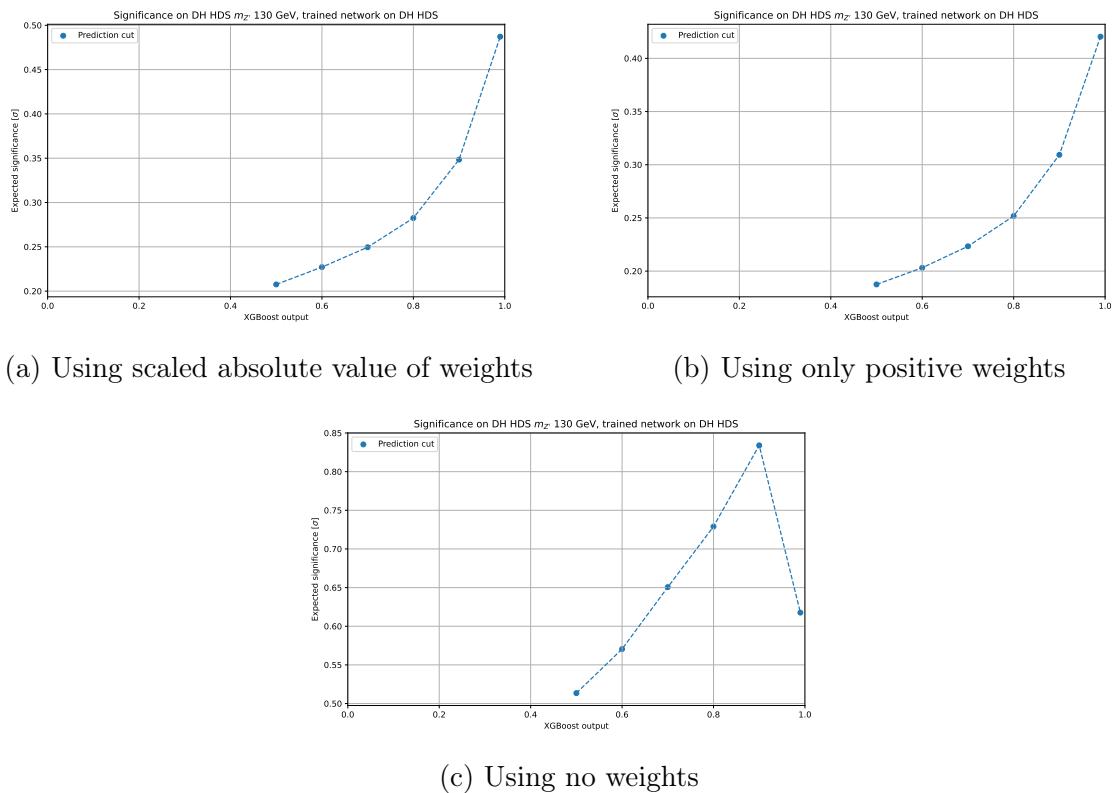


Figure E.16: Difference when using different weighting methods. All networks were trained using the balancing method explained in Section 7.3.1

### E.3 Discussion (draft)

Comment  
on lack  
of time  
and DNN  
thoughts.

The last thing to be noted is that having a DNN completely removes the possibility of combining the results of multiple networks trained on a single model, as the imbalance becomes too much for the network to see anything. A solution to this however, is that instead of combining the results of multiple networks trained on a singular model, one could try the Parametrized NN approach used by Baldi et al. [27], which could potentially avoid the imbalance problem, but this is proposed as a plausible new research project due to time constrain on this thesis.

Comment  
on fully  
converting  
to XG-  
Boost.

XGBoost » TensorFlow

# Appendix F

## Limit calculation tables

To calculate the signal efficiency  $\varepsilon_{sig}$ , we used the following formula

$$\varepsilon_{sig} = \frac{N_{sig}}{\sigma B \times \text{lumi}_{RunII}}$$

where  $N_{sig}$  are the number of signal events after the cut, and where we calculated

$$\sigma B \times \text{lumi}_{RunII} = \sum_{\text{period}} \sigma B_{\text{period}} \times \text{lumi}_{\text{period}}$$

extracting the cross-section of the DM sample from the DSID on each MC period and converting it to fb units, and using

$$\text{lumi}_{\text{period}} = \begin{cases} 36.4 \text{ fb}^{-1}, & \text{for period = a} \\ 44.3 \text{ fb}^{-1}, & \text{for period = d} \\ 58.5 \text{ fb}^{-1}, & \text{for period = e} \end{cases}$$

Table F.1: Inputs for the  $Z'h_D \rightarrow l^+l^-\chi\chi$  HDS  $\sigma B$  calculations. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	1.11	$ee$	$0.25 \pm 0.05$	$7.80 \pm 1.58$	$108.4 \pm 23.0$
		$\mu\mu$	$0.20 \pm 0.04$	$6.28 \pm 1.27$	$124.9 \pm 26.1$
200	$2.46 \times 10^{-1}$	$ee$	$0.54 \pm 0.11$	$3.67 \pm 0.74$	$114.1 \pm 24.4$
		$\mu\mu$	$0.41 \pm 0.08$	$2.78 \pm 0.56$	$123.2 \pm 25.8$
400	$1.49 \times 10^{-2}$	$ee$	$1.13 \pm 0.23$	$4.67 \times 10^{-1} \pm 9.37 \times 10^{-2}$	$107.0 \pm 23.4$
		$\mu\mu$	$0.79 \pm 0.16$	$3.29 \times 10^{-1} \pm 6.60 \times 10^{-2}$	$127.5 \pm 26.6$
600	$2.35 \times 10^{-3}$	$ee$	$1.40 \pm 0.28$	$9.12 \times 10^{-2} \pm 1.83 \times 10^{-2}$	$126.3 \pm 26.7$
		$\mu\mu$	$1.01 \pm 0.20$	$6.59 \times 10^{-2} \pm 1.32 \times 10^{-2}$	$126.3 \pm 26.3$
800	$5.43 \times 10^{-4}$	$ee$	$1.59 \pm 0.32$	$2.40 \times 10^{-2} \pm 4.81 \times 10^{-3}$	$118.8 \pm 25.6$
		$\mu\mu$	$1.11 \pm 0.22$	$1.67 \times 10^{-2} \pm 3.36 \times 10^{-3}$	$113.2 \pm 23.6$
900	$2.82 \times 10^{-4}$	$ee$	$1.60 \pm 0.32$	$1.25 \times 10^{-2} \pm 2.51 \times 10^{-3}$	$119.3 \pm 25.7$
		$\mu\mu$	$1.12 \pm 0.22$	$8.78 \times 10^{-3} \pm 1.76 \times 10^{-3}$	$114.8 \pm 24.0$
1100	$8.40 \times 10^{-5}$	$ee$	$1.63 \pm 0.33$	$3.81 \times 10^{-3} \pm 7.64 \times 10^{-4}$	$114.3 \pm 24.4$
		$\mu\mu$	$1.16 \pm 0.23$	$2.70 \times 10^{-3} \pm 5.42 \times 10^{-4}$	$118.6 \pm 24.7$
1200	$4.75 \times 10^{-5}$	$ee$	$1.65 \pm 0.33$	$2.18 \times 10^{-3} \pm 4.37 \times 10^{-4}$	$118.4 \pm 25.1$
		$\mu\mu$	$1.14 \pm 0.23$	$1.50 \times 10^{-3} \pm 3.01 \times 10^{-4}$	$125.6 \pm 26.3$
1300	$2.73 \times 10^{-5}$	$ee$	$1.69 \pm 0.34$	$1.28 \times 10^{-3} \pm 2.57 \times 10^{-4}$	$123.9 \pm 26.5$
		$\mu\mu$	$1.15 \pm 0.23$	$8.72 \times 10^{-4} \pm 1.75 \times 10^{-4}$	$130.7 \pm 27.2$
1400	$1.60 \times 10^{-5}$	$ee$	$1.67 \pm 0.33$	$7.43 \times 10^{-4} \pm 1.49 \times 10^{-4}$	$115.8 \pm 24.5$
		$\mu\mu$	$1.16 \pm 0.23$	$5.15 \times 10^{-4} \pm 1.03 \times 10^{-4}$	$125.4 \pm 26.1$
1500	$9.42 \times 10^{-6}$	$ee$	$1.69 \pm 0.34$	$4.44 \times 10^{-4} \pm 8.90 \times 10^{-5}$	$123.9 \pm 26.5$
		$\mu\mu$	$1.13 \pm 0.23$	$2.97 \times 10^{-4} \pm 5.96 \times 10^{-5}$	$130.7 \pm 27.2$

Table F.2: Inputs for the  $Z'h_D \rightarrow l^+l^-\chi\chi$  LDS  $\sigma B$  calculations. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	1.24	$ee$	$0.25 \pm 0.05$	$8.70 \pm 1.75$	$272.0 \pm 56.0$
		$\mu\mu$	$0.21 \pm 0.04$	$7.33 \pm 1.48$	$299.4 \pm 60.7$
200	1.05	$ee$	$0.29 \pm 0.06$	$8.34 \pm 1.68$	$294.9 \pm 60.3$
		$\mu\mu$	$0.23 \pm 0.05$	$6.68 \pm 1.34$	$304.4 \pm 61.7$
400	$6.08 \times 10^{-1}$	$ee$	$0.38 \pm 0.08$	$6.35 \pm 1.28$	$264.9 \pm 55.0$
		$\mu\mu$	$0.25 \pm 0.05$	$4.30 \pm 8.66 \times 10^{-1}$	$288.9 \pm 58.7$
600	$2.88 \times 10^{-1}$	$ee$	$0.70 \pm 0.14$	$5.64 \pm 1.13$	$275.2 \pm 56.6$
		$\mu\mu$	$0.50 \pm 0.10$	$3.98 \pm 7.98 \times 10^{-1}$	$298.3 \pm 60.4$
800	$1.44 \times 10^{-1}$	$ee$	$1.01 \pm 0.20$	$4.05 \pm 8.11 \times 10^{-1}$	$295.9 \pm 60.5$
		$\mu\mu$	$0.70 \pm 0.14$	$2.81 \pm 5.63 \times 10^{-1}$	$307.5 \pm 62.4$
900	$1.04 \times 10^{-1}$	$ee$	$1.14 \pm 0.23$	$3.30 \pm 6.61 \times 10^{-1}$	$271.3 \pm 55.8$
		$\mu\mu$	$0.80 \pm 0.16$	$2.30 \pm 4.60 \times 10^{-1}$	$293.2 \pm 59.4$
1100	$5.61 \times 10^{-2}$	$ee$	$1.30 \pm 0.26$	$2.03 \pm 4.07 \times 10^{-1}$	$270.8 \pm 55.7$
		$\mu\mu$	$0.90 \pm 0.18$	$1.40 \pm 2.81 \times 10^{-1}$	$290.0 \pm 58.8$
1200	$4.19 \times 10^{-2}$	$ee$	$1.35 \pm 0.27$	$1.58 \pm 3.16 \times 10^{-1}$	$273.9 \pm 56.2$
		$\mu\mu$	$0.95 \pm 0.19$	$1.10 \pm 2.21 \times 10^{-1}$	$289.4 \pm 58.8$
1300	$3.16 \times 10^{-2}$	$ee$	$1.41 \pm 0.28$	$1.24 \pm 2.48 \times 10^{-1}$	$292.8 \pm 60.0$
		$\mu\mu$	$0.97 \pm 0.19$	$8.49 \times 10^{-1} \pm 1.70 \times 10^{-1}$	$288.6 \pm 58.5$
1400	$2.40 \times 10^{-2}$	$ee$	$1.43 \pm 0.29$	$9.51 \times 10^{-1} \pm 1.91 \times 10^{-1}$	$298.8 \pm 61.2$
		$\mu\mu$	$0.97 \pm 0.19$	$6.47 \times 10^{-1} \pm 1.30 \times 10^{-1}$	$311.7 \pm 63.2$
1500	$1.84 \times 10^{-2}$	$ee$	$1.44 \pm 0.29$	$7.36 \times 10^{-1} \pm 1.47 \times 10^{-1}$	$287.9 \pm 59.1$
		$\mu\mu$	$0.96 \pm 0.19$	$4.90 \times 10^{-1} \pm 9.82 \times 10^{-2}$	$298.7 \pm 60.6$

Table F.3: Inputs for the  $Z'\chi_2 \rightarrow l^+l^-\chi_1\chi_1$  HDS  $\sigma B$  calculations. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	$6.93 \times 10^{-1}$	$ee$	$0.30 \pm 0.06$	$5.72 \pm 1.16$	$93.6 \pm 20.6$
		$\mu\mu$	$0.24 \pm 0.05$	$4.66 \pm 9.44 \times 10^{-1}$	$104.4 \pm 21.9$
200	$1.41 \times 10^{-1}$	$ee$	$0.69 \pm 0.14$	$2.71 \pm 5.45 \times 10^{-1}$	$102.5 \pm 22.7$
		$\mu\mu$	$0.51 \pm 0.10$	$2.02 \pm 4.08 \times 10^{-1}$	$102.4 \pm 21.4$
400	$6.90 \times 10^{-3}$	$ee$	$1.30 \pm 0.26$	$2.48 \times 10^{-1} \pm 4.99 \times 10^{-2}$	$107.2 \pm 22.7$
		$\mu\mu$	$0.91 \pm 0.18$	$1.75 \times 10^{-1} \pm 3.52 \times 10^{-2}$	$110.2 \pm 23.1$
600	$8.81 \times 10^{-4}$	$ee$	$1.56 \pm 0.31$	$3.83 \times 10^{-2} \pm 7.67 \times 10^{-3}$	$98.2 \pm 21.1$
		$\mu\mu$	$1.06 \pm 0.21$	$2.60 \times 10^{-2} \pm 5.21 \times 10^{-3}$	$91.4 \pm 19.7$
800	$1.66 \times 10^{-4}$	$ee$	$1.66 \pm 0.33$	$7.65 \times 10^{-3} \pm 1.53 \times 10^{-3}$	$101.6 \pm 21.6$
		$\mu\mu$	$1.16 \pm 0.23$	$5.33 \times 10^{-3} \pm 1.07 \times 10^{-3}$	$100.5 \pm 21.2$
900	$7.74 \times 10^{-5}$	$ee$	$1.71 \pm 0.34$	$3.67 \times 10^{-3} \pm 7.36 \times 10^{-4}$	$106.0 \pm 22.5$
		$\mu\mu$	$1.19 \pm 0.24$	$2.56 \times 10^{-3} \pm 5.14 \times 10^{-4}$	$89.2 \pm 19.0$
1100	$1.87 \times 10^{-5}$	$ee$	$1.73 \pm 0.35$	$9.03 \times 10^{-4} \pm 1.81 \times 10^{-4}$	$84.2 \pm 18.8$
		$\mu\mu$	$1.19 \pm 0.24$	$6.22 \times 10^{-4} \pm 1.25 \times 10^{-4}$	$106.1 \pm 22.3$
1200	$9.53 \times 10^{-6}$	$ee$	$1.76 \pm 0.35$	$4.65 \times 10^{-4} \pm 9.33 \times 10^{-5}$	$100.2 \pm 21.4$
		$\mu\mu$	$1.22 \pm 0.24$	$3.22 \times 10^{-4} \pm 6.46 \times 10^{-5}$	$105.1 \pm 22.0$
1300	$4.93 \times 10^{-6}$	$ee$	$1.73 \pm 0.35$	$2.38 \times 10^{-4} \pm 4.76 \times 10^{-5}$	$77.0 \pm 17.7$
		$\mu\mu$	$1.20 \pm 0.24$	$1.64 \times 10^{-4} \pm 3.30 \times 10^{-5}$	$104.5 \pm 22.0$
1400	$2.59 \times 10^{-6}$	$ee$	$1.79 \pm 0.36$	$1.29 \times 10^{-4} \pm 2.60 \times 10^{-5}$	$98.5 \pm 21.3$
		$\mu\mu$	$1.21 \pm 0.24$	$8.73 \times 10^{-5} \pm 1.75 \times 10^{-5}$	$97.8 \pm 20.6$
1500	$1.38 \times 10^{-6}$	$ee$	$1.79 \pm 0.36$	$6.86 \times 10^{-5} \pm 1.38 \times 10^{-5}$	$111.1 \pm 23.5$
		$\mu\mu$	$1.20 \pm 0.24$	$4.61 \times 10^{-5} \pm 9.26 \times 10^{-6}$	$96.3 \pm 20.2$

Table F.4: Inputs for the  $Z'\chi_2 \rightarrow l^+l^-\chi_1\chi_1$  LDS  $\sigma B$  calculations. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	6.80	$ee$	$0.07 \pm 0.01$	$13.8 \pm 2.83$	$182.6 \pm 38.0$
		$\mu\mu$	$0.05 \pm 0.01$	$10.0 \pm 2.07$	$260.9 \pm 52.9$
200	2.37	$ee$	$0.18 \pm 0.04$	$12.0 \pm 2.43$	$191.4 \pm 39.8$
		$\mu\mu$	$0.13 \pm 0.03$	$8.88 \pm 1.81$	$258.9 \pm 52.4$
400	$2.89 \times 10^{-1}$	$ee$	$0.68 \pm 0.14$	$5.45 \pm 1.10$	$186.6 \pm 38.7$
		$\mu\mu$	$0.41 \pm 0.08$	$3.28 \pm 6.61 \times 10^{-1}$	$256.9 \pm 52.0$
600	$7.34 \times 10^{-2}$	$ee$	$1.01 \pm 0.20$	$2.06 \pm 4.13 \times 10^{-1}$	$194.8 \pm 40.2$
		$\mu\mu$	$0.65 \pm 0.13$	$1.32 \pm 2.65 \times 10^{-1}$	$268.6 \pm 54.4$
800	$2.59 \times 10^{-2}$	$ee$	$1.21 \pm 0.24$	$8.71 \times 10^{-1} \pm 1.75 \times 10^{-1}$	$182.7 \pm 38.4$
		$\mu\mu$	$0.80 \pm 0.16$	$5.74 \times 10^{-1} \pm 1.15 \times 10^{-1}$	$256.9 \pm 52.0$
900	$1.65 \times 10^{-2}$	$ee$	$1.29 \pm 0.26$	$5.90 \times 10^{-1} \pm 1.18 \times 10^{-1}$	$176.1 \pm 36.5$
		$\mu\mu$	$0.86 \pm 0.17$	$3.92 \times 10^{-1} \pm 7.88 \times 10^{-2}$	$243.3 \pm 49.3$
1100	$7.34 \times 10^{-3}$	$ee$	$1.35 \pm 0.27$	$2.76 \times 10^{-1} \pm 5.52 \times 10^{-2}$	$190.8 \pm 39.4$
		$\mu\mu$	$0.92 \pm 0.18$	$1.87 \times 10^{-1} \pm 3.75 \times 10^{-2}$	$240.9 \pm 48.8$
1200	$5.08 \times 10^{-3}$	$ee$	$1.41 \pm 0.28$	$2.00 \times 10^{-1} \pm 4.00 \times 10^{-2}$	$179.8 \pm 37.2$
		$\mu\mu$	$0.96 \pm 0.19$	$1.36 \times 10^{-1} \pm 2.73 \times 10^{-2}$	$250.8 \pm 50.8$
1300	$3.58 \times 10^{-3}$	$ee$	$1.43 \pm 0.29$	$1.42 \times 10^{-1} \pm 2.84 \times 10^{-2}$	$190.7 \pm 39.5$
		$\mu\mu$	$0.98 \pm 0.20$	$9.72 \times 10^{-2} \pm 1.95 \times 10^{-2}$	$245.3 \pm 49.6$
1400	$2.56 \times 10^{-3}$	$ee$	$1.46 \pm 0.29$	$1.04 \times 10^{-1} \pm 2.08 \times 10^{-2}$	$185.9 \pm 38.9$
		$\mu\mu$	$0.99 \pm 0.20$	$7.09 \times 10^{-2} \pm 1.42 \times 10^{-2}$	$260.4 \pm 52.9$
1500	$1.86 \times 10^{-3}$	$ee$	$1.48 \pm 0.30$	$7.68 \times 10^{-2} \pm 1.54 \times 10^{-2}$	$185.1 \pm 38.2$
		$\mu\mu$	$0.98 \pm 0.20$	$5.10 \times 10^{-2} \pm 1.02 \times 10^{-2}$	$245.4 \pm 49.7$

Table F.5: Inputs for the EFT  $\rightarrow Z'\chi\chi$  HDS  $\sigma B$  calculations. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	$7.81 \times 10^{-6}$	$ee$	$0.28 \pm 0.06$	$6.08 \times 10^{-5} \pm 1.23 \times 10^{-5}$	$121.2 \pm 26.6$
		$\mu\mu$	$0.23 \pm 0.05$	$4.96 \times 10^{-5} \pm 1.01 \times 10^{-5}$	$105.8 \pm 22.4$
200	$6.81 \times 10^{-7}$	$ee$	$0.65 \pm 0.13$	$1.22 \times 10^{-5} \pm 2.46 \times 10^{-6}$	$139.3 \pm 29.1$
		$\mu\mu$	$0.49 \pm 0.10$	$9.19 \times 10^{-6} \pm 1.85 \times 10^{-6}$	$103.0 \pm 21.6$
300	$6.01 \times 10^{-8}$	$ee$	$1.01 \pm 0.20$	$1.69 \times 10^{-6} \pm 3.39 \times 10^{-7}$	$113.8 \pm 25.0$
		$\mu\mu$	$0.76 \pm 0.15$	$1.28 \times 10^{-6} \pm 2.57 \times 10^{-7}$	$113.3 \pm 23.8$
400	$8.42 \times 10^{-9}$	$ee$	$1.30 \pm 0.26$	$3.06 \times 10^{-7} \pm 6.13 \times 10^{-8}$	$118.0 \pm 25.7$
		$\mu\mu$	$0.92 \pm 0.18$	$2.16 \times 10^{-7} \pm 4.33 \times 10^{-8}$	$107.9 \pm 22.6$
500	$1.80 \times 10^{-9}$	$ee$	$1.46 \pm 0.29$	$7.32 \times 10^{-8} \pm 1.47 \times 10^{-8}$	$108.6 \pm 24.9$
		$\mu\mu$	$1.03 \pm 0.21$	$5.16 \times 10^{-8} \pm 1.04 \times 10^{-8}$	$97.9 \pm 20.7$
600	$4.83 \times 10^{-10}$	$ee$	$1.55 \pm 0.31$	$2.09 \times 10^{-8} \pm 4.18 \times 10^{-9}$	$117.8 \pm 25.0$
		$\mu\mu$	$1.09 \pm 0.22$	$1.46 \times 10^{-8} \pm 2.92 \times 10^{-9}$	$115.5 \pm 24.2$
700	$1.49 \times 10^{-10}$	$ee$	$1.64 \pm 0.33$	$6.82 \times 10^{-9} \pm 1.37 \times 10^{-9}$	$122.2 \pm 26.1$
		$\mu\mu$	$1.15 \pm 0.23$	$4.76 \times 10^{-9} \pm 9.56 \times 10^{-10}$	$113.3 \pm 23.9$
800	$5.12 \times 10^{-11}$	$ee$	$1.68 \pm 0.34$	$2.39 \times 10^{-9} \pm 4.80 \times 10^{-10}$	$118.5 \pm 25.0$
		$\mu\mu$	$1.17 \pm 0.23$	$1.66 \times 10^{-9} \pm 3.34 \times 10^{-10}$	$105.3 \pm 22.1$
900	$1.90 \times 10^{-11}$	$ee$	$1.71 \pm 0.34$	$9.05 \times 10^{-10} \pm 1.81 \times 10^{-10}$	$122.2 \pm 25.8$
		$\mu\mu$	$1.15 \pm 0.23$	$6.09 \times 10^{-10} \pm 1.22 \times 10^{-10}$	$116.5 \pm 24.4$
1000	$7.47 \times 10^{-12}$	$ee$	$1.70 \pm 0.34$	$3.53 \times 10^{-10} \pm 7.07 \times 10^{-11}$	$123.0 \pm 26.0$
		$\mu\mu$	$1.17 \pm 0.23$	$2.44 \times 10^{-10} \pm 4.89 \times 10^{-11}$	$117.0 \pm 24.6$
1100	$3.07 \times 10^{-12}$	$ee$	$1.74 \pm 0.35$	$1.48 \times 10^{-10} \pm 2.97 \times 10^{-11}$	$108.7 \pm 23.3$
		$\mu\mu$	$1.17 \pm 0.23$	$1.00 \times 10^{-10} \pm 2.01 \times 10^{-11}$	$100.9 \pm 21.3$
1200	$1.31 \times 10^{-12}$	$ee$	$1.75 \pm 0.35$	$6.41 \times 10^{-11} \pm 1.28 \times 10^{-11}$	$122.8 \pm 26.0$
		$\mu\mu$	$1.23 \pm 0.25$	$4.49 \times 10^{-11} \pm 9.01 \times 10^{-12}$	$109.7 \pm 23.1$
1300	$5.80 \times 10^{-13}$	$ee$	$1.75 \pm 0.35$	$2.82 \times 10^{-11} \pm 5.65 \times 10^{-12}$	$120.9 \pm 26.6$
		$\mu\mu$	$1.23 \pm 0.25$	$1.99 \times 10^{-11} \pm 3.99 \times 10^{-12}$	$115.4 \pm 24.4$
1400	$2.63 \times 10^{-13}$	$ee$	$1.74 \pm 0.35$	$1.27 \times 10^{-11} \pm 2.55 \times 10^{-12}$	$123.9 \pm 26.1$
		$\mu\mu$	$1.18 \pm 0.24$	$8.64 \times 10^{-12} \pm 1.73 \times 10^{-12}$	$107.3 \pm 22.6$
1500	$1.22 \times 10^{-13}$	$ee$	$1.78 \pm 0.36$	$6.02 \times 10^{-12} \pm 1.21 \times 10^{-12}$	$115.3 \pm 24.6$
		$\mu\mu$	$1.22 \pm 0.24$	$4.15 \times 10^{-12} \pm 8.32 \times 10^{-13}$	$108.3 \pm 22.8$

Table F.6: Inputs for the EFT  $\rightarrow Z'\chi\chi$  LDS  $\sigma B$  calculations. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	$3.35 \times 10^{-5}$	$ee$	$0.06 \pm 0.01$	$5.20 \times 10^{-5} \pm 1.07 \times 10^{-5}$	$248.4 \pm 51.7$
		$\mu\mu$	$0.04 \pm 0.01$	$3.98 \times 10^{-5} \pm 8.28 \times 10^{-6}$	$292.5 \pm 59.2$
200	$2.67 \times 10^{-6}$	$ee$	$0.17 \pm 0.03$	$1.23 \times 10^{-5} \pm 2.50 \times 10^{-6}$	$245.0 \pm 50.3$
		$\mu\mu$	$0.12 \pm 0.02$	$9.11 \times 10^{-6} \pm 1.86 \times 10^{-6}$	$291.6 \pm 59.0$
300	$2.06 \times 10^{-7}$	$ee$	$0.36 \pm 0.07$	$2.06 \times 10^{-6} \pm 4.15 \times 10^{-7}$	$248.1 \pm 51.0$
		$\mu\mu$	$0.24 \pm 0.05$	$1.36 \times 10^{-6} \pm 2.75 \times 10^{-7}$	$284.7 \pm 57.7$
400	$2.65 \times 10^{-8}$	$ee$	$0.61 \pm 0.12$	$4.52 \times 10^{-7} \pm 9.09 \times 10^{-8}$	$250.6 \pm 51.7$
		$\mu\mu$	$0.40 \pm 0.08$	$2.93 \times 10^{-7} \pm 5.91 \times 10^{-8}$	$281.9 \pm 57.0$
500	$5.46 \times 10^{-9}$	$ee$	$0.82 \pm 0.16$	$1.24 \times 10^{-7} \pm 2.48 \times 10^{-8}$	$243.1 \pm 50.3$
		$\mu\mu$	$0.51 \pm 0.10$	$7.69 \times 10^{-8} \pm 1.55 \times 10^{-8}$	$293.3 \pm 59.4$
600	$1.47 \times 10^{-9}$	$ee$	$1.03 \pm 0.21$	$4.21 \times 10^{-8} \pm 8.44 \times 10^{-9}$	$244.9 \pm 50.8$
		$\mu\mu$	$0.62 \pm 0.12$	$2.53 \times 10^{-8} \pm 5.08 \times 10^{-9}$	$294.2 \pm 59.5$
700	$4.72 \times 10^{-10}$	$ee$	$1.13 \pm 0.23$	$1.48 \times 10^{-8} \pm 2.97 \times 10^{-9}$	$256.1 \pm 52.4$
		$\mu\mu$	$0.73 \pm 0.15$	$9.56 \times 10^{-9} \pm 1.92 \times 10^{-9}$	$298.1 \pm 60.3$
800	$1.73 \times 10^{-10}$	$ee$	$1.22 \pm 0.24$	$5.89 \times 10^{-9} \pm 1.18 \times 10^{-9}$	$245.5 \pm 51.2$
		$\mu\mu$	$0.82 \pm 0.16$	$3.93 \times 10^{-9} \pm 7.89 \times 10^{-10}$	$301.5 \pm 61.1$
900	$7.02 \times 10^{-11}$	$ee$	$1.25 \pm 0.25$	$2.45 \times 10^{-9} \pm 4.91 \times 10^{-10}$	$257.9 \pm 52.7$
		$\mu\mu$	$0.88 \pm 0.18$	$1.71 \times 10^{-9} \pm 3.43 \times 10^{-10}$	$281.0 \pm 57.0$
1000	$3.09 \times 10^{-11}$	$ee$	$1.35 \pm 0.27$	$1.16 \times 10^{-9} \pm 2.32 \times 10^{-10}$	$251.1 \pm 51.5$
		$\mu\mu$	$0.89 \pm 0.18$	$7.66 \times 10^{-10} \pm 1.54 \times 10^{-10}$	$290.3 \pm 58.8$
1100	$1.45 \times 10^{-11}$	$ee$	$1.40 \pm 0.28$	$5.63 \times 10^{-10} \pm 1.13 \times 10^{-10}$	$238.6 \pm 49.0$
		$\mu\mu$	$0.95 \pm 0.19$	$3.85 \times 10^{-10} \pm 7.72 \times 10^{-11}$	$291.4 \pm 59.0$
1200	$7.19 \times 10^{-12}$	$ee$	$1.39 \pm 0.28$	$2.78 \times 10^{-10} \pm 5.57 \times 10^{-11}$	$249.4 \pm 51.0$
		$\mu\mu$	$0.95 \pm 0.19$	$1.89 \times 10^{-10} \pm 3.80 \times 10^{-11}$	$300.7 \pm 60.8$
1300	$3.74 \times 10^{-12}$	$ee$	$1.45 \pm 0.29$	$1.51 \times 10^{-10} \pm 3.02 \times 10^{-11}$	$242.4 \pm 50.0$
		$\mu\mu$	$0.97 \pm 0.19$	$1.01 \times 10^{-10} \pm 2.03 \times 10^{-11}$	$307.5 \pm 62.2$
1400	$2.02 \times 10^{-12}$	$ee$	$1.48 \pm 0.30$	$8.31 \times 10^{-11} \pm 1.67 \times 10^{-11}$	$244.0 \pm 50.7$
		$\mu\mu$	$1.00 \pm 0.20$	$5.65 \times 10^{-11} \pm 1.13 \times 10^{-11}$	$315.4 \pm 63.9$
1500	$1.13 \times 10^{-12}$	$ee$	$1.49 \pm 0.30$	$4.69 \times 10^{-11} \pm 9.40 \times 10^{-12}$	$230.8 \pm 47.4$
		$\mu\mu$	$0.98 \pm 0.20$	$3.07 \times 10^{-11} \pm 6.16 \times 10^{-12}$	$301.5 \pm 61.1$

Table F.7: Inputs for the  $Z'h_D \rightarrow l^+l^-\chi\chi$  HDS  $\sigma B$  calculations in SR1. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	1.11	$ee$	$0.04 \pm 0.01$	$1.21 \pm 0.26$	$283.9 \pm 58.7$
		$\mu\mu$	$0.03 \pm 0.01$	$1.06 \pm 0.23$	$282.7 \pm 57.2$
200	$2.46 \times 10^{-1}$	$ee$	$0.09 \pm 0.02$	$5.84 \times 10^{-1} \pm 1.22 \times 10^{-1}$	$273.9 \pm 55.9$
		$\mu\mu$	$0.05 \pm 0.01$	$3.45 \times 10^{-1} \pm 7.37 \times 10^{-2}$	$275.4 \pm 59.3$
400	$1.49 \times 10^{-2}$	$ee$	$0.09 \pm 0.02$	$3.90 \times 10^{-2} \pm 8.12 \times 10^{-3}$	$281.9 \pm 57.4$
		$\mu\mu$	$0.05 \pm 0.01$	$2.09 \times 10^{-2} \pm 4.49 \times 10^{-3}$	$294.8 \pm 59.7$
600	$2.35 \times 10^{-3}$	$ee$	$0.07 \pm 0.01$	$4.59 \times 10^{-3} \pm 9.69 \times 10^{-4}$	$267.8 \pm 54.5$
		$\mu\mu$	$0.03 \pm 0.01$	$2.07 \times 10^{-3} \pm 4.60 \times 10^{-4}$	$302.5 \pm 61.2$
800	$5.43 \times 10^{-4}$	$ee$	$0.05 \pm 0.01$	$7.29 \times 10^{-4} \pm 1.58 \times 10^{-4}$	$296.4 \pm 60.4$
		$\mu\mu$	$0.03 \pm 0.01$	$4.96 \times 10^{-4} \pm 1.11 \times 10^{-4}$	$317.0 \pm 64.1$
900	$2.82 \times 10^{-4}$	$ee$	$0.04 \pm 0.01$	$3.40 \times 10^{-4} \pm 7.42 \times 10^{-5}$	$270.4 \pm 55.1$
		$\mu\mu$	$0.02 \pm 0.00$	$1.78 \times 10^{-4} \pm 4.11 \times 10^{-5}$	$297.2 \pm 60.1$
1100	$8.40 \times 10^{-5}$	$ee$	$0.03 \pm 0.01$	$7.13 \times 10^{-5} \pm 1.62 \times 10^{-5}$	$276.8 \pm 57.1$
		$\mu\mu$	$0.02 \pm 0.00$	$4.47 \times 10^{-5} \pm 1.06 \times 10^{-5}$	$284.8 \pm 57.7$
1200	$4.75 \times 10^{-5}$	$ee$	$0.02 \pm 0.00$	$2.85 \times 10^{-5} \pm 6.70 \times 10^{-6}$	$276.0 \pm 57.2$
		$\mu\mu$	$0.02 \pm 0.00$	$2.57 \times 10^{-5} \pm 6.13 \times 10^{-6}$	$293.6 \pm 59.4$
1300	$2.73 \times 10^{-5}$	$ee$	$0.03 \pm 0.01$	$2.23 \times 10^{-5} \pm 5.08 \times 10^{-6}$	$286.0 \pm 58.2$
		$\mu\mu$	$0.02 \pm 0.00$	$1.32 \times 10^{-5} \pm 3.19 \times 10^{-6}$	$265.9 \pm 57.6$
1400	$1.60 \times 10^{-5}$	$ee$	$0.02 \pm 0.00$	$1.10 \times 10^{-5} \pm 2.54 \times 10^{-6}$	$279.5 \pm 57.0$
		$\mu\mu$	$0.02 \pm 0.00$	$7.78 \times 10^{-6} \pm 1.89 \times 10^{-6}$	$308.7 \pm 62.4$
1500	$9.42 \times 10^{-6}$	$ee$	$0.02 \pm 0.00$	$5.83 \times 10^{-6} \pm 1.36 \times 10^{-6}$	$268.5 \pm 55.5$
		$\mu\mu$	$0.01 \pm 0.00$	$3.13 \times 10^{-6} \pm 8.26 \times 10^{-7}$	$303.1 \pm 61.3$

Table F.8: Inputs for the  $Z'h_D \rightarrow l^+l^-\chi\chi$  HDS  $\sigma B$  calculations in SR2. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	1.11	$ee$	$0.10 \pm 0.02$	$3.17 \pm 0.65$	$59.6 \pm 15.2$
		$\mu\mu$	$0.08 \pm 0.02$	$2.41 \pm 0.50$	$80.8 \pm 16.9$
200	$2.46 \times 10^{-1}$	$ee$	$0.16 \pm 0.03$	$1.07 \pm 0.22$	$66.5 \pm 16.4$
		$\mu\mu$	$0.12 \pm 0.02$	$7.89 \times 10^{-1} \pm 1.62 \times 10^{-1}$	$78.9 \pm 16.7$
400	$1.49 \times 10^{-2}$	$ee$	$0.16 \pm 0.03$	$6.43 \times 10^{-2} \pm 1.32 \times 10^{-2}$	$55.5 \pm 13.4$
		$\mu\mu$	$0.10 \pm 0.02$	$4.34 \times 10^{-2} \pm 8.99 \times 10^{-3}$	$83.4 \pm 17.6$
600	$2.35 \times 10^{-3}$	$ee$	$0.13 \pm 0.03$	$8.19 \times 10^{-3} \pm 1.69 \times 10^{-3}$	$55.5 \pm 13.6$
		$\mu\mu$	$0.08 \pm 0.02$	$5.44 \times 10^{-3} \pm 1.14 \times 10^{-3}$	$77.9 \pm 16.3$
800	$5.43 \times 10^{-4}$	$ee$	$0.08 \pm 0.02$	$1.27 \times 10^{-3} \pm 2.67 \times 10^{-4}$	$63.6 \pm 13.9$
		$\mu\mu$	$0.07 \pm 0.01$	$9.86 \times 10^{-4} \pm 2.09 \times 10^{-4}$	$78.5 \pm 16.7$
900	$2.82 \times 10^{-4}$	$ee$	$0.08 \pm 0.02$	$6.43 \times 10^{-4} \pm 1.35 \times 10^{-4}$	$64.9 \pm 14.6$
		$\mu\mu$	$0.06 \pm 0.01$	$4.35 \times 10^{-4} \pm 9.30 \times 10^{-5}$	$80.8 \pm 17.1$
1100	$8.40 \times 10^{-5}$	$ee$	$0.06 \pm 0.01$	$1.43 \times 10^{-4} \pm 3.06 \times 10^{-5}$	$59.8 \pm 13.3$
		$\mu\mu$	$0.05 \pm 0.01$	$1.17 \times 10^{-4} \pm 2.53 \times 10^{-5}$	$83.0 \pm 17.3$
1200	$4.75 \times 10^{-5}$	$ee$	$0.06 \pm 0.01$	$7.42 \times 10^{-5} \pm 1.59 \times 10^{-5}$	$53.8 \pm 14.3$
		$\mu\mu$	$0.04 \pm 0.01$	$4.67 \times 10^{-5} \pm 1.03 \times 10^{-5}$	$80.8 \pm 17.0$
1300	$2.73 \times 10^{-5}$	$ee$	$0.05 \pm 0.01$	$3.81 \times 10^{-5} \pm 8.25 \times 10^{-6}$	$64.3 \pm 14.3$
		$\mu\mu$	$0.04 \pm 0.01$	$2.81 \times 10^{-5} \pm 6.21 \times 10^{-6}$	$78.0 \pm 16.4$
1400	$1.60 \times 10^{-5}$	$ee$	$0.04 \pm 0.01$	$1.88 \times 10^{-5} \pm 4.13 \times 10^{-6}$	$54.7 \pm 13.5$
		$\mu\mu$	$0.03 \pm 0.01$	$1.32 \times 10^{-5} \pm 2.99 \times 10^{-6}$	$82.7 \pm 17.4$
1500	$9.42 \times 10^{-6}$	$ee$	$0.04 \pm 0.01$	$1.17 \times 10^{-5} \pm 2.55 \times 10^{-6}$	$48.9 \pm 13.6$
		$\mu\mu$	$0.03 \pm 0.01$	$7.75 \times 10^{-6} \pm 1.75 \times 10^{-6}$	$87.6 \pm 18.3$

Table F.9: Inputs for the  $Z'h_D \rightarrow l^+l^-\chi\chi$  HDS  $\sigma B$  calculations in SR3. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	1.11	$ee$	$0.08 \pm 0.02$	$2.62 \pm 0.54$	$17.9 \pm 4.7$
		$\mu\mu$	$0.05 \pm 0.01$	$1.54 \pm 0.33$	$23.6 \pm 5.8$
200	$2.46 \times 10^{-1}$	$ee$	$0.28 \pm 0.06$	$1.91 \pm 0.39$	$15.7 \pm 6.7$
		$\mu\mu$	$0.19 \pm 0.04$	$1.27 \pm 0.26$	$24.5 \pm 6.0$
400	$1.49 \times 10^{-2}$	$ee$	$0.82 \pm 0.16$	$3.38 \times 10^{-1} \pm 6.79 \times 10^{-2}$	$15.3 \pm 4.6$
		$\mu\mu$	$0.57 \pm 0.11$	$2.34 \times 10^{-1} \pm 4.72 \times 10^{-2}$	$21.9 \pm 5.2$
600	$2.35 \times 10^{-3}$	$ee$	$1.19 \pm 0.24$	$7.74 \times 10^{-2} \pm 1.55 \times 10^{-2}$	$12.7 \pm 6.4$
		$\mu\mu$	$0.84 \pm 0.17$	$5.47 \times 10^{-2} \pm 1.10 \times 10^{-2}$	$20.8 \pm 4.9$
800	$5.43 \times 10^{-4}$	$ee$	$1.37 \pm 0.27$	$2.06 \times 10^{-2} \pm 4.14 \times 10^{-3}$	$14.0 \pm 6.4$
		$\mu\mu$	$0.97 \pm 0.19$	$1.46 \times 10^{-2} \pm 2.93 \times 10^{-3}$	$20.1 \pm 5.2$
900	$2.82 \times 10^{-4}$	$ee$	$1.44 \pm 0.29$	$1.13 \times 10^{-2} \pm 2.27 \times 10^{-3}$	$15.2 \pm 4.7$
		$\mu\mu$	$1.04 \pm 0.21$	$8.14 \times 10^{-3} \pm 1.63 \times 10^{-3}$	$21.9 \pm 5.2$
1100	$8.40 \times 10^{-5}$	$ee$	$1.55 \pm 0.31$	$3.62 \times 10^{-3} \pm 7.25 \times 10^{-4}$	$18.0 \pm 6.7$
		$\mu\mu$	$1.08 \pm 0.22$	$2.52 \times 10^{-3} \pm 5.06 \times 10^{-4}$	$23.7 \pm 5.8$
1200	$4.75 \times 10^{-5}$	$ee$	$1.60 \pm 0.32$	$2.11 \times 10^{-3} \pm 4.23 \times 10^{-4}$	$14.2 \pm 4.5$
		$\mu\mu$	$1.10 \pm 0.22$	$1.46 \times 10^{-3} \pm 2.92 \times 10^{-4}$	$20.9 \pm 5.0$
1300	$2.73 \times 10^{-5}$	$ee$	$1.61 \pm 0.32$	$1.22 \times 10^{-3} \pm 2.45 \times 10^{-4}$	$18.0 \pm 6.7$
		$\mu\mu$	$1.11 \pm 0.22$	$8.42 \times 10^{-4} \pm 1.69 \times 10^{-4}$	$19.3 \pm 5.1$
1400	$1.60 \times 10^{-5}$	$ee$	$1.62 \pm 0.32$	$7.20 \times 10^{-4} \pm 1.44 \times 10^{-4}$	$19.2 \pm 5.3$
		$\mu\mu$	$1.10 \pm 0.22$	$4.88 \times 10^{-4} \pm 9.80 \times 10^{-5}$	$21.5 \pm 5.2$
1500	$9.42 \times 10^{-6}$	$ee$	$1.64 \pm 0.33$	$4.30 \times 10^{-4} \pm 8.62 \times 10^{-5}$	$14.4 \pm 5.0$
		$\mu\mu$	$1.08 \pm 0.22$	$2.84 \times 10^{-4} \pm 5.70 \times 10^{-5}$	$19.4 \pm 4.6$

Table F.10: Inputs for the  $Z'h_D \rightarrow l^+l^-\chi\chi$  LDS  $\sigma B$  calculations in SR1. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	1.24	$ee$	$0.04 \pm 0.01$	$1.32 \pm 0.27$	$289.1 \pm 59.0$
		$\mu\mu$	$0.03 \pm 0.01$	$1.08 \pm 0.23$	$272.3 \pm 58.7$
200	1.05	$ee$	$0.07 \pm 0.01$	$2.16 \pm 0.44$	$276.7 \pm 56.6$
		$\mu\mu$	$0.05 \pm 0.01$	$1.32 \pm 0.27$	$297.5 \pm 60.1$
400	$6.08 \times 10^{-1}$	$ee$	$0.12 \pm 0.02$	$1.98 \pm 0.40$	$268.2 \pm 55.2$
		$\mu\mu$	$0.06 \pm 0.01$	$1.10 \pm 0.23$	$292.4 \pm 59.1$
600	$2.88 \times 10^{-1}$	$ee$	$0.17 \pm 0.03$	$1.37 \pm 0.28$	$276.6 \pm 56.5$
		$\mu\mu$	$0.10 \pm 0.02$	$7.91 \times 10^{-1} \pm 1.61 \times 10^{-1}$	$300.0 \pm 60.7$
800	$1.44 \times 10^{-1}$	$ee$	$0.24 \pm 0.05$	$9.67 \times 10^{-1} \pm 1.95 \times 10^{-1}$	$273.4 \pm 56.2$
		$\mu\mu$	$0.14 \pm 0.03$	$5.77 \times 10^{-1} \pm 1.17 \times 10^{-1}$	$268.9 \pm 58.1$
900	$1.04 \times 10^{-1}$	$ee$	$0.26 \pm 0.05$	$7.39 \times 10^{-1} \pm 1.49 \times 10^{-1}$	$289.5 \pm 59.5$
		$\mu\mu$	$0.14 \pm 0.03$	$4.06 \times 10^{-1} \pm 8.21 \times 10^{-2}$	$304.2 \pm 61.5$
1100	$5.61 \times 10^{-2}$	$ee$	$0.25 \pm 0.05$	$3.93 \times 10^{-1} \pm 7.91 \times 10^{-2}$	$283.6 \pm 57.7$
		$\mu\mu$	$0.14 \pm 0.03$	$2.13 \times 10^{-1} \pm 4.32 \times 10^{-2}$	$293.3 \pm 59.3$
1200	$4.19 \times 10^{-2}$	$ee$	$0.25 \pm 0.05$	$2.93 \times 10^{-1} \pm 5.89 \times 10^{-2}$	$287.9 \pm 58.7$
		$\mu\mu$	$0.14 \pm 0.03$	$1.60 \times 10^{-1} \pm 3.24 \times 10^{-2}$	$297.7 \pm 60.2$
1300	$3.16 \times 10^{-2}$	$ee$	$0.24 \pm 0.05$	$2.14 \times 10^{-1} \pm 4.31 \times 10^{-2}$	$296.1 \pm 60.7$
		$\mu\mu$	$0.13 \pm 0.03$	$1.17 \times 10^{-1} \pm 2.38 \times 10^{-2}$	$284.8 \pm 61.1$
1400	$2.40 \times 10^{-2}$	$ee$	$0.24 \pm 0.05$	$1.57 \times 10^{-1} \pm 3.17 \times 10^{-2}$	$274.4 \pm 56.2$
		$\mu\mu$	$0.13 \pm 0.03$	$8.35 \times 10^{-2} \pm 1.69 \times 10^{-2}$	$303.4 \pm 61.4$
1500	$1.84 \times 10^{-2}$	$ee$	$0.23 \pm 0.05$	$1.20 \times 10^{-1} \pm 2.42 \times 10^{-2}$	$277.0 \pm 56.6$
		$\mu\mu$	$0.12 \pm 0.02$	$5.99 \times 10^{-2} \pm 1.22 \times 10^{-2}$	$308.6 \pm 62.4$

Table F.11: Inputs for the  $Z'h_D \rightarrow l^+l^-\chi\chi$  LDS  $\sigma B$  calculations in SR2. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	1.24	$ee$	$0.09 \pm 0.02$	$3.07 \pm 0.63$	$52.8 \pm 15.1$
		$\mu\mu$	$0.08 \pm 0.02$	$2.65 \pm 0.54$	$81.0 \pm 17.0$
200	1.05	$ee$	$0.10 \pm 0.02$	$2.84 \pm 0.58$	$62.5 \pm 15.7$
		$\mu\mu$	$0.07 \pm 0.01$	$2.17 \pm 0.44$	$72.9 \pm 15.3$
400	$6.08 \times 10^{-1}$	$ee$	$0.13 \pm 0.03$	$2.16 \pm 0.44$	$67.0 \pm 16.6$
		$\mu\mu$	$0.09 \pm 0.02$	$1.53 \pm 0.31$	$82.6 \pm 17.4$
600	$2.88 \times 10^{-1}$	$ee$	$0.21 \pm 0.04$	$1.67 \pm 0.34$	$59.4 \pm 13.2$
		$\mu\mu$	$0.15 \pm 0.03$	$1.18 \pm 0.24$	$83.8 \pm 17.5$
800	$1.44 \times 10^{-1}$	$ee$	$0.27 \pm 0.05$	$1.07 \pm 0.22$	$57.1 \pm 13.9$
		$\mu\mu$	$0.18 \pm 0.04$	$7.07 \times 10^{-1} \pm 1.43 \times 10^{-1}$	$74.5 \pm 15.6$
900	$1.04 \times 10^{-1}$	$ee$	$0.28 \pm 0.06$	$8.02 \times 10^{-1} \pm 1.62 \times 10^{-1}$	$65.9 \pm 14.6$
		$\mu\mu$	$0.18 \pm 0.04$	$5.20 \times 10^{-1} \pm 1.05 \times 10^{-1}$	$68.1 \pm 14.5$
1100	$5.61 \times 10^{-2}$	$ee$	$0.29 \pm 0.06$	$4.47 \times 10^{-1} \pm 9.00 \times 10^{-2}$	$62.9 \pm 14.3$
		$\mu\mu$	$0.19 \pm 0.04$	$2.98 \times 10^{-1} \pm 6.02 \times 10^{-2}$	$81.5 \pm 17.2$
1200	$4.19 \times 10^{-2}$	$ee$	$0.31 \pm 0.06$	$3.58 \times 10^{-1} \pm 7.21 \times 10^{-2}$	$56.2 \pm 14.6$
		$\mu\mu$	$0.18 \pm 0.04$	$2.06 \times 10^{-1} \pm 4.16 \times 10^{-2}$	$86.7 \pm 18.2$
1300	$3.16 \times 10^{-2}$	$ee$	$0.29 \pm 0.06$	$2.52 \times 10^{-1} \pm 5.07 \times 10^{-2}$	$56.7 \pm 13.1$
		$\mu\mu$	$0.18 \pm 0.04$	$1.54 \times 10^{-1} \pm 3.11 \times 10^{-2}$	$84.9 \pm 17.7$
1400	$2.40 \times 10^{-2}$	$ee$	$0.28 \pm 0.06$	$1.86 \times 10^{-1} \pm 3.75 \times 10^{-2}$	$60.0 \pm 15.0$
		$\mu\mu$	$0.17 \pm 0.03$	$1.17 \times 10^{-1} \pm 2.36 \times 10^{-2}$	$83.2 \pm 17.5$
1500	$1.84 \times 10^{-2}$	$ee$	$0.28 \pm 0.06$	$1.41 \times 10^{-1} \pm 2.83 \times 10^{-2}$	$50.4 \pm 11.6$
		$\mu\mu$	$0.17 \pm 0.03$	$8.82 \times 10^{-2} \pm 1.78 \times 10^{-2}$	$83.4 \pm 17.6$

Table F.12: Inputs for the  $Z'h_D \rightarrow l^+l^-\chi\chi$  LDS  $\sigma B$  calculations in SR3. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	1.24	$ee$	$0.07 \pm 0.01$	$2.55 \pm 0.52$	$15.1 \pm 6.6$
		$\mu\mu$	$0.05 \pm 0.01$	$1.58 \pm 0.33$	$20.5 \pm 5.0$
200	1.05	$ee$	$0.12 \pm 0.02$	$3.51 \pm 0.71$	$22.5 \pm 5.7$
		$\mu\mu$	$0.08 \pm 0.02$	$2.27 \pm 0.46$	$18.8 \pm 4.7$
400	$6.08 \times 10^{-1}$	$ee$	$0.14 \pm 0.03$	$2.44 \pm 0.49$	$20.1 \pm 5.2$
		$\mu\mu$	$0.10 \pm 0.02$	$1.66 \pm 0.34$	$20.1 \pm 4.8$
600	$2.88 \times 10^{-1}$	$ee$	$0.20 \pm 0.04$	$1.61 \pm 0.33$	$18.4 \pm 5.2$
		$\mu\mu$	$0.15 \pm 0.03$	$1.19 \pm 0.24$	$14.0 \pm 4.0$
800	$1.44 \times 10^{-1}$	$ee$	$0.36 \pm 0.07$	$1.45 \pm 0.29$	$22.1 \pm 6.0$
		$\mu\mu$	$0.27 \pm 0.05$	$1.09 \pm 0.22$	$14.1 \pm 3.9$
900	$1.04 \times 10^{-1}$	$ee$	$0.47 \pm 0.09$	$1.37 \pm 0.27$	$15.4 \pm 6.4$
		$\mu\mu$	$0.35 \pm 0.07$	$1.01 \pm 0.20$	$15.0 \pm 3.8$
1100	$5.61 \times 10^{-2}$	$ee$	$0.65 \pm 0.13$	$1.01 \pm 0.20$	$21.6 \pm 5.4$
		$\mu\mu$	$0.48 \pm 0.10$	$7.47 \times 10^{-1} \pm 1.50 \times 10^{-1}$	$17.0 \pm 4.4$
1200	$4.19 \times 10^{-2}$	$ee$	$0.74 \pm 0.15$	$8.59 \times 10^{-1} \pm 1.72 \times 10^{-1}$	$18.9 \pm 5.4$
		$\mu\mu$	$0.53 \pm 0.11$	$6.20 \times 10^{-1} \pm 1.24 \times 10^{-1}$	$16.9 \pm 4.3$
1300	$3.16 \times 10^{-2}$	$ee$	$0.80 \pm 0.16$	$7.04 \times 10^{-1} \pm 1.41 \times 10^{-1}$	$20.1 \pm 5.5$
		$\mu\mu$	$0.57 \pm 0.11$	$5.03 \times 10^{-1} \pm 1.01 \times 10^{-1}$	$16.6 \pm 4.5$
1400	$2.40 \times 10^{-2}$	$ee$	$0.84 \pm 0.17$	$5.64 \times 10^{-1} \pm 1.13 \times 10^{-1}$	$12.2 \pm 6.5$
		$\mu\mu$	$0.61 \pm 0.12$	$4.07 \times 10^{-1} \pm 8.16 \times 10^{-2}$	$19.9 \pm 4.9$
1500	$1.84 \times 10^{-2}$	$ee$	$0.89 \pm 0.18$	$4.53 \times 10^{-1} \pm 9.09 \times 10^{-2}$	$24.0 \pm 5.8$
		$\mu\mu$	$0.63 \pm 0.13$	$3.20 \times 10^{-1} \pm 6.42 \times 10^{-2}$	$19.0 \pm 4.7$

Table F.13: Inputs for the  $Z'\chi_2 \rightarrow l^+l^-\chi_1\chi_1$  HDS  $\sigma B$  calculations in SR1. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	$6.93 \times 10^{-1}$	$ee$	$0.05 \pm 0.01$	$8.85 \times 10^{-1} \pm 1.90 \times 10^{-1}$	$290.3 \pm 59.0$
		$\mu\mu$	$0.04 \pm 0.01$	$7.31 \times 10^{-1} \pm 1.58 \times 10^{-1}$	$296.4 \pm 59.9$
200	$1.41 \times 10^{-1}$	$ee$	$0.09 \pm 0.02$	$3.64 \times 10^{-1} \pm 7.58 \times 10^{-2}$	$285.5 \pm 58.4$
		$\mu\mu$	$0.06 \pm 0.01$	$2.24 \times 10^{-1} \pm 4.77 \times 10^{-2}$	$287.7 \pm 61.7$
400	$6.90 \times 10^{-3}$	$ee$	$0.07 \pm 0.01$	$1.25 \times 10^{-2} \pm 2.66 \times 10^{-3}$	$275.8 \pm 56.5$
		$\mu\mu$	$0.04 \pm 0.01$	$7.67 \times 10^{-3} \pm 1.68 \times 10^{-3}$	$304.0 \pm 61.4$
600	$8.81 \times 10^{-4}$	$ee$	$0.04 \pm 0.01$	$9.99 \times 10^{-4} \pm 2.20 \times 10^{-4}$	$278.9 \pm 57.5$
		$\mu\mu$	$0.02 \pm 0.00$	$4.92 \times 10^{-4} \pm 1.16 \times 10^{-4}$	$296.3 \pm 59.9$
800	$1.66 \times 10^{-4}$	$ee$	$0.02 \pm 0.00$	$1.12 \times 10^{-4} \pm 2.58 \times 10^{-5}$	$275.4 \pm 56.6$
		$\mu\mu$	$0.01 \pm 0.00$	$6.37 \times 10^{-5} \pm 1.61 \times 10^{-5}$	$290.0 \pm 58.7$
900	$7.74 \times 10^{-5}$	$ee$	$0.02 \pm 0.00$	$4.86 \times 10^{-5} \pm 1.14 \times 10^{-5}$	$285.9 \pm 58.7$
		$\mu\mu$	$0.01 \pm 0.00$	$2.43 \times 10^{-5} \pm 6.25 \times 10^{-6}$	$297.8 \pm 60.3$
1100	$1.87 \times 10^{-5}$	$ee$	$0.01 \pm 0.00$	$7.79 \times 10^{-6} \pm 1.94 \times 10^{-6}$	$302.9 \pm 61.8$
		$\mu\mu$	$0.01 \pm 0.00$	$5.56 \times 10^{-6} \pm 1.48 \times 10^{-6}$	$277.3 \pm 59.7$
1200	$9.53 \times 10^{-6}$	$ee$	$0.02 \pm 0.00$	$4.03 \times 10^{-6} \pm 1.03 \times 10^{-6}$	$296.8 \pm 60.5$
		$\mu\mu$	$0.01 \pm 0.00$	$1.83 \times 10^{-6} \pm 5.31 \times 10^{-7}$	$294.5 \pm 59.6$
1300	$4.93 \times 10^{-6}$	$ee$	$0.01 \pm 0.00$	$1.42 \times 10^{-6} \pm 3.93 \times 10^{-7}$	$276.6 \pm 57.0$
		$\mu\mu$	$0.01 \pm 0.00$	$1.08 \times 10^{-6} \pm 3.10 \times 10^{-7}$	$302.1 \pm 61.1$
1400	$2.59 \times 10^{-6}$	$ee$	$0.01 \pm 0.00$	$5.90 \times 10^{-7} \pm 1.77 \times 10^{-7}$	$274.3 \pm 56.0$
		$\mu\mu$	$0.01 \pm 0.00$	$3.97 \times 10^{-7} \pm 1.23 \times 10^{-7}$	$296.7 \pm 60.0$
1500	$1.38 \times 10^{-6}$	$ee$	$0.01 \pm 0.00$	$2.90 \times 10^{-7} \pm 8.66 \times 10^{-8}$	$274.9 \pm 56.4$
		$\mu\mu$	$0.00 \pm 0.00$	$1.82 \times 10^{-7} \pm 6.31 \times 10^{-8}$	$282.0 \pm 57.1$

Table F.14: Inputs for the  $Z'\chi_2 \rightarrow l^+l^-\chi_1\chi_1$  HDS  $\sigma B$  calculations in SR2. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	$6.93 \times 10^{-1}$	$ee$	$0.12 \pm 0.02$	$2.22 \pm 0.46$	$61.5 \pm 14.2$
		$\mu\mu$	$0.11 \pm 0.02$	$2.06 \pm 0.43$	$73.5 \pm 15.5$
200	$1.41 \times 10^{-1}$	$ee$	$0.19 \pm 0.04$	$7.46 \times 10^{-1} \pm 1.52 \times 10^{-1}$	$54.7 \pm 13.8$
		$\mu\mu$	$0.14 \pm 0.03$	$5.39 \times 10^{-1} \pm 1.11 \times 10^{-1}$	$81.3 \pm 17.0$
400	$6.90 \times 10^{-3}$	$ee$	$0.13 \pm 0.03$	$2.49 \times 10^{-2} \pm 5.13 \times 10^{-3}$	$63.6 \pm 13.9$
		$\mu\mu$	$0.07 \pm 0.01$	$1.38 \times 10^{-2} \pm 2.91 \times 10^{-3}$	$77.8 \pm 16.6$
600	$8.81 \times 10^{-4}$	$ee$	$0.08 \pm 0.02$	$1.99 \times 10^{-3} \pm 4.17 \times 10^{-4}$	$49.2 \pm 13.1$
		$\mu\mu$	$0.05 \pm 0.01$	$1.29 \times 10^{-3} \pm 2.78 \times 10^{-4}$	$83.0 \pm 17.3$
800	$1.66 \times 10^{-4}$	$ee$	$0.05 \pm 0.01$	$2.34 \times 10^{-4} \pm 5.05 \times 10^{-5}$	$58.1 \pm 13.3$
		$\mu\mu$	$0.03 \pm 0.01$	$1.49 \times 10^{-4} \pm 3.31 \times 10^{-5}$	$74.3 \pm 15.8$
900	$7.74 \times 10^{-5}$	$ee$	$0.05 \pm 0.01$	$1.07 \times 10^{-4} \pm 2.33 \times 10^{-5}$	$59.9 \pm 13.4$
		$\mu\mu$	$0.03 \pm 0.01$	$6.38 \times 10^{-5} \pm 1.44 \times 10^{-5}$	$84.5 \pm 17.9$
1100	$1.87 \times 10^{-5}$	$ee$	$0.03 \pm 0.01$	$1.72 \times 10^{-5} \pm 3.86 \times 10^{-6}$	$46.2 \pm 13.2$
		$\mu\mu$	$0.02 \pm 0.00$	$9.42 \times 10^{-6} \pm 2.26 \times 10^{-6}$	$73.5 \pm 15.6$
1200	$9.53 \times 10^{-6}$	$ee$	$0.02 \pm 0.00$	$5.76 \times 10^{-6} \pm 1.37 \times 10^{-6}$	$72.5 \pm 15.5$
		$\mu\mu$	$0.02 \pm 0.00$	$4.05 \times 10^{-6} \pm 1.01 \times 10^{-6}$	$77.9 \pm 16.5$
1300	$4.93 \times 10^{-6}$	$ee$	$0.02 \pm 0.00$	$3.18 \times 10^{-6} \pm 7.52 \times 10^{-7}$	$74.0 \pm 16.3$
		$\mu\mu$	$0.01 \pm 0.00$	$1.80 \times 10^{-6} \pm 4.62 \times 10^{-7}$	$84.1 \pm 17.7$
1400	$2.59 \times 10^{-6}$	$ee$	$0.02 \pm 0.00$	$1.39 \times 10^{-6} \pm 3.34 \times 10^{-7}$	$57.3 \pm 14.2$
		$\mu\mu$	$0.01 \pm 0.00$	$6.88 \times 10^{-7} \pm 1.95 \times 10^{-7}$	$68.8 \pm 14.6$
1500	$1.38 \times 10^{-6}$	$ee$	$0.01 \pm 0.00$	$5.54 \times 10^{-7} \pm 1.45 \times 10^{-7}$	$48.6 \pm 14.6$
		$\mu\mu$	$0.01 \pm 0.00$	$2.79 \times 10^{-7} \pm 8.17 \times 10^{-8}$	$80.5 \pm 17.0$

Table F.15: Inputs for the  $Z'\chi_2 \rightarrow l^+l^-\chi_1\chi_1$  HDS  $\sigma B$  calculations in SR3. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	$6.93 \times 10^{-1}$	$ee$	$0.09 \pm 0.02$	$1.71 \pm 0.36$	$20.0 \pm 5.1$
		$\mu\mu$	$0.05 \pm 0.01$	$9.52 \times 10^{-1} \pm 2.02 \times 10^{-1}$	$24.6 \pm 5.8$
200	$1.41 \times 10^{-1}$	$ee$	$0.35 \pm 0.07$	$1.39 \pm 0.28$	$17.1 \pm 6.5$
		$\mu\mu$	$0.20 \pm 0.04$	$8.05 \times 10^{-1} \pm 1.64 \times 10^{-1}$	$21.8 \pm 5.2$
400	$6.90 \times 10^{-3}$	$ee$	$1.04 \pm 0.21$	$1.99 \times 10^{-1} \pm 4.00 \times 10^{-2}$	$20.9 \pm 5.4$
		$\mu\mu$	$0.69 \pm 0.14$	$1.32 \times 10^{-1} \pm 2.65 \times 10^{-2}$	$21.6 \pm 5.4$
600	$8.81 \times 10^{-4}$	$ee$	$1.38 \pm 0.28$	$3.38 \times 10^{-2} \pm 6.78 \times 10^{-3}$	$20.3 \pm 5.3$
		$\mu\mu$	$0.96 \pm 0.19$	$2.36 \times 10^{-2} \pm 4.74 \times 10^{-3}$	$18.9 \pm 4.8$
800	$1.66 \times 10^{-4}$	$ee$	$1.54 \pm 0.31$	$7.10 \times 10^{-3} \pm 1.42 \times 10^{-3}$	$18.4 \pm 5.2$
		$\mu\mu$	$1.11 \pm 0.22$	$5.12 \times 10^{-3} \pm 1.03 \times 10^{-3}$	$20.4 \pm 4.8$
900	$7.74 \times 10^{-5}$	$ee$	$1.63 \pm 0.33$	$3.51 \times 10^{-3} \pm 7.04 \times 10^{-4}$	$18.5 \pm 6.6$
		$\mu\mu$	$1.15 \pm 0.23$	$2.48 \times 10^{-3} \pm 4.97 \times 10^{-4}$	$19.7 \pm 4.8$
1100	$1.87 \times 10^{-5}$	$ee$	$1.70 \pm 0.34$	$8.87 \times 10^{-4} \pm 1.78 \times 10^{-4}$	$25.1 \pm 6.3$
		$\mu\mu$	$1.18 \pm 0.24$	$6.16 \times 10^{-4} \pm 1.24 \times 10^{-4}$	$22.9 \pm 5.5$
1200	$9.53 \times 10^{-6}$	$ee$	$1.71 \pm 0.34$	$4.52 \times 10^{-4} \pm 9.07 \times 10^{-5}$	$21.4 \pm 5.4$
		$\mu\mu$	$1.17 \pm 0.23$	$3.09 \times 10^{-4} \pm 6.20 \times 10^{-5}$	$20.0 \pm 4.8$
1300	$4.93 \times 10^{-6}$	$ee$	$1.70 \pm 0.34$	$2.33 \times 10^{-4} \pm 4.67 \times 10^{-5}$	$22.5 \pm 5.8$
		$\mu\mu$	$1.18 \pm 0.24$	$1.62 \times 10^{-4} \pm 3.26 \times 10^{-5}$	$17.3 \pm 4.3$
1400	$2.59 \times 10^{-6}$	$ee$	$1.73 \pm 0.35$	$1.25 \times 10^{-4} \pm 2.50 \times 10^{-5}$	$15.2 \pm 6.3$
		$\mu\mu$	$1.20 \pm 0.24$	$8.62 \times 10^{-5} \pm 1.73 \times 10^{-5}$	$21.2 \pm 5.2$
1500	$1.38 \times 10^{-6}$	$ee$	$1.79 \pm 0.36$	$6.88 \times 10^{-5} \pm 1.38 \times 10^{-5}$	$16.0 \pm 6.3$
		$\mu\mu$	$1.17 \pm 0.23$	$4.48 \times 10^{-5} \pm 8.98 \times 10^{-6}$	$18.8 \pm 4.5$

Table F.16: Inputs for the  $Z'\chi_2 \rightarrow l^+l^-\chi_1\chi_1$  LDS  $\sigma B$  calculations in SR1. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	6.80	$ee$	$0.03 \pm 0.01$	$4.92 \pm 1.05$	$269.8 \pm 55.1$
		$\mu\mu$	$0.02 \pm 0.00$	$3.53 \pm 0.77$	$285.8 \pm 57.8$
200	2.37	$ee$	$0.08 \pm 0.02$	$5.41 \pm 1.11$	$279.9 \pm 57.3$
		$\mu\mu$	$0.05 \pm 0.01$	$3.33 \pm 0.70$	$300.5 \pm 60.8$
400	$2.89 \times 10^{-1}$	$ee$	$0.23 \pm 0.05$	$1.83 \pm 0.37$	$271.4 \pm 55.3$
		$\mu\mu$	$0.12 \pm 0.02$	$9.94 \times 10^{-1} \pm 2.04 \times 10^{-1}$	$294.1 \pm 59.5$
600	$7.34 \times 10^{-2}$	$ee$	$0.27 \pm 0.05$	$5.51 \times 10^{-1} \pm 1.12 \times 10^{-1}$	$277.0 \pm 56.6$
		$\mu\mu$	$0.15 \pm 0.03$	$2.99 \times 10^{-1} \pm 6.10 \times 10^{-2}$	$274.4 \pm 59.1$
800	$2.59 \times 10^{-2}$	$ee$	$0.29 \pm 0.06$	$2.09 \times 10^{-1} \pm 4.23 \times 10^{-2}$	$266.7 \pm 54.9$
		$\mu\mu$	$0.15 \pm 0.03$	$1.07 \times 10^{-1} \pm 2.19 \times 10^{-2}$	$300.8 \pm 60.8$
900	$1.65 \times 10^{-2}$	$ee$	$0.27 \pm 0.05$	$1.25 \times 10^{-1} \pm 2.52 \times 10^{-2}$	$275.8 \pm 56.9$
		$\mu\mu$	$0.14 \pm 0.03$	$6.33 \times 10^{-2} \pm 1.30 \times 10^{-2}$	$292.1 \pm 59.1$
1100	$7.34 \times 10^{-3}$	$ee$	$0.26 \pm 0.05$	$5.20 \times 10^{-2} \pm 1.06 \times 10^{-2}$	$272.1 \pm 55.5$
		$\mu\mu$	$0.13 \pm 0.03$	$2.60 \times 10^{-2} \pm 5.35 \times 10^{-3}$	$294.8 \pm 59.6$
1200	$5.08 \times 10^{-3}$	$ee$	$0.25 \pm 0.05$	$3.53 \times 10^{-2} \pm 7.16 \times 10^{-3}$	$282.2 \pm 57.7$
		$\mu\mu$	$0.13 \pm 0.03$	$1.85 \times 10^{-2} \pm 3.80 \times 10^{-3}$	$290.0 \pm 58.7$
1300	$3.58 \times 10^{-3}$	$ee$	$0.24 \pm 0.05$	$2.37 \times 10^{-2} \pm 4.81 \times 10^{-3}$	$268.5 \pm 55.0$
		$\mu\mu$	$0.13 \pm 0.03$	$1.26 \times 10^{-2} \pm 2.60 \times 10^{-3}$	$294.2 \pm 59.5$
1400	$2.56 \times 10^{-3}$	$ee$	$0.25 \pm 0.05$	$1.79 \times 10^{-2} \pm 3.63 \times 10^{-3}$	$293.2 \pm 59.7$
		$\mu\mu$	$0.12 \pm 0.02$	$8.54 \times 10^{-3} \pm 1.76 \times 10^{-3}$	$274.7 \pm 59.1$
1500	$1.86 \times 10^{-3}$	$ee$	$0.25 \pm 0.05$	$1.29 \times 10^{-2} \pm 2.61 \times 10^{-3}$	$309.1 \pm 63.1$
		$\mu\mu$	$0.11 \pm 0.02$	$5.71 \times 10^{-3} \pm 1.18 \times 10^{-3}$	$271.1 \pm 58.6$

Table F.17: Inputs for the  $Z'\chi_2 \rightarrow l^+l^-\chi_1\chi_1$  LDS  $\sigma B$  calculations in SR2. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	6.80	$ee$	$0.03 \pm 0.01$	$6.16 \pm 1.30$	$72.5 \pm 15.6$
		$\mu\mu$	$0.03 \pm 0.01$	$5.65 \pm 1.20$	$75.8 \pm 15.9$
200	2.37	$ee$	$0.08 \pm 0.02$	$4.99 \pm 1.03$	$50.6 \pm 11.8$
		$\mu\mu$	$0.06 \pm 0.01$	$3.72 \pm 0.77$	$82.6 \pm 17.2$
400	$2.89 \times 10^{-1}$	$ee$	$0.21 \pm 0.04$	$1.66 \pm 0.34$	$63.5 \pm 14.4$
		$\mu\mu$	$0.11 \pm 0.02$	$8.96 \times 10^{-1} \pm 1.84 \times 10^{-1}$	$79.6 \pm 16.7$
600	$7.34 \times 10^{-2}$	$ee$	$0.25 \pm 0.05$	$5.09 \times 10^{-1} \pm 1.03 \times 10^{-1}$	$69.4 \pm 15.0$
		$\mu\mu$	$0.16 \pm 0.03$	$3.26 \times 10^{-1} \pm 6.64 \times 10^{-2}$	$77.8 \pm 16.6$
800	$2.59 \times 10^{-2}$	$ee$	$0.27 \pm 0.05$	$1.95 \times 10^{-1} \pm 3.95 \times 10^{-2}$	$63.4 \pm 13.9$
		$\mu\mu$	$0.18 \pm 0.04$	$1.32 \times 10^{-1} \pm 2.69 \times 10^{-2}$	$83.5 \pm 17.6$
900	$1.65 \times 10^{-2}$	$ee$	$0.28 \pm 0.06$	$1.27 \times 10^{-1} \pm 2.58 \times 10^{-2}$	$64.6 \pm 14.4$
		$\mu\mu$	$0.18 \pm 0.04$	$8.03 \times 10^{-2} \pm 1.64 \times 10^{-2}$	$71.7 \pm 15.1$
1100	$7.34 \times 10^{-3}$	$ee$	$0.27 \pm 0.05$	$5.54 \times 10^{-2} \pm 1.12 \times 10^{-2}$	$60.0 \pm 15.2$
		$\mu\mu$	$0.16 \pm 0.03$	$3.28 \times 10^{-2} \pm 6.70 \times 10^{-3}$	$78.3 \pm 16.5$
1200	$5.08 \times 10^{-3}$	$ee$	$0.26 \pm 0.05$	$3.72 \times 10^{-2} \pm 7.54 \times 10^{-3}$	$59.2 \pm 13.3$
		$\mu\mu$	$0.15 \pm 0.03$	$2.17 \times 10^{-2} \pm 4.43 \times 10^{-3}$	$82.5 \pm 17.3$
1300	$3.58 \times 10^{-3}$	$ee$	$0.27 \pm 0.05$	$2.65 \times 10^{-2} \pm 5.36 \times 10^{-3}$	$60.0 \pm 13.4$
		$\mu\mu$	$0.17 \pm 0.03$	$1.67 \times 10^{-2} \pm 3.41 \times 10^{-3}$	$83.7 \pm 17.4$
1400	$2.56 \times 10^{-3}$	$ee$	$0.25 \pm 0.05$	$1.79 \times 10^{-2} \pm 3.63 \times 10^{-3}$	$48.2 \pm 14.2$
		$\mu\mu$	$0.15 \pm 0.03$	$1.04 \times 10^{-2} \pm 2.12 \times 10^{-3}$	$74.9 \pm 15.8$
1500	$1.86 \times 10^{-3}$	$ee$	$0.26 \pm 0.05$	$1.33 \times 10^{-2} \pm 2.69 \times 10^{-3}$	$58.2 \pm 14.8$
		$\mu\mu$	$0.14 \pm 0.03$	$7.25 \times 10^{-3} \pm 1.49 \times 10^{-3}$	$78.6 \pm 16.5$

Table F.18: Inputs for the  $Z'\chi_2 \rightarrow l^+l^-\chi_1\chi_1$  LDS  $\sigma B$  calculations in SR3. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	6.80	$ee$	$0.02 \pm 0.00$	$3.96 \pm 0.86$	$17.5 \pm 5.1$
		$\mu\mu$	$0.01 \pm 0.00$	$1.88 \pm 0.44$	$19.0 \pm 4.5$
200	2.37	$ee$	$0.08 \pm 0.02$	$5.14 \pm 1.06$	$18.1 \pm 6.7$
		$\mu\mu$	$0.05 \pm 0.01$	$2.99 \pm 0.63$	$18.5 \pm 4.5$
400	$2.89 \times 10^{-1}$	$ee$	$0.24 \pm 0.05$	$1.97 \pm 0.40$	$20.0 \pm 5.1$
		$\mu\mu$	$0.17 \pm 0.03$	$1.38 \pm 0.28$	$23.8 \pm 5.6$
600	$7.34 \times 10^{-2}$	$ee$	$0.44 \pm 0.09$	$8.95 \times 10^{-1} \pm 1.80 \times 10^{-1}$	$22.0 \pm 5.3$
		$\mu\mu$	$0.32 \pm 0.06$	$6.49 \times 10^{-1} \pm 1.31 \times 10^{-1}$	$19.0 \pm 4.9$
800	$2.59 \times 10^{-2}$	$ee$	$0.61 \pm 0.12$	$4.40 \times 10^{-1} \pm 8.85 \times 10^{-2}$	$22.1 \pm 7.2$
		$\mu\mu$	$0.44 \pm 0.09$	$3.14 \times 10^{-1} \pm 6.33 \times 10^{-2}$	$20.5 \pm 5.3$
900	$1.65 \times 10^{-2}$	$ee$	$0.71 \pm 0.14$	$3.27 \times 10^{-1} \pm 6.56 \times 10^{-2}$	$18.8 \pm 5.0$
		$\mu\mu$	$0.48 \pm 0.10$	$2.21 \times 10^{-1} \pm 4.45 \times 10^{-2}$	$20.4 \pm 5.3$
1100	$7.34 \times 10^{-3}$	$ee$	$0.83 \pm 0.17$	$1.69 \times 10^{-1} \pm 3.39 \times 10^{-2}$	$22.2 \pm 7.2$
		$\mu\mu$	$0.56 \pm 0.11$	$1.14 \times 10^{-1} \pm 2.30 \times 10^{-2}$	$20.3 \pm 4.8$
1200	$5.08 \times 10^{-3}$	$ee$	$0.87 \pm 0.17$	$1.23 \times 10^{-1} \pm 2.48 \times 10^{-2}$	$22.4 \pm 5.9$
		$\mu\mu$	$0.61 \pm 0.12$	$8.65 \times 10^{-2} \pm 1.74 \times 10^{-2}$	$20.0 \pm 4.9$
1300	$3.58 \times 10^{-3}$	$ee$	$0.94 \pm 0.19$	$9.35 \times 10^{-2} \pm 1.88 \times 10^{-2}$	$16.0 \pm 6.6$
		$\mu\mu$	$0.65 \pm 0.13$	$6.49 \times 10^{-2} \pm 1.31 \times 10^{-2}$	$16.3 \pm 4.4$
1400	$2.56 \times 10^{-3}$	$ee$	$0.96 \pm 0.19$	$6.86 \times 10^{-2} \pm 1.38 \times 10^{-2}$	$21.1 \pm 5.9$
		$\mu\mu$	$0.67 \pm 0.13$	$4.76 \times 10^{-2} \pm 9.57 \times 10^{-3}$	$20.1 \pm 5.1$
1500	$1.86 \times 10^{-3}$	$ee$	$1.02 \pm 0.20$	$5.26 \times 10^{-2} \pm 1.06 \times 10^{-2}$	$17.1 \pm 6.8$
		$\mu\mu$	$0.67 \pm 0.13$	$3.47 \times 10^{-2} \pm 6.97 \times 10^{-3}$	$18.7 \pm 4.5$

Table F.19: Inputs for the EFT  $\rightarrow Z'\chi\chi$  HDS  $\sigma B$  calculations in SR1. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	$7.81 \times 10^{-6}$	$ee$	$0.06 \pm 0.01$	$1.29 \times 10^{-5} \pm 2.73 \times 10^{-6}$	$298.4 \pm 60.7$
		$\mu\mu$	$0.05 \pm 0.01$	$9.82 \times 10^{-6} \pm 2.10 \times 10^{-6}$	$290.6 \pm 58.8$
200	$6.81 \times 10^{-7}$	$ee$	$0.08 \pm 0.02$	$1.54 \times 10^{-6} \pm 3.24 \times 10^{-7}$	$273.0 \pm 55.9$
		$\mu\mu$	$0.06 \pm 0.01$	$1.12 \times 10^{-6} \pm 2.37 \times 10^{-7}$	$289.1 \pm 58.5$
300	$6.01 \times 10^{-8}$	$ee$	$0.04 \pm 0.01$	$7.16 \times 10^{-8} \pm 1.56 \times 10^{-8}$	$273.5 \pm 56.0$
		$\mu\mu$	$0.02 \pm 0.00$	$3.68 \times 10^{-8} \pm 8.57 \times 10^{-9}$	$304.3 \pm 61.5$
400	$8.42 \times 10^{-9}$	$ee$	$0.07 \pm 0.01$	$1.55 \times 10^{-8} \pm 3.28 \times 10^{-9}$	$296.3 \pm 60.4$
		$\mu\mu$	$0.04 \pm 0.01$	$8.75 \times 10^{-9} \pm 1.93 \times 10^{-9}$	$295.7 \pm 59.9$
500	$1.80 \times 10^{-9}$	$ee$	$0.04 \pm 0.01$	$2.00 \times 10^{-9} \pm 4.39 \times 10^{-10}$	$281.8 \pm 58.2$
		$\mu\mu$	$0.02 \pm 0.00$	$9.02 \times 10^{-10} \pm 2.17 \times 10^{-10}$	$286.8 \pm 58.0$
600	$4.83 \times 10^{-10}$	$ee$	$0.04 \pm 0.01$	$5.58 \times 10^{-10} \pm 1.22 \times 10^{-10}$	$273.8 \pm 56.0$
		$\mu\mu$	$0.02 \pm 0.00$	$2.61 \times 10^{-10} \pm 6.14 \times 10^{-11}$	$293.0 \pm 59.4$
700	$1.49 \times 10^{-10}$	$ee$	$0.03 \pm 0.01$	$1.08 \times 10^{-10} \pm 2.48 \times 10^{-11}$	$279.3 \pm 57.2$
		$\mu\mu$	$0.02 \pm 0.00$	$7.49 \times 10^{-11} \pm 1.80 \times 10^{-11}$	$278.5 \pm 59.9$
800	$5.12 \times 10^{-11}$	$ee$	$0.03 \pm 0.01$	$4.35 \times 10^{-11} \pm 9.86 \times 10^{-12}$	$294.4 \pm 59.9$
		$\mu\mu$	$0.02 \pm 0.00$	$2.20 \times 10^{-11} \pm 5.46 \times 10^{-12}$	$288.6 \pm 58.5$
900	$1.90 \times 10^{-11}$	$ee$	$0.02 \pm 0.00$	$8.79 \times 10^{-12} \pm 2.16 \times 10^{-12}$	$285.2 \pm 58.2$
		$\mu\mu$	$0.01 \pm 0.00$	$5.86 \times 10^{-12} \pm 1.54 \times 10^{-12}$	$266.9 \pm 57.7$
1000	$7.47 \times 10^{-12}$	$ee$	$0.01 \pm 0.00$	$2.65 \times 10^{-12} \pm 6.95 \times 10^{-13}$	$293.1 \pm 60.0$
		$\mu\mu$	$0.01 \pm 0.00$	$2.70 \times 10^{-12} \pm 6.86 \times 10^{-13}$	$299.3 \pm 60.6$
1100	$3.07 \times 10^{-12}$	$ee$	$0.02 \pm 0.00$	$1.29 \times 10^{-12} \pm 3.22 \times 10^{-13}$	$302.9 \pm 61.8$
		$\mu\mu$	$0.01 \pm 0.00$	$8.56 \times 10^{-13} \pm 2.31 \times 10^{-13}$	$277.3 \pm 59.7$
1200	$1.31 \times 10^{-12}$	$ee$	$0.01 \pm 0.00$	$5.00 \times 10^{-13} \pm 1.27 \times 10^{-13}$	$284.4 \pm 57.8$
		$\mu\mu$	$0.01 \pm 0.00$	$2.68 \times 10^{-13} \pm 7.76 \times 10^{-14}$	$280.5 \pm 56.8$
1300	$5.80 \times 10^{-13}$	$ee$	$0.01 \pm 0.00$	$1.63 \times 10^{-13} \pm 4.49 \times 10^{-14}$	$279.0 \pm 57.2$
		$\mu\mu$	$0.01 \pm 0.00$	$8.75 \times 10^{-14} \pm 2.78 \times 10^{-14}$	$295.9 \pm 59.9$
1400	$2.63 \times 10^{-13}$	$ee$	$0.01 \pm 0.00$	$8.52 \times 10^{-14} \pm 2.24 \times 10^{-14}$	$263.4 \pm 54.6$
		$\mu\mu$	$0.01 \pm 0.00$	$4.49 \times 10^{-14} \pm 1.42 \times 10^{-14}$	$290.9 \pm 58.9$
1500	$1.22 \times 10^{-13}$	$ee$	$0.01 \pm 0.00$	$1.95 \times 10^{-14} \pm 6.16 \times 10^{-15}$	$267.1 \pm 54.5$
		$\mu\mu$	$0.01 \pm 0.00$	$2.27 \times 10^{-14} \pm 7.01 \times 10^{-15}$	$310.0 \pm 62.7$

Table F.20: Inputs for the EFT  $\rightarrow Z'\chi\chi$  HDS  $\sigma B$  calculations in SR2. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	$7.81 \times 10^{-6}$	$ee$	$0.13 \pm 0.03$	$2.76 \times 10^{-5} \pm 5.68 \times 10^{-6}$	$61.2 \pm 14.7$
		$\mu\mu$	$0.11 \pm 0.02$	$2.28 \times 10^{-5} \pm 4.71 \times 10^{-6}$	$79.9 \pm 16.8$
200	$6.81 \times 10^{-7}$	$ee$	$0.19 \pm 0.04$	$3.52 \times 10^{-6} \pm 7.20 \times 10^{-7}$	$64.2 \pm 14.6$
		$\mu\mu$	$0.14 \pm 0.03$	$2.68 \times 10^{-6} \pm 5.50 \times 10^{-7}$	$81.6 \pm 17.3$
300	$6.01 \times 10^{-8}$	$ee$	$0.12 \pm 0.02$	$2.06 \times 10^{-7} \pm 4.26 \times 10^{-8}$	$68.0 \pm 14.6$
		$\mu\mu$	$0.08 \pm 0.02$	$1.26 \times 10^{-7} \pm 2.66 \times 10^{-8}$	$83.6 \pm 17.5$
400	$8.42 \times 10^{-9}$	$ee$	$0.13 \pm 0.03$	$3.12 \times 10^{-8} \pm 6.43 \times 10^{-9}$	$59.4 \pm 13.3$
		$\mu\mu$	$0.07 \pm 0.01$	$1.75 \times 10^{-8} \pm 3.68 \times 10^{-9}$	$74.2 \pm 15.7$
500	$1.80 \times 10^{-9}$	$ee$	$0.08 \pm 0.02$	$4.08 \times 10^{-9} \pm 8.56 \times 10^{-10}$	$66.6 \pm 14.7$
		$\mu\mu$	$0.05 \pm 0.01$	$2.71 \times 10^{-9} \pm 5.80 \times 10^{-10}$	$77.0 \pm 16.2$
600	$4.83 \times 10^{-10}$	$ee$	$0.08 \pm 0.02$	$1.02 \times 10^{-9} \pm 2.15 \times 10^{-10}$	$64.6 \pm 14.2$
		$\mu\mu$	$0.05 \pm 0.01$	$6.78 \times 10^{-10} \pm 1.46 \times 10^{-10}$	$80.1 \pm 16.9$
700	$1.49 \times 10^{-10}$	$ee$	$0.05 \pm 0.01$	$2.05 \times 10^{-10} \pm 4.44 \times 10^{-11}$	$72.9 \pm 16.0$
		$\mu\mu$	$0.04 \pm 0.01$	$1.54 \times 10^{-10} \pm 3.39 \times 10^{-11}$	$74.5 \pm 15.7$
800	$5.12 \times 10^{-11}$	$ee$	$0.05 \pm 0.01$	$7.33 \times 10^{-11} \pm 1.58 \times 10^{-11}$	$62.2 \pm 13.7$
		$\mu\mu$	$0.03 \pm 0.01$	$4.02 \times 10^{-11} \pm 9.06 \times 10^{-12}$	$78.7 \pm 16.6$
900	$1.90 \times 10^{-11}$	$ee$	$0.04 \pm 0.01$	$2.00 \times 10^{-11} \pm 4.42 \times 10^{-12}$	$64.3 \pm 14.2$
		$\mu\mu$	$0.03 \pm 0.01$	$1.53 \times 10^{-11} \pm 3.47 \times 10^{-12}$	$74.3 \pm 15.7$
1000	$7.47 \times 10^{-12}$	$ee$	$0.04 \pm 0.01$	$7.97 \times 10^{-12} \pm 1.76 \times 10^{-12}$	$56.8 \pm 14.5$
		$\mu\mu$	$0.02 \pm 0.00$	$4.10 \times 10^{-12} \pm 9.77 \times 10^{-13}$	$82.6 \pm 17.4$
1100	$3.07 \times 10^{-12}$	$ee$	$0.03 \pm 0.01$	$2.51 \times 10^{-12} \pm 5.70 \times 10^{-13}$	$56.0 \pm 14.7$
		$\mu\mu$	$0.02 \pm 0.00$	$1.73 \times 10^{-12} \pm 4.09 \times 10^{-13}$	$79.3 \pm 16.6$
1200	$1.31 \times 10^{-12}$	$ee$	$0.02 \pm 0.00$	$8.04 \times 10^{-13} \pm 1.91 \times 10^{-13}$	$67.0 \pm 14.6$
		$\mu\mu$	$0.02 \pm 0.00$	$6.02 \times 10^{-13} \pm 1.48 \times 10^{-13}$	$77.7 \pm 16.3$
1300	$5.80 \times 10^{-13}$	$ee$	$0.02 \pm 0.00$	$3.16 \times 10^{-13} \pm 7.56 \times 10^{-14}$	$56.8 \pm 13.0$
		$\mu\mu$	$0.01 \pm 0.00$	$1.53 \times 10^{-13} \pm 4.17 \times 10^{-14}$	$80.6 \pm 17.0$
1400	$2.63 \times 10^{-13}$	$ee$	$0.02 \pm 0.00$	$1.29 \times 10^{-13} \pm 3.21 \times 10^{-14}$	$63.0 \pm 14.0$
		$\mu\mu$	$0.01 \pm 0.00$	$6.20 \times 10^{-14} \pm 1.77 \times 10^{-14}$	$81.6 \pm 17.1$
1500	$1.22 \times 10^{-13}$	$ee$	$0.01 \pm 0.00$	$4.76 \times 10^{-14} \pm 1.22 \times 10^{-14}$	$49.9 \pm 13.8$
		$\mu\mu$	$0.01 \pm 0.00$	$2.68 \times 10^{-14} \pm 7.97 \times 10^{-15}$	$82.2 \pm 17.1$

Table F.21: Inputs for the EFT  $\rightarrow Z'\chi\chi$  HDS  $\sigma B$  calculations in SR3. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	$7.81 \times 10^{-6}$	$ee$	$0.09 \pm 0.02$	$1.90 \times 10^{-5} \pm 3.96 \times 10^{-6}$	$19.1 \pm 5.3$
		$\mu\mu$	$0.05 \pm 0.01$	$9.78 \times 10^{-6} \pm 2.10 \times 10^{-6}$	$21.2 \pm 5.3$
200	$6.81 \times 10^{-7}$	$ee$	$0.36 \pm 0.07$	$6.75 \times 10^{-6} \pm 1.37 \times 10^{-6}$	$22.4 \pm 6.0$
		$\mu\mu$	$0.20 \pm 0.04$	$3.85 \times 10^{-6} \pm 7.84 \times 10^{-7}$	$19.9 \pm 4.7$
300	$6.01 \times 10^{-8}$	$ee$	$0.61 \pm 0.12$	$1.03 \times 10^{-6} \pm 2.07 \times 10^{-7}$	$17.5 \pm 5.0$
		$\mu\mu$	$0.36 \pm 0.07$	$6.09 \times 10^{-7} \pm 1.23 \times 10^{-7}$	$19.4 \pm 4.5$
400	$8.42 \times 10^{-9}$	$ee$	$1.03 \pm 0.21$	$2.42 \times 10^{-7} \pm 4.86 \times 10^{-8}$	$16.0 \pm 6.5$
		$\mu\mu$	$0.70 \pm 0.14$	$1.63 \times 10^{-7} \pm 3.28 \times 10^{-8}$	$19.7 \pm 4.9$
500	$1.80 \times 10^{-9}$	$ee$	$1.19 \pm 0.24$	$5.95 \times 10^{-8} \pm 1.19 \times 10^{-8}$	$18.0 \pm 5.0$
		$\mu\mu$	$0.83 \pm 0.17$	$4.17 \times 10^{-8} \pm 8.38 \times 10^{-9}$	$21.0 \pm 5.0$
600	$4.83 \times 10^{-10}$	$ee$	$1.41 \pm 0.28$	$1.89 \times 10^{-8} \pm 3.78 \times 10^{-9}$	$19.1 \pm 5.1$
		$\mu\mu$	$0.96 \pm 0.19$	$1.29 \times 10^{-8} \pm 2.60 \times 10^{-9}$	$16.7 \pm 4.5$
700	$1.49 \times 10^{-10}$	$ee$	$1.47 \pm 0.29$	$6.09 \times 10^{-9} \pm 1.22 \times 10^{-9}$	$26.2 \pm 6.3$
		$\mu\mu$	$1.03 \pm 0.21$	$4.28 \times 10^{-9} \pm 8.60 \times 10^{-10}$	$18.6 \pm 4.7$
800	$5.12 \times 10^{-11}$	$ee$	$1.58 \pm 0.32$	$2.25 \times 10^{-9} \pm 4.52 \times 10^{-10}$	$20.1 \pm 5.7$
		$\mu\mu$	$1.11 \pm 0.22$	$1.58 \times 10^{-9} \pm 3.18 \times 10^{-10}$	$19.9 \pm 4.9$
900	$1.90 \times 10^{-11}$	$ee$	$1.67 \pm 0.33$	$8.82 \times 10^{-10} \pm 1.77 \times 10^{-10}$	$21.4 \pm 5.6$
		$\mu\mu$	$1.12 \pm 0.22$	$5.93 \times 10^{-10} \pm 1.19 \times 10^{-10}$	$19.0 \pm 4.8$
1000	$7.47 \times 10^{-12}$	$ee$	$1.69 \pm 0.34$	$3.52 \times 10^{-10} \pm 7.05 \times 10^{-11}$	$18.5 \pm 6.9$
		$\mu\mu$	$1.18 \pm 0.24$	$2.46 \times 10^{-10} \pm 4.93 \times 10^{-11}$	$20.5 \pm 5.1$
1100	$3.07 \times 10^{-12}$	$ee$	$1.69 \pm 0.34$	$1.44 \times 10^{-10} \pm 2.90 \times 10^{-11}$	$21.2 \pm 5.7$
		$\mu\mu$	$1.19 \pm 0.24$	$1.01 \times 10^{-10} \pm 2.03 \times 10^{-11}$	$17.4 \pm 4.5$
1200	$1.31 \times 10^{-12}$	$ee$	$1.72 \pm 0.34$	$6.28 \times 10^{-11} \pm 1.26 \times 10^{-11}$	$18.3 \pm 5.0$
		$\mu\mu$	$1.18 \pm 0.24$	$4.32 \times 10^{-11} \pm 8.68 \times 10^{-12}$	$18.7 \pm 4.8$
1300	$5.80 \times 10^{-13}$	$ee$	$1.72 \pm 0.34$	$2.77 \times 10^{-11} \pm 5.55 \times 10^{-12}$	$24.1 \pm 5.9$
		$\mu\mu$	$1.19 \pm 0.24$	$1.91 \times 10^{-11} \pm 3.84 \times 10^{-12}$	$18.1 \pm 4.9$
1400	$2.63 \times 10^{-13}$	$ee$	$1.74 \pm 0.35$	$1.28 \times 10^{-11} \pm 2.56 \times 10^{-12}$	$17.1 \pm 5.1$
		$\mu\mu$	$1.18 \pm 0.24$	$8.66 \times 10^{-12} \pm 1.74 \times 10^{-12}$	$20.4 \pm 4.7$
1500	$1.22 \times 10^{-13}$	$ee$	$1.81 \pm 0.36$	$6.14 \times 10^{-12} \pm 1.23 \times 10^{-12}$	$15.6 \pm 6.6$
		$\mu\mu$	$1.16 \pm 0.23$	$3.92 \times 10^{-12} \pm 7.87 \times 10^{-13}$	$23.0 \pm 5.6$

Table F.22: Inputs for the EFT  $\rightarrow Z'\chi\chi$  LDS  $\sigma B$  calculations in SR1. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	$3.35 \times 10^{-5}$	$ee$	$0.02 \pm 0.00$	$2.22 \times 10^{-5} \pm 4.78 \times 10^{-6}$	$303.7 \pm 62.1$
		$\mu\mu$	$0.02 \pm 0.00$	$1.70 \times 10^{-5} \pm 3.72 \times 10^{-6}$	$271.4 \pm 58.6$
200	$2.67 \times 10^{-6}$	$ee$	$0.08 \pm 0.02$	$6.24 \times 10^{-6} \pm 1.28 \times 10^{-6}$	$268.5 \pm 54.9$
		$\mu\mu$	$0.05 \pm 0.01$	$3.45 \times 10^{-6} \pm 7.23 \times 10^{-7}$	$289.9 \pm 58.6$
300	$2.06 \times 10^{-7}$	$ee$	$0.08 \pm 0.02$	$4.55 \times 10^{-7} \pm 9.42 \times 10^{-8}$	$269.1 \pm 55.0$
		$\mu\mu$	$0.04 \pm 0.01$	$2.02 \times 10^{-7} \pm 4.33 \times 10^{-8}$	$304.0 \pm 61.5$
400	$2.65 \times 10^{-8}$	$ee$	$0.25 \pm 0.05$	$1.84 \times 10^{-7} \pm 3.73 \times 10^{-8}$	$286.9 \pm 58.7$
		$\mu\mu$	$0.12 \pm 0.02$	$8.56 \times 10^{-8} \pm 1.75 \times 10^{-8}$	$284.0 \pm 57.5$
500	$5.46 \times 10^{-9}$	$ee$	$0.20 \pm 0.04$	$2.99 \times 10^{-8} \pm 6.09 \times 10^{-9}$	$274.1 \pm 55.8$
		$\mu\mu$	$0.09 \pm 0.02$	$1.38 \times 10^{-8} \pm 2.86 \times 10^{-9}$	$303.3 \pm 61.3$
600	$1.47 \times 10^{-9}$	$ee$	$0.28 \pm 0.06$	$1.13 \times 10^{-8} \pm 2.28 \times 10^{-9}$	$270.9 \pm 55.7$
		$\mu\mu$	$0.14 \pm 0.03$	$5.82 \times 10^{-9} \pm 1.19 \times 10^{-9}$	$299.1 \pm 60.5$
700	$4.72 \times 10^{-10}$	$ee$	$0.27 \pm 0.05$	$3.54 \times 10^{-9} \pm 7.17 \times 10^{-10}$	$278.1 \pm 56.7$
		$\mu\mu$	$0.14 \pm 0.03$	$1.80 \times 10^{-9} \pm 3.68 \times 10^{-10}$	$291.6 \pm 58.9$
800	$1.73 \times 10^{-10}$	$ee$	$0.27 \pm 0.05$	$1.30 \times 10^{-9} \pm 2.63 \times 10^{-10}$	$288.3 \pm 58.7$
		$\mu\mu$	$0.14 \pm 0.03$	$6.80 \times 10^{-10} \pm 1.39 \times 10^{-10}$	$297.4 \pm 60.2$
900	$7.02 \times 10^{-11}$	$ee$	$0.27 \pm 0.05$	$5.35 \times 10^{-10} \pm 1.08 \times 10^{-10}$	$279.1 \pm 56.9$
		$\mu\mu$	$0.15 \pm 0.03$	$2.84 \times 10^{-10} \pm 5.81 \times 10^{-11}$	$296.5 \pm 60.0$
1000	$3.09 \times 10^{-11}$	$ee$	$0.26 \pm 0.05$	$2.24 \times 10^{-10} \pm 4.54 \times 10^{-11}$	$288.4 \pm 59.0$
		$\mu\mu$	$0.13 \pm 0.03$	$1.12 \times 10^{-10} \pm 2.30 \times 10^{-11}$	$296.4 \pm 60.0$
1100	$1.45 \times 10^{-11}$	$ee$	$0.25 \pm 0.05$	$1.01 \times 10^{-10} \pm 2.05 \times 10^{-11}$	$290.0 \pm 59.5$
		$\mu\mu$	$0.14 \pm 0.03$	$5.63 \times 10^{-11} \pm 1.15 \times 10^{-11}$	$278.3 \pm 56.3$
1200	$7.19 \times 10^{-12}$	$ee$	$0.25 \pm 0.05$	$5.01 \times 10^{-11} \pm 1.02 \times 10^{-11}$	$287.9 \pm 59.1$
		$\mu\mu$	$0.13 \pm 0.03$	$2.57 \times 10^{-11} \pm 5.27 \times 10^{-12}$	$299.4 \pm 60.6$
1300	$3.74 \times 10^{-12}$	$ee$	$0.26 \pm 0.05$	$2.67 \times 10^{-11} \pm 5.41 \times 10^{-12}$	$278.1 \pm 56.7$
		$\mu\mu$	$0.12 \pm 0.02$	$1.28 \times 10^{-11} \pm 2.63 \times 10^{-12}$	$293.2 \pm 59.4$
1400	$2.02 \times 10^{-12}$	$ee$	$0.23 \pm 0.05$	$1.30 \times 10^{-11} \pm 2.65 \times 10^{-12}$	$283.7 \pm 57.9$
		$\mu\mu$	$0.13 \pm 0.03$	$7.09 \times 10^{-12} \pm 1.46 \times 10^{-12}$	$290.4 \pm 58.7$
1500	$1.13 \times 10^{-12}$	$ee$	$0.23 \pm 0.05$	$7.19 \times 10^{-12} \pm 1.46 \times 10^{-12}$	$268.5 \pm 54.8$
		$\mu\mu$	$0.11 \pm 0.02$	$3.56 \times 10^{-12} \pm 7.35 \times 10^{-13}$	$292.2 \pm 59.1$

Table F.23: Inputs for the EFT  $\rightarrow Z'\chi\chi$  LDS  $\sigma B$  calculations in SR2. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	$3.35 \times 10^{-5}$	$ee$	$0.04 \pm 0.01$	$3.40 \times 10^{-5} \pm 7.15 \times 10^{-6}$	$66.7 \pm 14.4$
		$\mu\mu$	$0.04 \pm 0.01$	$3.32 \times 10^{-5} \pm 6.95 \times 10^{-6}$	$72.9 \pm 15.4$
200	$2.67 \times 10^{-6}$	$ee$	$0.07 \pm 0.01$	$5.13 \times 10^{-6} \pm 1.06 \times 10^{-6}$	$54.6 \pm 13.4$
		$\mu\mu$	$0.05 \pm 0.01$	$3.90 \times 10^{-6} \pm 8.12 \times 10^{-7}$	$77.0 \pm 16.2$
300	$2.06 \times 10^{-7}$	$ee$	$0.09 \pm 0.02$	$5.01 \times 10^{-7} \pm 1.04 \times 10^{-7}$	$61.9 \pm 13.6$
		$\mu\mu$	$0.06 \pm 0.01$	$3.45 \times 10^{-7} \pm 7.21 \times 10^{-8}$	$73.4 \pm 15.4$
400	$2.65 \times 10^{-8}$	$ee$	$0.18 \pm 0.04$	$1.36 \times 10^{-7} \pm 2.76 \times 10^{-8}$	$54.9 \pm 14.3$
		$\mu\mu$	$0.11 \pm 0.02$	$8.41 \times 10^{-8} \pm 1.72 \times 10^{-8}$	$71.4 \pm 15.0$
500	$5.46 \times 10^{-9}$	$ee$	$0.17 \pm 0.03$	$2.51 \times 10^{-8} \pm 5.12 \times 10^{-9}$	$51.7 \pm 13.8$
		$\mu\mu$	$0.11 \pm 0.02$	$1.71 \times 10^{-8} \pm 3.51 \times 10^{-9}$	$86.1 \pm 18.2$
600	$1.47 \times 10^{-9}$	$ee$	$0.25 \pm 0.05$	$1.03 \times 10^{-8} \pm 2.09 \times 10^{-9}$	$50.0 \pm 11.3$
		$\mu\mu$	$0.16 \pm 0.03$	$6.40 \times 10^{-9} \pm 1.31 \times 10^{-9}$	$88.0 \pm 18.5$
700	$4.72 \times 10^{-10}$	$ee$	$0.24 \pm 0.05$	$3.09 \times 10^{-9} \pm 6.27 \times 10^{-10}$	$61.6 \pm 13.9$
		$\mu\mu$	$0.16 \pm 0.03$	$2.05 \times 10^{-9} \pm 4.18 \times 10^{-10}$	$87.9 \pm 18.5$
800	$1.73 \times 10^{-10}$	$ee$	$0.26 \pm 0.05$	$1.24 \times 10^{-9} \pm 2.52 \times 10^{-10}$	$56.0 \pm 12.7$
		$\mu\mu$	$0.17 \pm 0.03$	$8.40 \times 10^{-10} \pm 1.71 \times 10^{-10}$	$76.9 \pm 16.1$
900	$7.02 \times 10^{-11}$	$ee$	$0.28 \pm 0.06$	$5.53 \times 10^{-10} \pm 1.12 \times 10^{-10}$	$51.5 \pm 14.2$
		$\mu\mu$	$0.17 \pm 0.03$	$3.38 \times 10^{-10} \pm 6.90 \times 10^{-11}$	$78.3 \pm 16.7$
1000	$3.09 \times 10^{-11}$	$ee$	$0.27 \pm 0.05$	$2.28 \times 10^{-10} \pm 4.63 \times 10^{-11}$	$62.4 \pm 14.0$
		$\mu\mu$	$0.18 \pm 0.04$	$1.52 \times 10^{-10} \pm 3.10 \times 10^{-11}$	$74.9 \pm 15.7$
1100	$1.45 \times 10^{-11}$	$ee$	$0.28 \pm 0.06$	$1.11 \times 10^{-10} \pm 2.26 \times 10^{-11}$	$65.0 \pm 14.6$
		$\mu\mu$	$0.16 \pm 0.03$	$6.63 \times 10^{-11} \pm 1.35 \times 10^{-11}$	$78.7 \pm 16.4$
1200	$7.19 \times 10^{-12}$	$ee$	$0.27 \pm 0.05$	$5.43 \times 10^{-11} \pm 1.10 \times 10^{-11}$	$64.6 \pm 14.5$
		$\mu\mu$	$0.17 \pm 0.03$	$3.32 \times 10^{-11} \pm 6.78 \times 10^{-12}$	$80.5 \pm 16.9$
1300	$3.74 \times 10^{-12}$	$ee$	$0.25 \pm 0.05$	$2.55 \times 10^{-11} \pm 5.17 \times 10^{-12}$	$49.7 \pm 13.8$
		$\mu\mu$	$0.15 \pm 0.03$	$1.59 \times 10^{-11} \pm 3.26 \times 10^{-12}$	$80.5 \pm 16.8$
1400	$2.02 \times 10^{-12}$	$ee$	$0.25 \pm 0.05$	$1.42 \times 10^{-11} \pm 2.88 \times 10^{-12}$	$68.5 \pm 15.0$
		$\mu\mu$	$0.13 \pm 0.03$	$7.47 \times 10^{-12} \pm 1.53 \times 10^{-12}$	$81.7 \pm 17.2$
1500	$1.13 \times 10^{-12}$	$ee$	$0.25 \pm 0.05$	$7.93 \times 10^{-12} \pm 1.61 \times 10^{-12}$	$69.5 \pm 15.3$
		$\mu\mu$	$0.13 \pm 0.03$	$4.17 \times 10^{-12} \pm 8.57 \times 10^{-13}$	$83.9 \pm 17.6$

Table F.24: Inputs for the EFT  $\rightarrow Z'\chi\chi$  LDS  $\sigma B$  calculations in SR3. The first three columns are the  $Z'$  mass, the theoretical cross-section times branching ratio  $\sigma B$ , and what  $Z'$  decay channel we are looking at. The next two are  $\varepsilon_{\text{sig}}$ , which is the signal selection efficiency, and  $N_{\text{sig}}$ , which is the theoretical number of signal events after the cuts. The last two columns are the number of background events,  $N_{\text{bkg}}$ , and the events observed in the data,  $N_{\text{obs}}$ . The uncertainties of  $\varepsilon_{\text{sig}}$ ,  $N_{\text{sig}}$  and  $N_{\text{bkg}}$  are statistical with an assumed 20% systematic uncertainty. The MET threshold is  $E_{\text{T},\text{min}}^{\text{miss}} = 50\text{GeV}$  and the invariant mass threshold is  $m_{ll}^{\text{min}} = 110\text{GeV}$  and is the same for all inputs.

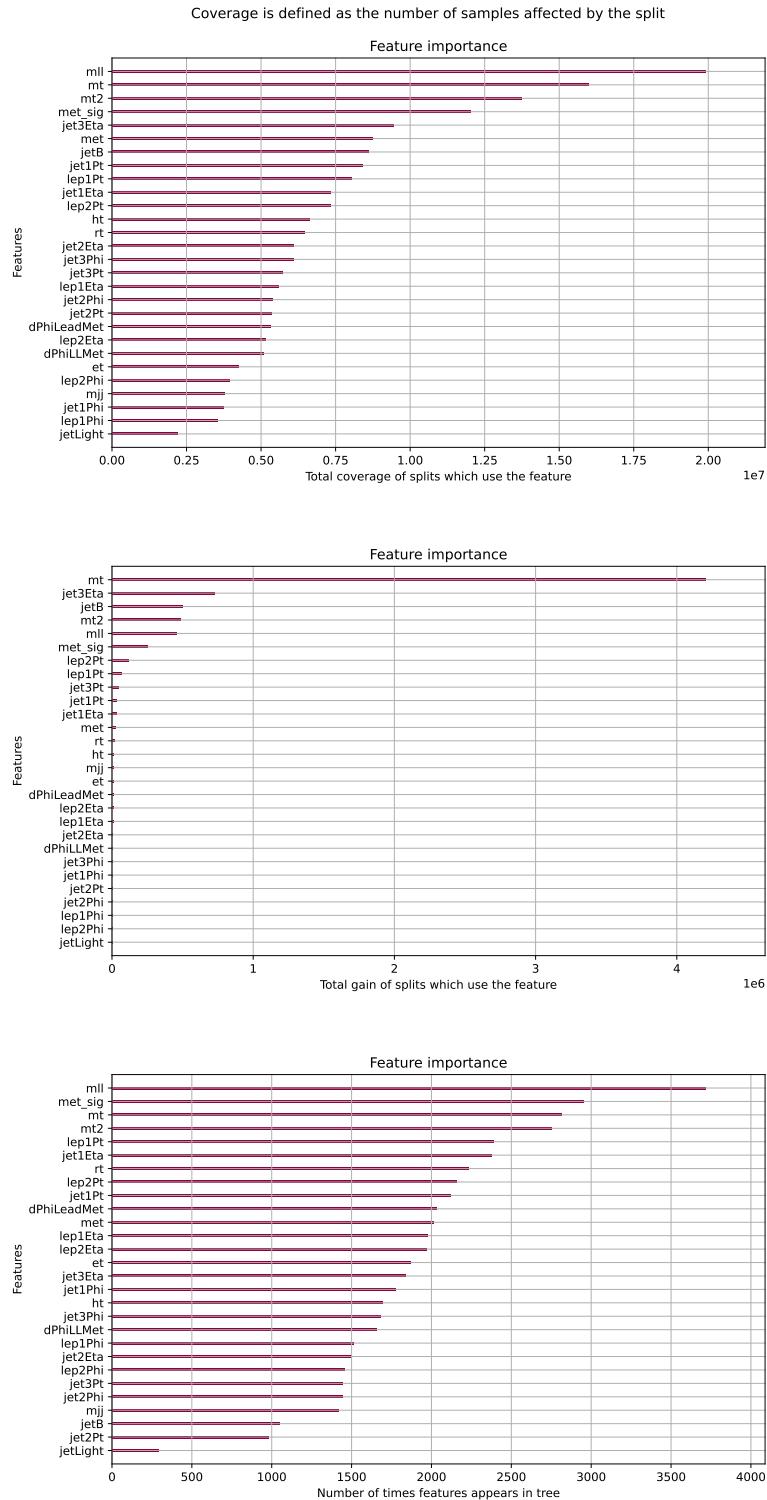
$m_{Z'}$ [GeV]	$\sigma B$ [fb]	Channel	$\varepsilon_{\text{sig}}$ [ $\times 10^{-1}$ ]	$N_{\text{sig}}$	$N_{\text{bkg}}$
130	$3.35 \times 10^{-5}$	$ee$	$0.02 \pm 0.00$	$1.86 \times 10^{-5} \pm 4.05 \times 10^{-6}$	$26.5 \pm 6.5$
		$\mu\mu$	$0.01 \pm 0.00$	$8.90 \times 10^{-6} \pm 2.08 \times 10^{-6}$	$15.7 \pm 3.9$
200	$2.67 \times 10^{-6}$	$ee$	$0.07 \pm 0.01$	$5.06 \times 10^{-6} \pm 1.05 \times 10^{-6}$	$23.7 \pm 6.1$
		$\mu\mu$	$0.05 \pm 0.01$	$3.46 \times 10^{-6} \pm 7.24 \times 10^{-7}$	$22.6 \pm 5.5$
300	$2.06 \times 10^{-7}$	$ee$	$0.13 \pm 0.03$	$7.71 \times 10^{-7} \pm 1.57 \times 10^{-7}$	$14.6 \pm 6.5$
		$\mu\mu$	$0.08 \pm 0.02$	$4.33 \times 10^{-7} \pm 8.95 \times 10^{-8}$	$18.3 \pm 4.4$
400	$2.65 \times 10^{-8}$	$ee$	$0.27 \pm 0.05$	$2.00 \times 10^{-7} \pm 4.04 \times 10^{-8}$	$15.9 \pm 4.9$
		$\mu\mu$	$0.17 \pm 0.03$	$1.27 \times 10^{-7} \pm 2.57 \times 10^{-8}$	$20.6 \pm 4.8$
500	$5.46 \times 10^{-9}$	$ee$	$0.31 \pm 0.06$	$4.75 \times 10^{-8} \pm 9.60 \times 10^{-9}$	$18.2 \pm 4.8$
		$\mu\mu$	$0.21 \pm 0.04$	$3.15 \times 10^{-8} \pm 6.39 \times 10^{-9}$	$18.5 \pm 4.7$
600	$1.47 \times 10^{-9}$	$ee$	$0.46 \pm 0.09$	$1.89 \times 10^{-8} \pm 3.81 \times 10^{-9}$	$16.7 \pm 4.9$
		$\mu\mu$	$0.31 \pm 0.06$	$1.27 \times 10^{-8} \pm 2.57 \times 10^{-9}$	$21.1 \pm 5.2$
700	$4.72 \times 10^{-10}$	$ee$	$0.49 \pm 0.10$	$6.40 \times 10^{-9} \pm 1.29 \times 10^{-9}$	$21.5 \pm 5.5$
		$\mu\mu$	$0.35 \pm 0.07$	$4.56 \times 10^{-9} \pm 9.20 \times 10^{-10}$	$17.2 \pm 4.3$
800	$1.73 \times 10^{-10}$	$ee$	$0.63 \pm 0.13$	$3.05 \times 10^{-9} \pm 6.14 \times 10^{-10}$	$21.5 \pm 5.8$
		$\mu\mu$	$0.42 \pm 0.08$	$2.04 \times 10^{-9} \pm 4.11 \times 10^{-10}$	$18.7 \pm 4.8$
900	$7.02 \times 10^{-11}$	$ee$	$0.72 \pm 0.14$	$1.41 \times 10^{-9} \pm 2.84 \times 10^{-10}$	$18.8 \pm 6.9$
		$\mu\mu$	$0.49 \pm 0.10$	$9.62 \times 10^{-10} \pm 1.94 \times 10^{-10}$	$20.1 \pm 4.9$
1000	$3.09 \times 10^{-11}$	$ee$	$0.75 \pm 0.15$	$6.47 \times 10^{-10} \pm 1.30 \times 10^{-10}$	$15.3 \pm 6.8$
		$\mu\mu$	$0.53 \pm 0.11$	$4.51 \times 10^{-10} \pm 9.08 \times 10^{-11}$	$20.8 \pm 4.9$
1100	$1.45 \times 10^{-11}$	$ee$	$0.83 \pm 0.17$	$3.37 \times 10^{-10} \pm 6.76 \times 10^{-11}$	$21.1 \pm 5.6$
		$\mu\mu$	$0.59 \pm 0.12$	$2.40 \times 10^{-10} \pm 4.82 \times 10^{-11}$	$23.4 \pm 5.6$
1200	$7.19 \times 10^{-12}$	$ee$	$0.90 \pm 0.18$	$1.79 \times 10^{-10} \pm 3.60 \times 10^{-11}$	$19.7 \pm 5.6$
		$\mu\mu$	$0.62 \pm 0.12$	$1.23 \times 10^{-10} \pm 2.48 \times 10^{-11}$	$21.9 \pm 5.2$
1300	$3.74 \times 10^{-12}$	$ee$	$0.93 \pm 0.19$	$9.63 \times 10^{-11} \pm 1.93 \times 10^{-11}$	$12.4 \pm 6.2$
		$\mu\mu$	$0.65 \pm 0.13$	$6.77 \times 10^{-11} \pm 1.36 \times 10^{-11}$	$14.0 \pm 3.7$
1400	$2.02 \times 10^{-12}$	$ee$	$0.97 \pm 0.19$	$5.46 \times 10^{-11} \pm 1.10 \times 10^{-11}$	$9.2 \pm 6.2$
		$\mu\mu$	$0.66 \pm 0.13$	$3.70 \times 10^{-11} \pm 7.44 \times 10^{-12}$	$18.4 \pm 4.5$
1500	$1.13 \times 10^{-12}$	$ee$	$1.02 \pm 0.20$	$3.20 \times 10^{-11} \pm 6.43 \times 10^{-12}$	$24.4 \pm 6.5$
		$\mu\mu$	$0.65 \pm 0.13$	$2.04 \times 10^{-11} \pm 4.11 \times 10^{-12}$	$19.4 \pm 4.6$

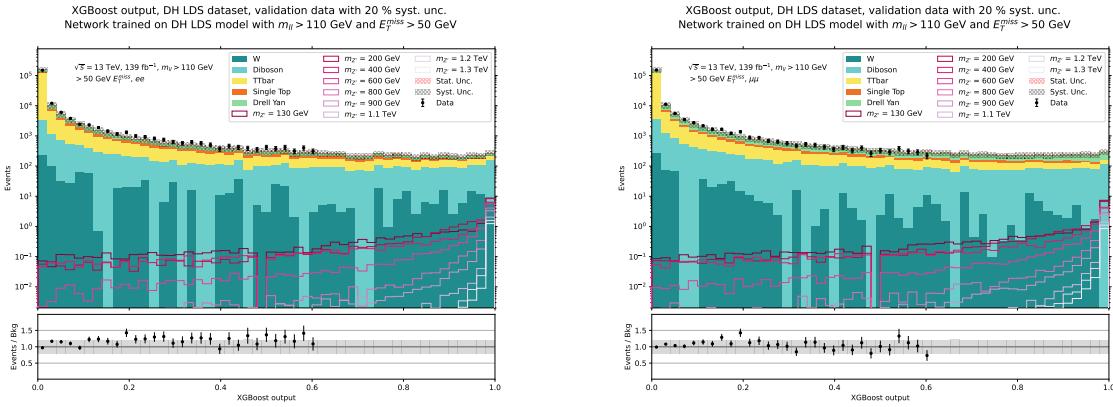
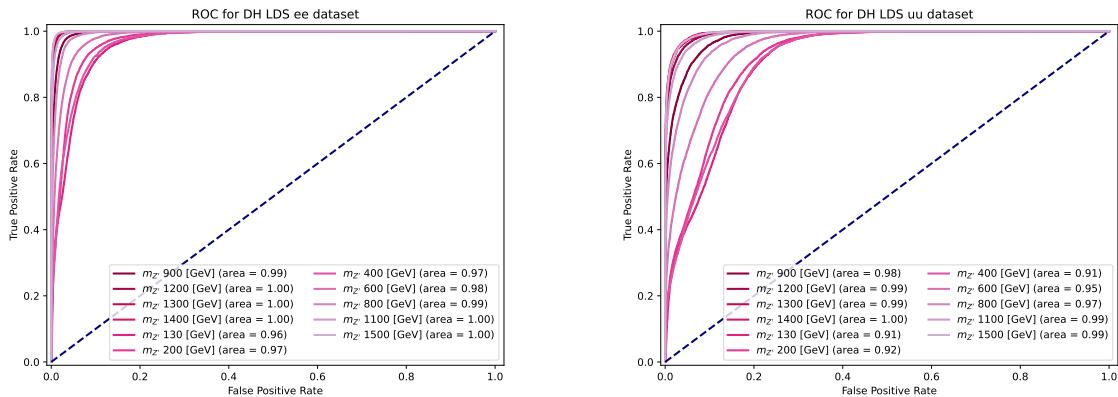
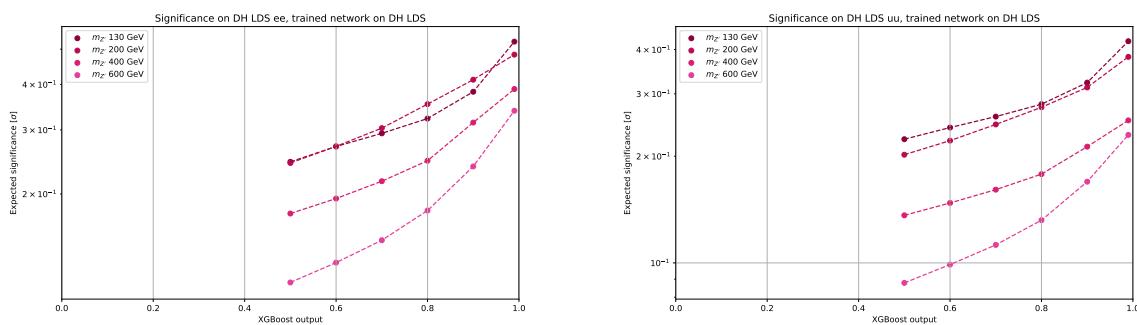


# Appendix G

## Model dependent approach

### G.1 Dark Higgs Light Dark Sector

Figure G.1: Feature importance for network trained on  $Z'$  DH LDS

Figure G.2: Validation plots for network trained on  $Z'$  DH LDSFigure G.3: ROC plots for every  $Z'$  mass point on network trained on  $Z'$  DH LDSFigure G.4: Expected significance plots for  $Z'$  mass points on network trained on  $Z'$  DH LDS

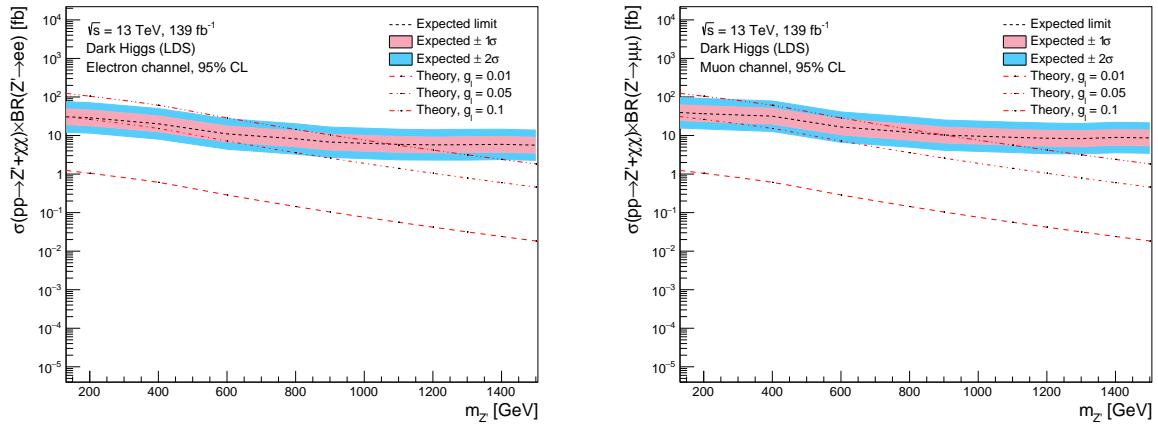


Figure G.5: Mass exclusion limits of  $ee$  and  $\mu\mu$  channel for all  $Z'$  DH LDS model

## G.2 Light Vector Heavy Dark Sector

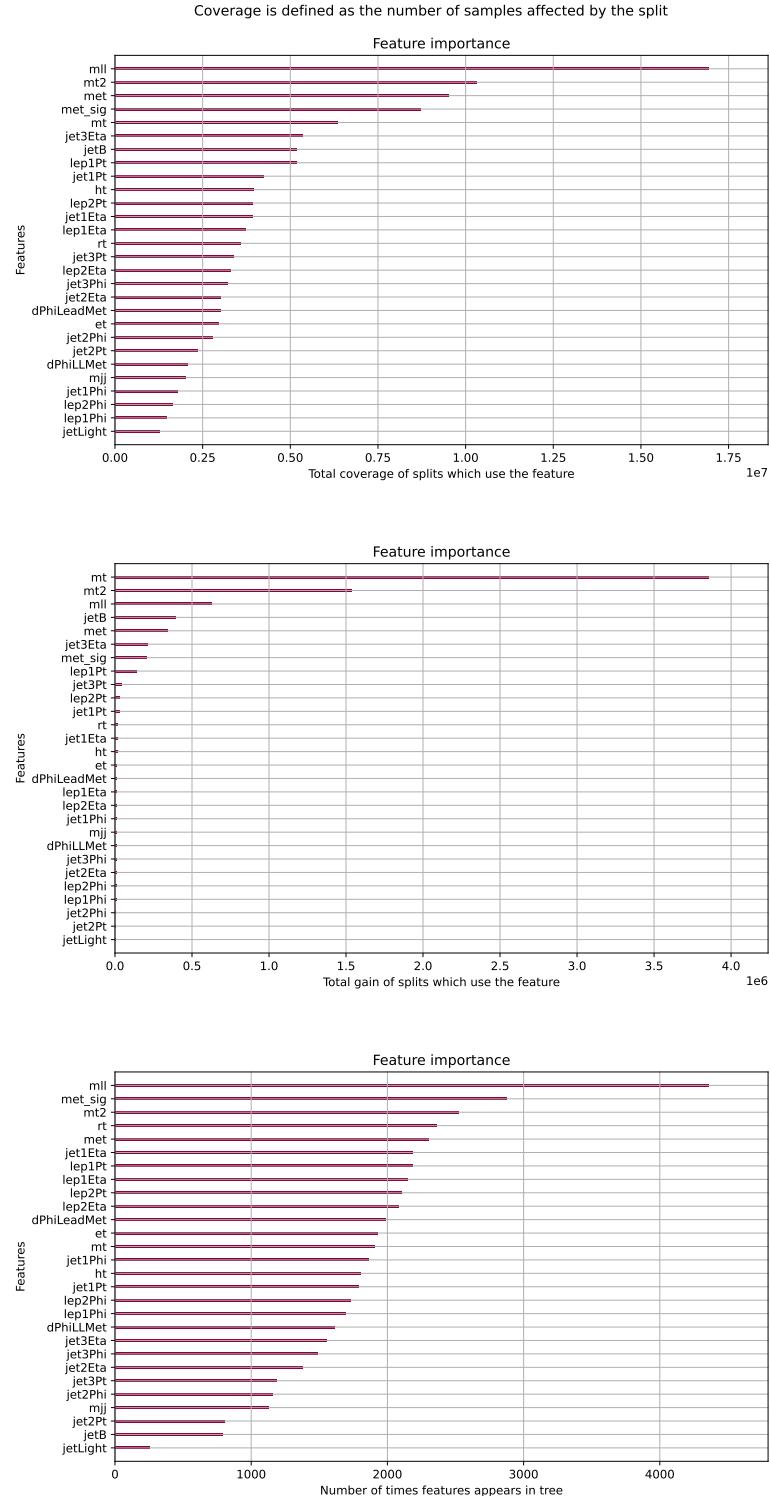
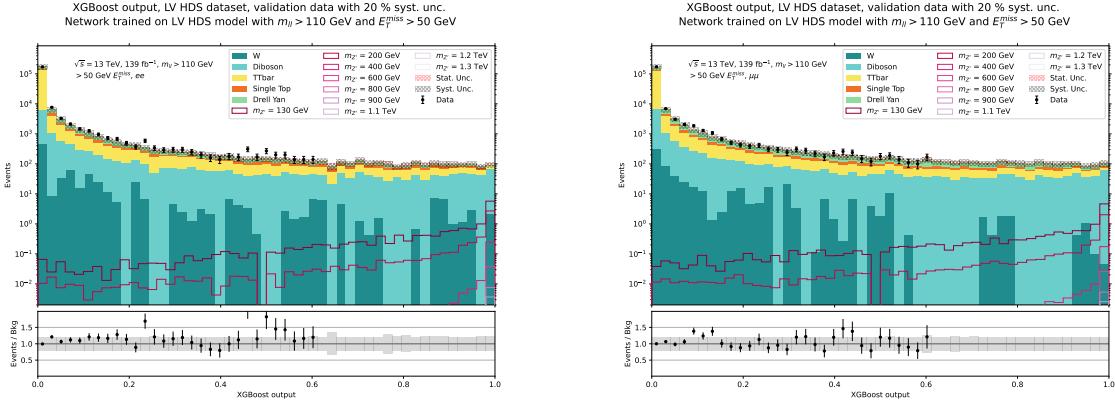
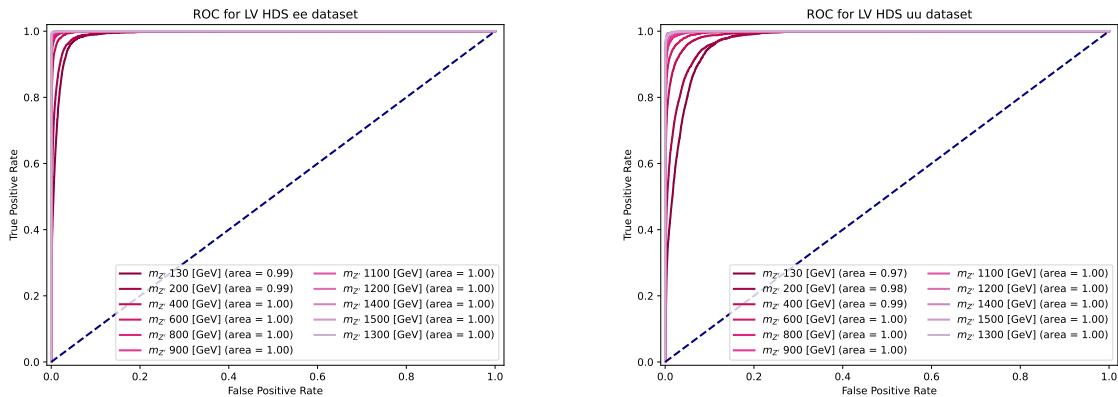
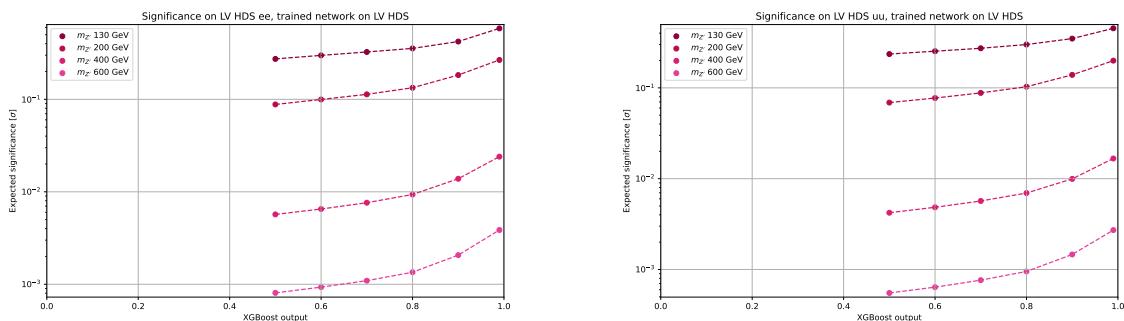


Figure G.6: Feature importance for network trained on  $Z'$  LV HDS

Figure G.7: Validation plots for network trained on  $Z'$  LV HDSFigure G.8: ROC plots for every  $Z'$  mass point on network trained on  $Z'$  LV HDSFigure G.9: Expected significance plots for  $Z'$  mass points on network trained on  $Z'$  LV HDS

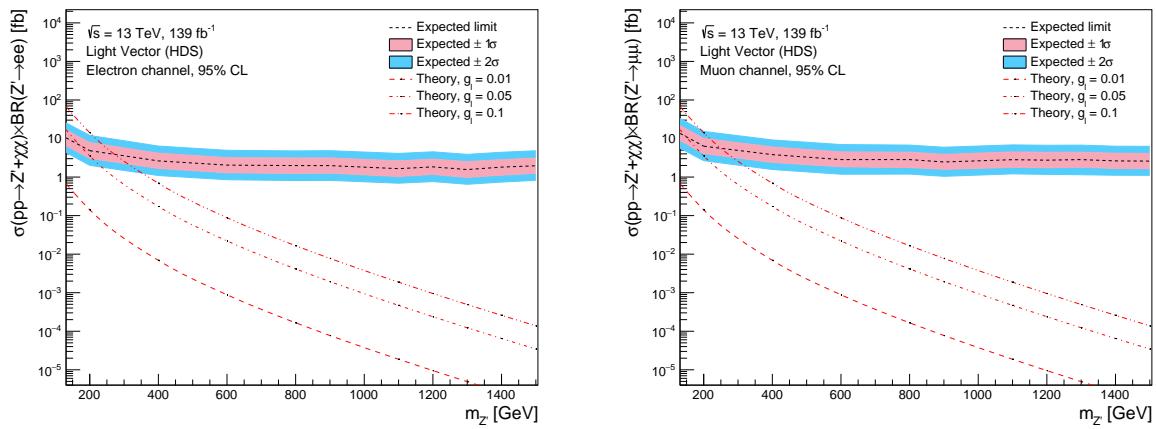


Figure G.10: Mass exclusion limits of  $ee$  and  $\mu\mu$  channel for all  $Z'$  LV HDS model

### G.3 Light Vector Light Dark Sector

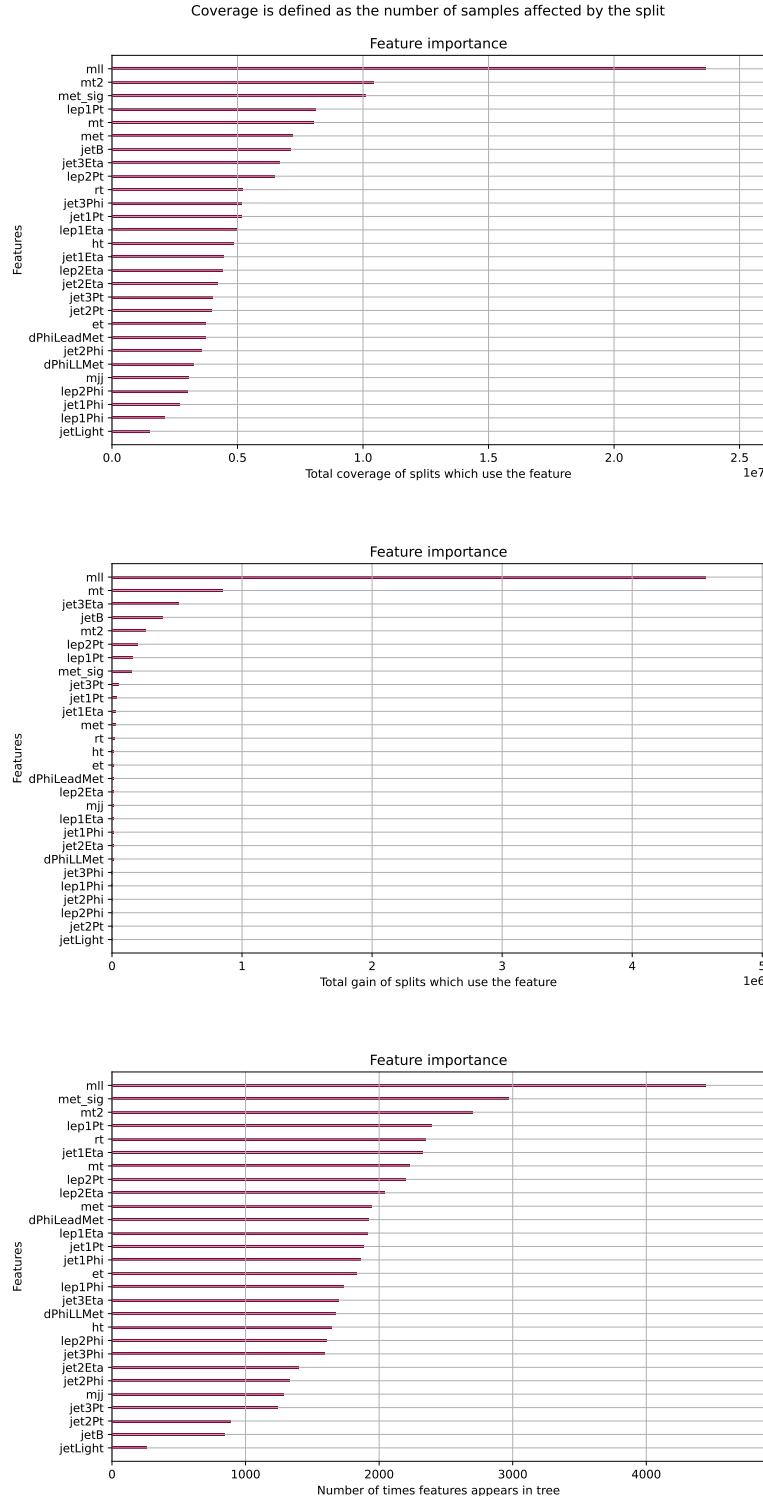
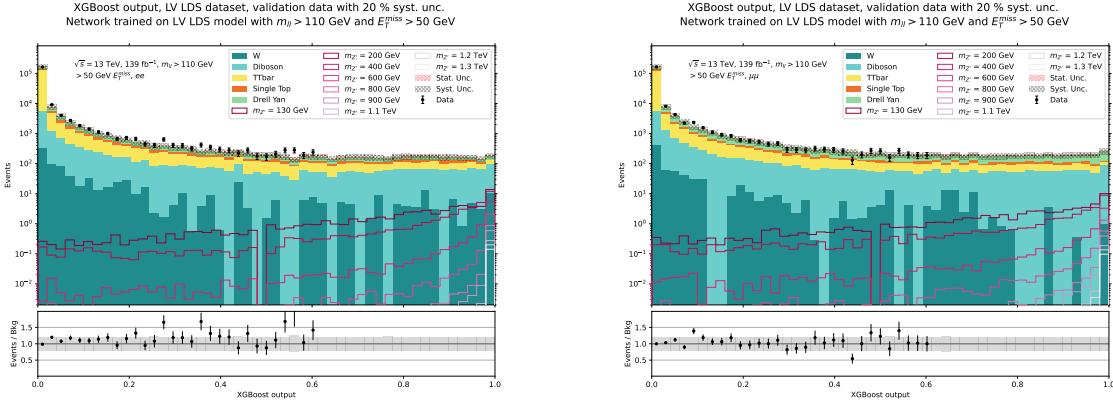
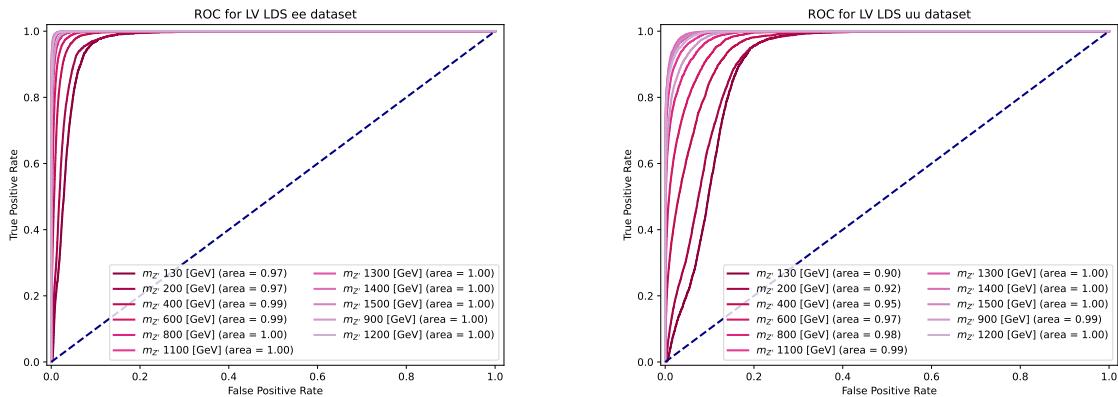
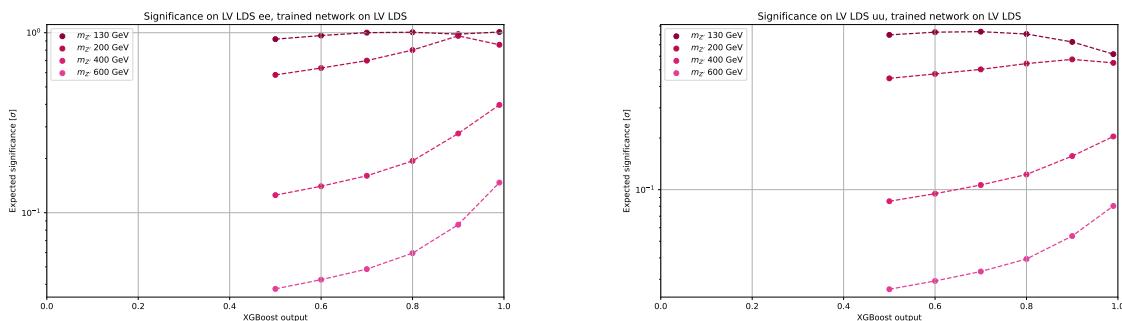


Figure G.11: Feature importance for network trained on  $Z'$  LV LDS

Figure G.12: Validation plots for network trained on  $Z'$  LV LDSFigure G.13: ROC plots for every  $Z'$  mass point on network trained on  $Z'$  LV LDSFigure G.14: Expected significance plots for  $Z'$  mass points on network trained on  $Z'$  LV LDS

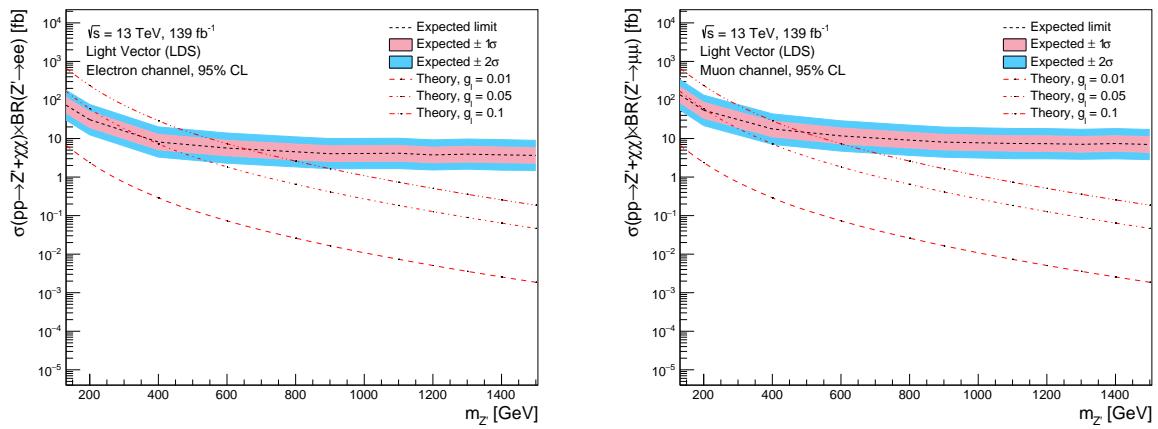


Figure G.15: Mass exclusion limits of  $ee$  and  $\mu\mu$  channel for all  $Z'$  LV LDS model

## G.4 Effective Field Theory Heavy Dark Sector

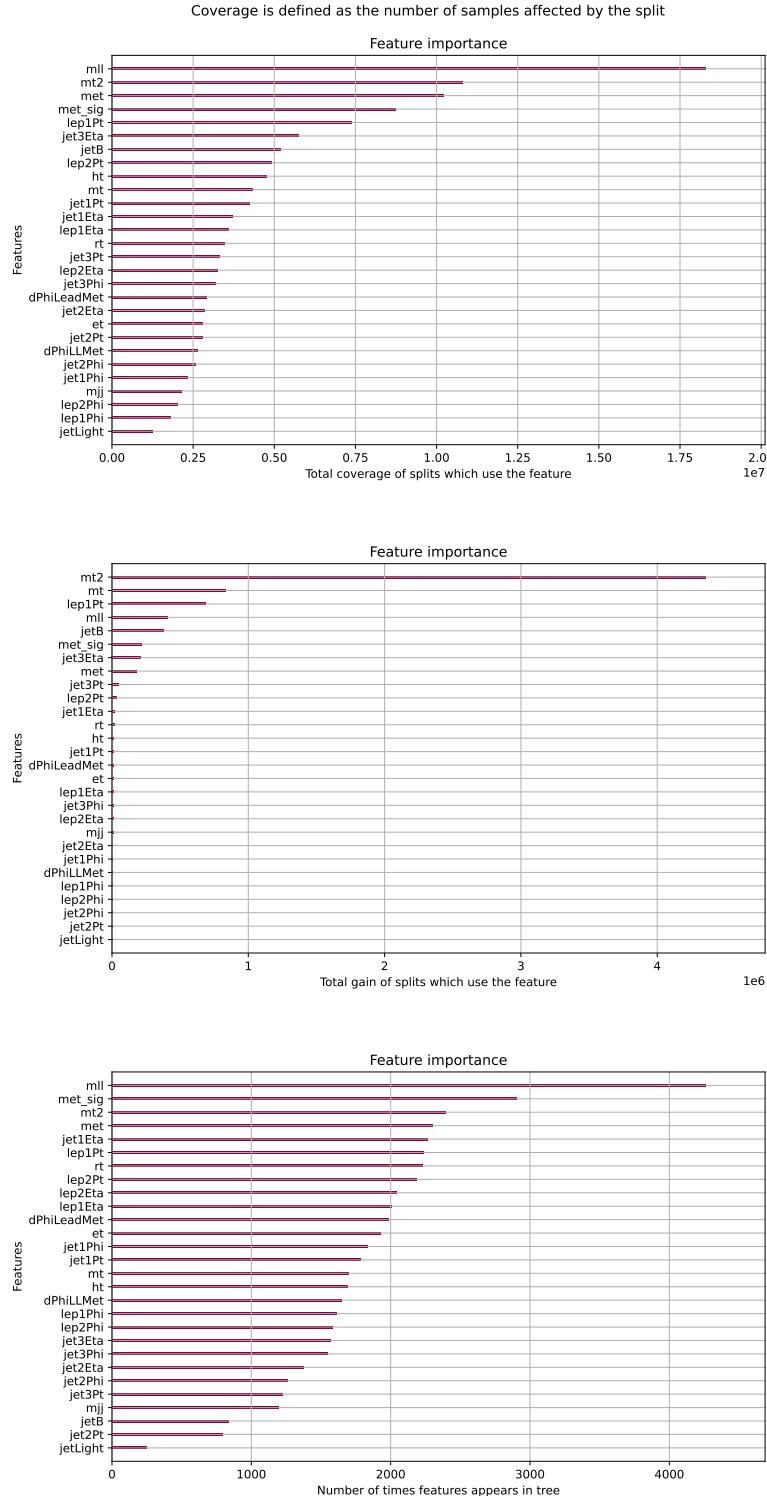
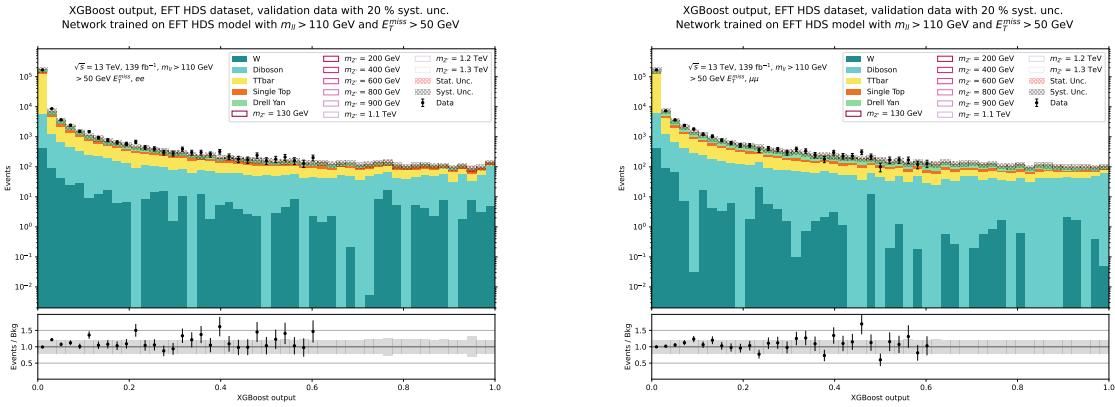
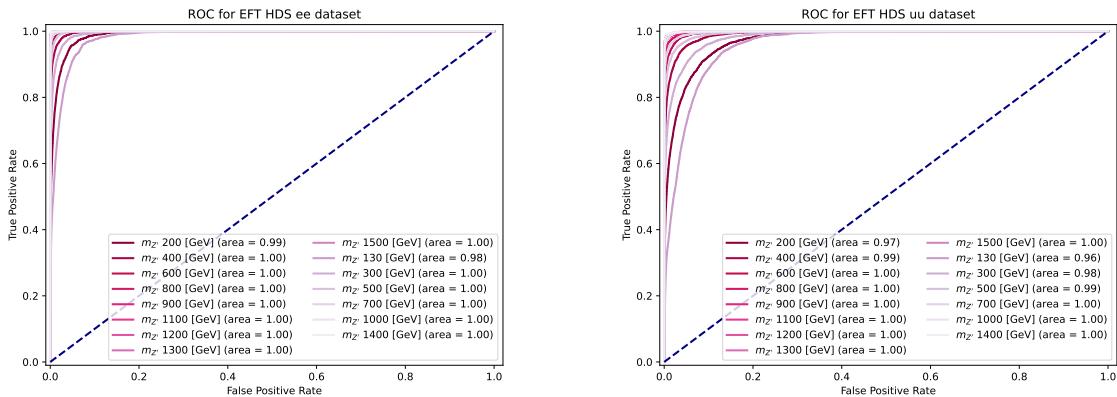
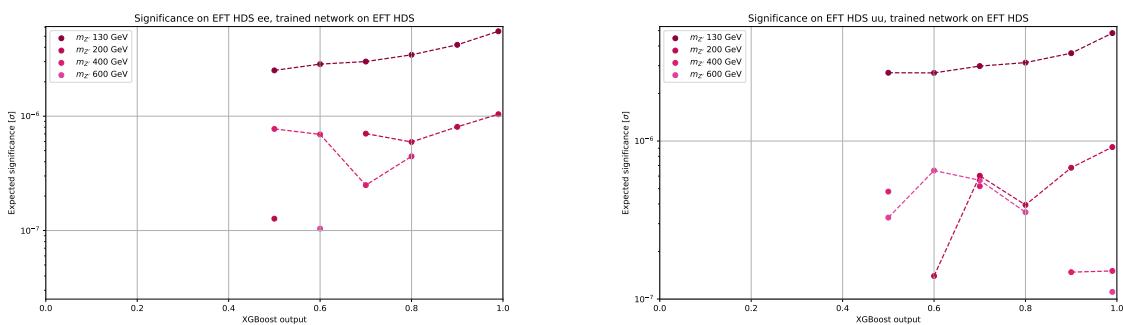


Figure G.16: Feature importance for network trained on  $Z'$  EFT HDS

Figure G.17: Validation plots for network trained on  $Z'$  EFT HDSFigure G.18: ROC plots for every  $Z'$  mass point on network trained on  $Z'$  EFT HDSFigure G.19: Expected significance plots for  $Z'$  mass points on network trained on  $Z'$  EFT HDS

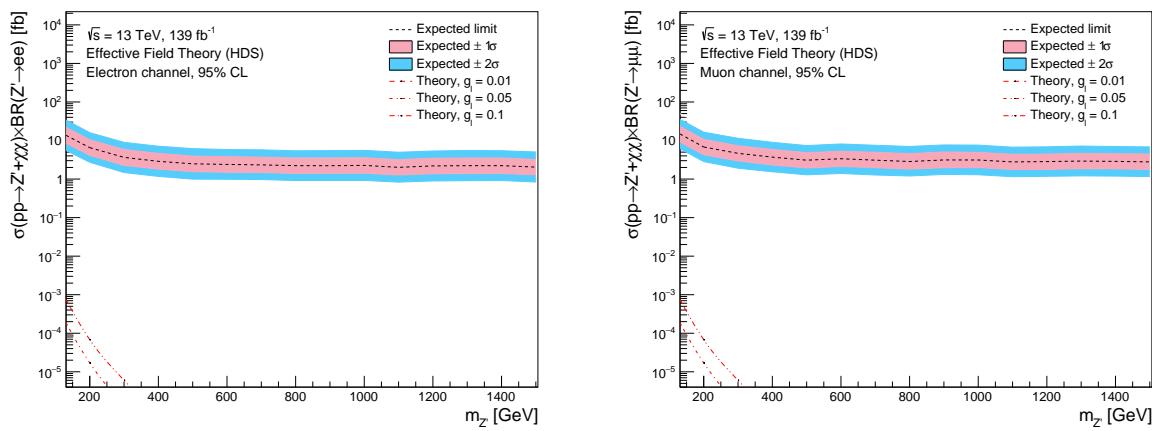


Figure G.20: Mass exclusion limits of  $ee$  and  $\mu\mu$  channel for all  $Z'$  EFT HDS model

## G.5 Effective Field Theory Light Dark Sector

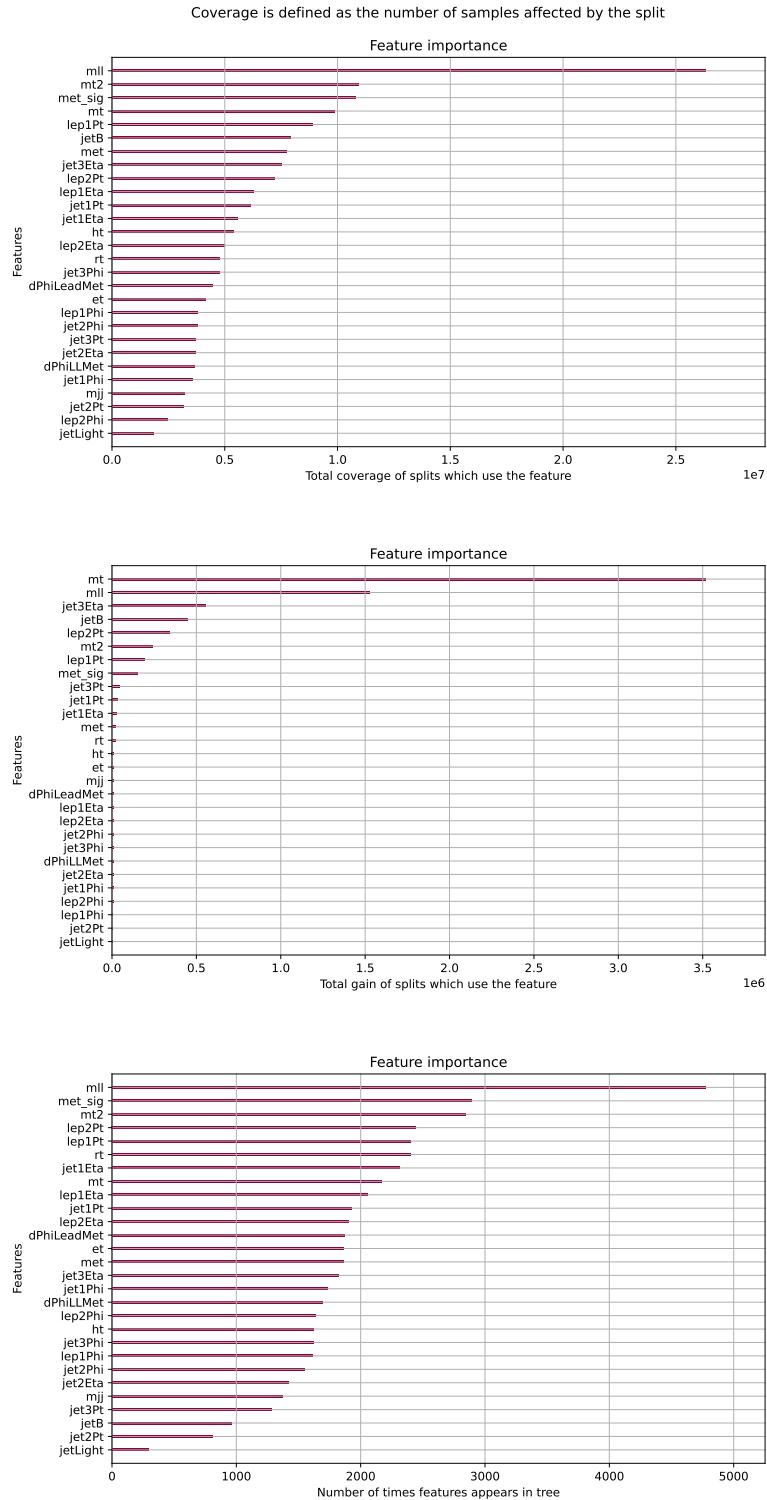
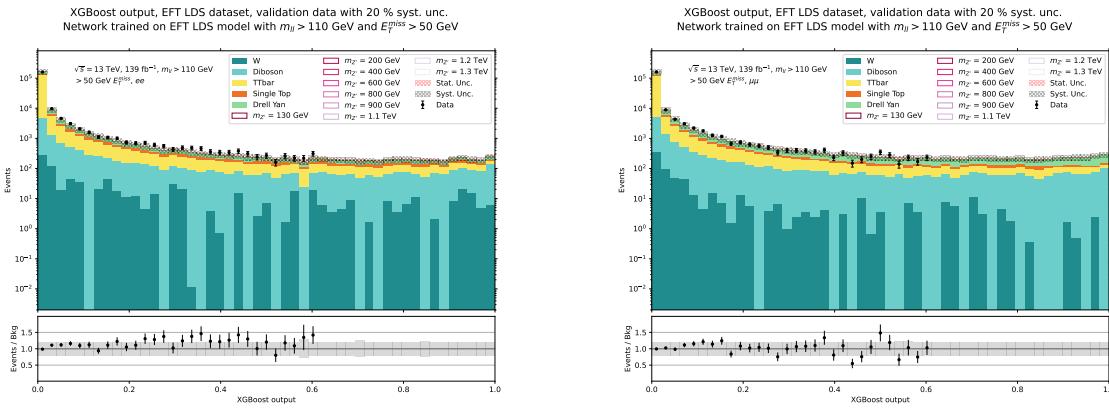
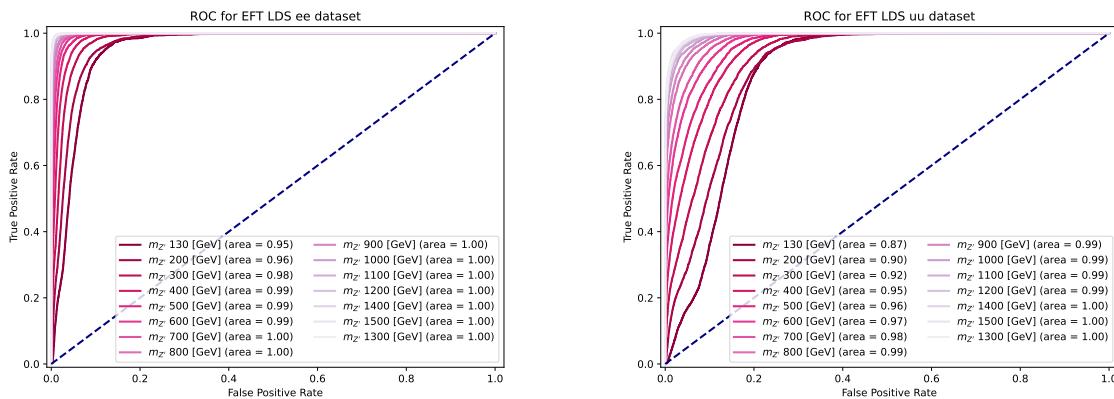
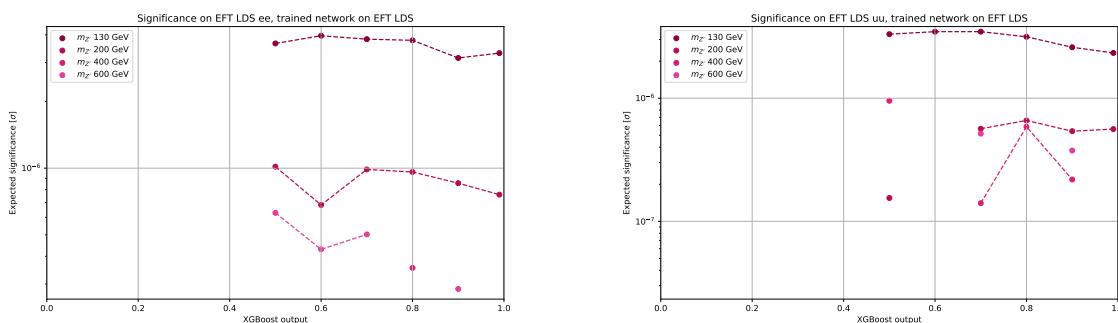


Figure G.21: Feature importance for network trained on  $Z'$  EFT LDS

Figure G.22: Validation plots for network trained on  $Z'$  EFT LDSFigure G.23: ROC plots for every  $Z'$  mass point on network trained on  $Z'$  EFT LDSFigure G.24: Expected significance plots for  $Z'$  mass points on network trained on  $Z'$  EFT LDS

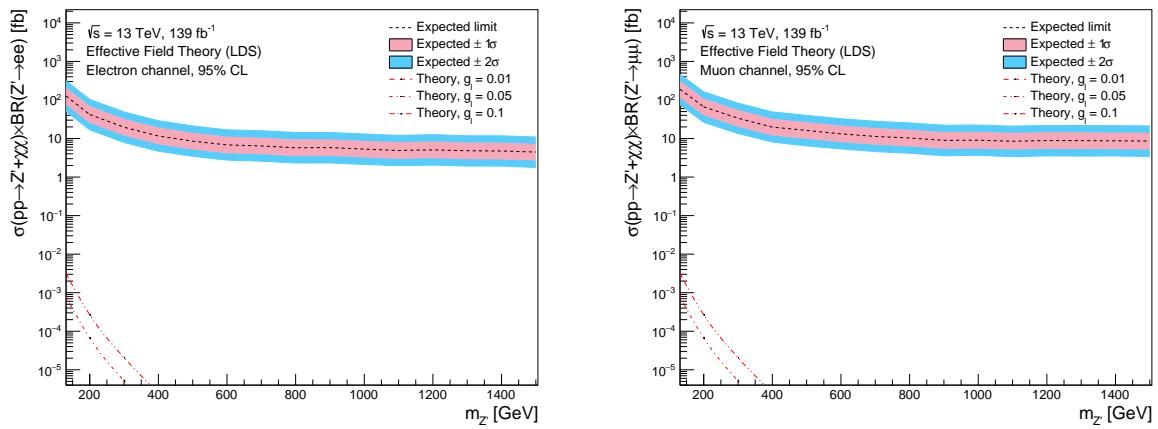


Figure G.25: Mass exclusion limits of  $ee$  and  $\mu\mu$  channel for all  $Z'$  EFT LDS model

## Appendix H

### Model independent approach

#### H.1 Dark Higgs Light Dark Sector

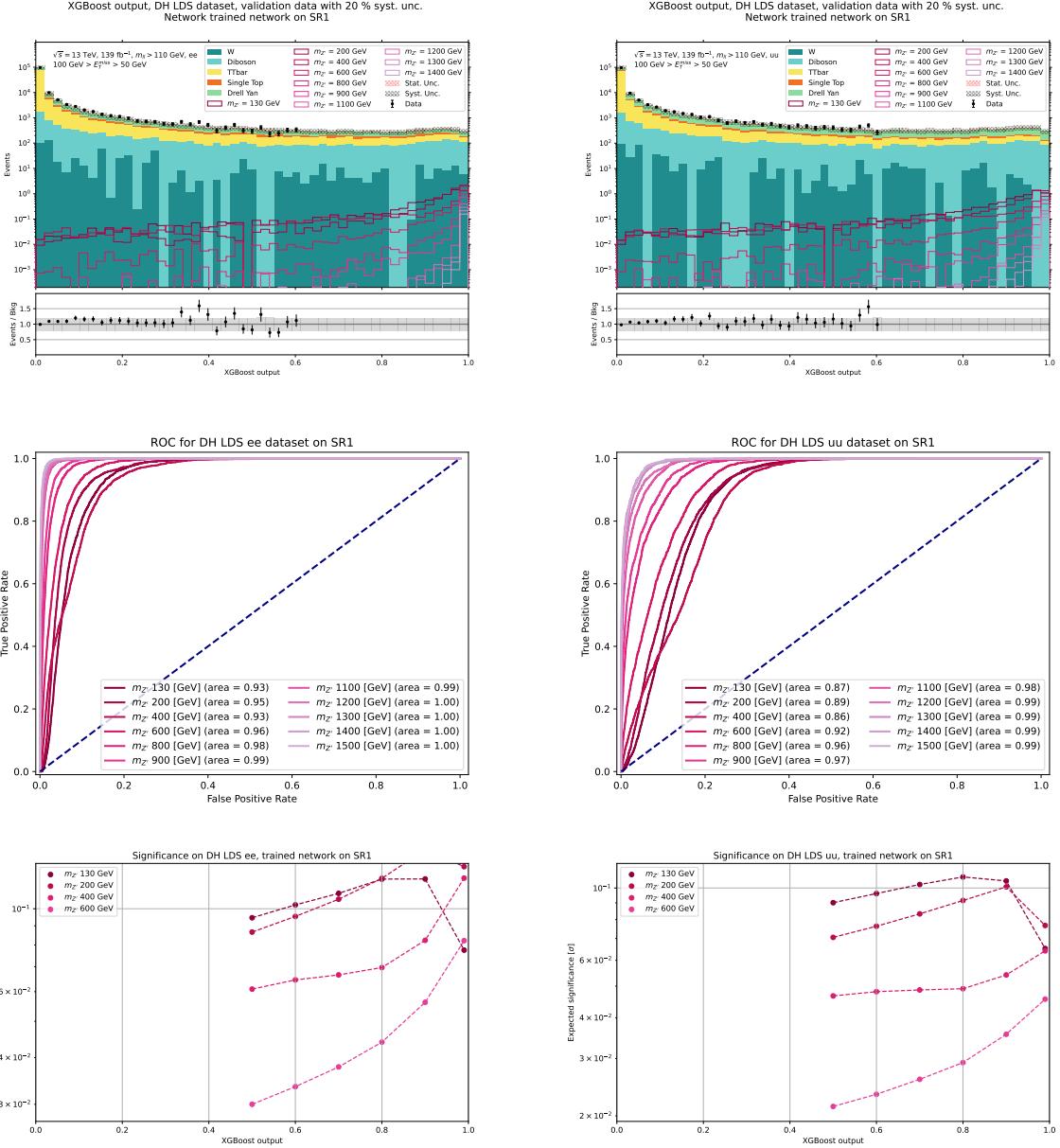
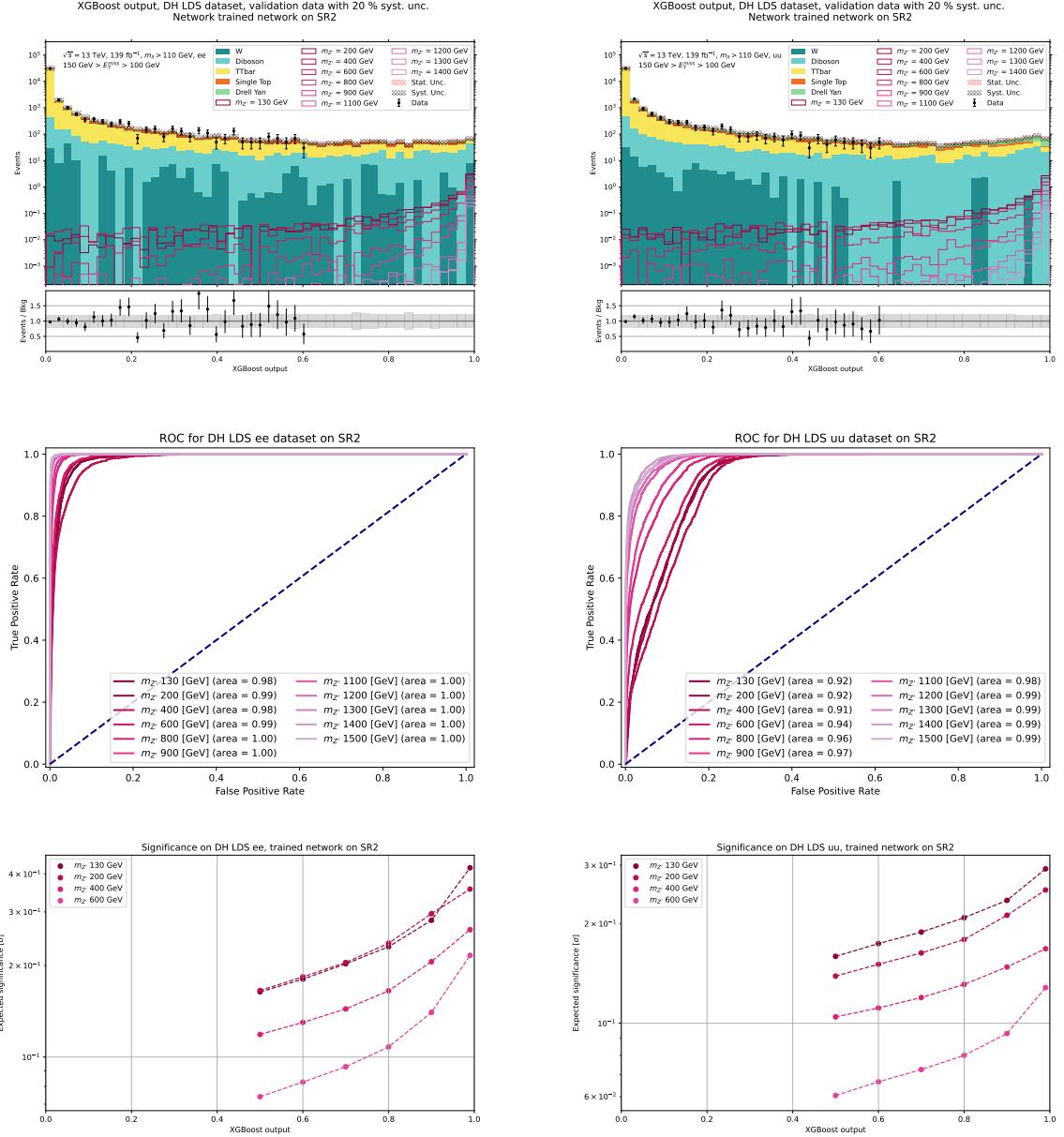


Figure H.1: XGBoost results for DH LDS model on  $ee$  and  $\mu\mu$  channel in SR1

Figure H.2: XGBoost results for DH LDS model on  $ee$  and  $\mu\mu$  channel in SR2

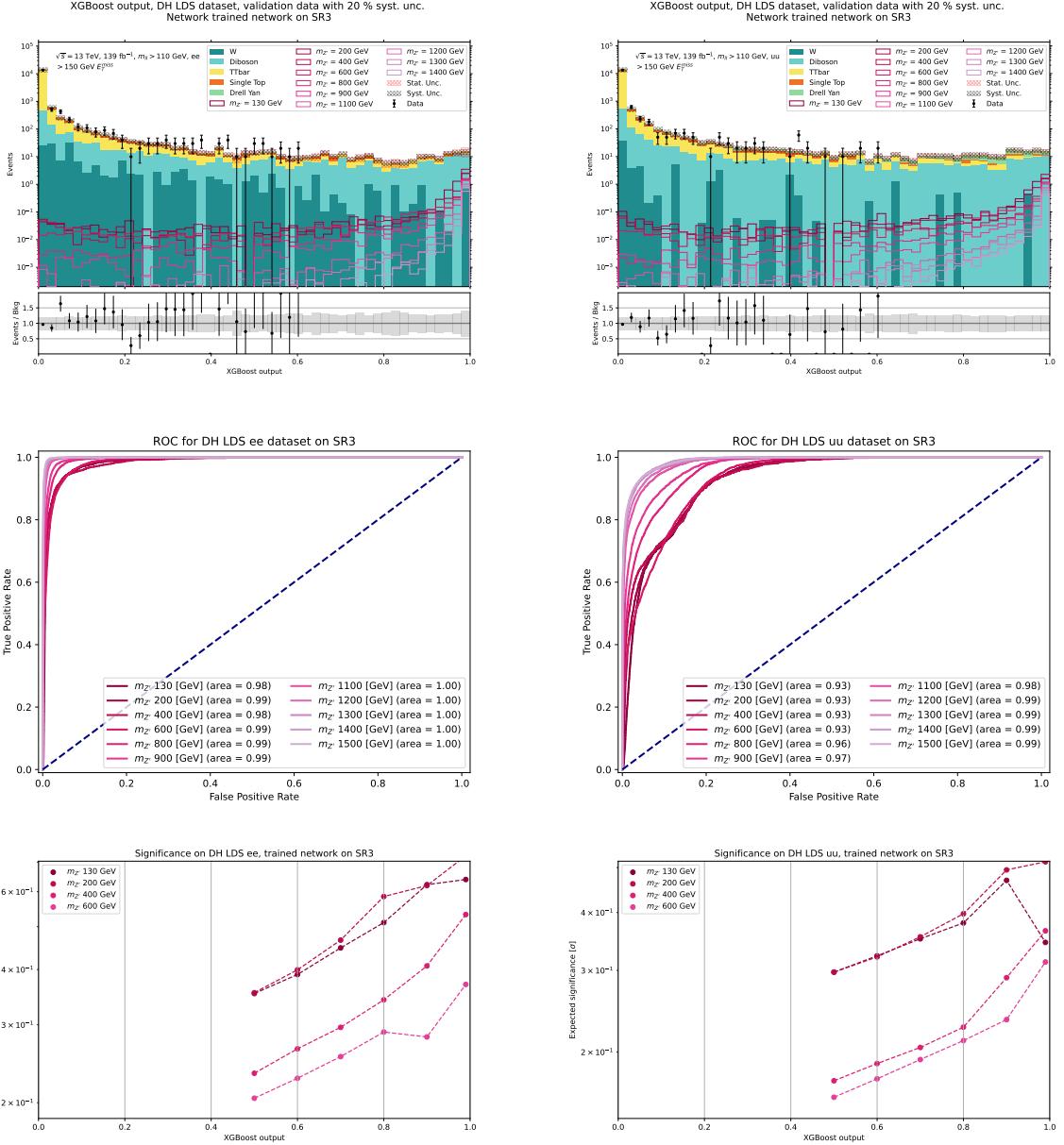


Figure H.3: XGBoost results for DH LDS model on  $ee$  and  $\mu\mu$  channel in SR3

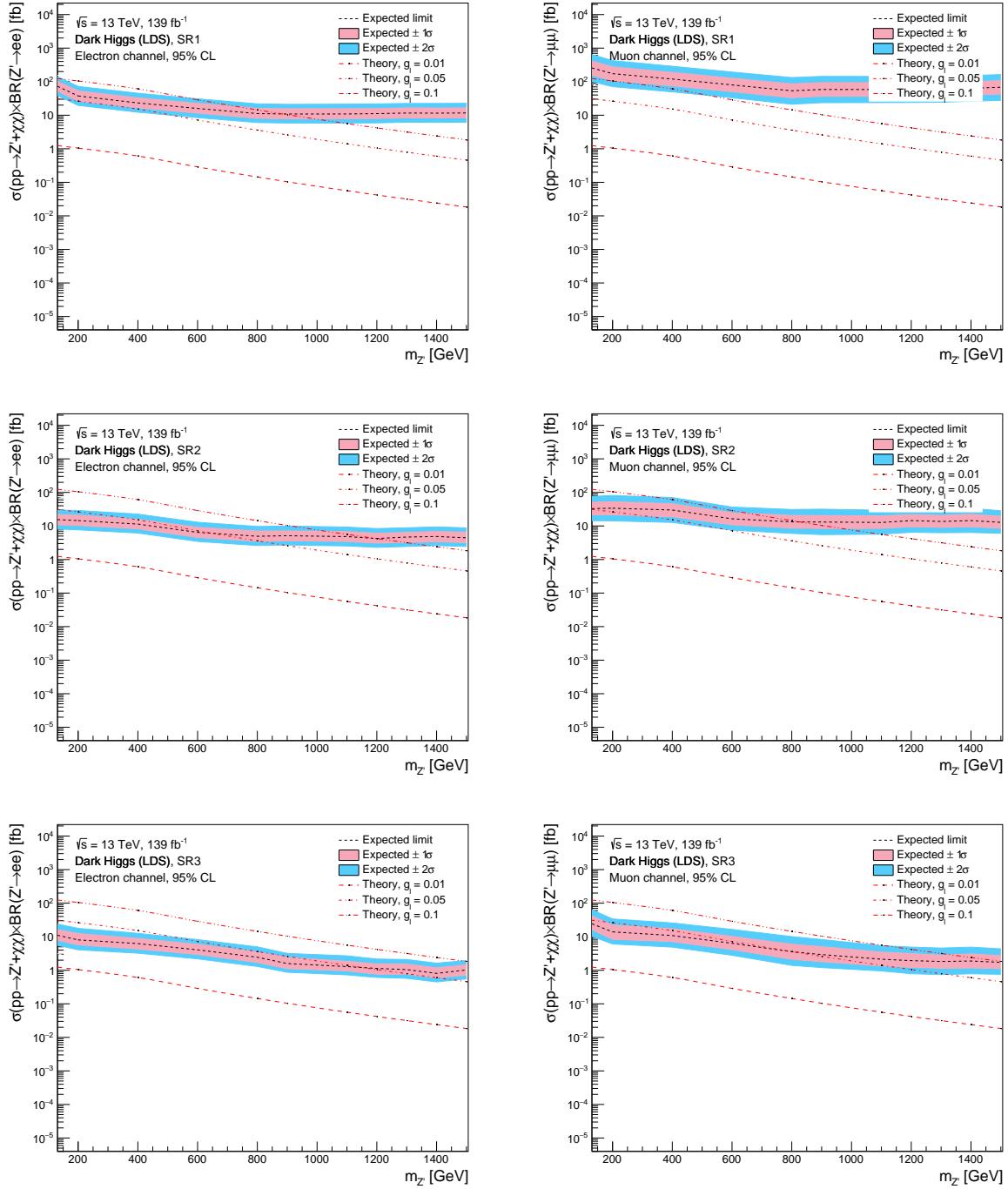


Figure H.4: Mass exclusion limits results for DH LDS model on  $ee$  and  $\mu\mu$  channel in all SRs

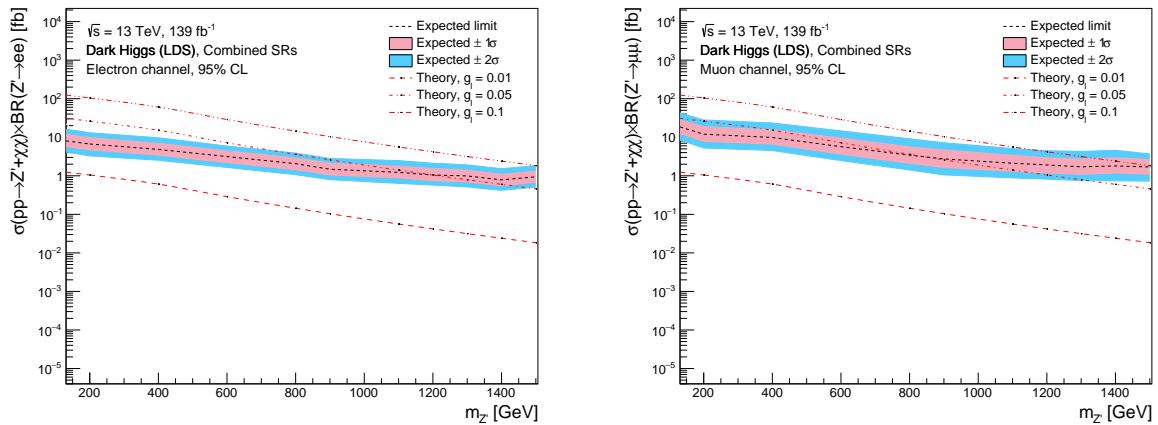


Figure H.5: Mass exclusion limits results for DH LDS model on  $ee$  and  $\mu\mu$  channel in combined SRs

## H.2 Light Vector Heavy Dark Sector

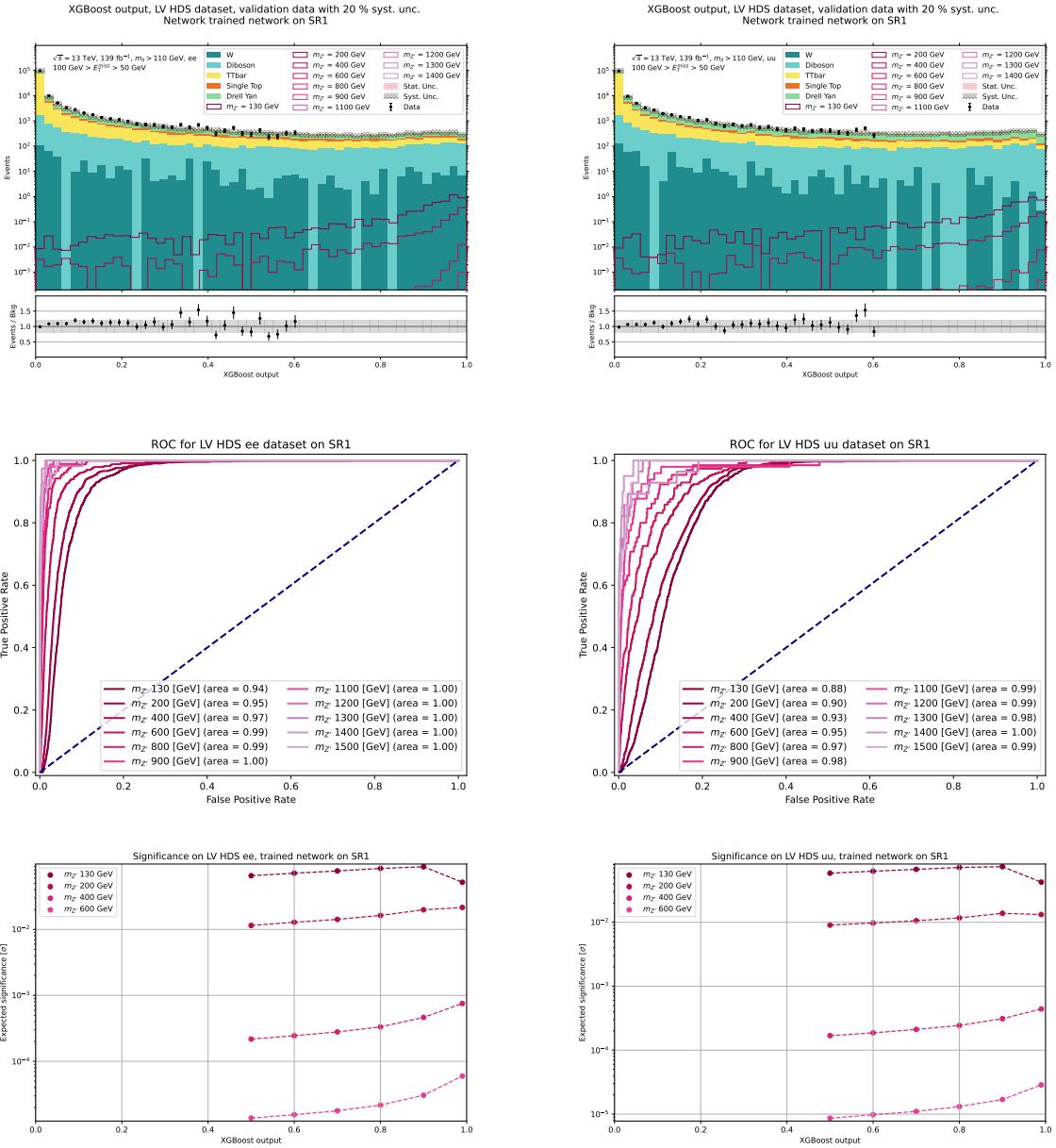


Figure H.6: XGBoost results for LV HDS model on  $ee$  and  $\mu\mu$  channel in SR1

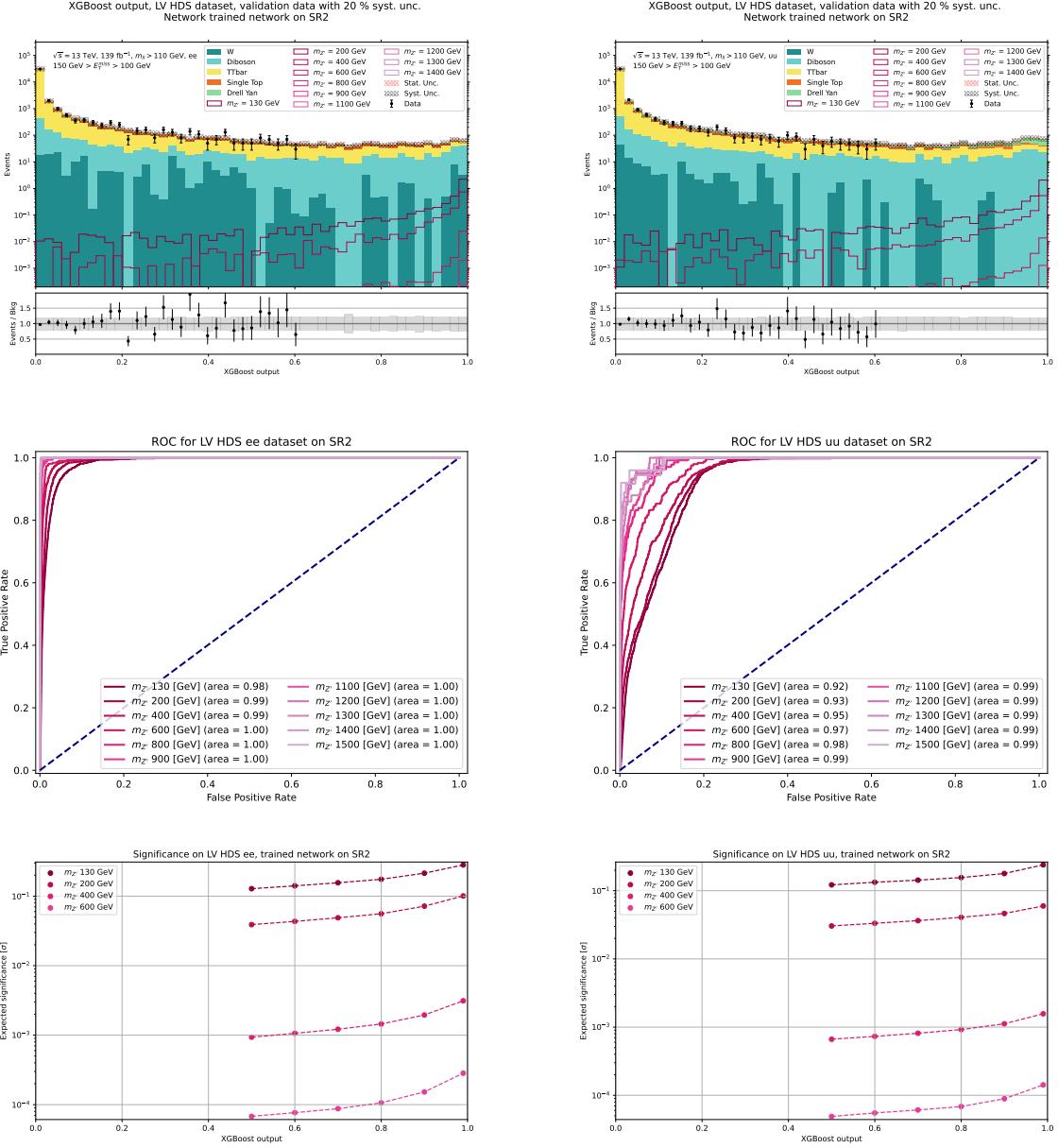
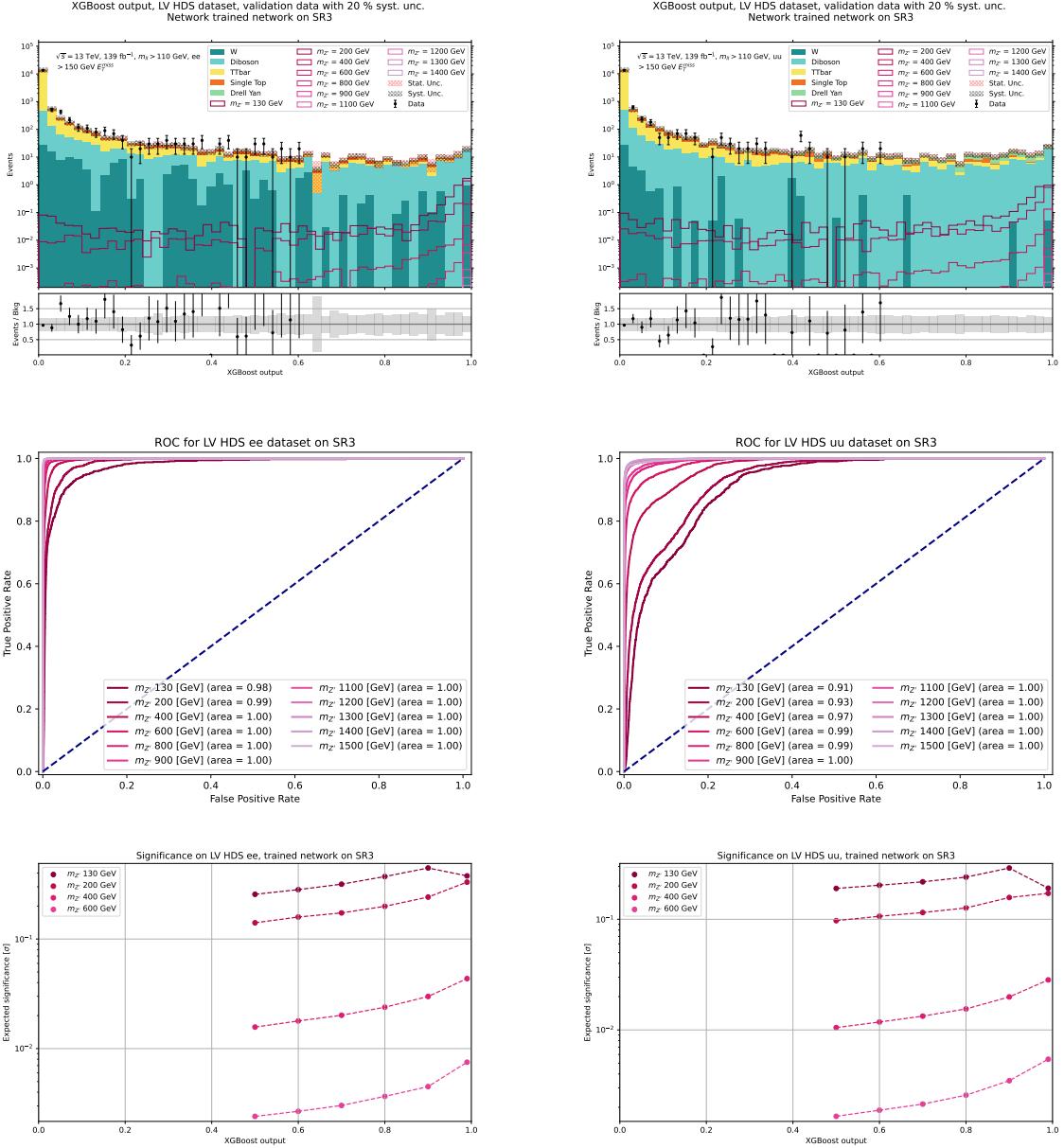


Figure H.7: XGBoost results for LV HDS model on  $ee$  and  $\mu\mu$  channel in SR2

Figure H.8: XGBoost results for LV HDS model on  $ee$  and  $\mu\mu$  channel in SR3

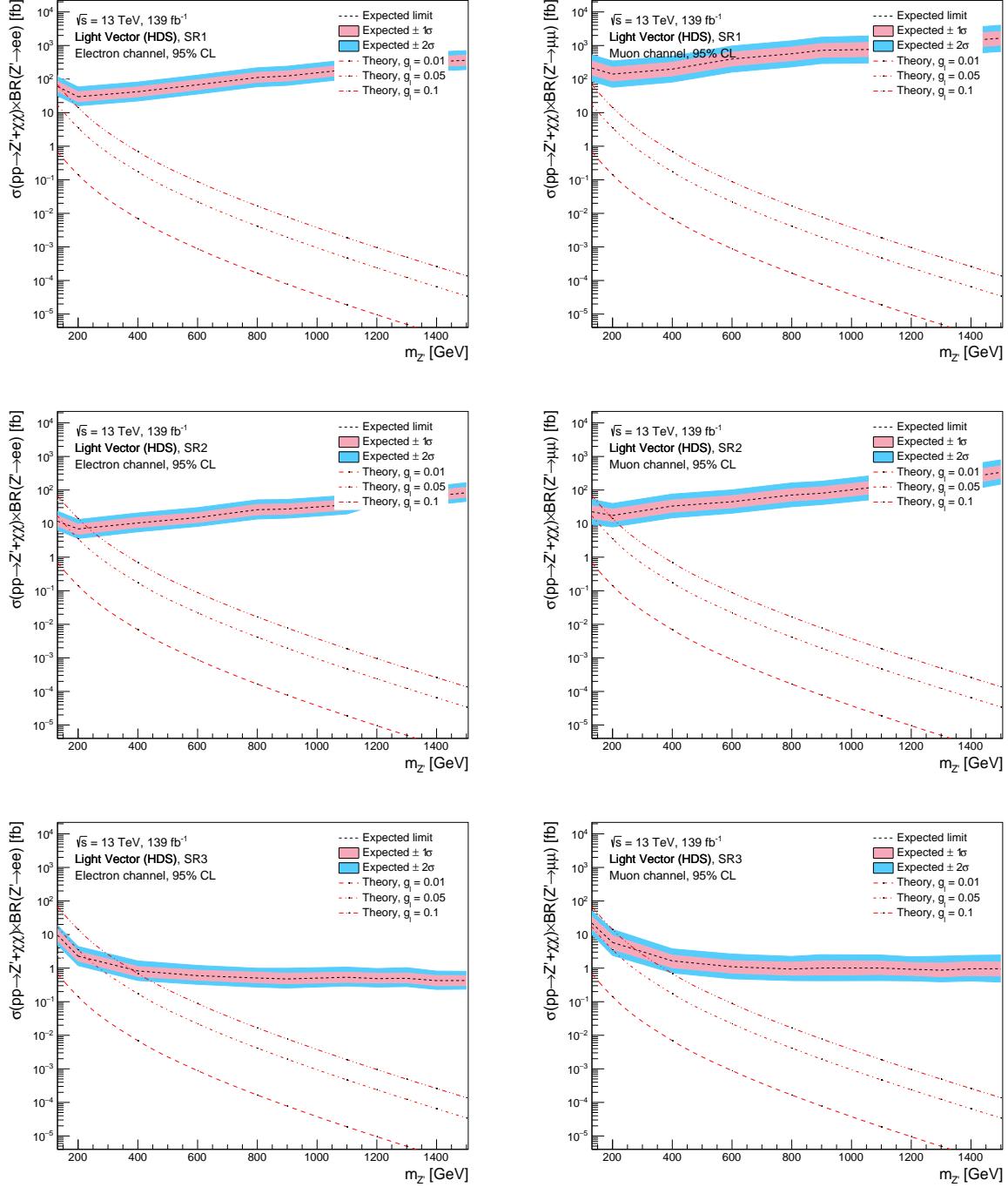


Figure H.9: Mass exclusion limits results for LV HDS model on  $ee$  and  $\mu\mu$  channel in all SRs

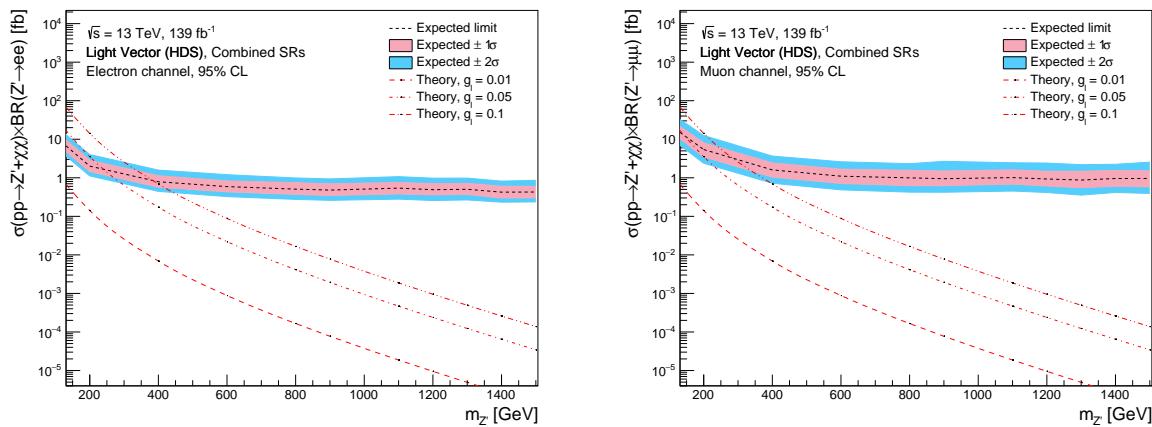


Figure H.10: Mass exclusion limits results for LV HDS model on  $ee$  and  $\mu\mu$  channel in combined SRs

### H.3 Light Vector Light Dark Sector

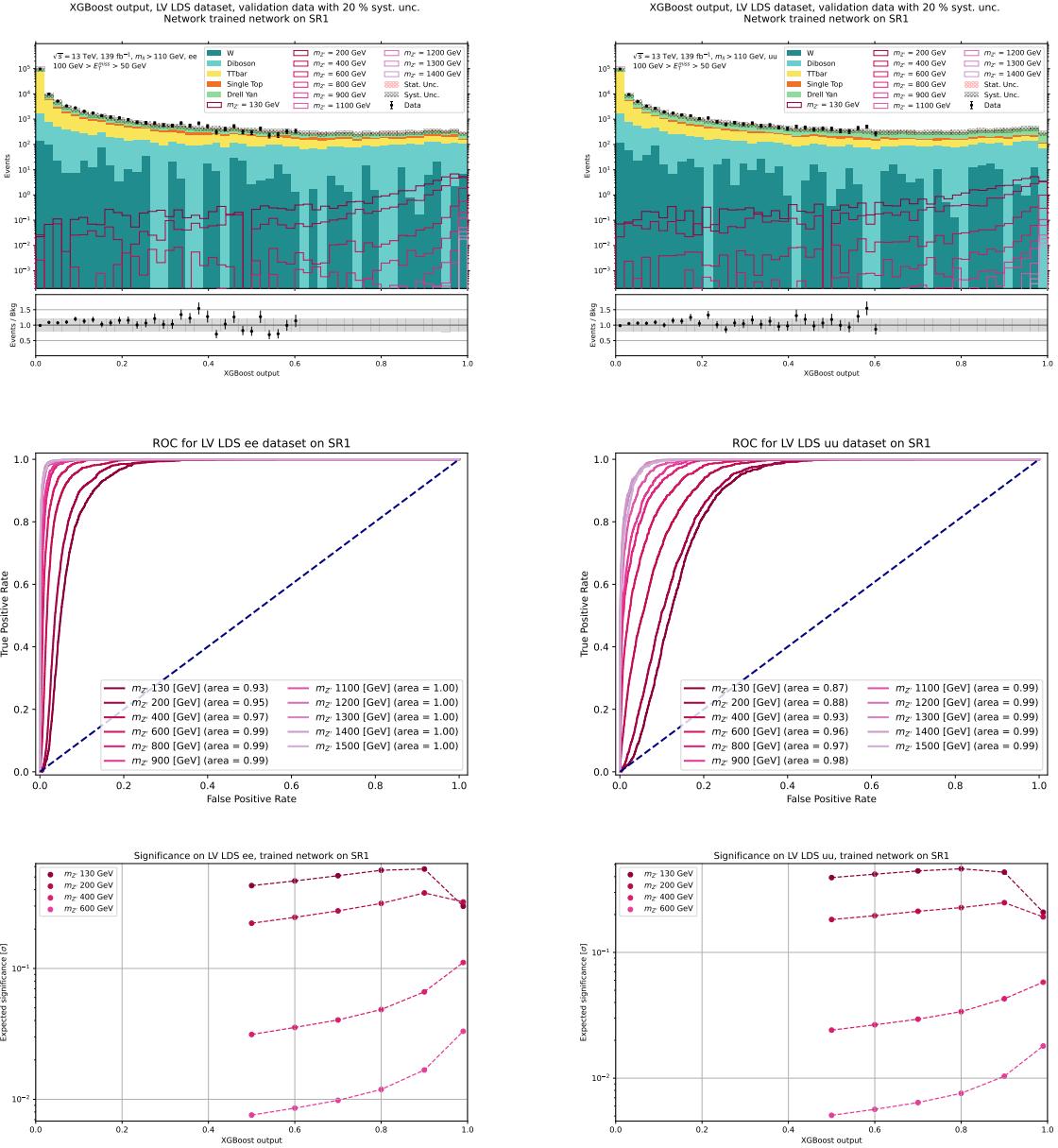
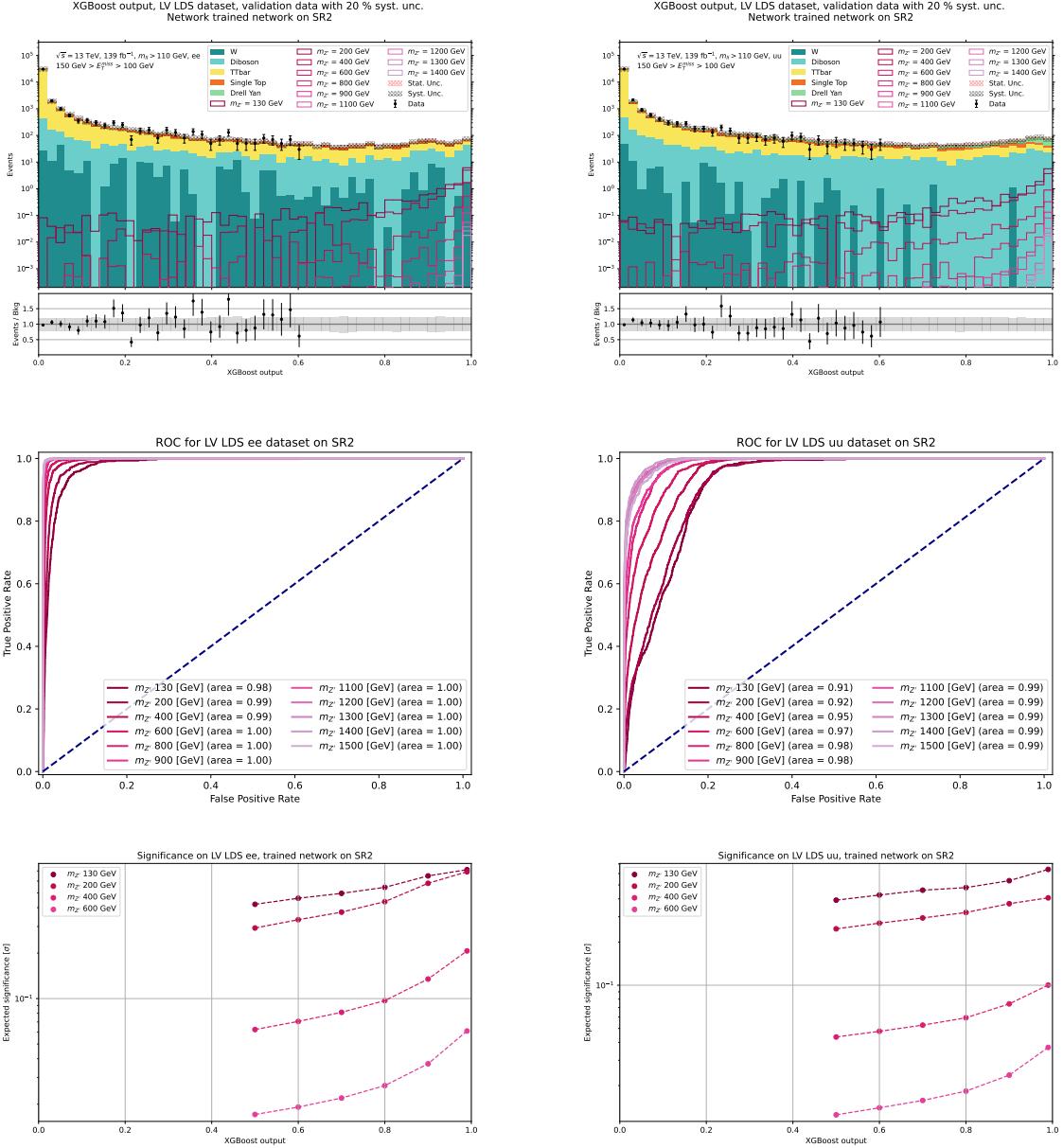


Figure H.11: XGBoost results for LV LDS model on ee and  $\mu\mu$  channel in SR1

Figure H.12: XGBoost results for LV LDS model on  $ee$  and  $\mu\mu$  channel in SR2

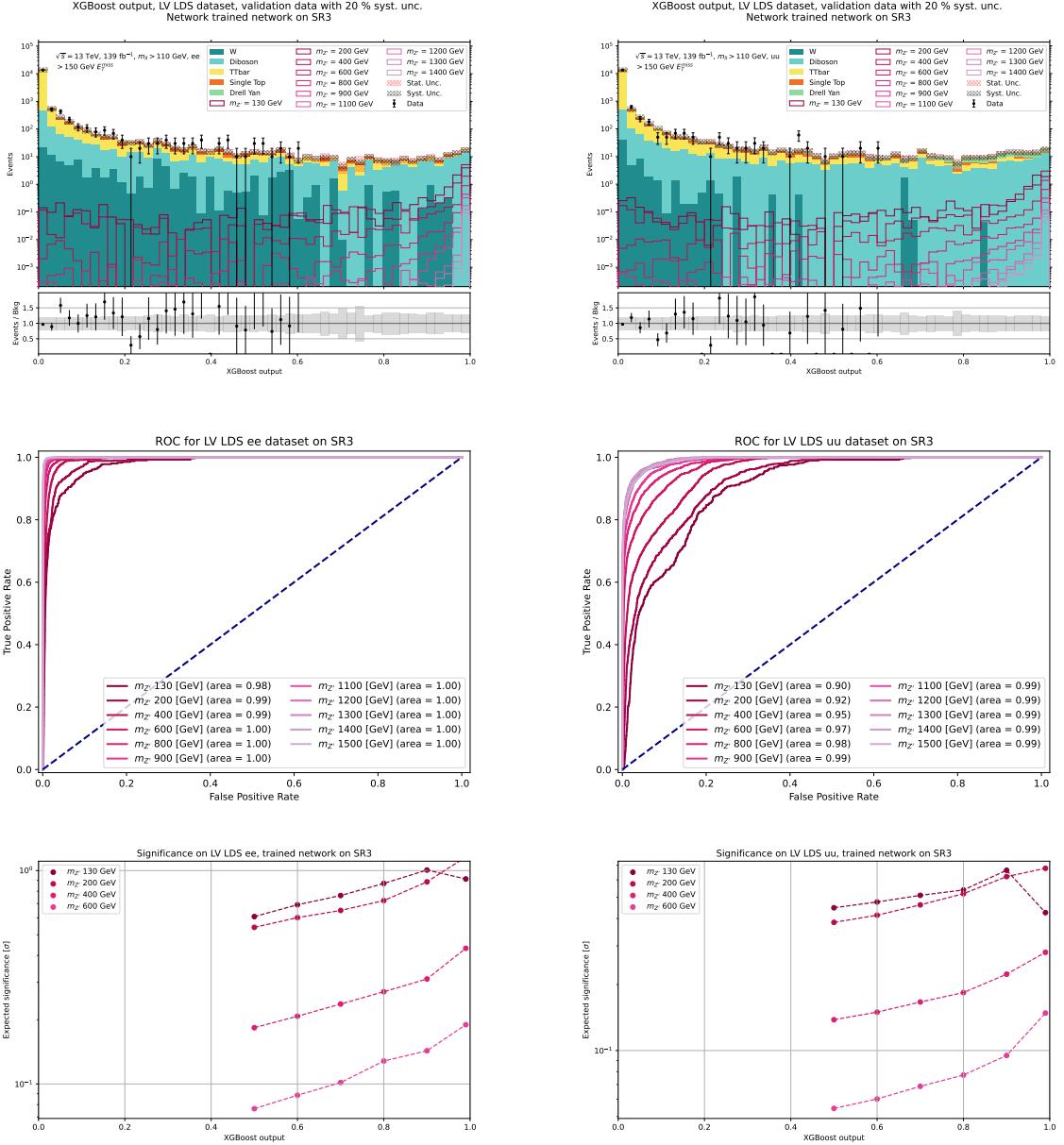


Figure H.13: XGBoost results for LV LDS model on  $ee$  and  $\mu\mu$  channel in SR3

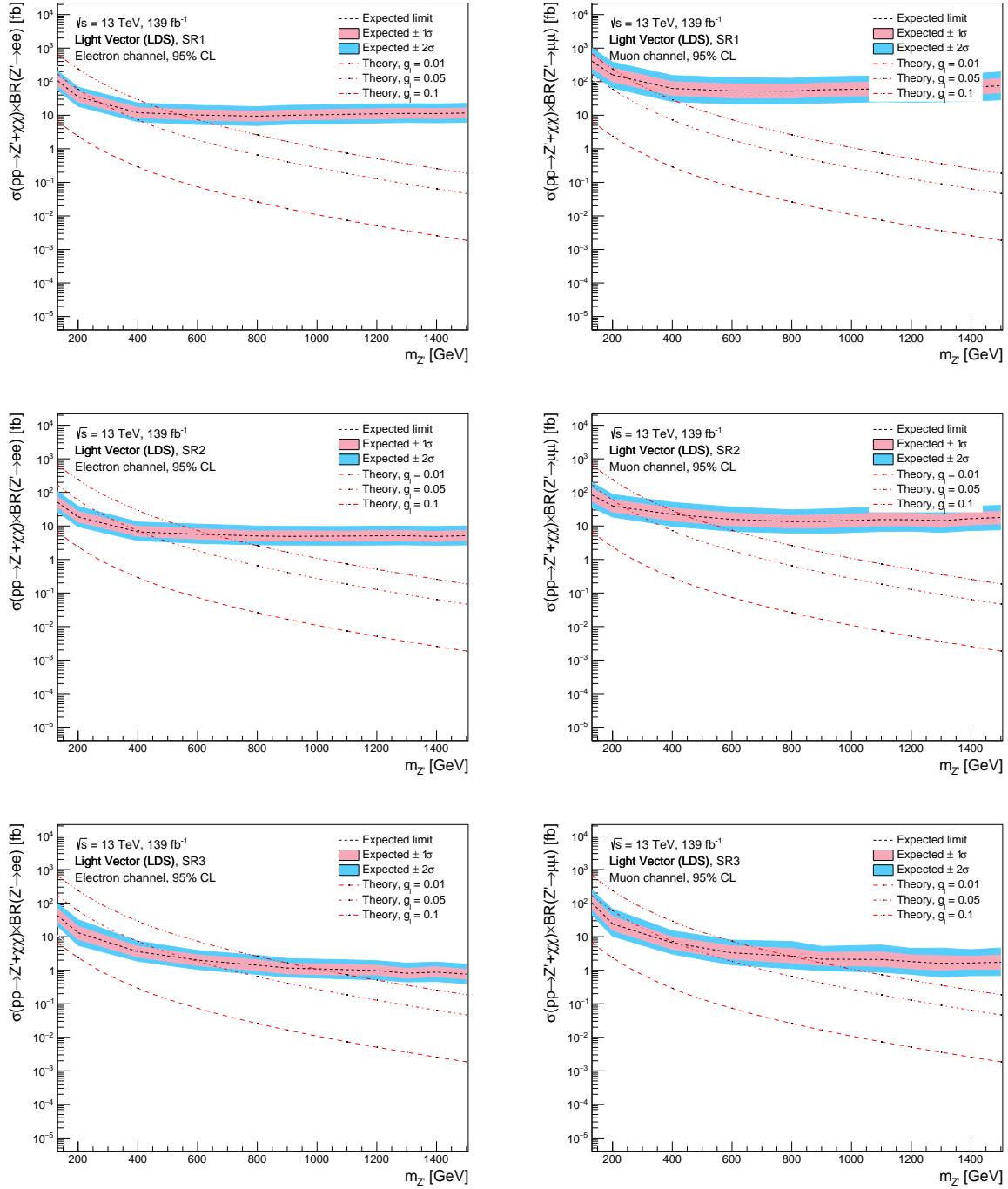


Figure H.14: Mass exclusion limits results for LV LDS model on  $ee$  and  $\mu\mu$  channel in all SRs

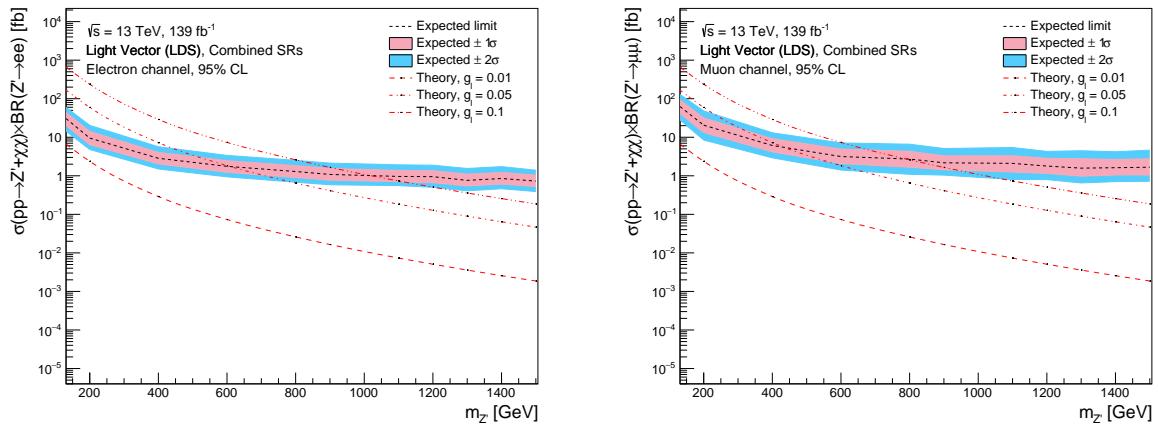


Figure H.15: Mass exclusion limits results for LV LDS model on  $ee$  and  $\mu\mu$  channel in combined SRs

## H.4 Effective Field Theory Heavy Dark Sector

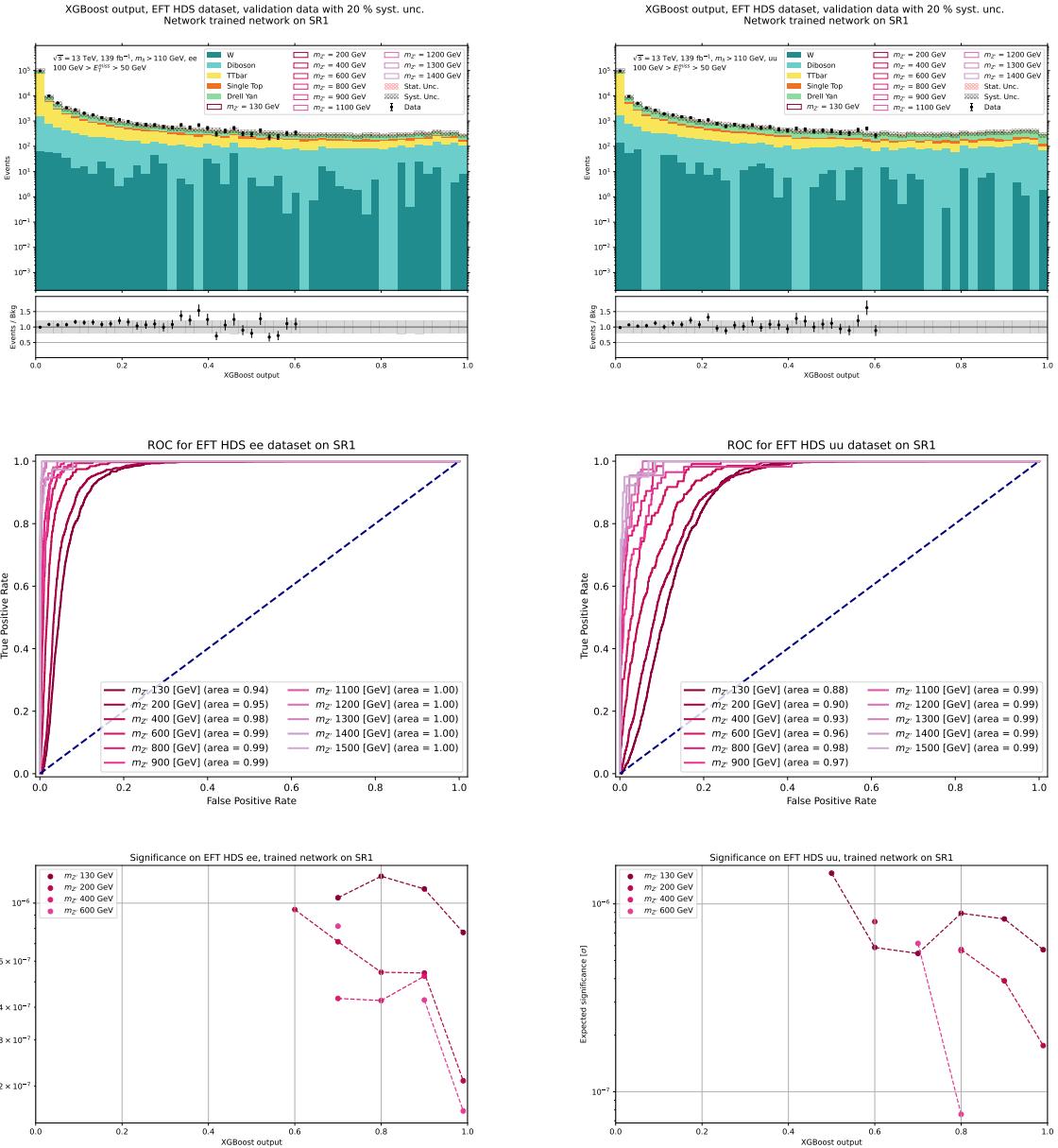


Figure H.16: XGBoost results for EFT HDS model on  $ee$  and  $\mu\mu$  channel in SR1

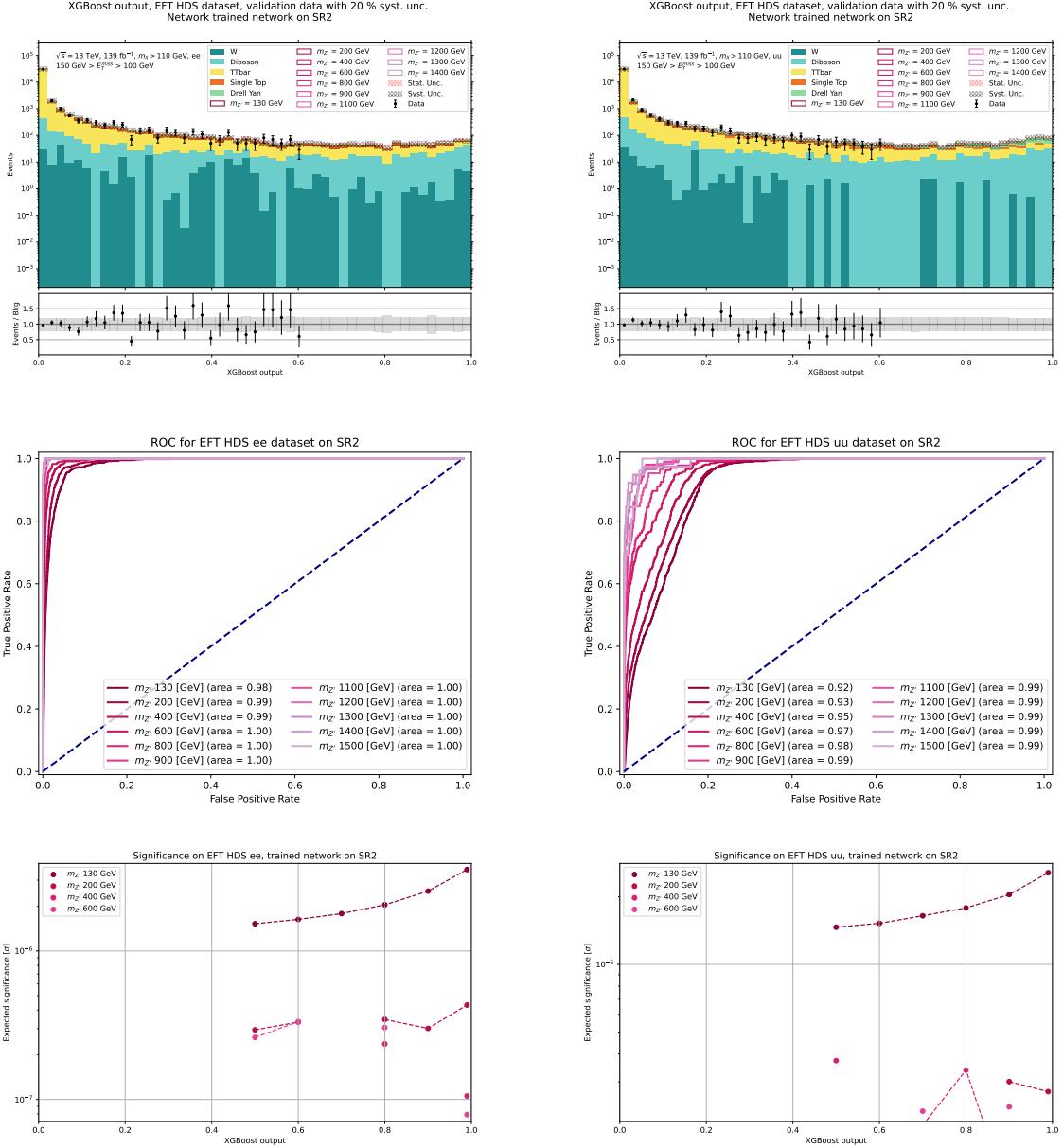
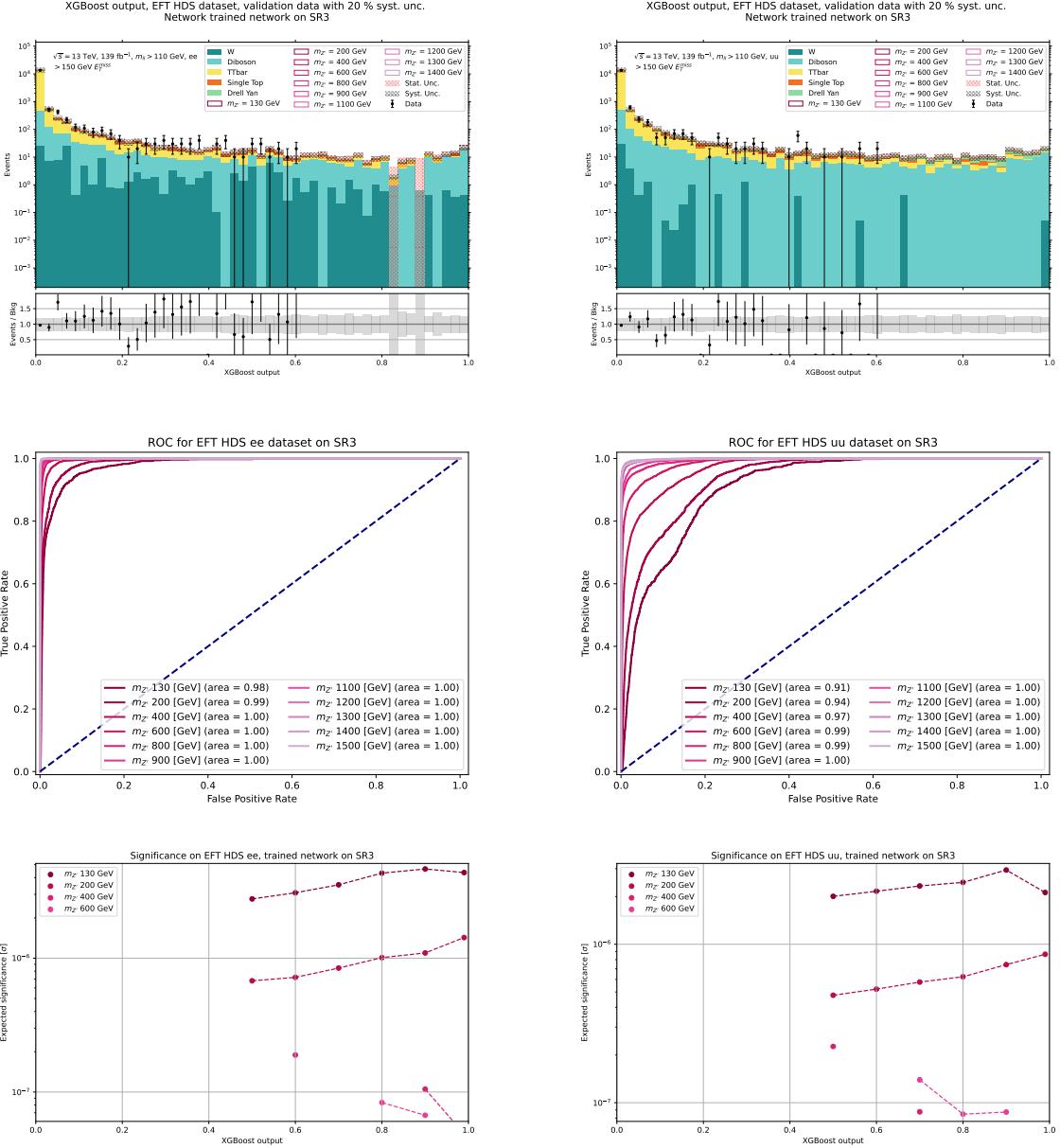


Figure H.17: XGBoost results for EFT HDS model on  $ee$  and  $\mu\mu$  channel in SR2

Figure H.18: XGBoost results for EFT HDS model on  $ee$  and  $\mu\mu$  channel in SR3

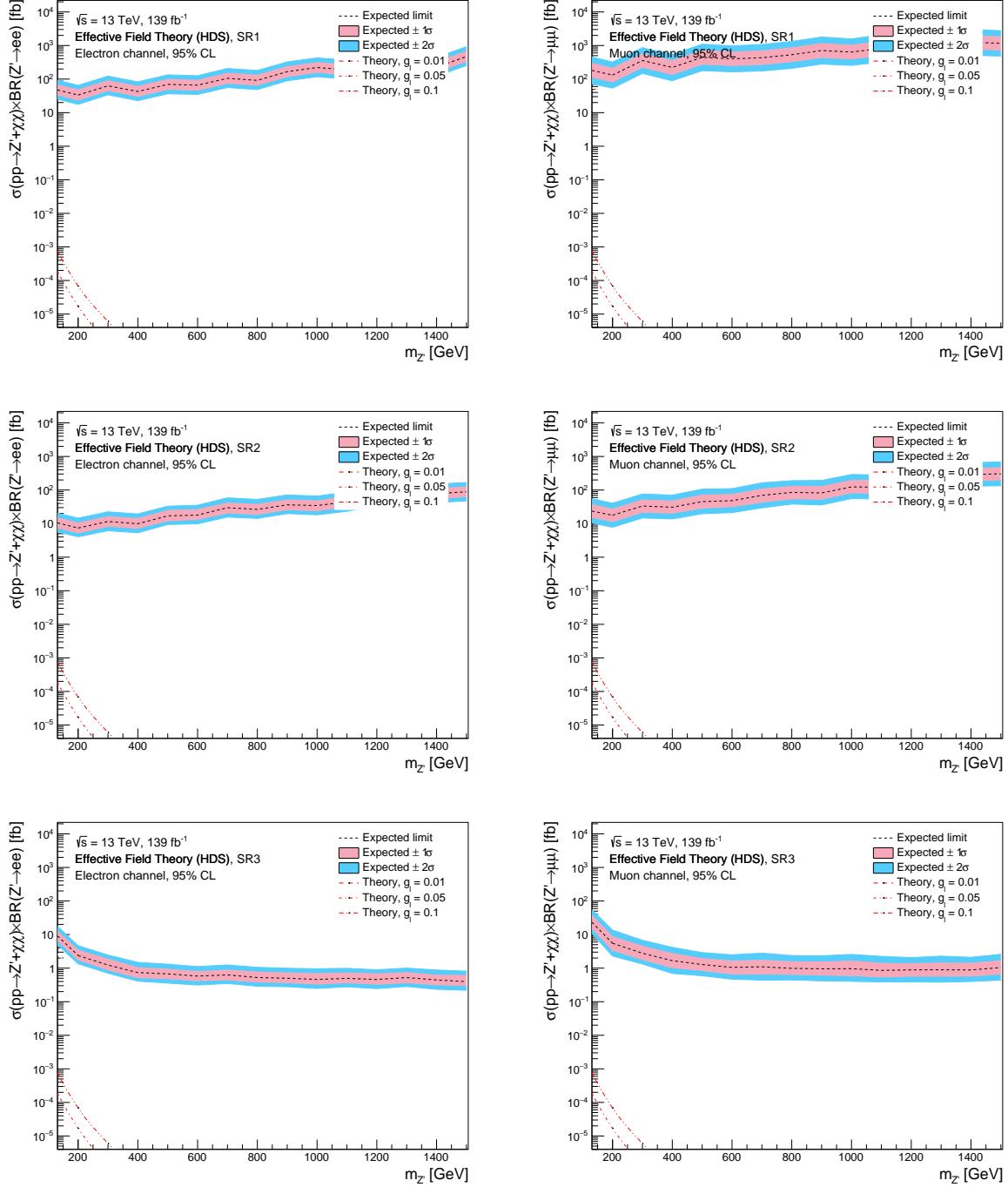


Figure H.19: Mass exclusion limits results for EFT HDS model on  $ee$  and  $\mu\mu$  channel in all SRs

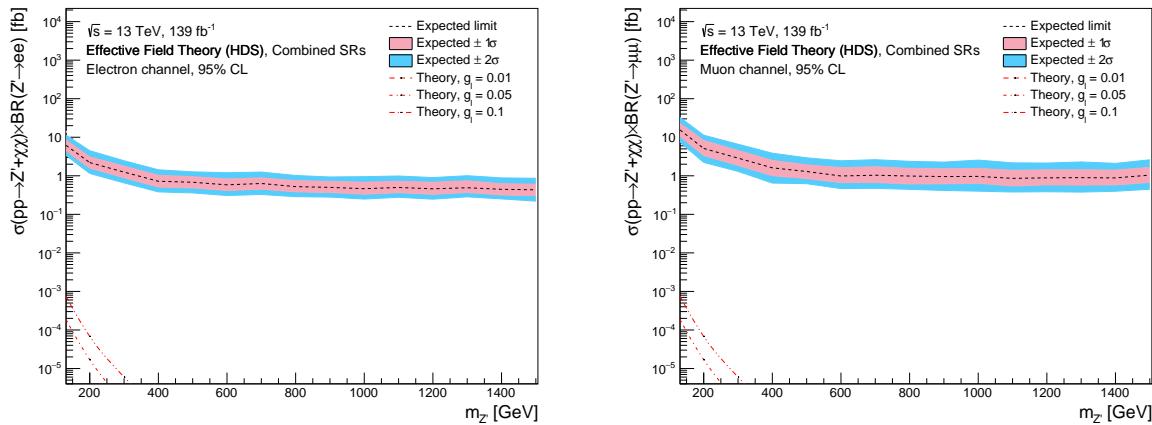


Figure H.20: Mass exclusion limits results for EFT HDS model on  $ee$  and  $\mu\mu$  channel in combined SRs

## H.5 Effective Field Theory Light Dark Sector

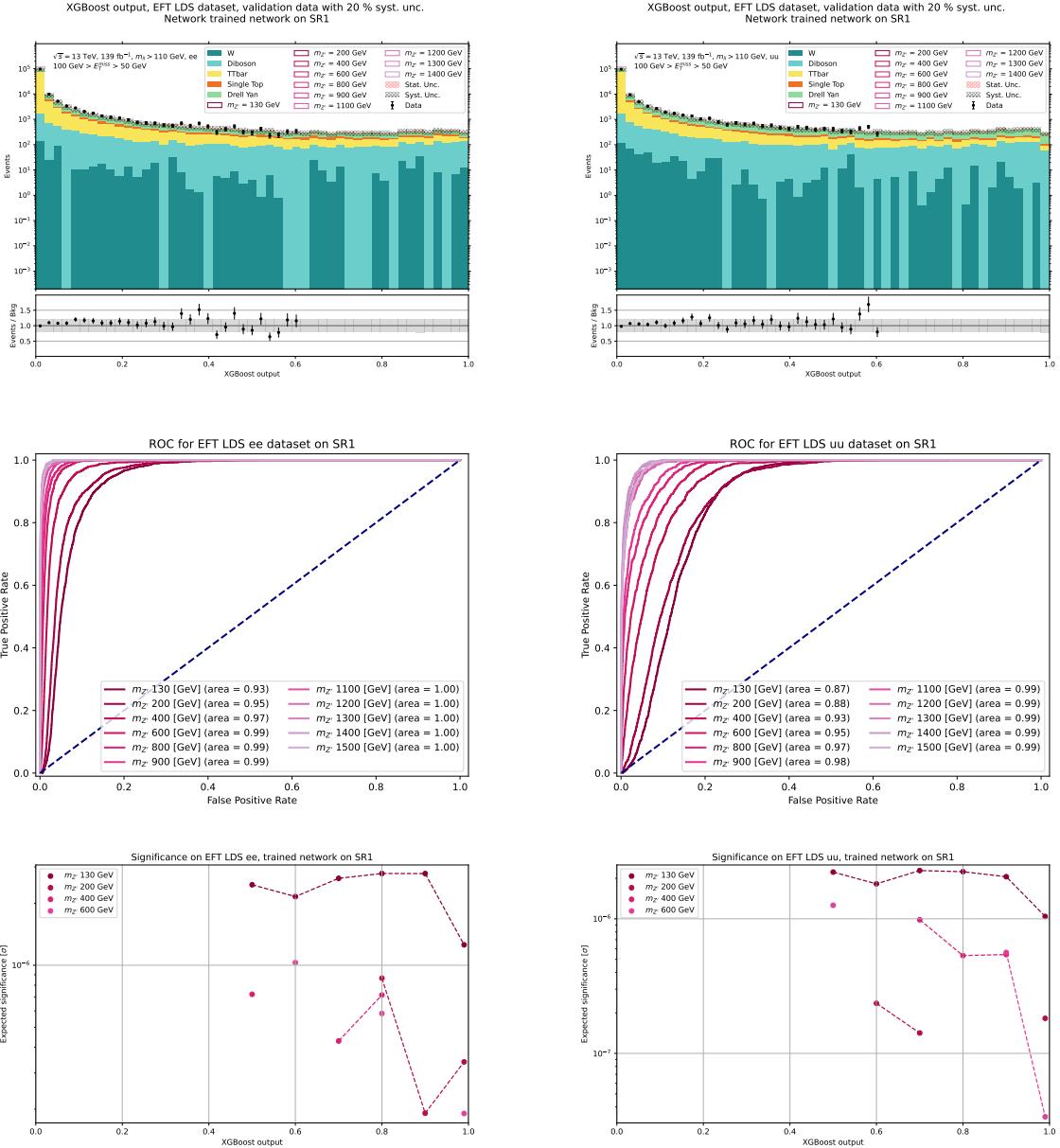


Figure H.21: XGBoost results for EFT LDS model on  $ee$  and  $\mu\mu$  channel in SR1

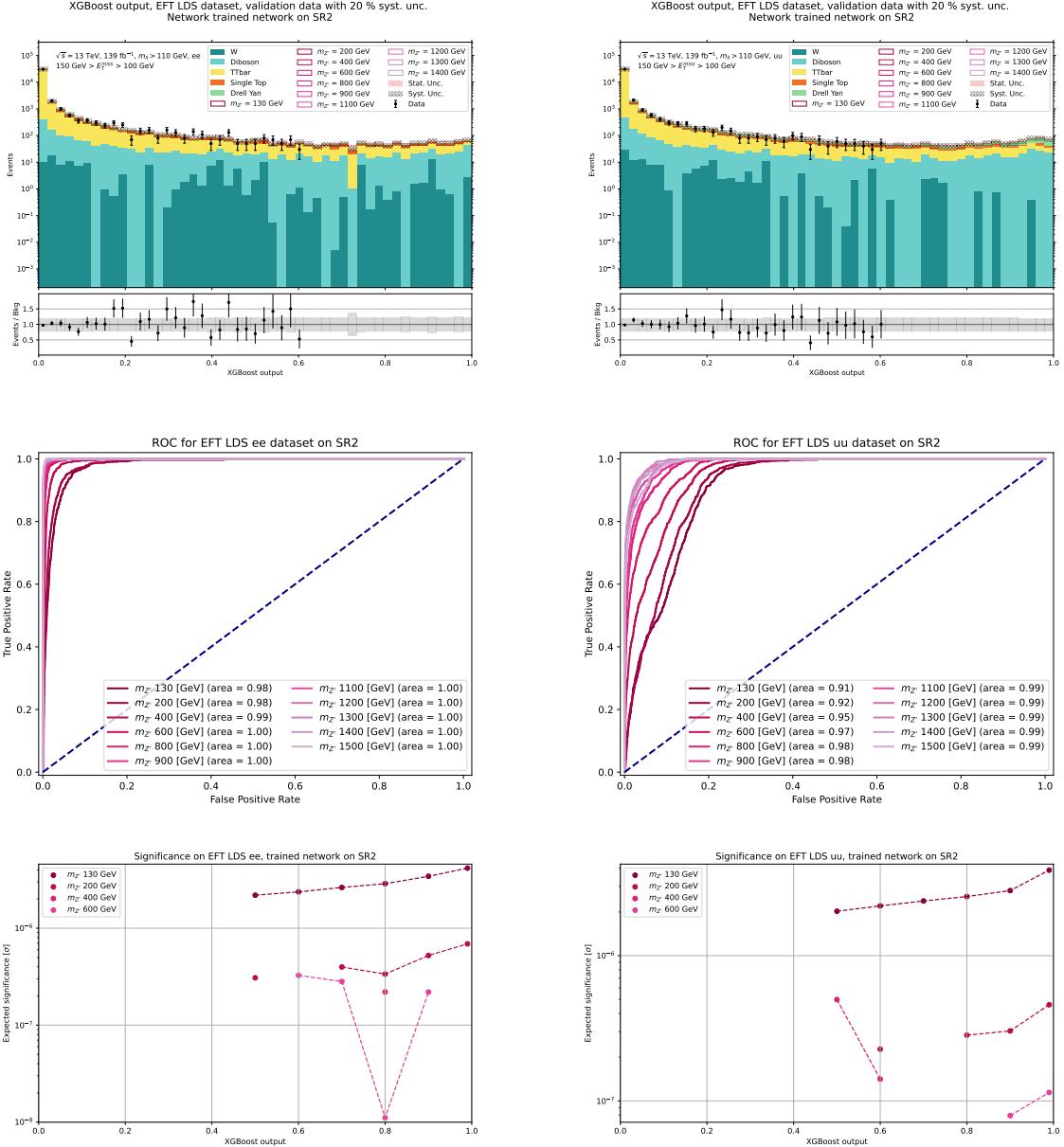


Figure H.22: XGBoost results for EFT LDS model on  $ee$  and  $\mu\mu$  channel in SR2

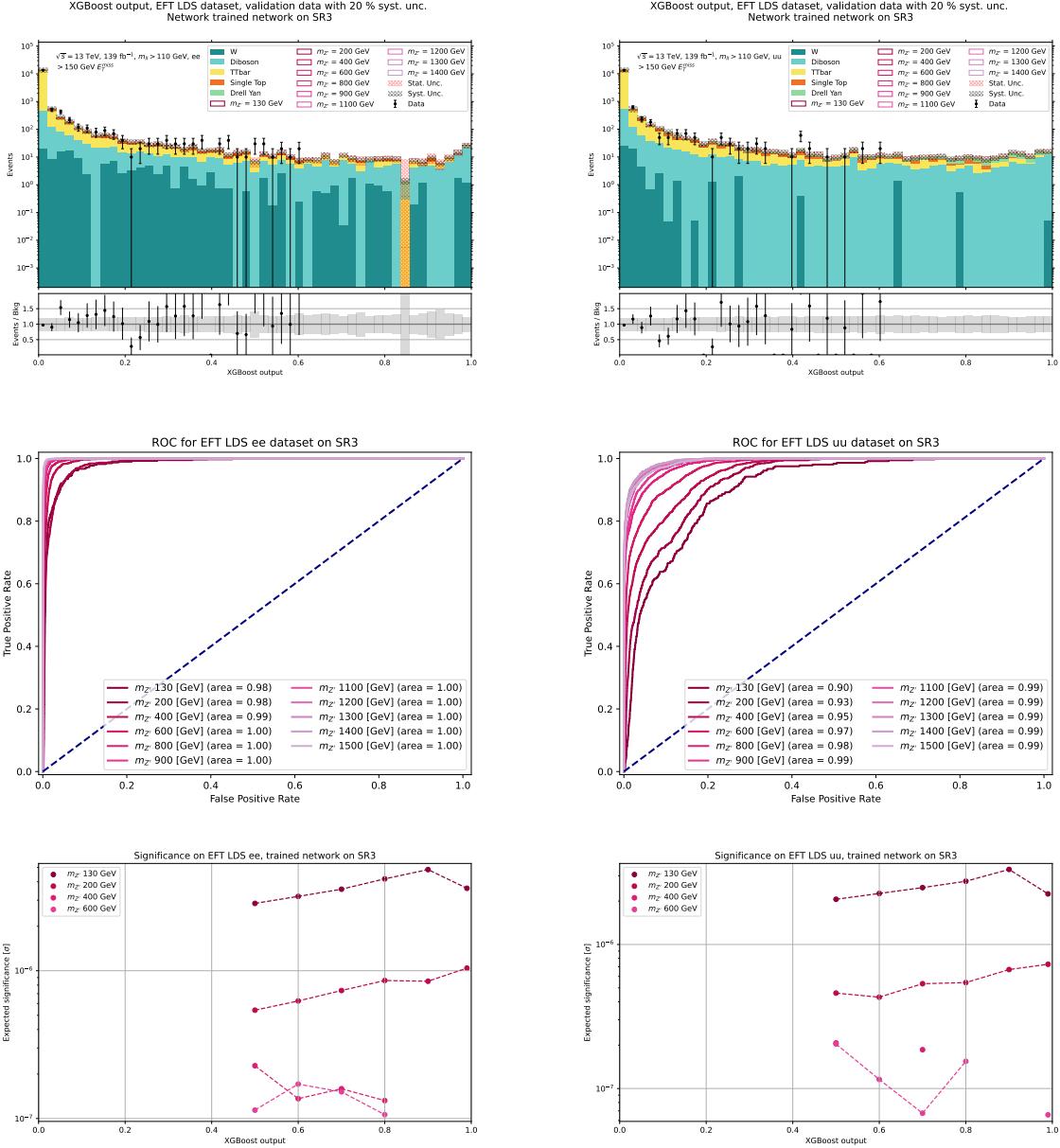


Figure H.23: XGBoost results for EFT LDS model on  $ee$  and  $\mu\mu$  channel in SR3

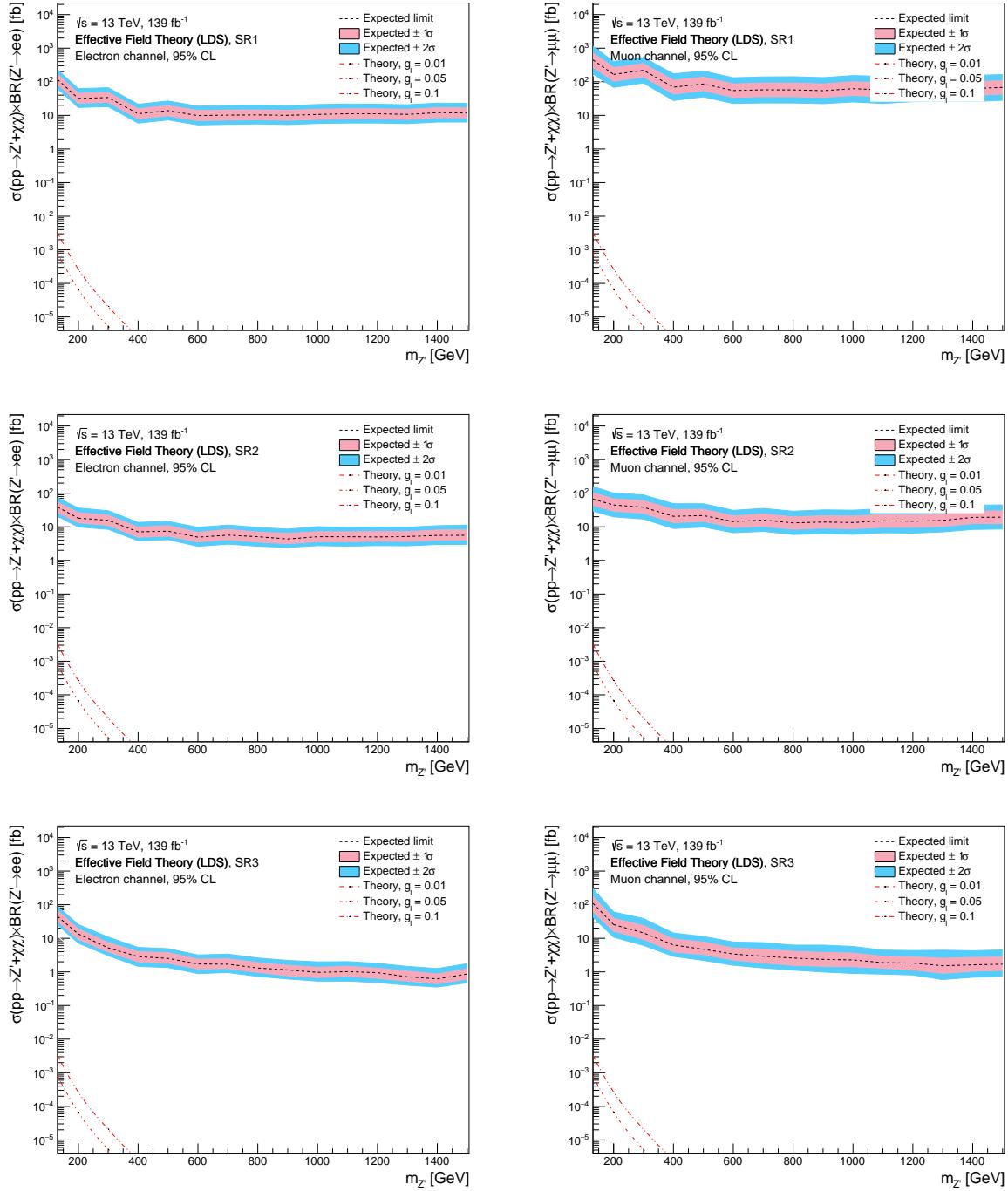


Figure H.24: Mass exclusion limits results for EFT LDS model on  $ee$  and  $\mu\mu$  channel in all SRs

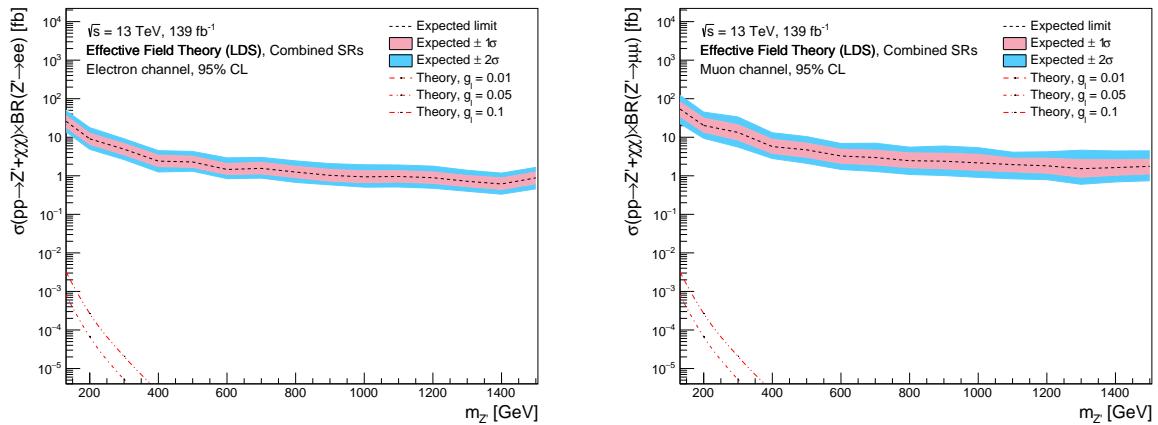


Figure H.25: Mass exclusion limits results for EFT LDS model on  $ee$  and  $\mu\mu$  channel in combined SRs

# Appendix I

## BDT of depth 30

Before conducting the final grid search for the final networks used on the results, we experimented with different hyperparameters to change. On one of grid searches we set the learning rate as  $\eta = 0.1$  as the trend showed this giving the best results with less overtraining, and  $\lambda = 10^{-5}$ . This grid search had `n_estimators`  $\in [10, 100, 500, 1000]$  and depth  $\in [3, 4, 5, 6]$ . The expected significance is shown in Figure I.1. The testing and training AUC can be seen in Figure I.2.

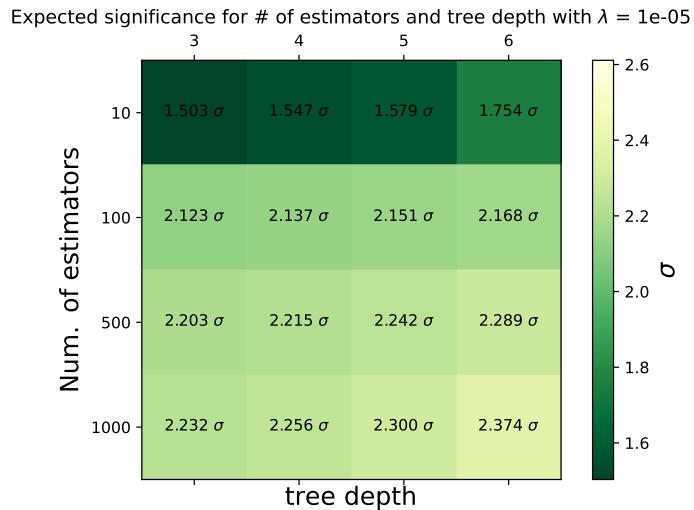


Figure I.1: Grid search expected significance when setting  $\lambda = 10^{-5}$  and  $\eta = 0.1$

The best networks (depth of 6 and 1000 estimators) feature importance plots is shown in Figure I.3.

However, as we can on Figure I.1 the expected significance does not seem to converge. Because of this, and out of curiosity we decided to keep training the networks with a

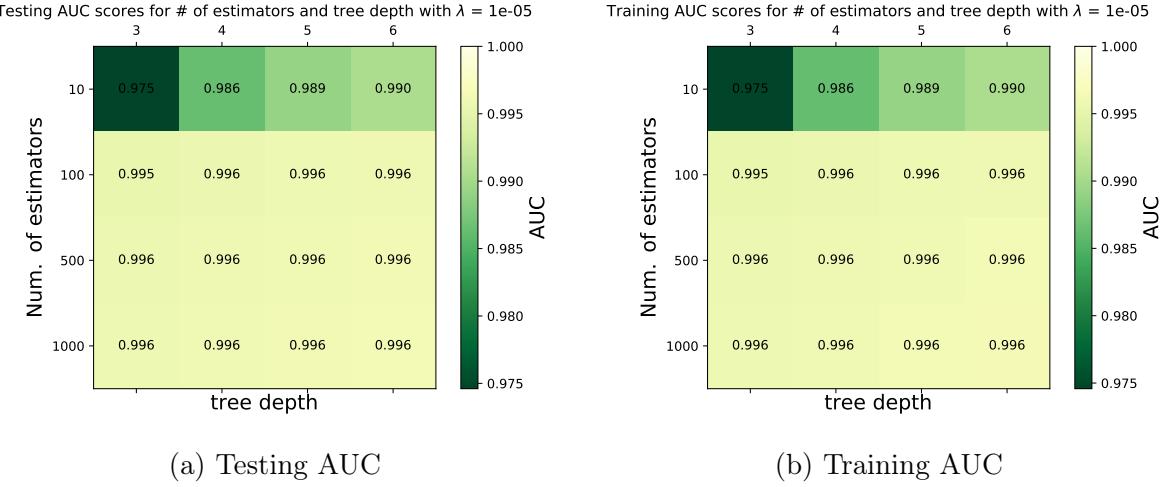
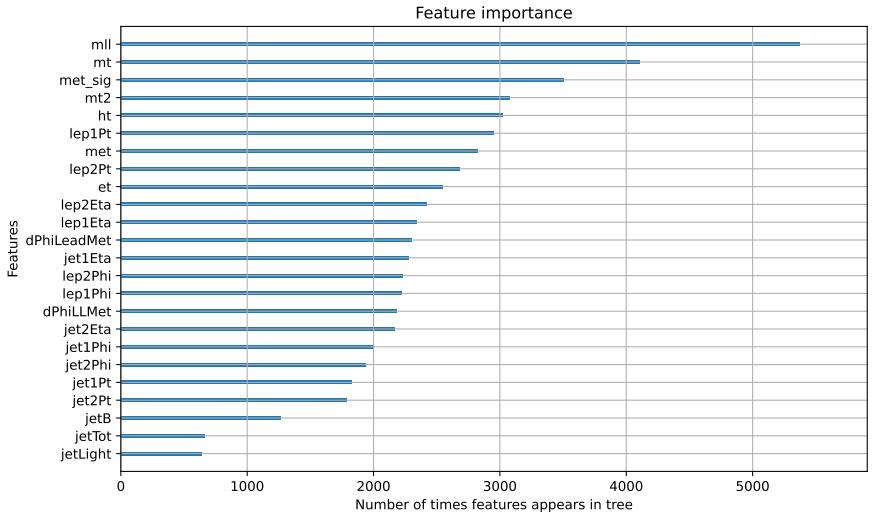


Figure I.2: Grid search AUC when setting  $\lambda = 10^{-5}$  and  $\eta = 0.1$

greater depth. The results can be shown in Figure I.4.

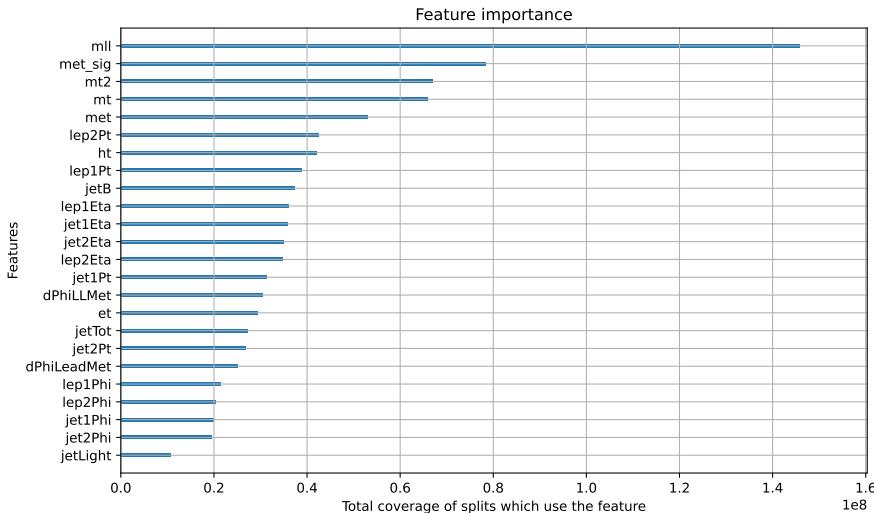
In the Figure we see that the networks expected significance does not seem to converge, and rather just keeps getting greater and greater. This is however highly radical as the convention is to normally not have a depth greater than 7, which already is radical. The reason for not having deep BDTs being that the network is highly likely to overtrain and give wrong predictions. However, this was not the case for us as seen for example in Figure I.5.

I understand however that this is controversial since we are splitting a data set, that is at best of size  $2^{27}$ , 30 times. That means that after a depth of 27 there is exactly one event pr branch. So how does a depth of 30 make sense? To help with this we could use a feature in XGBoost to see which features are most important when evaluating a signal. When testing the network trained on the FULL Z' DM data set on a DH HDS  $m_{Z'} = 130$  GeV model we get the features shown in Figure I.6 as most important.



(a) Using "weight" metric

Coverage is defined as the number of samples affected by the split



(b) Using "coverage" metric

Figure I.3: Feature importance of depth 6 network trained on FULL Z' DM data set when testing it on DH HDS  $m_{Z'} = 130$  GeV model.

As we can see these features vary a lot depending on which metric we use to evaluate the importance. When using the "coverage" metric, which as stated is defined as the number of samples affected by the split, we get the features we physically expect to be important when trying to single out a DM model. And this metric is arguably the one we need to use to define what features are important. Since the more samples a feature split, the more powerful it is to separate signal from background.

We can see however that when we use "weight" as a metric, which is the XGBoost

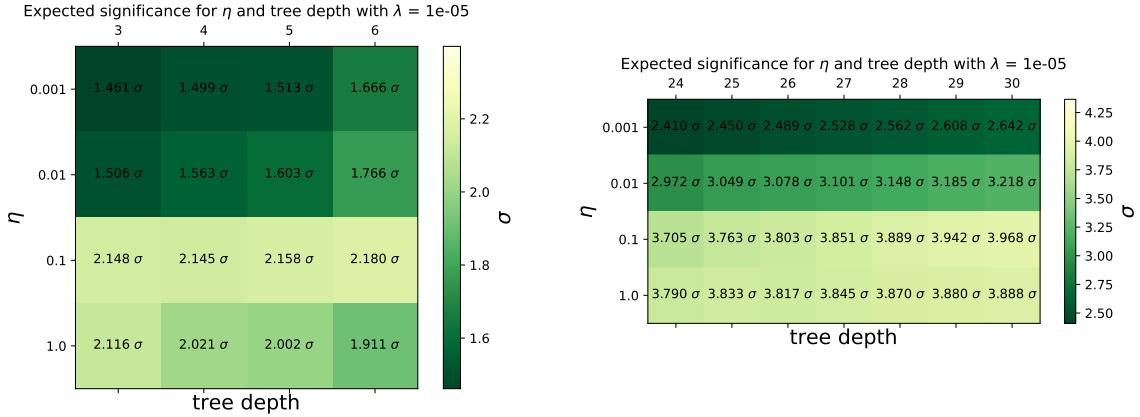
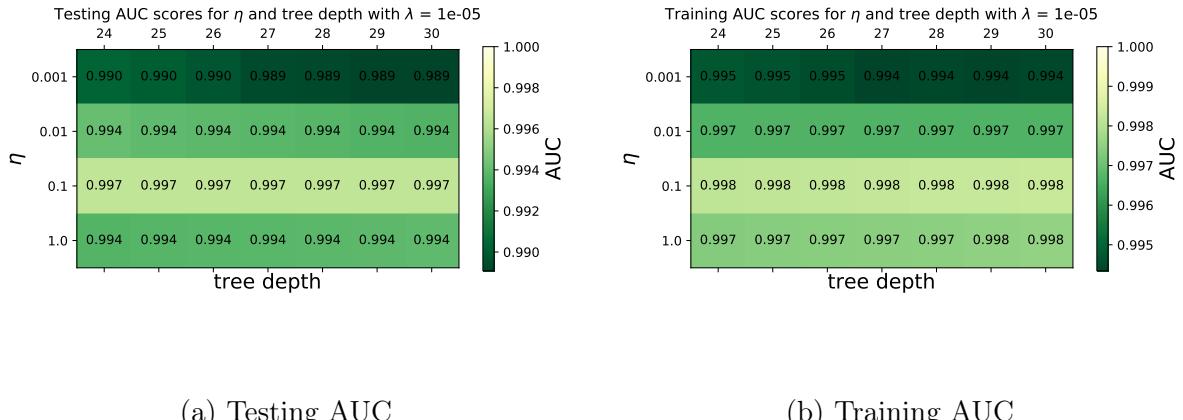


Figure I.4: Grid search expected significance going to a depth of up to 30



(a) Testing AUC

(b) Training AUC

Figure I.5: Grid search AUC going to a depth of up to 30

standard metric, we get completely unexpected features that we physically don't expect to be important when trying to single out a DM model. But as described by the metric, the "weight" is the number of times a feature appears in a tree. Which might explain that the reason the pseudorapidity and  $\phi$  range so high on this list, is simply because the tree is struggling to find a pattern here and is trying extra hard to single out DM from SM.

To showcase the difference in signal recognition between the monstrous 30 depth BDT to the more sensible 6 depth BDT, I again tested the networks on the good old DH HDS  $m_{Z'} = 130$  GeV model. The results as well as their expected significance can be seen below.

The difference is extreme, when looking at the monster of depth 30 we can get an expected significance of  $1.2 \sigma$  (without uncertainties) on our model of max 15 events, only

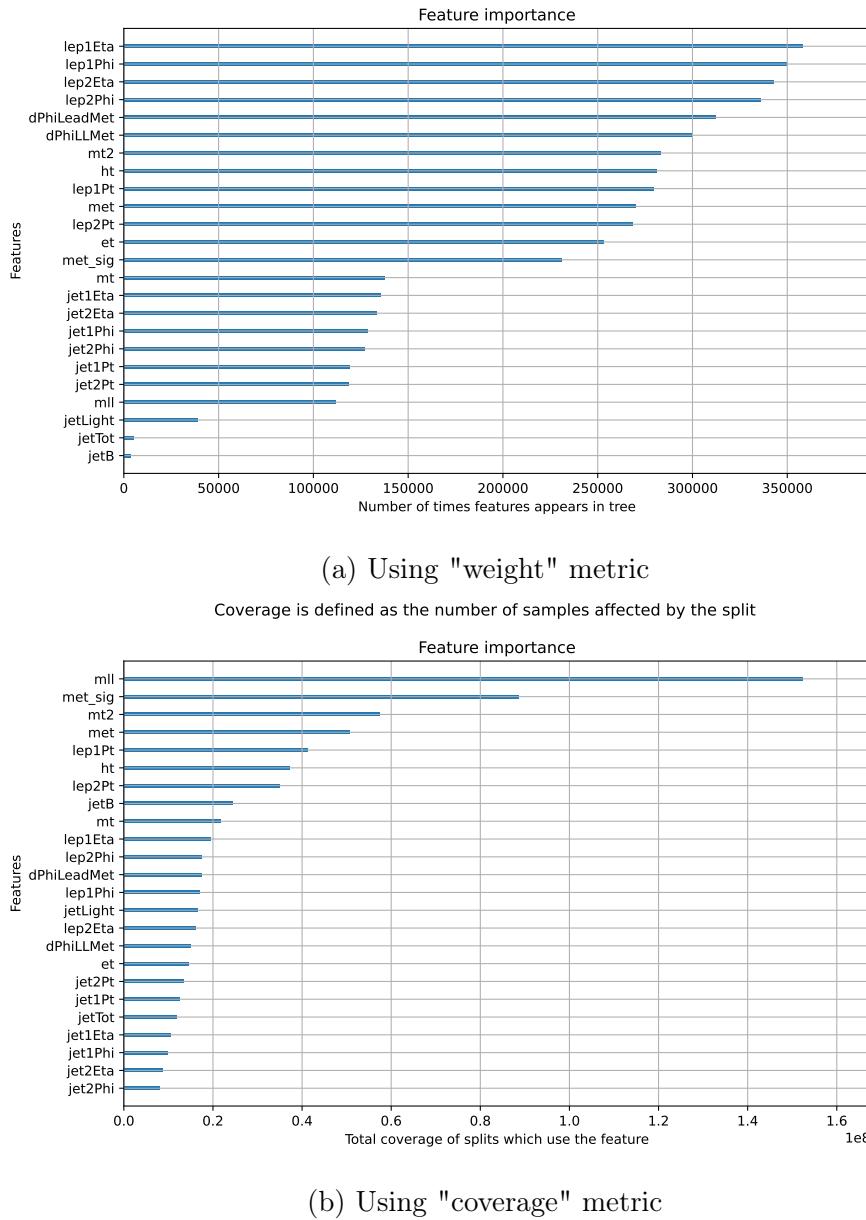


Figure I.6: Feature importance of depth 30 network trained on FULL Z' DM data set when testing it on DH HDS  $m_{Z'} = 130$  GeV model.

having made a cut of 50 GeV on the missing transverse energy. We can however see that the data and background do not agree to the same degree of the network with depth 6. Using purely statistical uncertainty and assuming a systematic uncertainty of 30%, we see that a few data points do not agree with the MC background. These data points are points the network classified as signal, so if we completely trusted the network this would be a hint of new physics! However, this is the last thing we should assume, and rather take this as a hint that the network is doing something fishy.

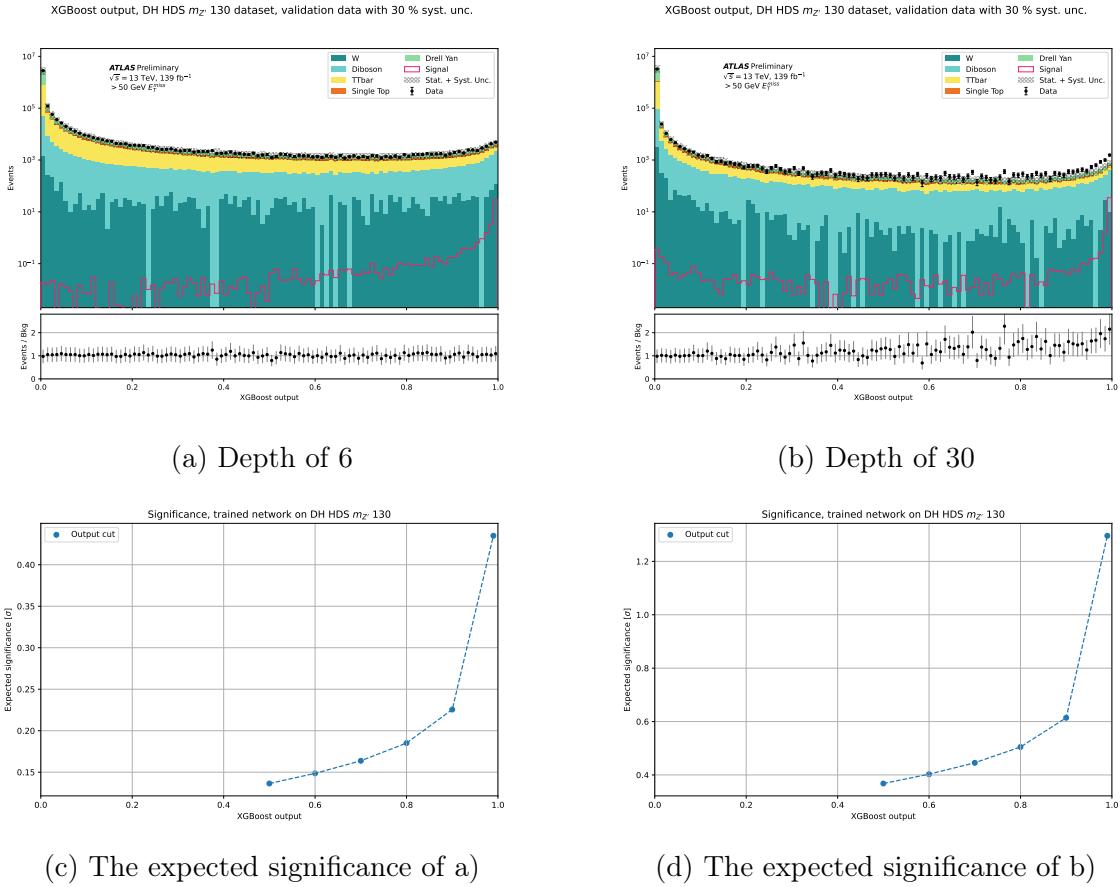


Figure I.7: Comparison of the network performance when having a depth of 6 and 30. Figure a) and b) show the validation data of both cases, c) and d) show the expected significance of the validation plots when making a cut on the output.

If I had access to XGBoost with built GPU support, I would increase the number of estimators even more to check if this increases the significance while still having a depth of maximum 6. However, as of now this is not possible. As the weighting method explained in the previous section was not included here, we will drop going to a tree depth of 30, and have a maximum of 6.

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