732A97 Multivariate Statistics Lab 1

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Question 1: Describing individual variables

Consider the data set in the T1-9.dat file, National track records for women. For 55 different countries we have the national records for 7 variables (100, 200, 400, 800, 1500, 3000m and marathon). Use R to do the following analyses.

input

a) Describe the 7 variables with mean values, standard deviations e.t.c

```
apply(trackrcs[,-1], 2, FUN = function(cl){
   c("mean"=mean(cl),
     "median"=median(cl),
     "sd"=sd(cl),
     "95% quantile"=quantile(cl, probs = 0.975, names = FALSE),
     "5% quantile"=quantile(cl, probs = 0.025, names = FALSE),
     "max"=max(cl),
     "min"=min(cl))
}) %>% t()
```

```
##
                  mean median
                                        sd 95% quantile 5% quantile
## x100m
             11.357778 11.325 0.39410116
                                               12.29875
                                                           10.74300 12.52
## x200m
             23.118519 22.980 0.92902547
                                               25.33625
                                                           21.76200 25.91
## x400m
             51.989074 51.645 2.59720188
                                               56.29075
                                                           48.07450 61.65
                                                                      2.29
## x800m
              2.022407
                         2.005 0.08687304
                                                2.26700
                                                            1.91325
## x1500m
              4.189444
                         4.100 0.27236502
                                                4.75500
                                                            3.87975
                                                                      5.42
## x3000m
              9.080741
                         8.845 0.81532689
                                               10.81075
                                                            8.36000 13.12
## marathon 153.619259 148.430 16.43989508
                                              205.58625
                                                          138.76900 221.14
##
              min
## x100m
             10.49
## x200m
             21.34
             47.60
## x400m
## x800m
              1.89
## x1500m
              3.84
## x3000m
              8.10
## marathon 135.25
```

b) Illustrate the variables with different graphs (explore what plotting possibilities R has). Make sure that the graphs look attractive (it is absolutely necessary to look at the labels, font sizes, point types). Are there any apparent extreme values? Do the variables seem normally distributed? Plot the best fitting (match the mean and standard deviation, i.e. method of moments) Gaussian density curve on the datas histogram. For the last part you may be interested in the hist() and density() functions.

```
j=0; lapply(trackrcs2, FUN = function(i){
    j <<- j+1
    hist(i, main = colnames(trackrcs2)[j], xlab=colnames(trackrcs2)[j])
})</pre>
```

Question 2: Relationships between the variables

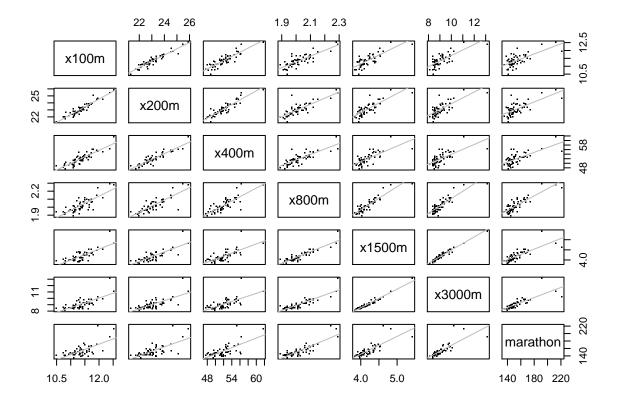
a) Compute the covariance and correlation matrices for the 7 variables. Is there any apparent structure in them? Save these matrices for future use.

```
C <- cov((trackrcs)[,-1])</pre>
corr_m <- cor((trackrcs)[,-1])</pre>
##
              x100m
                       x200m
                                x400m
                                          x800m
                                                  x1500m
## x100m
         ## x200m
         ## x400m
         0.89129602 2.1928363 6.7454576 0.181807932 0.50917683
## x800m
         ## x1500m
         ## x3000m
## marathon 4.33417757 10.3849876 28.9037314 1.219654647 3.53983732
##
              x3000m
                     marathon
## x100m
          0.23388281
                     4.334178
## x200m
          0.55435017 10.384988
## x400m
          1.42681579
                    28.903731
## x800m
          0.06137932
                     1.219655
## x1500m
          0.21615514
                     3.539837
## x3000m
          0.66475793 10.706091
## marathon 10.70609113 270.270150
corr_m
##
             x100m
                     x200m
                              x400m
                                      x800m
                                             x1500m
                                                      x3000m
## x100m
         1.0000000 0.9410886 0.8707802 0.8091758 0.7815510 0.7278784
         0.9410886 1.0000000 0.9088096 0.8198258 0.8013282 0.7318546
## x200m
## x400m
         0.8707802 0.9088096 1.0000000 0.8057904 0.7197996 0.6737991
         0.8091758 0.8198258 0.8057904 1.0000000 0.9050509 0.8665732
## x800m
## x1500m
         0.7815510 0.8013282 0.7197996 0.9050509 1.0000000 0.9733801
## x3000m
         0.7278784 0.7318546 0.6737991 0.8665732 0.9733801 1.0000000
## marathon 0.6689597 0.6799537 0.6769384 0.8539900 0.7905565 0.7987302
##
          marathon
## x100m
         0.6689597
## x200m
         0.6799537
## x400m
         0.6769384
## x800m
         0.8539900
## x1500m
          0.7905565
## x3000m
          0.7987302
## marathon 1.0000000
```

Both matrices are symmetric. The correlation matrix has ones on the main diagonal.

b) Generate and study the scatterplots between each pair of variables. Any extreme values?

```
pairs(trackrcs[,-1], pch = ".", cex = 1.5, panel = function(x, y, ...){
   points(x, y, ...)
   abline(lm(y ~ x), col = "grey") })
```



The scatterplot matrix tells us that "marathon" is quite an outlier.

c) Explore what other plotting possibilities R offers for multivariate data. Present other (at least two) graphs that you find interesting with respect to this data set.

chernoff face

```
library(aplpack)
faces(trackrcs2)
```

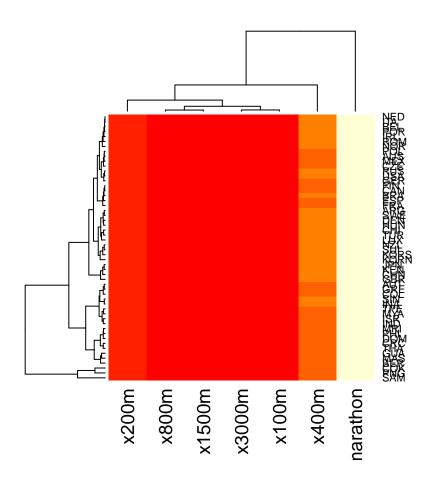


```
## effect of variables:
   modified item
                       Var
   "height of face
                     " "x100m"
##
##
  "width of face
                    " "x200m"
   "structure of face" "x400m"
##
   "height of mouth " "x800m"
##
                     " "x1500m"
  "width of mouth
##
##
  "smiling
                     " "x3000m"
                     " "marathon"
##
  "height of eyes
                   " "x100m"
## "width of eyes
                    " "x200m"
##
  "height of hair
                    " "x400m"
## "width of hair
                    " "x800m"
## "style of hair
                   " "x1500m"
## "height of nose
                    " "x3000m"
##
  "width of nose
##
  "width of ear
                    " "marathon"
                    " "x100m"
   "height of ear
##
```

A stars plot is not very useful. We can tell from literature that it is also outdated.

heatmaps

```
heatmap(x=as.matrix(trackrcs2))
```



Question 3: Examining for extreme values

a) Look at the plots (esp. scatterplots) generated in the previous question. Which 3-4 countries appear most extreme? Why do you consider them extreme?

The 3 countries that seem most extreme are Brazil, Russia and the United States.

b) Compute the squared Euclidean distance (i.e. r=2) of the observation from the sample mean for all 55 countries using R's matrix operations. First center the raw data by the means to get (x arrow - x bar) for each country. Then do a calculation with matrices that will result in a matrix that has on its diagonal the requested squared distance for each country. Copy this diagonal to a vector and report on the five most extreme countries. In this questions you MAY NOT use any loops.

```
x bar = apply(trackrcs2,1,mean)
d0 = as.matrix(trackrcs2-x_bar); dim(d0)
## [1] 54 7
deviation = sqrt( d0%*%t(d0) ); dim(deviation)
## [1] 54 54
diagonal_vector <- diag(deviation)</pre>
deviation_countries <-
  cbind.data.frame(countries = as.vector(trackrcs[,1]),diagonal_vector)
deviation_countries_ordered <-
  deviation_countries[order(-deviation_countries$diagonal_vector), ]
deviation countries ordered[1:5,]
##
       countries diagonal_vector
## PNG
             PNG
                        193.0557
## COK
             COK
                         185.0669
## SAM
             SAM
                        165.7015
## BER
             BER
                         151.3534
## GUA
             GUA
                         148.7706
```

The five most extreme countries are PNG, COK, SAM, BER, GUA.

c)

```
V <- diag(apply(trackrcs2,2,var))
d_sq_v <- d0%*%solve(V)%*%t(d0)
diagonal_vector2 <- diag(d_sq_v)
deviation_countries2 <-
    cbind.data.frame(countries = as.vector(trackrcs[,1]),diagonal_vector2)
deviation_countries_ordered2 <-
    deviation_countries2[order(-deviation_countries2$diagonal_vector2), ]

deviation_countries_ordered2[1:5,]</pre>
```

```
##
       countries diagonal_vector2
## COK
             COK
                          302349.9
## PNG
             PNG
                          302325.3
## SAM
             SAM
                          256366.7
## GUA
             GUA
                          213229.3
## BER
             BER
                          211849.1
```

Except Great Britain, still the top five most extreme countries are the same and they are COK, PNG, SAM, GUA, BER

d) Compute the Mahalanobis distance, which countries are most extreme now?

```
d_sq_m <- d0%*%solve(C)%*%t(d0)
diagonal_vector3 <- diag(d_sq_m)
deviation_countries3 <-
    cbind.data.frame(countries = as.vector(trackrcs[,1]),diagonal_vector3)
deviation_countries_ordered3 <-
    deviation_countries[order(-deviation_countries3$diagonal_vector3), ]

deviation_countries_ordered3[1:5,]</pre>
```

```
##
       countries diagonal_vector
## COK
                         185.0669
             COK
## PNG
             PNG
                         193.0557
## SAM
             SAM
                         165.7015
## GUA
             GUA
                         148.7706
## BER
             BER
                         151.3534
```

Still the top five most extreme countries are the same and they are COK, PNG, SAM, GUA, BER

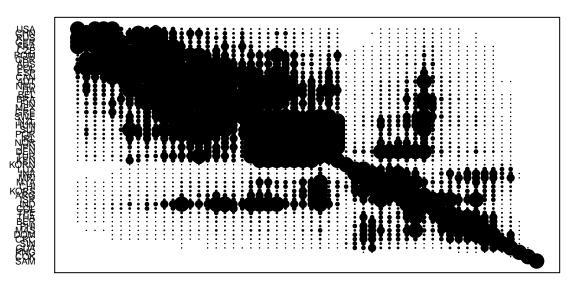
e) Compare the results in b){d). Some of the countries are in the upper end with all the measures and perhaps they can be classified as extreme. Discuss this. But also notice the different measures give rather different results (how does Sweden behave?). Summarize this graphically. Produce Czekanowski's diagram using e.g. the RMaCzek package. In case of problems please describe them.

Sweden

Czekanowski's diagram

```
library(RMaCzek)
x<-czek_matrix(trackrcs2, n_classes = 7)
plot(x)
plot.czek_matrix(x)</pre>
```

Czekanowski's diagram



REAL TO SEA STANDARD STANDARD