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# Index

Bold face page numbers are used to indicate pages with important information about the entry, e.g. the precise definition of the term or user-defined predicate, while page numbers in normal type indicate a textual reference.

- !, 362–365
- ::, 32
- [X|Y], 188
- [], 188
- , 144
- , 135, 141
- ⇒, 141
- ⇒\*, 313
- ≡, 21
- [ ], 118, 303, 343
- ↔, 14
- [ ], 101, 118, 303, 343
- ≠, 102
- ∧, 13
- | |, 60
- ( -> ; ), 230, 365
- =..., 328
- %, 216
- , 12, 134, 188
  
- accumulator, 197, 210, 329
- Ackermann's function, 410
- addkey, 194, 200
- alldifferent, 110, 190, 256, 268, 269, 271
- alldifferent.neq, 190, 254
- anonymous variable (-), 188
- answer, 141, 142, 147
  - generated, 400
  - qualified, 316
- answer redundant, 223, 225, 229
- append, 189, 317
- arc consistency, 92, 92–96
- arc\_consistent, 94
- arc\_consistent\_primitive, 94, 110
- arc\_solv, 95
- arg, 328
- arithmetic, 299, 326
- arithmetic constraint solver
  - Gauss-Jordan, 20
  - incremental, 376
  - incremental Gauss-Jordan, 353
  - simplex, 71
- arithmetic CSP, 98
- artificial variable, 69
- ask delay condition, 315, 428
- assert, 332
- assignment problem, 266–269
- association list, 193–198, 200, 204, 238, 274
  - accessing a record, 193
  - deleting a record, 194
  - empty, 194
  - inserting a record, 194
  - modifying a record, 195
- atom, 326
- attribute (of relation), 416
  
- back\_arc\_solv, 96
- back\_int\_opt, 117, 305
- backtrack stack, 355
- backtrack\_solve, 90
- backtracking
  - chronological, 89
  - in evaluation, 147
  - semantic, 360

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- backtracking goal solver, 350
  - for cut, 364
  - for minimization
    - backtracking, 368
    - retry, 366
  - incremental, 355
- backtracking integer optimizer, 305
- base (in nucleotide), 31
- basic feasible solution, 65
- basic feasible solved form, 65, 377
- basic variable, 65
- bb.int\_opt, 119
- binary CSP, 88
- binary search tree, 199, 200
  - finding an item (find), 199
  - inserting an item (insert\_bst), 200
- binary tree, 198–201, 203
  - layout, 203–207
  - search, *see* binary search tree
  - traversal (traverse), 198
- Bland's anti-cycling rule, 72
- blocks world, 32–33, 61
- body of rule, *see* rule
- bool.solve, 30, 35
- Boolean
  - constraint, 27–30
  - solver, 30, 317
- bottom-up, 402
- bottom-up evaluation, 395–404
  - mimicking top-down, 407–412
  - termination, 412–416
  - with equivalence, 401
  - with subsumption testing, 414
- bounds consistency, 98, 97–109
- bounds propagation, 97–109
- bounds\_consistent, 106
- bounds\_consistent\_addition, 100
- bounds\_consistent\_inequality, 101
- bounds\_consistent\_primitive, 110
- branch and bound, 119, 301–305
- building a house, 17, 62, 195, 196
- built-ins, 179, 230, 234, 303, 308, 309, 324–342
  - database, 332–338, 341
  - debugging, 338–342
  - examining variables, 326–332
  - input/output, 324–326
- butterfly, *see* options trading
- c\_add, 186, 294
- c\_mult, 186, 294
- call, 308, 321
- call option, *see* options trading
- canonical form, 73
- canonical form simplifier, 77, 412
- cardinality ( $| \ |$ ), 60
- Cartesian product, 416
- CCP, 427
- ceiling ( $\lceil \ \rceil$ ), 118, 303, 343
- children of a tree, 22
- choice, 169–174
- choicepoint, 143, 358, 362
- CHR, 430
- chronological backtracking, 89
- clause, 332
- CLP scheme, 151, 425
- CLP(FD), 152, 251
- CLP(Tree), 151
- CLP( $\mathcal{R}$ ), 152, 167
- CNF, *see* conjunctive normal form
- combining models, 270
- comment (%), 216
- complete solver, *see* solver
- complex number, 186, 294
- compound, 326
- concat, 294, 295, 322
- concatenation ( $::$ ), 32, 189, 294
- concurrent constraint programming, 427
- conjunction ( $\wedge$ ), 13, 34
- conjunctive normal form, 30, 79, 436
- cons, 22, 188
- consistency, 91, 92
  - arc, 92, 92–96
  - bounds, 98
  - generalized, 109–114
  - hyper-arc, 97, 283

- node, **92**, 92–96
- constant, **22**
- constrain and generate, 253, 275
- constrained lambda calculus, 434
- constraint, **13**, 11–15
  - Boolean, 27–30
  - complex, 110, 256–258
  - disjunctive, 138
  - equivalent, **14**
  - primitive, **12**, 38
  - projection, **54**, 53–60
  - redundancy-free, **52**
  - redundant, **52**, 223, 276, 278, 431
    - answer redundant, 223, 225, 229
    - in rule, 223
    - solver redundant, 225, 226, 239
  - reified, 284
  - satisfaction, 18–21
  - satisfiable, **14**
  - sequence, 31–32, 294
  - solved form, 20
  - solver, *see* solver
  - store, *see* constraint store
  - tree, **24**, 22–27
  - unsatisfiable, **14**
  - user-defined, **134**, 133–137
    - deterministic, 221
- constraint based graphics, 442
- constraint database, 391, 393
- constraint domain, 12
  - Real*, 12
  - Tree*, 22
  - blocks world, 32
  - Boolean, 27
  - sequences, 31
- constraint handling rules, 430
- constraint logic program, *see* program
- constraint satisfaction problem, *see* CSP
- constraint solver, *see* solver
- constraint solving toolkits, 440
- constraint store, **141**, 353, 355, 366
  - saving and restoring, 358–361
- contig, 31
- crypto-arithmetic problem, 254, 287
- CSP, **86**, 86–88, 275
  - arc consistent, **92**
  - arithmetic, 98
  - binary, 88
  - bounds consistent, **98**
  - false domain, **92**
  - hyper-arc consistent, **97**
  - node consistent, **92**
  - valuation domain, **92**
- cumulative, **112**, 256, 278
- cut (!), 362–365
- data structures, 185–207
  - association list, *see* association list
  - list, *see* list
  - record, *see* record
  - tree, *see* binary tree
- database
  - constraint, 391, 393
  - relational, *see* relational database
  - spatial, 392
  - temporal, 393
- debug, **339**
- debugging, 338–342
- definition of a predicate, 135
- delay condition, 315, 430
  - ask, 315, 428
  - tell, 428
- delay\_until, **315**
- delaying literal, **315**
- deleteff, 260
- deleteffc, 261
- delkey, 194
- deriv, **299**
- derivation, **141**
  - failed, **143**, 146
  - infinite, 146, 149
  - safe, **316**
    - successful, 316
  - selection, **154**
  - simplified, **150**

- step, *see* derivation step
- successful, 142, 146
- derivation step, 141
  - if-then-else, 230
  - minimization, 180
  - negative, 309
  - once, 234
  - selection, 154
- derivation tree, 143, 143–151, 213
  - simplified, 150, 217
- determined solved form, 37
- determined variable, 36, 37
- determines*, 38, 39
- deterministic, 221, 222, 230, 318
- difference list, 210
- disequation ( $\neq$ ), 102, 267
  - solver, 310, 315, 330
- DNA mapping, 31
- dom, 259, 261, 327
- domain, 86, 252
  - false, 92
  - for relational database, 416
  - range, 98
  - valuation, 92
- domain splitting, 264, 306
- don't care non-determinism, 429, 430, 438
- don't know non-determinism, 426, 428
- dump, 80, 325
- dynamic scheduling, 157, 313–319, 330, 343
  - goal-based, 315
  - predicate-based, 315
- electric circuit, 15, 202
  - RLC, 201, 202
- element, 114, 256, 268–271
- eliminate, 354, 370
- empty goal ( $\square$ ), 135, 141
  - , 144
- empty list ( $\{\}$ ), 188
- `empty_alist`, 194, 200
- `emptylist`, 428
- enabled literal, 315
- entry variable, 66
- equiv*, 77
- equivalence ( $\leftrightarrow$ ), 14, 75–78
  - fact, 399
  - projected, 58
  - tester, 77, 412
- `eval`, 354
- `evaln`, 299
- evaluation, 140–143, 147, 349–352
  - algorithm, 350, 355
  - backtracking, 147
  - bottom-up, 395–404
  - bottom-up vs top-down, 405–406
  - incremental solver, 352–357
  - top-down, 140–143
- exit variable, 66
- `fac`, 139, 141, 143, 144, 148, 150, 154, 160, 164
- `fact`, 135, 398
  - equivalence, 399
  - head normal form, 398
  - simplification rules, 400
  - simplifier, 399
  - subsumed, 414
- `fail`, 308, 335, 365
- failed derivation, 143
- false*, 13, 34, 141, 151, 154
- false domain, 92
- `find`, 199
- finite failure, 146
- finite tree, 23
- first fail principle, 261, 263, 281, 291
- first phase problem, 69
- fixed variable, 214
- floor ( $\lfloor \rfloor$ ), 101, 118, 303, 343
- floundered, 316
- Fourier elimination, 55, 56, 60
- `fourier_eliminate`, 57
- `fourier_simplify`, 57, 60, 63
- free variable, 214
- fsimpl*, 399
- functional languages, 433

- functor, 328**
- Gauss-Jordan elimination, 20, 353
- `gauss.jordan`, 21, 27
- `gauss.jordan.simplify`, 73, 74, 78
- `gauss.jordan.solve`, 21, 35, 159
- `gen.ans`, 400
- `gen.facts`, 402
- generate and test, 256
- goal, 135**
  - answer to, *see* answer
  - empty ( $\square$ ), 135, 141
  - rewriting of, 136
- goal evaluation, *see* evaluation
- ground, 315, 326**
- guard, 428, 430
- head normal form, 398
- head of rule, *see* rule
- height of tree, 23
- hierarchical constraints, 439, 442
- hierarchical modelling, 201–203
- higher-order predicate, 307
- hyper-arc consistency, 97, 283
- if-then-else, 230, 362, 365
- iff, 271**
- immediate consequences, 401
- imperative languages, 439
- impl*, 76
- implication ( $\rightarrow$ ), 52, 75–78
  - projected, 414
  - tester, 76
- `inc.arith.solve`, 382
- `inc.bounds.solv`, 375
- `inc.gauss.jordan.solve`, 354
- `inc.simplex`, 378
- `inc.solve.goal`, 356
- `inc.tree.solve`, 371
- incomplete solver, 35
- incremental arithmetic solver, 381
- incremental Gauss-Jordan solver, 353
- incremental solver, 353
  - arithmetic, 381
  - bounds consistency, 374
  - Gauss-Jordan, 353, 358, 360
  - simplex, 377
  - tree constraints, 371
- independence of negative constraints, 416
- `indomain`, 259
- infinite tree, 23
- `insert.bst`, 200
- integer, 303, 326, 343**
- intended mode of usage, 215
- intersect, 333, 339**
- is\_compatible, 311**
- isolv*, 353, 355
- iteration, 174–179
- Kaleidoscope, 439
- Kirchhoff's Laws, 15
- labeling, 253
- labelling, 258–266, 271, 280
  - domain splitting, 264
  - value order, 259, 261
  - variable order, 259, 261
- labellingff, 260**
- length, 261, 262**
- `less_than`, 199, 200
- library predicates, *see* built-ins
- linear constraint, 19
- linear expression, 19
- linear inequality, 19
- list, 188–193**
  - notation, 188
- `list.append`, 196
- literal, 135**
  - delaying, 315
  - enabled, 315
  - if-then-else, 230
  - minimization, 179
  - negative, 309
  - once, 234
- literal ordering, 220
- literal selection
  - fair, 157
  - independence, 153–157

- right-to-left, 154
  - strategy, **316**
  - safe, **316**
- local propagation, 35–41, 317
- local\_propagation\_solve, **39**
- lookup, 194, 200, 205, 277
- map colouring problem, 86
- matrix, 191
- max<sub>D</sub>*, **98**
- maxdomain, 259, 264, **327**
- maximal bipartite matching, 112
- member, **193**, 199, 259, 263, 312, 333
- meta-program, 320
- meta-programming, 320–323
- metal plate problem, 185, 191, 444
- min<sub>D</sub>*, **98**
- mindomain, 259, 264, **327**
- minimization, *see* optimization
- minimize, **179**, 180, 204, 227, 276, 336, 366
- mode of usage, **214**, 220, 222, 227, 232, 314
  - intended, **215**
  - satisfies, **214**
- modelling, 15–18, 86–88, 167–180
  - a function, 173
  - a graph, 195
    - adjacency list, 195
  - choice, 169–174
  - combining models, 270
  - different models for a problem, 114, 266–272
    - comparing models, 269
  - electric circuit, 15, 202
  - hierarchical, 201–203
  - iteration, 174–179
  - list, *see* list
  - matrix, 191
  - negation, 309–313
  - optimization, 179–180
  - record, *see* record
  - relation, 252
  - symmetry, 289
  - vector, 294, 329
- modelling language, 426
  - mathematical, 443–445
- modkey, 195
- monotonic solver, **35**, 156
- mortgage, 175, 178
- N-queens problem, 86, 262
- natural join, 418
- ne, 310, 314, 315, 330, 343
- negation, 309–313
- negative subgoal, **309**
- new, **402**, **414**
- Newton-Raphson method, 297, 300
- nil*, 22, 188
- n1**, **325**
- node*, 23, 198
- node consistency, **92**, 92–96
- node\_arc\_consistent, **95**
- node\_consistent, **94**
- node\_consistent\_primitive, **94**, 110
- nodebug, **339**
- non-parameter, 20
- nonemptylist, 428
- nonvar, 315, 323, **326**
- normalising solver, 20
- nospy, **339**
- nospyall, **339**
- not, **309**, 364
- not\_empty, 294, 322
- not\_member, **190**, 309
- notrace, **339**
- NP-complete, 29
- null*, 23, 198
- objective function, **61**
- occurs check, 373
- Ohm's Law, 15
- old-fashioned marriage problem, 87, 252, 283
- once, **234**, 274, 335, 364
- optimal solution, **61**
- optimization, 61–72, 114–120, 179–180, 204, 227, 301–307, 445

- implementation, 336, 366–369
- integer, 114–120
  - backtracking, 117, 368
  - branch and bound, 119, 301–305
  - retry, 115, 366
- optimistic partitioning, 306
- problem, 61, 64, 179
- simplex, 67
- options trading, 170–174, 210
  - butterfly, 172, 174, 180
  - call option, 170
  - put option, 170
  - straddle, 180
- Oz, 434
- parallel\_resistors**, 134, 135, 136
- parameter, 20, 65
- partial solution, 54, 134
- pivoting, 66
- predecessors, 196, 234, 277
- predicate, 134
  - definition of, 135
  - higher-order, 307
- preferred valuation, 61
- primitive constraint, 12, 38
- primitives*, 15, 34, 35
- principle of least commitment, 264
- probabilistic algorithm, 30
- problem
  - NP-complete, 29
  - optimization, *see* optimization
  - satisfaction, 18
  - solution, 18
- process view of CLP, 427
- product, 418
- program, 135
- program consequences, 401
- projected equivalence, 58
- projected implication, 414
- projecting simplifier, 60
- projection, 54, 53–60
  - for relational databases, 417
  - of constraint, 54
- propagation
  - bounds, 97–109
  - local, 35–41
- propagation rules, 99–105
  - for minimum, 102
  - for addition, 99
  - for disequations, 102
  - for multiplication, 103, 104
- put option, *see* options trading
- qualified answer, 316
- query
  - on database, 418
- query transformation, 410
- range, for finite domains, 98
- read, 324
- Real*, 12, 152
- real\_opt**, 118
- record, 186–188, 202
- recursion, 139, 175, 189, 206, 220
- redundancy, 52
- redundancy-free simplifier, 60
- reified constraint, 284
- relation, 169–170, 416
- relational database, 170, 416–421
  - attribute, 416
  - domain, 416
  - natural join, 418
  - product, 418
  - projection, 417
  - query, 418
  - relation, 416
  - relational expression, 418
  - selection, 418
  - union, 417
- relational expression, 418
- renaming, 34, 136, 141, 154
  - application of, 34, 136
- retract**, 333
- retry integer optimization, 115
- retry\_int\_opt**, 115, 366
- rewrite rules, *see* term rewriting
- rewriting of goal, *see* goal, 141, 154

- river crossing problem, 168
- rule, 133, 134, **135**, 137–140
  - body of, **135**
  - head of, **135**
  - recursive, 139, 198
- rule ordering, 220
- same, **402**
- SAT, 29
- satisfaction problem, 18
- satisfiable, 14
- satisfiable*, **38**, 39, 89, 92
- scheduling, 251, 272–281, 431–433
- search space, **146**
- seesaw problem, 257, 265, 289
- selected literal, **154**
- selection, 418
- selection derivation, 316
- semantic backtracking, 360
- sequence constraint, 31–32, 294
- set based solver, **35**, 154
- shadow of space, 55
- simpl*, **58**, 142, 149, 150
- simple\_solve\_goal*, **350**
- simplex algorithm, **67**, 63–72, 376
  - artificial variable, 69
  - basic feasible solution, **65**
  - basic feasible solved form, **65**
  - basic variable, **65**
  - Bland's rule, 72
  - entry variable, 66
  - exit variable, 66
  - first phase problem, 69
  - form of constraints, **64**
  - incremental, 377
  - pivoting, 66
  - slack variable, 65
  - solver, **71**, 377
- simplex\_opt*, **68**
- simplex\_solve*, **72**
- simplification, 51–60
- simplified derivation, **150**
- simplified derivation tree, **150**, 217
- simplified state, **150**
- simplifier, **58**, 57–60, 151
  - canonical form, **73**, 72–74, 77, 412
  - properties, 60
  - projecting, **60**, 152
  - redundancy-free, **60**
  - weakly projecting, **60**, 152
- slack variable, 65
- smm*, **4**, **254**, 260
- smuggler's knapsack problem, 101, 108, 114, 115, 117, 252, 304
- solution, **14**
  - basic feasible, 65
  - of state or goal, **180**
  - optimal, **61**
  - partial, **54**, 134
  - problem, **18**
- solv*, **34**, 141, 154
- solved form, **20**
  - basic feasible, **65**
  - determined, 37
- solver, **18**, **34**, 33–35, 151
  - arc consistency, 281
  - backtracking, 89, 96
  - Boolean, **30**, 317
  - bounds consistency, 281, 374
    - complete, 108
    - incomplete, 107
  - branch and bound, 267
  - complete, **35**, 89, 96, 253
  - finite domain, 267
    - backtracking, 89
    - bounds consistency, 107, 108
    - node and arc consistency, 95, 96
  - Gauss-Jordan, 21, 353
  - incomplete, **30**, **35**, 95, 225, 252, 381
  - incremental, *see* incremental solver
  - local propagation, **38**, 317
  - node and arc consistency
    - complete, 96
    - incomplete, 95
  - normalising, 20, 53



- properties, 33–35
  - monotonic, 35, 156
  - set based, 35, 154
  - variable name independent, 35, 152
- simplex, 71
- tree constraints, 25, 371
- well-behaved, 35, 141, 152
- solver redundant, 225, 226, 239
- spatial database, 392
- spy, 339
- spypoint, 339
- state, 141
  - critical, 150
  - fail, 142, 144
  - success, 142, 144
- store, *see* constraint store
- straddle, *see* options trading
- subsumed
  - fact, 414
- successful derivation, 142, 146
- symbolic algebra package, 445–446
- syntactic identity ( $\equiv$ ), 21
- syntactic object, 136
- tell delay condition, 428
- temporal database, 393
- term, 24
- term equation, 24
- term rewriting, 436
  - augmented, 436
  - constrained, 438
- time stamping, 358
- top-down evaluation, 397
- trace, 339
- trailing, 358
- traverse, 198, 205
- Tree*, 22, 151, 152
- tree, 22
  - binary, *see* binary tree
  - children of, 22
  - constraint, 22, 24
  - constructor, 22, 188
  - finite, 23
  - height, 23
  - infinite, 23
- tree.simplify, 59, 59, 60, 73, 151
- tree.solve, 26, 35, 151
- true, 13, 34
- true, 232
- underscore ( $-$ ), 12, 134, 188
- unify, 26, 27, 53, 59, 370
- union, 417
- unknown, 30, 34, 252
- unsatisfiable, 14
- user-defined constraint, *see* constraint
- valuation, 14, 33
  - extension, 54
  - preferred, 61
- valuation domain, 92
- var, 326
- variable, 11
  - anonymous, 188
  - artificial, 69
  - basic, 65
  - Boolean, 267
  - determined, 36, 37
  - fixed, 214
  - free, 214
  - non-parameter, 20
  - parameter, 20, 65
  - procedural, 177
  - slack, 65
- variable name independent solver, 35, 152
- variant, 34, 35, 136
- vars, 14
- vector, 294, 296
- weakly projecting simplifier, 60
- well-behaved solver, 35, 141, 152
- write, 325