Advanced Data Mining - Lab 2

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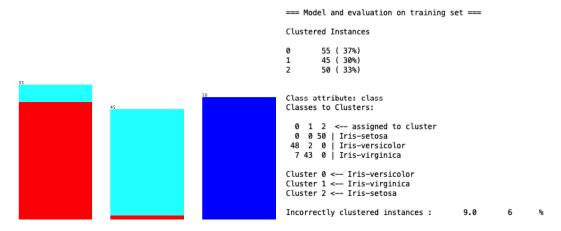
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Lab 2: Association Analysis - 1

In this lab we will use Iris dataset. This dataset has 4 numeric continues features and one categorical feature which is name of the Species. We will use only first 4 numeric continues features in order to use them with a clustering algorithm (K-Means for all experiments). But with numeric continues features we cannot cluster the data, so first of all we have to split these features to different count of bins. We will try different count of bins. We use 3 (recommended bin count), 5 and 10 as bin count for each features which are "sepallength", "sepalwidth", "petallength" and "petalwidth". All cluster names in Clustering sections references to association rules, not "Model and evaluation on training set" plot, so if we use cluster1 this means "Cluster 0" in that plot.

Recommended Parameters k=3; bins=3

Clustering



Before starting our parameter experiments we will use recommended parameters and see how the association rules are good. Recommended parameters are bins=3 and k=3. First we run k-means algorithm with k=3 and

we get the clusters below respectively cluster1, cluster2 and cluster3. Additionally we can see the performance of clustering at the right side above We have some incorrectly clustered instances, but it is not majority, just 6%. The only bad thing is that incorrect clustered instances are mostly from one class which is Iris-setosa.

Association Rules

```
Best rules found:
             conf:(1)
                                                                                                   sepalwidth='(-inf-2.8]'
                sepalwidth='(2.8-3.6]'
sepalwidth='(2.8-3.6]'
                 sepalwidth='(-inf-2.8]
                 sepalwidth='(2.8-3.61'
                sepallength='(5.5-6.7]'
sepalwidth='(2.8-3.6]'
                 sepallength='(5.5-6.7]'
sepallength='(5.5-6.7]'
                 sepallength='(5.5-6.7]'
sepallength='(5.5-6.7]'
                                                                                                         \label{eq:continuous} $$ sepalwidth='(2.8-3.6]' petallength='(2.966667-4.933333]' petalwidth='(0.9-1.7]' 18 \Longrightarrow cluster=cluster1 18 $$ petallength='(4.933333-inf)' 17 \Longrightarrow cluster=cluster2 17 conf:(1) $$ petallength='(4.933333-inf)' 16 \Longrightarrow cluster=cluster2 16 conf:(1) $$ sepalwidth='(2.8-3.6]' petallength='(4.933333-inf)' 16 \Longrightarrow cluster=cluster2 16 conf:(1) $$ petallength='(4.933333-inf)' petalwidth='(1.7-inf)' 16 \Longrightarrow cluster=cluster2 15 conf:(1) $$ sepalwidth='(-inf-2.8]' petallength='(2.966667-4.933333]' petalwidth='(0.9-1.7]' 15 \Longrightarrow cluster=cluster1 15 $$ sepalwidth='(2.8-3.6]' petallength='(4.933333-inf)' petalwidth='(1.7-inf)' 15 \Longrightarrow cluster=cluster2 15 conpetalwidth='(0.9-1.7]' 38 \Longrightarrow cluster=cluster1 37 conf:(0.97)' $$ sepalwidth='(2.8-3.6]' 37 \Longrightarrow cluster=cluster1 37 conf:(0.97)' $$ sepalwidth='(2.8-3.6]' 37 \Longrightarrow cluster=cluster1 37 conf:(0.97)' $$ sepalwidth='(2.8-3.6]' 37 \Longrightarrow cluster=cluster2 35 conf:(0.97)' $$ sepalwidth='(2.8-3.6]' 37 \Longrightarrow cluster=cluster2 36 conf:(0.97)' $$ sepalwidth='(2.8-3.6]' 37 \Longrightarrow cluster=cluster2 36 conf:(0.97)' $$ sepalwidth='(2.8-3.6]' 37 \Longrightarrow cluster=cluster2 37 conf:(0.97)' $$ sepalwidth='(2.8-3.6]' 37 \Longrightarrow cluster=cluster2 37 conf:(0.97)' $$ sepalwidth='(2.8-3.6]' 37 \Longrightarrow cluster=cluster2 37 conf:(0.97)' $$ sepalwidth='(0.97)' $$ sepalwid
                 sepallength='(6.7-inf)'
sepallength='(6.7-inf)'
                  sepallength='(5.5-6.71'
                sepallength='(6.7-inf)'
sepallength='(5.5-6.7]'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     conf:(1)
                 sepallength='(5.5-6.71'
               sepallength='(i.5-b.7]' petalwidth='(0.9-1.7)' 38 => cluster=cluster1 37 conf:(0.97) sepallength='(-i.nf-5.5)' sepalwidth='(2.8-3.6)' 37 ==> cluster=cluster3 36 conf:(0.97) petalwidth='(0.9-1.7)' 54 => cluster=cluster1 52 conf:(0.96) sepallength='(5.5-6.7]' sepalwidth='(2.8-3.6]' petalwidth='(0.9-1.7]' 19 => cluster=cluster1 18 petallength='(2.966667-4.933333]' 54 ==> cluster=cluster1 51 conf:(0.94)
                                                                                                                                                                                                                                                                                                                                                                                                  conf:(0.95)
                   conf: (0.93)
               petallength='(4.933333-inf)' 46 ==> cluster=cluster2 42 conf:(0.91) sepalwidth='(2.8-3.6]' petalwidth='(0.9-1.7]' 23 ==> cluster=cluster1 21 sepallength='(5.5-6.7]' petalwidth='(1.7-inf)' 30 ==> cluster=cluster2 27
                                                                                                                                                                                                                                                                                                               conf: (0.9)
```

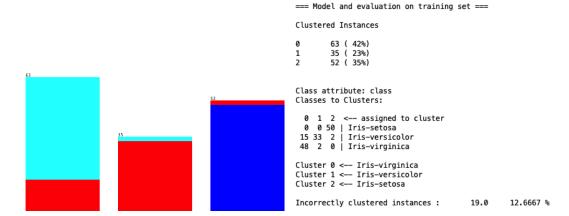
After getting clusters above we can move forward to find association rules with apriori algorithm. We can see the rules that we obtain above, we have 43 rules which have more than 90% confidence. We can see our first 32 rules have 100% confidence. We captured at least one rule for each cluster as we want. Moreover, we have many rules have 100% confidence for each cluster. We have 11 rules for cluster1; 12 rules for cluster2 and cluster3 with 100% conf. We can say by looking all these foundings, this is a good clustering and binning settings for creating strong association rules, because we have almost equal count of rules for each cluster in the best rules. Moreover in total we have

After this recommended settings we will test different bin values by keeping same k value for clustering which is already recommended and the actual cluster count in the dataset. Below we will discuss affect of different bin values to association rules. We use bins=3,5 and 10.

Experiments

k=3; bins=5

Clustering



With this binning setting, we split all features to 5 bins. We can see that Iris-versicolor have many incorrectly clustered instances. Except this Iris-setosa is clustered perfectly again and Iris-virginica is also close to perfect, but in total we have 19 incorrectly clustered instances which means 12.66% of total data. It is slightly more than double of k=3;bins=3 settings. We can see the effects of increased bins count as increasing incorrectly clustered instances.

Association Rules

```
Best rules found:
       1. petallength='(-inf-2.18]' 50 => cluster=cluster3 50 conf:(1)
2. petalwidth='(-inf-0.58]' 49 => cluster=cluster3 49 conf:(1)
3. petallength='(-inf-2.18]' petalwidth='(-inf-0.58]' 49 => cluster=cluster3 49
4. sepallength='(-inf-5.02]' petallength='(-inf-0.58]' 27 => cluster=cluster3 27
5. sepallength='(-inf-5.02]' petallength='(-inf-0.58]' 27 => cluster=cluster3 27
6. sepallength='(5.74-6.46]' petallength='(-inf-2.18]' 27 => cluster=cluster3 27
7. sepalwidth='(2.96-3.44]' petallength='(-inf-2.18]' 27 => cluster=cluster3 27
8. sepalwidth='(-inf-2.18]' 27 => cluster=
                                                                                                                                                                                                                                                                                                                                                                                                                                                    conf:(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                    conf:(1)
                       sepalwidth='(2.96-3.44]'
sepalwidth='(2.96-3.44]'
sepallength='(-inf-5.02]'
                                                                                                                                                                                                                                                                                                                                                                                                                                                   conf:(1)
                                                                                                                                                     petalwidth='(-inf-0.58]' 27 ==> cluster=cluster3 27
' petallength='(-inf-0.18]' petalwidth='(-inf-0.58]'
                                                                                                                                                                                                                                                                                                                                                                                                                                                ==> cluster=cluster3 27
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                     sepalwidth='(2.96-3.44]' petallength='(-inf-2.18]' sepalwidth='(2.96-3.44]' petallength='(4.54-5.72]'
                                                                                                                                                                                                                                                                                        petalwidth='(-inf-0.58]' 27
25 ==> cluster=cluster1 25
                                                                                                                                                                                                                                                                                                                                                                                                                                                   ⇒ cluster=cluster3 27
                                                                                                                                                                                                                                                                                                                                                                                                                                                  conf:(1)
                      sepallength='(-inf-5.02]'
sepallength='(-inf-5.02]'
                                                                                                                                                          sepalwidth='(2.96-3.44]' 22 ==> cluster=cluster3 22 sepalwidth='(2.96-3.44]' petallength='(-inf-2.18]'
                                                                                                                                                                                                                                                                                                                                                                                                                                                   conf:(1)
                                                                                                                                                         sepalwidth='(2.96-3.44|' petallength='(-inf-0.58|' 22 \Longrightarrow cluster=cluster3 22 conf:(1) conf:(1) sepallength='(-inf-2.18|' petallength='(-inf-0.58|' 22 \Longrightarrow cluster=cluster3 22 conf:(1) petallength='(-inf-0.58|' 21 \Longrightarrow cluster=cluster3 21 conf:(1) petallength='(-inf-0.58|' 21 \Longrightarrow cluster=cluster3 21 conf:(1) petallength='(-inf-0.58|' 21 \Longrightarrow cluster=cluster3 21 conf:(1)
                                                                                                                                                                                                                                                                                         petallength='(-inf-2.181' 22
                      sepallength='(-inf-5.02]'
sepallength='(-inf-5.02]'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    conf:(1)
                      sepallength='(5.02-5.74]'
sepallength='(5.02-5.74]'
                      sepallength='(5.02-5.74]'
petallength='(4.54-5.72]'
                                                                                                                                                     petal length='(-inf-2.18]' petal width='(-inf-0.58]' 2
'petal width='(1.54-2.02]' 20 ==> cluster=cluster1 20
petal length='(3.36-4.54]' 18 ==> cluster=cluster2 18
'petal length='(3.36-4.54)' 17 ==> cluster=cluster2 17
                                                                                                                                                                                                                                                                                                                                                                                                                                                        > cluster=cluster3 21
                                                                                                                                                                                                                                                                                                                                                                                                                                                   conf:(1)
                      sepalwidth='(2.48-2.96]'
sepallength='(5.02-5.74]'
                   sepallength='(5.02-5.74]' petallength='(3.36-4.54]' 17 => cluster=cluster2 17 conf:(1) sepalwidth='(2.96-3.44]' petalwidth='(2.02-inf)' 17 => cluster=cluster1 17 conf:(1) sepalwidth='(3.44-3.92]' petallength='(-inf-2.18]' 17 => cluster=cluster3 17 conf:(1) sepallength='(5.02-5.74]' petalwidth='(1.06-1.54]' 16 => cluster=cluster2 16 conf:(1) sepallength='(5.02-5.74]' petalwidth='(-inf-0.58]' 16 => cluster=cluster3 16 conf:(1) sepallength='(5.74-6.46]' sepalwidth='(2.48-2.96]' petallength='(4.54-5.72]' 16 => cluster=cluster1 16 sepalwidth='(3.44-3.92]' petalwidth='(1.64-2.02]' 15 => cluster=cluster1 15 conf:(1) sepallength='(5.74-6.46]' petalwidth='(1.54-2.02]' 15 => cluster=cluster1 15 conf:(1) sepallength='(5.02-5.74]' petallength='(3.36-4.54]' petalwidth='(1.06-1.54]' 15 => cluster=cluster2 15 sepallength='(6.46-7.18]' sepalwidth='(2.96-3.44]' petallength='(4.54-5.72]' 15 => cluster=cluster1 15 sepalwidth='(1.54-2.02]' 29 => cluster=cluster1 28 conf:(0.97) sepallength='(5.72-inf)' 23 => cluster=cluster1 28 conf:(0.94) petallength='(5.72-inf)' 16 => cluster=cluster1 15 conf:(0.94) petallength='(4.54-5.72]' 47 => cluster=cluster1 44 conf:(0.94)
                                                                                                                                                                                                                                                                                                                                                                                                                                                        conf:(1)
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  conf:(1)
                       petallength='(4.54-5.72)' 47 => cluster=cluster1 44 conf:(0.94)

petallength='(3.36-4.54)' petalwidth='(1.06-1.54)' 27 => cluster=cluster2 25

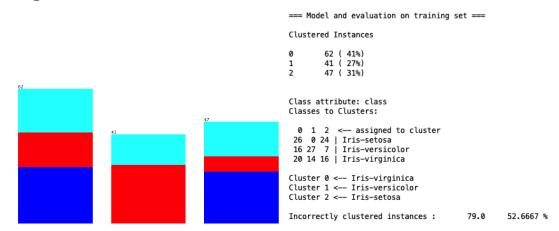
sepallength='(6.46-7.18)' sepalwidth='(2.96-3.44)' 20 => cluster=cluster1 18
                                                                                                                                                                                                                                                                                                                                                                                                                                                   conf:(0.93)
```

This time although we increased the rule count to 50, we have only 38 rules which is greater than 90% confidence. This number is less than previous one. This shows us when we have more bins it is harder to create association rules. 31 of them have 100% confidence. We have rules with 100% confidence for cluster3

in majority again. We have 19 rules for cluster3, 5 rules for cluster2 and 7 rules for cluster1. As we can see that we have strong rules for each cluster and we get good rules as before.

k=3; bins=10

Clustering



This time we used 10 bins. We can see that we have 79 incorrectly clustered instances which is 52.66% of the total data. The experiments that we did before we always have Iris-setosa clustered perfectly, but this time it is incorrectly clustered almost half of it. We can see increasing bin count affects the wellness of clustering as we observed before.

Association Rules

Best rules found:

- sepallength='(4.66-5.02]' petalwidth='(-inf-0.34]' 17 ==> cluster=cluster3 17 conf:(1)
- 2. sepalwidth='(2.96-3.2]' petalwidth='(-inf-0.34]' 16 ==> cluster=cluster3 16
 3. sepallength='(4.66-5.02]' 23 ==> cluster=cluster3 22 conf:(0.96) conf:(1)

This time we have only 3 rules which are only for cluster3. With this settings beside having a bad clustering performance, we also get bad association rules.

Conclusion of Bin Count Experiments

Statistics of 100% Confidence

	cl1	cl2	cl3	total
k=3;bins=3	0.3125000	0.3437500	0.3750000	32
k=3;bins=5	0.2258065	0.1612903	0.6129032	31
k=3;bins=10	0.0000000	0.0000000	1.0000000	2

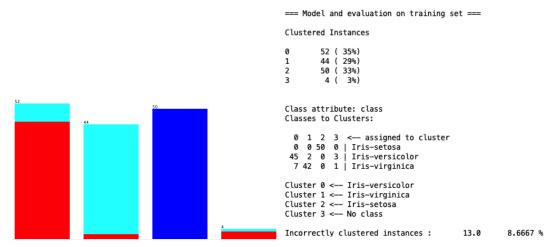
Statistics of Total

	cl1	cl2	cl3	total
k=3;bins=3	0.3720930	0.3255814	0.3023256	43
k=3;bins=5	0.3157895	0.1578947	0.5263158	38
k=3;bins=10	0.0000000	0.0000000	1.0000000	3

As far as we see, increasing bin count affects the clustering and association algorithms. More categories to cluster and associate means more confusing, more complex models and it is not good idea to use bins=10. In next experiments we will not use bins=10. We can use bins=3 or bins=5. We will select bins=3, because it provides more quantity of strong association rules. k=3;bins=3 experiment has 43 rules in total. 32/43 have 100% confidence, 11/43 have 90-99.9% confidence. On the other hand, k=3;bins=5 has 38 rules in total and 31/38 have 100% confidence, 7/38 have 90-99.9% confident. But as we can see from the statistics above k=3;bins=3 has almost equally number of rules, so it is sensible to continue with bins=3. The statistics present counts of all clusters in proportional. k=3;bins=5 settings create more rules for cluster3 than for the others.

k=4; bins=3

Clustering



In this experiment part, we will increase cluster count. As we can see we have 3 cluster (1,2,3) which has majority inside them, but cluster4 is too small to say that it is a cluster next to others. It has only 4 element inside it. We cannot say this is a good clustering result. Strongest cluster is cluster3 here, because all Iris-setosa instances are captured in this cluster. We will see how this clustering results will affect the association rules.

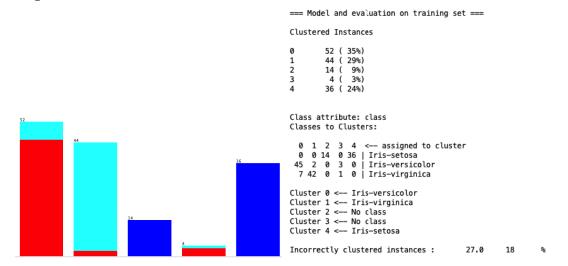
Association Rules

```
1. petallength='(-inf-2.96667)' 50 => cluster=cluster3 50 conf:(1)
2. petallength='(-inf-2.96667)' 50 => cluster=cluster3 50 conf:(1)
3. petallength='(-inf-2.96667)' petalwidth='(-inf-0.9)' 50 => cluster=cluster3 50 conf:(1)
4. sepallength='(-inf-5.5)' petallength='(-inf-0.9)' 47 => cluster=cluster3 47 conf:(1)
5. sepallength='(-inf-5.5)' petalwidth='(-inf-0.9)' 47 => cluster=cluster3 47 conf:(1)
6. sepallength='(-inf-5.5)' petalwidth='(-inf-0.9)' 47 => cluster=cluster3 47 conf:(1)
7. petallength='(4.93333-inf)' petalwidth='(1.7-inf)' 40 => cluster=cluster3 47 conf:(1)
8. sepalwidth='(2.8-3.6)' petallength='(-inf-2.96667)' 36 => cluster=cluster3 36 conf:(1)
9. sepalwidth='(2.8-3.6)' petallength='(-inf-0.9)' 47 => cluster=cluster3 36 conf:(1)
10. sepallength='(-inf-5.5)' sepalwidth='(2.8-3.6)' petalwidth='(-inf-0.9)' 36 => cluster=cluster3 36 conf:(1)
11. sepallength='(-inf-5.5)' sepalwidth='(2.8-3.6)' petalwidth='(-inf-0.9)' 36 => cluster=cluster3 36 conf:(1)
12. sepalwidth='(2.8-3.6)' petallength='(-inf-2.96667)' petalwidth='(-inf-0.9)' 36 => cluster=cluster3 36 conf:(1)
13. sepallength='(-inf-5.5)' sepalwidth='(2.8-3.6)' petalwidth='(-inf-0.9)' 36 => cluster=cluster3 36 conf:(1)
14. sepalwidth='(2.8-3.6)' petallength='(-inf-0.96667)' petalwidth='(-inf-0.9)' 36 => cluster=cluster3 36 conf:(1)
15. sepalwidth='(-inf-2.8)' sepalwidth='(2.8-3.6)' petalwidth='(-inf-0.9)' 36 => cluster=cluster3 36 conf:(1)
16. sepalwidth='(-inf-0.9)' petalwidth='(-inf-0.9)' 31 => cluster=cluster3 36 conf:(1)
17. sepalwidth='(-inf-0.9)' petalwidth='(-inf-0.9)' 31 => cluster=cluster3 36 conf:(1)
18. sepalwidth='(-inf-0.9)' petalwidth='(-inf-0.9)' 31 => cluster=cluster3 36 conf:(1)
19. sepalwidth='(-inf-0.9)' petalwidth='(0.9-1.7)' 31 => cluster=cluster3 30 conf:(1)
19. sepalwidth='(-inf-0.8)' petalwidth='(0.9-1.7)' 31 => cluster=cluster3 30 conf:(1)
19. sepalwidth='(-inf-0.8)' petalwidth='(0.9-1.7)' 19 => cluster=cluster1 30 conf:(1)
19. sepalwidth='(-inf-0.8)' petalwidth='(-inf-0.8)' petalwidth='(-inf-0.8)' petalwidth='(-inf-0.8)' pe
```

We have 29/39 rules have 100% confidence, but there is no rule for cluster4. This situation is expected after that bad clustering. Because we do not have enough instances in cluster4 to associate.

k=5; bins=3

Clustering



With this settings also we have same situation. We have the same cluster which has only 4 element (cluster4). In this time we have also splitted clusters which have only Iris-setosa instances which are really good clustered in previous experiments (cluster3 and cluster5). We can observe that increasing cluster count splits clusters to many small pieces and some of instances which have strong relation between their features resists this split.

Association Rules

Best rules found:

```
1. petallength='(4.93333-inf)' petalwidth='(1.7-inf)' 40 => cluster=cluster2 40 conf:(1)
2. sepalwidth='(2.8-3.6]' petalwidth='(-inf-2.966667]' 36 => cluster=cluster5 36 conf:(1)
3. sepalwidth='(2.8-3.6]' petalwidth='(-inf-2.966667]' 36 => cluster=cluster5 36 conf:(1)
4. sepallength='(-inf-5.5]' sepalwidth='(2.8-3.6]' petalwidth='(-inf-2.966667]' 36 => cluster=cluster5 36 conf:(1)
5. sepallength='(-inf-5.5]' sepalwidth='(2.8-3.6]' petalwidth='(-inf-2.966667]' 36 => cluster=cluster5 36 conf:(1)
6. sepalwidth='(2.8-3.6]' petallength='(-inf-2.966667]' petalwidth='(-inf-2.966667]' petalwidth='(-inf-2.96667]' petalwidth='(-inf-2.966667]' petalwidth='(-inf-2.91)' 36 => cluster=cluster5 36 conf:(1)
7. sepallength='(-inf-5.5]' sepalwidth='(2.96667-4.93333]' petalwidth='(-inf-2.91)' 33 => cluster=cluster1 33 conf:(1)
8. sepalwidth='(-inf-2.6]' petallength='(2.96667-4.93333]' 30 => cluster=cluster1 30 conf:(1)
19. sepalwidth='(-inf-2.8)' petalwidth='(inf-2.96667-4.93333]' petalwidth='(inf-2.91)' 27 => cluster=cluster1 27 conf:(1)
11. sepalwidth='(-inf-2.8)' petallength='(2.966667-4.93333]' petalwidth='(inf-2.91)' 27 => cluster=cluster1 27 conf:(1)
12. sepalwidth='(inf-2.8)' petallength='(4.933333-inf)' petalwidth='(inf-1.7-inf)' 26 => cluster=cluster1 27 conf:(1)
13. sepalwidth='(inf-2.8)' petallength='(4.933333-inf)' petalwidth='(inf-1.7-inf)' 26 => cluster=cluster1 26 conf:(1)
14. sepallength='(5.5-6.7)' sepalwidth='(inf-2.8)' petalwidth='(inf-2.8)' petal
```

We have 23/33 rules have 100% confidence which does not contain rules for cluster4. This problem is very similar to previous experiment with k=4. We should create association rules for each cluster that satisfies minimum support threshold. Obviously, increasing k value is not good for our association rules.

Final Conclusion

Statistics of 100% Confidence

	cl1	cl2	cl3	cl4	cl5	total
k=3;bins=3	0.3125000	0.3437500	0.3750000	0	0.0000000	32
k=4;bins=3	0.2758621	0.3103448	0.4137931	0	0.0000000	29
k=5;bins=3	0.3478261	0.3913043	0.0000000	0	0.2608696	23

Statistics of Total

	cl1	cl2	cl3	cl4	cl5	total
k=3;bins=3	0.3720930	0.3255814	0.3023256	0	0.0000000	43
k=4;bins=3	0.3333333	0.3333333	0.3333333	0	0.0000000	39
k=5;bins=3	0.3939394	0.3939394	0.0000000	0	0.2121212	33

The statistics above, if k=3 we expect to see a value different from 0 at cl1, cl2, cl3 or same thing if k=4, we expect something at cl1, cl2, cl3 and cl4. As we can see we have missing values at k=4;bins=3 (cl4) and k=5;bins=3 (cl3, cl4). There is only one option left that we can choose which is recommended settings k=3;bins=3.