Package 'ForestSDC'

June 20, 2025

Title Forest stand Structure, tree Diversity, and species Composition

Type Package

Version 0.1.0				
Author Ernesto Rubio				
Maintainer Ernesto Rubio <ernestorub@gmail.com></ernestorub@gmail.com>				
Description The package provides tools for forest inventory analysis, including functions to calculate structural diversity indices, biodiversity metrics, and Nearest Neighbour Summary Statistics. It is designed to support researchers and practitioners in assessing forest dynamics, ecosystem health, and biodiversity.				
Imports FNN, dplyr, tidyr				
License GPL-3				
Encoding UTF-8				
LazyData true				
RoxygenNote 7.3.2				
Contents				
A_index 2 A_max 3 A_rel 4 bal 4 BALMOD 5 ca 6 Caha 7 cat_d 7 coordxy 8 dg 9 dista 9 dom_trees 10 d_dom 11 ForestSDC 12 g 12 Gha 13				
h_dom				

2 A_index

																											24
simpson_complement	 •	 		•	•	 •	•	•	•	 •	•	•	•	 •	•	•	•	•	•	•	•	•		•	•	•	22
$simpson \ . \ . \ . \ . \ .$																											
$shannon_evenness\ .\ .$																											
shannon																											
sdi																											
rich																											
pielou																											
$nnss_square \ . \ . \ . \ .$																											
nnss_circle																											
Nha																											
$menhinick \ . \ . \ . \ . \ .$																											
margalet		 	•			 •	•			 •	•	•			•	•	•	•	•	•	•	•	•				14

A_index

Index

Species Profile Index A

Description

This function calculates the Species Profile Index A, which measures species diversity across three height zones:

- Zone 1: Trees with heights \geq 80% of the maximum height.
- Zone 2: Trees with heights between 50% and 80% of the maximum height.
- Zone 3: Trees with heights < 50% of the maximum height.

Usage

A_index(x, y)

Arguments

x A numeric vector representing tree heights.

y A character or factor vector representing species corresponding to each tree height.

Details

#' For each zone, the species proportions are used to compute a diversity profile index:

$$PI = \sum_{i=1}^{S} |p_i \cdot \ln(p_i)|$$

Where:

- ullet S is the total number of species in the zone.
- p_i is the proportion of the *i*-th species in the zone.

The Species Profile Index A is the sum of the profile indices across all three zones:

$$A = PI_1 + PI_2 + PI_3$$

A_max 3

Value

A numeric value representing the Species Profile Index A.

References

Pretzsch, H. (2009). Forest Dynamics, Growth and Yield: From Measurement to Model. Springer-Verlag. https://doi.org/10.1007/978-3-540-88307-4

Examples

```
x <- c(10, 20, 30, 40, 50, 25, 30, 22, 11, 10)
y <- c(
  "P. patula", "P. patula", "P. patula", "A. religiosa", "Q. castanea",
  "P. patula", "P. patula", "P. patula", "P. patula"
)
A_index(x, y)</pre>
```

A_max

Maximum Value for the Species Profile Index A

Description

This function calculates the maximum possible value of the Species Profile Index A, based on the number of distinct species present. It assumes that each species is equally distributed across the three height zones.

Usage

```
A_{max}(x)
```

Arguments

Х

A character or factor vector representing species.

Value

A numeric value representing the maximum possible Species Profile Index A.

```
x <- c(
   "P. patula", "P. patula", "P. patula", "A. religiosa", "Q. castanea",
   "P. patula", "P. patula", "P. patula", "P. patula", "P. patula"
)
A_max(x)</pre>
```

4 bal

A_rel

Relative Value for the Species Profile Index A

Description

This function calculates the relative value of the Species Profile Index A, which represents the observed species diversity in relation to the maximum possible diversity for a given set of species. The relative value is expressed as a percentage.

Usage

```
A_{rel}(x, y)
```

Arguments

x A numeric vector representing tree heights.

y A character or factor vector representing species.

Value

A numeric value representing the relative Species Profile Index A (as a percentage).

Examples

```
x <- c(10, 20, 30, 40, 50, 25, 30, 22, 11, 10)
y <- c(
  "P. patula", "P. patula", "P. patula", "A. religiosa",
  "Q. castanea", "P. patula", "P. patula", "P. patula",
  "P. patula", "P. patula"
)
A_rel(x, y)</pre>
```

bal

Calculate Basal Area Larger Index (BAL)

Description

This function calculates the Basal Area Larger Index (BAL), which is the sum of the basal area of trees larger than a given subject tree in a specified plot area. It provides an index of competition based on tree size.

Usage

```
bal(x, y)
```

Arguments

x Numeric vector. Diameters of the subject trees in cm.

y Numeric. Plot area in square meters.

BALMOD 5

Details

The formula for each tree is:

$$BAL_i = \frac{\sum (BA_j > BA_i)}{A}$$

where:

- BA_i is the basal area of the subject tree.
- BA_i is the basal area of a competing tree larger than BA_i .
- A is the plot area in square meters.

Value

Numeric vector. The BAL values for each tree in x.

Examples

```
x <- c(30, 20, 20, 35, 65) # Tree diameters in cm bal_result <- bal(x, 400) # Calculate BAL for a plot area of 400 square meters bal_result
```

BALMOD

BALMOD Competition Index

Description

This function calculates the BALMOD competition index for trees based on their diameters, heights, and the area of the plot. The BALMOD index measures competition among trees by integrating basal area proportion, relative spacing, and dominant height.

Usage

```
BALMOD(x, y, z)
```

Arguments

x A numeric vector representing the diameters of the trees in cm.

y A numeric vector representing the heights of the trees in meters.

z A numeric variable representing the plot area in square meters.

Details

The BALMOD index is computed as:

$$BALMOD = \frac{1 - \pi}{RS}$$

where:

- π is the proportion of the basal area of the individual tree $(\pi = \frac{\text{BAL}}{G_{\text{ha}}})$,
- RS is the relative spacing ($RS = \frac{\sqrt{10000/N}}{h_{\mathrm{dom}}}$),
- ullet N is the total number of trees in the plot,
- \bullet $h_{
 m dom}$ is the dominant height, defined as the mean height of the tallest trees.

6 ca

Value

A numeric vector containing the BALMOD index for each tree.

Examples

```
x \leftarrow c(10, 20, 30, 40, 50, 25, 30, 22, 11, 10) # Tree diameters in cm y \leftarrow c(12, 23, 33, 45, 43, 22, 31, 32, 13, 11) # Tree heights in meters z \leftarrow 400 # Plot area in square meters

BALMOD(x, y, z) # Calculate BALMOD index
```

ca

Individual Tree Crown Area

Description

This function calculates the crown area of an individual tree based on two measurements of its crown diameters. The crown area is computed using the average of the two diameters and is assumed to be circular.

Usage

```
ca(x, y)
```

Arguments

x A numeric variable representing the first tree crown diameter in meters.

y A numeric variable representing the second tree crown diameter in meters.

Value

A numeric variable representing the tree crown area in square meters.

```
\# Calculate the crown area for two crown diameters of 10 m and 15 m crown_area <- ca(10, 15) crown_area \# Output: Area in square meters
```

Caha 7

Caha

Calculate Crown Area Cover per Hectare

Description

This function calculates the total crown area cover per hectare based on the tree crown diameters provided. It computes the crown area for each tree as the area of a circle using the formula:

$$A = \pi \times \left(\frac{cw}{2}\right)^2$$

where cw is the crown diameter in m. The total crown area is then scaled to a per-hectare value using the specified plot area.

Usage

```
Caha(x, y)
```

Arguments

x Numeric vector. Tree crown diameters (in meters).

y Numeric. Total plot area (in square meters).

Value

Numeric. Crown area cover per hectare (in square meters).

Examples

```
# Example crown diameters and plot area x \leftarrow c(10, 8, 6, 8, 5, 7, 2, 3, 11, 10) y \leftarrow 1000 # Calculate crown area cover per hectare Caha(x, y)
```

cat_d

Diameter Category Classification

Description

This function categorizes tree diameters into classes of 5 cm, starting from 2.5 cm. It takes a numeric variable or vector representing tree diameters and returns the corresponding diameter categories.

Usage

 $cat_d(x)$

Arguments

Χ

A numeric variable or vector representing tree diameters in centimeters.

8 coordxy

Value

A factor variable or vector representing tree diameter classes in increments of 10 cm.

Examples

```
# Create a data frame with tree diameters
d_data <- data.frame(d = c(10.1, 23, 31.5, 40, 52.4, 27, 33, 22, 11, 10))
# Categorize the diameters into classes
d_data$diam_cat <- cat_d(d_data$d)
# Display the categorized data
print(d_data)</pre>
```

coordxy

Calculate Coordinates from Azimuth and Distance

Description

This function calculates the Cartesian coordinates (x, y) based on a given azimuth angle and distance from a reference point. The function can be used for both circular and square plots, where the size of the plot is specified by the diameter (for circles) or the side length (for squares).

Usage

```
coordxy(azi, dis, z)
```

Arguments

azi	Numeric variable. Azimuth angle in degrees (0-360).
dis	Numeric variable. Distance from the reference point (in the same unit as z).
Z	Numeric variable. Diameter of the circle or side length of the square plot.

Value

A numeric vector containing the calculated coordinates (x, y).

```
# Calculate coordinates for an azimuth of 350 degrees and a distance of 15 units coordxy(350, 15, 20)
```

dg 9

dg

Calculate Quadratic Mean Diameter (QMD)

Description

This function calculates the quadratic mean diameter (QMD) of a set of tree diameters. The QMD is a commonly used forestry measure to assess the average tree diameter in a stand, weighted by the basal area of the trees. It is useful for understanding stand structure and growth.

Usage

dg(x)

Arguments

Х

Numeric vector. A vector of tree diameters (in centimeters).

Details

The formula used is:

$$QMD = \sqrt{\frac{\sum BA}{k \times n}}$$

where: - $\sum BA$ is the sum of the basal areas of all trees. - k is a constant factor for conversion. - n is the number of trees.

Value

Numeric. The quadratic mean diameter (in centimeters).

Examples

```
# Example tree diameters x \leftarrow c(10, 20, 30, 40, 50, 25, 30, 22, 11, 10) # Calculate the quadratic mean diameter dg(x)
```

dista

Compute the Distance between Two Points

Description

This function calculates the Euclidean distance between two points in a 2D space. The distance is computed using the formula:

$$d = \sqrt{(x1 - x)^2 + (y1 - y)^2}$$

where (x, y) and (x1, y1) are the coordinates of the two points.

10 dom_trees

Usage

```
dista(x, y, x1, y1)
```

Arguments

X	Numeric. The x-coordinate of the first point.
У	Numeric. The y-coordinate of the first point.
x1	Numeric. The x-coordinate of the second point.
y1	Numeric. The y-coordinate of the second point.

Value

Numeric. The Euclidean distance between the two points.

Examples

```
\# Calculate the distance between points (5, 5) and (4, 4) dista(5, 5, 4, 4)
```

dom_trees

Identify Dominant Trees in a Plot Area

Description

This function identifies the dominant trees in a specified plot area by selecting the 100 thickest trees based on their diameters. Dominant trees are classified as those whose diameters fall within the top 100 in the given plot area.

Usage

```
dom_trees(x, y)
```

Arguments

x Numeric vector. A vector of tree diameters measured in centimeters.

y Numeric variable. The total plot area in square meters.

Value

Character vector. A vector of the same length as 'x', where each entry is labeled as "dom_tree" for dominant trees and "not_dom" for non-dominant trees.

d_dom 11

Examples

```
# Example tree diameters
x <- c(10, 20, 30, 40, 50, 25, 30, 22, 11, 10)
# Specify the plot area
y <- 1000
# Identify dominant trees
dom_trees(x, y)</pre>
```

 d_dom

Dominant Tree Diameter

Description

This function calculates the dominant tree diameter, defined as the mean diameter at breast height (dbh) of the 100 thickest trees within a specified plot area. It considers the tree diameters provided and determines which trees qualify as dominant based on their thickness.

Usage

```
d_dom(d, ps)
```

Arguments

d Numeric vector. A vector of tree diameters (in centimeters).ps Numeric variable. The plot area (in square meters).

Value

Numeric value representing the mean diameter at breast height of the dominant trees (in centimeters).

```
# Example tree diameters and plot area d <- c(12, 25, 40, 40, 55, 35, 35, 25, 12, 15) ps <- 400  
# Calculate the dominant tree diameter d_dom(d, ps)
```

12 g

ForestSDC Forest stand Structure, tree Diversity, and species Composition

Description

The ForestSDC package is a comprehensive tool set for analyzing data from forest inventories and permanent research plots. It includes functions to estimate structural indices, biodiversity metrics, and the nearest neighbor summary statistics. These tools are essential for assessing forest dynamics, biodiversity, and ecosystem health.

Details

Key features include:

- Structural indices such as Shannon's diversity, Simpson's complement, and species richness.
- Spatial analysis using nearest-neighbor methods.
- Customization tools for biodiversity and forest dynamics evaluation.

The package leverages dplyr and tidyr for data manipulation and FNN for efficient nearest-neighbor calculations.

Author(s)

Ernesto Rubio <ernestorub@gmail.com>

g

Basal Area from Tree Diameter

Description

This function calculates the basal area of a tree based on its diameter at breast height (DBH). The formula used is $g=\frac{\pi}{4}\times\left(\frac{d}{100}\right)^2$, where d is the diameter in centimeters.

Usage

g(x)

Arguments

х

Numeric variable. Tree diameter in centimeters.

Value

Numeric variable. Basal area in square meters.

Examples

```
x <- 25
```

g(x) # Calculates the basal area for a tree with a 25 cm diameter.

Gha 13

Gha

Calculate Basal Area per Hectare (G/ha)

Description

This function calculates the basal area per hectare (G/ha) using the formula:

$$G/ha = \frac{\sum g}{A} \times 10000$$

where:

- $\sum g$ is the sum of the basal area of individual trees.
- A is the plot area in square meters.

Usage

```
Gha(x, y)
```

Arguments

x Numeric vector. A vector of tree diameters (e.g., in cm).

y Numeric. The plot area (e.g., in square meters).

Value

Numeric. The basal area per hectare (G/ha).

Examples

```
x \leftarrow c(10, 20, 30, 40, 50, 25, 30, 22, 11, 10)

y \leftarrow 1000

Gha(x, y)
```

h_dom

Dominant Tree Height (Mean Height of the 100 Thickest Trees in a Hectare)

Description

This function calculates the dominant tree height, which is the mean height of the 100 thickest trees in a specified plot area, based on their diameters.

Usage

```
h_dom(h, d, ps)
```

14 margalef

Arguments

h	Numeric vector. Tree heights (in centimeters).
d	Numeric vector. Tree diameters (in centimeters).
ps	Numeric variable. Plot area (in square meters).

Value

Numeric value representing the dominant tree height, which is the mean height of the 100 thickest trees

Examples

margalef

Margalef's Species Richness Index

Description

This function calculates Margalef's species richness index, which is an indicator of the species richness in a given sample. The index is based on the number of species and the total number of individuals. It is calculated using the following formula:

Usage

```
margalef(x)
```

Arguments

Χ

A numeric or factor variable representing the species or individuals in a sample.

Details

$$D = \frac{S - 1}{\log(N)}$$

where:

- S is the number of unique species in the sample,
- ullet N is the total number of individuals in the sample.

Value

A numeric value representing Margalef's species richness index.

menhinick 15

Examples

```
x \leftarrow c("P. patula", "A. religiosa", "A. religiosa", "Q. castanea", "P. patula") margalef(x)
```

menhinick

Menhinick's Species Richness Index

Description

This function calculates Menhinick's species richness index, which is another measure of species diversity in a given sample. The index is calculated using the following formula:

Usage

menhinick(x)

Arguments

Х

A numeric or factor variable representing the species or individuals in a sample.

Details

$$D = \frac{S}{\sqrt{N}}$$

where:

- S is the number of unique species in the sample,
- $\bullet \ N$ is the total number of individuals in the sample.

Value

A numeric value representing Menhinick's species richness index.

```
x \leftarrow c("P. patula", "A. religiosa", "A. religiosa", "Q. castanea", "P. patula") menhinick(x)
```

nnss_circle

Nha

Number of Trees per Hectare

Description

This function calculates the number of trees per hectare based on the total number of trees in a given plot area. The index is calculated using the following formula:

Usage

```
Nha(x, y)
```

Arguments

x A numeric or character vector representing tree diameter or other tree attribute.

y A numeric variable representing the plot area in square meters.

Details

$$N = \frac{N_{\rm trees} \times 10000}{A}$$

where:

- N_{trees} is the total number of trees in the sample,
- A is the plot area in square meters.

Value

A numeric value representing the number of trees per hectare.

Examples

```
x <- c(10, 20, 30, 40, 50, 25, 30, 22, 11, 10)

y <- 1000

Nha(x, y)
```

nnss_circle

Calculate Nearest Neighbor Indices for Circular Plots

Description

This function calculates nearest neighbor indices for trees within a circular plot. It requires coordinates, tree diameter, height, and species information, and returns several indices related to tree competition and spacing.

Usage

```
nnss_circle(plot, x, y, sp, d, h, r, data = NULL)
```

nnss_square 17

Arguments

plot	A numeric or character variable representing the plot identifier.
x	A numeric vector of x-coordinates for each tree.
У	A numeric vector of y-coordinates for each tree.
sp	A factor or character vector representing tree species.
d	A numeric vector representing tree diameters.
h	A numeric vector representing tree heights.
r	A numeric value representing the radius of the circular plot (must be positive).
data	A data frame containing all the required columns (plot, x, y, sp, d, h).

Value

A data frame with calculated nearest neighbor indices for each tree. Columns include:

- Ui: Uniformity index
- Mi: Mixture index
- dDomi: Dominance based on diameter
- · hDomi: Dominance based on height
- dDif: Diameter difference
- hDif: Height difference
- NN1: Distance to the nearest neighbor

Examples

```
set.seed(42)
x <- runif(100, min = 1, max = 99)
y <- runif(100, min = 1, max = 99)
sp <- factor(sample(c("Pinus", "Quercus"), 100, replace = TRUE))
d <- runif(100, min = 7.5, max = 60)
h <- runif(100, min = 2, max = 40)
plot <- rep("P01", 100)
dataP01 <- data.frame(plot, x, y, sp, d, h)
nnss_circle(plot = plot, x = x, y = y, sp = sp, d = d, h = h, r = 50, data = dataP01)</pre>
```

nnss_square

Calculate Nearest Neighbor Indices for Square Plots

Description

This function calculates nearest neighbor indices for trees within a square plot. It requires coordinates, tree diameter, height, and species information, along with the plot's maximum x and y dimensions. The function returns several indices related to tree competition and spacing.

Usage

```
nnss_square(plot, x, y, sp, d, h, xmax, ymax, data = NULL)
```

18 pielou

Arguments

plot	A numeric or character variable representing the plot identifier.
X	A numeric vector of x-coordinates for each tree.
У	A numeric vector of y-coordinates for each tree.
sp	A factor or character vector representing tree species.
d	A numeric vector representing tree diameters.
h	A numeric vector representing tree heights.
xmax	A numeric value representing the maximum x-coordinate value for the plot.
ymax	A numeric value representing the maximum y-coordinate value for the plot.
data	A data frame containing all the required columns (plot, x, y, sp, d, h).

Value

A data frame with calculated nearest neighbor indices for each tree. Columns include:

• Ui: Uniformity index

· Mi: Mixture index

• dDomi: Dominance based on diameter

· hDomi: Dominance based on height

• dDif: Diameter difference

• hDif: Height difference

• NN1: Distance to the nearest neighbor

Examples

```
set.seed(42)
x <- runif(100, min = 1, max = 50)
y <- runif(100, min = 1, max = 50)
sp <- factor(sample(c("Pinus", "Quercus"), 100, replace = TRUE))
d <- runif(100, min = 7.5, max = 60)
h <- runif(100, min = 2, max = 40)
plot <- rep("P01", 100)
dataP01 <- data.frame(plot, x, y, sp, d, h)
nnss_square(plot = plot, x = x, y = y, sp = sp, d = d, h = h, xmax = 50, ymax = 50, data = dataP01)</pre>
```

pielou

Calculate Pielou's Equitativity Index

Description

This function calculates Pielou's equitativity index, which measures the evenness of species distribution in a community. The formula is:

$$J' = \frac{H'}{\log(S)}$$

where:

- H' is the Shannon diversity index.
- S is the number of unique categories or species.

rich 19

Usage

```
pielou(x)
```

Arguments

Х

Numeric or factor variable. A vector representing species or categories.

Value

Numeric. The Pielou equitativity index.

Examples

```
x <- c("n", "m", "n", "n", "m")
pielou(x)</pre>
```

rich

Calculate Species Richness (S)

Description

This function calculates species richness (S), which represents the number of unique species or categories in the given data. The formula is:

$$S = \sum I(counts > 0)$$

where:

ullet counts represents the frequency of each unique species or category.

Usage

rich(x)

Arguments

Χ

Numeric or factor variable. A vector representing species or categories.

Value

Numeric. The species richness (S).

```
x <- c("n", "m", "n", "n", "m")
rich(x)</pre>
```

20 shannon

sdi

Calculate Stand Density Index (SDI)

Description

This function calculates the Stand Density Index (SDI) using the formula:

$$SDI = Nha \times \left(\frac{dg}{25.4}\right)^{1.605}$$

where:

- Nha is the number of trees per hectare.
- dg is the quadratic mean diameter (in cm).

Usage

```
sdi(x, y)
```

Arguments

x Numeric vector. A vector of tree diameters (e.g., in cm).

y Numeric. The plot area (e.g., in square meters).

Value

Numeric. The stand density index.

Examples

```
x \leftarrow c(10, 20, 30, 40, 50, 25, 30, 22, 11, 10)

y \leftarrow 1000

sdi(x, y)
```

shannon

Shannon's Entropy Index

Description

This function calculates Shannon's entropy index (H') for a given dataset. Shannon's entropy index measures the diversity in the dataset, considering both the richness (number of unique categories) and evenness (distribution of individuals).

Usage

shannon(x)

Arguments

Χ

A numeric or factor vector representing categories (e.g., species or groups).

shannon_evenness 21

Details

The formula is:

$$H' = -\sum_{i=1}^{S} p_i \log(p_i)$$

Where:

- p_i is the proportion of individuals belonging to the *i*-th category.
- ullet S is the total number of unique categories in the dataset.

Value

A numeric value representing Shannon's entropy index (H').

Examples

```
x <- c("n", "m", "n", "n", "m")
shannon(x)</pre>
```

shannon_evenness

Shannon's Evenness Index

Description

This function calculates Shannon's evenness index, which measures the evenness of the distribution of species (or any type of data) in a community. The formula used is:

Usage

shannon_evenness(x)

Arguments

х

A numeric or factor vector representing species or groups in the community.

Details

$$E_H = \frac{H'}{H_{\text{max}}}$$

where:

• H' is the Shannon diversity index:

$$H' = -\sum p_i \log(p_i)$$

with p_i being the proportion of individuals of species i.

• H_{max} is the maximum Shannon index for a given number of unique species S, and is given by $H_{\text{max}} = \log(S)$.

22 simpson_complement

Value

A numeric value representing Shannon's evenness index, which ranges from 0 (uneven) to 1 (perfectly even).

Examples

```
x <- c("n", "m", "n", "n", "m")
shannon_evenness(x)</pre>
```

simpson

Simpson's index.

Description

Simpson's index.

Usage

```
simpson(x)
```

Arguments

Х

Numeric or factor variable

Value

Numeric variable.

Examples

```
x <- c("n", "m", "n", "n", "m")
simpson(x)</pre>
```

simpson_complement

Simpson's Index Complement

Description

This function calculates the complement of Simpson's index (D'), a diversity measure that represents the probability of two randomly selected individuals belonging to different categories.

Usage

```
simpson_complement(x)
```

Arguments

Χ

A numeric or factor vector representing categories (e.g., species or groups).

simpson_complement 23

Details

The formula is:

$$D' = 1 - \sum_{i=1}^{S} p_i^2$$

Where:

- p_i is the proportion of individuals in the i-th category,
- ullet S is the total number of categories.

Value

A numeric value representing the complement of Simpson's index (D').

```
x \leftarrow c("n", "m", "n", "n", "m")

simpson\_complement(x)
```

Index

```
A_{index, 2}
A_{max}, 3
A_rel, 4
bal, 4
BALMOD, 5
ca, 6
Caha, 7
cat_d, 7
coordxy, 8
d_dom, 11
dg, 9
dista, 9
dom_trees, 10
ForestSDC, 12
ForestSDC-package (ForestSDC), 12
g, 12
Gha, 13
h_dom, 13
margalef, 14
menhinick, 15
Nha, 16
nnss_circle, 16
nnss_square, 17
pielou, 18
rich, 19
sdi, 20
shannon, 20
shannon\_evenness, \textcolor{red}{21}
\verb|simpson|, 22|
simpson_complement, 22
```