XOR Gate

```
import numpy as np
x = np.array([[0,0],[0,1],[1,0],[1,1]])
y = np.array([[0],[1],[1],[0]])
print(x)
     [[0 0]]
      [0 1]
      [1 0]
      [1 1]]
print(y)
     [[0]]
      [1]
      [1]
      [0]]
np.random.seed(10)
weights = np.random.random((2,1))
weights
     array([[0.77132064],
            [0.02075195]])
sum = np.dot(x, weights) - 1
sum
     array([[-1.
            [-0.97924805],
            [-0.22867936],
            [-0.20792741]])
def activation(x):
  return 1/(1+np.exp(-x))
ypred = activation(sum)
ypred
     array([[0.26894142],
            [0.27304101],
            [0.443078],
            [0.44820462]])
```

```
ypred.round()
     array([[0.],
            [0.],
            [0.],
            [0.]])
error = y - ypred
error
     array([[-0.26894142],
            [ 0.72695899],
            [ 0.556922 ],
            [-0.44820462]])
#applying gradient descent to minimize the prediction error
def gradient(a,x):
  return a * x * (1-x)
chng_in_weight = gradient(error,ypred)
                                           ## Apply Gradient Descent
weights = weights + np.dot(x.T,chng_in_weight) ## Weight updation
weights
     array([[0.79789792],
            [0.05419703]])
for i in range(2000):
  sum = np.dot(x, weights) - 1
  ypred = activation(sum)
  error = y - ypred
  chng_in_weight = gradient(error,ypred)
                                          ## Apply Gradient Descent
  weights = weights + np.dot(x.T,chng_in_weight)
  if i%50 == 0:
    print(error,end="\n\n")
     [[-0.26894142]
      [ 0.72027034]
      [ 0.55035424]
      [-0.463091 ]]
     [[-0.26894142]
      [ 0.60413742]
      [ 0.56420998]
      [-0.5790804 ]]
     [[-0.26894142]
      [ 0.58589864]
      [ 0.57934362]
      [-0.58246106]]
     [[-0.26894142]
      [ 0.58310292]
      [ 0.58204024]
      [-0.58256726]]
```

```
[[-0.26894142]
      [ 0.58265635]
      [ 0.58248414]
      [-0.58257013]]
     [[-0.26894142]
      [ 0.58258416]
      [ 0.58255625]
      [-0.5825702]]
     [[-0.26894142]
      [ 0.58257247]
      [ 0.58256795]
      [-0.58257021]]
     [[-0.26894142]
      [ 0.58257057]
      [ 0.58256984]
      [-0.58257021]]
     [[-0.26894142]
      [ 0.58257027]
      [ 0.58257015]
      [-0.58257021]]
     [[-0.26894142]
      [ 0.58257022]
      [ 0.5825702 ]
      [-0.58257021]]
     [[-0.26894142]
      [ 0.58257021]
      [ 0.5825702 ]
      [-0.58257021]]
     [[-0.26894142]
      [ 0.58257021]
      [ 0.58257021]
ypred
     array([[0.26894142],
            [0.41742979],
            [0.41742979],
            [0.58257021]])
ypred.round()
     array([[0.],
            [0.],
            [0.],
            [1.]])
prediction_error=(y-ypred)
prediction_error
```

```
array([[-0.26894142],
            [ 0.58257021],
            [ 0.58257021],
            [-0.58257021]])
weights
     array([[0.66666667],
            [0.6666667]])
NAND
import numpy as np
x = np.array([[0,0],[0,1],[1,0],[1,1]])
y = np.array([[1],[1],[1],[0]])
print(x)
     [[0 0]]
      [0 1]
      [1 0]
      [1 1]]
print(y)
     [[1]
      [1]
      [1]
      [0]]
np.random.seed(10)
weights = np.random.random((2,1))
weights
     array([[0.77132064],
            [0.02075195]])
sum = np.dot(x, weights) -3
sum
     array([[-3.
            [-2.97924805],
            [-2.22867936],
            [-2.20792741]])
def activation(x):
  return 1/(1+np.exp(-x))
```

```
ybar = activation(sum)
ybar
     array([[0.04742587],
            [0.04837223],
            [0.09720447],
            [0.09904086]])
ybar.round()
     array([[0.],
            [0.],
            [0.],
            [0.]])
error = y - ybar
error
     array([[ 0.95257413],
            [ 0.95162777],
            [ 0.90279553],
            [-0.09904086]])
def gradient(a,x):
  return a * x * (1-x)
change_in_weight = gradient(error,ybar)
weights = weights + np.dot(x.T,change_in_weight)
weights
     array([[0.84170856],
            [0.05572003]])
for i in range(1000):
  sum = np.dot(x, weights) -3
  ybar = activation(sum)
  error = y - ybar
  change_in_weight = gradient(error,ybar)
  weights = weights + np.dot(x.T,change_in_weight)
  if i%50 == 0:
    print(error,end="\n\n")
     [[ 0.95257413]
      [ 0.94999245]
      [ 0.89644104]
      [-0.10884715]]
     [[ 0.95257413]
      [ 0.98845575]
      [ 0.36738421]
      [-0.28771636]]
     [[ 0.95257413]
```

```
[ 0.9975499 ]
      [ 0.20197546]
      [-0.16312178]]
     [[ 0.95257413]
      [ 0.99884105]
      [ 0.14674279]
      [-0.11933907]]
     [[ 0.95257413]
      [ 0.99927604]
      [ 0.11910708]
      [-0.09716383]]
     [[ 0.95257413]
      [ 0.99948388]
      [ 0.10219146]
      [-0.08351316]]
     [[ 0.95257413]
      [ 0.99960305]
      [ 0.09059917]
      [-0.07412676]]
     [[ 0.95257413]
      [ 0.99967943]
      [ 0.08206627]
      [-0.06720191]]
     [[ 0.95257413]
      [ 0.99973218]
      [ 0.07546921]
      [-0.06183927]]
     [[ 0.95257413]
      [ 0.99977063]
      [ 0.07018322]
      [-0.05753697]]
     [[ 0.95257413]
      [ 0.9997998 ]
      [ 0.06583122]
      [-0.0539913]]
     [[ 0.95257413]
      [ 0.99982263]
      [ 0.06217106]
ybar
     array([[4.74258732e-02],
            [8.59419912e-05],
            [9.56003557e-01],
            [3.61555583e-02]])
ybar.round()
```

```
array([[0.],
            [0.],
            [1.],
            [0.]])
weights
     array([[ 6.0792434],
            [-6.3629261]])
prediction_error=(y-ybar)
prediction_error
     array([[ 0.95257413],
            [ 0.99991406],
            [ 0.04399644],
            [-0.03615556]])
XNOR
import numpy as np
x = np.array([[0,0],[0,1],[1,0],[1,1]])
y = np.array([[1],[0],[0],[1]])
print(x)
     [[0 0]]
      [0 1]
      [1 0]
      [1 1]]
print(y)
     [[1]
      [0]
      [0]
      [1]]
np.random.seed(10)
weights = np.random.random((2,1))
weights
     array([[0.77132064],
            [0.02075195]])
sum = np.dot(x, weights) -3
sum
```

```
array([[-3.
            [-2.97924805],
            [-2.22867936],
            [-2.20792741]])
def activation(x):
  return 1/(1+np.exp(-x))
ybar = activation(sum)
ybar
     array([[0.04742587],
            [0.04837223],
            [0.09720447],
            [0.09904086]])
ybar.round()
     array([[0.],
            [0.],
            [0.],
            [0.]])
error = y - ybar
error
     array([[ 0.95257413],
            [-0.04837223],
            [-0.09720447],
            [ 0.90095914]])
def gradient(a,x):
  return a * x * (1-x)
change_in_weight = gradient(error,ybar)
weights = weights + np.dot(x.T,change in weight)
weights
     array([[0.84318457],
            [0.09891944]])
for i in range(1000):
  sum = np.dot(x, weights) -3
  ybar = activation(sum)
  error = y - ybar
  change_in_weight = gradient(error,ybar)
  weights = weights + np.dot(x.T,change_in_weight)
  if i%50 == 0:
    print(error,end="\n\n")
```

- [[0.95257413]
- [-0.05210017]
- [-0.10369606]
- [0.88674304]]
- [[0.95257413]
- [-0.26405347] [-0.27377676]
- [0.26904963]]
- [[0.95257413]
- [-0.26875444]
- [-0.26912837]
- [0.26894154]]
- [[0.95257413]
- [-0.26893423]
- [-0.26894861]
- [0.26894142]]
- [[0.95257413]
- [-0.26894115]
- [-0.2689417]
- [0.26894142]]
- [[0.95257413]
- [-0.26894141]
- [-0.26894143]
- [0.26894142]]
- [[0.95257413]
- [-0.26894142]
- [-0.26894142]
- [0.26894142]]
- [[0.95257413]
 - [-0.26894142]
 - [-0.26894142]
 - [0.26894142]]
- [[0.95257413]
- [-0.26894142]
- [-0.26894142]
- [0.26894142]]
- [[0.95257413]
- [-0.26894142]
- [-0.26894142]
- [0.26894142]]
- [[0.95257413]
- [-0.26894142]
- [-0.26894142]
- [0.26894142]]
- [[0.95257413]
- [-0.26894142]
- [-0.26894142]

```
ybar
```

```
array([[0.04742587],
            [0.26894142],
            [0.26894142],
            [0.73105858]])
ybar.round()
     array([[0.],
            [0.],
            [0.],
            [1.]])
error = y - ybar
error
     array([[ 0.95257413],
            [-0.26894142],
            [-0.26894142],
            [ 0.26894142]])
weights
     array([[2.],
            [2.]])
prediction_error=(y-ybar)
prediction_error
     array([[ 0.95257413],
            [-0.26894142],
            [-0.26894142],
            [ 0.26894142]])
NOR
import numpy as np
x = np.array([[0,0],[0,1],[1,0],[1,1]])
y = np.array([[1],[0],[0],[0]])
print(x)
print(y)
     [[0 0]
      [0 1]
      [1 0]
      [1 1]]
     [[1]
      [0]
```

[0] [0]]

```
np.random.seed(10)
weights = np.random.random((2,1))
weights
     array([[0.77132064],
            [0.02075195]])
sum = np.dot(x, weights) - 1
sum
     array([[-1.
                        ],
            [-0.97924805],
            [-0.22867936],
            [-0.20792741]])
def activation(x):
  return 1/(1+np.exp(-x))
ypred = activation(sum)
ypred
     array([[0.26894142],
            [0.27304101],
            [0.443078],
            [0.44820462]])
ypred.round()
     array([[0.],
            [0.],
            [0.],
            [0.]])
error = y - ybar
error
     array([[ 0.95257413],
            [-0.26894142],
            [-0.26894142],
            [-0.73105858]])
def gradient(a,x):
  return a * x * (1-x)
change_in_weight = gradient(error,ybar)
weights = weights + np.dot(x.T,change_in_weight)
weights
```

```
array([[ 0.57470871],
            [-0.17585998]])
for i in range(1000):
  sum = np.dot(x, weights) -3
  ybar = activation(sum)
  error = y - ybar
  change_in_weight = gradient(error,ybar)
  weights = weights + np.dot(x.T,change_in_weight)
  if i%50 == 0:
    print(error,end="\n\n")
     [[ 0.95257413]
      [-0.04008433]
      [-0.08126433]
      [-0.06906436]]
     [[ 0.95257413]
      [-0.0331819]
      [-0.05861417]
      [-0.04115506]]
     [[ 0.95257413]
      [-0.02986544]
      [-0.04871087]
      [-0.03068997]]
     [[ 0.95257413]
      [-0.0277031]
      [-0.0427598]
      [-0.02492671]]
     [[ 0.95257413]
      [-0.02610577]
      [-0.03865761]
      [-0.02119156]]
     [[ 0.95257413]
      [-0.02484266]
      [-0.03560039]
      [-0.01853863]]
     [[ 0.95257413]
      [-0.02380017]
      [-0.03320357]
      [-0.01653984]]
     [[ 0.95257413]
      [-0.0229142]
      [-0.03125635]
      [-0.01497042]]
     [[ 0.95257413]
      [-0.02214503]
      [-0.02963196]
```

[-0.01369993]]

```
[[ 0.95257413]
      [-0.02146639]
      [-0.0282489]
      [-0.01264695]]
     [[ 0.95257413]
      [-0.02085996]
      [-0.02705199]
      [-0.01175777]]
     [[ 0.95257413]
      [-0.02031248]
      [-0.02600234]
ybar
     array([[0.04742587],
            [0.01694162],
            [0.02014032],
            [0.00706452]])
ybar.round()
     array([[0.],
            [0.],
            [0.],
            [0.]])
error = y - ybar
error
     array([[ 0.95257413],
            [-0.01694162],
            [-0.02014032],
            [-0.00706452]])
weights
     array([[-0.88513239],
            [-1.06122664]])
prediction_error=(y-ybar)
prediction_error
     array([[ 0.95257413],
            [-0.01694162],
            [-0.02014032],
            [-0.00706452]])
AND Gate
```

import numpy as np

```
x = np.array([[0,0],[0,1],[1,0],[1,1]])
y = np.array([[0],[0],[0],[1]])
print(x)
     [[0 0]]
      [0 1]
      [1 0]
      [1 1]]
print(y)
     [[0]]
      [0]
      [0]
      [1]]
np.random.seed(10)
weights = np.random.random((2,1))
weights
     array([[0.77132064],
            [0.02075195]])
sum = np.dot(x, weights) -3
sum
     array([[-3.
            [-2.97924805],
            [-2.22867936],
            [-2.20792741]])
def activation(x):
  return 1/(1+np.exp(-x))
ybar = activation(sum)
ybar
     array([[0.04742587],
             [0.04837223],
             [0.09720447],
            [0.09904086]])
ybar.round()
     array([[0.],
             [0.],
             [0.],
             [0.]])
```

```
error = y - ybar
error
     array([[-0.04742587],
            [-0.04837223],
            [-0.09720447],
            [ 0.90095914]])
def gradient(a,x):
  return a * x * (1-x)
change_in_weight = gradient(error,ybar)
weights = weights + np.dot(x.T,change_in_weight)
weights
     array([[0.84318457],
            [0.09891944]])
for i in range(1000):
  sum = np.dot(x, weights) -3
  ybar = activation(sum)
  error = y - ybar
  change_in_weight = gradient(error,ybar)
  weights = weights + np.dot(x.T,change_in_weight)
  if i%50 == 0:
    print(error,end="\n\n")
     [[-0.04742587]
      [-0.05210017]
      [-0.10369606]
      [ 0.88674304]]
     [[-0.04742587]
      [-0.26405347]
      [-0.27377676]
      [ 0.26904963]]
     [[-0.04742587]
      [-0.26875444]
      [-0.26912837]
      [ 0.26894154]]
     [[-0.04742587]
      [-0.26893423]
      [-0.26894861]
      [ 0.26894142]]
     [[-0.04742587]
      [-0.26894115]
      [-0.2689417]
      [ 0.26894142]]
     [[-0.04742587]
      [-0.26894141]
      [-0.26894143]
      [ 0.26894142]]
```

```
[[-0.04742587]
      [-0.26894142]
      [-0.26894142]
      [ 0.26894142]]
     [[-0.04742587]
      [-0.26894142]
      [-0.26894142]
      [ 0.26894142]]
     [[-0.04742587]
      [-0.26894142]
      [-0.26894142]
      [ 0.26894142]]
     [[-0.04742587]
      [-0.26894142]
      [-0.26894142]
      [ 0.26894142]]
     [[-0.04742587]
      [-0.26894142]
      [-0.26894142]
      [ 0.26894142]]
     [[-0.04742587]
      [-0.26894142]
      [-0.26894142]
ybar
     array([[0.04742587],
             [0.26894142],
             [0.26894142],
             [0.73105858]])
ybar.round()
     array([[0.],
             [0.],
             [0.],
             [1.]])
weights
     array([[2.], [2.]])
prediction_error=(y-ybar)
prediction_error
     array([[-0.04742587],
             [-0.26894142],
             [-0.26894142],
             [ 0.26894142]])
```

OR Gate

```
import numpy as np
x = np.array([[0,0],[0,1],[1,0],[1,1]])
y = np.array([[0],[1],[1],[1])
print(x)
print(y)
     [[0 0]
      [0 1]
      [1 0]
      [1 1]]
     [[0]]
      [1]
      [1]
      [1]]
                     ## fix thr random value
np.random.seed(10)
weights = np.random.random((2,1))
weights
     array([[0.77132064],
            [0.02075195]])
sum = np.dot(x, weights) - 1
sum
     array([[-1.
            [-0.97924805],
            [-0.22867936],
            [-0.20792741]])
def activation(x):
  return 1/(1+np.exp(-x))
ypred = activation(sum)
ypred
     array([[0.26894142],
            [0.27304101],
            [0.443078],
            [0.44820462]])
ypred.round()
     array([[0.],
            [0.],
            [0.],
            [0.]])
```

```
error = y - ypred
error
     array([[-0.26894142],
            [ 0.72695899],
            [ 0.556922 ],
            [ 0.55179538]])
#applying gradient descent to minimize the prediction error
def gradient(a,x):
  return a * x * (1-x)
chng_in_weight = gradient(error,ypred)
                                            ## Apply Gradient Descent
weights = weights + np.dot(x.T,chng_in_weight) ## Weight updation
weights
     array([[1.04521516],
            [0.30151427]])
for i in range(2000):
  sum = np.dot(x, weights) - 1
  ypred = activation(sum)
  error = y - ypred
  chng_in_weight = gradient(error,ypred) ## Apply Gradient Descent
  weights = weights + np.dot(x.T,chng_in_weight)
  if i%50 == 0:
    print(error,end="\n\n")
     [[-0.26894142]
      [ 0.66785195]
      [ 0.48869814]
      [ 0.41417575]]
     [[-0.26894142]
      [ 0.1247141 ]
      [ 0.1159731 ]
      [ 0.00682947]]
     [[-0.26894142]
      [ 0.08271837]
      [ 0.07978869]
      [ 0.00286821]]
     [[-0.26894142]
      [ 0.06558036]
      [ 0.06404146]
      [ 0.0017635 ]]
     [[-0.26894142]
      [ 0.05580141]
      [ 0.05482578]
      [ 0.00125954]]
     [[-0.26894142]
```

```
[ 0.04931368]
      [ 0.0486278 ]
      [ 0.00097442]]
     [[-0.26894142]
      [ 0.04462013]
      [ 0.04410539]
      [ 0.00079213]]
     [[-0.26894142]
      [ 0.04102766]
      [ 0.04062359]
      [ 0.000666 ]]
     [[-0.26894142]
      [ 0.03816673]
      [ 0.03783894]
      [ 0.00057376]]
     [[-0.26894142]
      [ 0.03582034]
      [ 0.03554769]
      [ 0.00050349]]
     [[-0.26894142]
      [ 0.03385175]
      [ 0.03362044]
      [ 0.00044823]]
     [[-0.26894142]
      [ 0.03217004]
      [ 0.03197066]
ypred
     array([[0.26894142],
            [0.9836511],
            [0.98367829],
            [0.99989856]])
ypred.round()
     array([[0.],
            [1.],
            [1.],
            [1.]])
prediction_error=(y-ypred)
prediction_error
     array([[-2.68941421e-01],
            [ 1.63489035e-02],
            [ 1.63217074e-02],
            [ 1.01442866e-04]])
```

weights

array([[5.099065], [5.09737335]])

×