

# *Computer Graphics*

*by Ruen-Rone Lee*  
**ICL/ITRI**



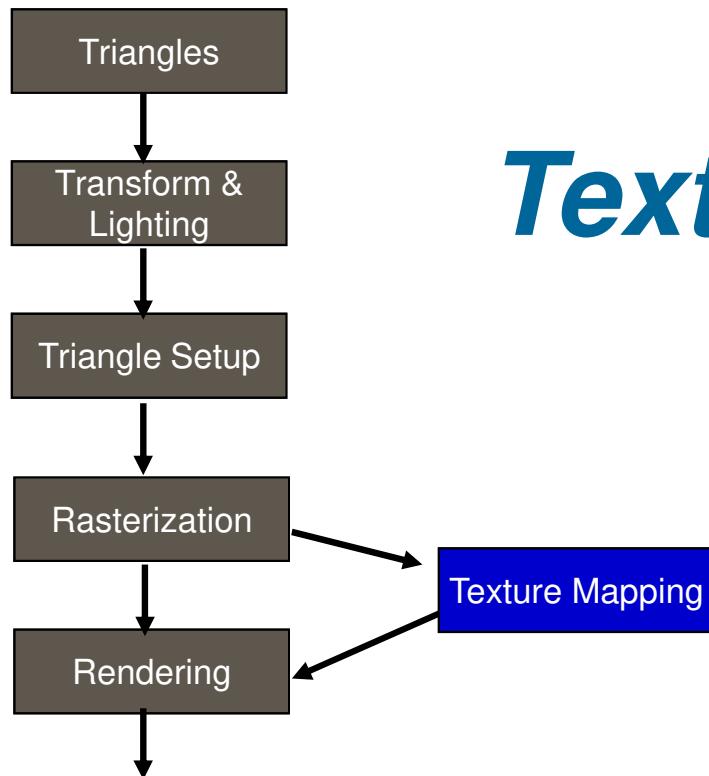
# *Wrap up from last course*

## ◆ **Hidden surface removal**

- Backface culling
- Z-buffer algorithm
- BSP tree
- Portal culling



# *Conventional 3D Graphics Pipeline*



## *Texture Mapping (A)*

*Concept of Texture Mapping  
Texture Filtering  
Texture Mapping Applications*

Conventional 3D Graphics Pipeline



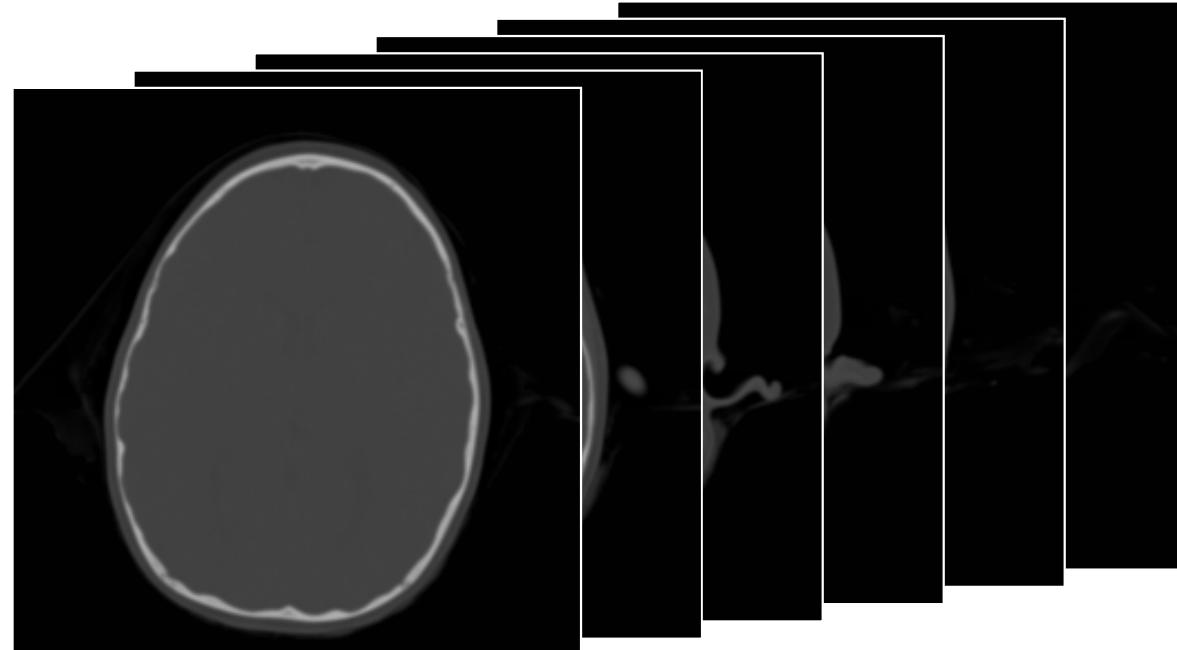
# *2D Textures*

- ◆ A 2D texture is a two-dimensional image
- ◆ Each texture element is called a texel

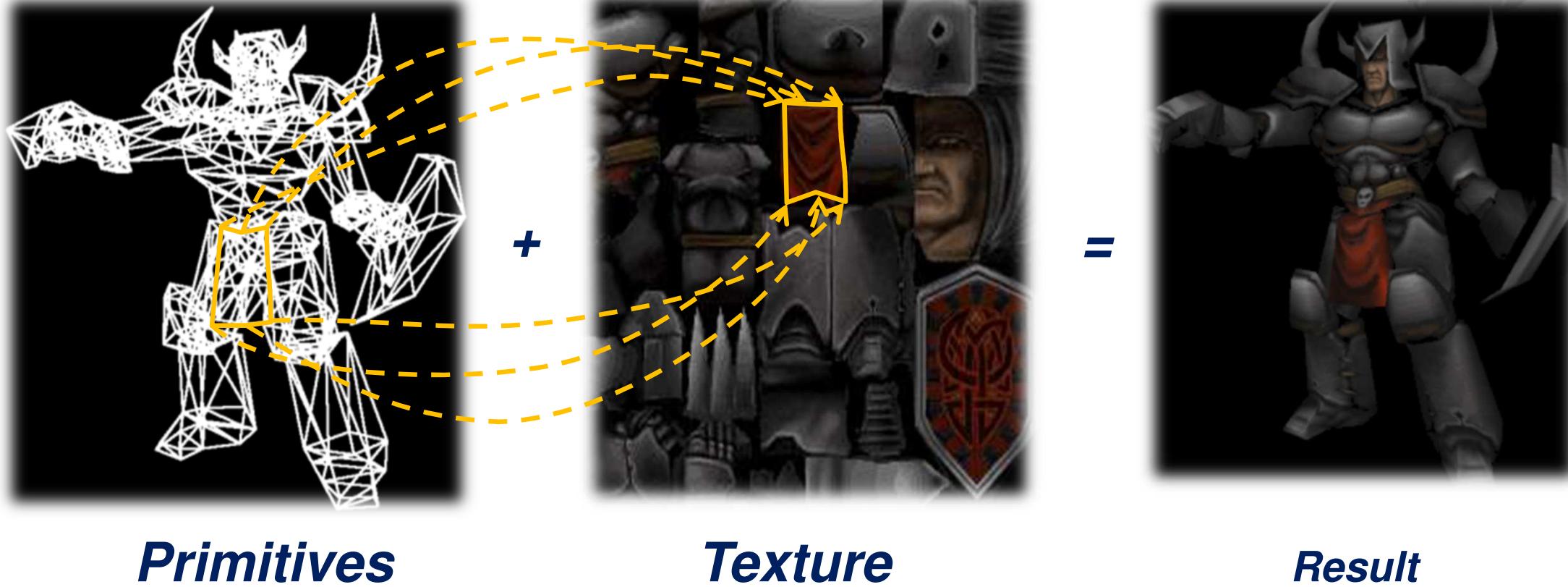


# *3D Textures*

- ◆ A 3D texture is a set of 2D textures that constitute a three-dimensional volume texture
- ◆ Each texture element is called a voxel

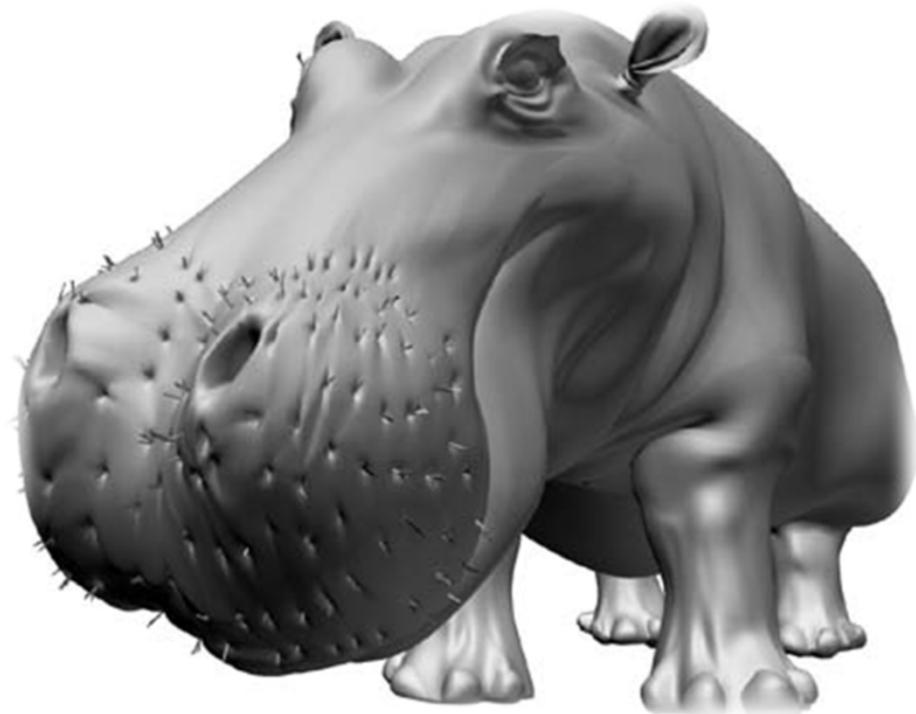


# *Texture Mapping*



# *Example of Texture Mapping*

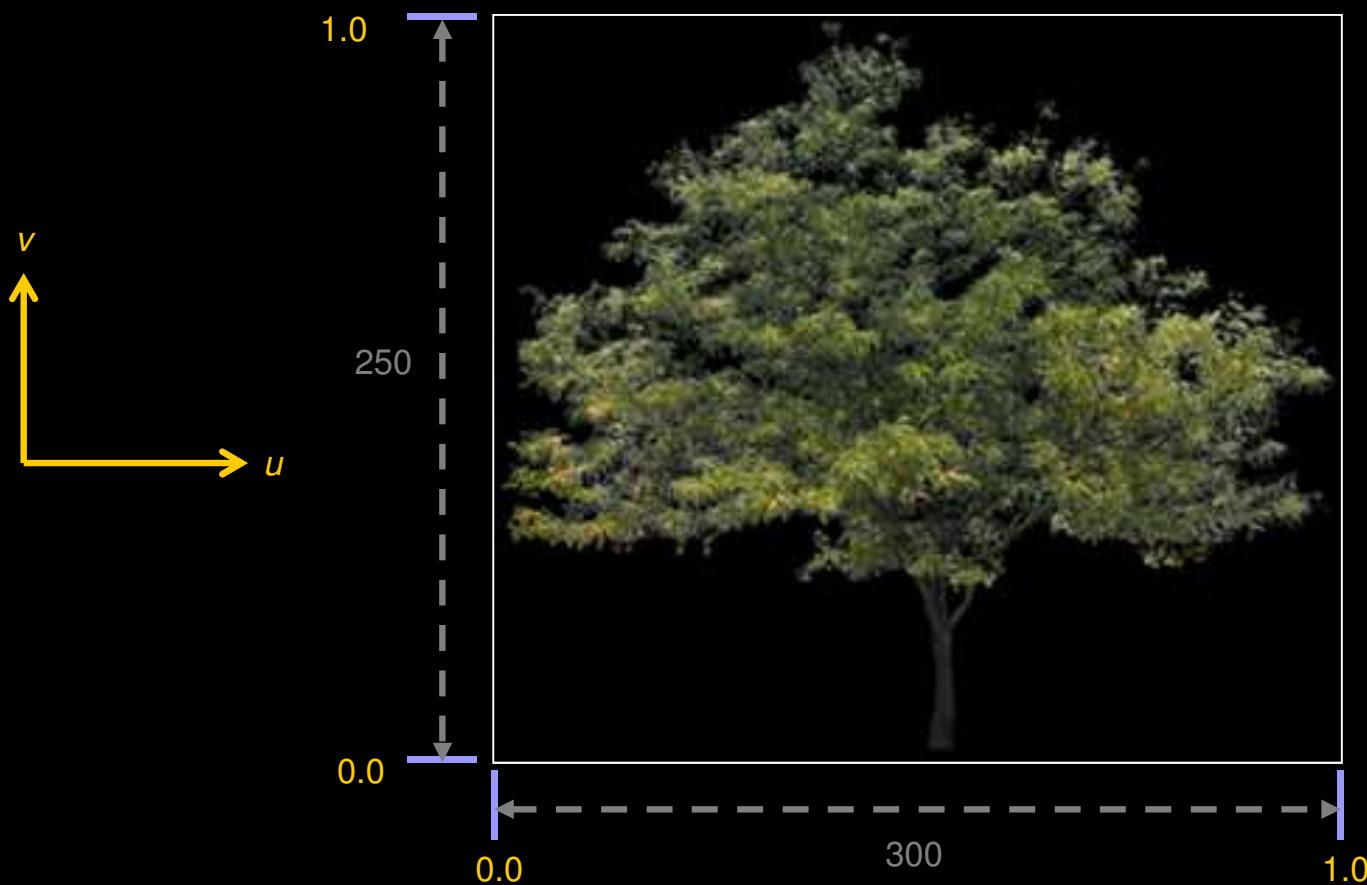
- ◆ Improve realism: not just texture but also lighting



Images from 3dRender.com

# *Texture Coordinates*

## ◆ Texture Coordinates



$$T_x = u \times (M_x - 1)$$

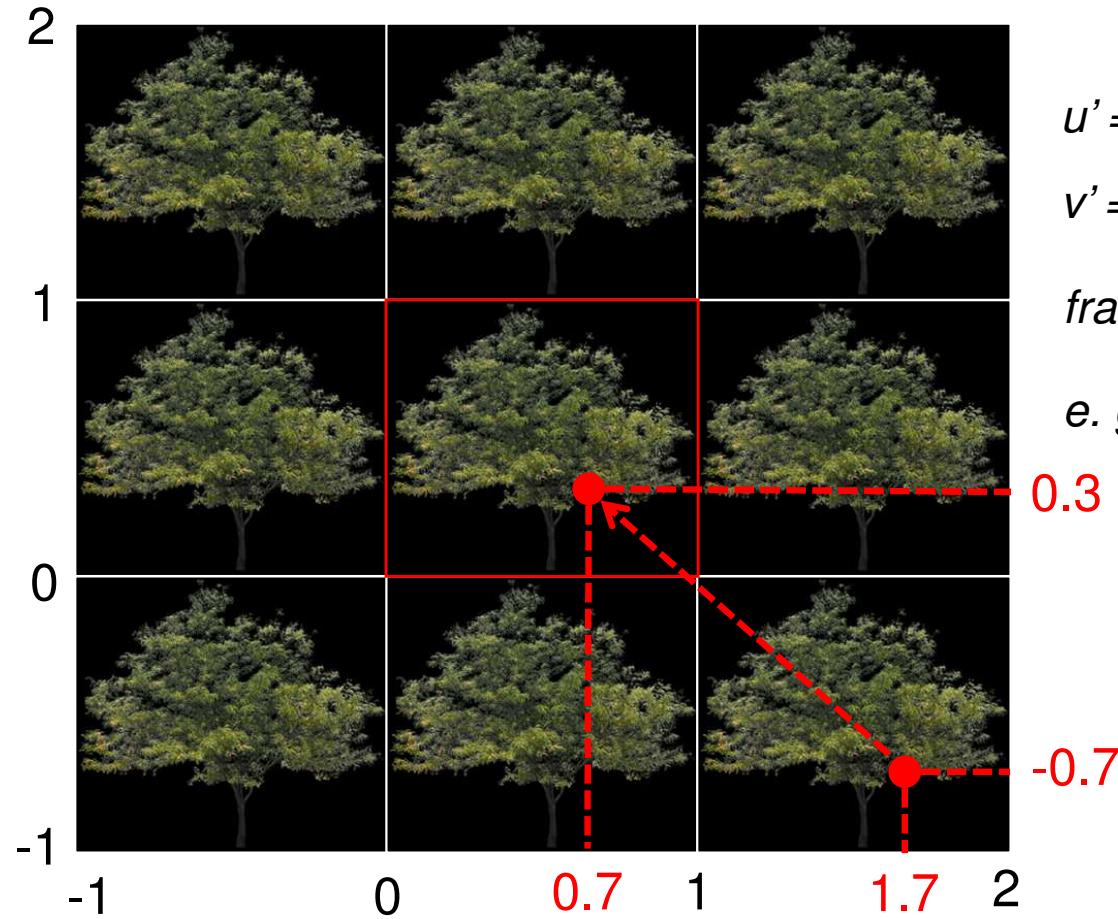
$$T_y = v \times (M_y - 1)$$

$T_x, T_y$ : output texel coord.  
 $u, v$ : texture coord.  
 $M_x, M_y$ : texture width/height



# Texture Coordinate Addressing Mode

## ◆ Repeat or Wrap Mode



$$u' = \text{frac}(u)$$

$$v' = \text{frac}(v)$$

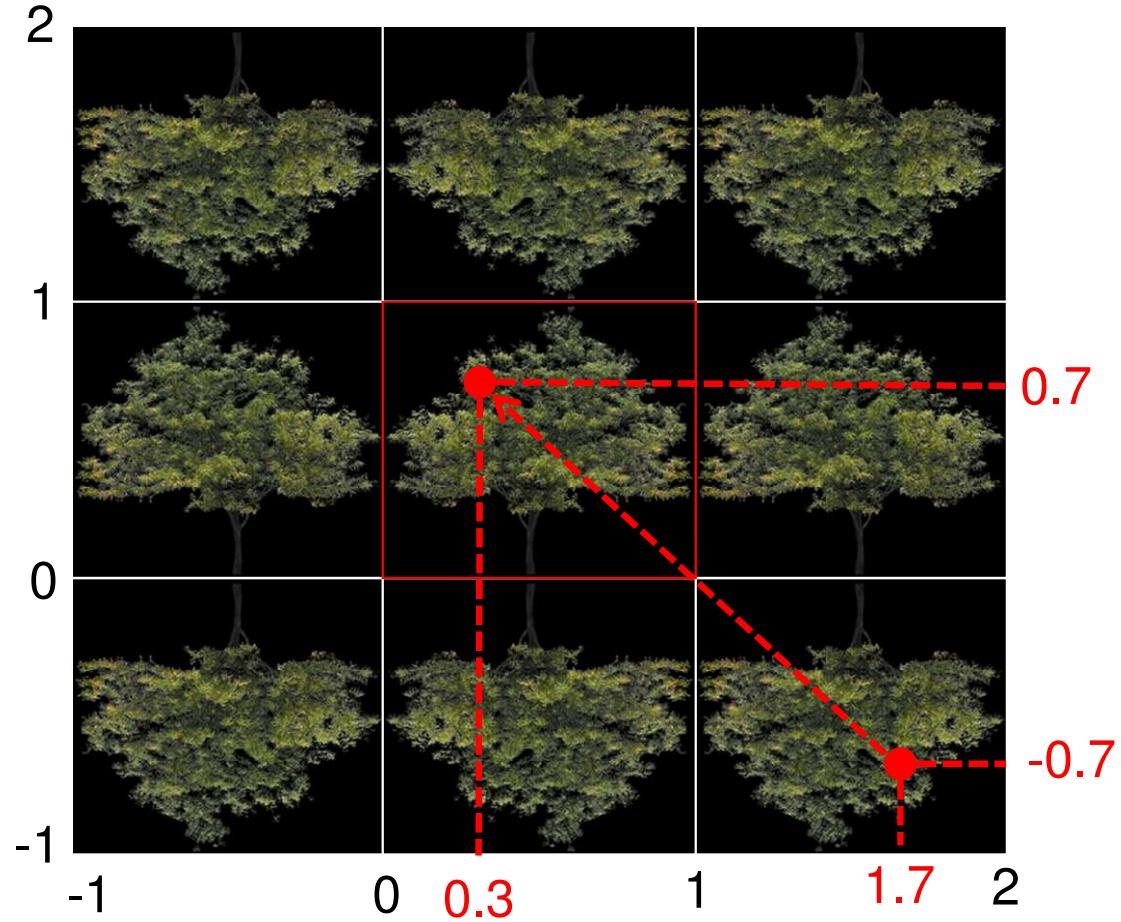
$$\text{frac}(x) = x - \lfloor x \rfloor$$

e. g.,  $(u, v) = (1.7, -0.7)$   
 $(u', v') = (0.7, 0.3)$



# Texture Coordinate Addressing Mode

## ◆ Mirror Mode



$$u' = \begin{cases} \text{frac}(u) & \text{if } \lfloor u \rfloor \text{ is even} \\ 1 - \text{frac}(u) & \text{if } \lfloor u \rfloor \text{ is odd} \end{cases}$$

$$v' = \begin{cases} \text{frac}(v) & \text{if } \lfloor v \rfloor \text{ is even} \\ 1 - \text{frac}(v) & \text{if } \lfloor v \rfloor \text{ is odd} \end{cases}$$

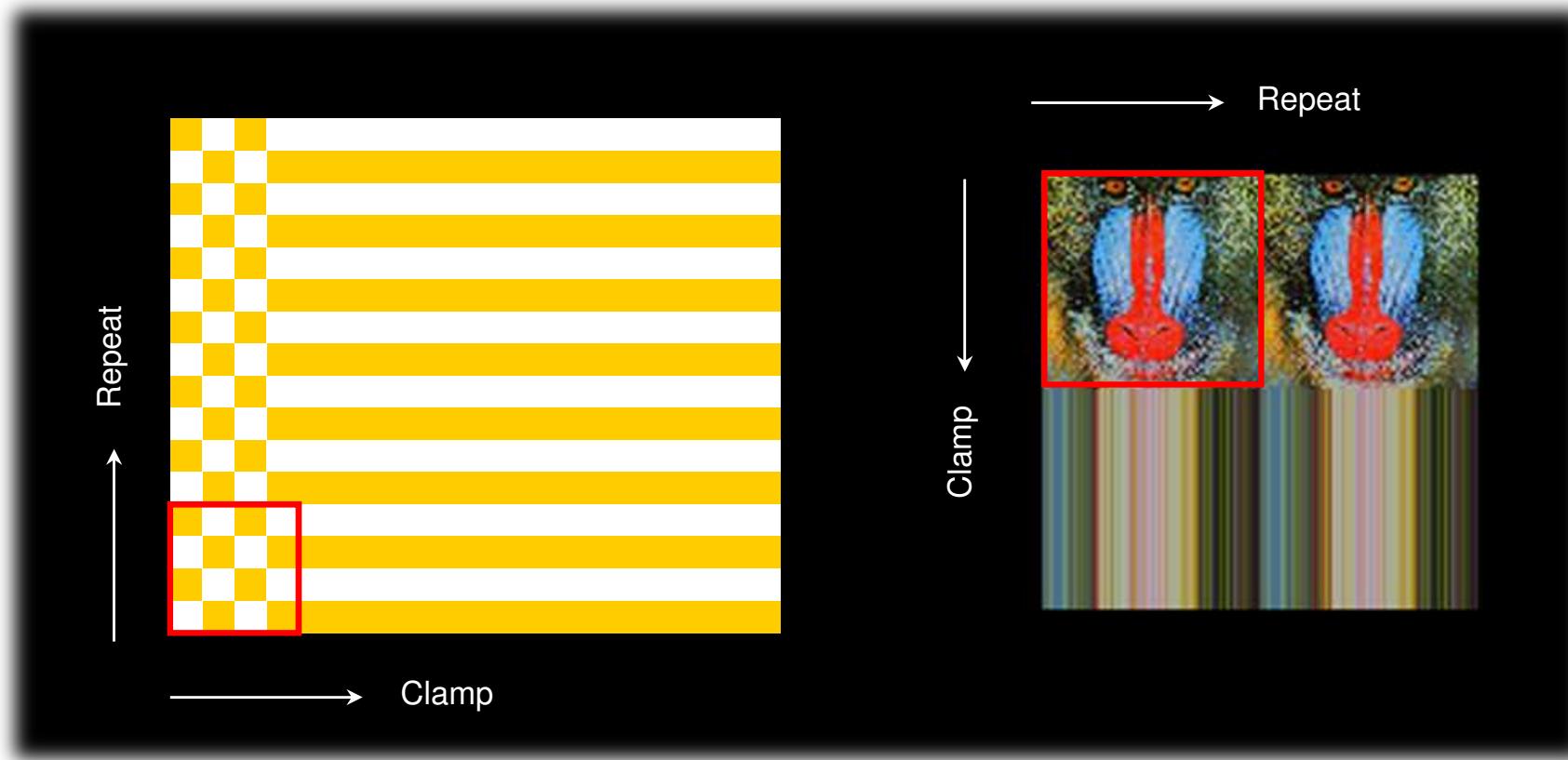
$$\text{frac}(x) = x - \lfloor x \rfloor$$

e. g.,  $(u, v) = (1.7, -0.7)$

$$(u', v') = (0.3, 0.7)$$

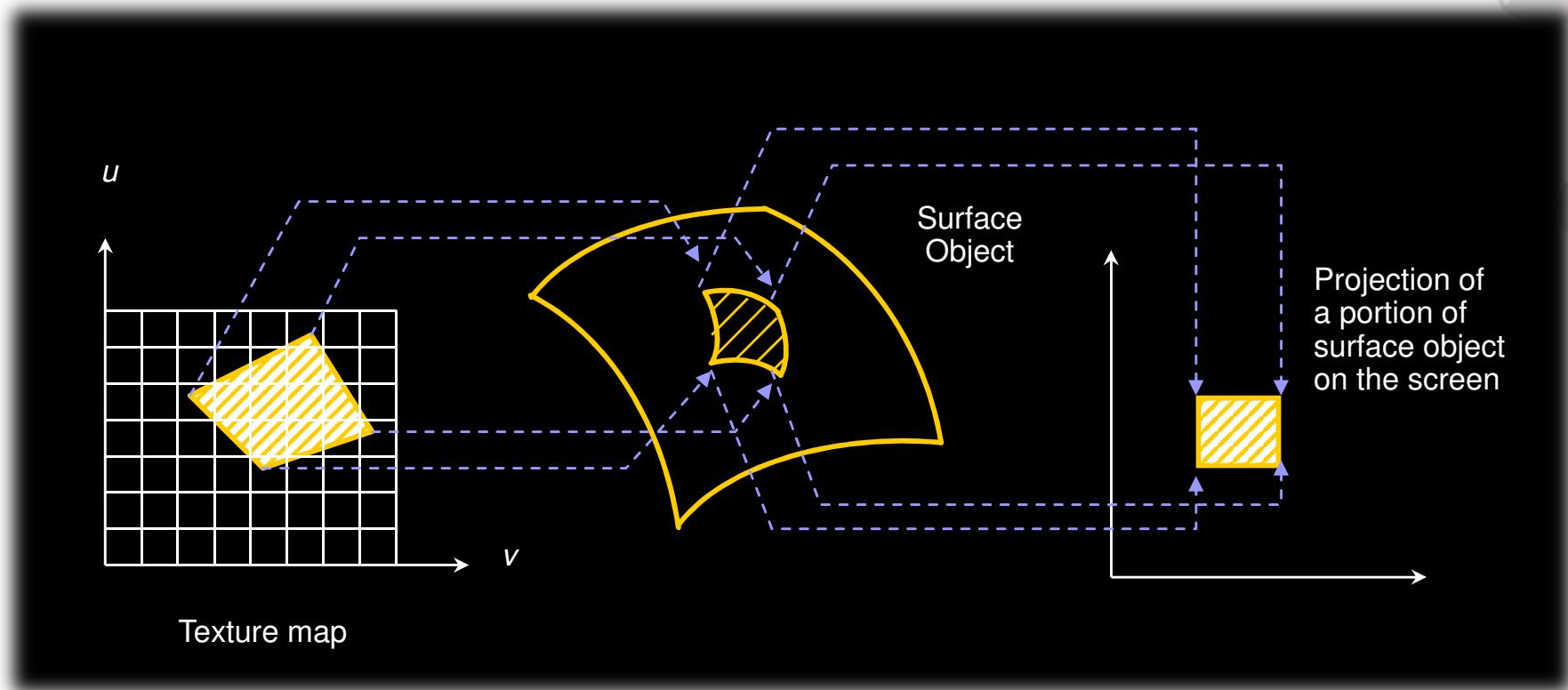
# *Texture Coordinate Addressing Mode*

## ◆ Clamp Mode



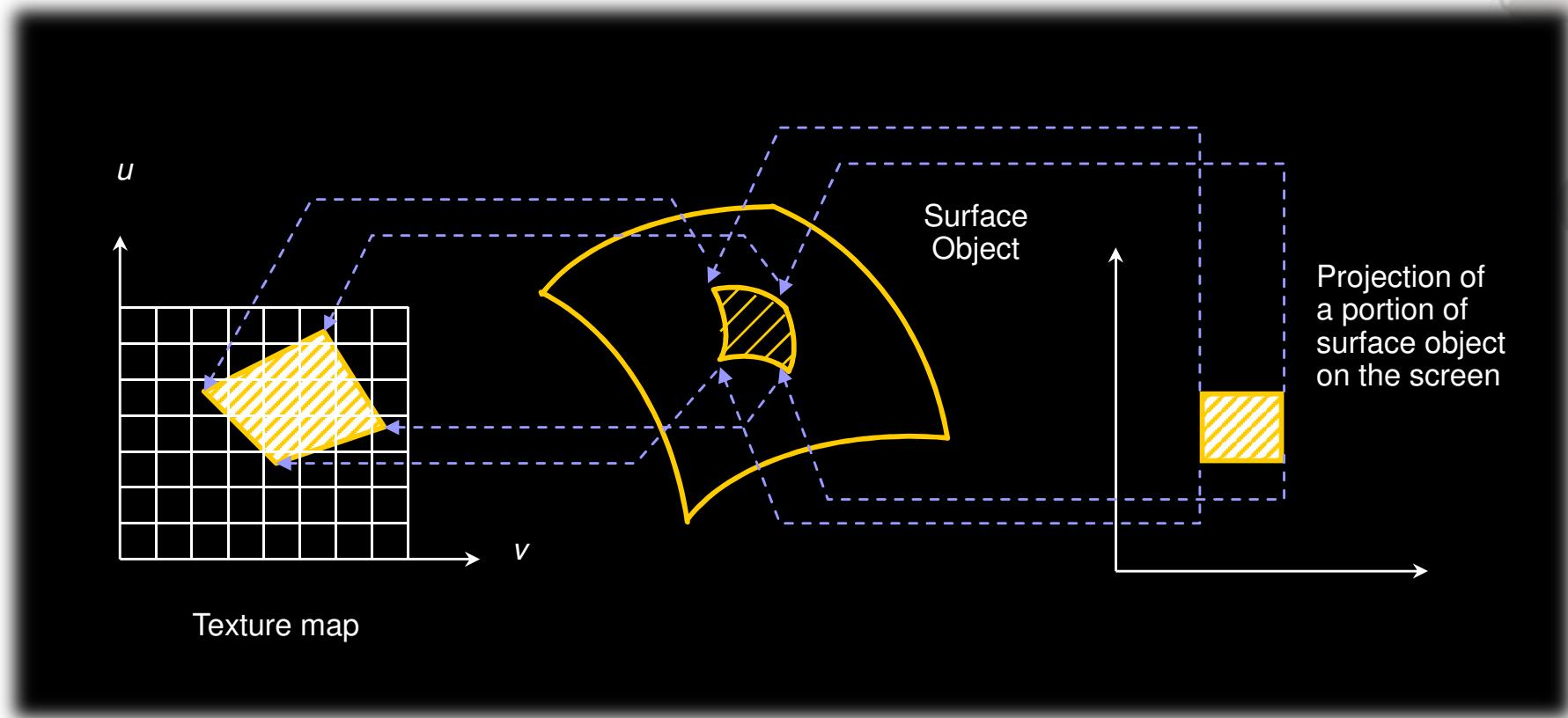
# *Principle of Texture Mapping*

## ◆ Forward Mapping



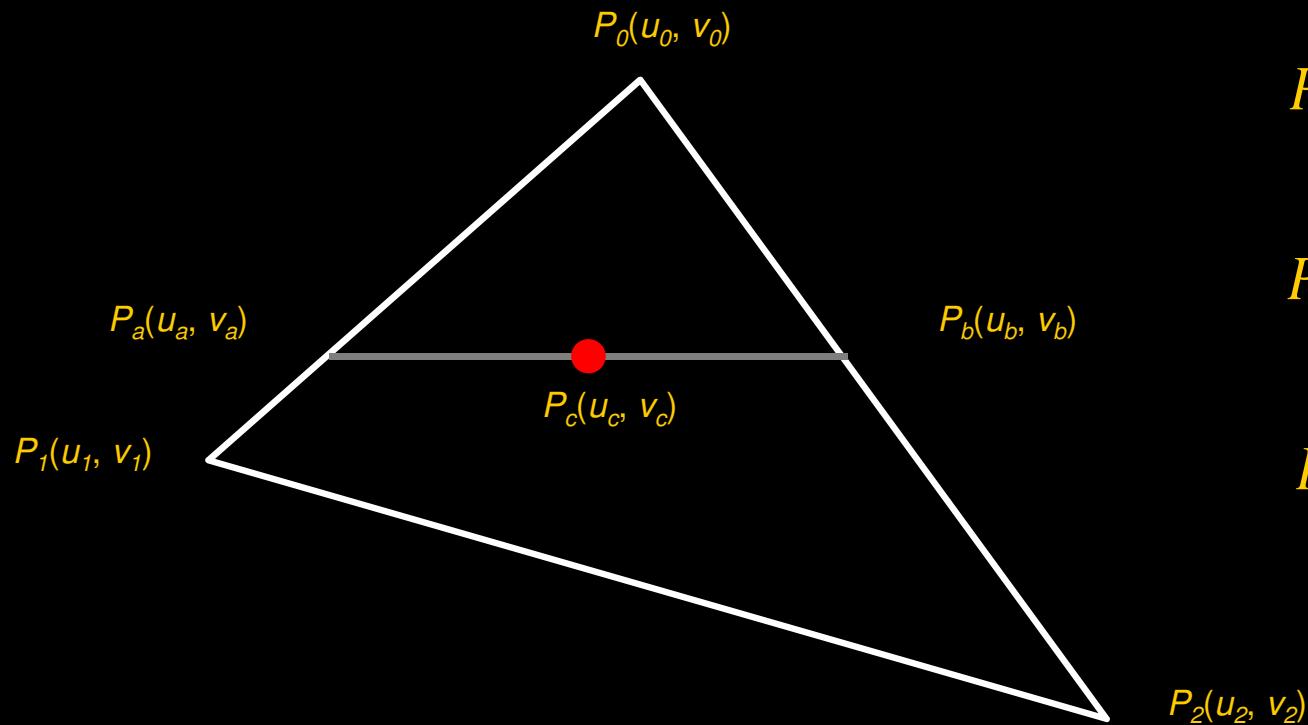
# *Principle of Texture Mapping*

## ◆ Backward Mapping



# Interpolating Texture Coordinates

- ◆ Similar to color or depth value interpolation



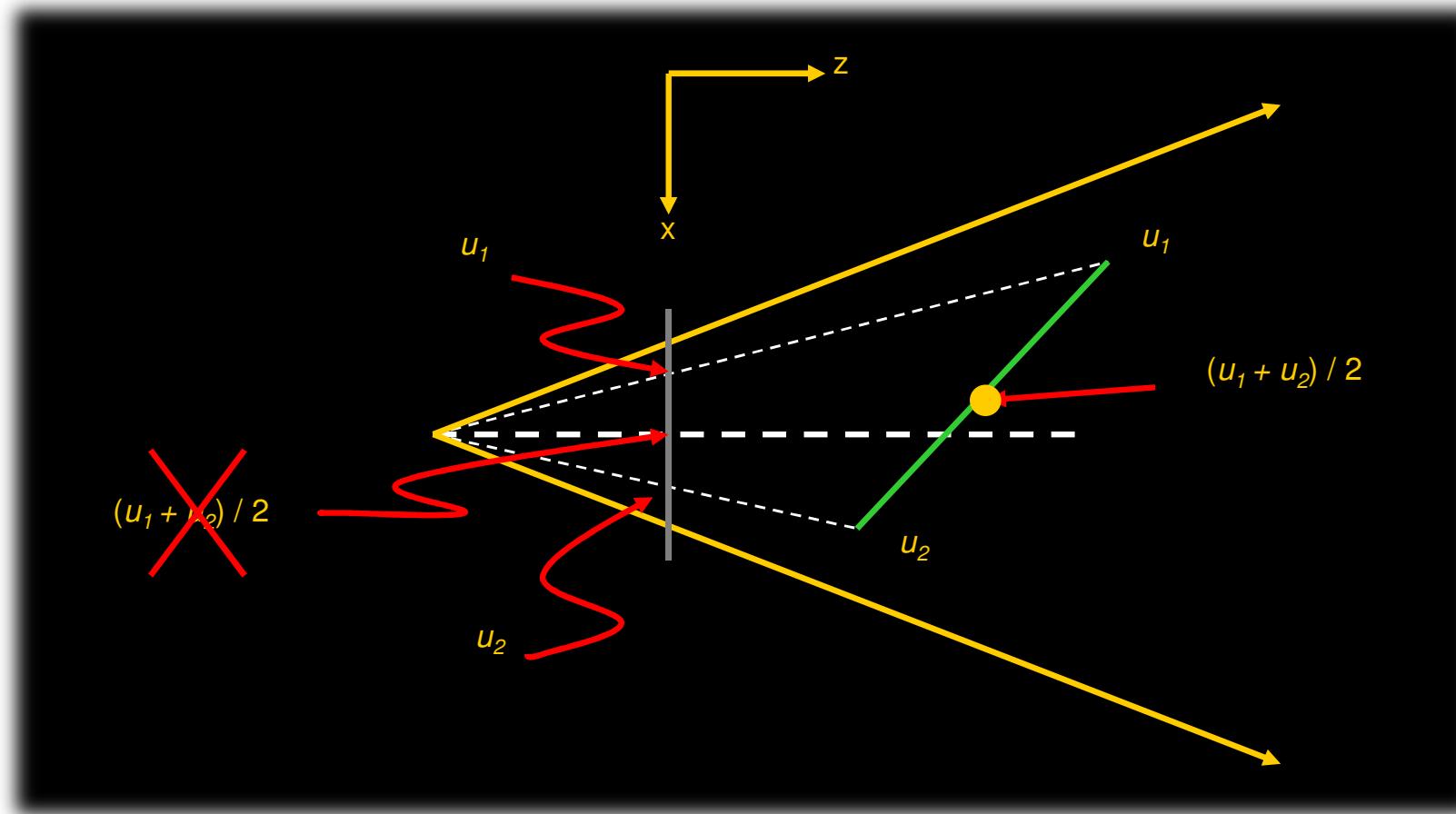
$$P_a = P_0 \left(1 - \frac{y_a - y_0}{y_1 - y_0}\right) + P_1 \frac{y_a - y_0}{y_1 - y_0}$$

$$P_b = P_0 \left(1 - \frac{y_b - y_0}{y_2 - y_0}\right) + P_2 \frac{y_b - y_0}{y_2 - y_0}$$

$$P_c = P_a \left(1 - \frac{x_c - x_a}{x_b - x_a}\right) + P_b \frac{x_c - x_a}{x_b - x_a}$$

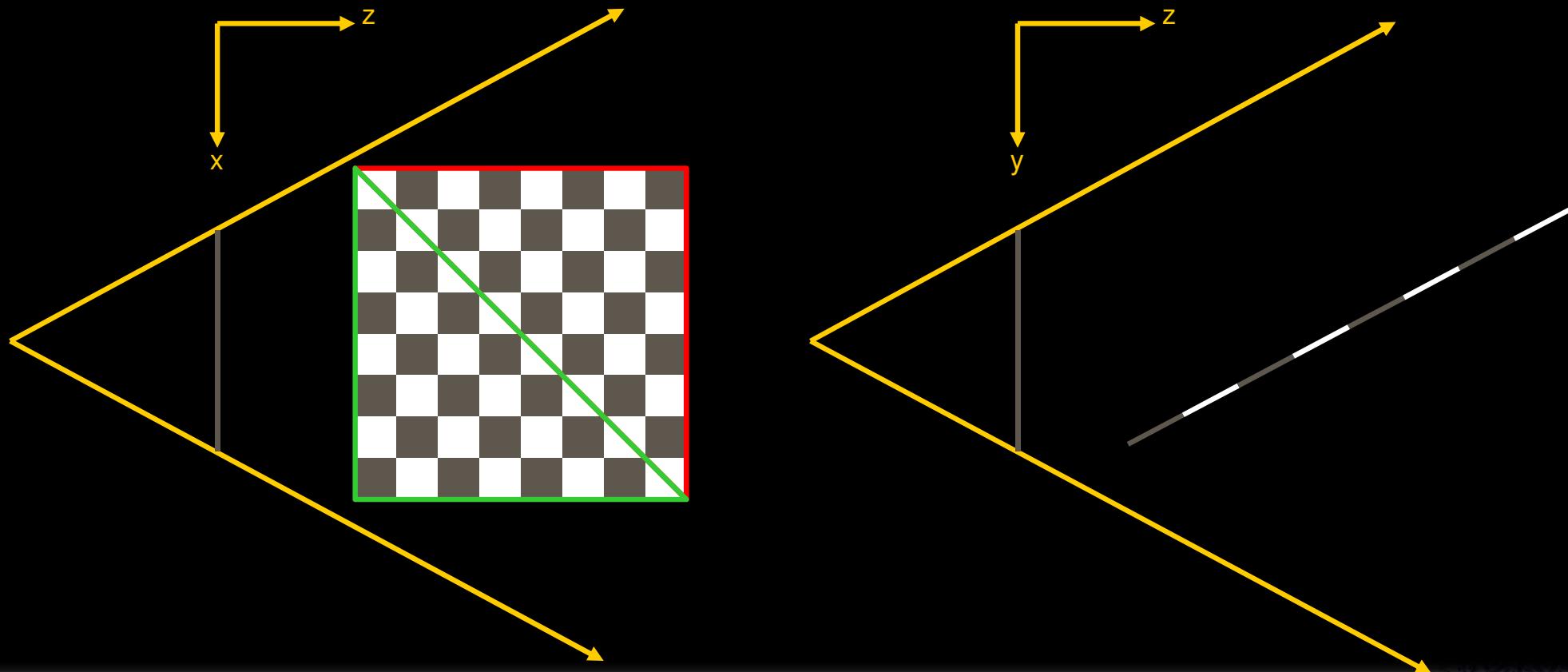
# Interpolating Texture Coordinates

- ◆ Linear interpolation in screen space does not imply linear interpolation in world space



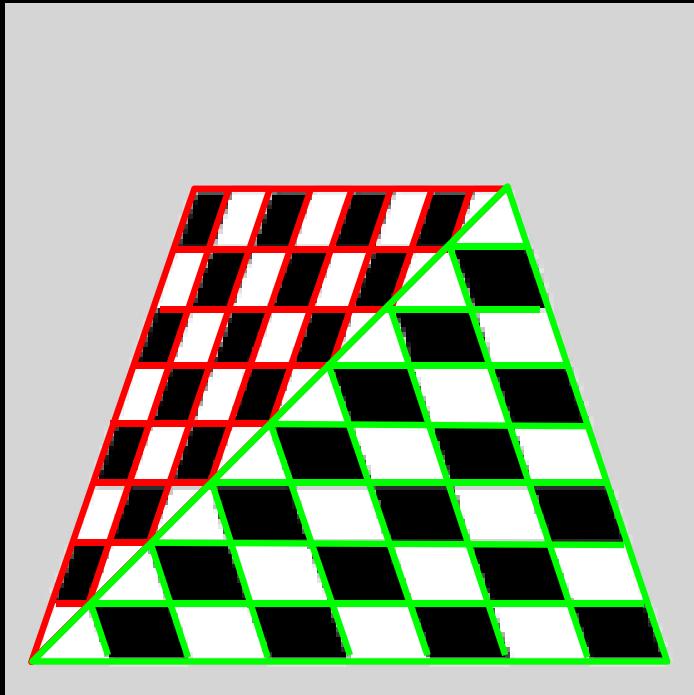
# *Interpolating Texture Coordinates*

- ◆ Example of using world space texture coordinates directly

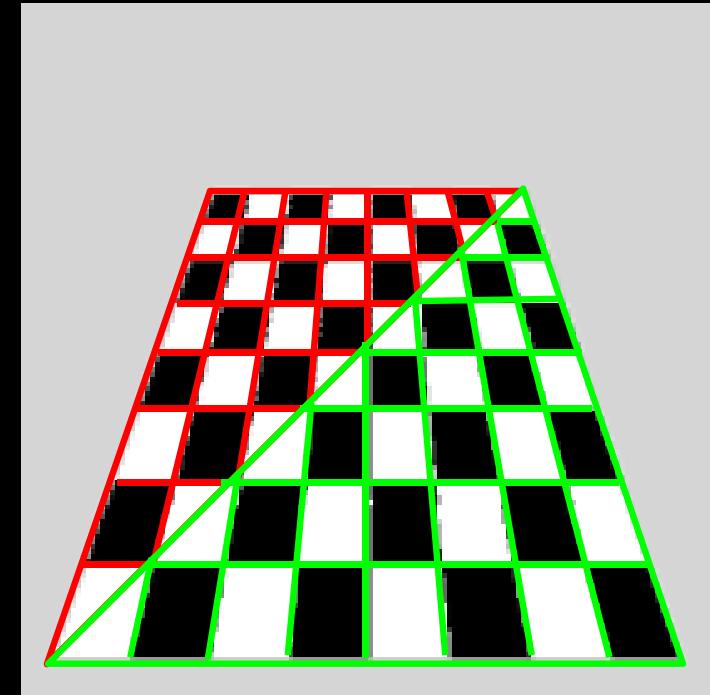


# *Interpolating Texture Coordinates*

- ◆ Result of using world space texture coordinates



Actual result from the screen



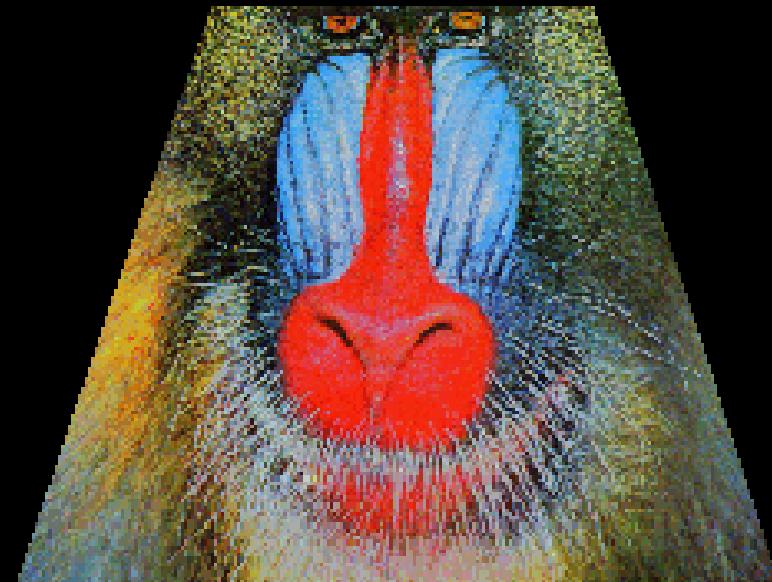
Expect to see on the screen

# *Interpolating Texture Coordinates*

- ◆ Another result of using world space texture coordinates



Actual result on the screen

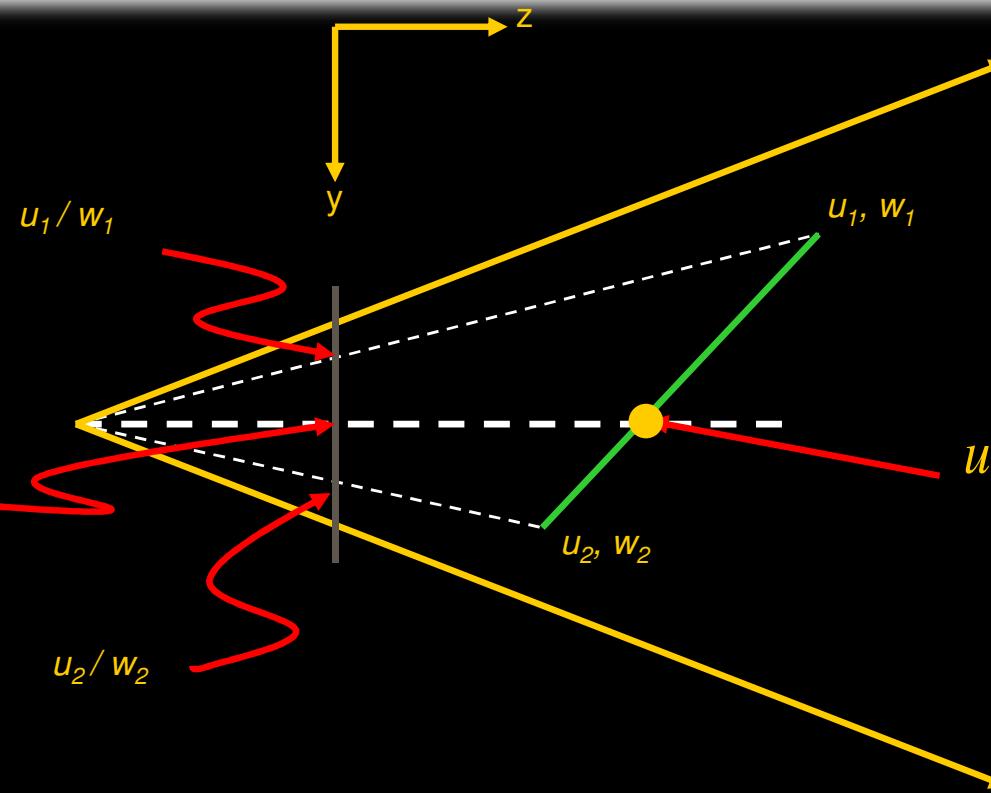


Expect to see on the screen

# Interpolating Texture Coordinates

- ◆ Using perspective correction to resolve the incorrect result of using world space texture coordinates

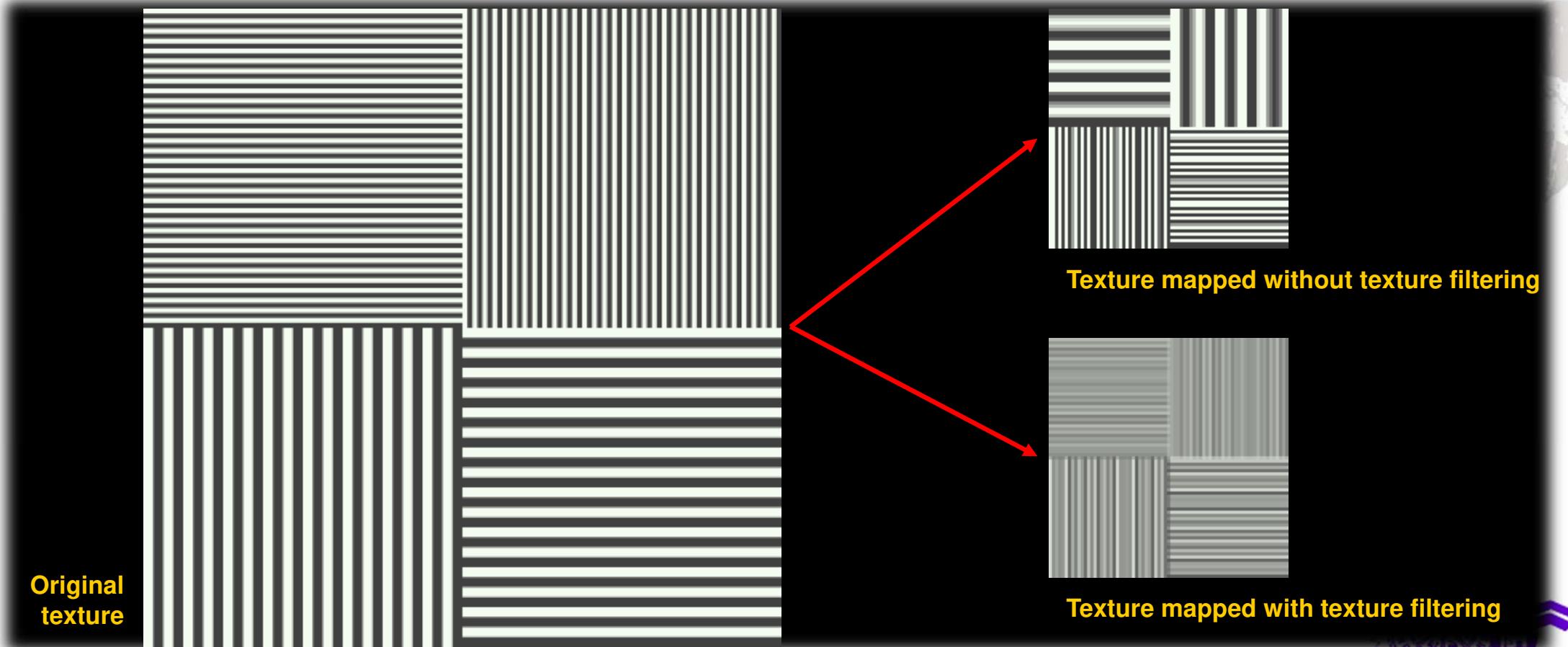
$$\frac{u_m}{w_m} = \frac{1}{2} \left( \frac{u_1}{w_1} + \frac{u_2}{w_2} \right)$$
$$\frac{1}{w_m} = \frac{1}{2} \left( \frac{1}{w_1} + \frac{1}{w_2} \right)$$



$$u_m = \frac{\frac{1}{2} \left( \frac{u_1}{w_1} + \frac{u_2}{w_2} \right)}{\frac{1}{2} \left( \frac{1}{w_1} + \frac{1}{w_2} \right)} = \frac{u_1 w_2 + u_2 w_1}{w_1 + w_2}$$

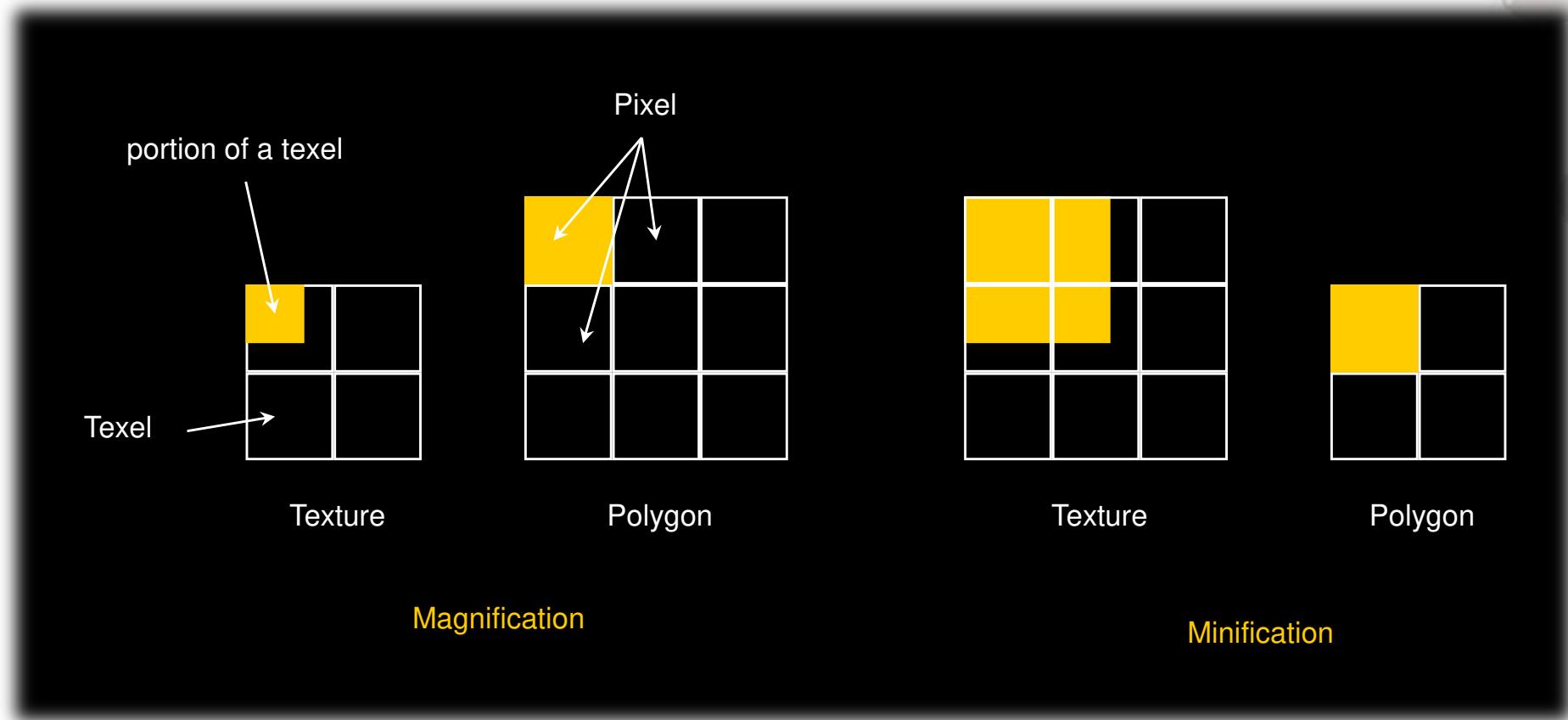
# *Texture Filtering*

- ◆ Why need texture filtering?
  - A method to resolve texture aliasing



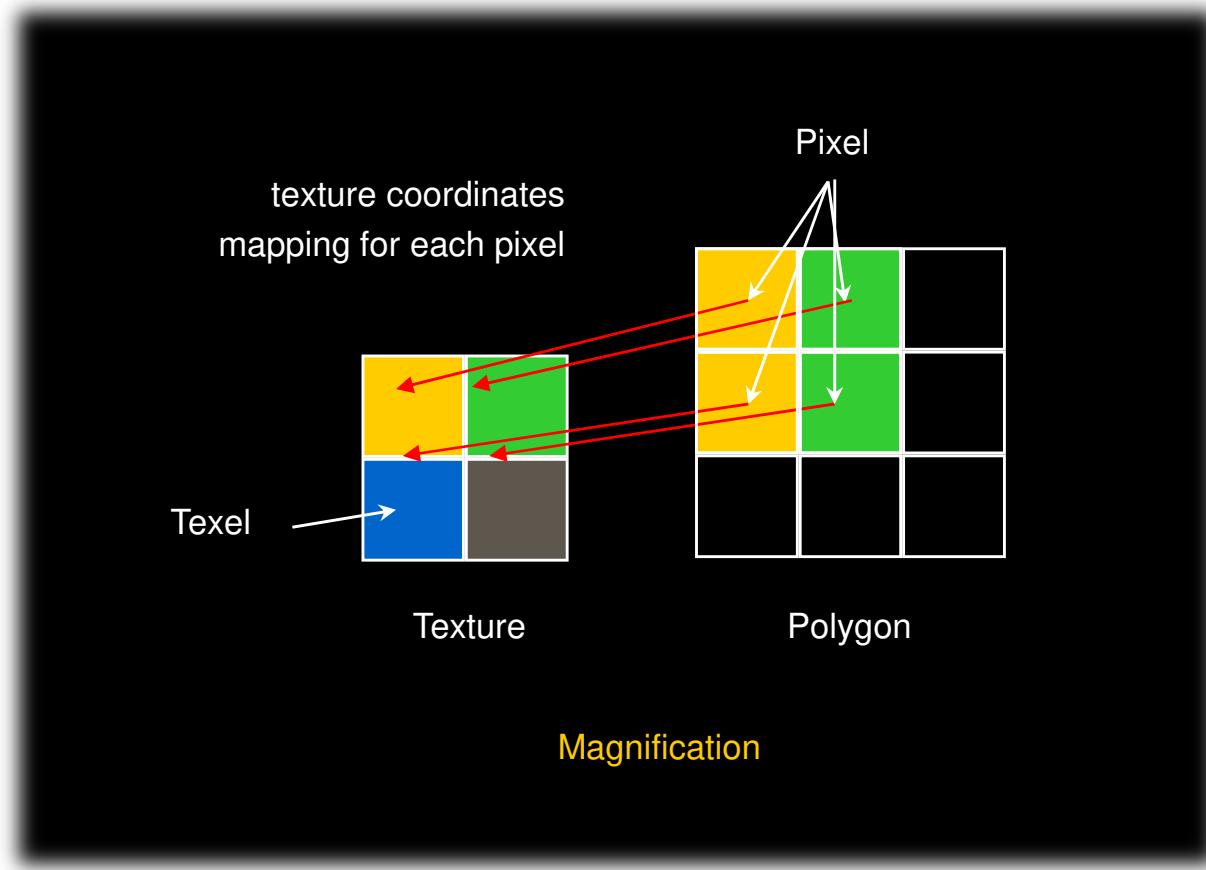
# *Texture Filtering*

## ◆ Texture Filtering Modes



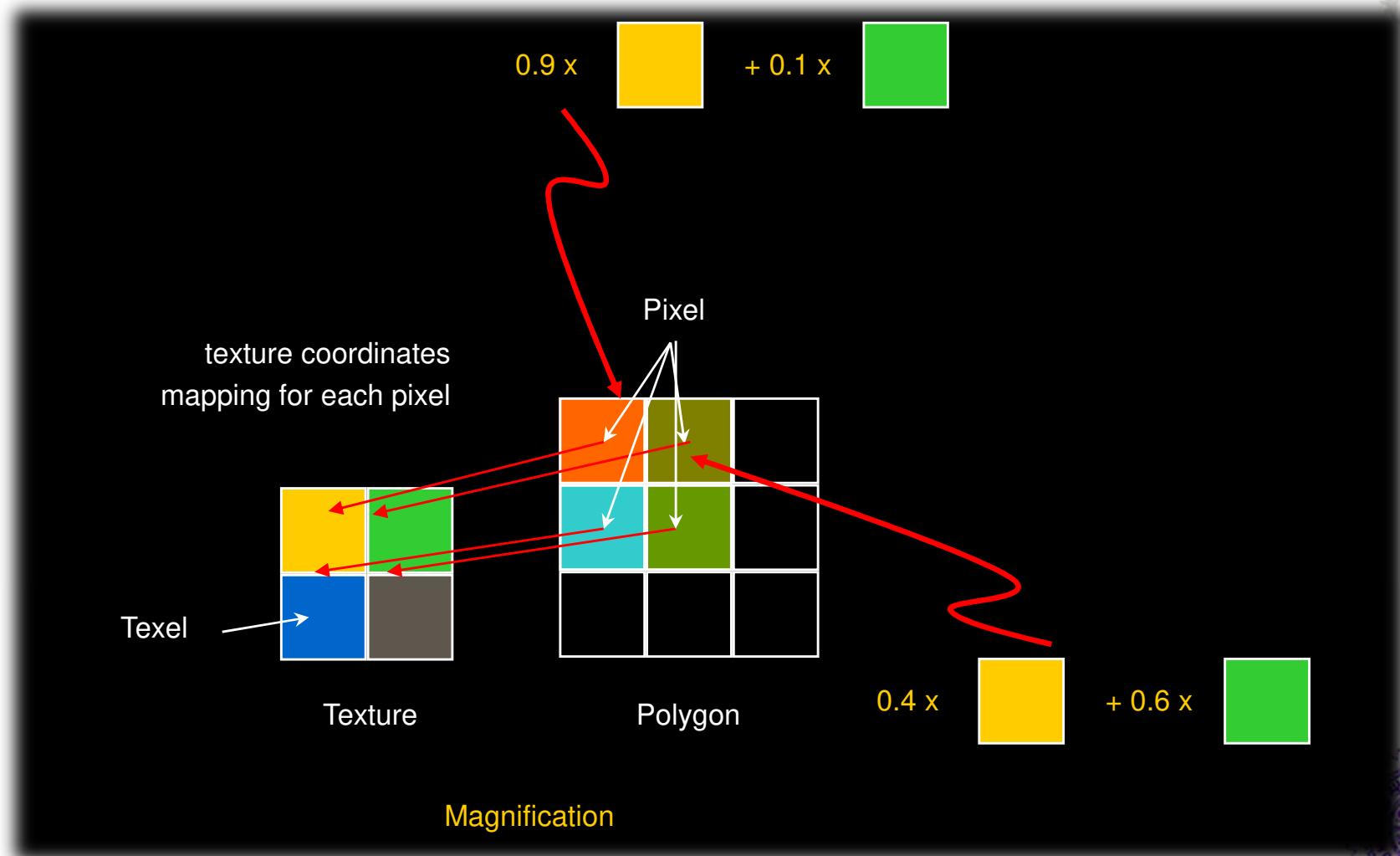
# *Magnification*

## ◆ Nearest Sampling



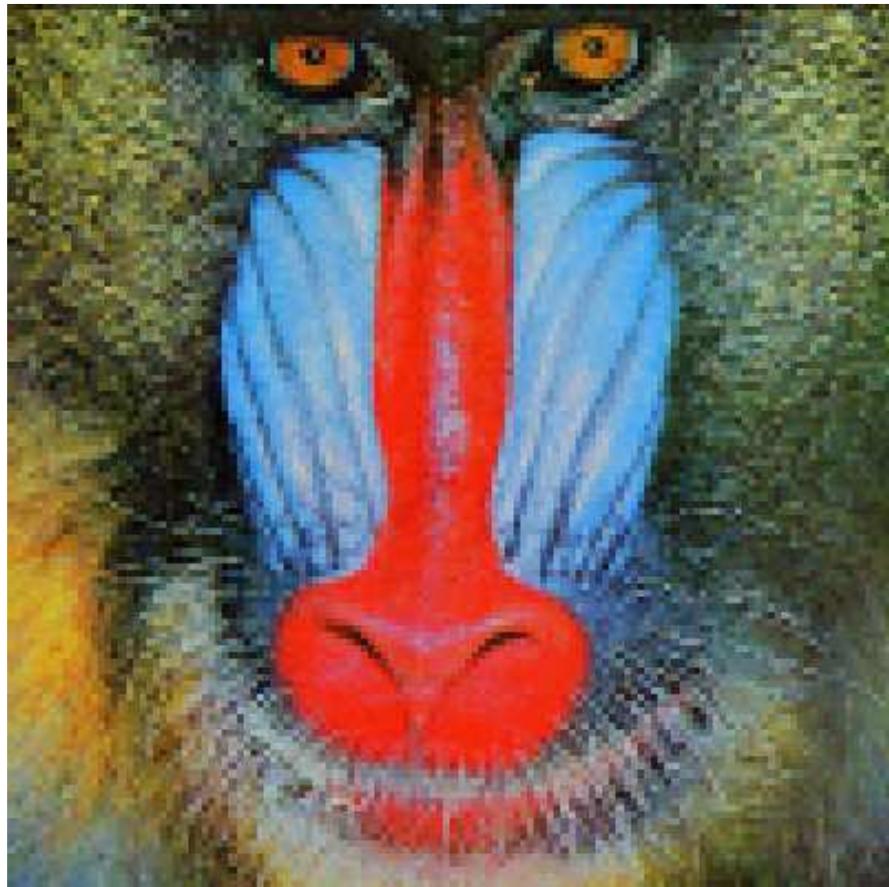
# *Magnification*

## ◆ Linear Sampling

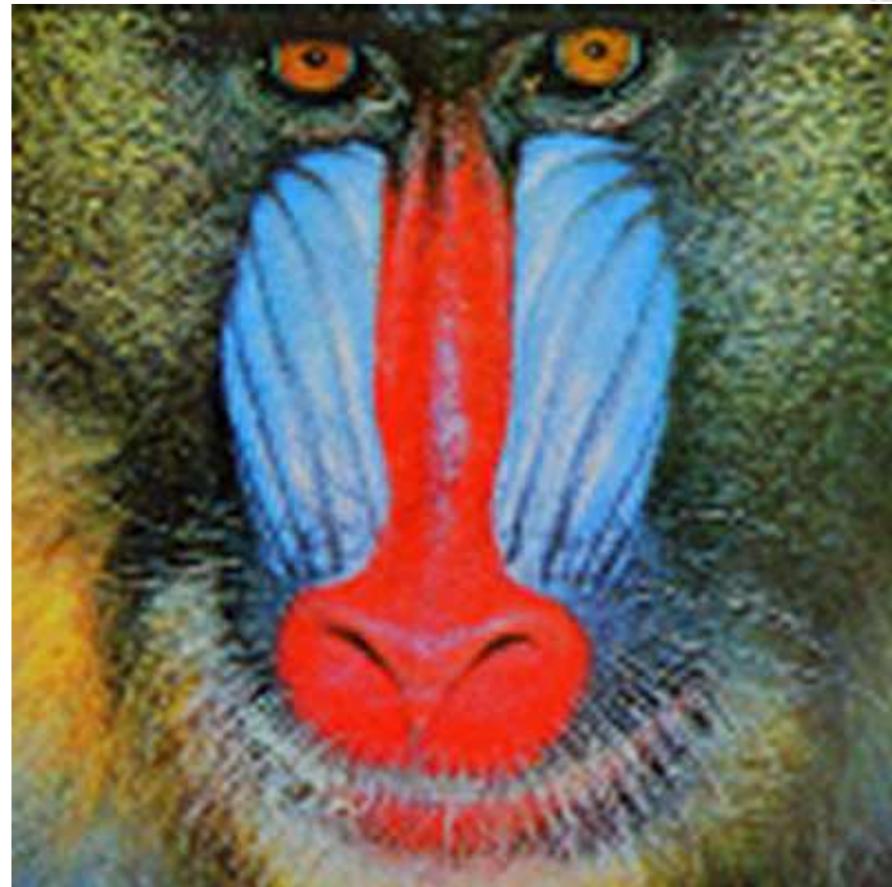


# *Magnification*

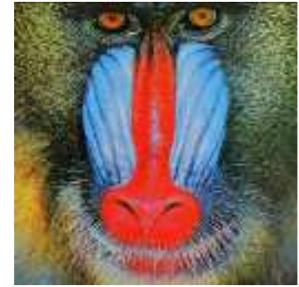
## ◆ Nearest Sampling vs. Linear Sampling



Nearest Sampling

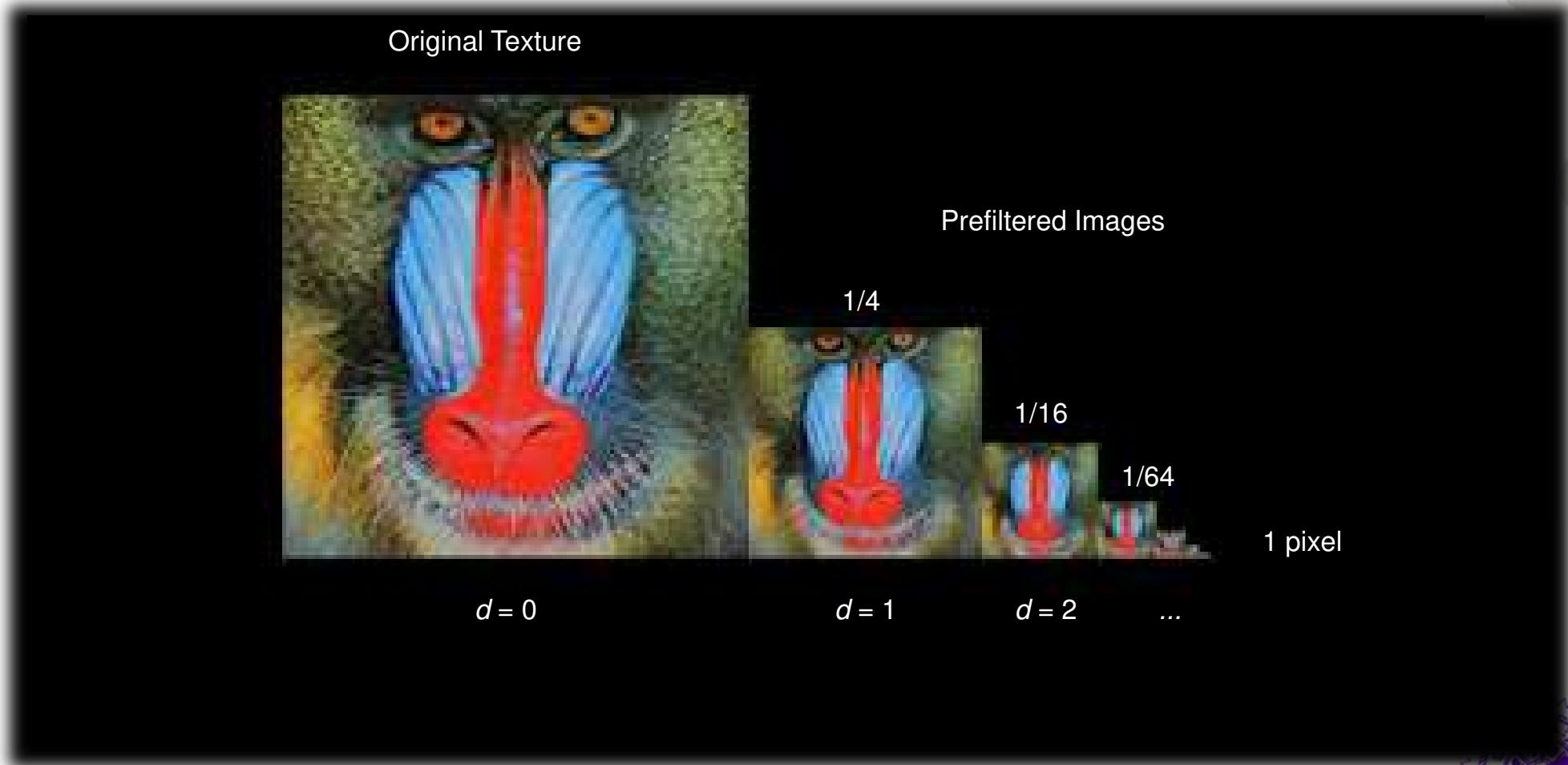


Linear Sampling



# *Texture Mipmapping for Minification*

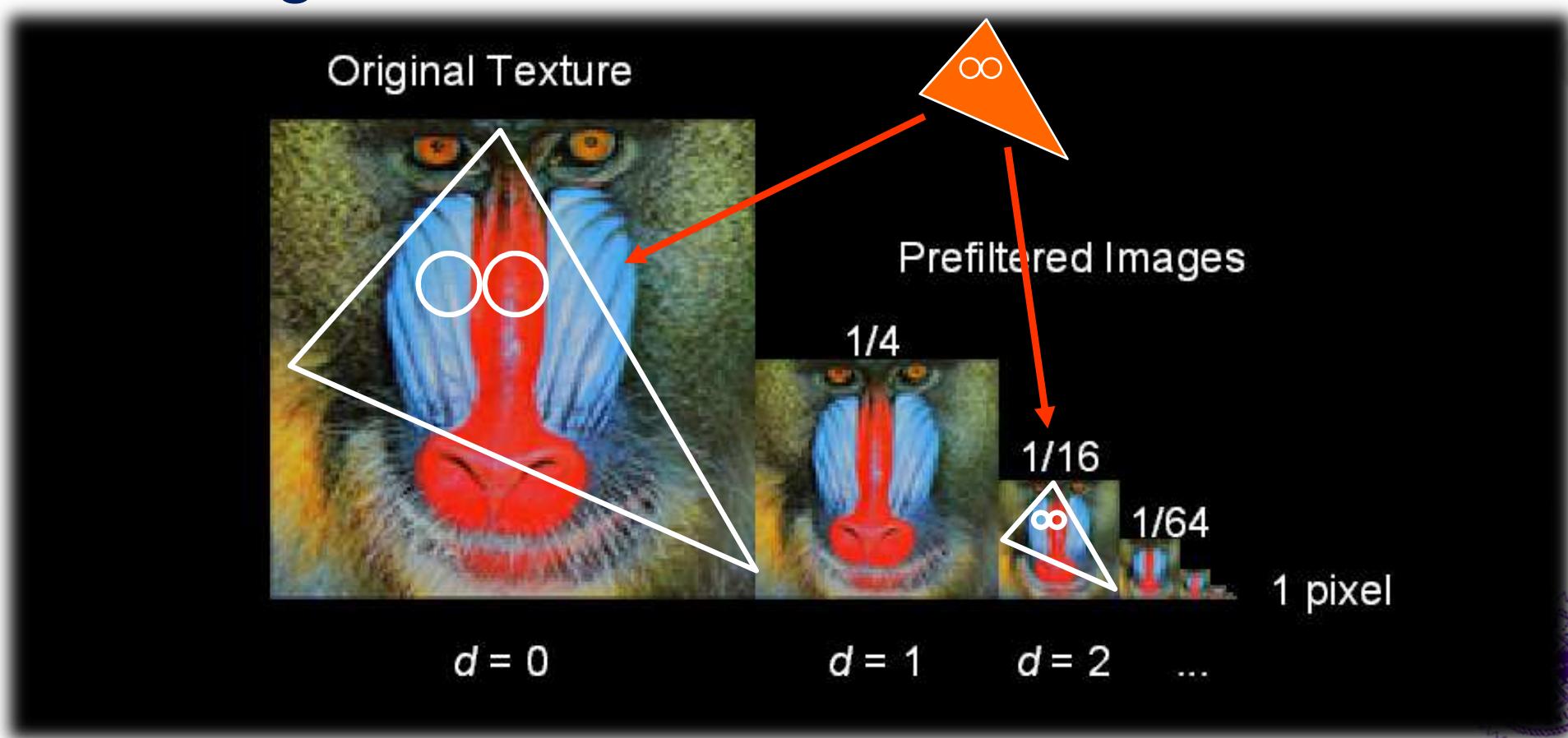
## ◆ Texture Mipmap (Multum in Parvo)



# *Level of Detail (LOD)*

## ◆ Concept

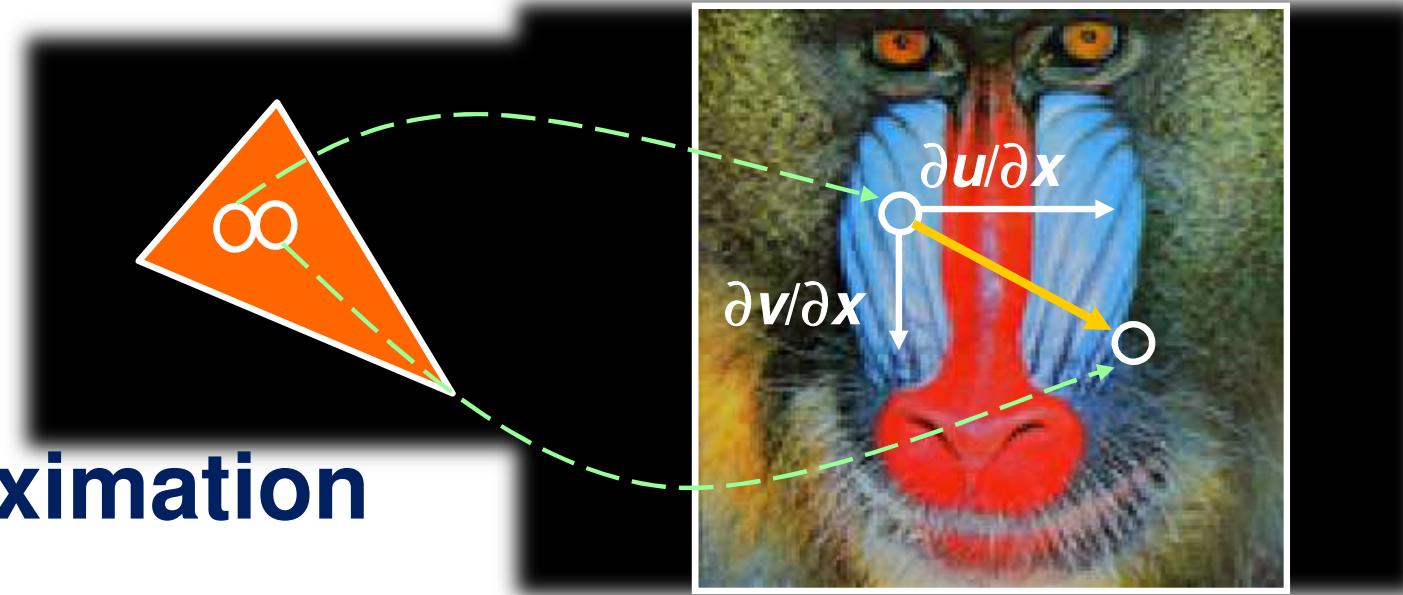
- Find a suitable pre-filtered image for later texture filtering



# *LOD Calculation*

- ◆ **Definition (OpenGL)**

$$LOD = \log_2 \left( \max \left\{ \sqrt{\left( \frac{\partial u}{\partial x} \right)^2 + \left( \frac{\partial v}{\partial x} \right)^2}, \sqrt{\left( \frac{\partial u}{\partial y} \right)^2 + \left( \frac{\partial v}{\partial y} \right)^2} \right\} \right)$$



- ◆ **Approximation**

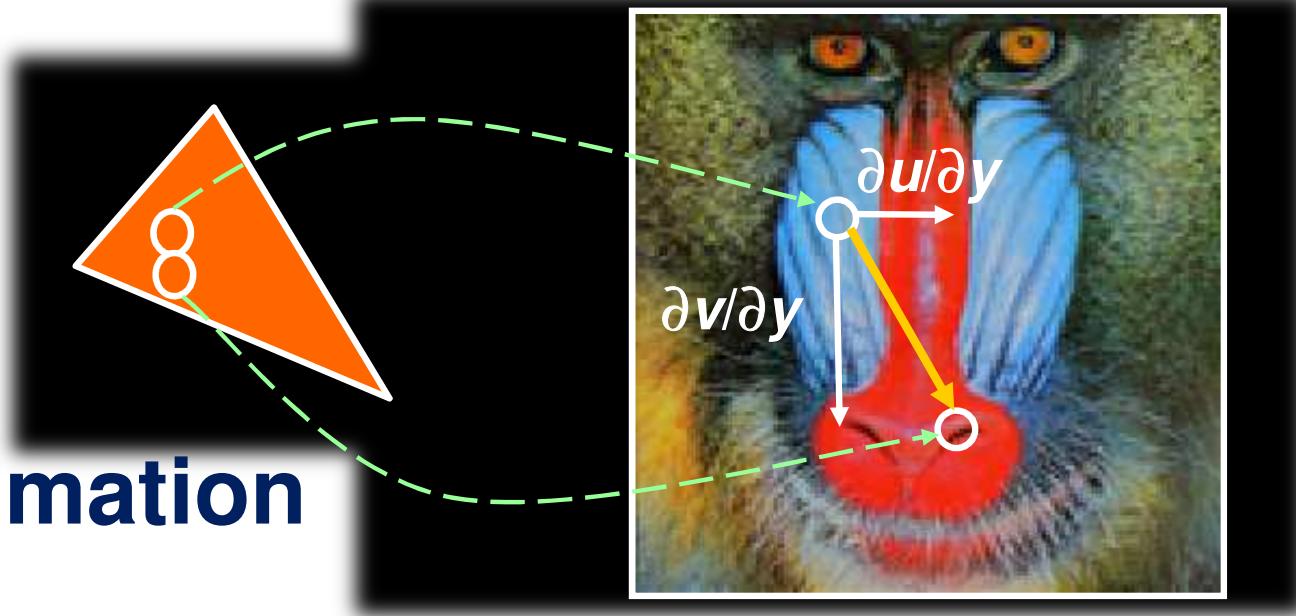
$$LOD = \log_2 \left( \max \left\{ \left| \frac{\partial u}{\partial x} \right|, \left| \frac{\partial v}{\partial x} \right|, \left| \frac{\partial u}{\partial y} \right|, \left| \frac{\partial v}{\partial y} \right| \right\} \right)$$

# *LOD Calculation*

- ◆ **Definition (OpenGL)**

$$LOD = \log_2 \left( \max \left\{ \sqrt{\left( \frac{\partial u}{\partial x} \right)^2 + \left( \frac{\partial v}{\partial x} \right)^2}, \sqrt{\left( \frac{\partial u}{\partial y} \right)^2 + \left( \frac{\partial v}{\partial y} \right)^2} \right\} \right)$$

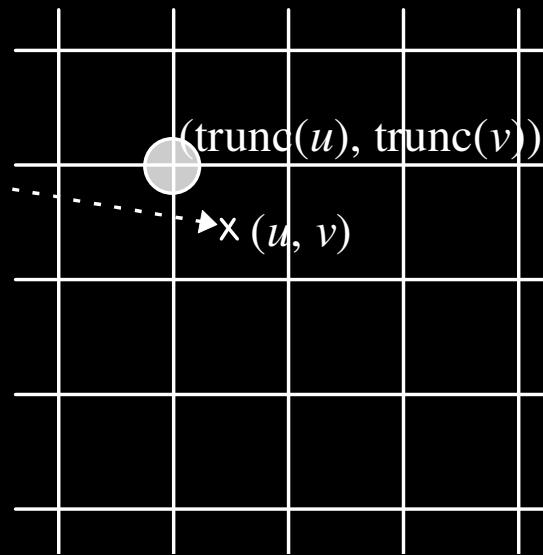
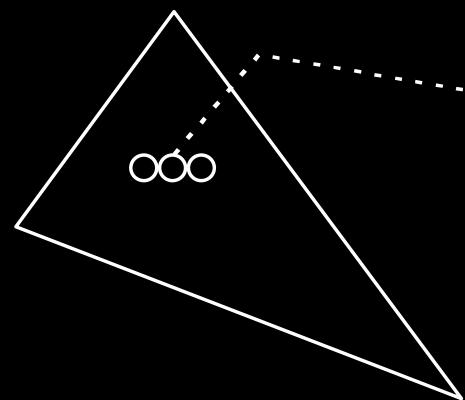
- ◆ **Approximation**



$$LOD = \log_2 \left( \max \left\{ \left| \frac{\partial u}{\partial x} \right|, \left| \frac{\partial v}{\partial x} \right|, \left| \frac{\partial u}{\partial y} \right|, \left| \frac{\partial v}{\partial y} \right| \right\} \right)$$

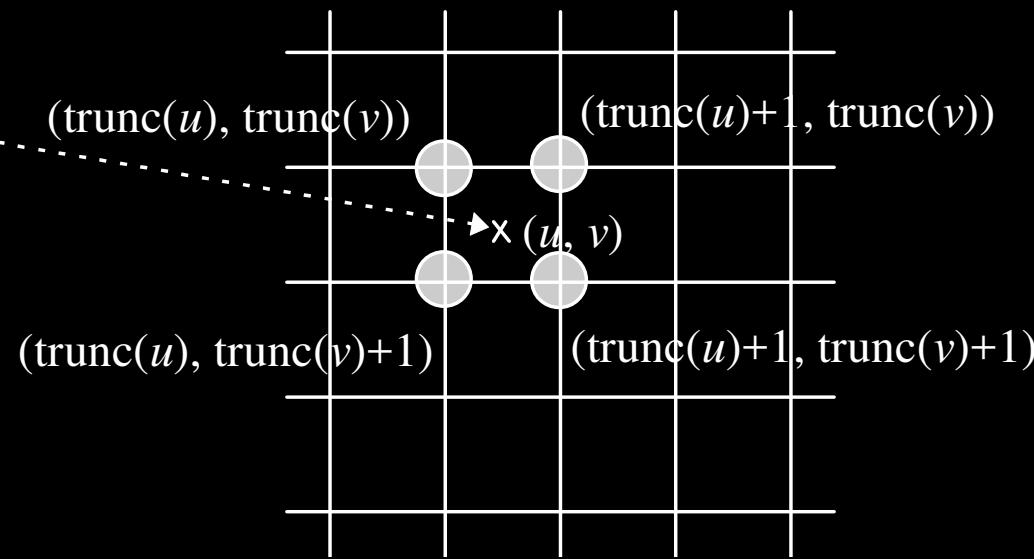
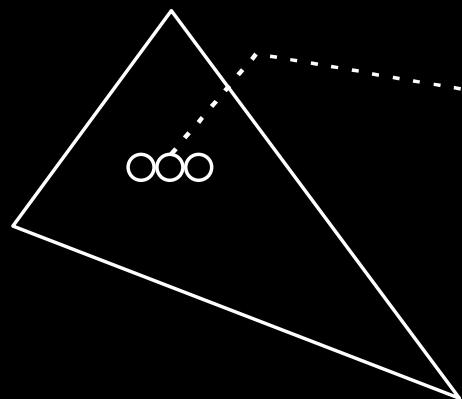
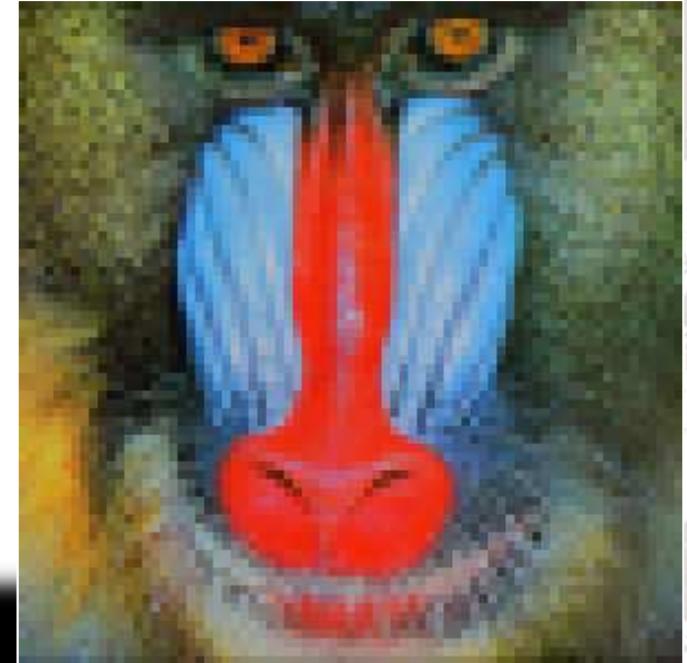
# Minification

## ◆ Nearest



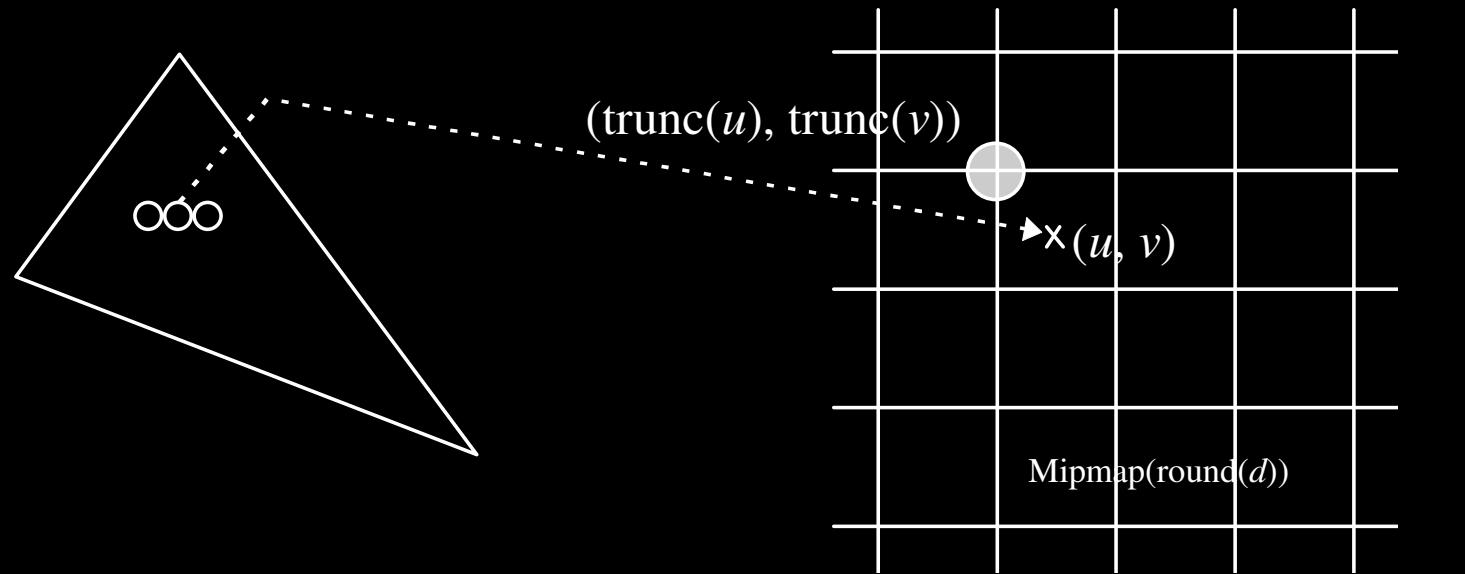
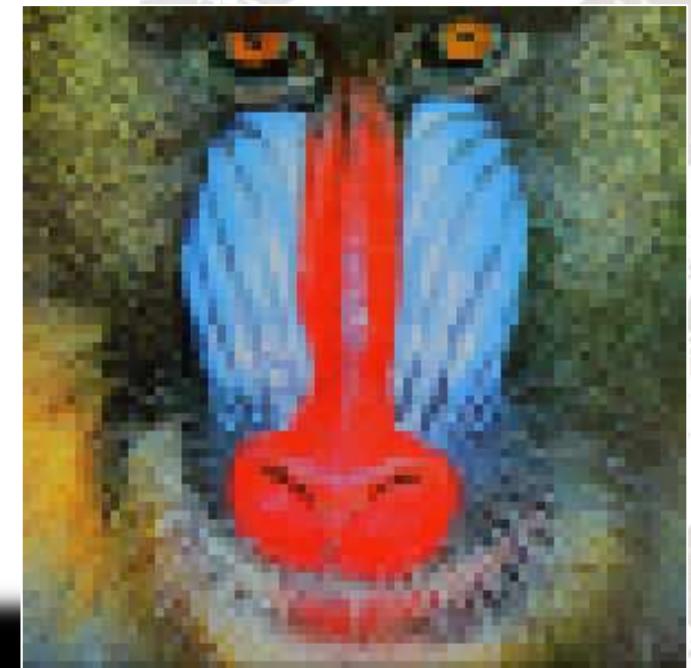
# Minification

## ◆ Linear



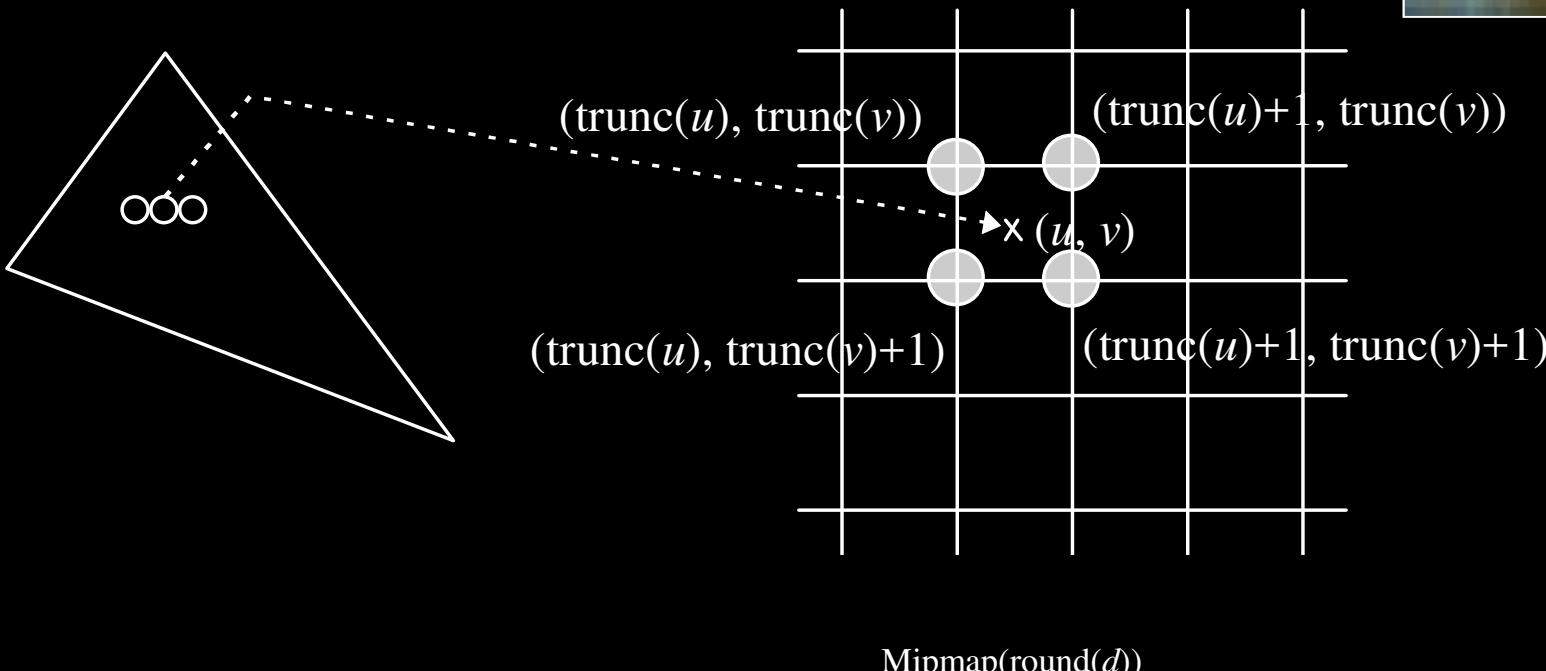
# *Minification*

## ◆ Nearest\_Mipmap\_Nearest



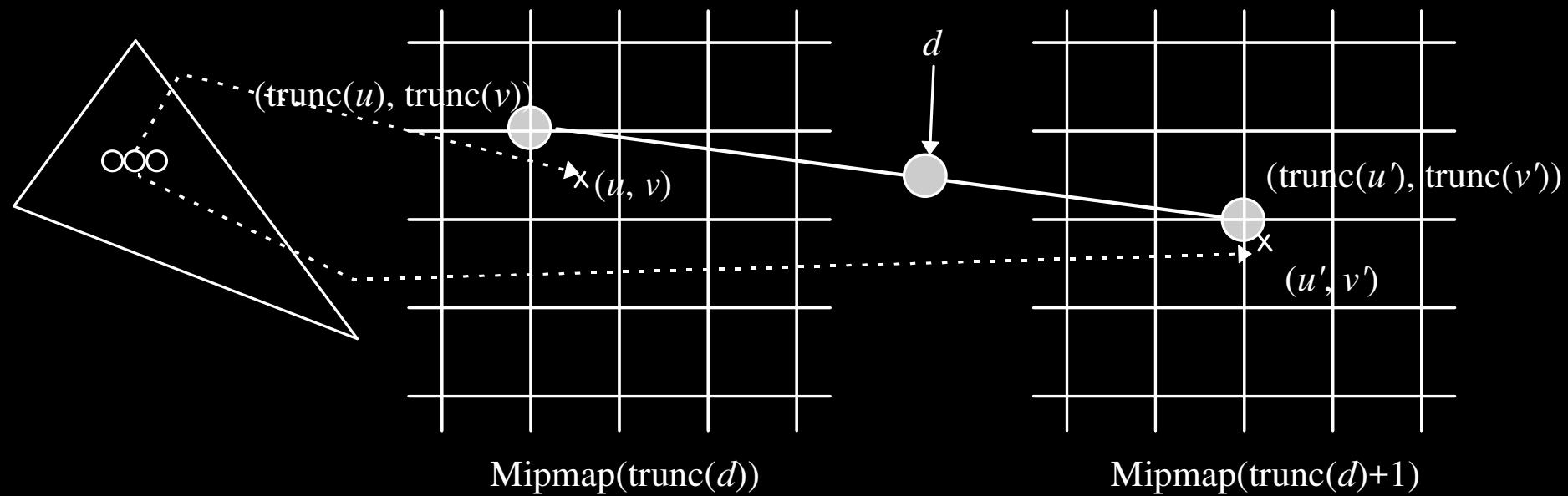
# Minification

## ◆ Linear\_Mipmap\_Nearest



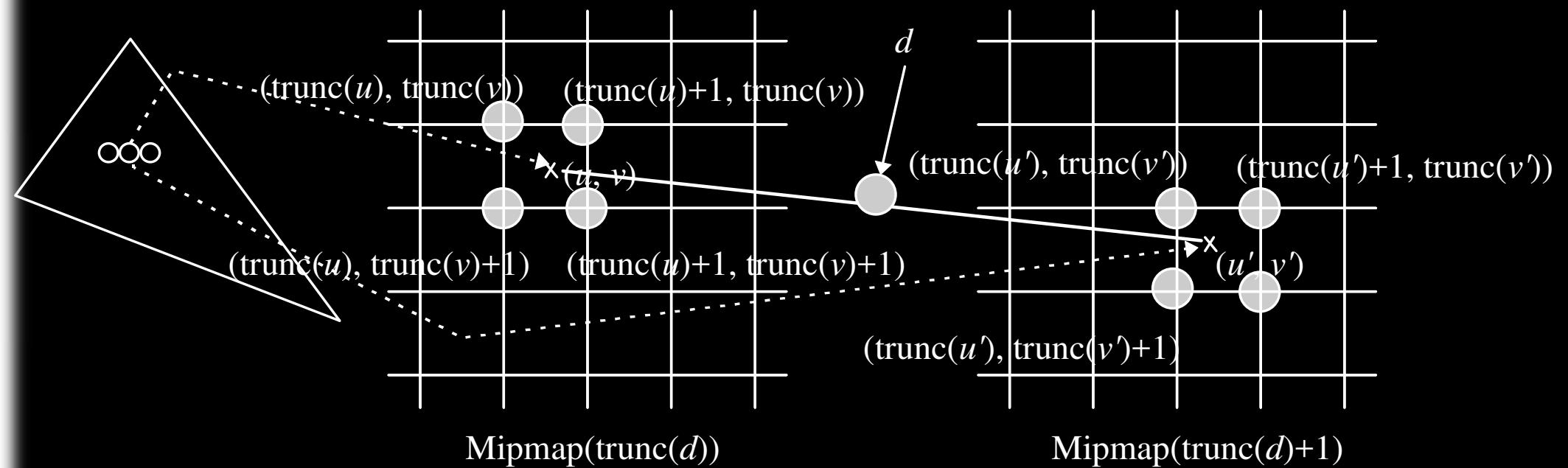
# Minification

## ◆ Nearest\_Mipmap\_Linear



# Minification

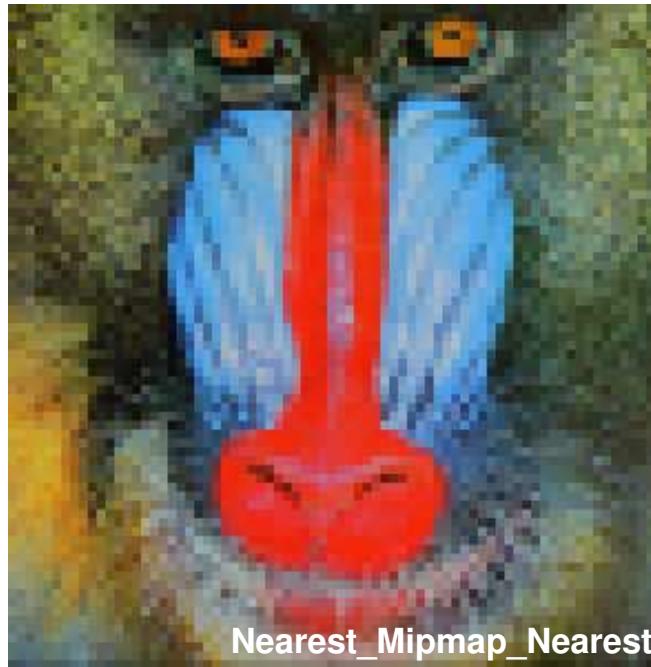
## ◆ Linear\_Mipmap\_Linear



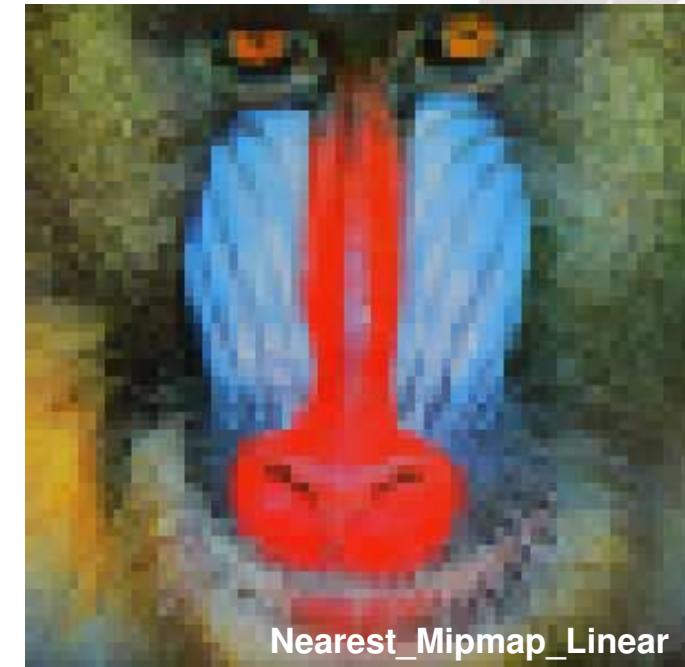
# *Minification*



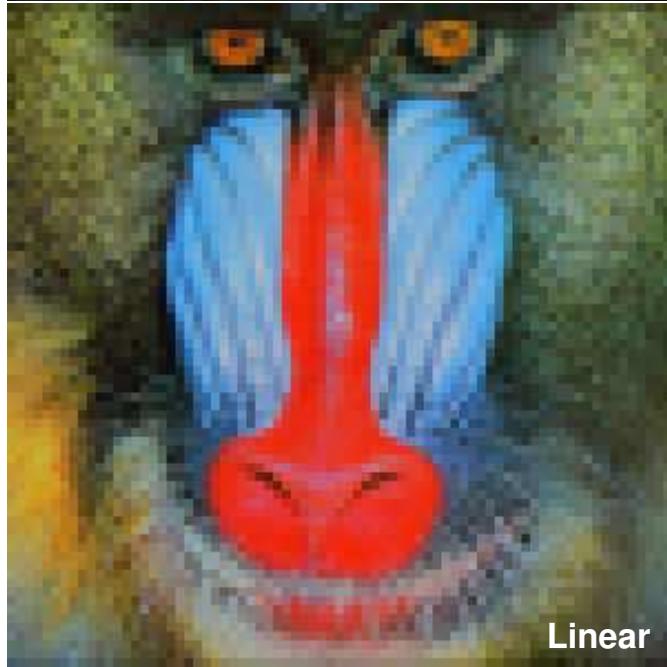
Nearest



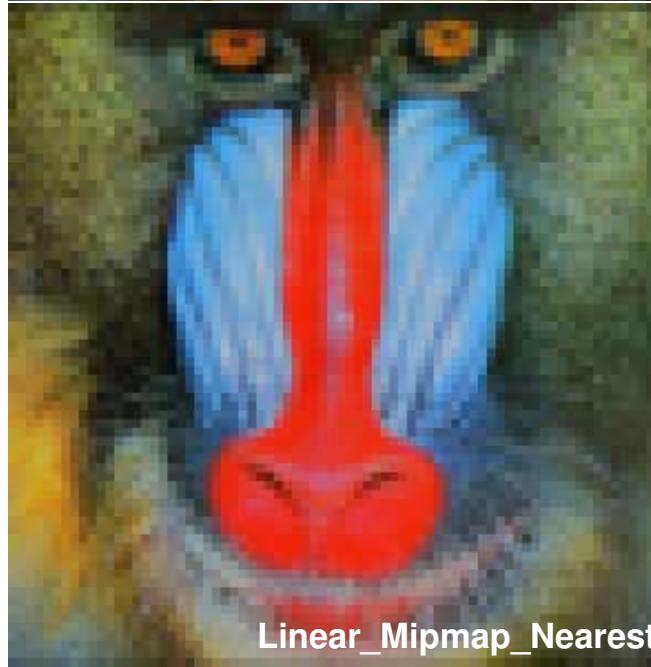
Nearest\_Mipmap\_Nearest



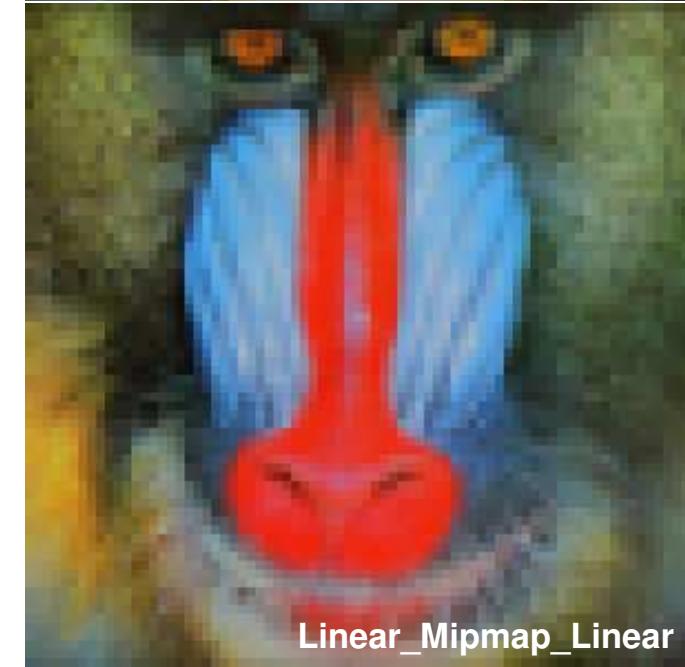
Nearest\_Mipmap\_Linear



Linear

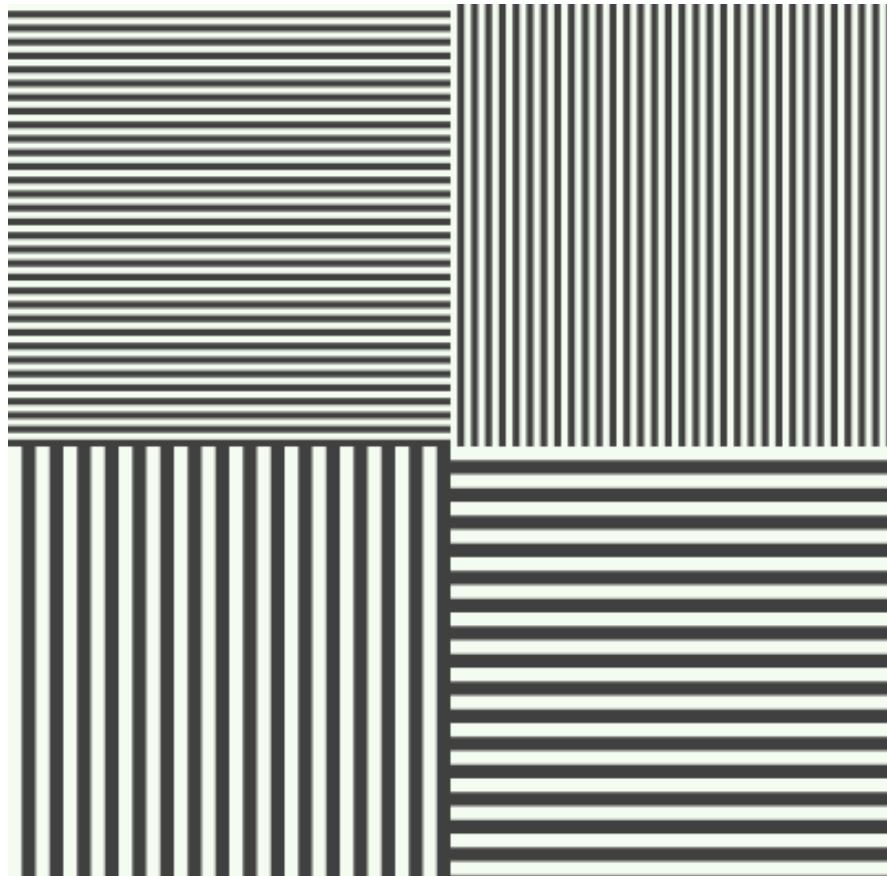


Linear\_Mipmap\_Nearest

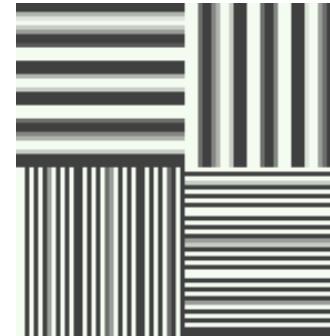


Linear\_Mipmap\_Linear

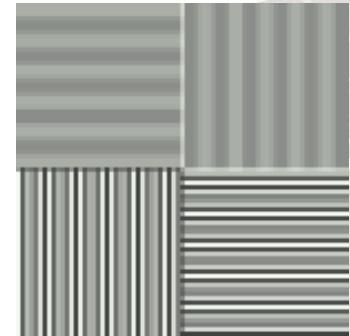
# *Minification*



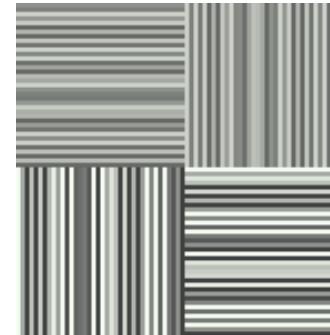
Original texture



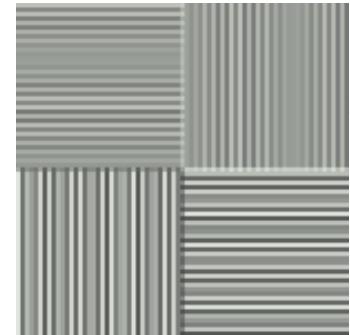
Nearest



Linear



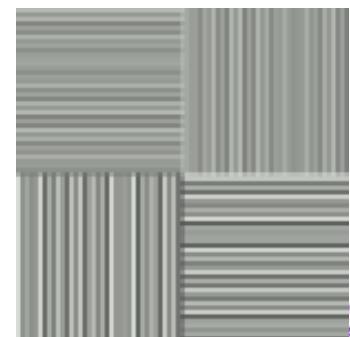
Nearest\_Mipmap\_Nearest



Linear\_Mipmap\_Nearest



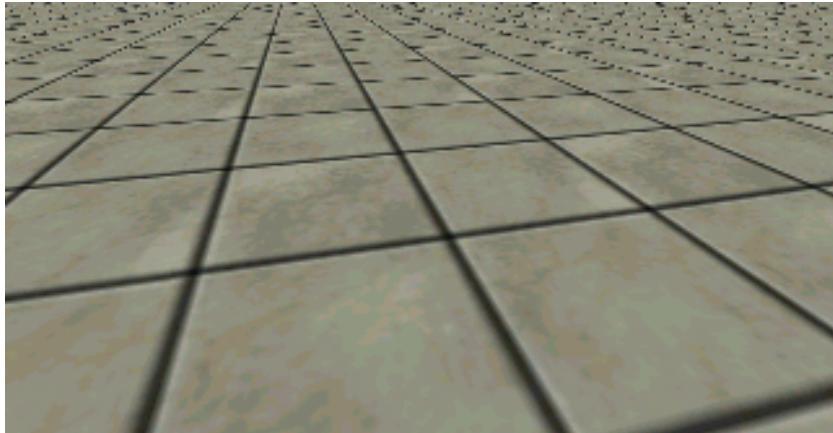
Nearest\_Mipmap\_Linear



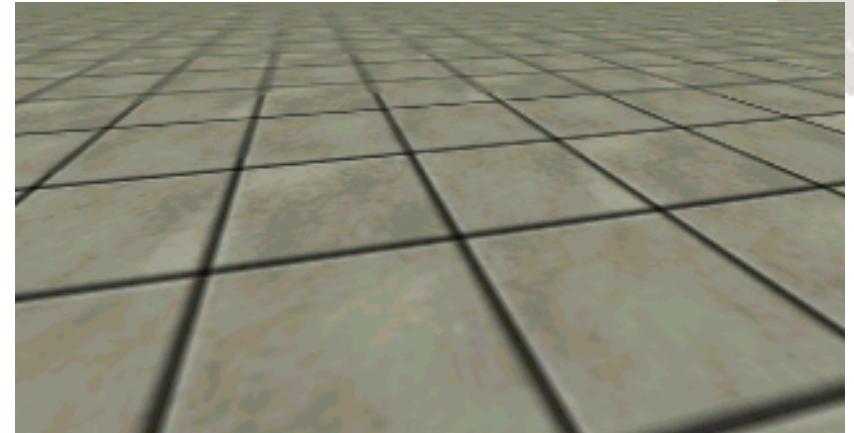
Linear\_Mipmap\_Linear



# *Application of Texture Mipmap*



Without texture mipmaping



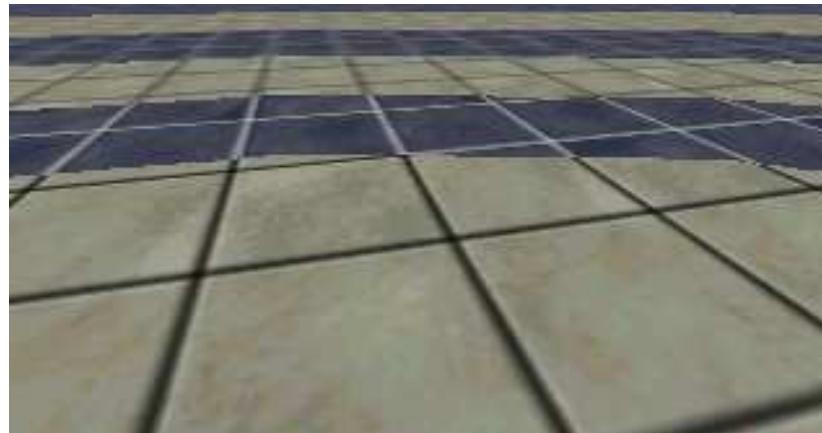
With texture mipmaping

$d = 3$

$d = 2$

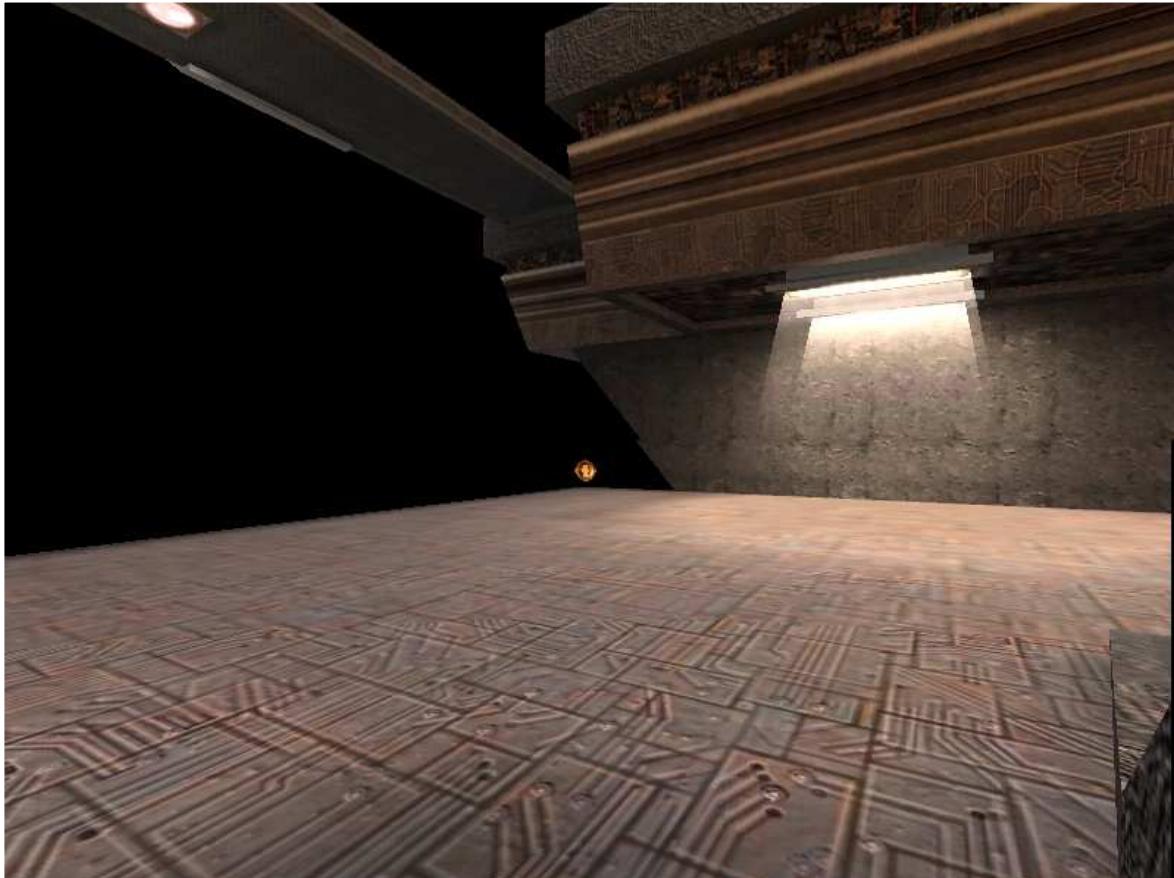
$d = 1$

$d = 0$

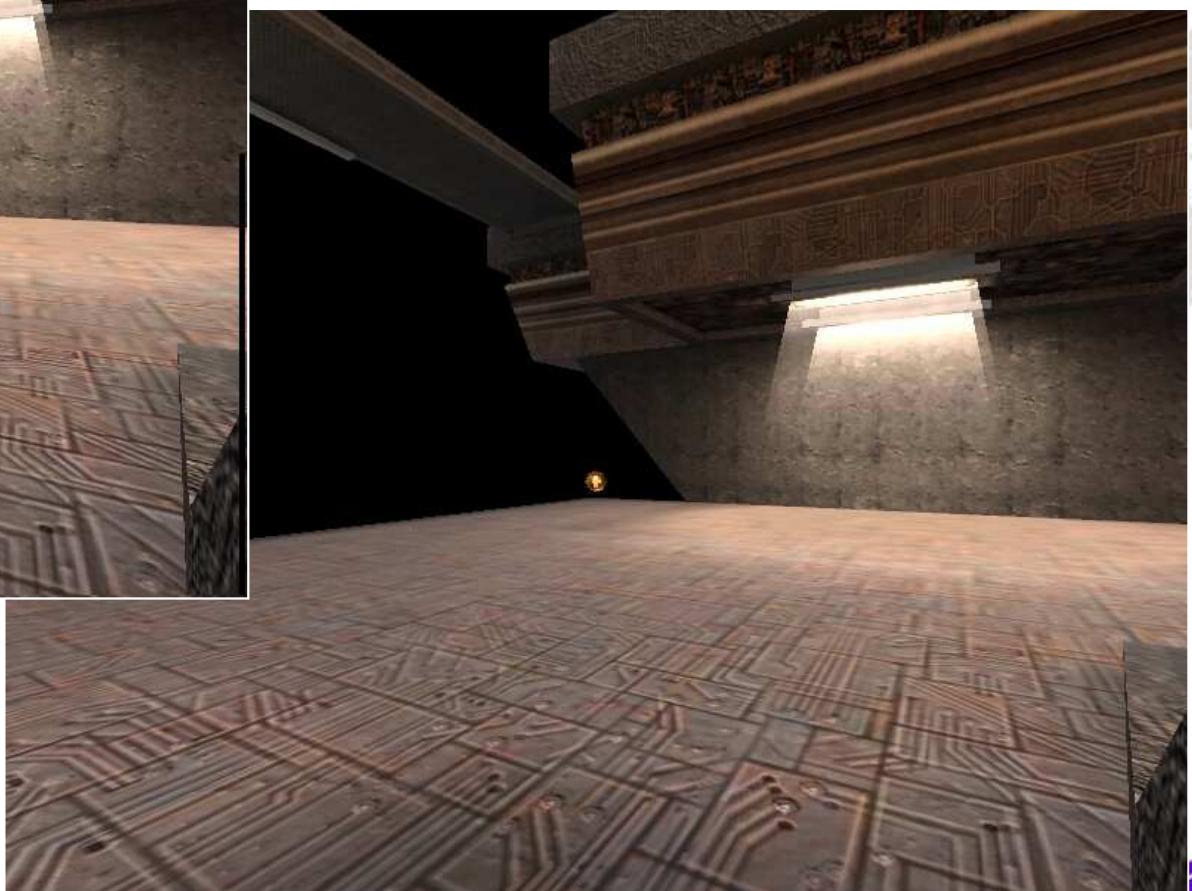


Mipmap LODs

# *Bi-linear vs. Tri-linear*

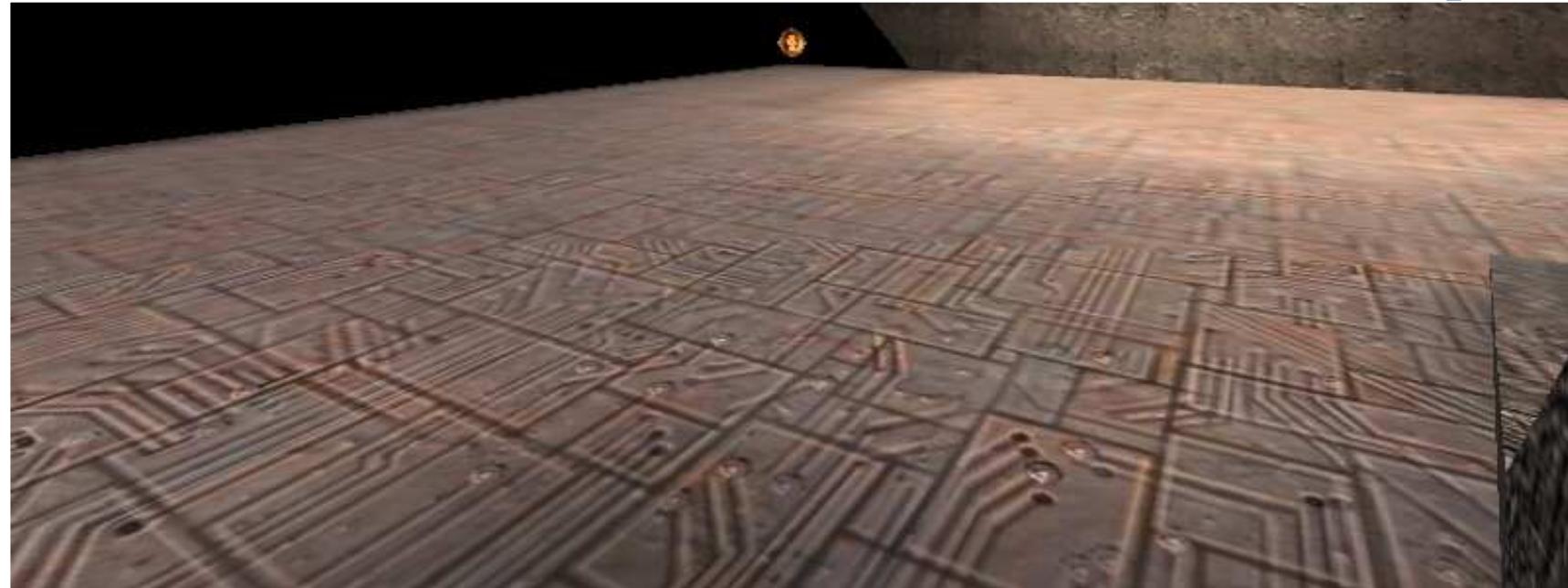


Bi-linear filtering



Tri-linear filtering

# *Bi-linear vs. Tri-linear (Close-up)*

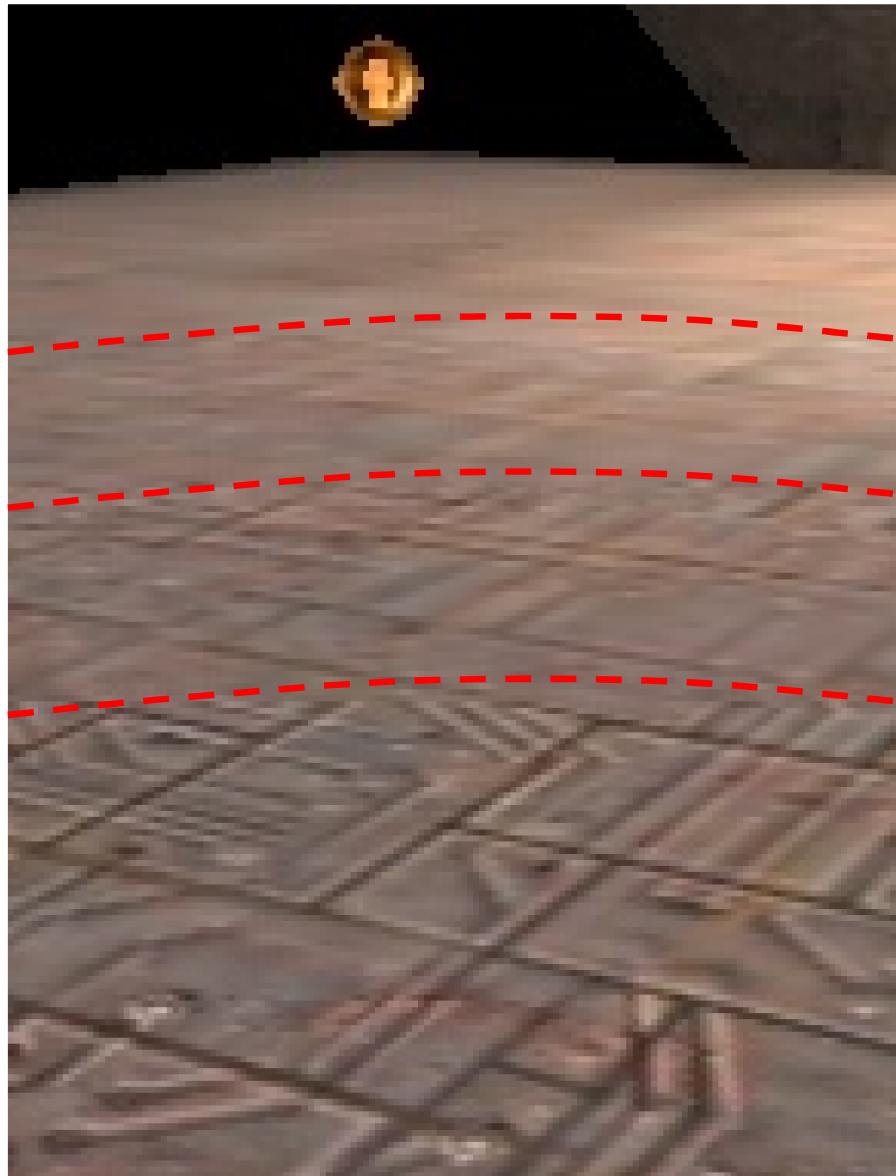


Bi-linear  
filtering

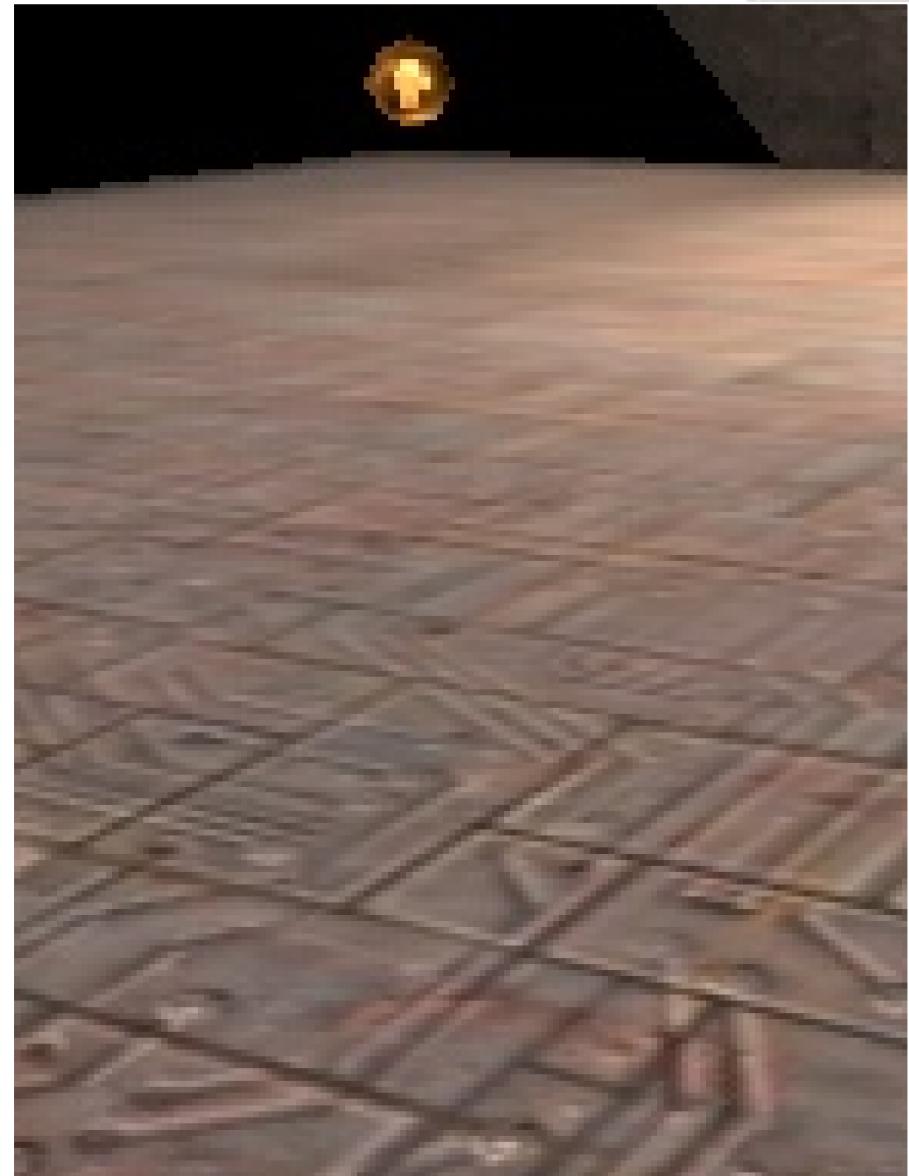


Tri-linear  
filtering

# *Bi-linear vs. Tri-linear (Close-up more)*



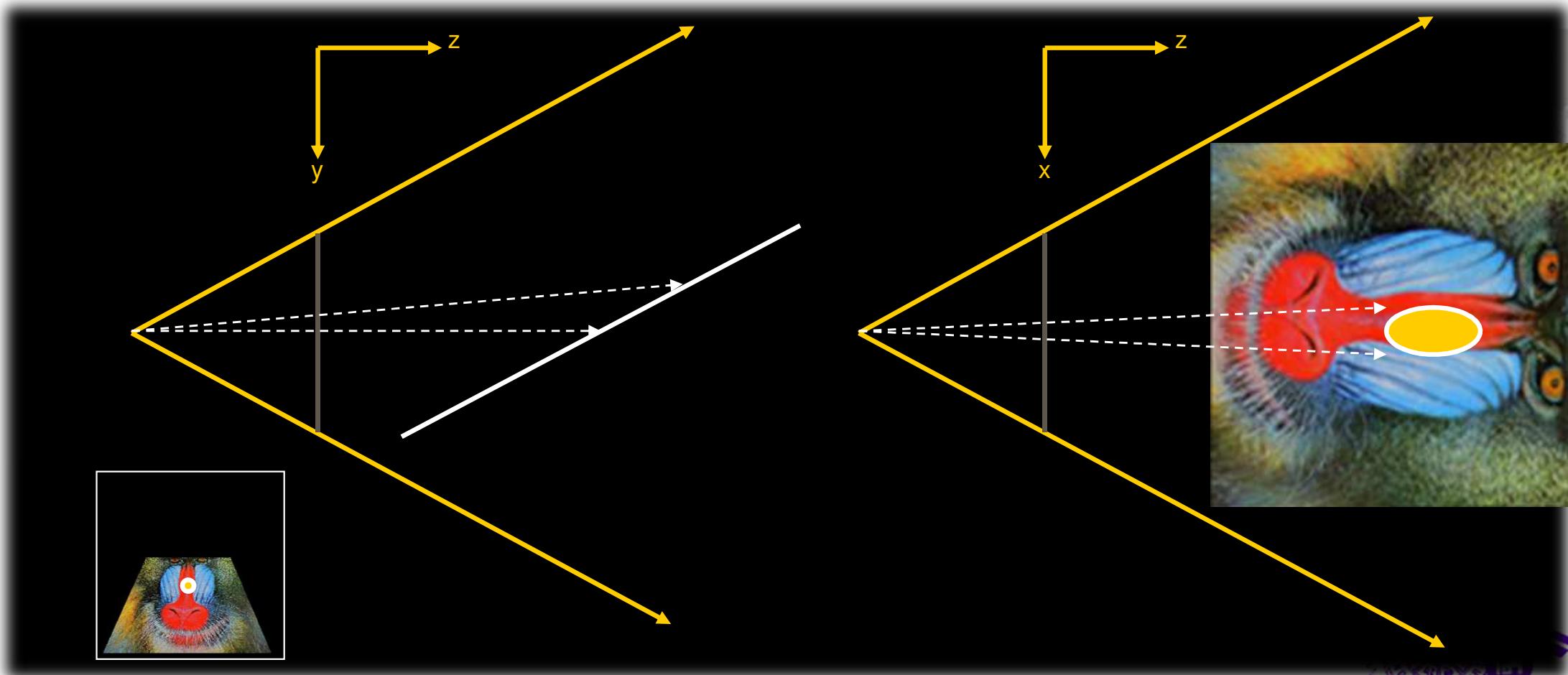
Bi-linear filtering



Tri-linear filtering

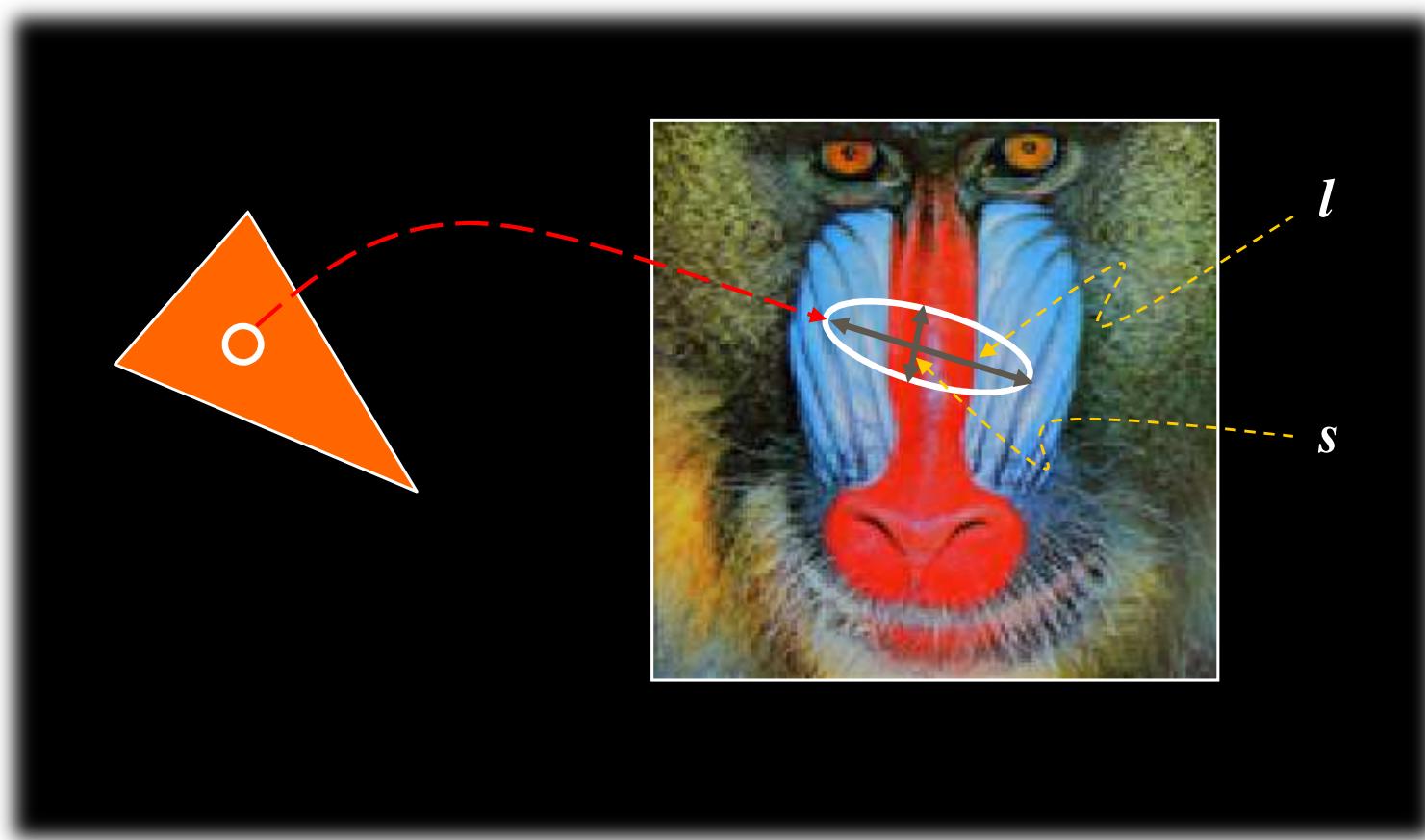
# *Texture Mapped Region of a Pixel*

- ◆ Texture mapped region of a projected pixel is not always a square



# Anisotropic Texture Filtering

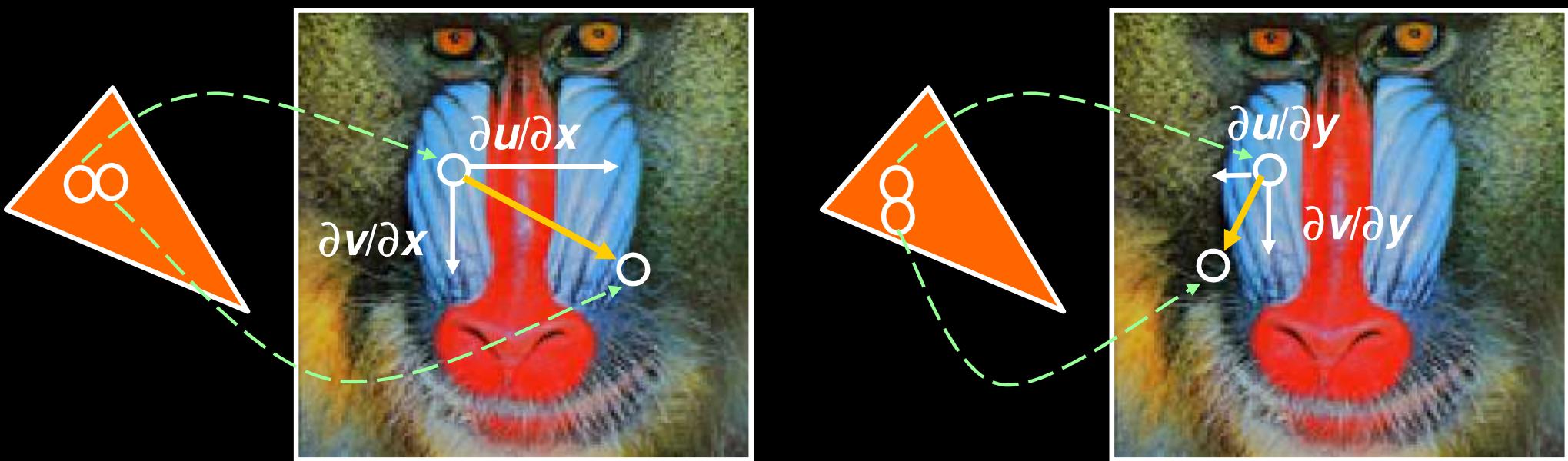
- ◆ Degree of Anisotropy
  - The ratio of  $l/s$



# Anisotropic Texture Filtering

## ◆ Approximation to the degree of anisotropy

$$\text{Degree of anisotropy} = \sqrt{\left(\frac{\partial u}{\partial x}\right)^2 + \left(\frac{\partial v}{\partial x}\right)^2} / \sqrt{\left(\frac{\partial u}{\partial y}\right)^2 + \left(\frac{\partial v}{\partial y}\right)^2}$$



# Anisotropic Texture Filtering

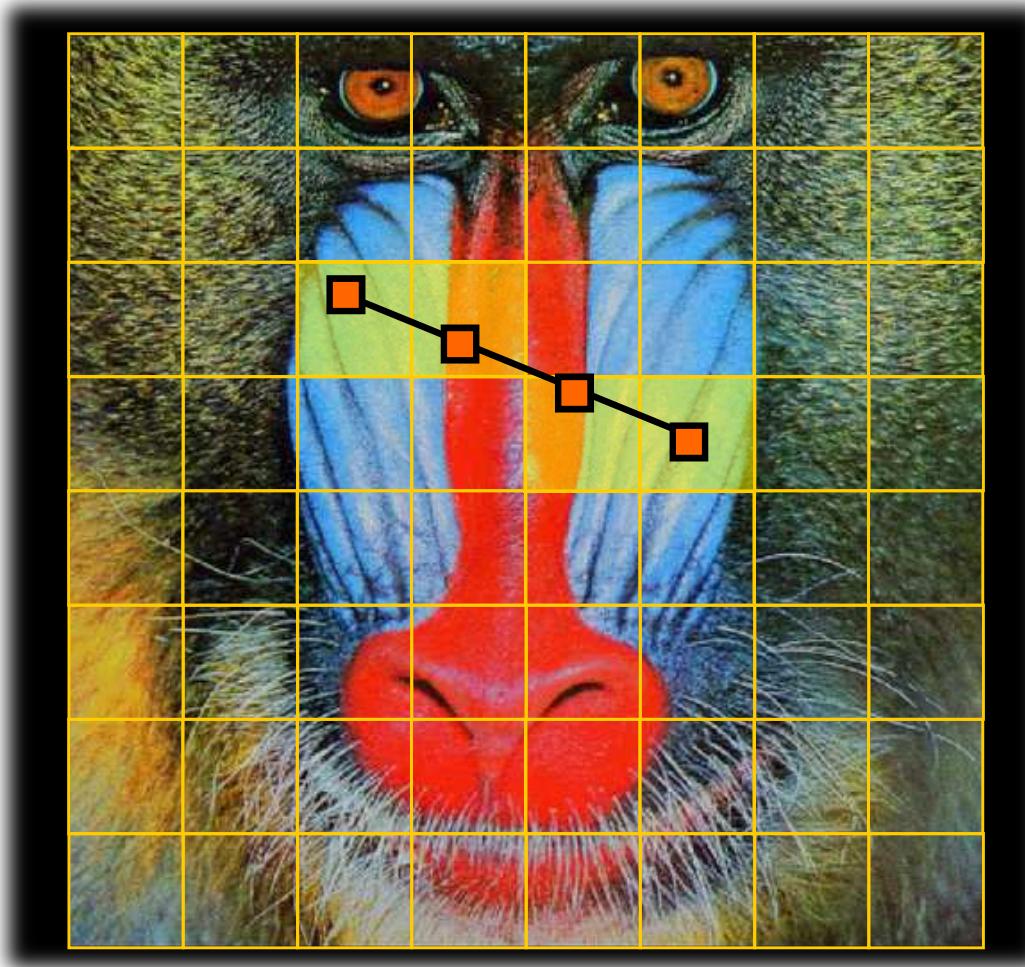
- ◆ LOD calculation

$$LOD = \log_2 \left( \min \left\{ \sqrt{\left( \frac{\partial u}{\partial x} \right)^2 + \left( \frac{\partial v}{\partial x} \right)^2}, \sqrt{\left( \frac{\partial u}{\partial y} \right)^2 + \left( \frac{\partial v}{\partial y} \right)^2} \right\} \right)$$

- ◆ Keep the details for smaller gradient
- ◆ Filter more along the larger gradient

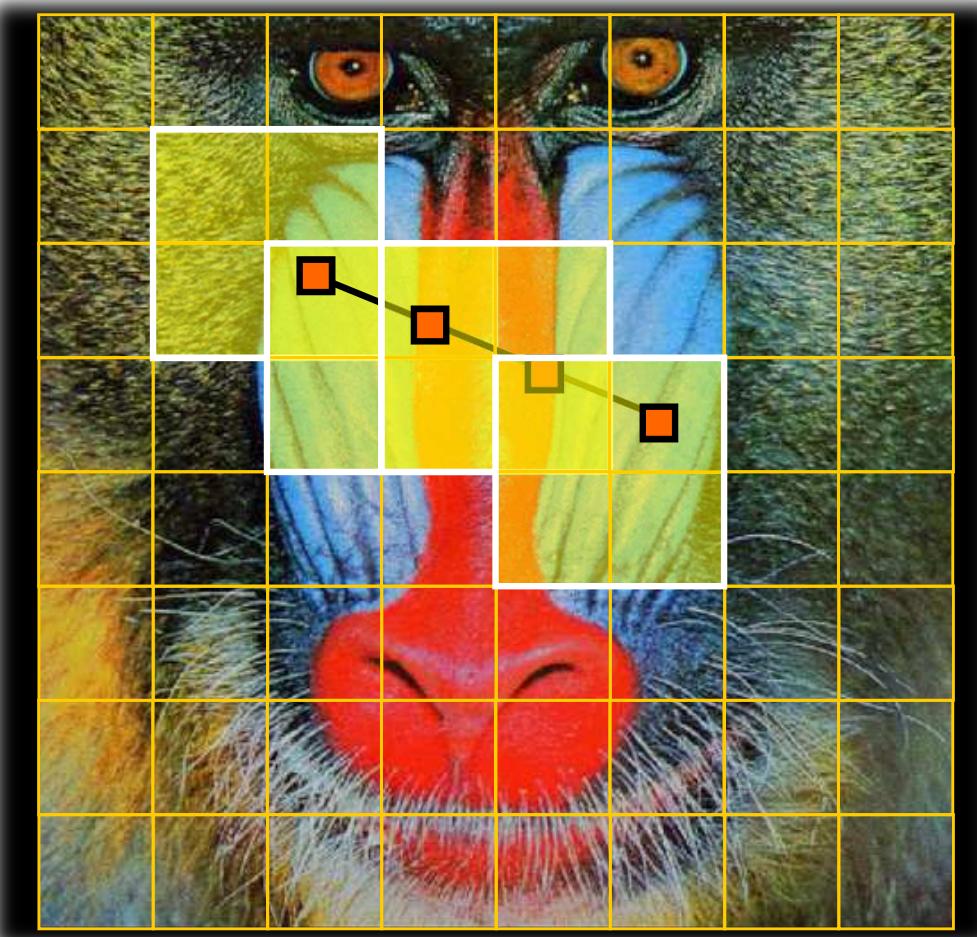
# Anisotropic Texture Filtering

- ◆ Nearest Filtering (Point Sampling)
  - Anisotropy = 4



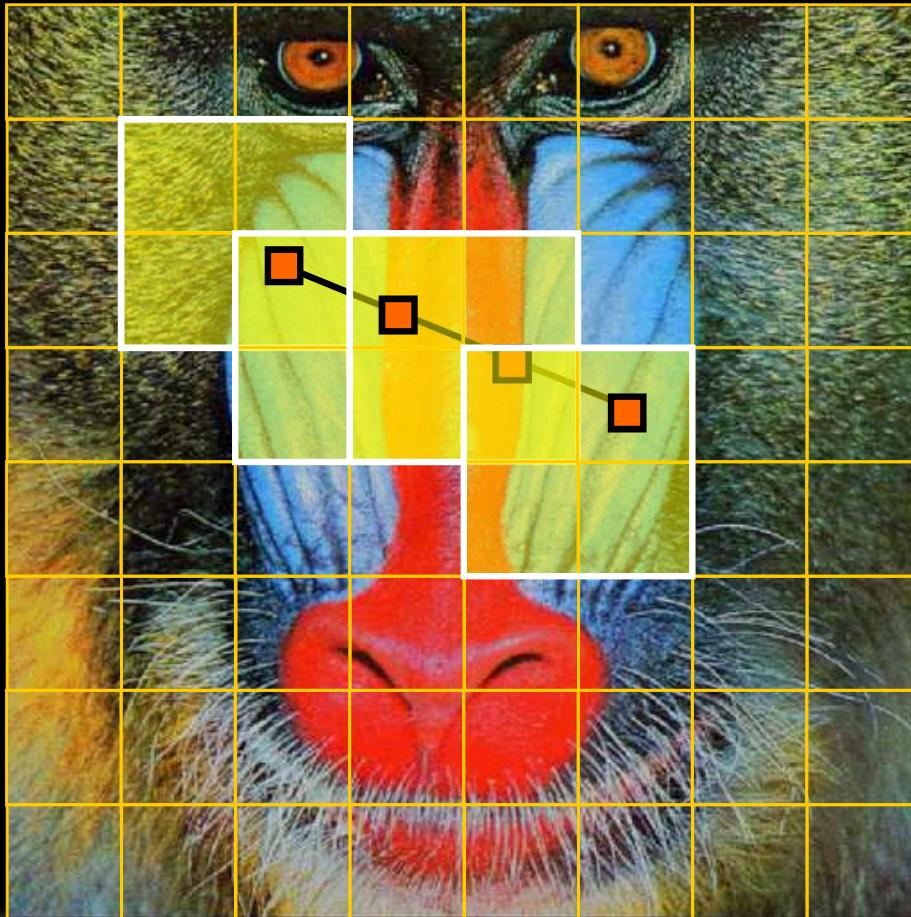
# Anisotropic Texture Filtering

- ◆ Linear Filtering (Bi-linear)
  - Anisotropy = 4

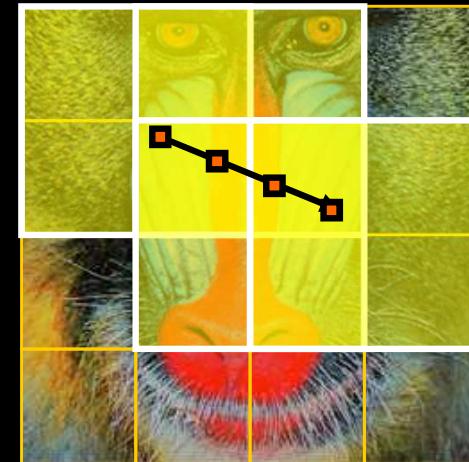


# Anisotropic Texture Filtering

- ◆ Tri-linear Filtering
  - Anisotropy = 4



$LOD = l$



$LOD = l+1$

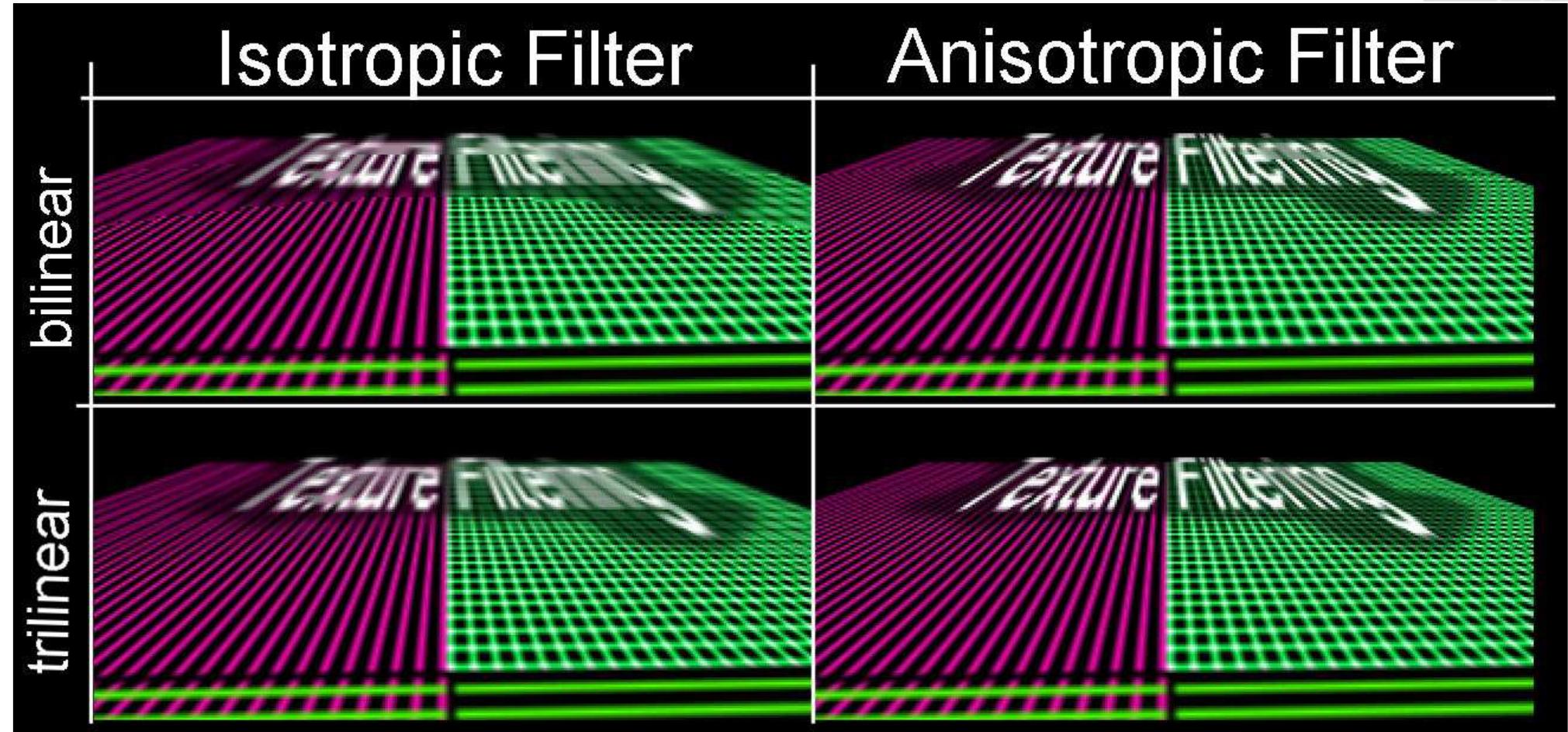
# Anisotropic Texture Filtering



# Anisotropic Texture Filtering

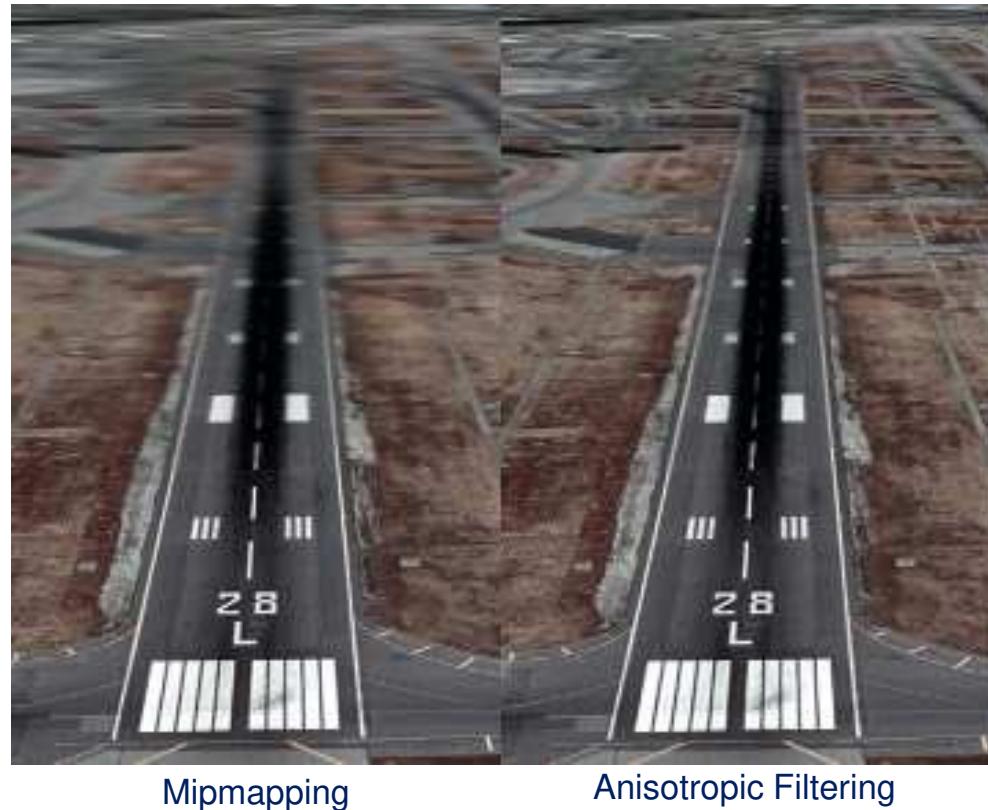


# Anisotropic Texture Filtering



# *Advantage of Anisotropic Filtering*

- ◆ Reducing blur and preserving surface detail at extreme viewing angles

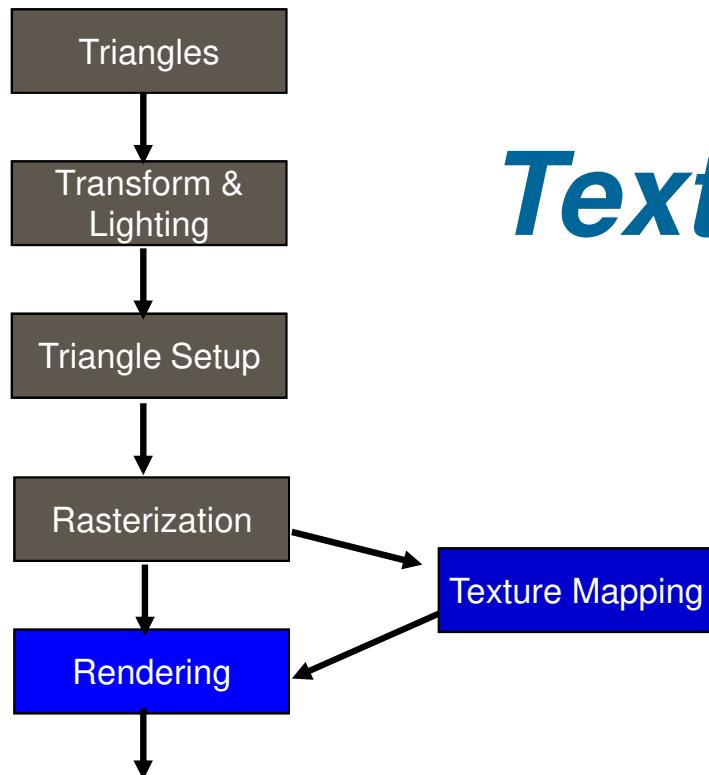


# *Disadvantage of Anisotropic Filtering*

- ◆ **Require more texels to read for anisotropic filtering if the degree of anisotropy is high**
  - **Most hardware implementations provide the setting of maximum degree of anisotropy to limit the number of texels read so that the performance impact is managed**



# *Conventional 3D Graphics Pipeline*



Conventional 3D Graphics Pipeline

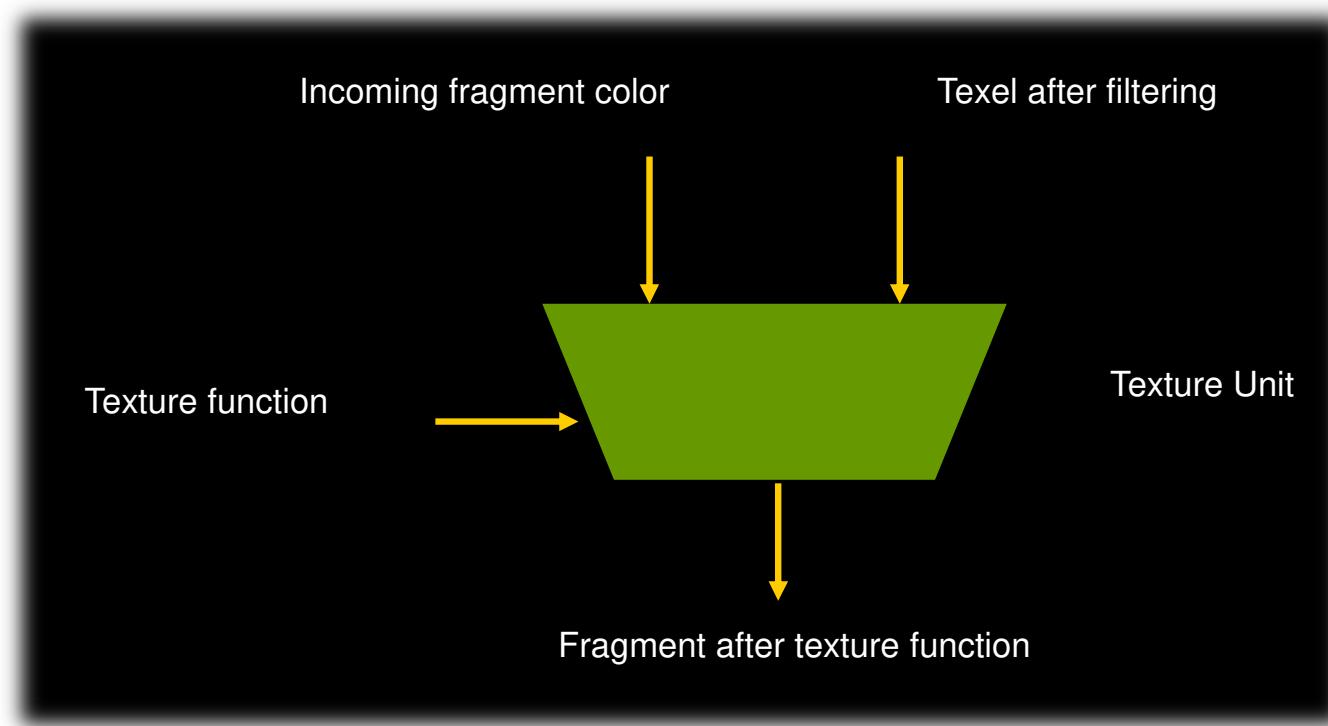
## *Texture Mapping (B)*

## *Advanced Texture Mapping*



# *Texture Functions*

- ◆ **Texture functions are used to define how a texel is to combine with a fragment being processed**



# Texture Functions

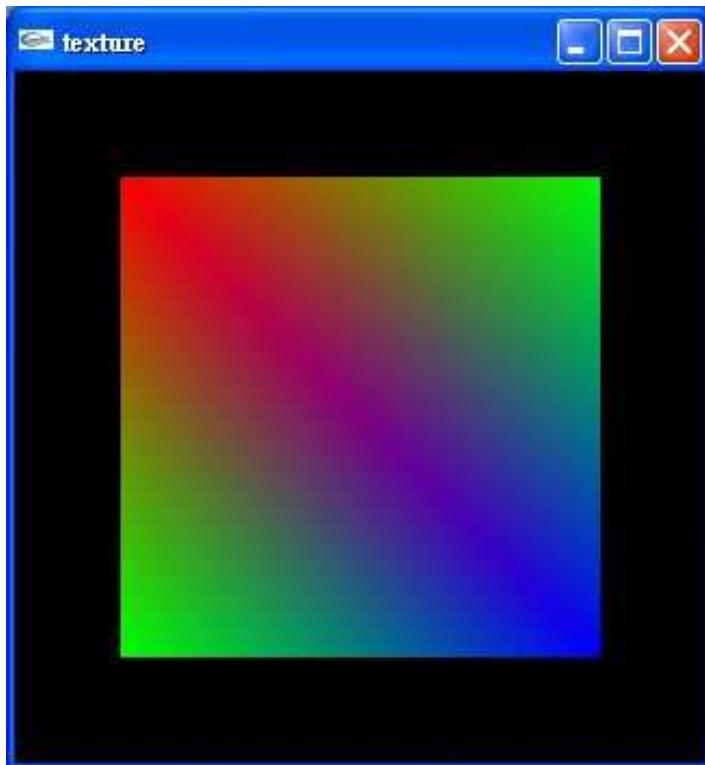
## ◆ Eg. OpenGL texture functions

Base Internal Format	GL_REPLACE Function	GL_MODULATE Function	GL_DECAL Function
GL_ALPHA	$C = C_f$ $A = A_s$	$C = C_f$ $A = A_f A_s$	undefined
GL_LUMINANCE	$C = C_s$ $A = A_f$	$C = C_f C_s$ $A = A_f$	undefined
GL_LUMINANCE_ALPHA	$C = C_s$ $A = A_s$	$C = C_f C_s$ $A = A_f A_s$	undefined
GL_INTENSITY	$C = C_s$ $A = C_s$	$C = C_f C_s$ $A = A_f C_s$	undefined
GL_RGB	$C = C_s$ $A = A_f$	$C = C_f C_s$ $A = A_f$	$C = C_s$ $A = A_f$
GL_RGBA	$C = C_s$ $A = A_s$	$C = C_f C_s$ $A = A_f A_s$	$C = C_f(1 - A_s) + C_s A_s$ $A = A_f$

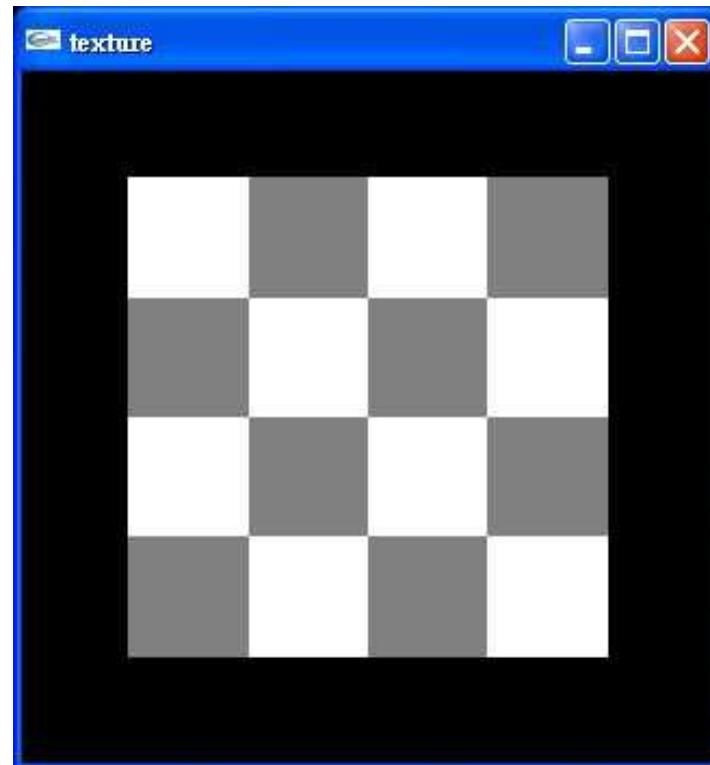
Base Internal Format	GL_BLEND Function	GL_ADD Function
GL_ALPHA	$C = C_f$ $A = A_f A_s$	$C = C_f$ $A = A_f A_s$
GL_LUMINANCE	$C = C_f(1 - C_s) + C_c C_s$ $A = A_f$	$C = C_f + C_s$ $A = A_f$
GL_LUMINANCE_ALPHA	$C = C_f(1 - C_s) + C_c C_s$ $A = A_f A_s$	$C = C_f + C_s$ $A = A_f A_s$
GL_INTENSITY	$C = C_f(1 - C_s) + C_c C_s$ $A = A_f(1 - A_s) + A_c A_s$	$C = C_f + C_s$ $A = A_f + A_s$
GL_RGB	$C = C_f(1 - C_s) + C_c C_s$ $A = A_f$	$C = C_f + C_s$ $A = A_f$
GL_RGBA	$C = C_f(1 - C_s) + C_c C_s$ $A = A_f A_s$	$C = C_f + C_s$ $A = A_f A_s$

# *Texture Functions*

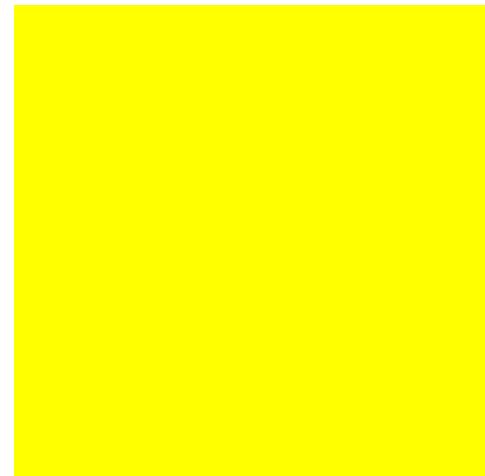
## ◆ Examples



Fragment color



Texture  
Alpha: 1.0 for white area  
0.5 for gray area

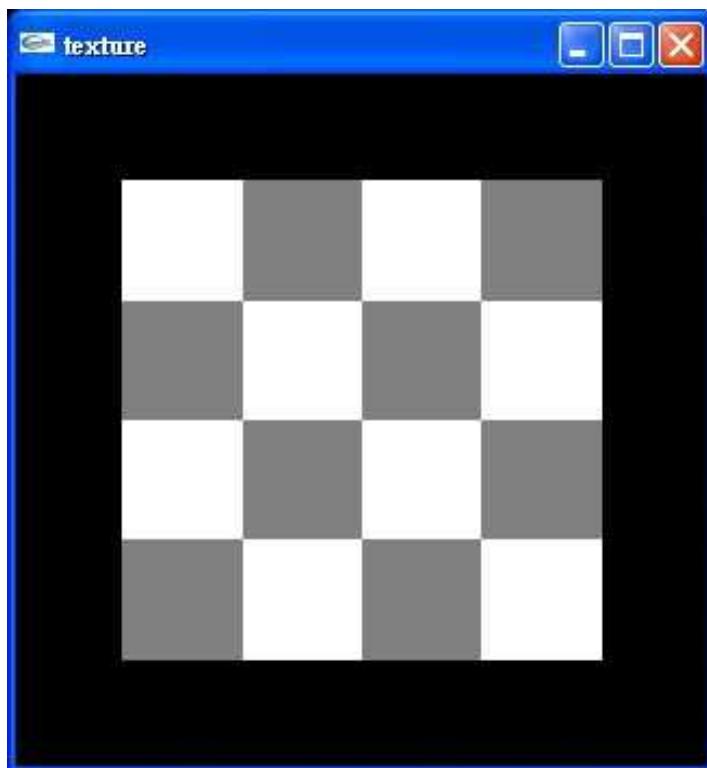


Constant color



# *Texture Functions*

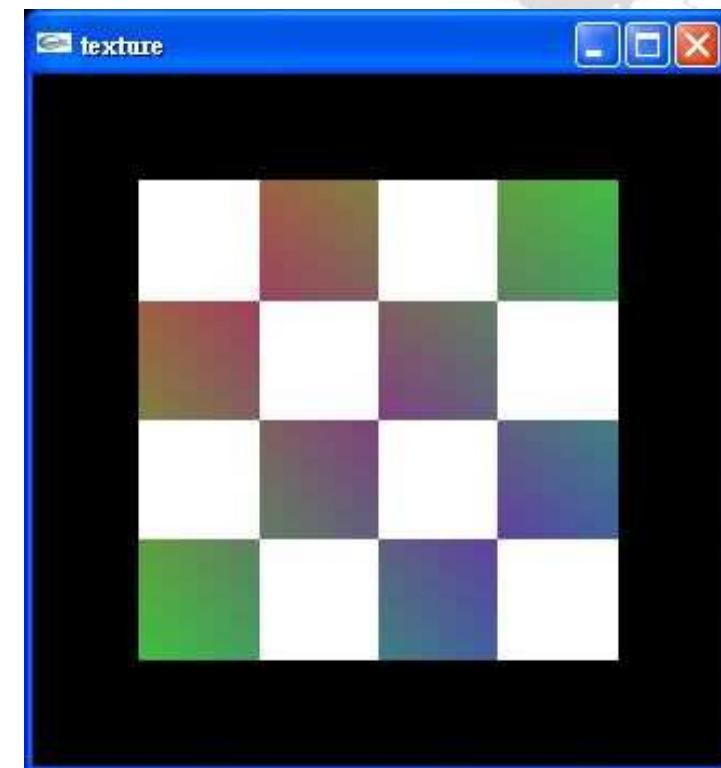
## ◆ Examples



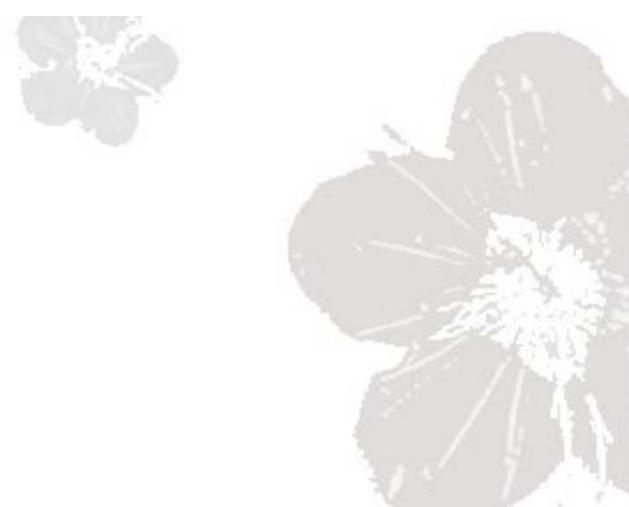
Replace



Modulate

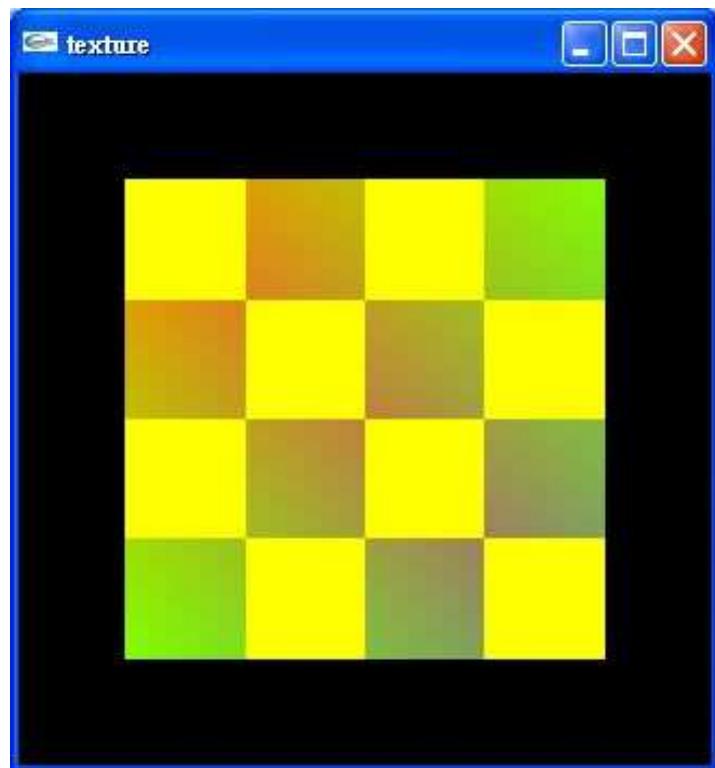


Decal

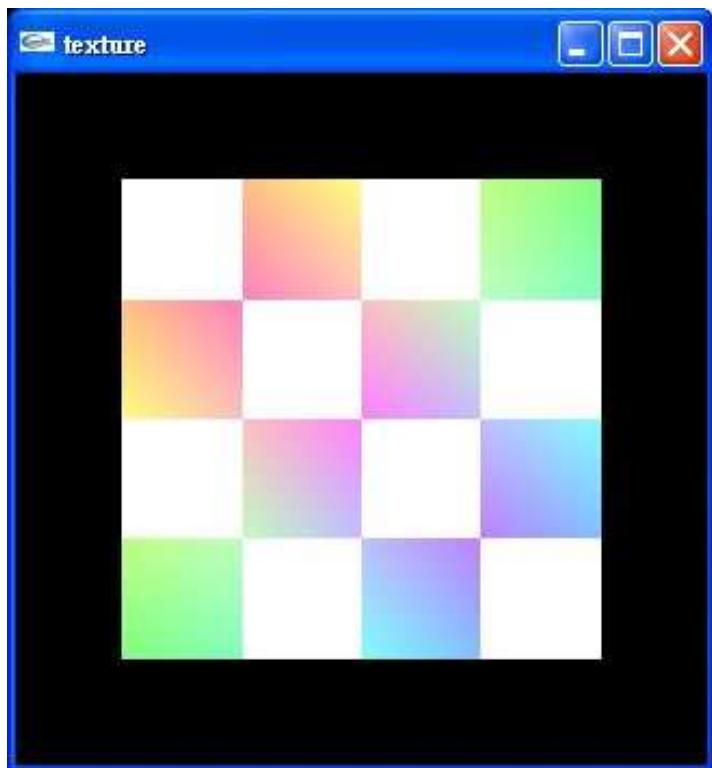


# *Texture Functions*

## ◆ Examples



Blend



Add

# *Texture Functions*

- ◆ Example
  - Modulation



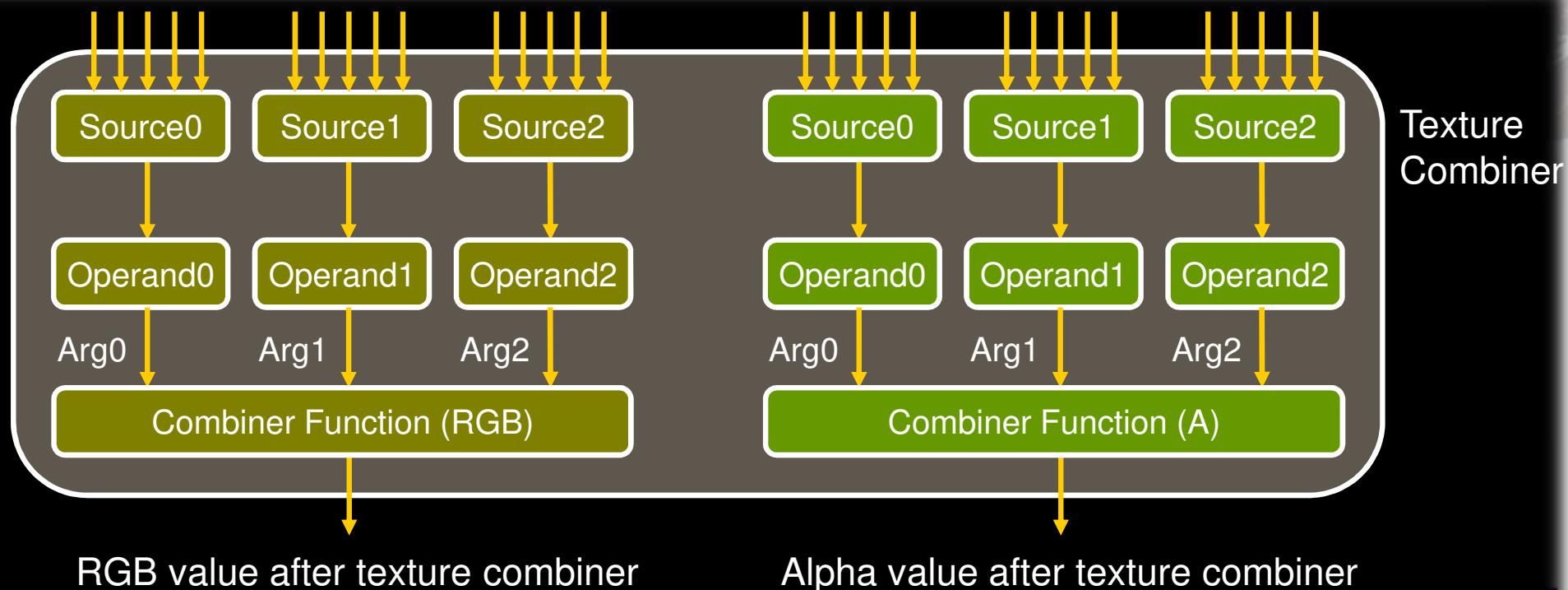
Lighting

Texturing

Lighting + Texturing

# *Texture Combiner Functions*

- ◆ Texture combiner functions are more powerful texture functions with flexible combinations of arguments and operations



# *Texture Combiner Functions*

## ◆ Eg. OpenGL texture combiner functions

<b>glTexEnv param</b>	<b>Combiner Function</b>
GL_REPLACE	$Arg0$
GL_MODULATE (default)	$Arg0 * Arg1$
GL_ADD	$Arg0 + Arg1$
GL_ADD_SIGNED	$Arg0 + Arg1 - 0.5$
GL_INTERPOLATE	$Arg0 * Arg2 + Arg1 * (1 - Arg2)$
GL_SUBTRACT	$Arg0 - Arg1$
GL_DOT3_RGB	$4 * ((Arg0_r - 0.5) * (Arg1_r - 0.5) +$
GL_DOT3_RGBA	$(Arg0_g - 0.5) * (Arg1_g - 0.5) +$ $(Arg0_b - 0.5) * (Arg1_b - 0.5))$

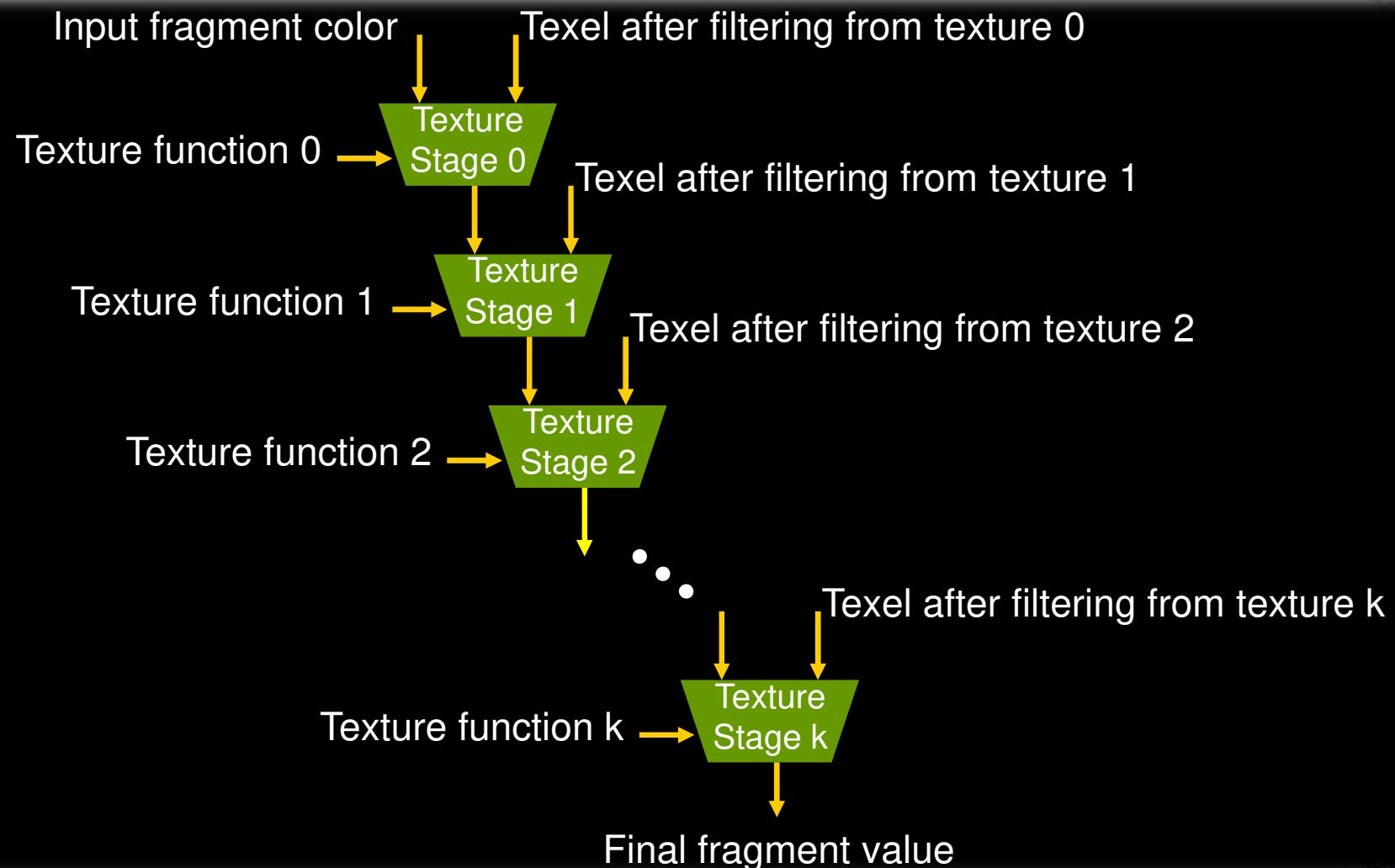


# *Texture Combiner Functions*

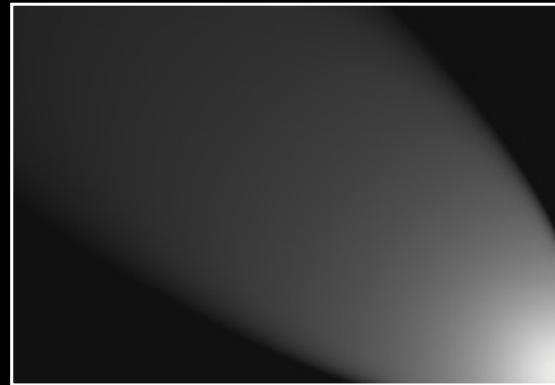
- ◆ Eg. OpenGL texture combiner functions
  - $\text{GL_SRC}_i\text{_RGB}$  or  $\text{GL_SRC}_i\text{_ALPHA}$  could be  $\text{GL\_TEXTURE}$ ,  $\text{GL\_TEXTURE}_n$ ,  $\text{GL\_CONSTANT}$ ,  $\text{GL\_PRIMARY\_COLOR}$ , or  $\text{GL\_PREVIOUS}$
  - $\text{GL_OPERAND}_i\text{_RGB}$  could be  $\text{SRC}_{RGB}$ ,  $1 - \text{SRC}_{RGB}$ ,  $\text{SRC}_A$ , or  $1 - \text{SRC}_A$
  - $\text{GL_OPERAND}_i\text{_ALPHA}$  could be  $\text{SRC}_A$ , or  $1 - \text{SRC}_A$

# Multi-Texturing

## ◆ Texture Stages



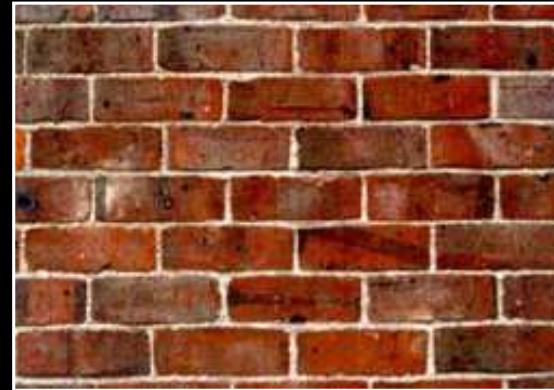
# *Multi-Texturing*



**Light Map**

×

(modulate)



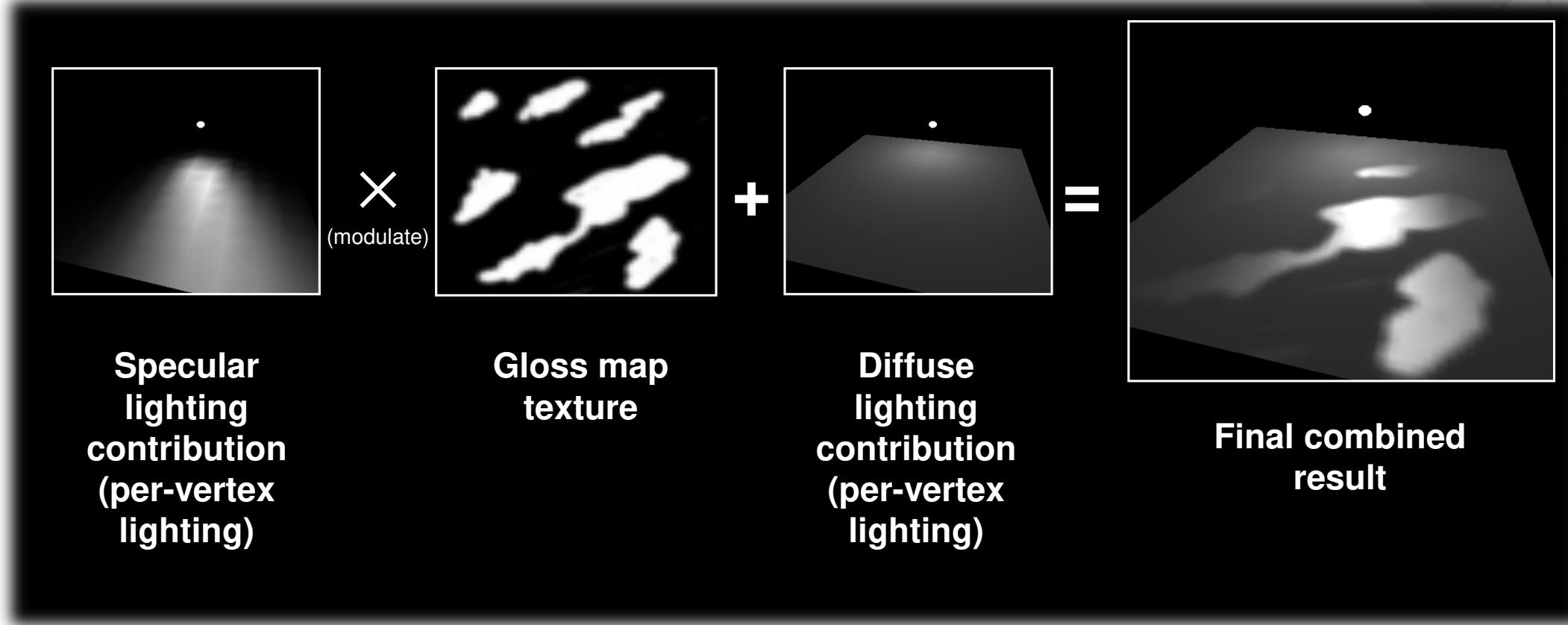
**Texture Map**

=

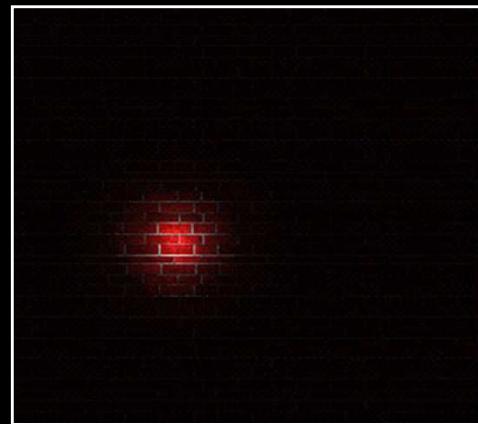


**Light Map Combine with Texture Map**

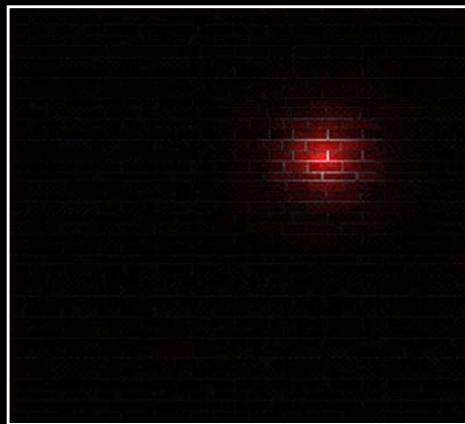
# *Multi-texturing*



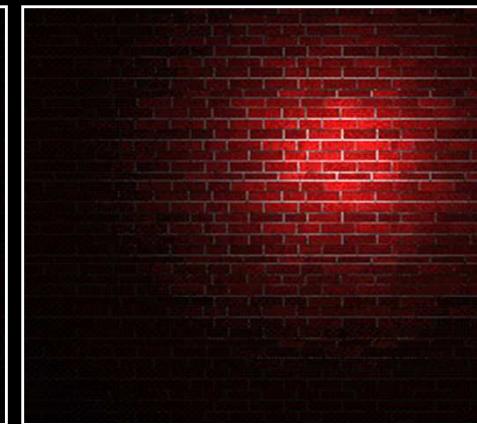
# *Texture Transform*



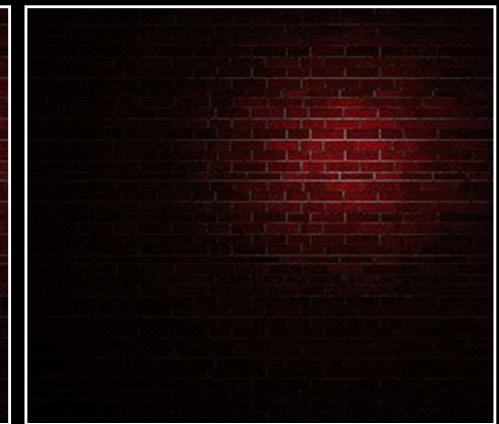
Original



Translate  
Spotlight  
Texture  
Coordinates



Scale  
Spotlight  
Texture  
Coordinates

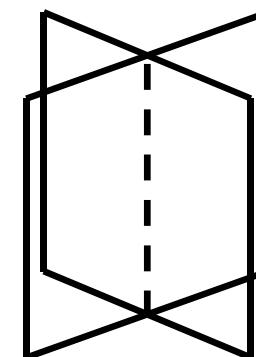


Change Base  
Polygon  
Intensity

Use texture matrix to perform spotlight texture coordinates transformations.

# *Billboard*

- ◆ Model details without increasing the complexity of geometric modeling

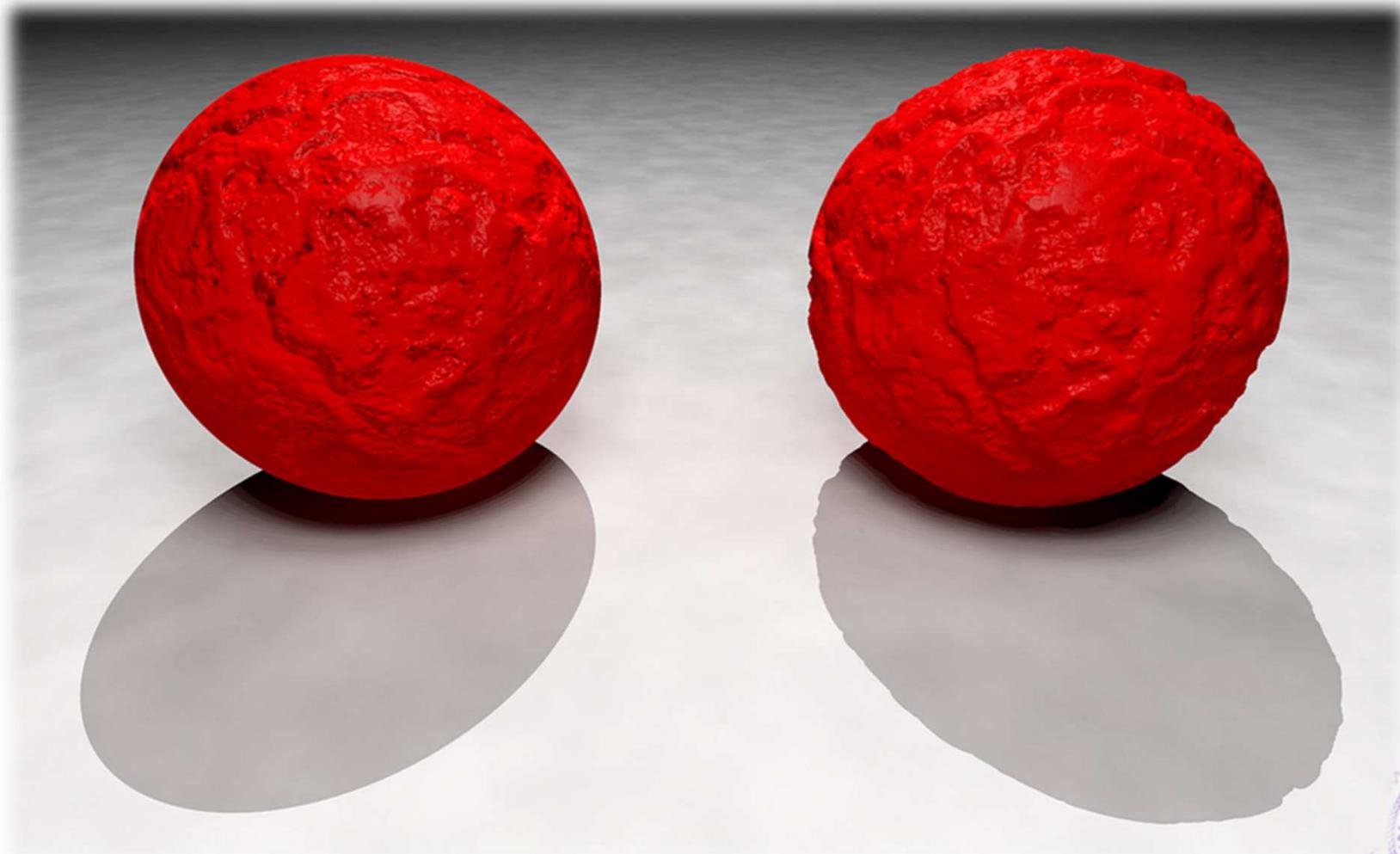


# *Bump Mapping*



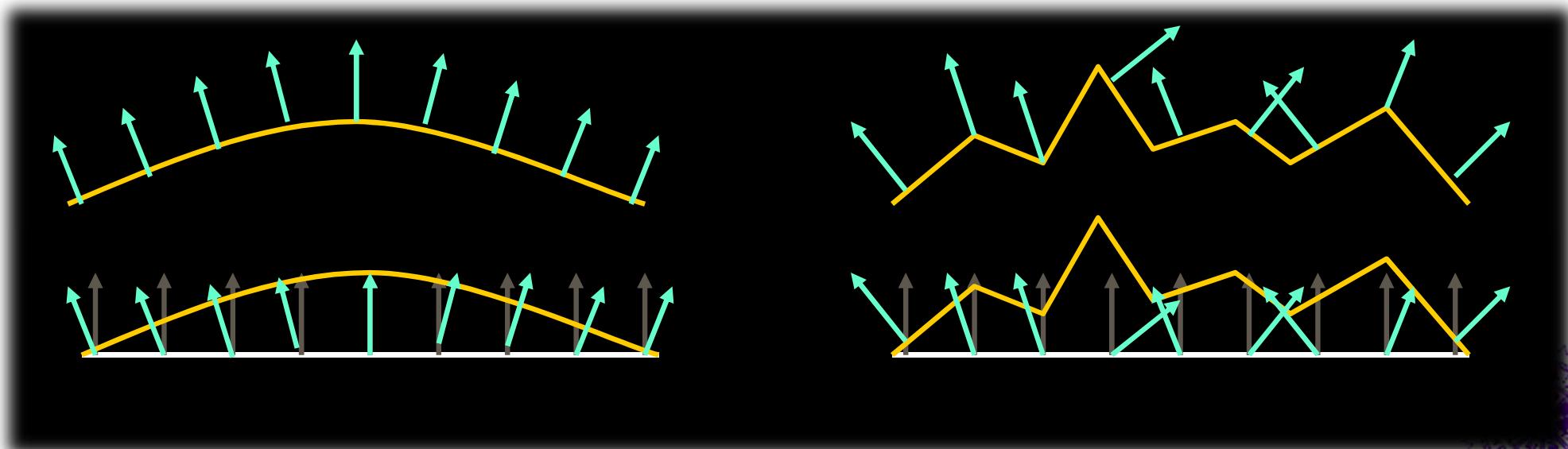
# *Bump Mapping*

- ◆ Bump mapping vs. displacement mapping



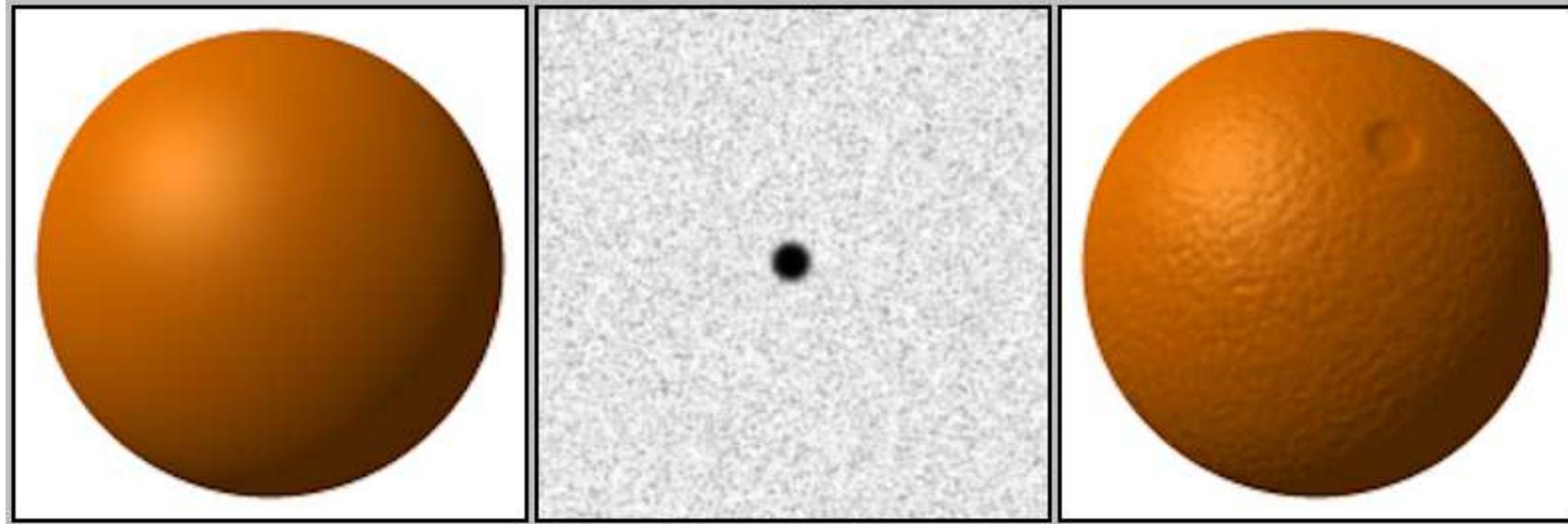
# Bump Mapping

- ◆ Apply texture map as the perturbation vectors to the pixel normals
- ◆ Apply lighting operation on the perturbed normals to create the illusion of bumpy surface



# Bump Mapping

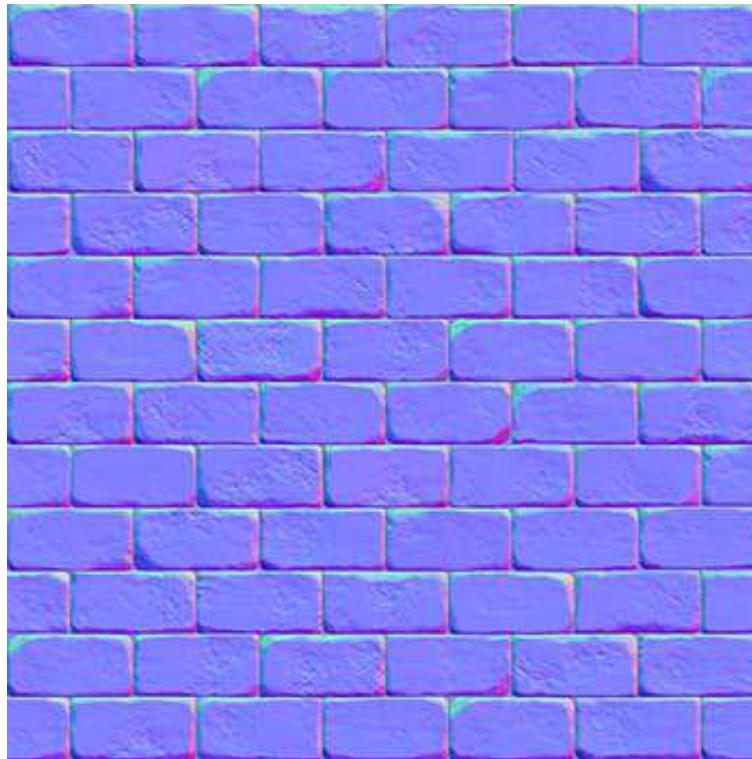
- ◆ Using height map to alter the surface normal



1. Look up the height in the heightmap that corresponds to the position on the surface.
2. Calculate the surface normal of the heightmap, typically using the finite difference method.
3. Combine the surface normal from step two with the true ("geometric") surface normal so that the combined normal points in a new direction.
4. Calculate the interaction of the new "bumpy" surface with lights in the scene using, for example, the Phong reflection model.

# *Bump Mapping*

- ◆ Using normal map to alter the surface normal



# *Bump Mapping*

- ◆ Using normal map to alter the surface normal



WITHOUT NORMAL MAPPING



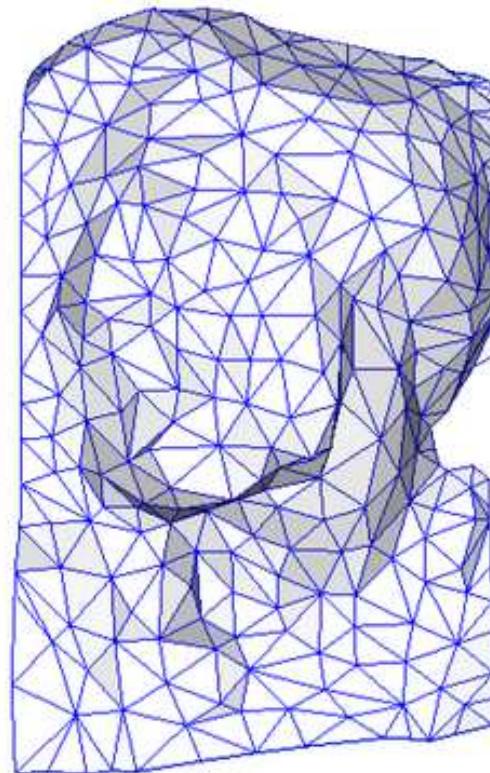
WITH NORMAL MAPPING

# Bump Mapping

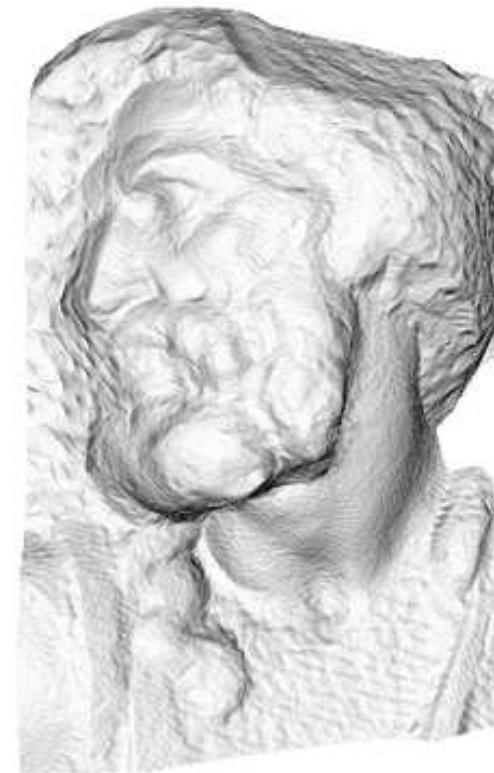
- ◆ Using normal map to alter the surface normal



original mesh  
4M triangles



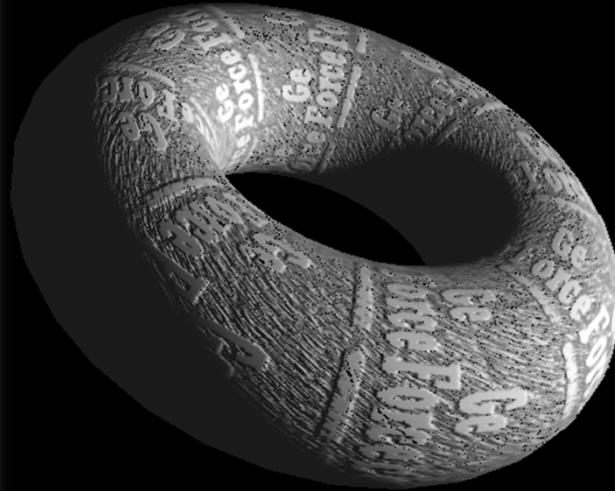
simplified mesh  
500 triangles



simplified mesh  
and normal mapping  
500 triangles

# Bump Mapping

Diffuse



Decal



Specular



X

+

=



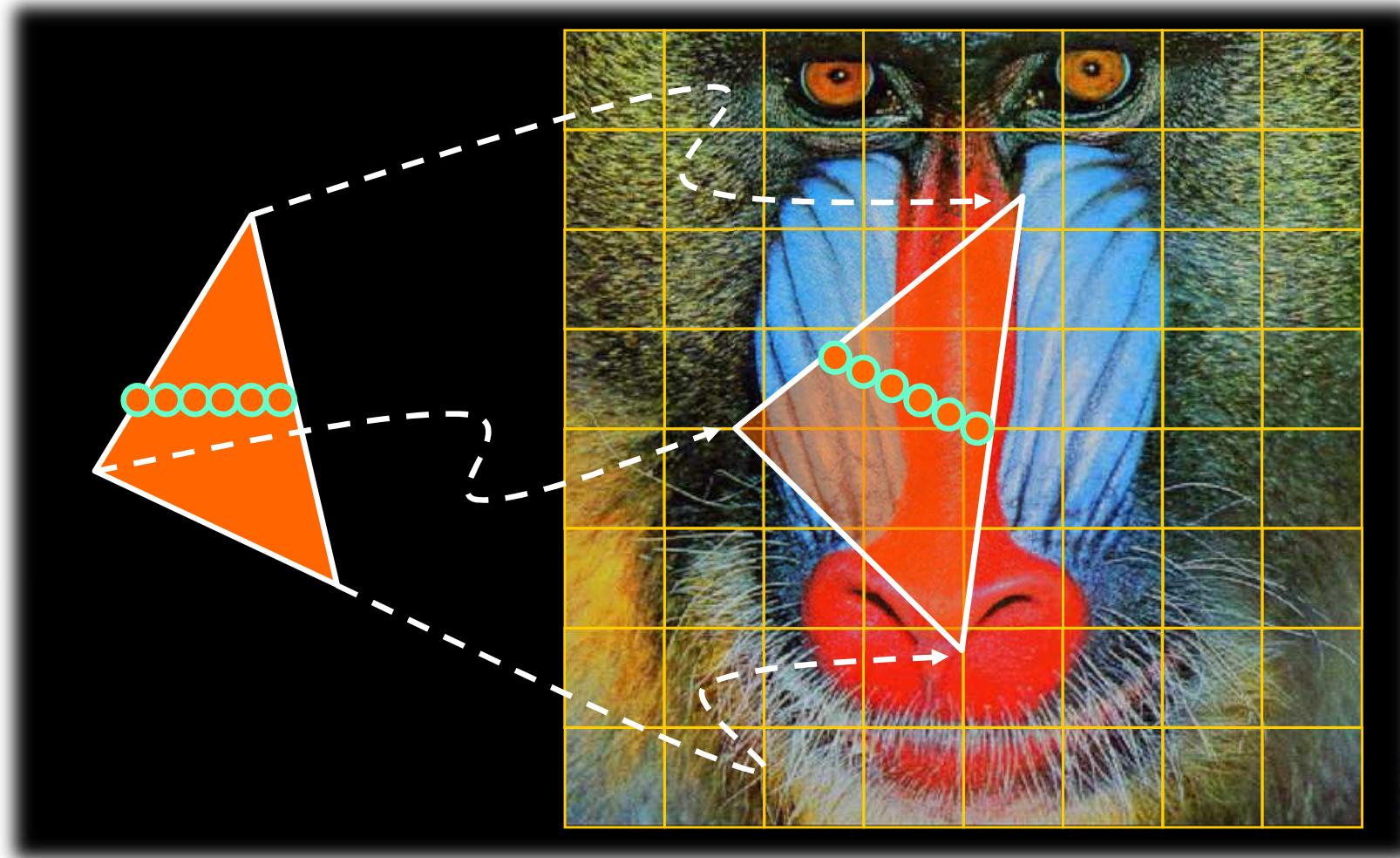
# *Hardware Consideration*

- ◆ **Use texture cache to reduce the number of memory access**
  - Access a group of texels instead of a single texel each time
  - Neighboring texels are likely to be accessed for the next fragment in texture mapping process
  - Texels are accessed and stored in the texture cache
  - Optimize the texel hit rate with suitable cache size and replacement rule



# *Hardware Consideration*

- ◆ Use tiled texture to utilize the locality of texture access



# *Hardware Consideration*

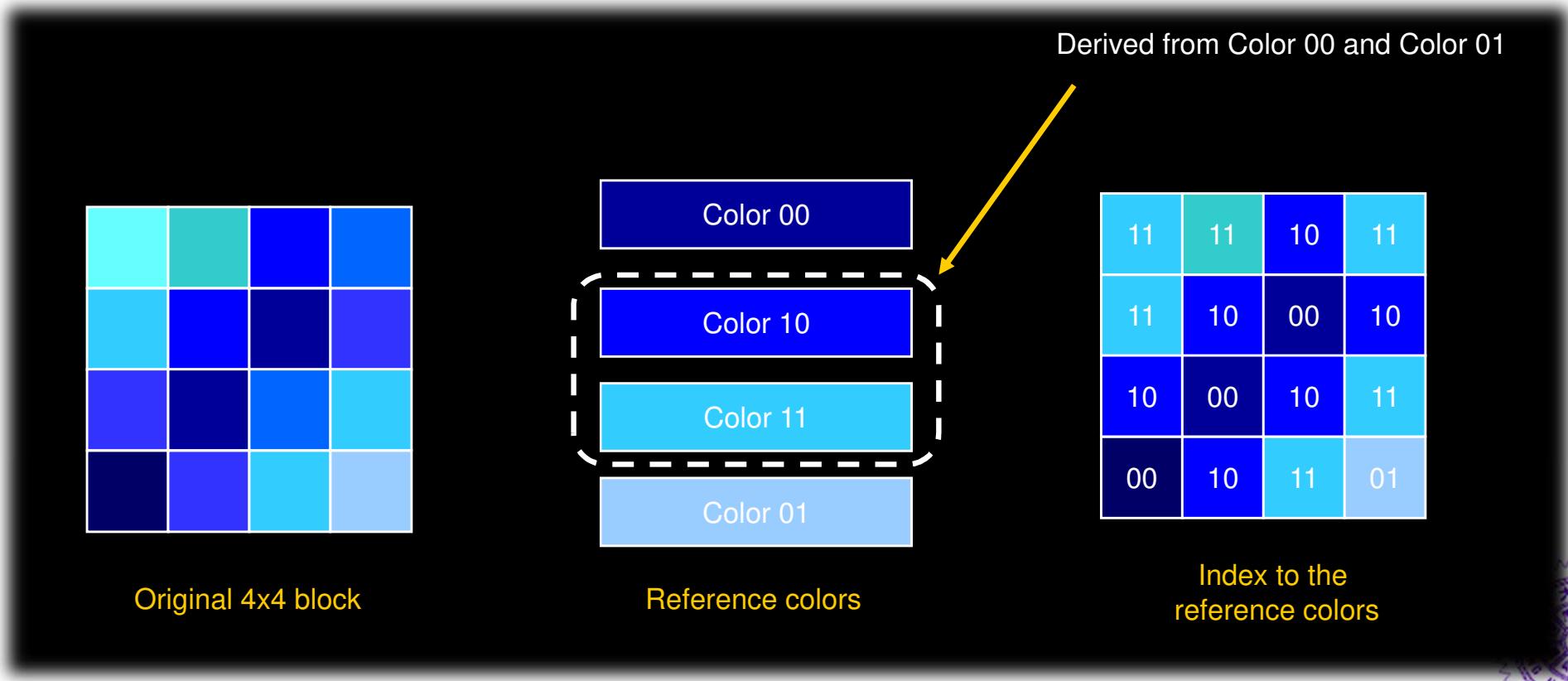
- ◆ **Use compressed texture to reduce the memory bandwidth requirement**
  - Decoding speed must fast
  - Good for random access
  - Lossy compression is allowed
  - Encoding speed is not as critical as other real time encoding requirement
  - Eg. S3TC, PVRTC, Ericsson TC



# Hardware Consideration

## ◆ S3TC Texture Compression

- 4x4 block encoding
- Fixed rate encode



# *Compressed Textures*

- ◆ Quality of compressed textures
- ◆ Eg. S3TC



a)

Uncompressed Texture



b)

S3TC compressed Texture

# Q&A

