

Matrix class

(provided by Matrices.h and .cpp)

Matrix initialization

```
//calculating rotation matrix
float sinX = sin(rotationX);
float cosX = cos(rotationX);
Matrix4 Rx = Matrix4(1, 0, 0, 0,
                      0, cosX, -1*sinX, 0,
                      0, sinX, cosX, 0,
                      0, 0, 0, 1);
```

```
float sinY = sin(rotationY);
float cosY = cos(rotationY);
Matrix4 Ry = Matrix4(cosY, 0, sinY, 0,
                      0, 1, 0, 0,
                      -1*sinY, 0, cosY, 0,
                      0, 0, 0, 1);
```

```
float sinZ = sin(rotationZ);
float cosZ = cos(rotationZ);
Matrix4 Rz = Matrix4(cosZ, -1*sinZ, 0, 0,
                      sinZ, cosZ, 0, 0,
                      0, 0, 1, 0,
                      0, 0, 0, 1);
```

Matrix multiplication

```
Matrix4 R = Rz*Ry*Rx
```



Vector class

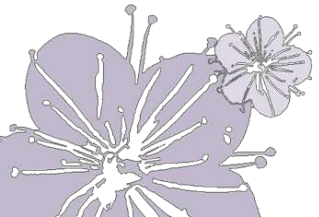
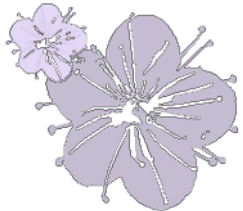
(provided by Matrices.h and .cpp)

initialization

```
Vector3 eyePos(eyeX, eyeY, eyeZ);
```

```
forwardVector = eyeLookAt - eyePos;
```

operation



MVP matrix

$$\mathbf{MVP} = \mathbf{P} * \mathbf{V} * \mathbf{M} = \mathbf{P} * (\mathbf{Vr} * \mathbf{Vt}) * (\mathbf{T} * \mathbf{S} * \mathbf{R} * \mathbf{N})$$

P: projection matrix

V: viewing matrix

→ Vr: viewing rotation, Vt: viewing translation

M: model matrix

→ T: model translation, S: model rotation,
R: model rotation, N: Normalization

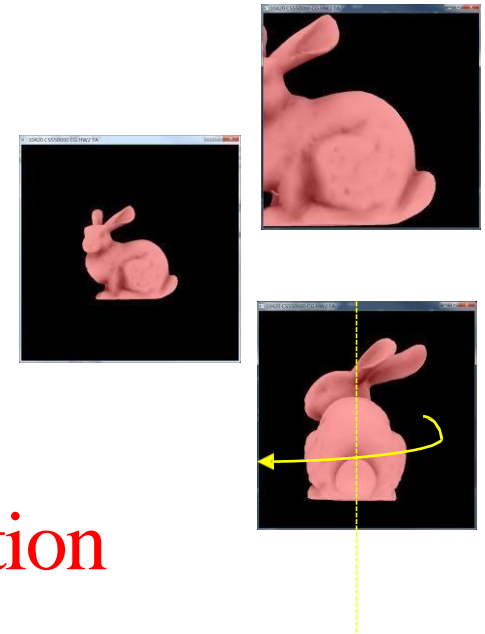


Geometrical Transformation

- Manipulate 3D models
 - Translation, scaling, rotation

$$\begin{bmatrix} \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \end{bmatrix} \begin{bmatrix} \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \end{bmatrix} \begin{bmatrix} \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \end{bmatrix}$$

P **V** **M**



- Normalize the model with transformation matrix!



Viewing Transformation

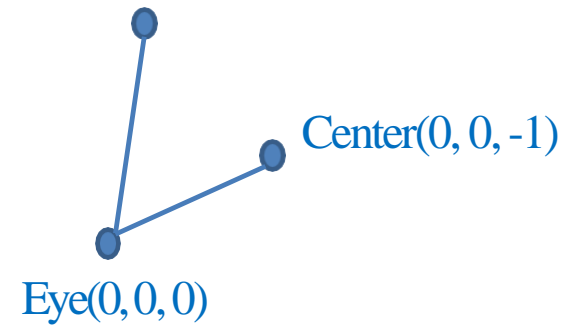
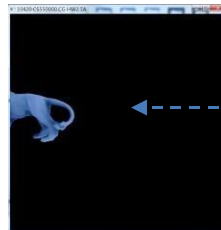
- Display 3D models from different view.
 - Eye position, center position, up position

$$\begin{bmatrix} \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \end{bmatrix} \begin{bmatrix} \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \end{bmatrix} \begin{bmatrix} \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \end{bmatrix}$$

P

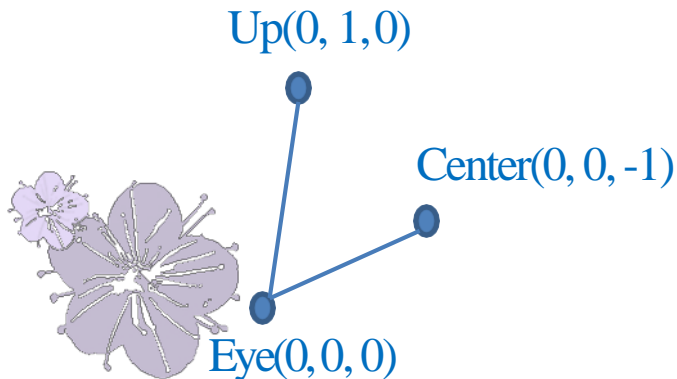
V

M

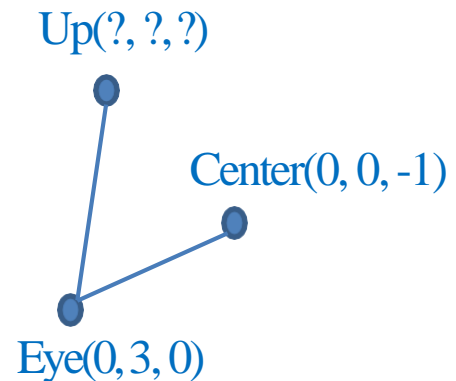


Relationship between Eye, Center, Up

- When change eye(center) position, we have to adjust up position to get a proper result, here is an example, if we move eye from $(0,0,0)$ to $(0,3,0)$



$$\text{Forward} = \text{center}(0,0,-1) - \text{eye}(0,0,0) = (0,0,-1)$$

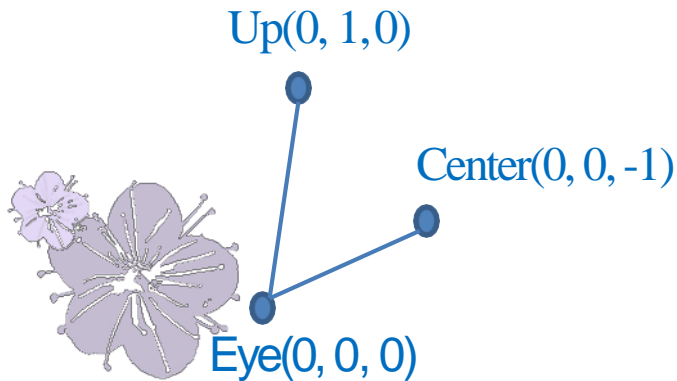


$$\text{Forward} = \text{center}(0,0,-1) - \text{eye}(0,3,0) = (0,-3,-1)$$

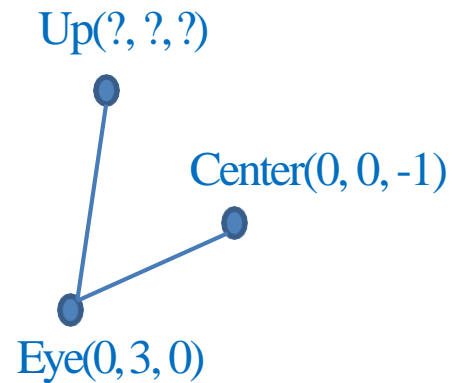


Relationship between Eye, Center, Up

- Because the forward vector and up vector must be perpendicular, now forward vector changed, we need to compute new up vector



$$\text{Forward} = \text{center}(0,0,-1) - \text{eye}(0,0,0) = (0,0,-1)$$

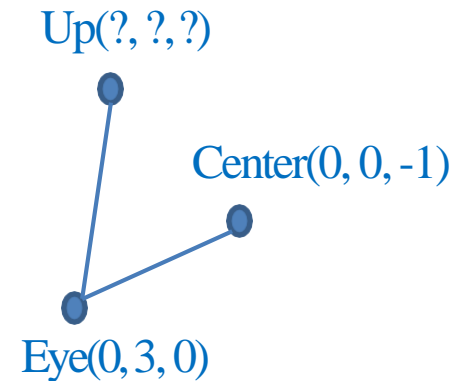
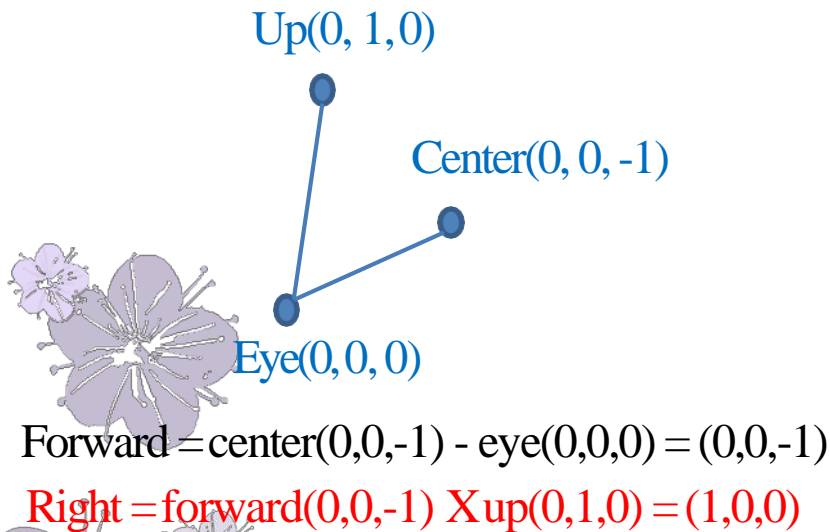


$$\text{Forward} = \text{center}(0,0,-1) - \text{eye}(0,3,0) = (0,-3,-1)$$



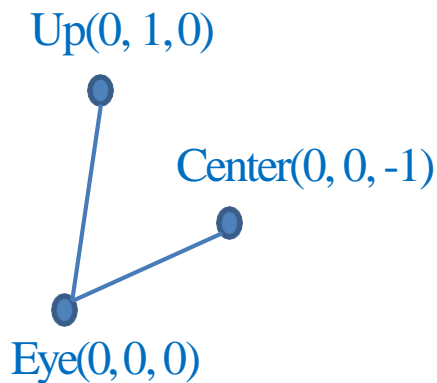
Relationship between Eye, Center, Up

- In this case, we can compute right vector by the cross product of forward and up vector(old one)

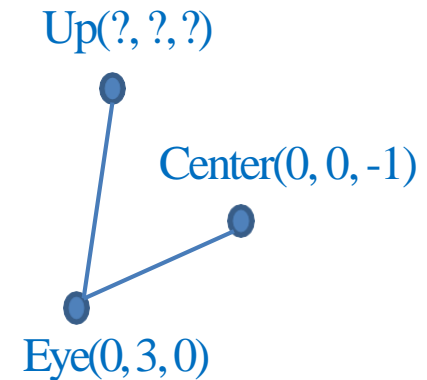


Relationship between Eye, Center, Up

- Finally re-compute new up vector by the cross product of right vector and forward vector, and find new up position!



$$\begin{aligned}\text{Forward} &= \text{center}(0,0,-1) - \text{eye}(0,0,0) = (0,0,-1) \\ \text{Right} &= \text{forward}(0,0,-1) \times \text{up}(0,1,0) = (1,0,0) \\ \text{Up} &= \text{right}(1,0,0) \times \text{forward}(0,0,-1) = (0,1,0)\end{aligned}$$



$$\begin{aligned}\text{Forward} &= \text{center}(0,0,-1) - \text{eye}(0,3,0) = (0,-3,-1) \\ \text{Right} &= \text{forward}(0,-3,-1) \times \text{up}(0,1,0) = (1,0,0)\end{aligned}$$

$$\begin{aligned}\text{Up vector(new)} &= \\ \text{right}(1,0,0) \times \text{forward}(0,-3,-1) &= (0,1,-3) \\ \text{Up(position)} &= \\ \text{eye}(0,3,0) + \text{up vector}(0,1,-3) &= (0,4,-3)\end{aligned}$$



Projection Transformation

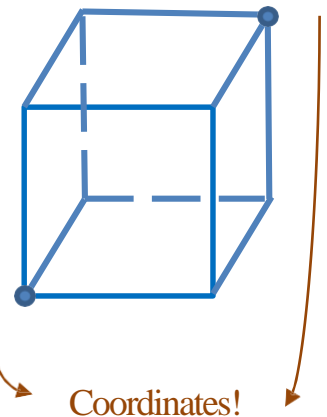
- Project 3D models on screen in different way.
 - Parallel(orthogonal), perspective projection

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \end{bmatrix} \begin{bmatrix} \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \end{bmatrix}$$

P **V** **M**

Default value in HW1
(parallel)
(xmax, ymax, zfar) = (1, 1, -1)

(xmin, ymin, znear) = (-1, -1, 1)



• Reference

– Transformation p.81-p.95



Projection Transformation

- Project 3D models on screen in different way.
 - Parallel(orthogonal), perspective

$$\begin{bmatrix} \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \end{bmatrix} \begin{bmatrix} \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \end{bmatrix} \begin{bmatrix} \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \\ \square & \square & \square & \square \end{bmatrix}$$

P

V

M

