

Subregular Learning of a Phonology and a Set of Underlying Forms

Wenyue Hua, Adam Jardine, and Huteng Dai

Rutgers University

Introduction

- **Learning problem:** the **simultaneous inference** of underlying representation (URs) and a phonological grammar from alternating surface representations (SRs)
(Merchant, 2008; Tesar, 2014; Cotterell et al., 2015)
- **Our proposal:** a solution based on the structure provided by the **input strictly local (ISL)** functions
(Chandlee and Heinz, 2018; Jardine et al., 2014)

English plural

The plural morpheme in English has at least two pronunciations: [s] and [z].

Morphemes	SR
CAT-PL	[kæts]
CUFF-PL	[kʌfs]
DEATH-PL	[dεθs]
GIRL-PL	[gɜ:rlz]
CHAIR-PL	[tʃɛərz]
BOY-PL	[bɔɪz]
...	...

English plural

The plural morpheme in English has at least two pronunciations: [s] and [z].

Analysis:

- A **map** from morphemes to URs
CAT → /kæt/
PL → /z/
etc.
- A **map** from URs to SRs
/z/ → [s] /[-SONORANT] —

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Formalizing the problem

- M : set of morphemes
- Σ : alphabet of both SR and UR segments
- Targets:
 - lexicon function $\ell : M^* \rightarrow \Sigma^*$
 - phonology function $\varphi : \Sigma^* \rightarrow \Sigma^*$
- Note: ℓ is an ISL₁ function from morphemes to URs

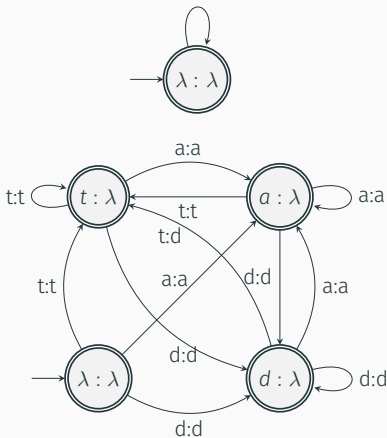
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- Note: ℓ is an ISL₁ function from morphemes to URs
- Learning data is generated by $\varphi \circ \ell$; i.e., a finite set D such that

$$\forall \langle m, s \rangle \in D, \quad \varphi(\ell(m)) = s$$

Target transducers and learning data

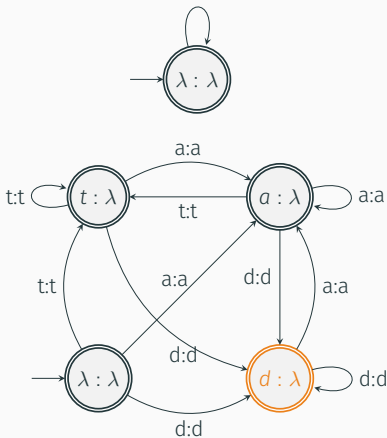
$r_1 : /tat/$ $s_1 : /ta/$
 $r_2 : /tad/$ $s_2 : /da/$
 $r_3 : /a/$ $s_3 : /da/$



m	s
$r_1 s_1$	[tatta]
$r_1 s_2$	[tatda]
$r_1 s_3$	[tata]
$r_2 s_1$	[tadda]
$r_2 s_2$	[tadda]
$r_2 s_3$	[tada]
$r_3 s_1$	[ata]
$r_3 s_2$	[ada]
$r_3 s_3$	[aa]

Target transducers and learning data

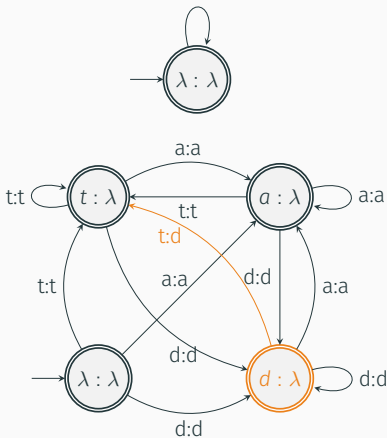
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$r_3 s_1$	[ata]
$r_3 s_2$	[ada]
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What does the learner know *a priori*?

- A lexicon of morphemes/lexical meanings (M), in which each morpheme has only one UR (ℓ is ISL_1).
- The ISL_k structure of phonology function. Here, we focus on ISL_2

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- The ISL_k structure of phonology function. Here, we focus on ISL_2
- ISL functions only make changes in the output with respect to the local information in the input.

Proposed Learner

- Initial hypothesis
- Learning procedure
 - Inconsistency detection
 - Environment collection
 - UR selection
 - Modification

- Initial hypothesis for ℓ : prefix tree transducer T_ℓ , obtained from SR segmentation based on longest common prefix (LCP)
(Oncina et al., 1993; Jardine et al., 2014)

Single Process Example: Initial lexicon transducer

<i>m</i>	<i>s</i>
r_1s_1	[tatta]
r_1s_2	[tatda]
r_1s_3	[tata]
r_2s_1	[tadda]
r_2s_2	[tadda]
r_2s_3	[tada]
r_3s_1	[ata]
r_3s_2	[ada]
r_3s_3	[aa]

← LCP of morphemes is r_1 , LCP of SR is tat

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← LCP of morphemes is r_2 , LCP of SR is tad

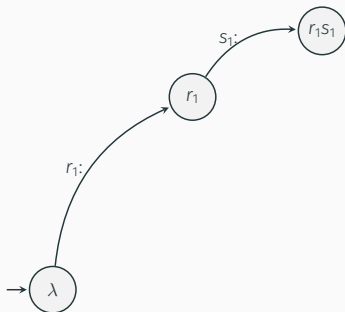
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r_2s_2	[tadda]
r_2s_3	[tada]
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r_3s_2	[ada]
r_3s_3	[aa]

← LCP of morphemes is r_3 , LCP of SR is a

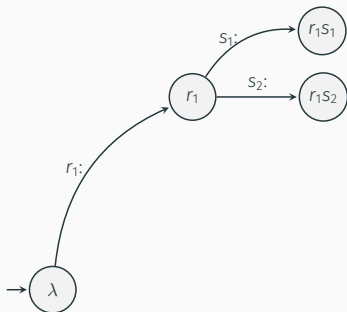
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<i>m</i>	<i>s</i>
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r_1s_3	[tata]
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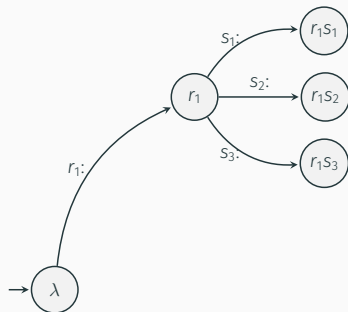
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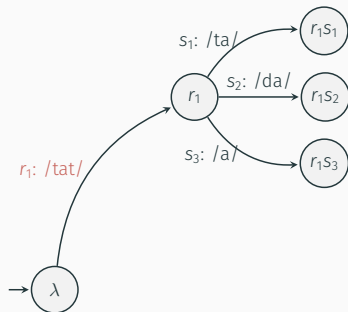
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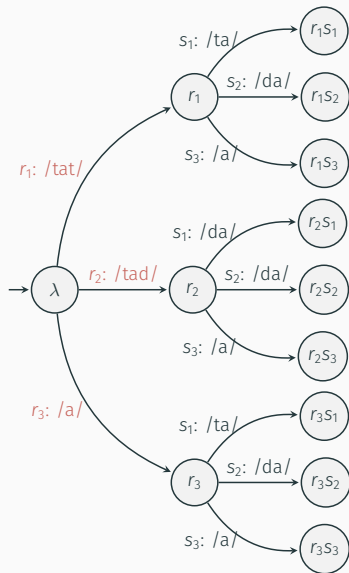
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Single Process Example: Initial lexicon transducer

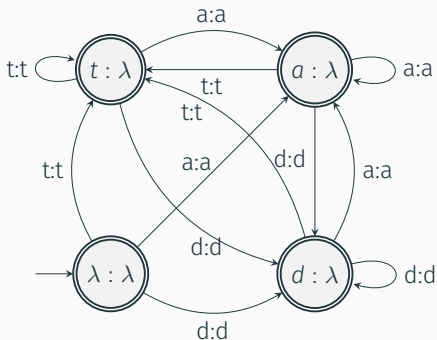
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Initial hypothesis

- Initial hypothesis for ℓ : prefix tree transducer T_ℓ , obtained from SR segmentation based on longest common prefix
(Oncina et al., 1993; Jardine et al., 2014)
- Initial hypothesis for φ : ISL₂ transducer T_φ for identity function

Single Process Example: phonology transducer



Identity function:

/tadt/ → [tadt]

/tatt/ → [tatt]

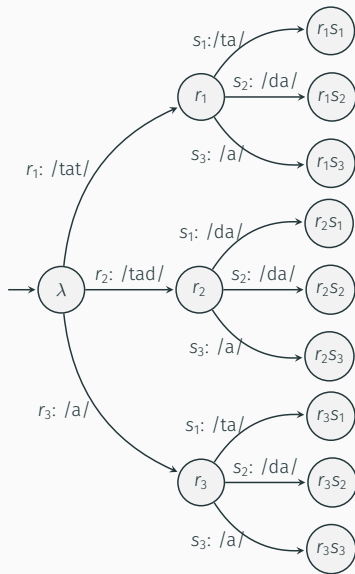
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Learning Procedure

- Modify lexicon transducer T_ℓ until one UR per morpheme
- For each change in lexicon transducer T_ℓ , make *opposite* change in phonology transducer T_φ

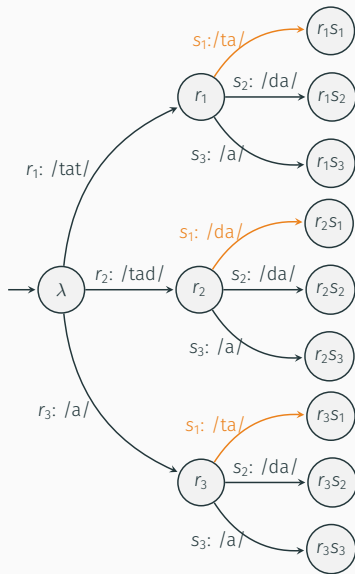
Inconsistency detection

The learner detects the inconsistency on lexicon transducer T_ℓ



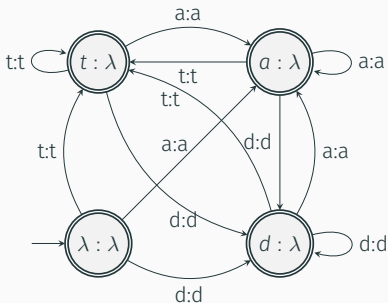
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Environment Collection

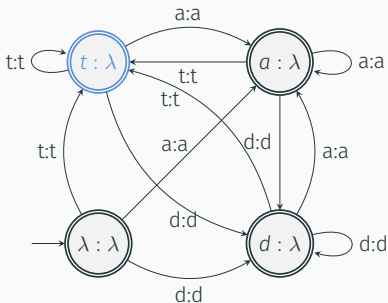
Find environment for different SRs based on the phonology transducer.



environment	S_1
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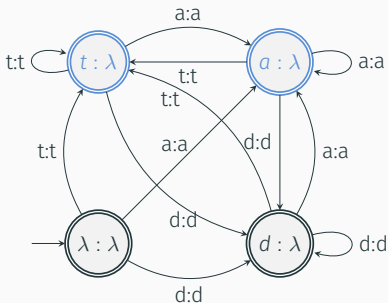
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	environment	s_1
$r_1 s_1$	tat	ta

Environment Collection

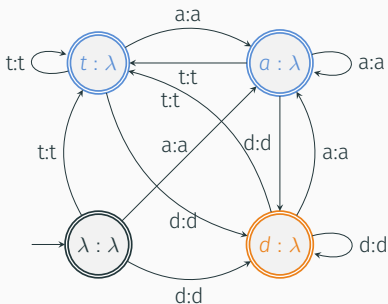
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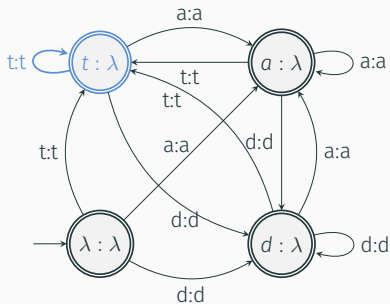
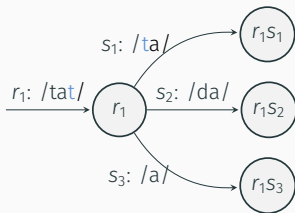


	environment	S_1
$r_1 S_1$	tat	ta
$r_3 S_1$	a	ta
$r_2 S_1$	tad	da

Modifying Transducers

Change SR into UR in the prefix-tree transducer.

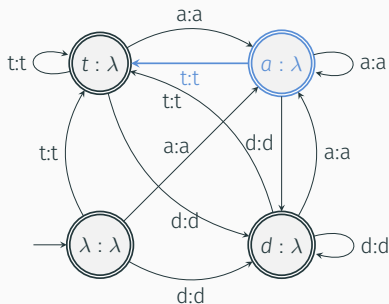
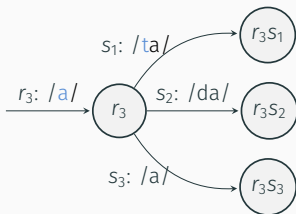
Make an opposite change in the phonology transducer.



Modifying Transducers

Change SR into UR in the prefix-tree transducer.

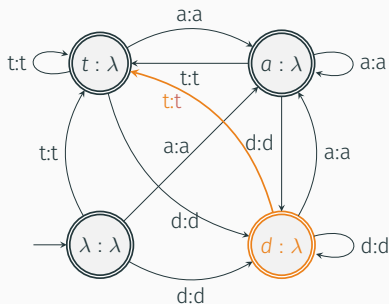
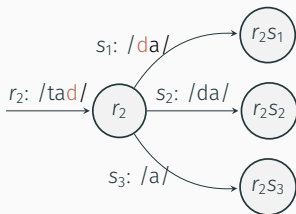
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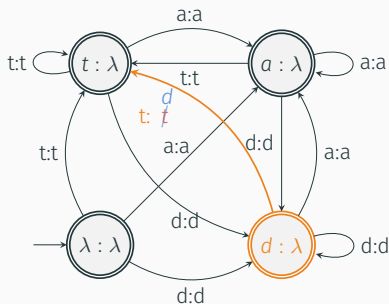
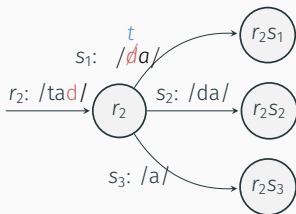
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Modifying Transducers

Change SR into UR in the prefix-tree transducer.

Make an opposite change in the phonology transducer.



Primary Result

- The learner can learn assimilation, dissimilation, deletion, epenthesis and metathesis.
- So far it learns only one phonology process from a data set.
- In particular, it is able to learn opacity, *i.e.* self-counter-feeding and self-counter-bleeding.

- Learn multiple phonology processes simultaneously from one data set.
- Learn all ISL_2 functions.
- Learn all ISL_k functions for any given k .
- Learn Output-Strictly-Local (OSL) phonology transformations.
(Chandlee et al., 2015).
- ...

Discussion

Three questions

- Why we design an ISL learner, *i.e.* why not OSL learner or Output Tier Based Strictly Local (OTSL) learner?

(Chandlee et al., 2015; Burness and McMullin, 2019)

- How abstract is the learnt UR? Specifically, is it able to learn abstract URs?

(Kiparsky, 1968; Kenstowicz and Kisseberth, 2014)

- What differentiate subregular learners from other learners?

- Empirically significant: 94% of phonology patterns in P-Base database are ISL.

(Mielke, 2004; Chandlee and Heinz, 2018).

- Learning based on the structure of ISL class can be extended to OSL and OTSL functions, which both share a particular structure

Can we learn abstract URs?

- It depends.

Can we learn abstract URs?

- It depends.
- Two cases: whether the abstract UR exerts phonological influence on the target phonology function.

Subregular learner vs. Other learners

- Current learner: **specific to learning phonology**.
(Gallistel and King, 2011; Heinz, 2010).
- Cue-based parameter setting model and Learners based on Optimality Theory: **non-specific to learning phonology**
(Dresher and Kaye, 1990; Dresher, 1999; Jarosz, 2006; Apoussidou, 2007; Merchant, 2008; Merchant and Tesar, 2008).

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(Dresher and Kaye, 1990; Dresher, 1999; Jarosz, 2006; Apoussidou, 2007; Merchant, 2008; Merchant and Tesar, 2008).
- Modular learning: an ISL learner is an independent module in learning the whole phonology. By composing different modules, the knowledge of the whole is acquired.

Heinz (2010, 2011).

Conclusion

- Subregular classes of functions provide structure for the simultaneous induction of URs and the phonological grammar
- The general procedure here can be extended to learning iterative (output-based) processes, long-distance processes, and process interactions

Acknowledgements

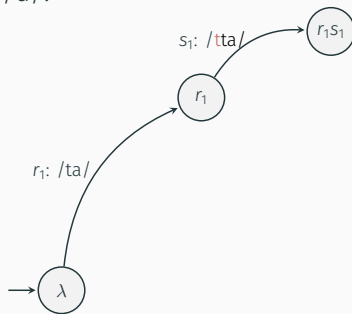
We thank Bruce Tesar, Adam McCollum, Mariapaola D'imperio, Chris Oakden, Dine Mamadou, Jill Harper, Sreekar Raghotham, the Rutgers MathLing group, and the audience at the Rutgers/SBU/Haverford/Delaware subregular phonology workshop, for their insightful comments.

Questions?

Regressive Assimilation

/t/ becomes voiced [d] before /d/.

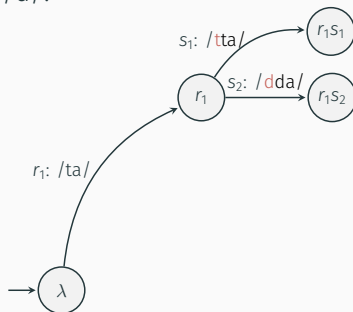
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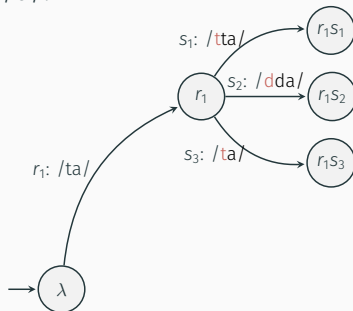
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Regressive Assimilation

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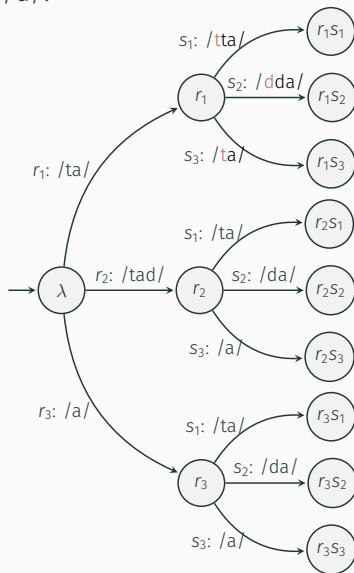
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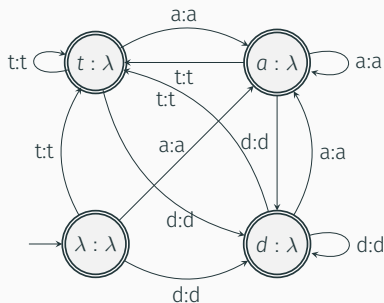
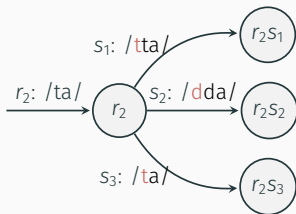
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Modifying Transducers

Change SR into UR in the prefix-tree transducer.

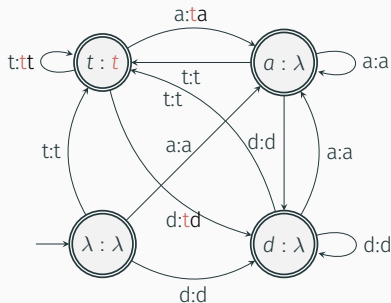
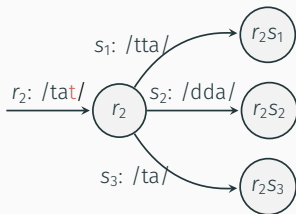
Make an opposite change in the phonology transducer.



Modifying Transducers

Change SR into UR in the prefix-tree transducer.

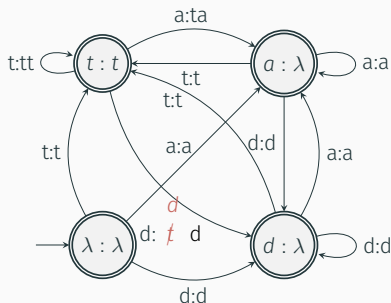
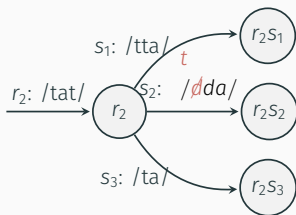
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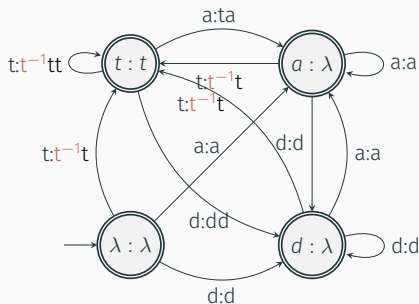
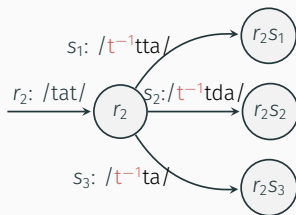
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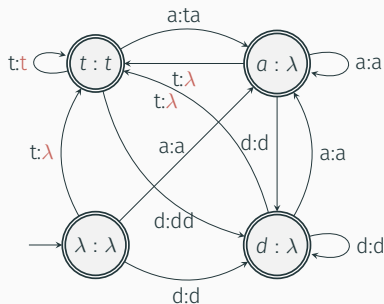
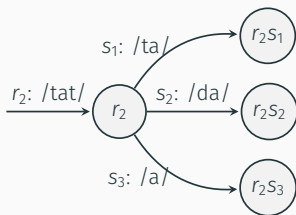
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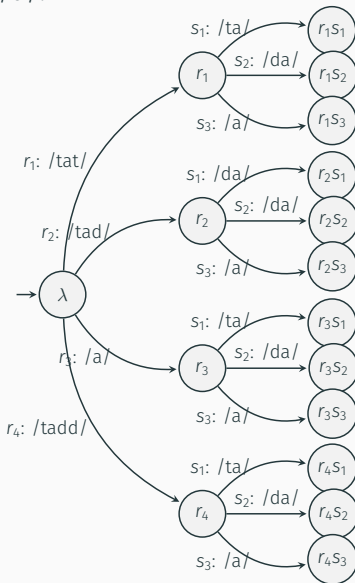


- counter-feeding:
- counter-bleeding:

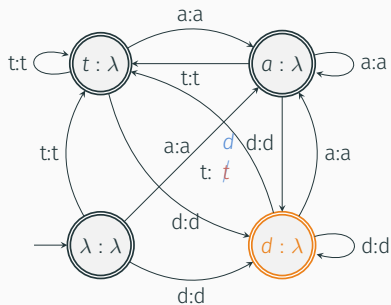
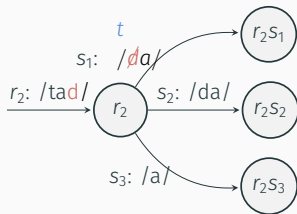
Counter-feeding

/t/ becomes a voiced [d] after /d/.

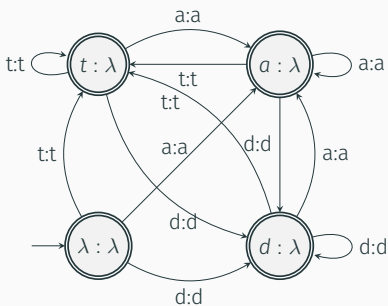
<i>m</i>	<i>s</i>
r_1s_1	[tatta]
r_1s_2	[tatda]
r_1s_3	[tata]
r_2s_1	[tadda]
r_2s_2	[tadda]
r_2s_3	[tada]
r_3s_1	[ata]
r_3s_2	[ada]
r_3s_3	[aa]
r_4s_1	[taddta]
r_4s_2	[taddda]
r_4s_3	[tadda]



Modified Transducer

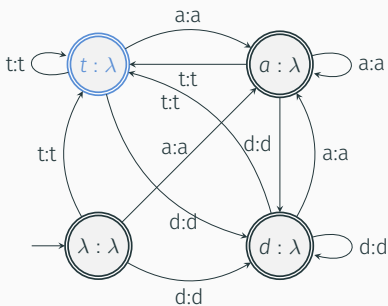


What about the environment?



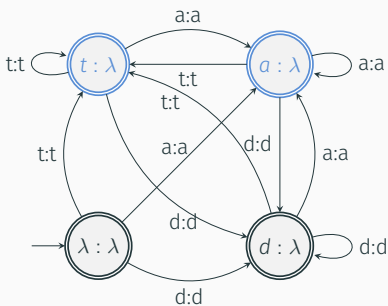
environment	s_1
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What about the environment?



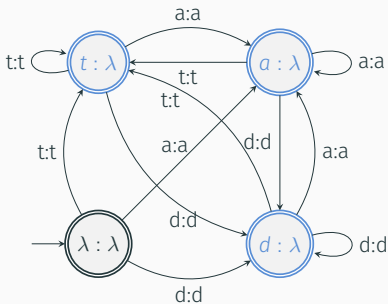
environment	s_1
$r_1 s_1$	tat ta

What about the environment?



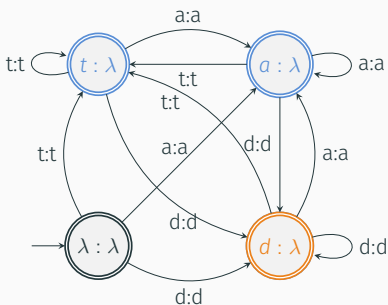
	environment	s_1
$r_1 s_1$	tat	ta
$r_3 s_1$	a	ta

What about the environment?



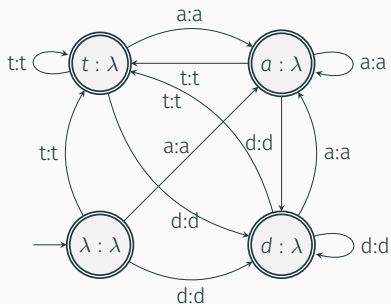
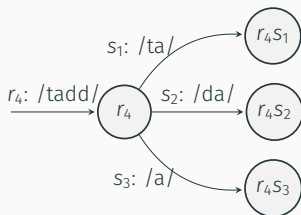
	environment	s_1
$r_1 s_1$	tat	ta
$r_3 s_1$	a	ta
$r_4 s_1$	tadd	ta

What about the environment?

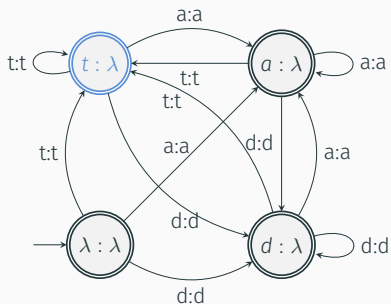
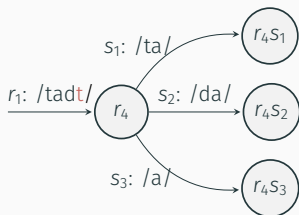


	environment	s_1
$r_1 s_1$	tat	ta
$r_3 s_1$	a	ta
$r_4 s_1$	tadd	ta
$r_2 s_1$	tad	da

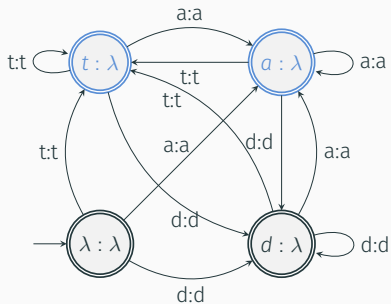
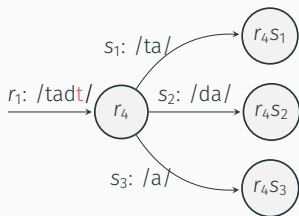
What should we do about the clash of the environment?



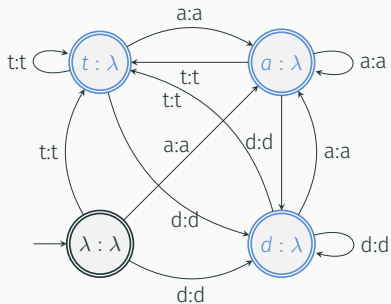
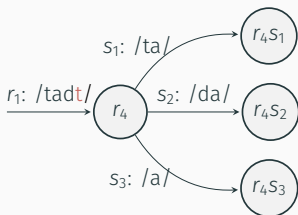
What should we do about the clash of the environment?



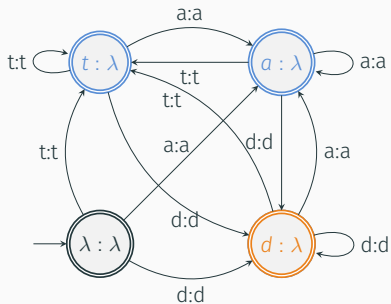
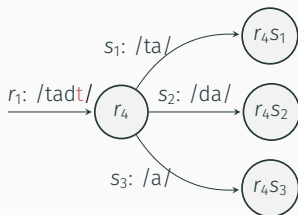
What should we do about the clash of the environment?



What should we do about the clash of the environment?



What should we do about the clash of the environment?



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