

## R-1.12

The following remarkably short and tricky function determines whether a nonnegative integer  $i$  is a power of 2.

```
bool isTwoPower(int i) {  
    return (i != 0) && (((i-1) & i) == 0);  
}
```

The function makes use of the fact that the binary representation of a of  $i = 2^k$  is a 1 bit followed by  $k$  0 bits. In this case, the binary representation of  $i - 1$  is a 0 bit followed by  $i$  1 bits. Thus, when we take the bitwise “and” of the two bit strings, all the bits cancel out.

$$\begin{aligned}i &= 1024_{10} &= 000010000000000_2 \\i - 1 &= 1023_{10} &= 000001111111111_2 \\i \& (i - 1) &= 000000000000000_2\end{aligned}$$

If  $i$  is not a power of 2 and  $i > 0$ , then the bit strings for  $i$  and  $i - 1$  share at least one bit in common, the highest order bit, and so their bitwise “and” will be nonzero. We need to include a special check for zero, since it will pass this test but zero is not a power of 2.