Test a Perceptual Phenomenon

August 18, 2018

```
In [3]: import pandas as pd
    import math as m
    from scipy import stats
```

1 Questions For Investigation

1.1 1. What is our independent variable? What is our dependent variable?

The independent variable is different conceptual conditions. The dependent variable is response time.

1.2 2. What is an appropriate set of hypotheses for this task? What kind of statistical test do you expect to perform? Justify your choices.

The population parameters are not given. So the t-test is a reasonable choice. According to the Wikipedia article about Stroop effect, naming the ink of congruent stimuli is faster than the neutral condition by the *semantic facilitation*. By the way, the naming the ink of incongruent stimuli is slower than the neutral condition by the *semantic interference*. Therefore, I'll use a one-sided test of the hypothesis. The null and alternative hypothesis follow

- H_0 : $\mu_c = \mu_i$ The time to say the color of the ink is the same for congruent and incongruent word set.
- H_a: μ_c < μ_i The time to say the color of the ink of congruent word set is shorter than that of incongruent word set.

Also, the two conditions are measured repeatedly on paired samples. So I'll perform a dependent t-test for paired samples.

1.3 3. Report some descriptive statistics regarding this datasets. Include at least one measure of central tendency and at least one measure of variability.

First, read the data into DataFrame.

```
Out [4]:
             Congruent
                         Incongruent
                12.079
                              19.278
        0
        1
                16.791
                              18.741
        2
                              21.214
                 9.564
        3
                 8.630
                              15.687
        4
                              22.803
                14.669
        5
                12.238
                              20.878
        6
                14.692
                              24.572
        7
                 8.987
                              17.394
        8
                 9.401
                              20.762
        9
                14.480
                              26.282
                              24.524
        10
                22.328
        11
                15.298
                              18.644
                              17.510
        12
                15.073
                              20.330
        13
                16.929
        14
                18.200
                              35.255
        15
                12.130
                              22.158
        16
                18.495
                              25.139
        17
                10.639
                              20.429
        18
                11.344
                              17.425
        19
                12.369
                              34.288
        20
                12.944
                              23.894
        21
                14.233
                              17.960
        22
                19.710
                              22.058
        23
                16.004
                              21.157
```

The number of particiants is 24. The mean time of incongruent is larger than congruent condition as expected. I'll test the statistics whether this difference has a significant meaning.

```
In [9]: stroop.describe()
```

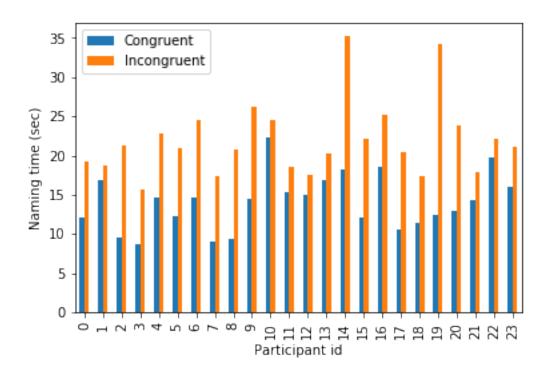
```
Out [9]:
               Congruent
                           Incongruent
        count
               24.000000
                             24.000000
               14.051125
                             22.015917
        mean
        std
                 3.559358
                              4.797057
        min
                 8.630000
                             15.687000
        25%
               11.895250
                             18.716750
        50%
               14.356500
                             21.017500
        75%
               16.200750
                             24.051500
        max
               22.328000
                             35.255000
```

1.4 4. Provide one or two visualizations that show the distribution of the sample data. Write one or two sentences noting what you observe about the plot or plots.

Every participant was slower when they name the incongruent word set.

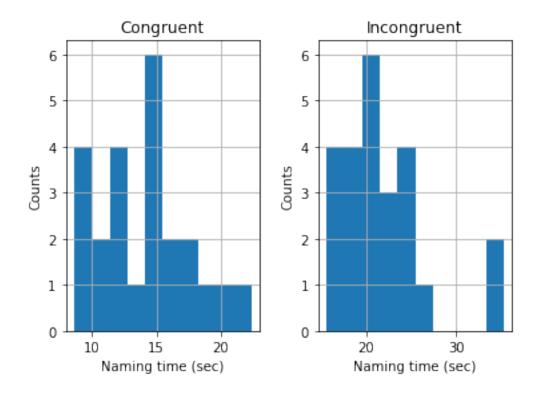
```
In [8]: ax = stroop.plot(kind='bar')
          ax.set_xlabel("Participant id")
          ax.set_ylabel("Naming time (sec)")
```

Out[8]: Text(0,0.5,'Naming time (sec)')



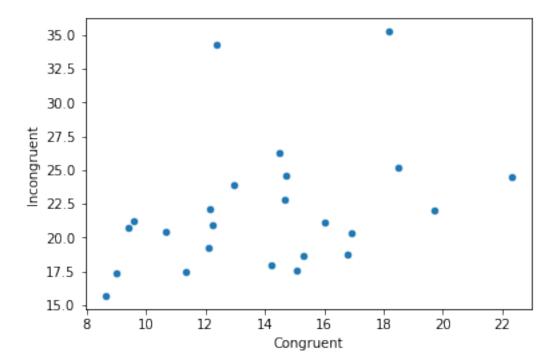
The congruent and incongruent data have a mode at around 15 and 20 seconds, respectively.

```
In [33]: axarr = stroop.hist(bins=10)
    for ax in axarr.flatten():
        ax.set_xlabel("Naming time (sec)")
        ax.set_ylabel("Counts")
```



The participant takes more time to name congruent word set, also take more time to name incongruent word set.

```
In [36]: stroop.plot(kind='scatter', x='Congruent', y='Incongruent')
Out[36]: <matplotlib.axes._subplots.AxesSubplot at 0x112b5da90>
```



The data of congruent and incongruent has week correlation.

1.5 5. Now, perform the statistical test and report your results. What are your confidence level and your critical static value? Do you reject the null hypothesis or fail to reject it? Come to a conclusion in terms of the experiment task. Did the results match up with your expectations?

The mean times of each condition are $\bar{t}_c = 14.05$, $\bar{t}_i = 22.02$.

The standard deviation of the differences is S = 4.86.

```
In [45]: (stroop['Congruent'] - stroop['Incongruent']).std()
Out[45]: 4.864826910359056
   The t-statistic is t = -8.02.
In [47]: (stroop['Congruent'].mean() - stroop['Incongruent'].mean()) / ((stroop['Congruent'] - Out[47]: -8.020706944109955)
```

The p-value of this t-statistic is too small to find at t-table. However, we can still use a software from GraphPad. With the degree of freedom, df = 23, it shows that the corresponding p-value is less than 0.0001. Therefor, we can reject the null with confidence interval of 99.9%.

The above procedure can be done with the following simple step. The p-value of the following result is for a two-tailed test, so the value should be halved to be used for the one-tailed test.

```
In [49]: stats.ttest_rel(stroop['Congruent'], stroop['Incongruent'])
Out[49]: Ttest_relResult(statistic=-8.020706944109957, pvalue=4.103000585711178e-08)
```

1.6 6. Optional: What do you think is responsible for the effects observed? Can you think of an alternative or similar task that would result in a similar effect? Some research about the problem will be helpful for thinking about these two questions!

According to the Wikipedia article, there are several theories to explain the Stroop effect and are known as *race models*. This is based on that the two information are processed in parallel, but 'race' to enter the single central processor during response selection.

There are several variations of the Stroop effect. For example, the orientation and position of arrows consist of the interference information. Another example is the written number and size of that number.