Test a Perceptual Phenomenon

August 18, 2018

```
In [46]: import pandas as pd
         import math as m
         from scipy import stats
```

1 Questions For Investigation

1.1 1. What is our independent variable? What is our dependent variable?

The independent variable is a list of words with congruent and incongruent word conditions. The dependent variable is time to say out loud the color of the ink in which the word is printed.

1.2 2. What is an appropriate set of hypotheses for this task? What kind of statistical test do you expect to perform? Justify your choices.

The population parameters are not given. So the t-test is a reasonable choice. According to the Wikipedia article about Stroop effect, naming the ink of congruent stimuli is faster than the neutral condition by the *semantic facilitation*. By the way, the naming the ink of incongruent stimuli is slower than the neutral condition by the *semantic interference*. Therefore, I'll use a one-sided test of the hypothesis. The null and alternative hypothesis follow

- H_0: $t_c \geq t_i$ The time to say the color of the ink is the same for congruent and incongruent word set.
- H_a: $t_c < t_i$ The time to say the color of the ink of congruent word set is shorter incongruent word set.

Also, the two conditions are measured repeatedly on paired samples. So I'll perform a dependent t-test for paired samples.

1.3 3. Report some descriptive statistics regarding this datasets. Include at least one measure of central tendency and at least one measure of variability.

First, read the data into DataFrame.

```
In [6]: stroop = pd.read_csv("./stroopdata.csv")
        stroop
```

```
Out[6]:      Congruent  Incongruent
        0       12.079       19.278
        1       16.791       18.741
        2        9.564       21.214
        3        8.630       15.687
        4       14.669       22.803
        5       12.238       20.878
        6       14.692       24.572
        7        8.987       17.394
        8        9.401       20.762
        9       14.480       26.282
        10      22.328       24.524
        11      15.298       18.644
        12      15.073       17.510
        13      16.929       20.330
        14      18.200       35.255
        15      12.130       22.158
        16      18.495       25.139
        17      10.639       20.429
        18      11.344       17.425
        19      12.369       34.288
        20      12.944       23.894
        21      14.233       17.960
        22      19.710       22.058
        23      16.004       21.157
```

The number of particiants is 24. The mean time of incongruent is larger than congruent condition as expected. I'll test the statistics whether this difference has a significant meaning.

```
In [9]: stroop.describe()

Out[9]:        Congruent  Incongruent
        count  24.000000    24.000000
        mean   14.051125    22.015917
        std     3.559358     4.797057
        min     8.630000    15.687000
        25%    11.895250    18.716750
        50%    14.356500    21.017500
        75%    16.200750    24.051500
        max    22.328000    35.255000
```
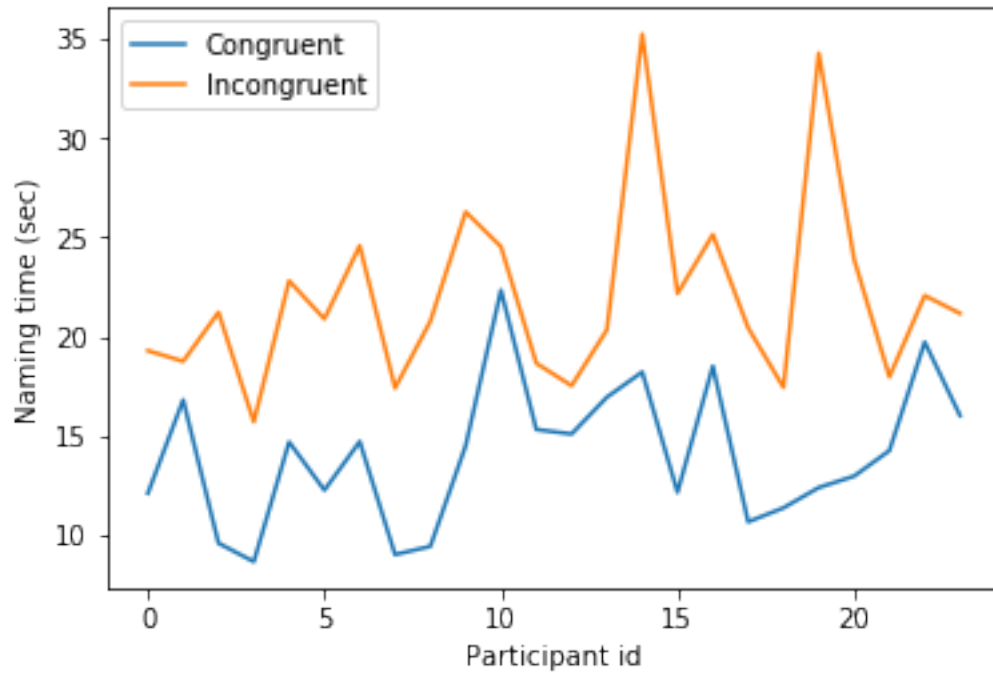
1.4 4. Provide one or two visualizations that show the distribution of the sample data. Write one or two sentences noting what you observe about the plot or plots.

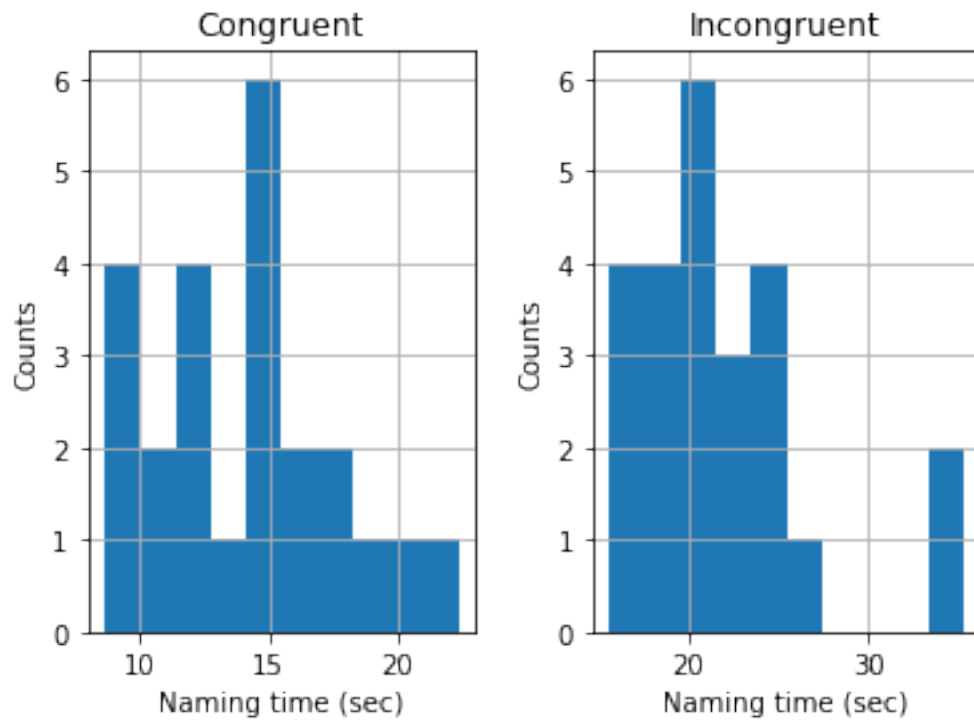Every participant was slower when they name the incongruent word set.

```
In [30]: ax = stroop.plot()
         ax.set_xlabel("Participant id")
         ax.set_ylabel("Naming time (sec)")
```

2

The congruent and incongruent data have a mode at around 15 and 20 seconds, respectively.
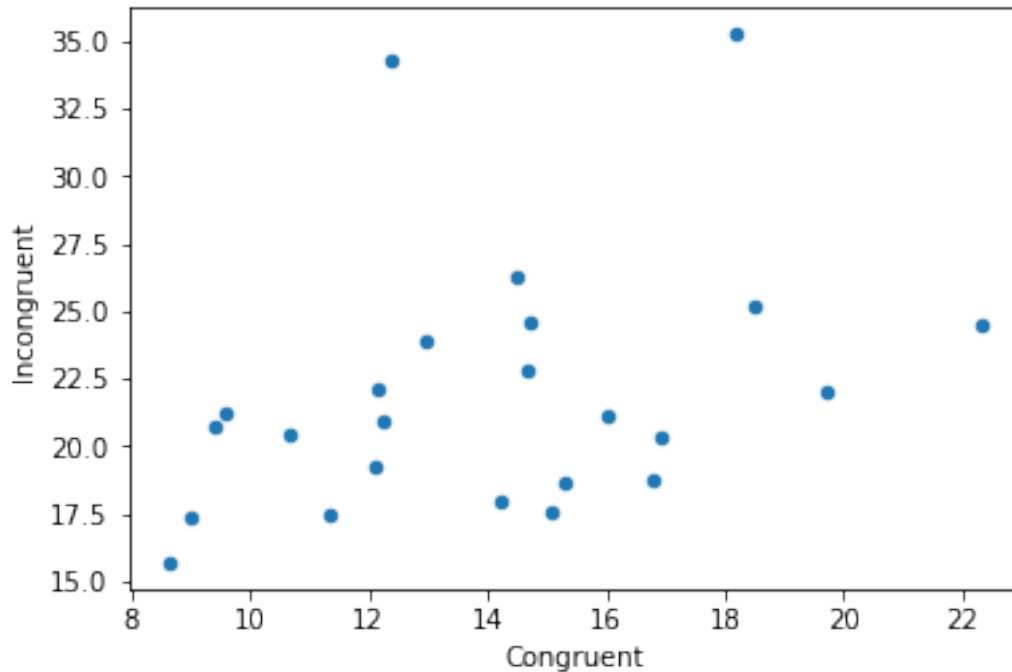
```
In [33]: axarr = stroop.hist(bins=10)
         for ax in axarr.flatten():
             ax.set_xlabel("Naming time (sec)")
             ax.set_ylabel("Counts")
```

The participant takes more time to name congruent word set, also take more time to name incongruent word set.

```
In [36]: stroop.plot(kind='scatter', x='Congruent', y='Incongruent')

Out[36]: <matplotlib.axes._subplots.AxesSubplot at 0x112b5da90>
```

The data of congruent and incongruent has week correlation.

```
In [37]: stroop.corr()
```

```
Out[37]:               Congruent  Incongruent
         Congruent      1.00000      0.35182
         Incongruent    0.35182      1.00000
```

1.5   5. Now, perform the statistical test and report your results. What are your confidence level and your critical static value? Do you reject the null hypothesis or fail to reject it? Come to a conclusion in terms of the experiment task. Did the results match up with your expectations?

The mean times of each condition are $\bar{t}_c = 14.05$, $\bar{t}_i = 22.02$.

```
In [38]: stroop.mean()
```

```
Out[38]: Congruent      14.051125
         Incongruent    22.015917
         dtype: float64
```

The point estimate is $\mu_c - \mu_i = -7.96$.

```
In [44]: stroop['Congruent'].mean() - stroop['Incongruent'].mean()
```

```
Out[44]: -7.964791666666665
```

The standard deviation of the differences is $S = 4.86$.

```
In [45]: (stroop['Congruent'] - stroop['Incongruent']).std()

Out[45]: 4.864826910359056
```

The t-statistic is $t = -8.02$.

```
In [47]: (stroop['Congruent'].mean() - stroop['Incongruent'].mean()) / ((stroop['Congruent'] -

Out[47]: -8.020706944109955
```

The p-value of this t-statistic is too small to find at t-table. However, we can still use a software from GraphPad. With the degree of freedom, df $= 23$, it shows that the corresponding p-value is less than 0.0001. Therefor, we can reject the null with confidence level of 99.9%.

The above procedure can be done with the following simple step. The p-value of the following result is for a two-tailed test, so the value should be halved to be used for the one-tailed test.

```
In [49]: stats.ttest_rel(stroop['Congruent'], stroop['Incongruent'])

Out[49]: Ttest_relResult(statistic=-8.020706944109957, pvalue=4.103000585711178e-08)
```

1.6 6. Optional: What do you think is responsible for the effects observed? Can you think of an alternative or similar task that would result in a similar effect? Some research about the problem will be helpful for thinking about these two questions!

According to the Wikipedia article, there are several theories to explain the Stroop effect and are known as *race models*. This is based on that the two information are processed in parallel, but 'race' to enter the single central processor during response selection.

There are several variations of the Stroop effect. For example, the orientation and position of arrows consist of the interference information. Another example is the written number and size of that number.