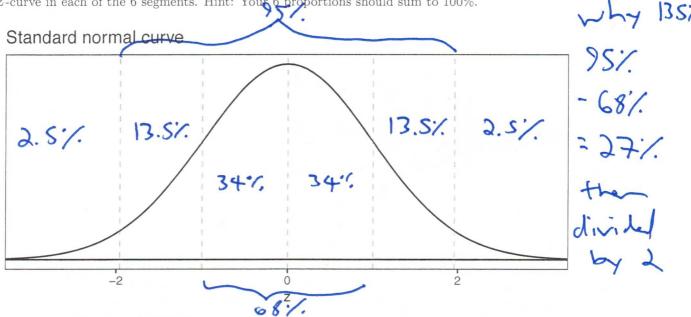
Short Answer 1

a) Below we have a standard Normal Z-curve along with 5 vertical dashed lines at z = -1.96, -1, 0, 1, and 1.96 cutting the x-axis into 6 segments. In the plot below, write down the 6 proportion of values under the Z-curve in each of the 6 segments. Hint: Your 6 proportions should sum to 100%.



a) Analysis of Variance (ANOVA) compares k group means for the following hypothesis test:

$$H_0: \mu_1 = \mu_2 = \ldots = \mu_k$$

 H_A : At least one of the k means is different

For example, in class we compared the mean life expectancy of countries in k=5 continents. What other

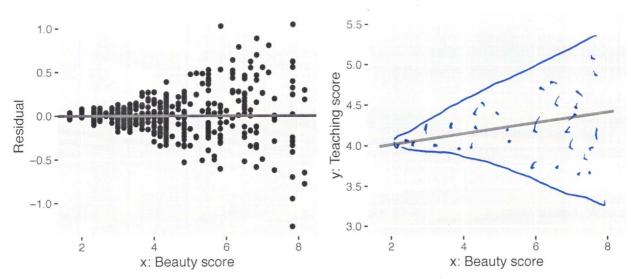
achieved by regession

statistical technique covered in this course would allow us to similarly compare group means?

d) A test statistic is a X of the unknown population parameter of interest used for hypothesis testing. What is X? point estimate

f) The null distribution used in hypothesis testing for computing p-values is the X distribution of the test statistic assuming Y. What are X and Y?

Sam pling null hypothesis is to d) Say we perform a regression to model an instructors' teaching score as a function of their beauty score, and obtain the following residual plot on the left which exhibits heteroskedasticity. Draw a rough sketch of what the scatterplot of x and y would look like given that the red line is the fitted regression line.



e) Say we perform a residual analysis of a regression model and find that the residuals exhibit very strong heteroskedasticity as above. What implications does this have for the results of our analysis?

for p-value & confidence internals
for regression to have valid
interpretation, all of conditions
for inference must be met.
If violated, we'll need to
improve the model some how

3 Evals continued

Recall the evals data of teaching evaluations of professors. Let say instead that these 463 professors are a randomly chosen set of instructors from all of the University of Texas system and not just UT Austin. Consider the following *simple linear regression* using only one numerical explanatory variable:

score_model <- lm(score ~ age, data = evals)
get_regression_table(score_model)</pre>

term	estimate	std_error	lower_ci	upper_ci
intercept	4.46	0.13	4.21	4.7
age	-0.01	0.00	-0.01	0.0

a) Interpret the slope coefficient for age.

For every of of I year in age, there is an associated decrease of on any 0.01 teaching units

b) Using statistical language, interpret the standard error for the slope for age.

If we were to take more samples
of your essors them the same or
Similar population & reported this
analysis, the SE quantities the variation
of Using non technical language, interpret the standard error for the slope for age.

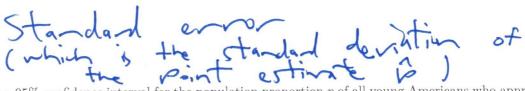
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4 Confidence Intervals

Recall we saw an example of an NPR poll of n = 2089 young Americans' approval of Obama back in 2013. Of these respondents, 856 said they approved of Obama's job performance.

a) What is the numerical value of \widehat{p} , the point estimate of the population proportion p of all young Amercians who approve of Obama's job performance?

b) Say CBS conducted a similar poll with n=2089 and finds that 860 young Americans approve of Obama, leading to one point estimate \widehat{p} of p. Say NBC conducted a similar poll with n=2089 and finds that 844 young Americans approve of Obama, leading to another point estimate \widehat{p} of p. Say Buzzfeed News conducted a similar poll with n=2089 and finds that 871 young Americans approve of Obama, leading to yet another point estimate \widehat{p} of p. What is the name of the value that quantifies this variability?



c) Construct a 95% confidence interval for the population proportion p of all young Americans who approved of Obama's job performance. Note the following mathematical formula approximating the standard error:

SE
$$_{\hat{p}} \approx \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

A 24 Sampling distribution is normal 95% CZ is $PE \pm 1.96 \times SE$

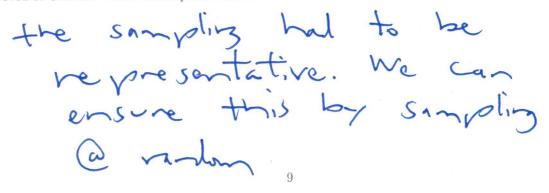
$$= \hat{p} \pm 1.96 \times \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

$$= 0.41 \pm 1.96 \times 0.011$$

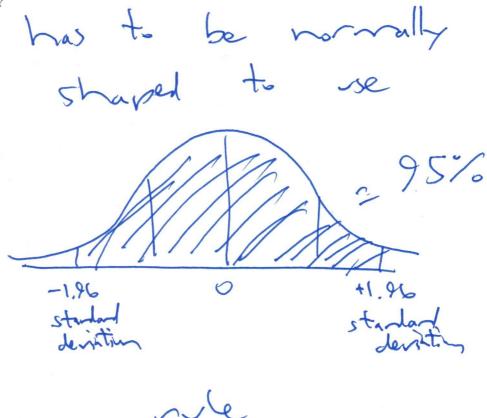
$$= 0.41 \pm 0.02$$

$$= 0.39, 0.43$$

d) Marc-Edouard Vlasic states "I read on NPR that back in 2013, as little as 43% of all young Americans approved of Obama." What assumption must be met for Marc-Edouard's statement to be valid?



e) What assumption about the sampling distribution of \widehat{p} must be met for the confidence interval in part c) to be valid?



5 Inference for Regression

Recall our professor evaluations dataset based on the study from the University of Texas in Austin. In particular, we were interested in explaining a professor's teaching evaluation score using their gender and age as explanatory variables. Here is a random sample of 5 rows out of the n=463 professors in dataset:

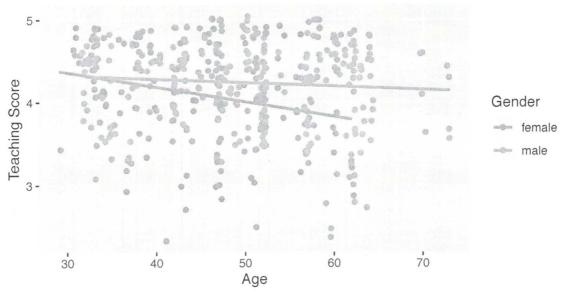
```
## # A tibble: 5 x 3
##
     score gender
                     age
     <dbl> <fct>
##
##
       4.3 female
                       48
##
       4.2 male
                       42
       3.9 male
                       37
## 4
       3.3 female
## 5
       3.6 female
                      38
```

Recall we fit the following regression model with an interaction term:

$$\begin{array}{lcl} \widehat{y} &=& b_0 + b_1 x_1 + b_2 x_2 + b_3 x_1 x_2 \\ \widehat{\text{score}} &=& b_0 + b_{\mbox{age}} \text{age} + b_{\mbox{male}} \blacksquare [\text{is male}] + b_{\mbox{age}, \mbox{male}} \text{age} 1 [\text{is male}] \end{array}$$

Recall the visual representation of the our model. Hint: look at this closely.

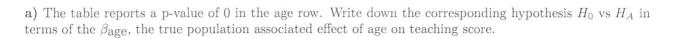
(Jittered) Scatterplot of Teaching Evaluations

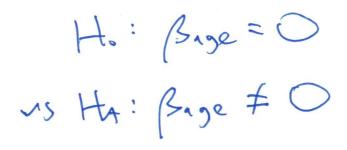


Finally, recall the results of the regression with confidence intervals

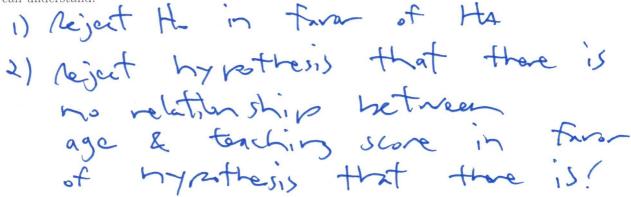
evals_model <- lm(score ~ age * gender, data=evals)
get_regression_table(evals_model)</pre>

term	estimate	std_error	statistic	p_value	lower_ci	upper_ci
intercept	4.88	0.20	23.8	0.00	4.48	5.29
age	-0.02	0.00	-3.9	0.00	-0.03	-0.01
gendermale	-0.45	0.26	-1.7	0.09	-0.97	0.08
age:gendermale	0.01	0.01	2.5	0.02	0.00	0.02



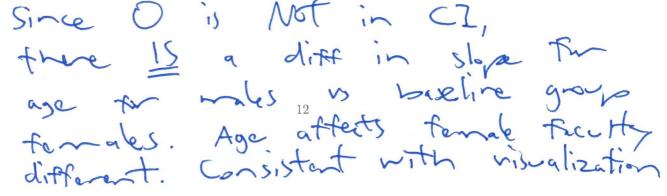


b) The p-value mentioned in part a) is 0. Report what this means for the hypothesis test corresponding to the two hypotheses above. Report this both in 1) statistical terms and 2) language that non-statisticians can understand.

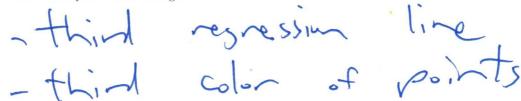


c) Based on these results, among male professors at the University of Austin for every year increase in age, there is an associated X of on average Y units in teaching score. What are X and Y?

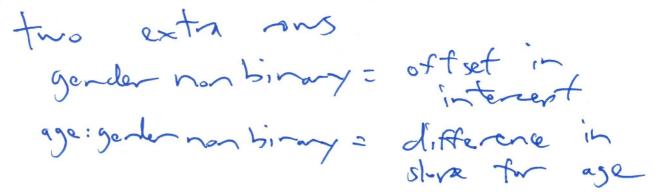
d) What conclusion is suggested by the 95% confidence interval for $\beta_{\text{age:gendergmale}}$ of (0.003, 0.024)?



e) Say we relaxed the gender categorical variable to allow for the following three levels: female, male, and non-binary, and furthermore say some professors selected the new "non-binary" option. Describe precisely how the above plot would change.



f) BONUS 1 Describe precisely how the shape of the above regression table would change.



g) BONUS 2 The 95% confidence interval for $\beta_{\rm gendermale}$ is (-0.968, 0.076). Based on values in the table, write down your best guess of the formula that R uses to compute the left end point of -0.968. Your formula and the reported left endpoint of -0.968 should match up to 2 decimal places.

Regression

You run the code below to analyze departure delays from the 3 New York City airports, but for some weird reason, you only get the incomplete output below. Note AS corresponds to Alaska, F9 corresponds to Frontier, and AA corresponds to American.

library(dplyr)

library(nycflights13)

library(moderndive)

flights_subset <- flights %>%

filter(carrier == "AS" | carrier == "F9" | carrier == "AA")

dep_delay_model <- lm(dep_delay ~ carrier, data = flights_subset)</pre> get_regression_table(dep_delay_model, digits = 3)

term	estimate	std_error	statistic	p_value	lower_ci	upper_ci
intercept	8.6	0.21	40.7	0.000	8.2	8.999
carrierAS	-2.8	1.43	-1.9	0.052	-5.6	0.025
carrierF9	11.6	1.46	8.0	0.000	8.8	NA

a) Interpret the 11.6 estimate value in the carrierF9 row (third row, second column). Is its relationship of with the outcome variable meaningful?

Diff in departure delay Pur

Since 95% CZ is [8.8,

does not contain yes, it is meaningf

b) Compute the missing right endpoint of the 95% confidence interval in the carrierF9 row.

PE 1 1.96 * SE = 11.6 ±1,26 × 1.46 = 11.6 ± 2.86 2 [8.74, 14.46]

c) State the scientific conclusion reached based on the now complete 95% confidence interval.

15

e) Write down the hypothesis test corresponding to the carrierAS row using mathematical notation. Do not carry out the hypothesis test, simply state the two competing hypotheses.

Ho: BarrierAs = 0

f) Say you were given an α cutoff value of 0.01 for the hypothesis test above. Write down the conclusion of this hypothesis test both in statistical terms and using non-statistical language that an airline executive can understand.

Since prvalue 0.052 > d = 0.01me do not reject Ho.

i.e. we do not have evidence to

Segest the avg difference in

delays for AS vs AA is not 0.

c) In the second row, fifth column there is a p-value missing. What is the hypothesis test corresponding to this missing p-value?

d) Sketch on the follow plot of the corresponding *null* distribution what the missing p-value in the second row, fifth column is:

ignore.

